

Prospects of Reactor ν Oscillation Experiments

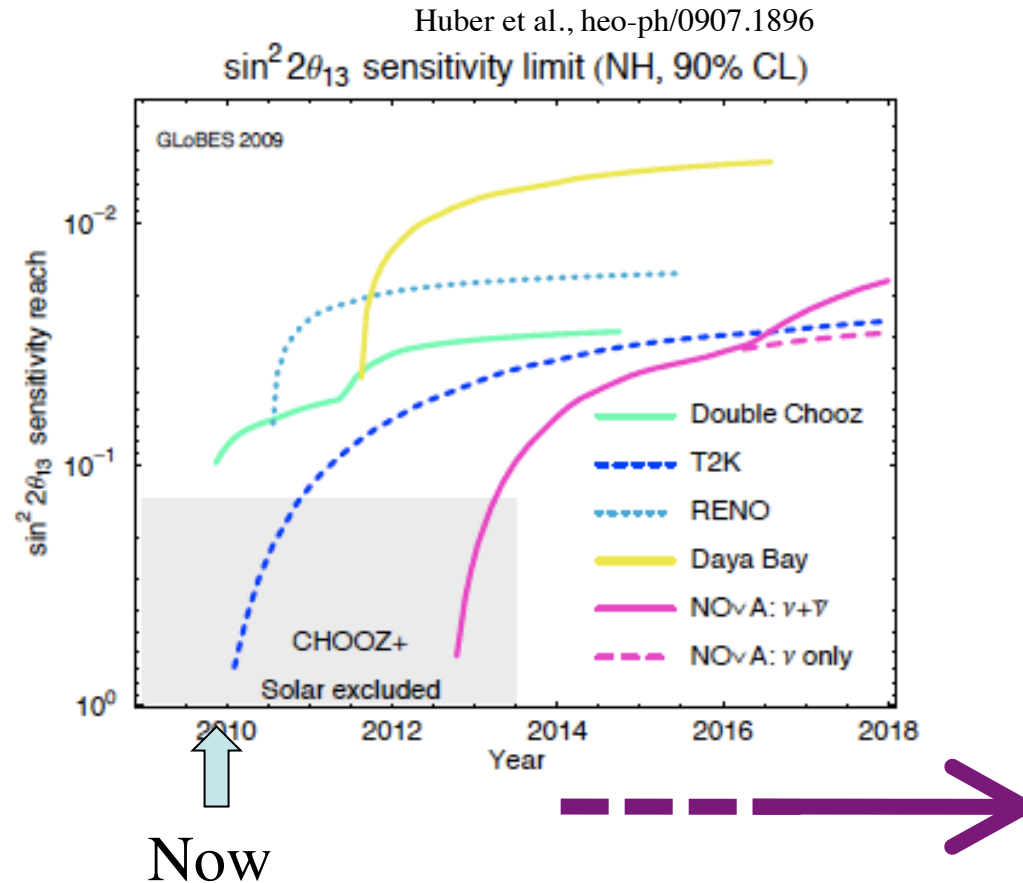
F. Suekane
RCNS, Tohoku Univ.

@Erice School
23/09/2009

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 - @2nd Δm^2_{12} O.M.
- * Summary

An exciting time is just around the corner ...



What reactor experiments could do next?

Issues for ν oscillation & solving methods

4 still unknowns

- (1) $\sin^2 2\theta_{13}$
- (2) Mass Hierarchy
- (3) θ_{23} degeneracy
- (4) CP violating δ

Available information

- (1) $\nu_\mu \Rightarrow \nu_e$ (accelerator)
- (2) $\bar{\nu}_\mu \Rightarrow \bar{\nu}_e$ (accelerator)
- (3) Matter effect (accelerator)
- (4) $\nu_\mu \Rightarrow \nu_\mu$ (accelerator)
- (5) $\bar{\nu}_e \Rightarrow \bar{\nu}_e$ (reactor)
- (6) Solar, Atmospheric

Construction(\$\$\$)
+ $\nu = \$\$$

Construction(\$~\$\$)
 $\nu = \text{free}$

Reactor ν experiments are cost-effective way to get important information.

Physics of ν Oscillation (a different view)

Oscillation Formula: $P(\nu_e \rightarrow \nu_\mu) = \sin^2 2\theta \sin^2 \Delta_{21}; \quad \Delta_{21} \equiv \frac{(m_2^2 - m_1^2)L}{4E}$

Neutrino Mixing:

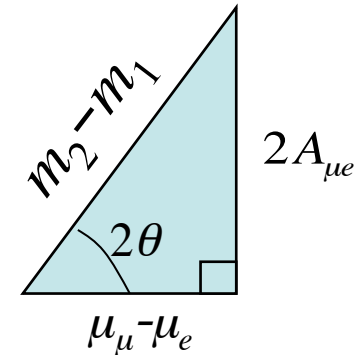
$$\begin{pmatrix} \nu_1 \\ \nu_2 \end{pmatrix} = \begin{pmatrix} \cos\theta & \sin\theta \\ -\sin\theta & \cos\theta \end{pmatrix} \begin{pmatrix} \nu_e \\ \nu_\mu \end{pmatrix}$$

Time evolution of mass eigenstate

Mass eigenstate

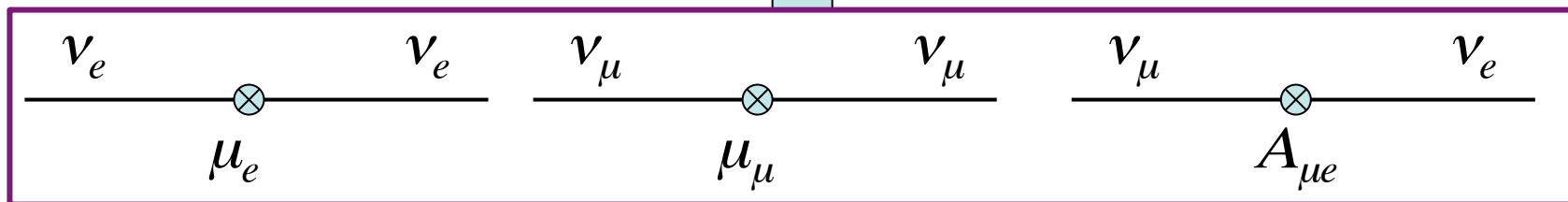
ν Equation of Motion:

$$i \frac{d}{dt} \begin{pmatrix} \nu_e \\ \nu_\mu \end{pmatrix} = \begin{pmatrix} \mu_e & A_{\mu e} \\ A_{\mu e} & \mu_\mu \end{pmatrix} \begin{pmatrix} \nu_e \\ \nu_\mu \end{pmatrix}$$

