

# Isotopic Dependence of the Caloric Curve

W. Trautmann, GSI Darmstadt





# Isotopic **I**ndependence of the Caloric Curve

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introduction

- I. motivation: limiting temperatures
- II. ALADIN experiment S254
- III. results and consequences
- IV. isoscaling and the symmetry energy outlook

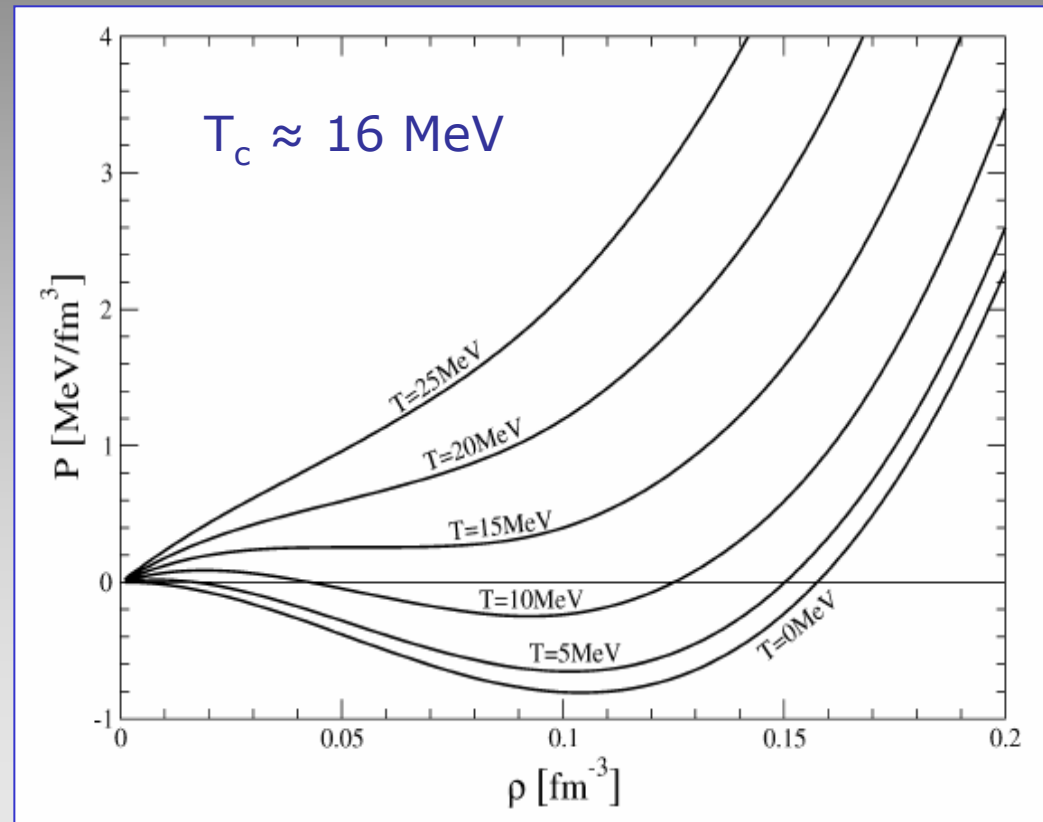
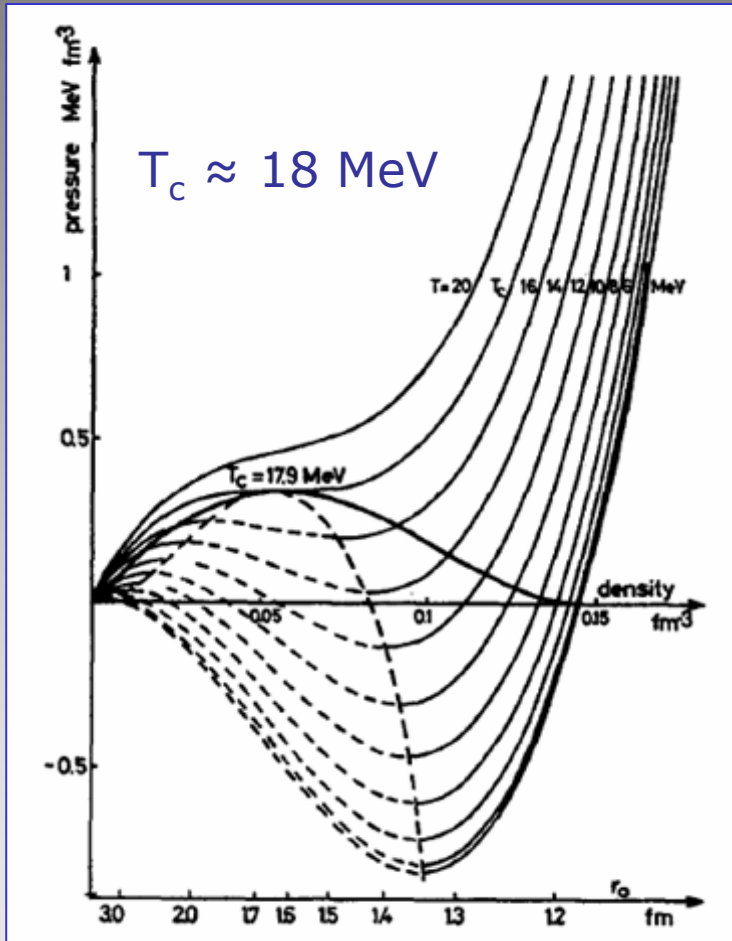
S. Bianchin, A.S. Botvina, M. de Napoli, A. Le Fèvre, J. Łukasik, A. Mykulyak, C. Sfienti, and the ALADiN2000 collaboration

# the nuclear phase diagram

temperature dependent  
Hartree-Fock theory

1976 - today

chiral effective  
field theory

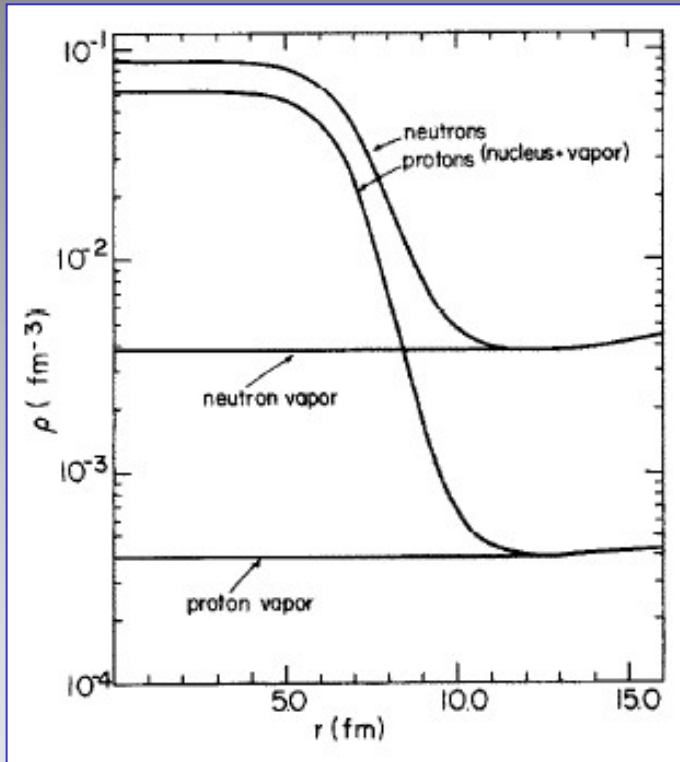


from Sauer, Chandra, Mosel  
Nucl. Phys. A 264, 221 (1976)

from Fritsch, Kaiser, Weise  
Nucl. Phys. A 750, 259 (2005)

# I. motivation: limiting temperatures

Bonche, Levit, Vautherin,  
NPA 436, 265 (1985)



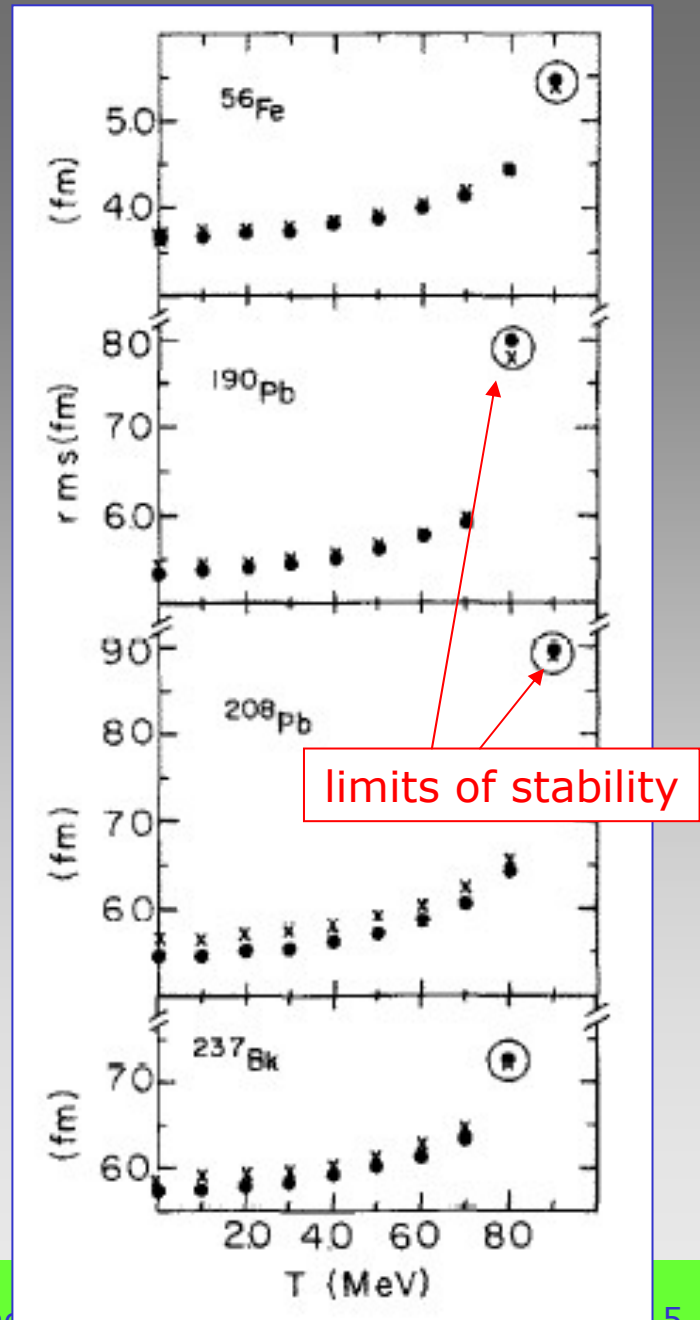
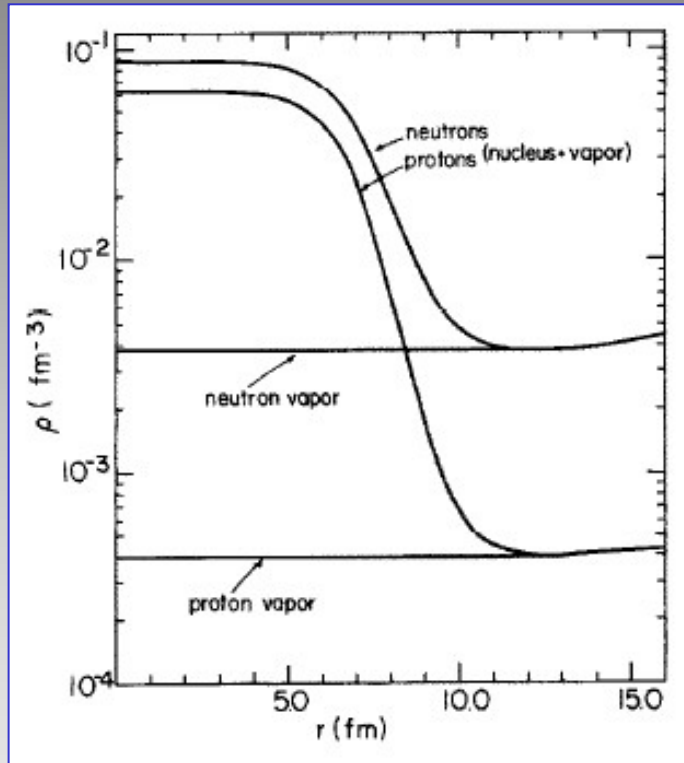
question:  
what is the limiting temperature  
up to which a compound nucleus  
can be excited

answered with  
temperature-dependent Hartree-Fock  
calculations

the nucleus in equilibrium with its  
surrounding vapor

# limiting temperatures

Bonche, Levit, Vautherin,  
NPA 436, 265 (1985)



# limiting temperatures

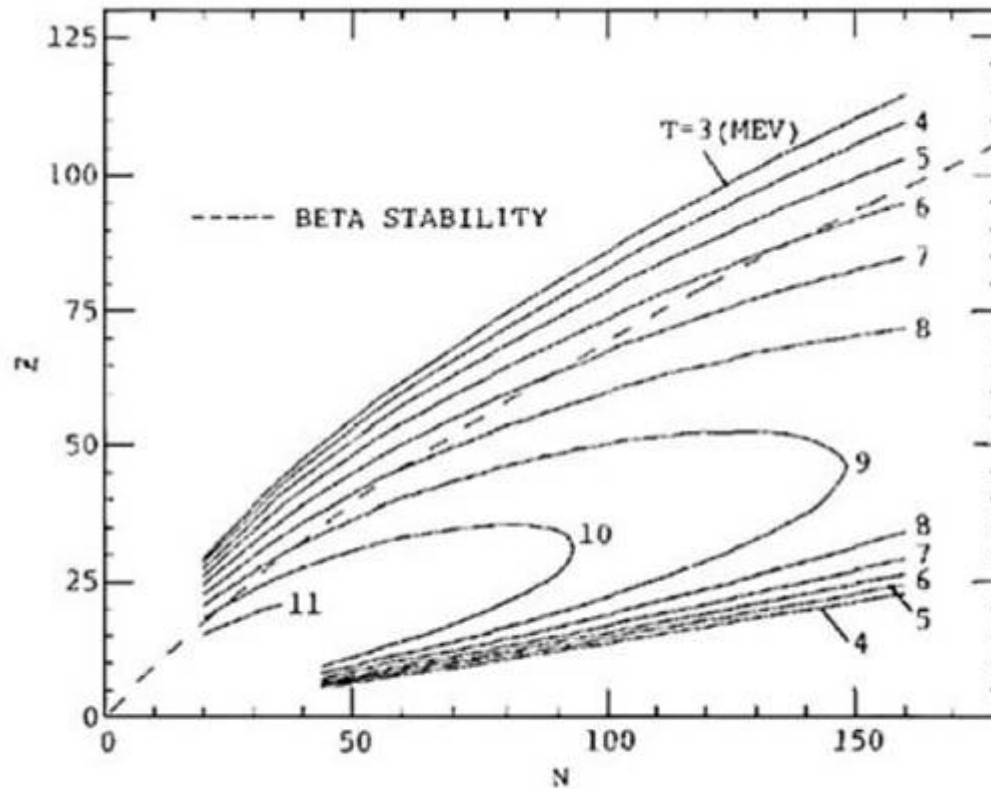


Fig. 1. Limiting temperatures predicted by Besprosvany and Levit [86]. Phys. Lett. B 217, 1 (1989)

liquid-drop model  
formulated to represent  
the physics of the  
finite-temperature  
Hartree-Fock calculations

the interest:

the limiting temperature  
is sensitive to the  
equation of state  
and to the  
temperature dependence  
of the surface tension