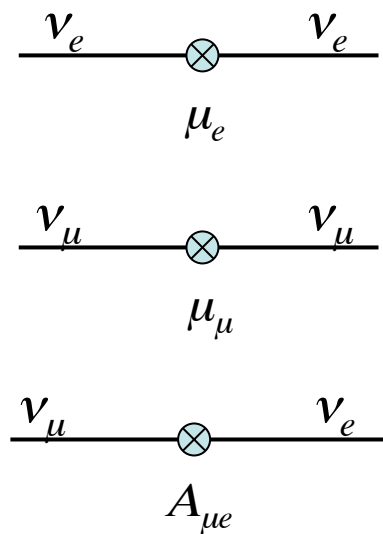


Flavor Transitions:

Transition Amplitudes

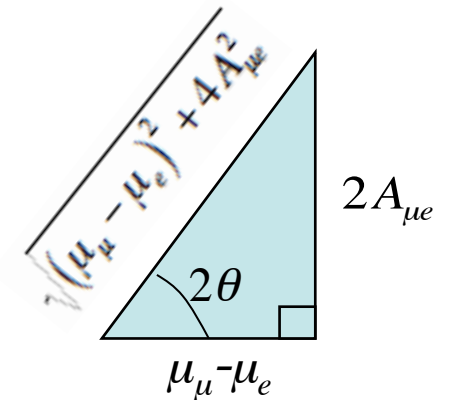


What we measure by ν Oscillation



$$P(\nu_e \rightarrow \nu_\mu) = \sin^2 2\theta \sin^2 \frac{\Delta m^2 L}{4E}$$

$$\begin{cases} \tan 2\theta = \frac{2A_{\mu e}}{\mu_\mu - \mu_e} \\ \Delta m^2 = (\mu_\mu + \mu_e) \sqrt{(\mu_\mu - \mu_e)^2 + 4A_{\mu e}^2} \end{cases}$$



Existence of ν Oscillation is an evidence of finite $A_{\mu e}$

Transition amplitudes can be determined together with absolute mass.

Purpose of ν Oscillation experiment

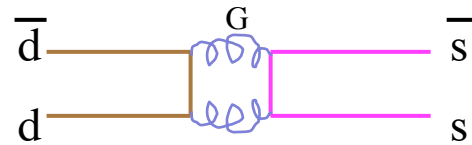
Physics of ν oscillation is to measure the flavor transition amplitudes (\Leftarrow experimentalist) and think of its origin (\Leftarrow theorist).

Now we know ν_α ν_β exists.

Non Standard Higgs?

Sub Structure??

For Example,

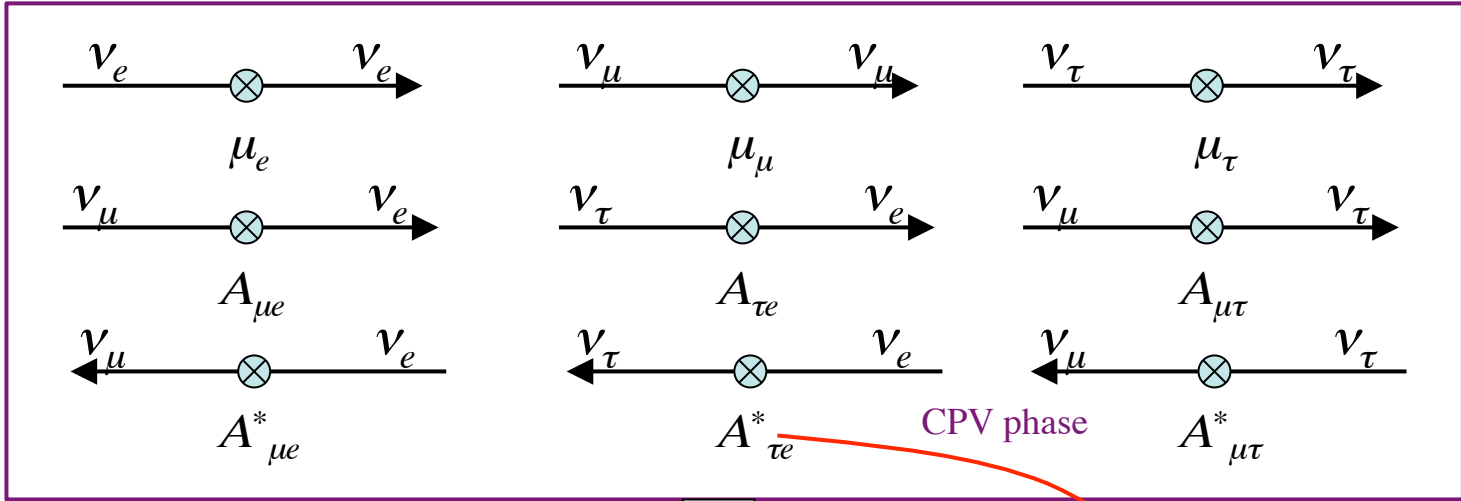


$$\begin{pmatrix} \pi^0 \\ \eta \\ \eta' \end{pmatrix} \sim \begin{pmatrix} 0.7 & 0.7 & 0 \\ -0.4 & 0.4 & 0.8 \\ 0.6 & -0.6 & 0.6 \end{pmatrix} \begin{pmatrix} |u\bar{u}\rangle \\ |d\bar{d}\rangle \\ |s\bar{s}\rangle \end{pmatrix}$$

Or something else??
 $A_{NP}?$

3 Flavors case

Transitions



Mixing

$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = \begin{pmatrix} U_{e1} & U_{e2} & U_{e3} \\ U_{\mu1} & U_{\mu2} & U_{\mu3} \\ U_{\tau1} & U_{\tau2} & U_{\tau3} \end{pmatrix} \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix} \begin{pmatrix} c_{13} & 0 & s_{13}e^{i\delta} \\ 0 & 1 & 0 \\ -s_{13}e^{-i\delta} & 0 & c_{13} \end{pmatrix} \begin{pmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix}$$

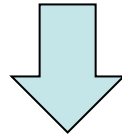
Oscillation

$$\begin{aligned}
 P(\nu_\alpha \rightarrow \nu_\beta) &= \delta_{\alpha\beta} - 4 \sum_{i>j} \text{Re}(U_{\alpha i}^* U_{\beta i} U_{\alpha j} U_{\beta j}^*) \sin^2 \Delta_{ij} \mp 2 \sum_{i>j} \text{Im}(U_{\alpha i}^* U_{\beta i} U_{\alpha j} U_{\beta j}^*) \sin 2\Delta_{ij} \\
 P(\bar{\nu}_\alpha \rightarrow \bar{\nu}_\beta) &= \delta_{\alpha\beta} - 4 \sum_{i>j} \text{Re}(U_{\alpha i}^* U_{\beta i} U_{\alpha j} U_{\beta j}^*) \sin^2 \Delta_{ij} \mp 2 \sum_{i>j} \text{Im}(U_{\alpha i}^* U_{\beta i} U_{\alpha j} U_{\beta j}^*) \sin 2\Delta_{ij}
 \end{aligned}$$

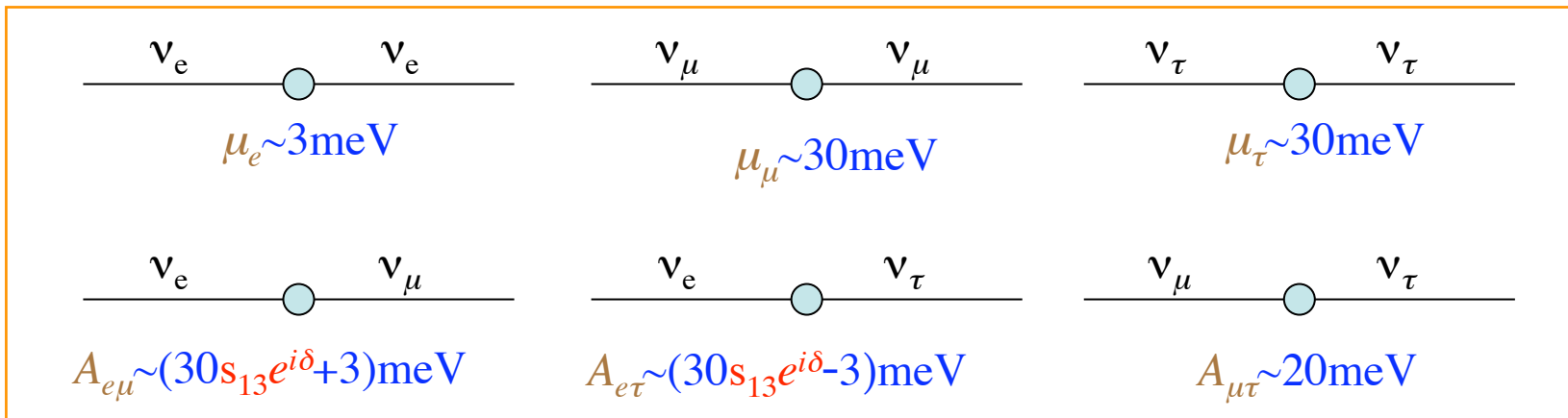
Our Current Knowledge

$$|m_3^2 - m_2^2| \sim 2.6 \times 10^{-3} \text{ eV}^2, \quad (m_2^2 - m_1^2) \sim 8 \times 10^{-5} \text{ eV}^2$$

$$U_{MNS} \sim \begin{pmatrix} 0.8 & 0.5 & s_{13} e^{i\delta} \\ -0.4 & 0.6 & 0.7 \\ 0.4 & -0.6 & 0.7 \end{pmatrix} \quad |s_{13}| < 0.2$$

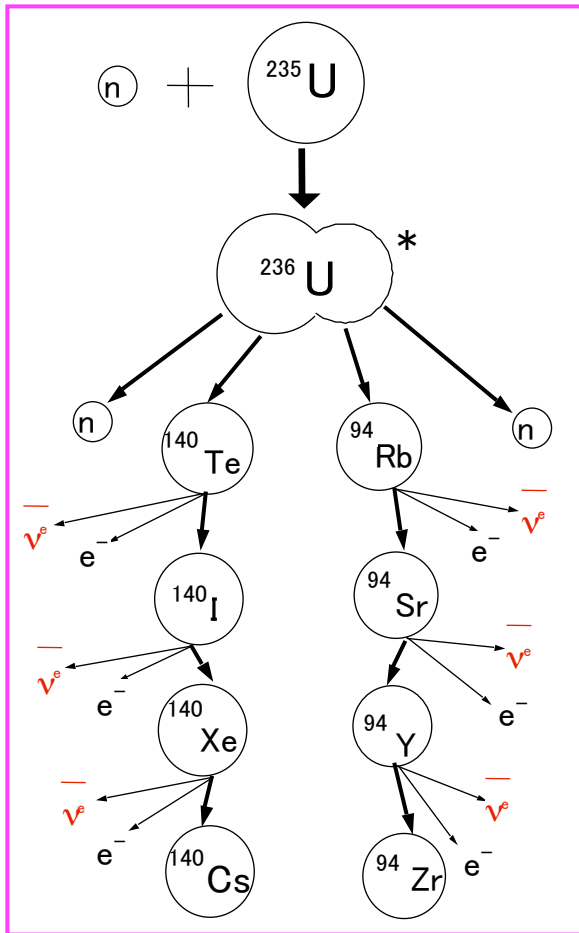


If $m_3 > m_2 \gg m_1 \sim 0$,



(charged lepton=mass eigenstate)