# limiting temperature

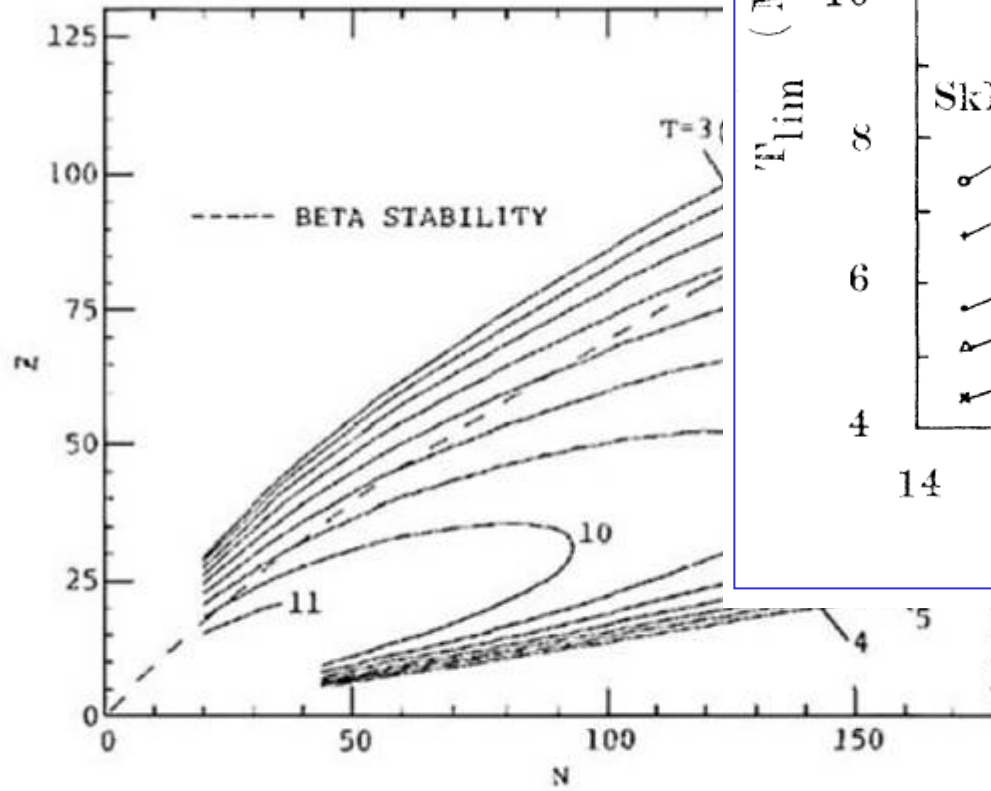
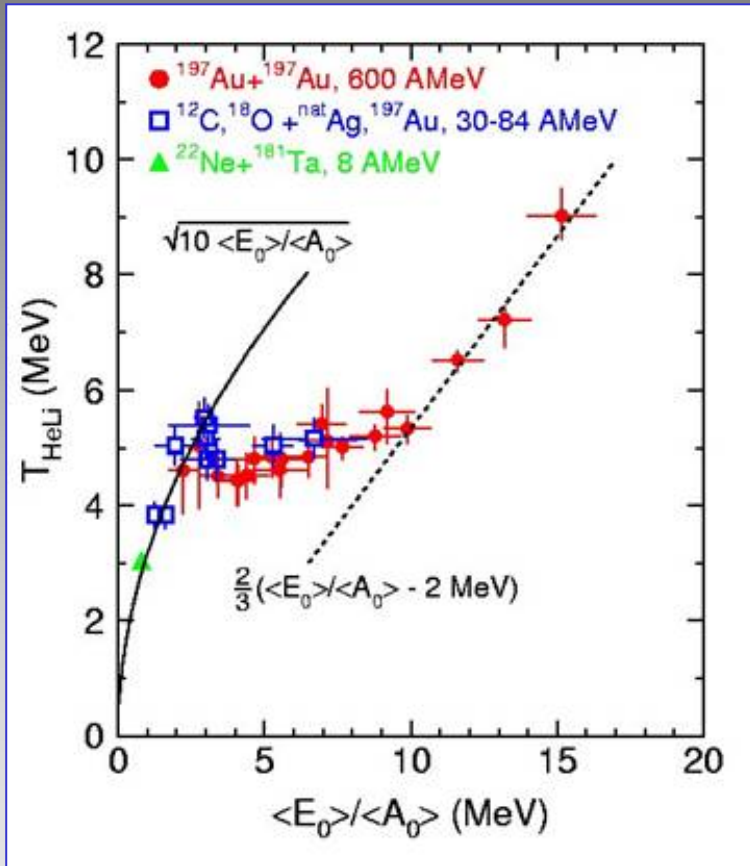


Fig. 1. Limiting temperatures predicted by Besprosvany and Levit [86]. Phys. Lett. B 217, 1 (1989)

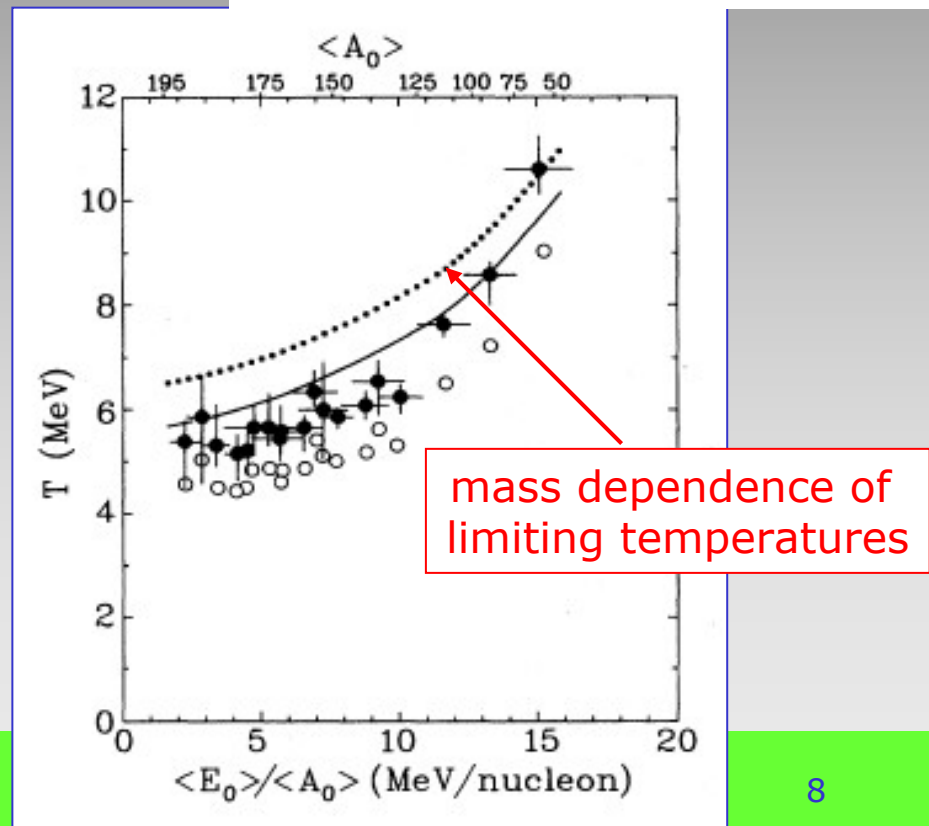
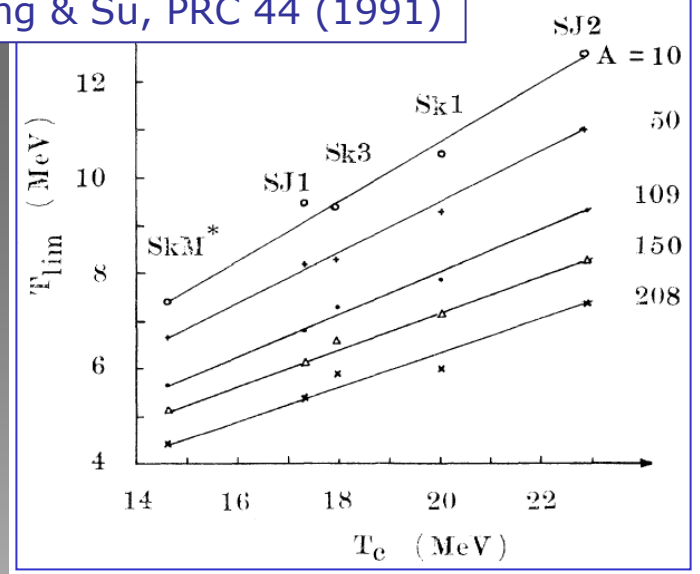
the limiting temperature is sensitive to the equation of state and to the temperature dependence of the surface tension

# the nuclear caloric curve

J. Pochodzalla et al.,  
Phys. Rev. Lett. 75 (1995)

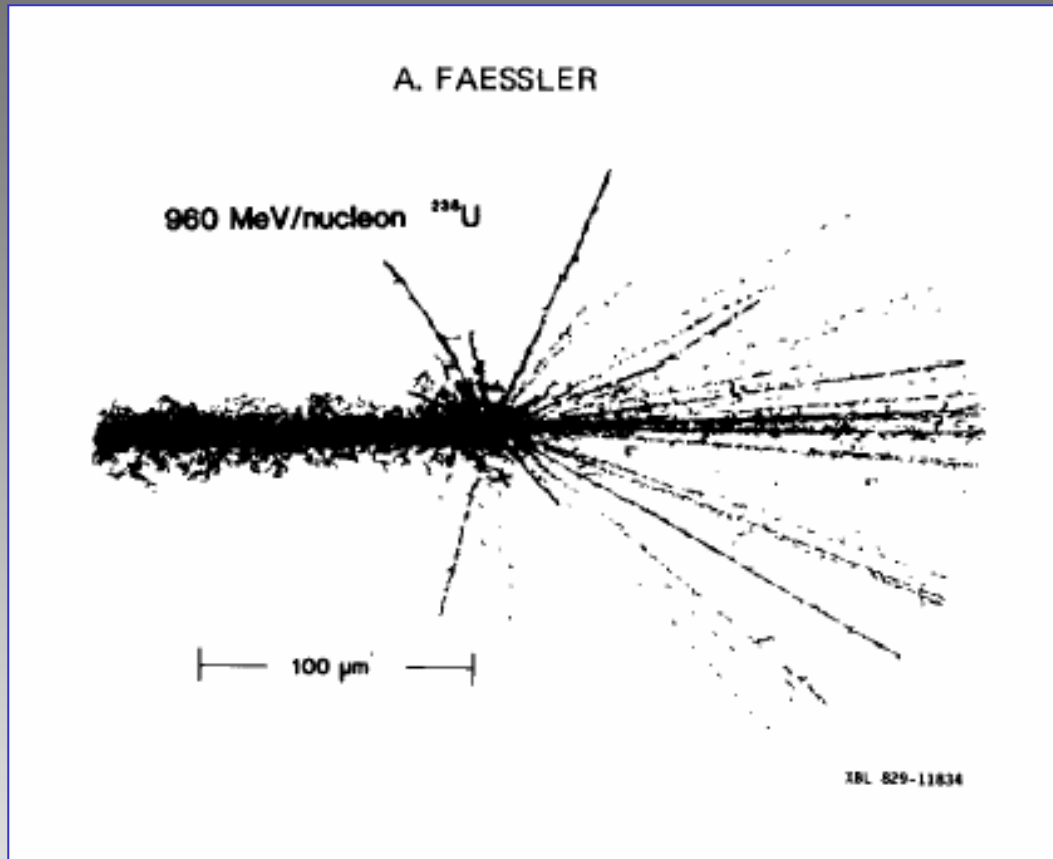


J.B. Natowitz et al.,  
Phys. Rev. C 52 (1995)





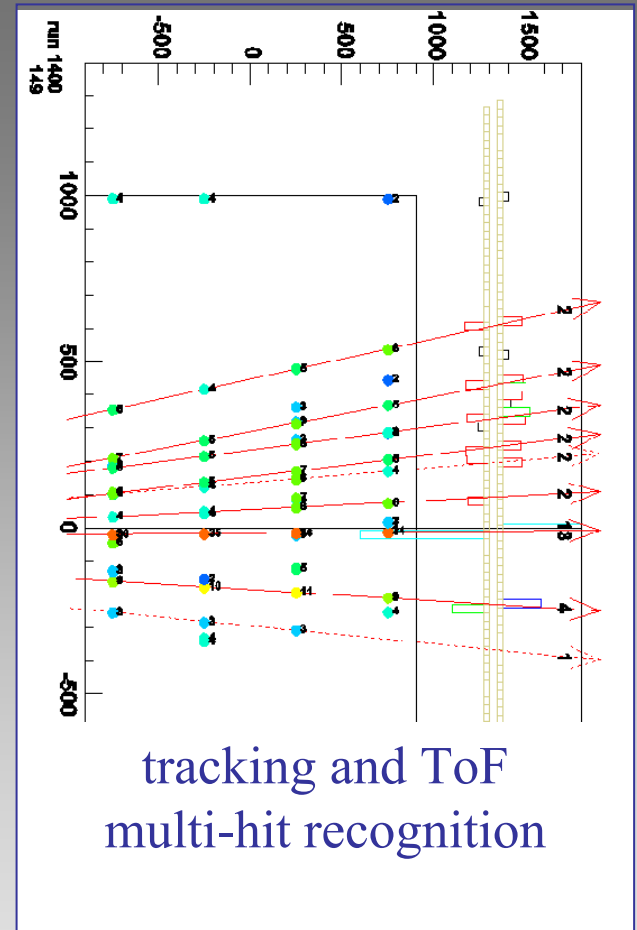
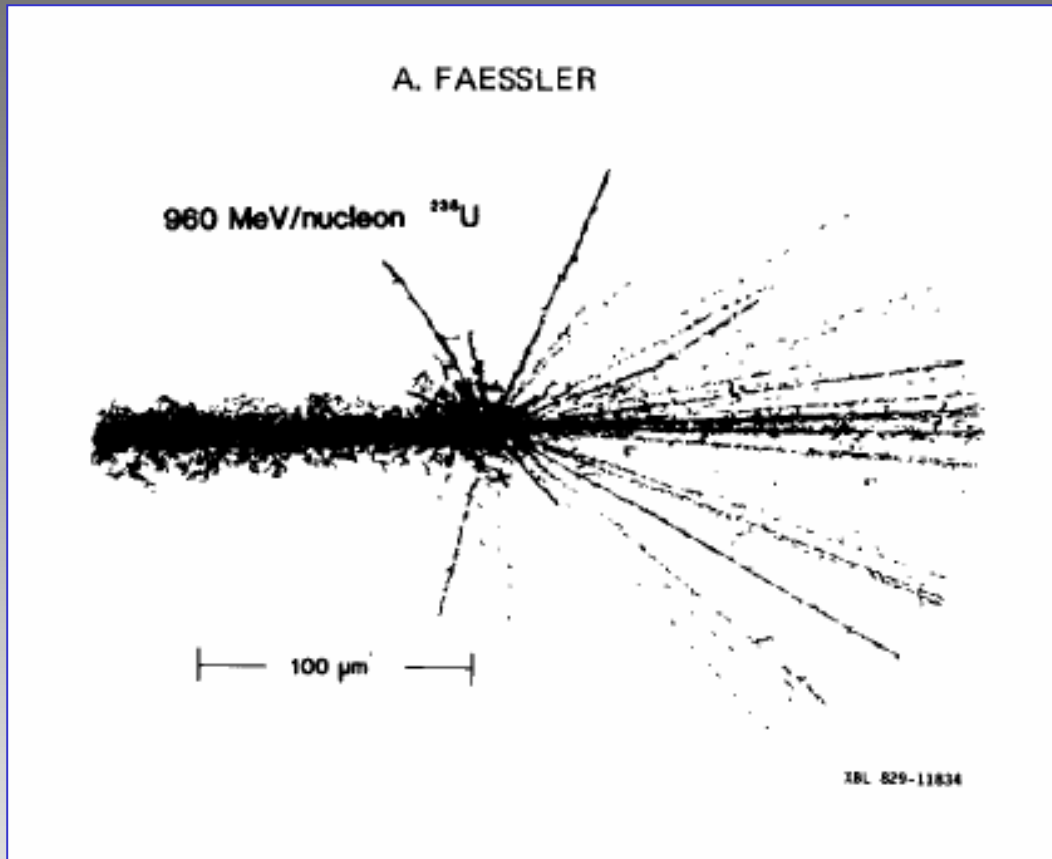
## II. experiment: projectile fragmentation



"... the future has already started  
and we have to go back to work not to miss it."

taken from summary talk by A. Faessler at Int. Conf. on Nucleus-Nucleus Collisions,  
MSU, East Lansing, Michigan, Sept/Oct 1982  
Nucl. Phys. A 400 (1983) 565; H.H. Heckman et al., Phys. Rev. C 27 (1983)