Reactor neutrino

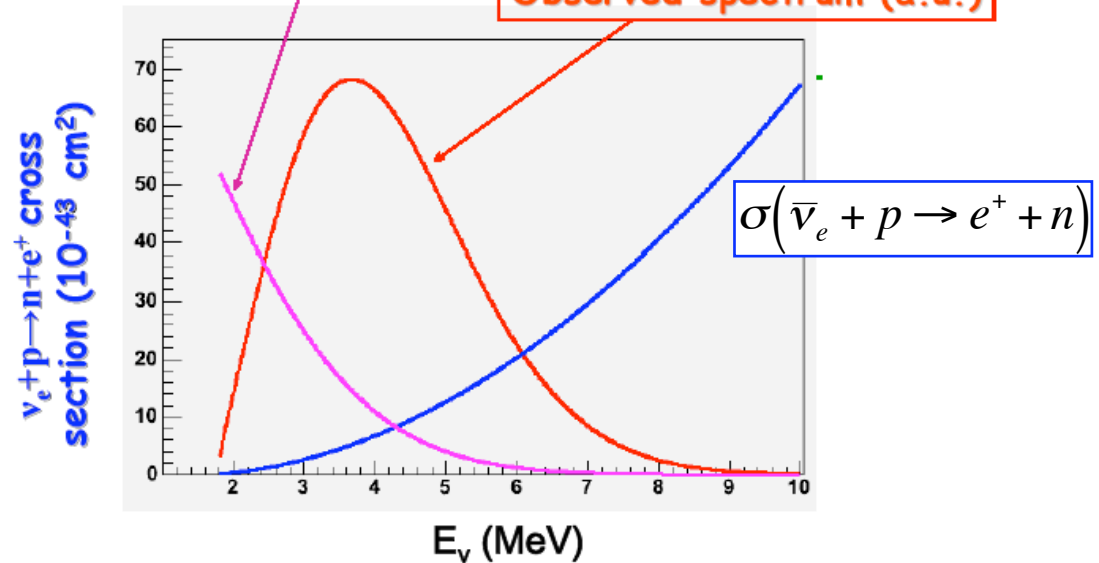


$\bar{\nu}$ are produced in β -decays of fission products.
 $\sim 6 \times 10^{20} \bar{\nu}_e / s / reactor$

The $\bar{\nu}_e$ energy spectrum

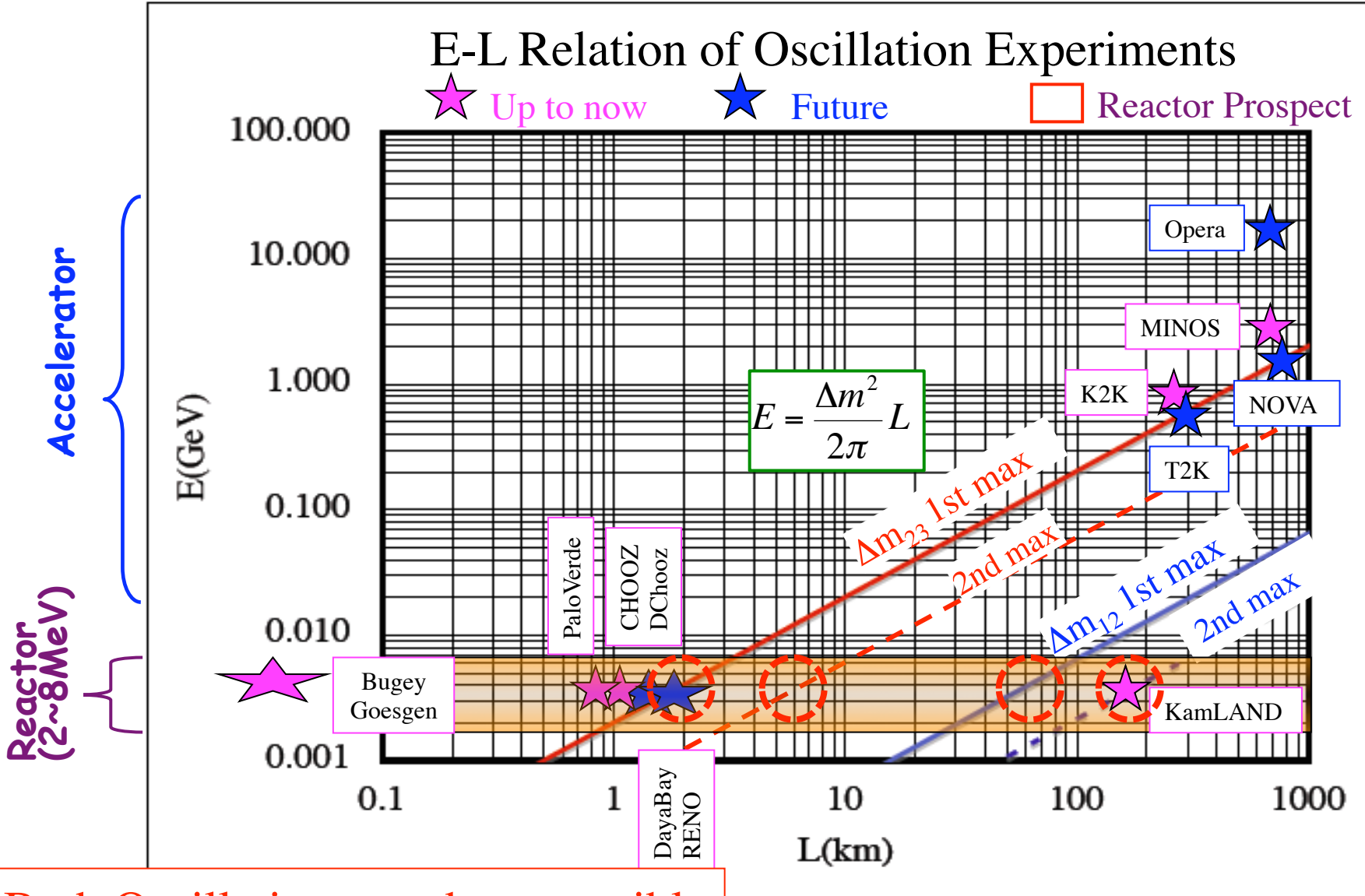
Reactor $\bar{\nu}_e$ spectrum (a.u.)

Observed spectrum (a.u.)



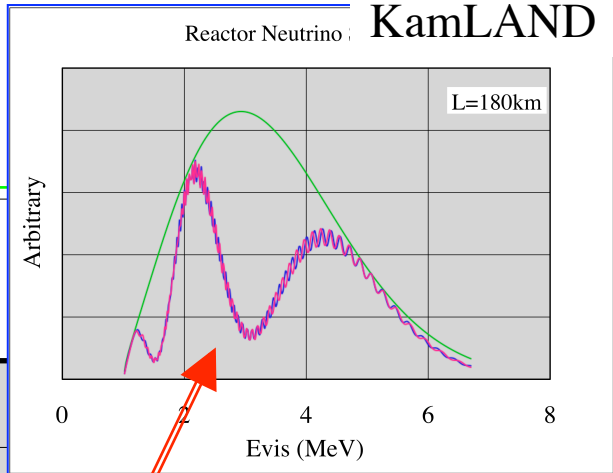
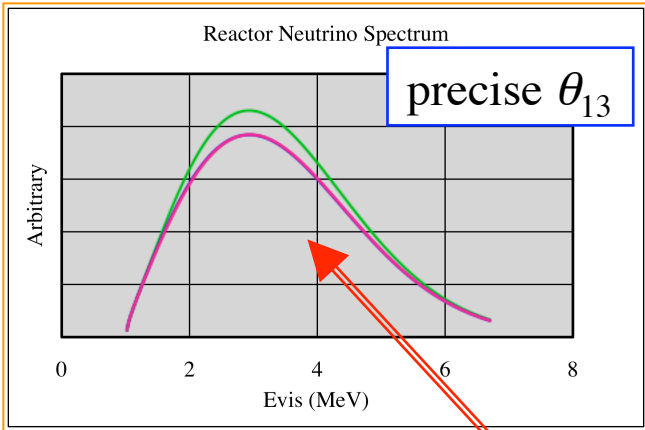
$$E_\nu \sim 4^{+4}_{-2} \text{ MeV}$$

Accessible Oscillations by Reactor ν



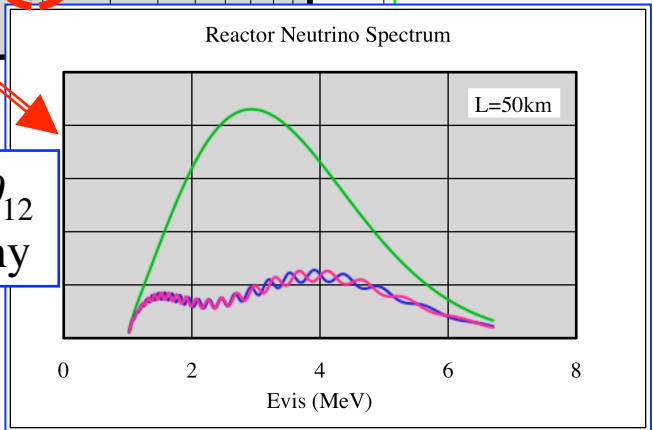
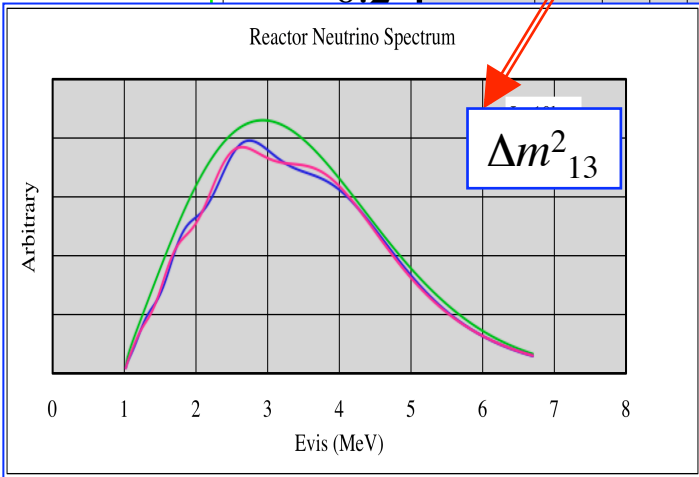
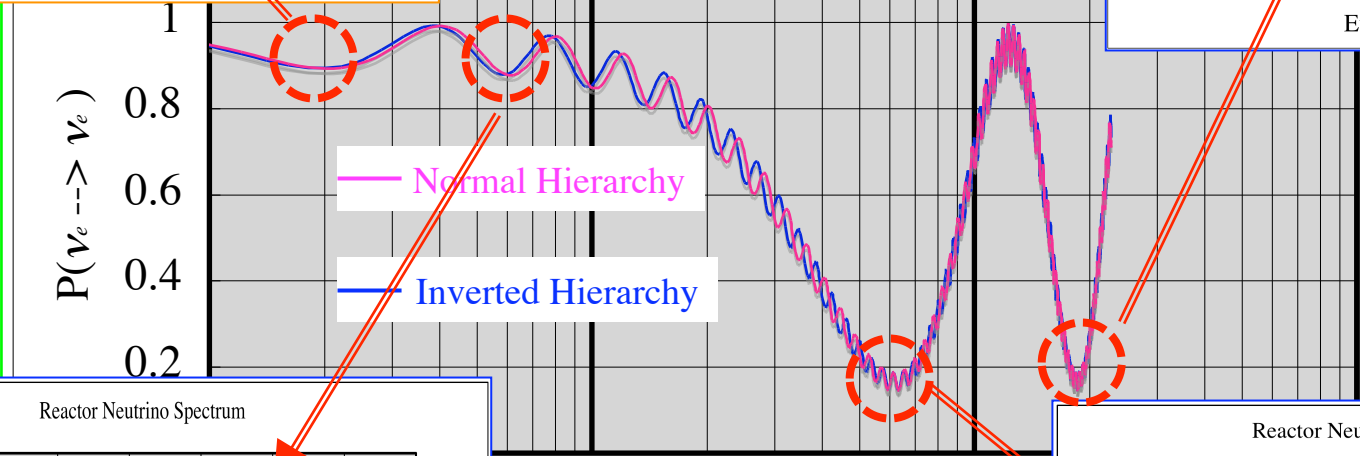
Both Oscillations can be accessible