# projectile fragmentation with ALADIN

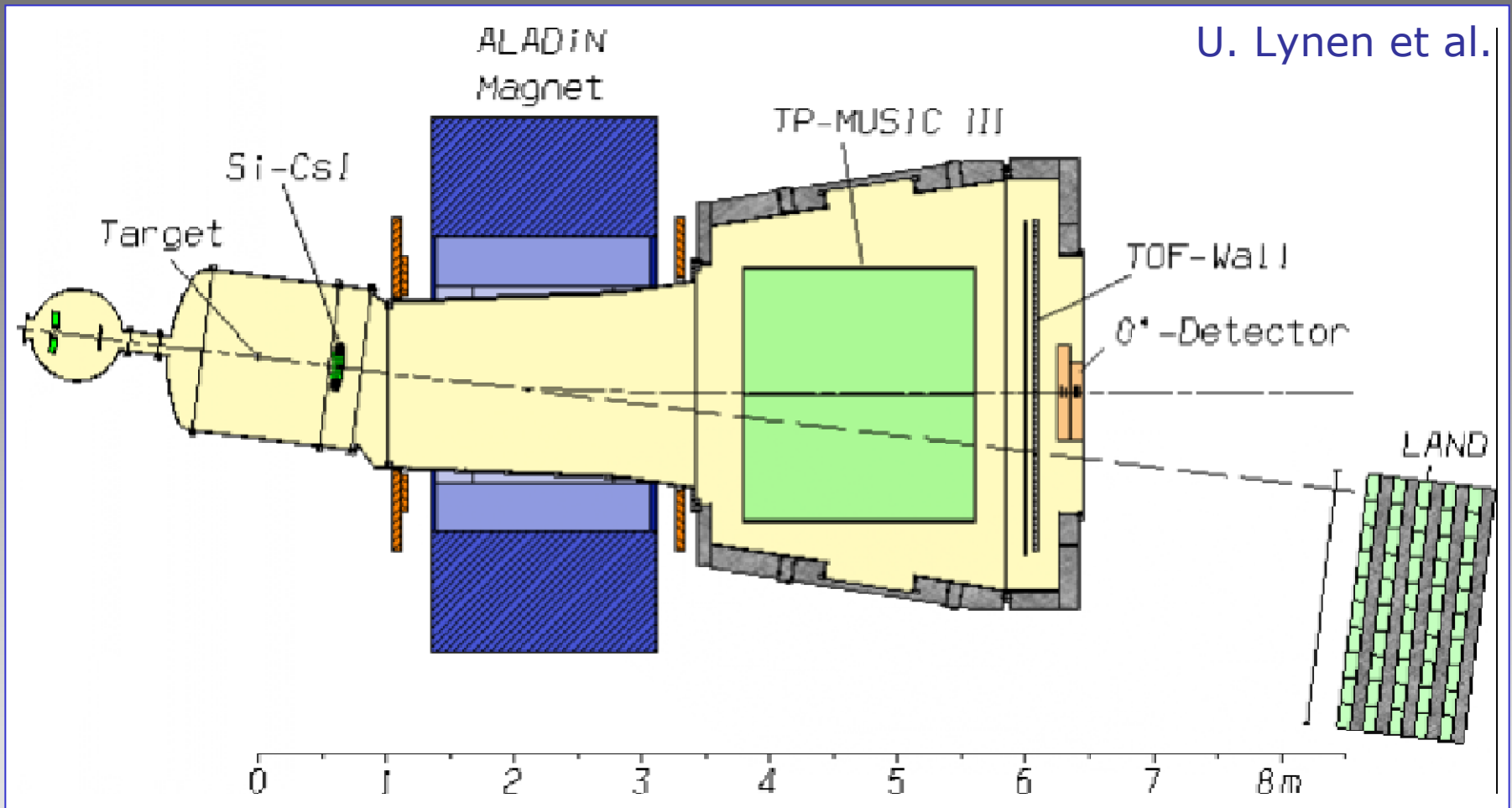


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MSU, East Lansing, Michigan, Sept/Oct 1982  
Nucl. Phys. A 400 (1983) 565; H.H. Heckman et al., Phys. Rev. C 27 (1983)

# the ALADiN spectrometer

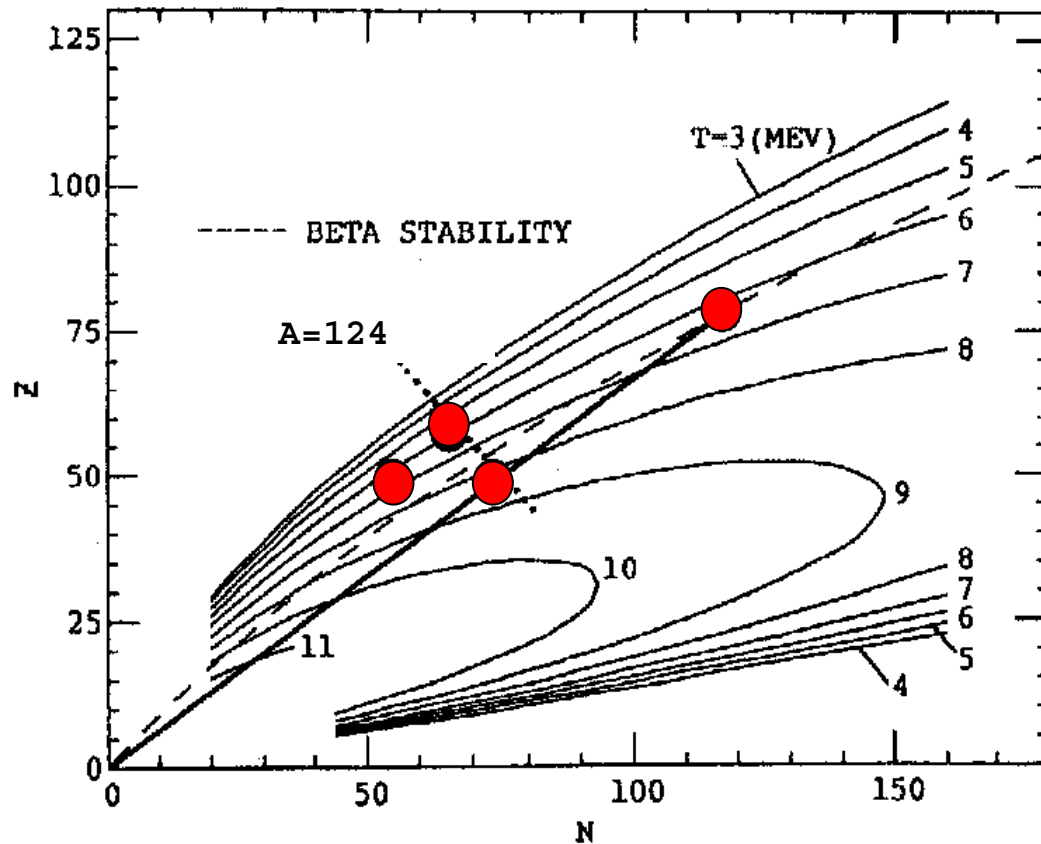
U. Lynen et al.



*A, Z resolution, large acceptance and dynamic range, no threshold, neutrons*

# ALADIN experiment S254

## "Mass and isospin effects in multifragmentation"



$^{107}\text{Sn}$ ,  $^{124}\text{La}$   
 $^{124}\text{Sn}$ ,  $^{197}\text{Au}$

600 A MeV

our lines represent  
ng temperatures

erature dependent  
ee-Fock calculations  
Skyrme forces



# radioactive beam production

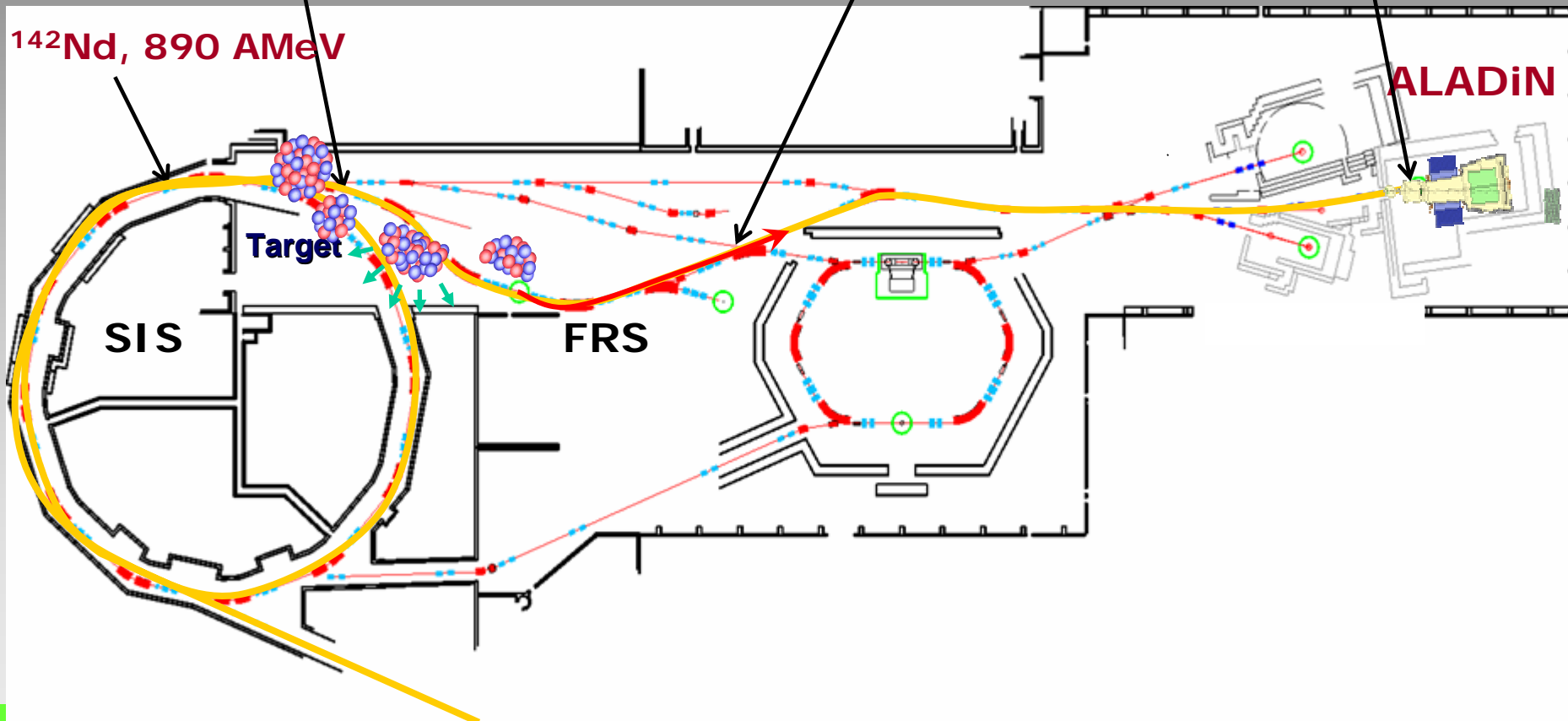
production target

${}^9\text{Be}$ , 4009 mg/cm<sup>2</sup>

${}^{124}\text{La}({}^{107}\text{Sn})$  600 A MeV

reaction target

${}^{142}\text{Nd}$ , 890 A MeV



# radioactive beam production

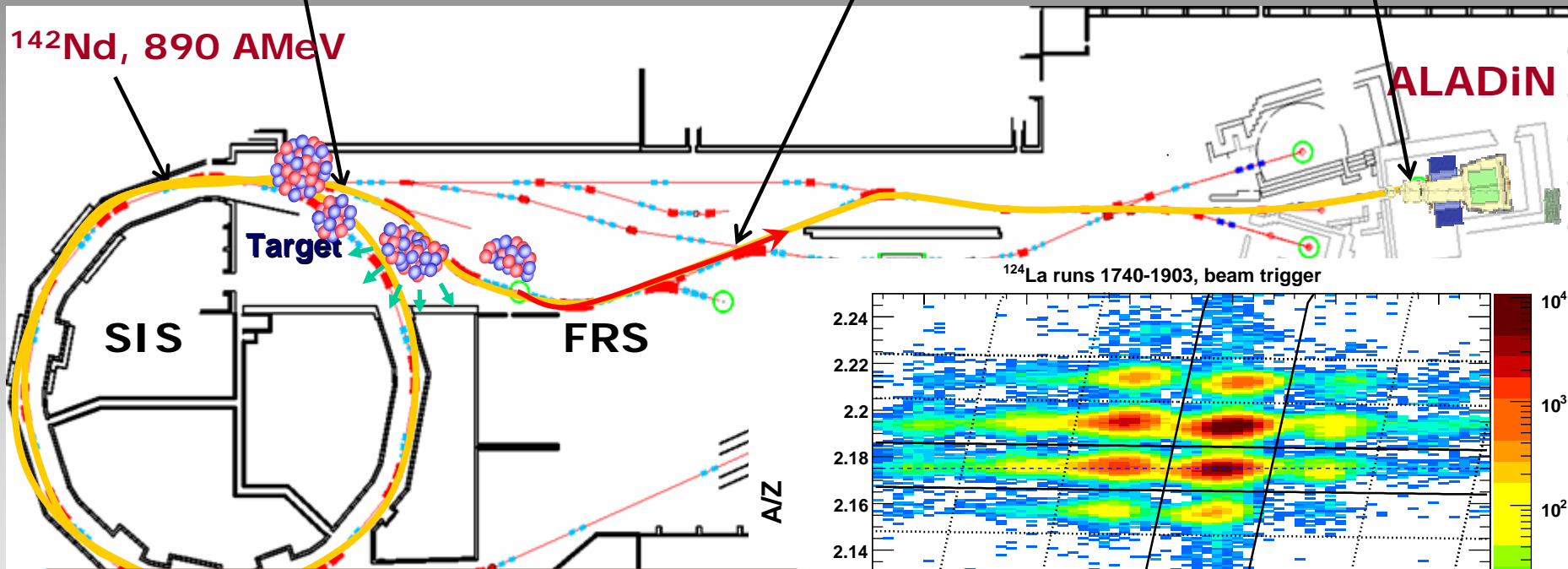
$^{124}\text{La} (^{107}\text{Sn})$  600 A MeV

production target

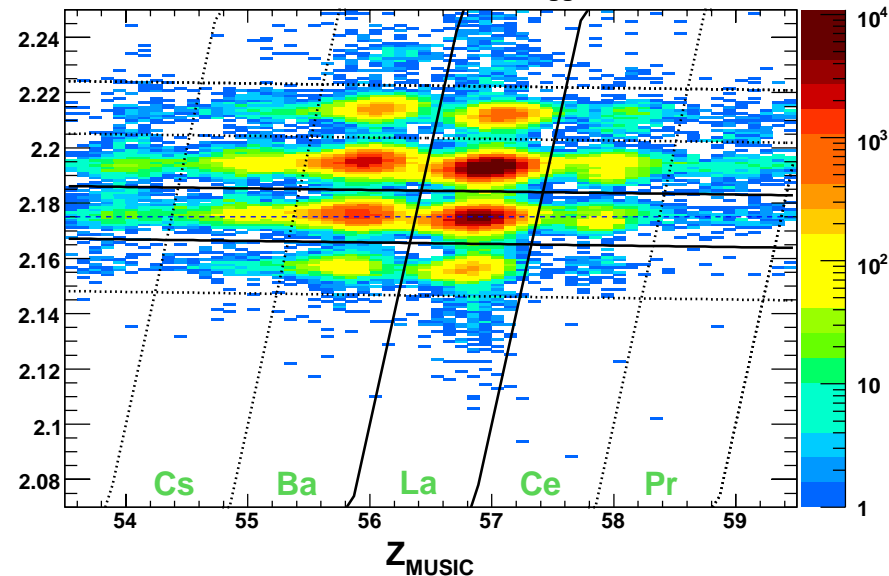
$^9\text{Be}$ , 4009 mg/cm<sup>2</sup>

reaction target

$^{142}\text{Nd}$ , 890 A MeV



use discriminant analysis  
to select pure isotopic beams  
(J. Łukasik et al., NIM 587 (2008) 413)