$$P(\bar{\nu}_e \rightarrow \bar{\nu}_e) = 1 - \cos^4 \theta_{13} \sin^2 2\theta_{12} \sin^2 \Delta_{21} - \sin^2 2\theta_{13} (\cos^2 \theta_{12} \sin^2 \Delta_{31} + \sin^2 \theta_{12} \sin^2 \Delta_{32})$$



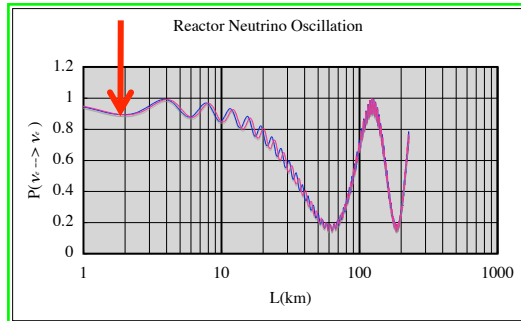
Reactor Neutrino Oscillation

$\sin^2 2\theta_{13} = 0.1$ assumed



Very precise θ_{12}
Mass Hierarchy

Physics @ 1st Δm^2_{13} Maximum ($L \sim 1.5 \text{ km}$) ; θ_{13}



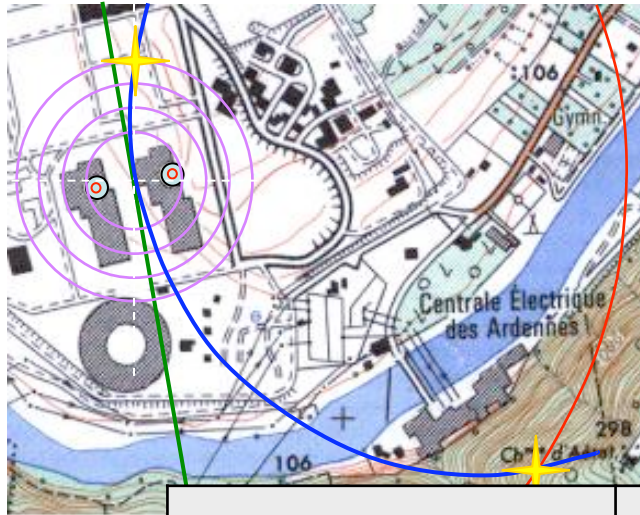
$$P_R(\bar{\nu}_e \rightarrow \bar{\nu}_e) \approx 1 - \sin^2 2\theta_{13} \sin^2 \Delta_{31}$$

Future ν experiments strongly depends on θ_{13}
 Precise measurement of θ_{13} is very important.

Parameter	Measurement Method
δ_{CP}	$\left[P_A(\nu_\mu \rightarrow \nu_e) - P_A(\bar{\nu}_\mu \rightarrow \bar{\nu}_e) \right]_{@ \Delta_{23}} \sim 0.1 \sin 2\theta_{13} \sin \delta$ $P_A(\nu_\mu \rightarrow \nu_e)_{@ \Delta_{23}} \sim 0.5 \sin^2 2\theta_{13} \pm 0.05 \sin 2\theta_{13} \sin \delta$
θ_{23} degeneracy	$\left[P_A(\nu_\mu \rightarrow \nu_e) + P_A(\bar{\nu}_\mu \rightarrow \bar{\nu}_e) \right]_{@ \Delta_{23}} \sim 2 \sin^2 \theta_{23} \sin^2 2\theta_{13}$
Mass Hierarchy	$\left[P_A(\nu_\mu \rightarrow \nu_e; L) + P_A(\nu_\mu \rightarrow \nu_e; L') \right]_{@ \Delta_{23}} \sim \text{sign}(\Delta m^2_{23})(L' - L) \sin^2 2\theta_{13}$ $P_R(\bar{\nu}_e \rightarrow \bar{\nu}_e)_{@ \Delta_{12}} \sim 1 - 0.5 \sin^2 2\theta_{13} (\sin^2 \Delta_{31} + \tan^2 \theta_{12} \sin^2 \Delta_{32})$

DoubleChooz, Dayabay, RENO

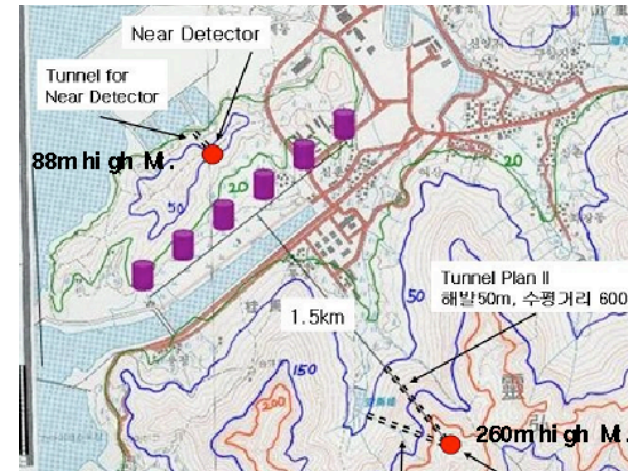
Double Chooz



Daya Bay



RENO



	Double Chooz	Dayabay	RENO
Power(GWth)	8.6GW	11.6GWth (17.4GW>2011)	16.4GW
Detector(ton)	8+8	20x4+2(20x2)	16+2
Baseline(km)	1.05	1.8	1.4
$\sin^2 2\theta_{13}$ Sensitivity	~ 0.03	~ 0.01	~ 0.02
Operation start	2010/2011	2011	2010