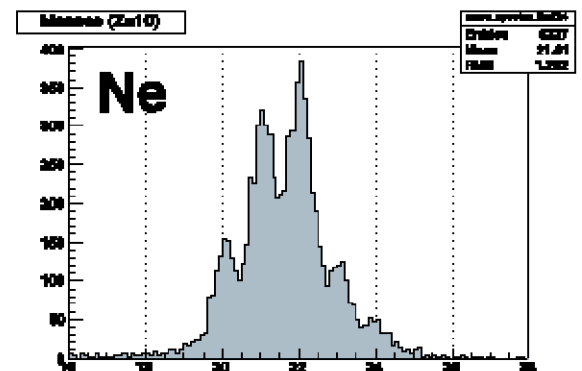
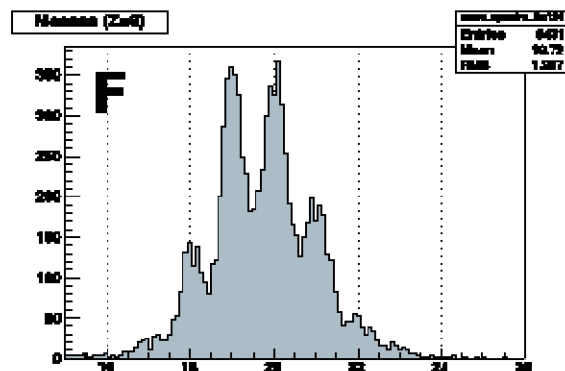
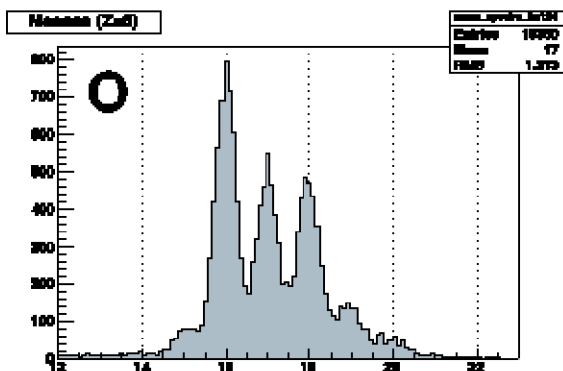
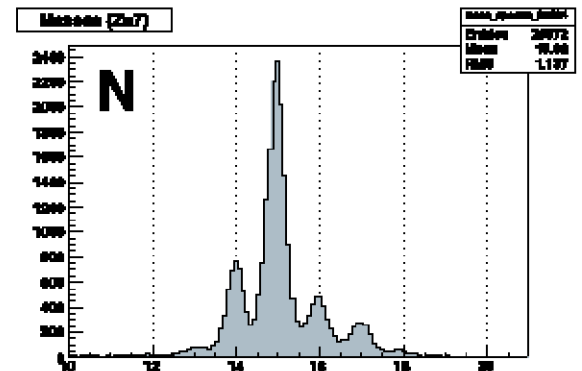
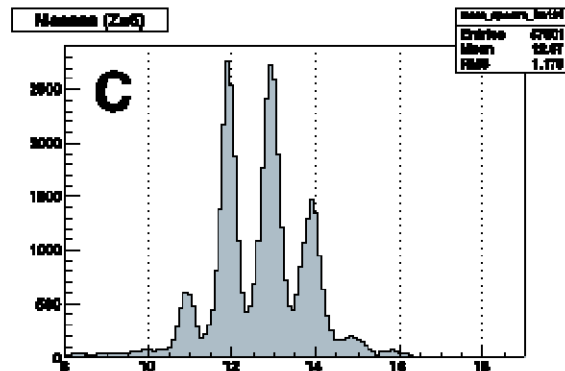
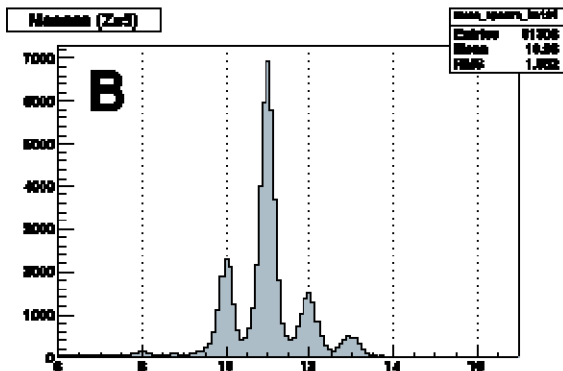
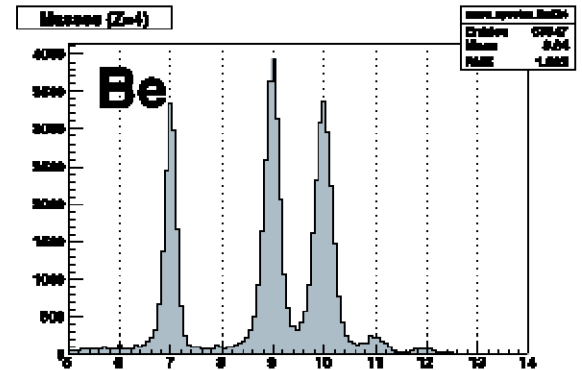
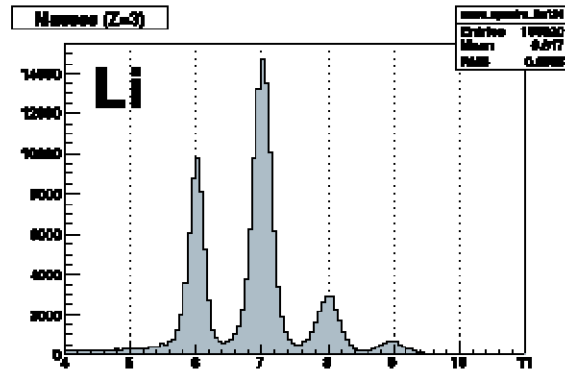
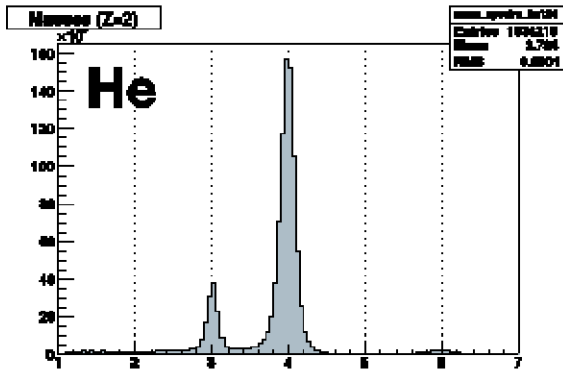
# The Aladdin 2000 Collaboration



S. Bianchin, K. Kezzar, A. Le Fèvre, J. Lühning, J. Lukasik, U. Lynen, W.F.J. Müller, H. Orth, A.N. Otte, H. Sann, C.Schwarz, C. Sfienti, W. Trautmann, J. Wiechula, M.Hellström, D. Henzlova, K. Sümmerer, H. Weick, P. Adrich, T. Aumann, H. Emling, H. Johansson, Y. Leifels, R. Palit, H. Simon, M. De Napoli, G. Imme', G. Raciti, E. Rapisarda, R. Bassini, C. Boiano, I. Iori, A. Pullia, W.G. Lynch, M. Mocko, M.B. Tsang, G. Verde, M. Wallace, C.O. Bacri, A. Lafriakh, A. Boudard, J-E. Ducret, E. LeGentil, C. Volant, T. Barczyk, J. Brzychczyk, Z. Majka, A. Wieloch, J. Cibor, B. Czech, P. Pawlowski, A. Mykulyak, B. Zwieglinski, A. Chbihi, J. Frankland and A.S. Botvina

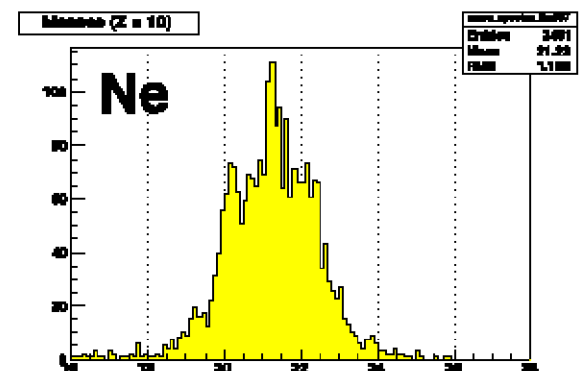
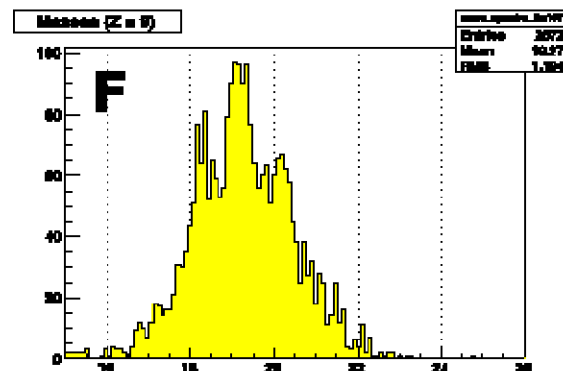
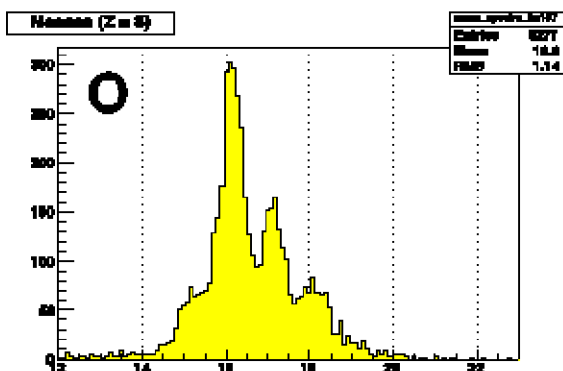
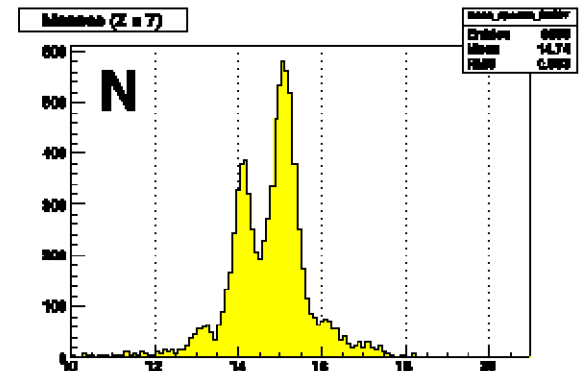
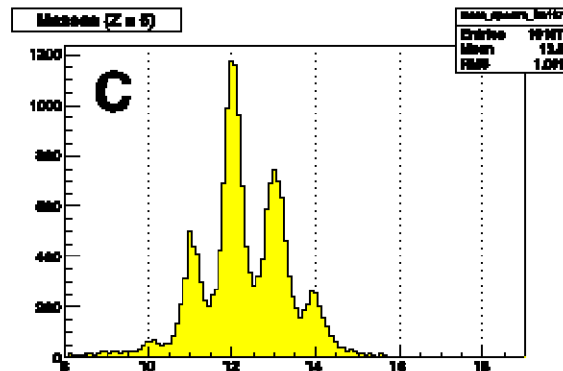
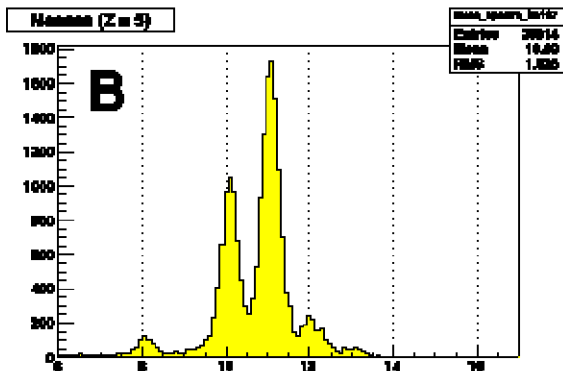
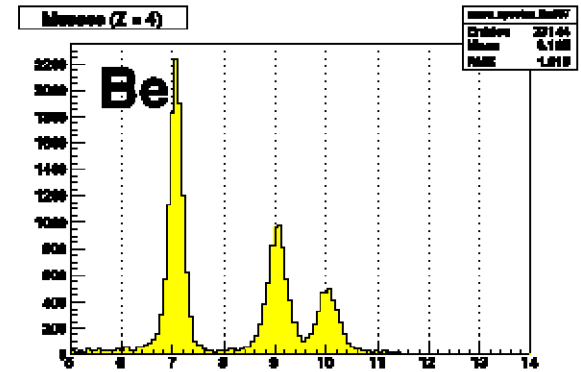
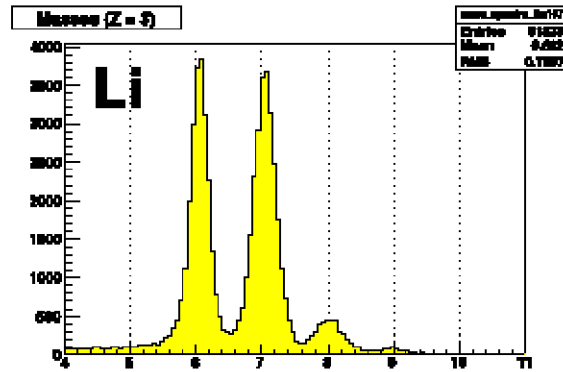
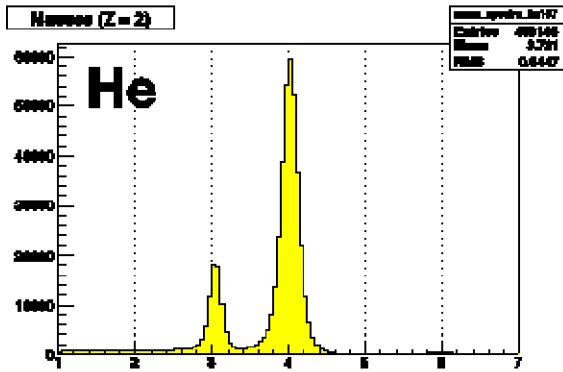


# final mass spectra: $^{124}\text{Sn}$

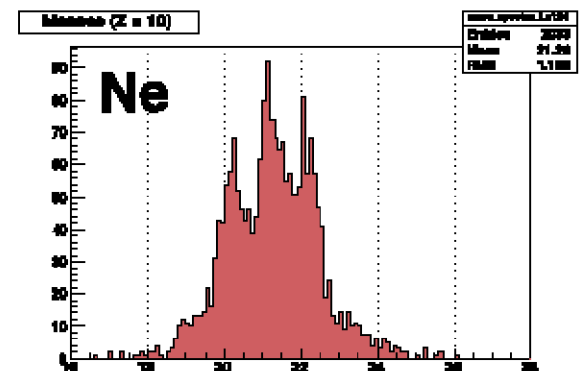
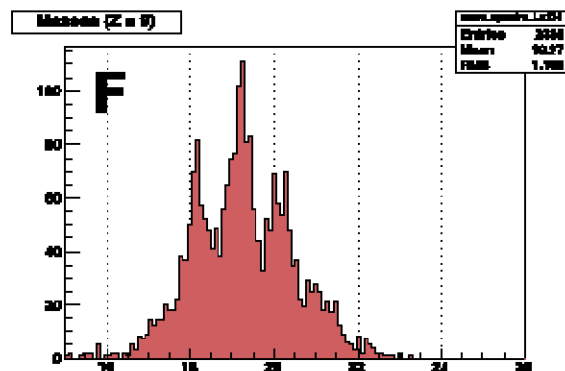
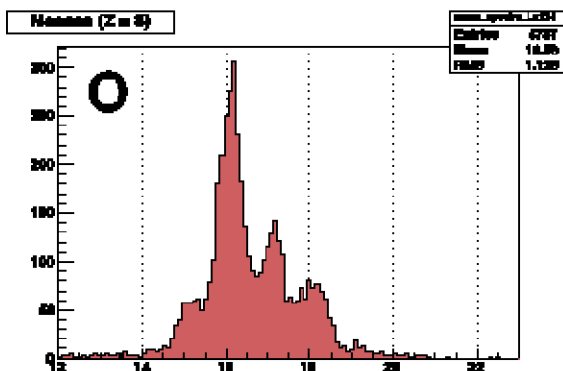
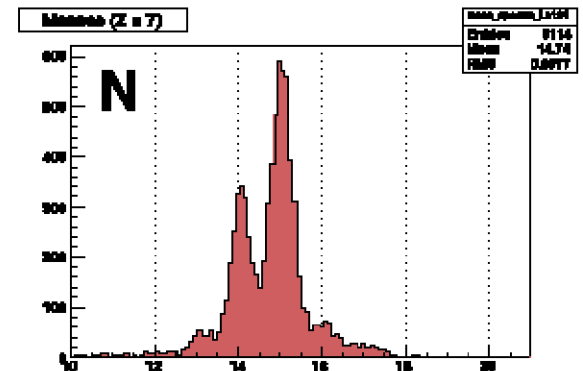
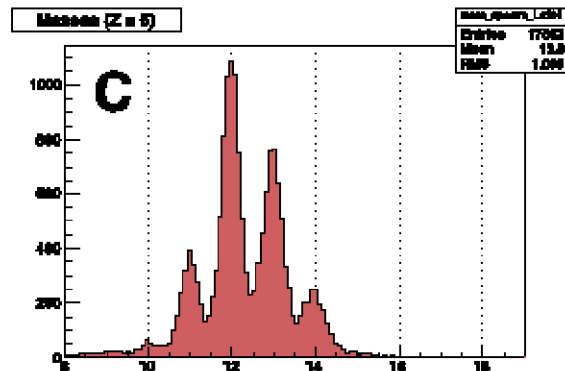
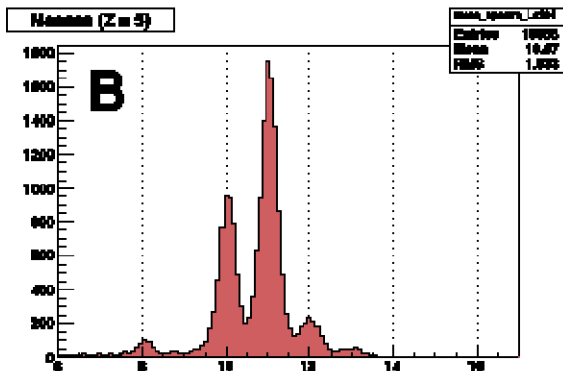
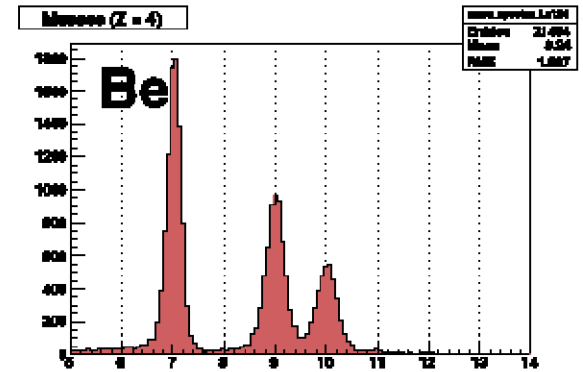
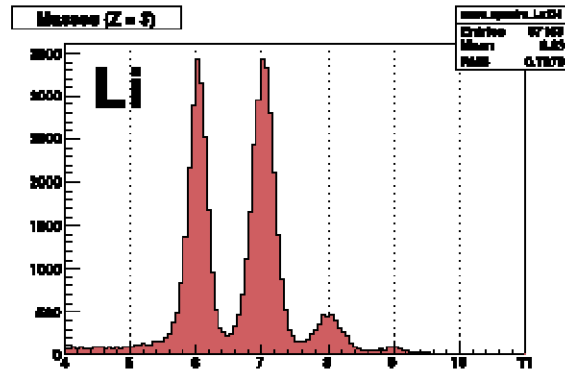
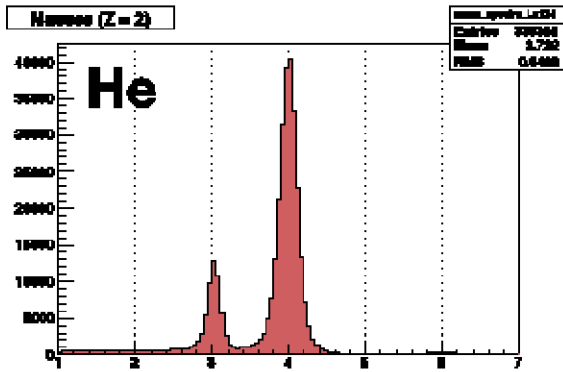




# final mass spectra: $^{107}\text{Sn}$

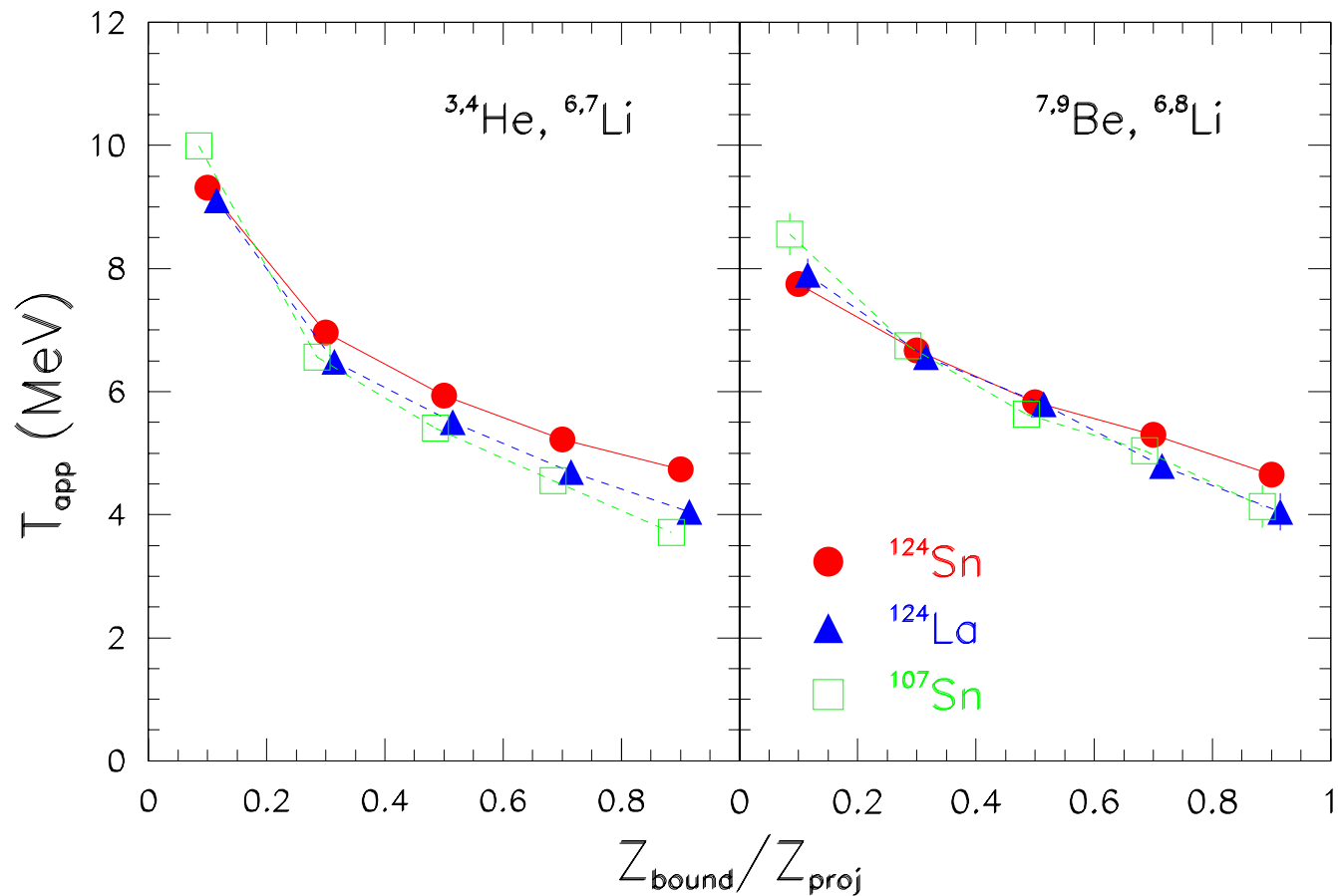


# final mass spectra: $^{124}\text{La}$



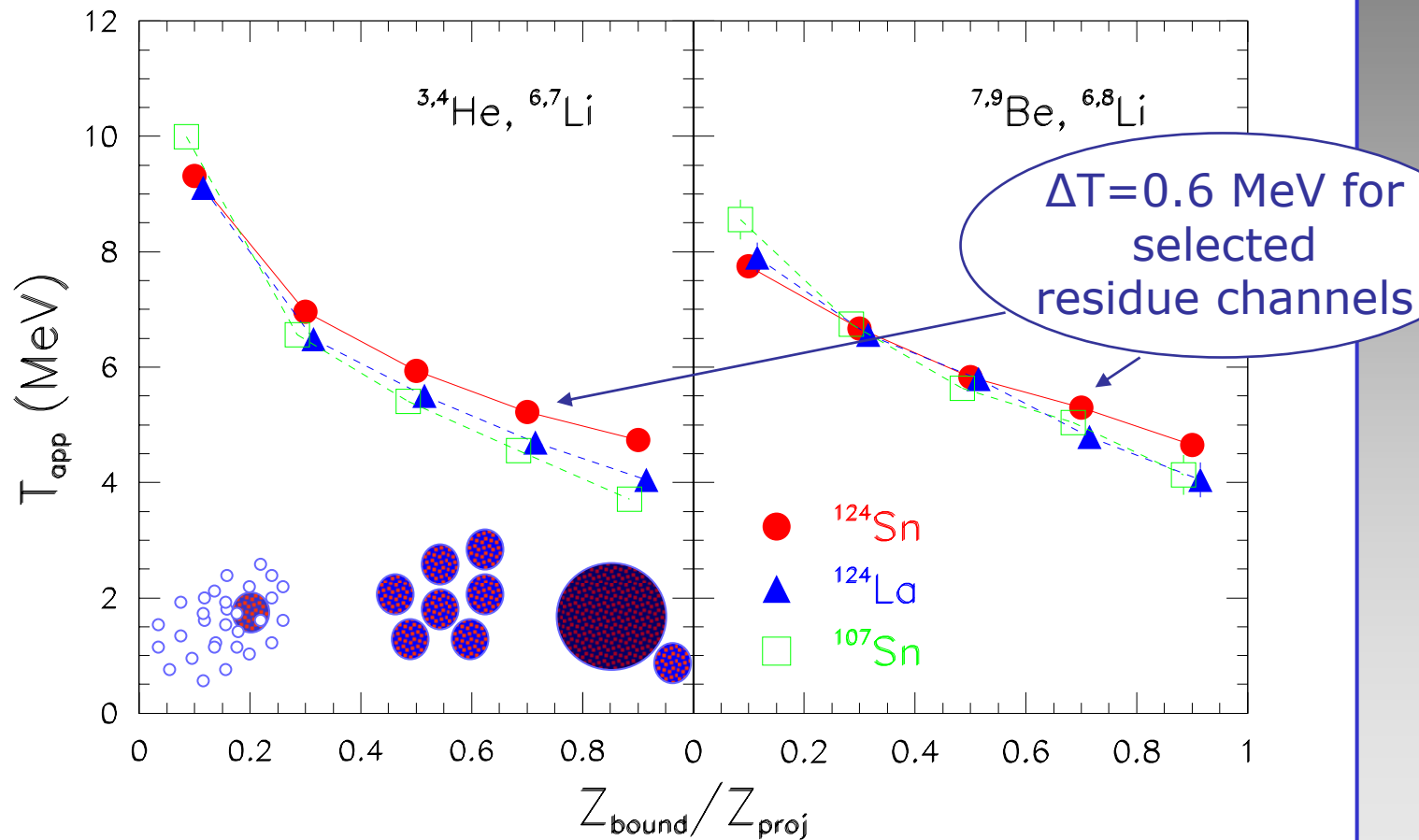
# chemical freeze-out temperatures

from double isotope yield ratios:  $T_{\text{HeLi}}$  ( $^{3,4}\text{He}, ^{6,7}\text{Li}$ )  
(Albergo's formula)  $T_{\text{BeLi}}$  ( $^{7,9}\text{Be}, ^{6,8}\text{Li}$ )



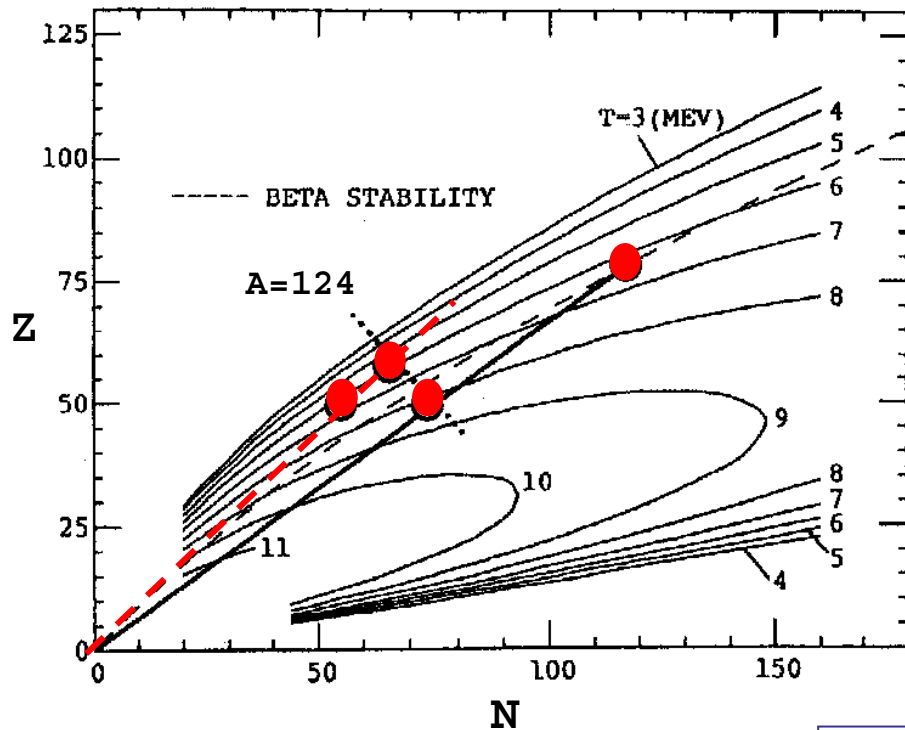
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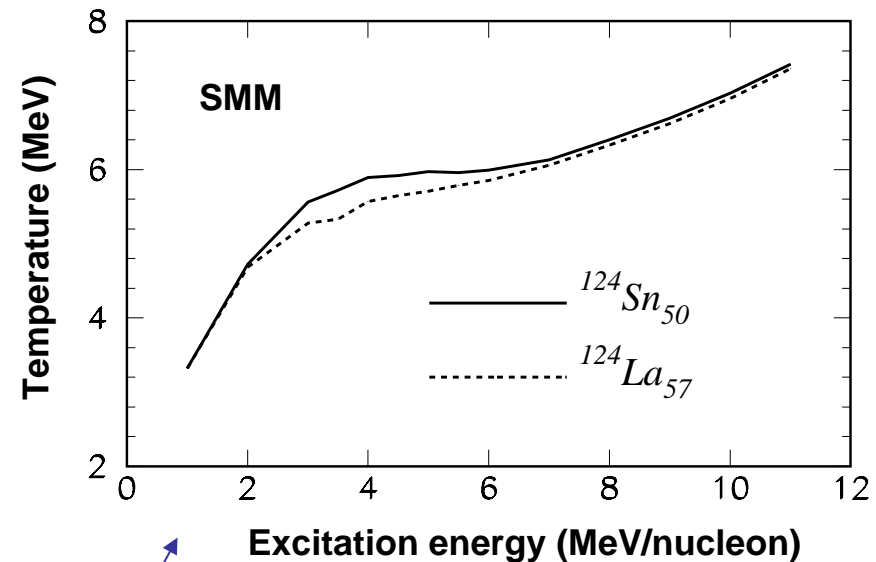




# N/Z independence of the nuclear caloric curve



Statistical Multifragmentation Model  
Ogul and Botvina, PRC 66 (2002)