Results: within 2~5years

Complementarity of Reactor-Accelerator θ_{13} measurement

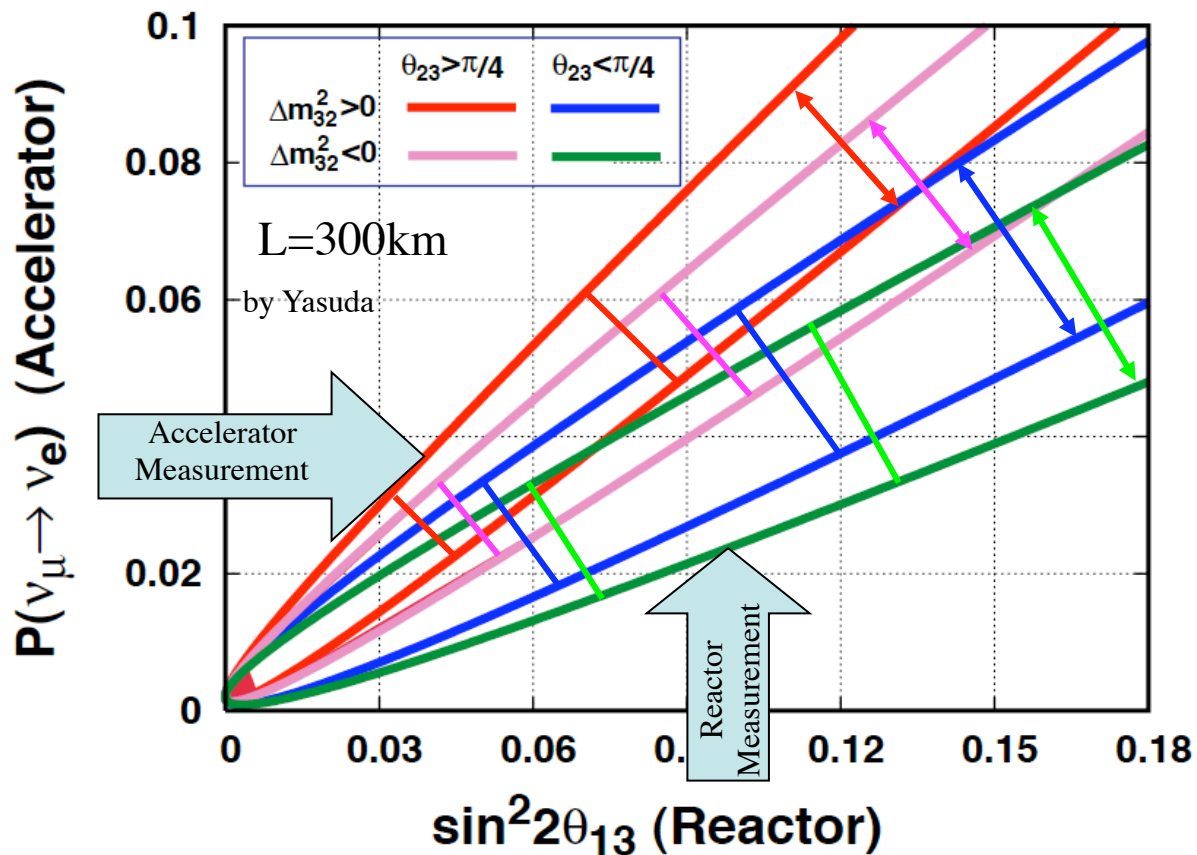
θ_{23} degeneracy

$$P_{AC}(\nu_{\mu} \rightarrow \nu_e) = \frac{0.50 \pm 0.11}{(1 \mp 0.00017L[km])^2} \sin^2 2\theta_{13} \pm 0.045 \sin 2\theta_{13} \sin \delta$$