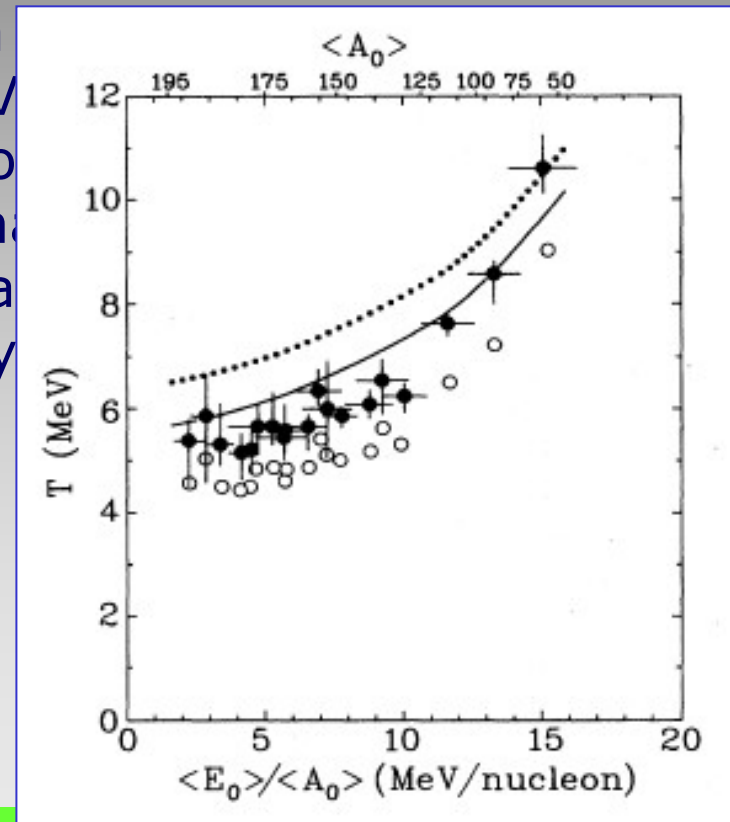


*good agreement with the SMM predictions*

*the predicted isospin dependence is not observed*

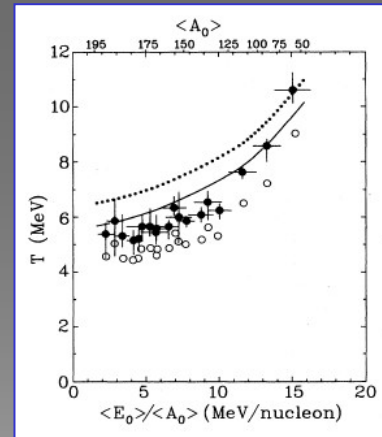
### III. consequences

1. the  $Z_{\text{bound}}$  dependence is not primarily a mass effect
2. Coulomb effect  $\Delta T=0.6$  MeV in
  - 2a. limiting temperature of 6 MeV
  - 2b. the limiting temperature is not determined by asymptotic phase
3. multifragmentation: phase-space instead of Coulomb instability

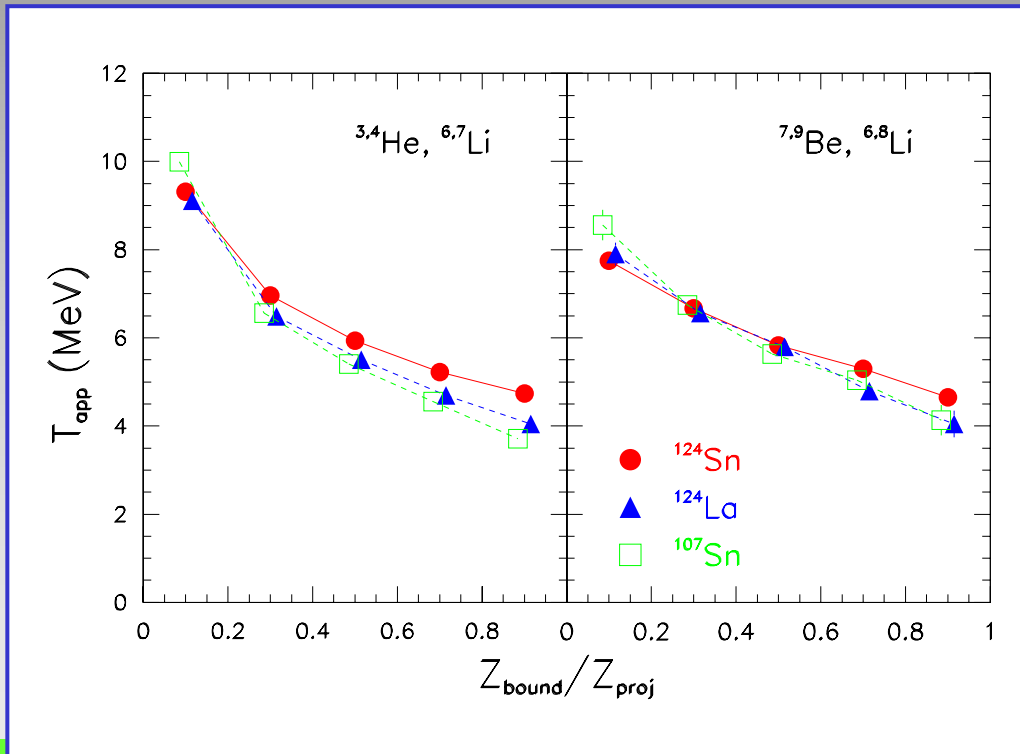


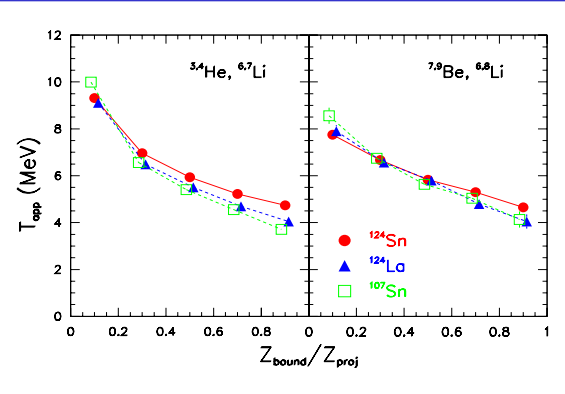
### III. consequences

1. the  $Z_{\text{bound}}$  dependence is not primarily a mass effect
2. Coulomb effect  $\Delta T = 0.6$  MeV in residue production

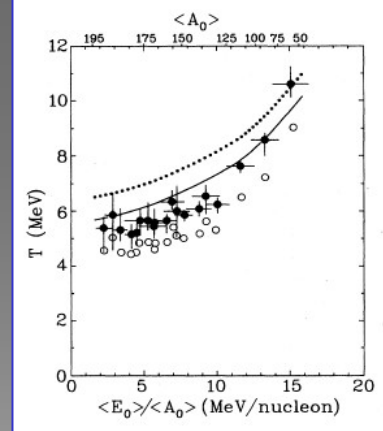


$V \rightarrow T_c = 15$  MeV  
 not tested  $\rightarrow$   
 phase space  
 space driven instability  
 by

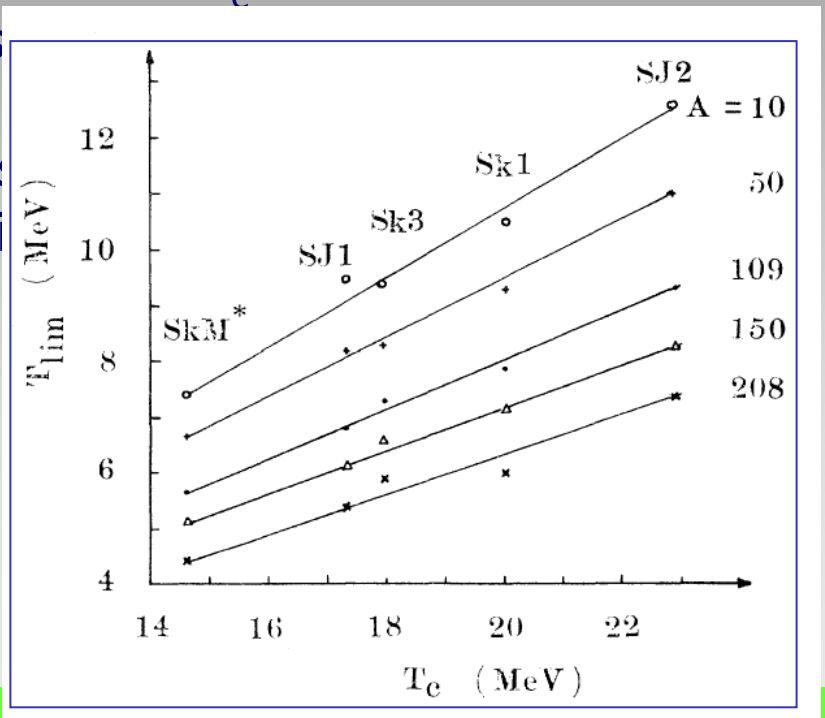




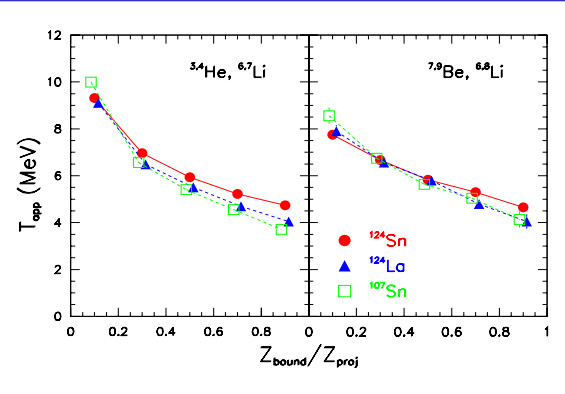
### III. consequences



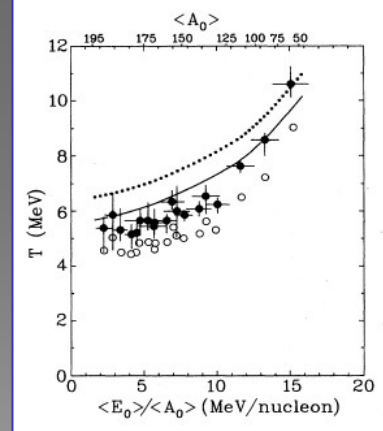
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2. Coulomb effect  $\Delta T = 0.6$  MeV in residue production
  - 2a. limiting temperature of 6 MeV  $\rightarrow T_c = 15$  MeV
  - 2b. the limiting temperature is determined by asymptotic
3. multifragmentation: phase- instead of Coulomb instability



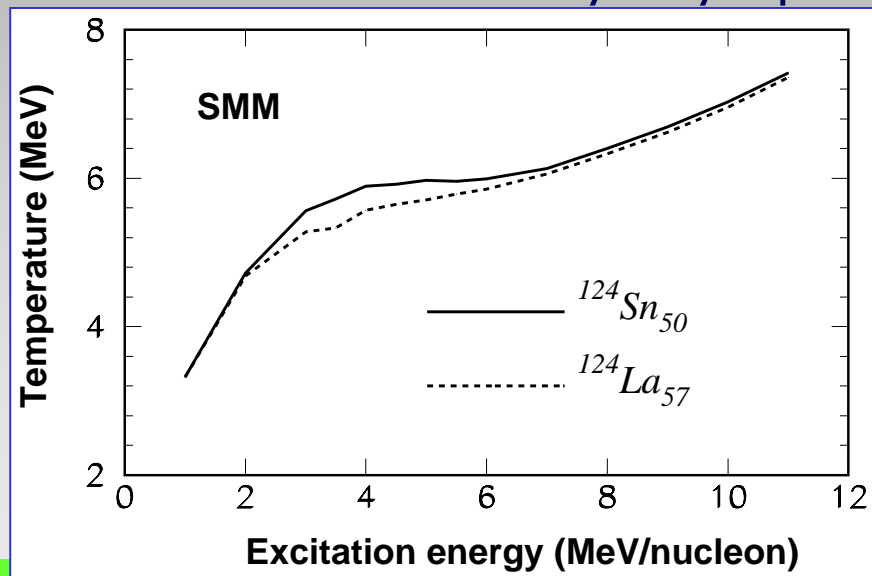




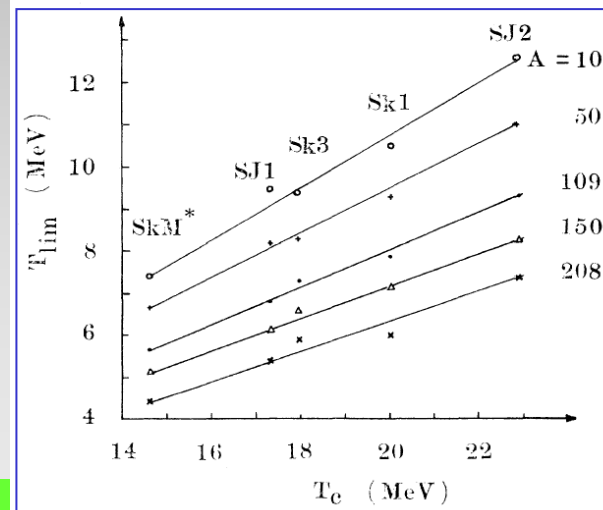
### III. consequences

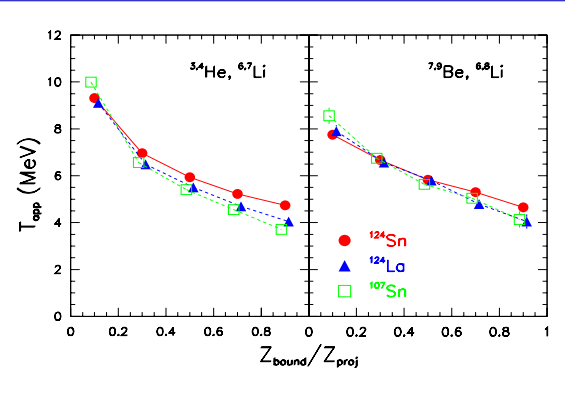


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2. Coulomb effect  $\Delta T = 0.6$  MeV in residue production
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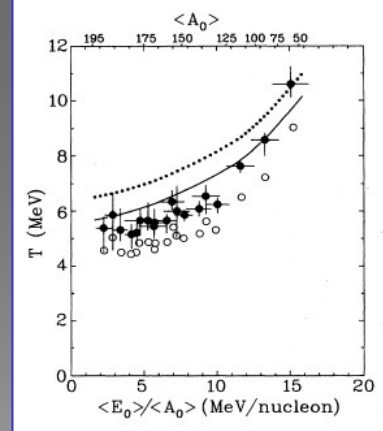


Phase-space driven instability  
 stability

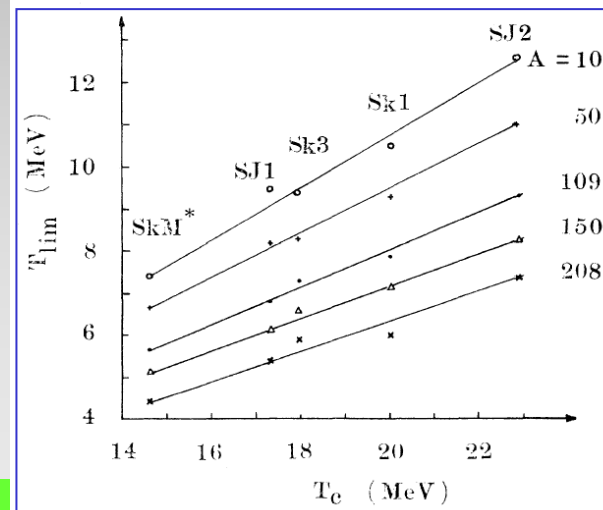
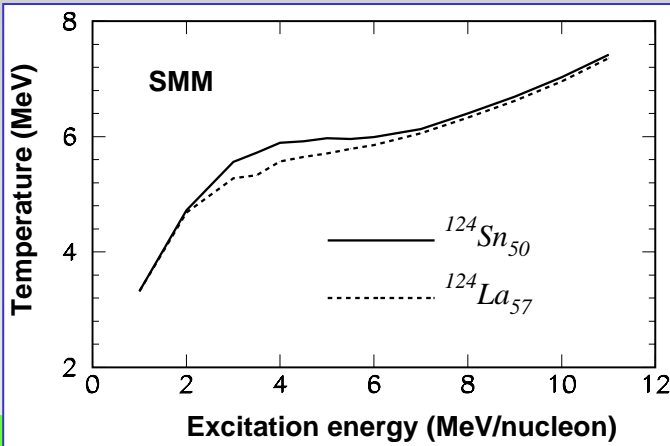


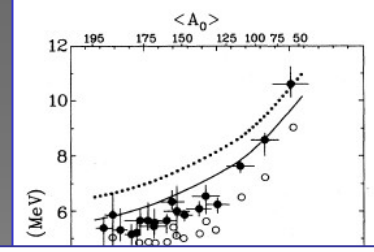
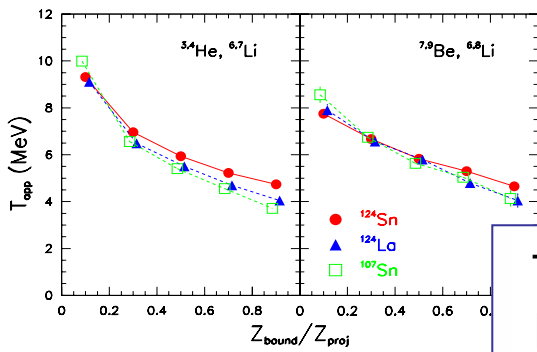


### III. consequences



1. the  $Z_{\text{bound}}$  dependence is not primarily a mass effect
2. Coulomb effect  $\Delta T = 0.6$  MeV in residue production
  - 2a. limiting temperature of 6 MeV  $\rightarrow T_c = 15$  MeV
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3. multifragmentation: phase-space driven instability instead of Coulomb instability



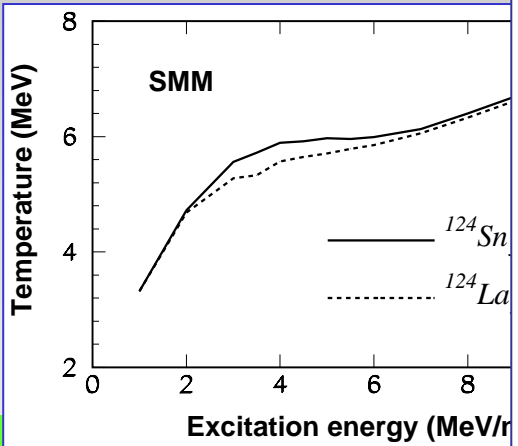
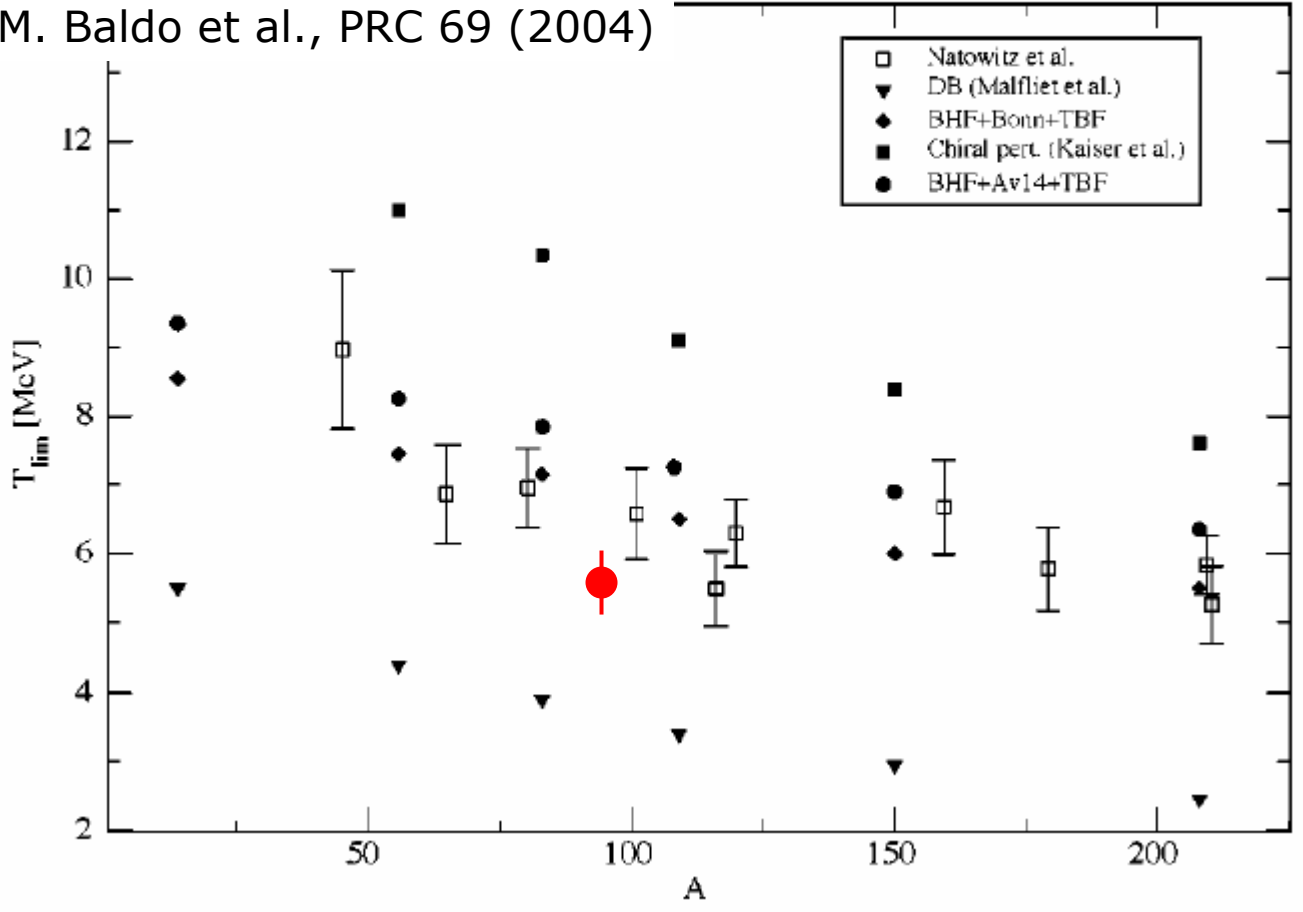


### III. consequences

## THE LIMITING TEMPERATURE OF HOT NUCLEI FROM MICROSCOPIC EQUATION OF STATE

M. Baldo et al., PRC 69 (2004)

1. the  $Z_{bound}$
2. Coulomb
- 2a. limiting
- 2b. the lim
- determ
3. multifrag
- instead

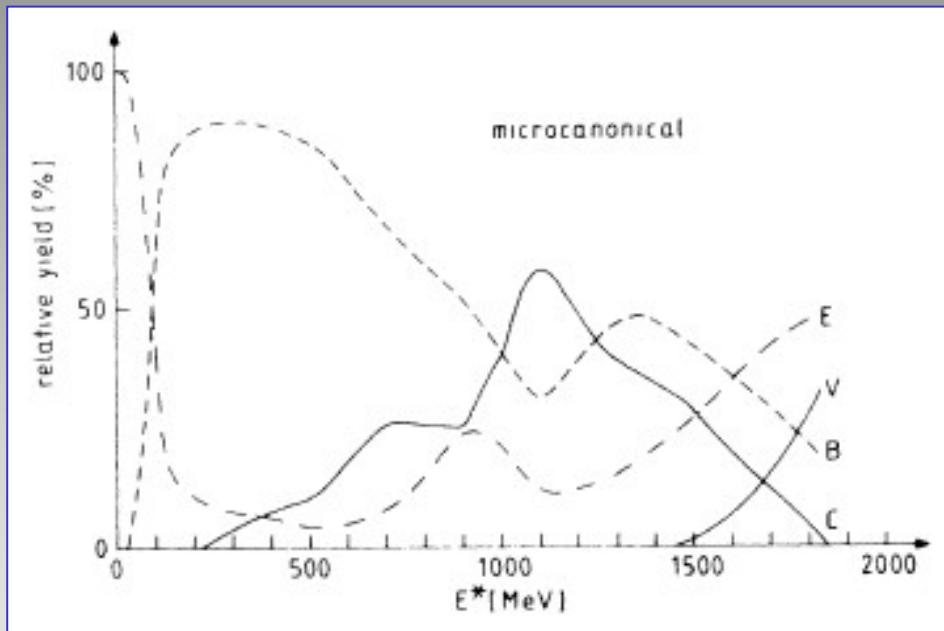


if it is not Coulomb ...  
what drives the system to expansion ?

1. the asymptotic phase space
2. early fragment recognition and persistence

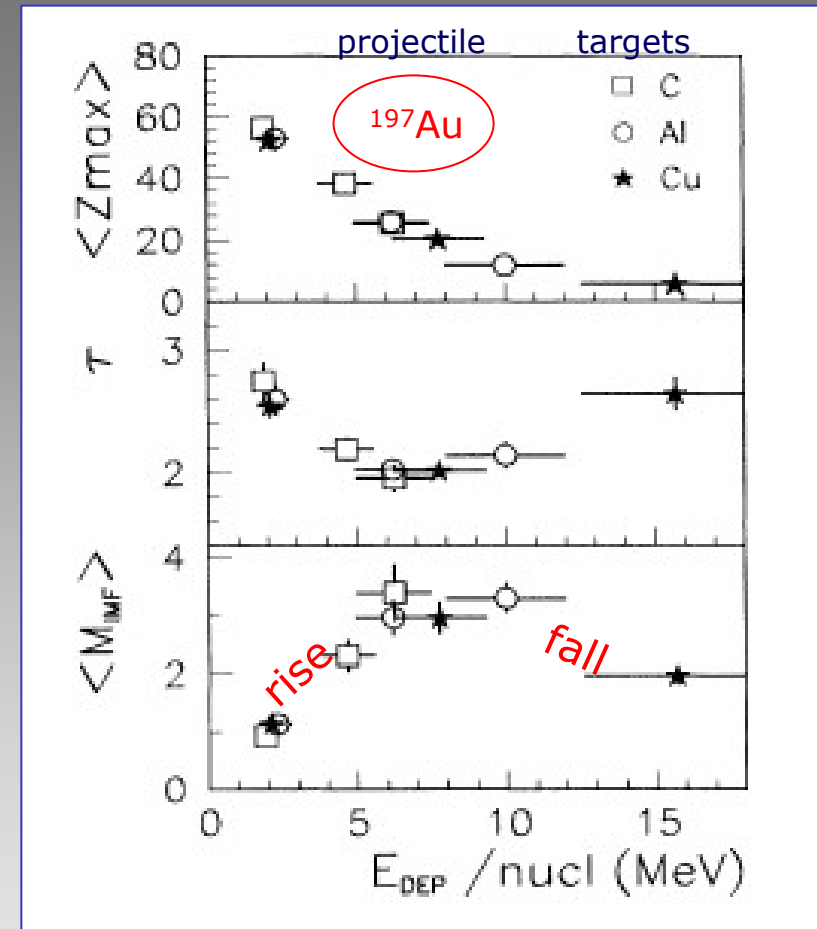
# the asymptotic phase space

D.H.E. Gross et al.  
PRL 56, 1544 (1986)



decay modes of  $^{238}\text{U}$   
c = cracking

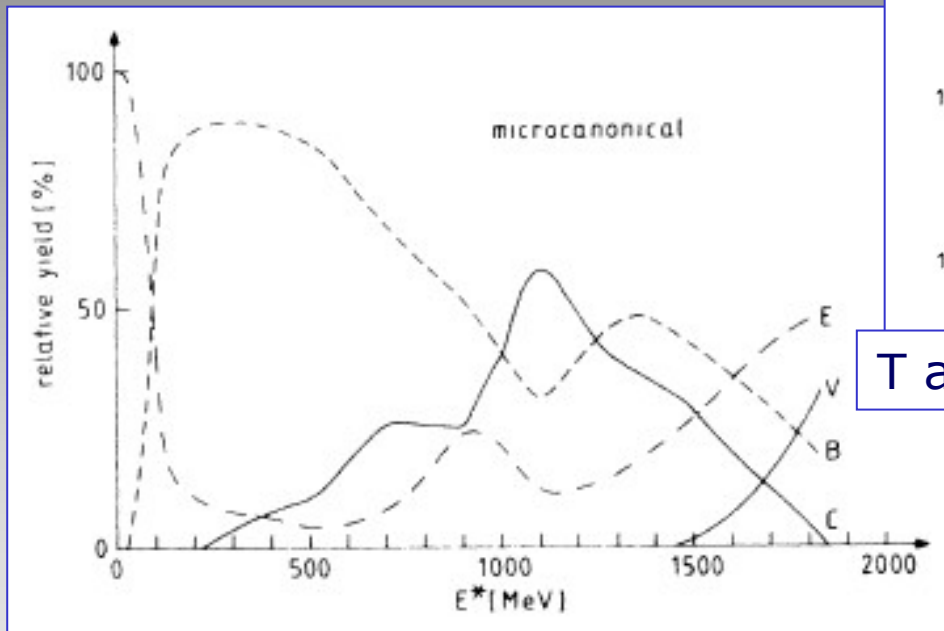
C.A. Ogilvie et al., PRL (1991)



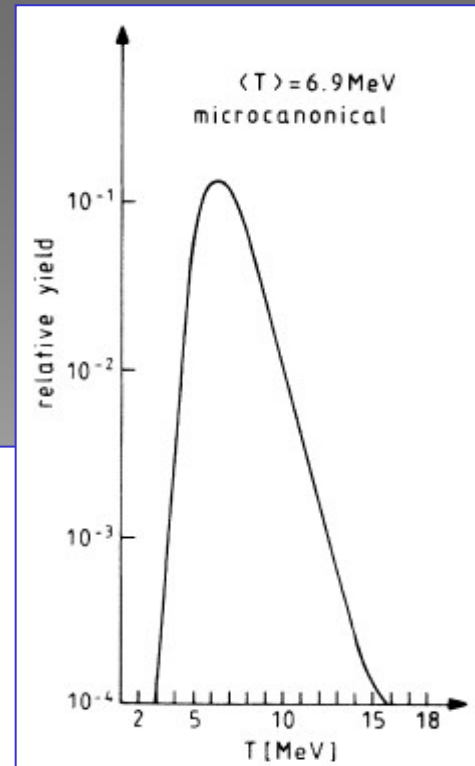
rise and fall of  
multi-fragment emission

# the asymptotic phase space

D.H.E. Gross et al.  
PRL 56, 1544 (1986)

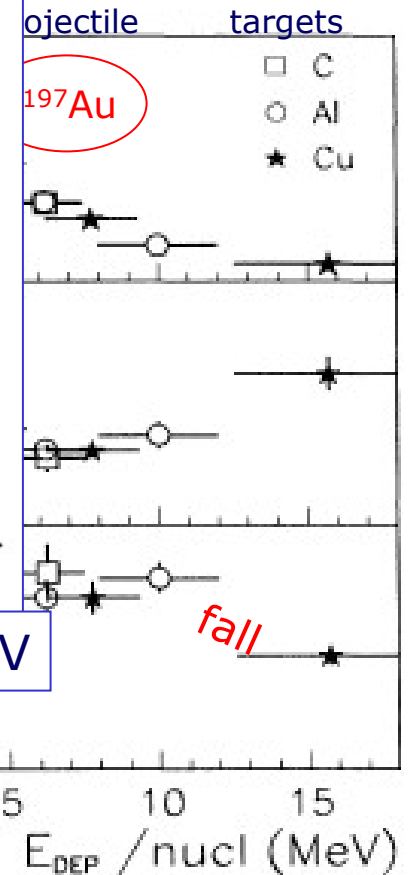


decay modes of  $^{238}\text{U}$   
c = cracking



T at  $E^* = 1100$  MeV

et al., PRL (1991)

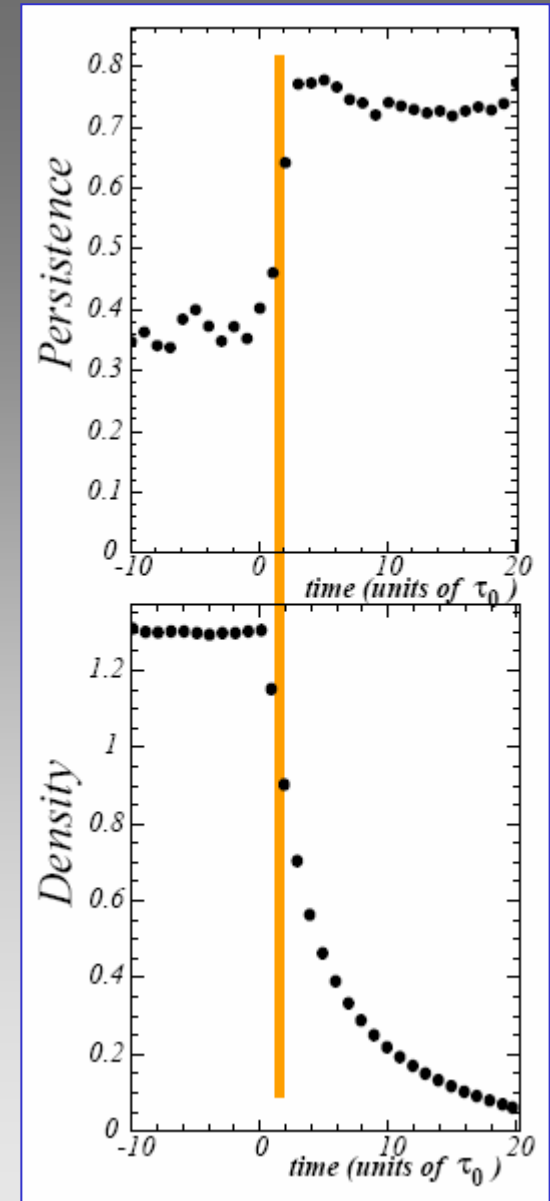
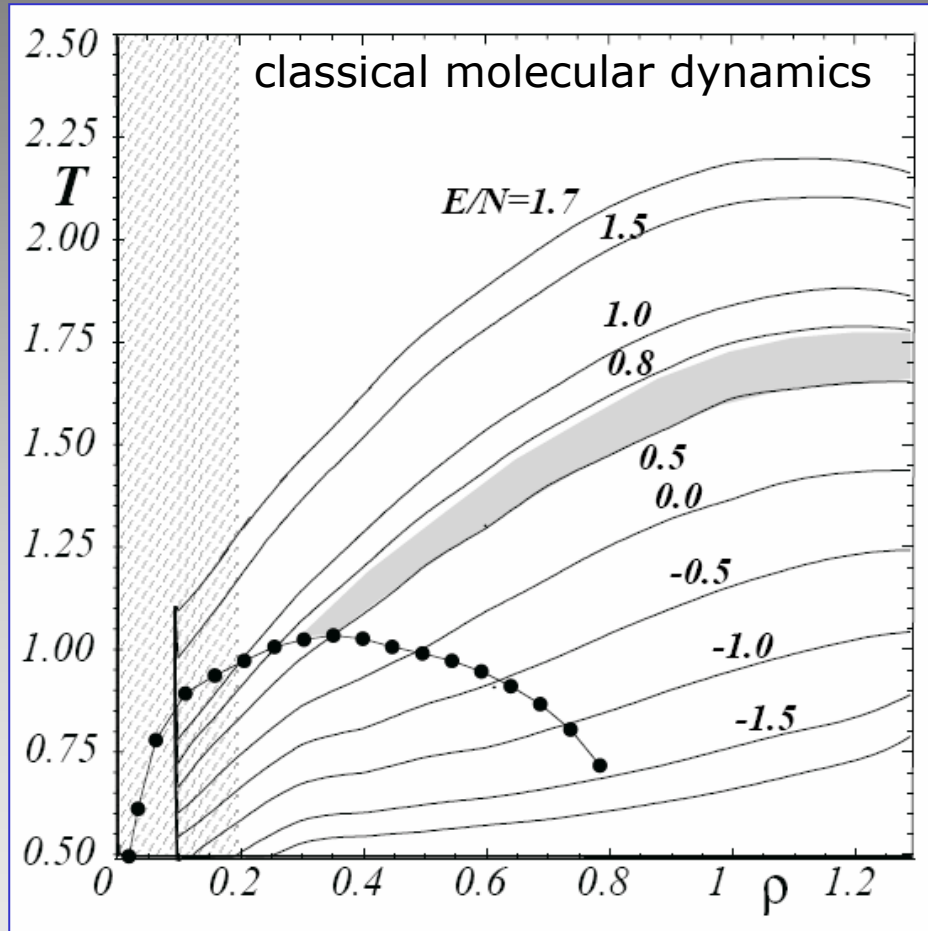


rise and fall of  
multi-fragment emission



# early fragment recognition and persistence

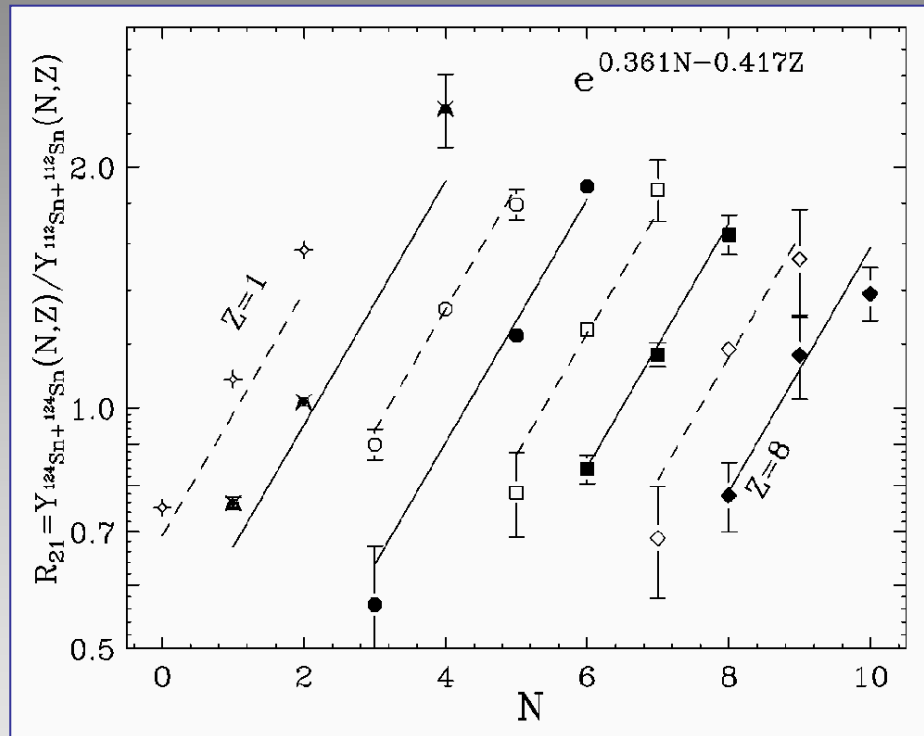
Campi et al., PRC 67, 044610 (2003)



see also: A. Le Fèvre and J. Aichelin, Phys. Rev. Lett. 100, 042701 (2008)

## IV. isoscaling

in reactions  $^{112}\text{Sn}+^{112}\text{Sn}$  and  $^{124}\text{Sn}+^{124}\text{Sn}$  at 50 A MeV

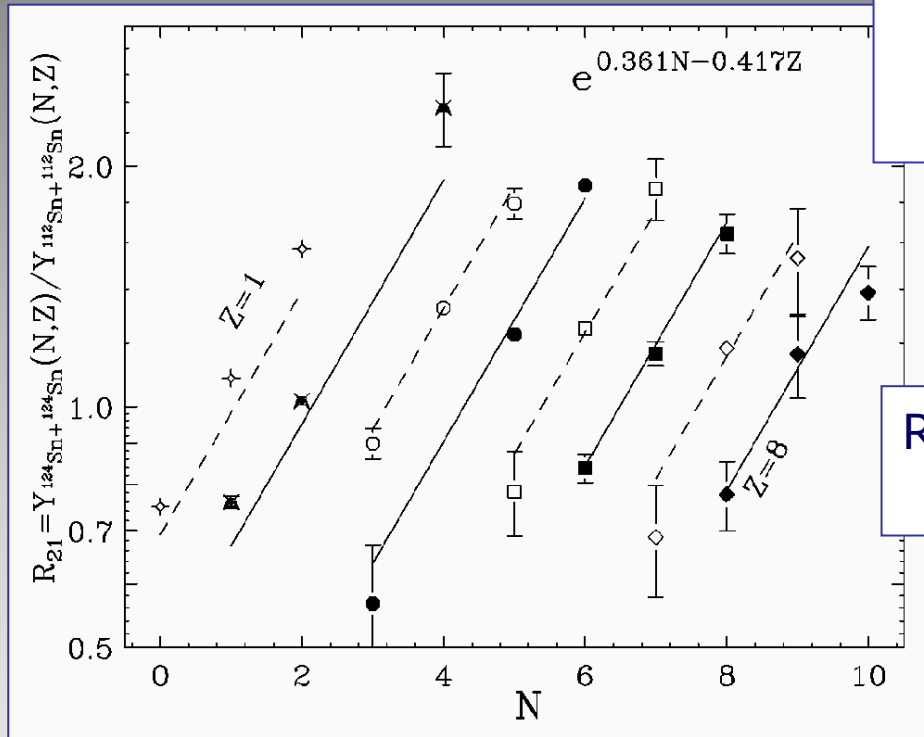
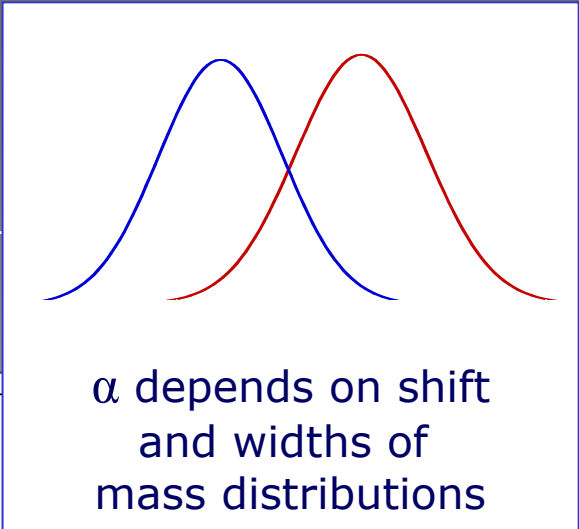


M.B. Tsang et al.,  
PRC 64, 054615 (2001)

*"systematic behavior of yield ratios following grandcanonical expectations"*

# IV. isoscaling

in reactions  $^{112}\text{Sn}+^{112}\text{Sn}$  and  $^{124}\text{Sn}+^{124}\text{Sn}$



$$R = C \cdot \exp(\alpha N + \beta Z)$$

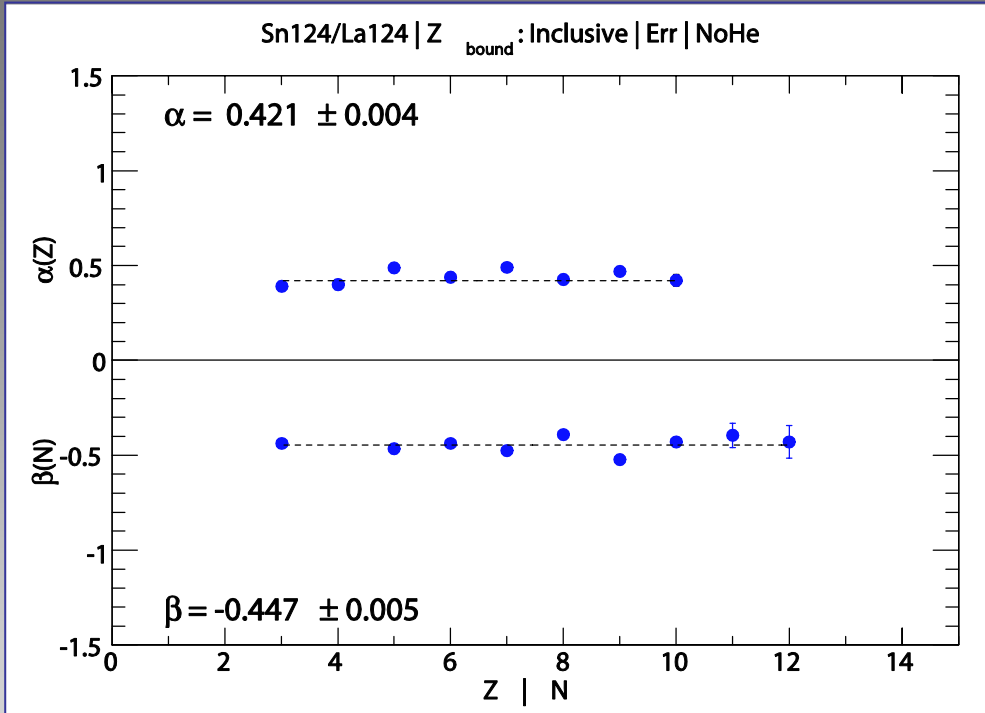
$$\alpha = \Delta\mu_n/T$$

M.B. Tsang et al.,  
PRC 64, 054615 (2001)

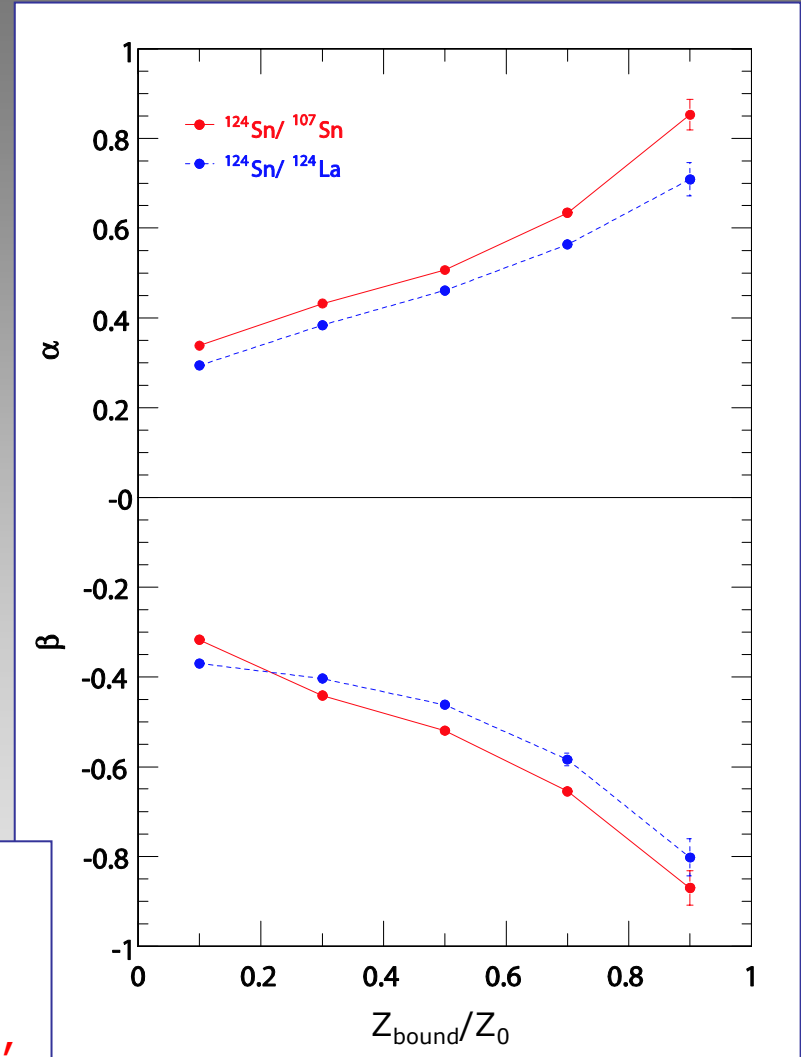
*"systematic behavior of yield ratios following grandcanonical expectations"*

# isoscaling in S254

S. Bianchin, J. Łukasik



$p_0$  fit of individual-Z (or N) fits



two experimental results:

- 1) the individual slopes are identical for  $Z \geq 3$
- 2) the isoscaling parameters drop with increasing excitation as seen with INDRA@GSI, A. Le Fèvre et al., PRL 94 (2005)

# summary of S254

1. **secondary beams essential** to enhance effects
2. **small changes of global observables** with  $N/Z$  important for isolating isospin effects
3. isotope distributions exhibit **memory and structure effects**
4.  $N/Z$  dependence of nuclear caloric curve indicates **phase-space driven instability** rather than Coulomb instability
5. isoscaling obeyed with high accuracy; results of INDRA@GSI confirmed and extended; **reduced symmetry term** for hot fragments