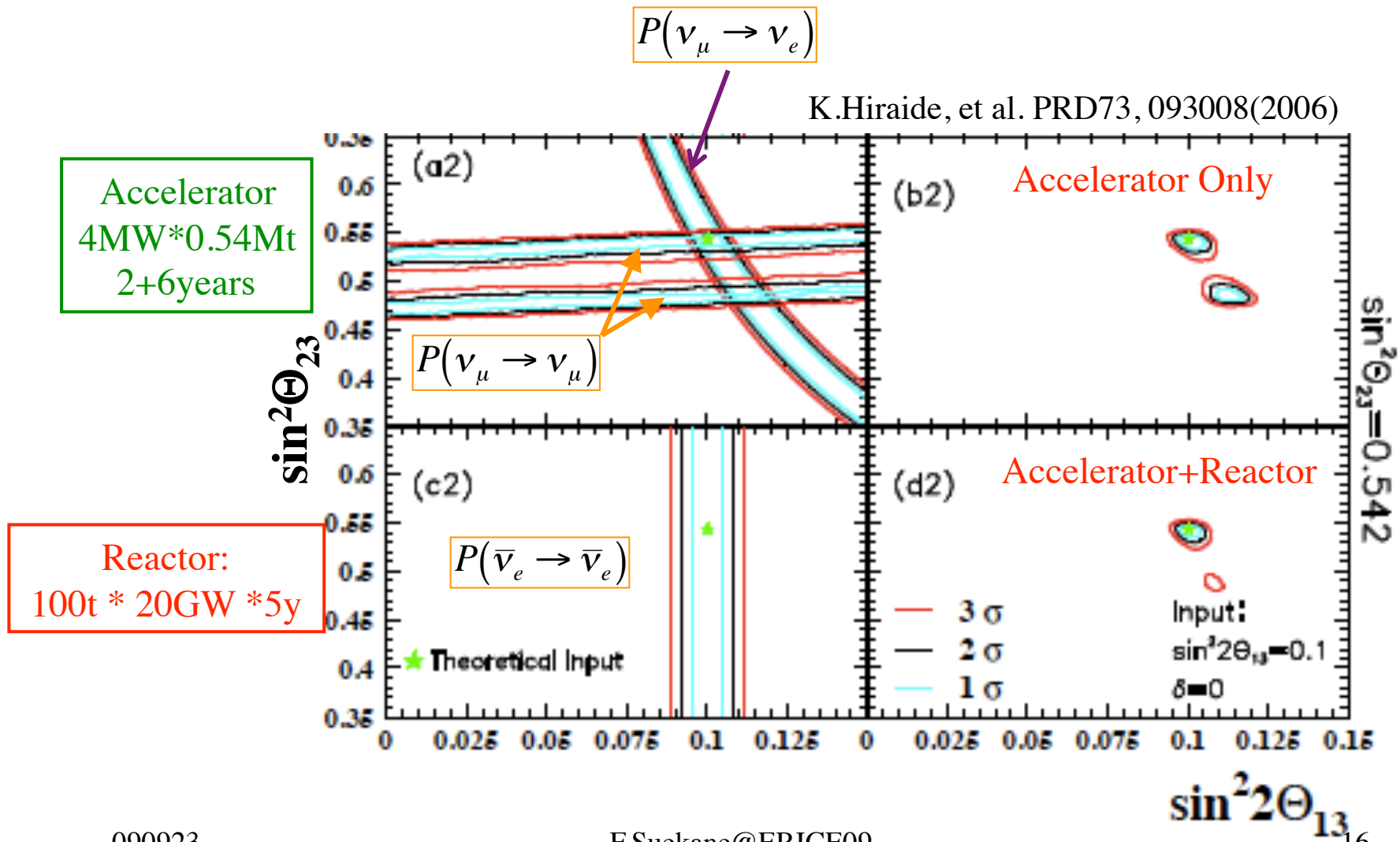
Matter effect

$$\sin^2 2\theta_{23} = 0.95$$

δ dependence

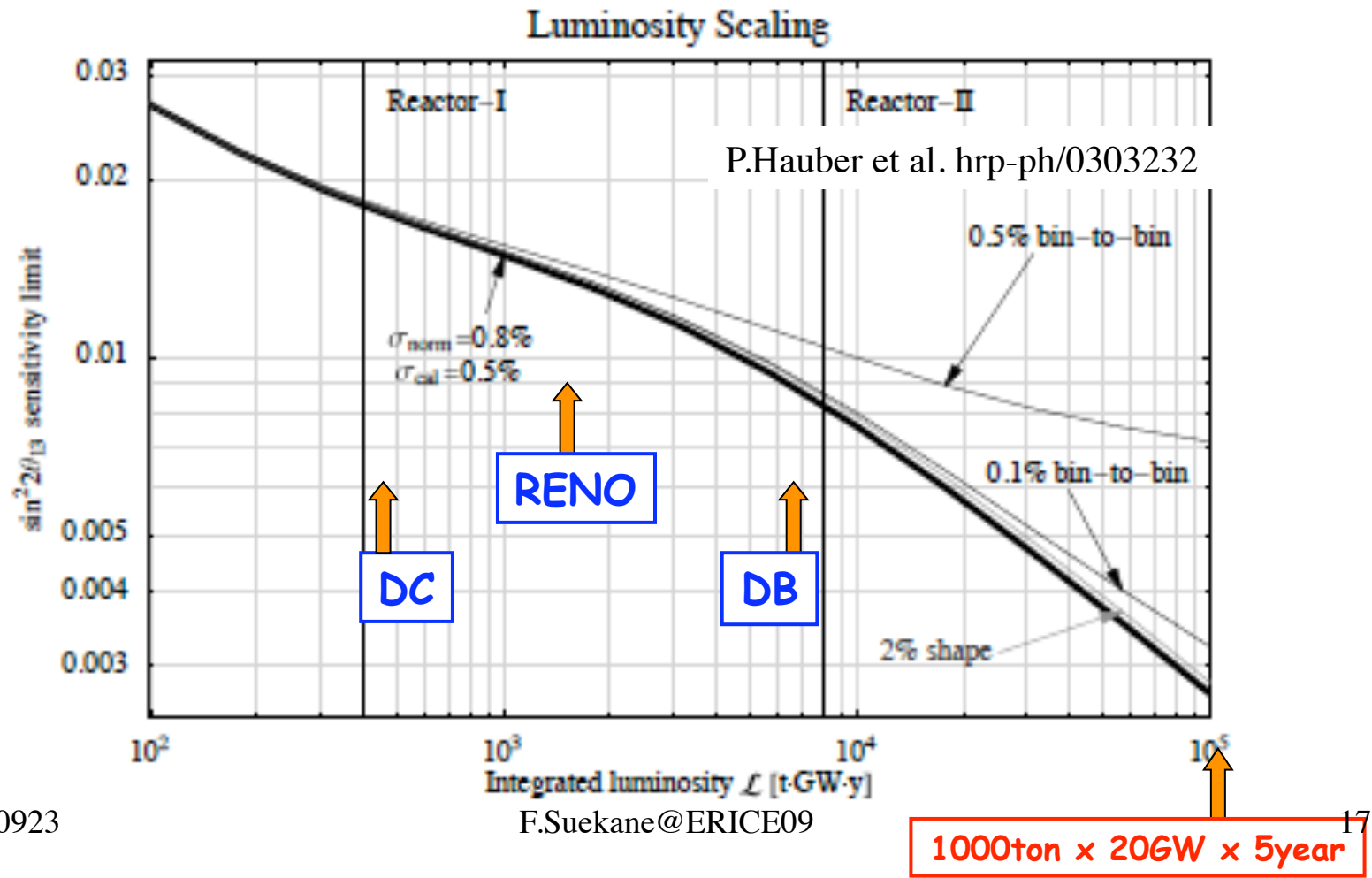


Settlement of θ_{23} Degeneracy

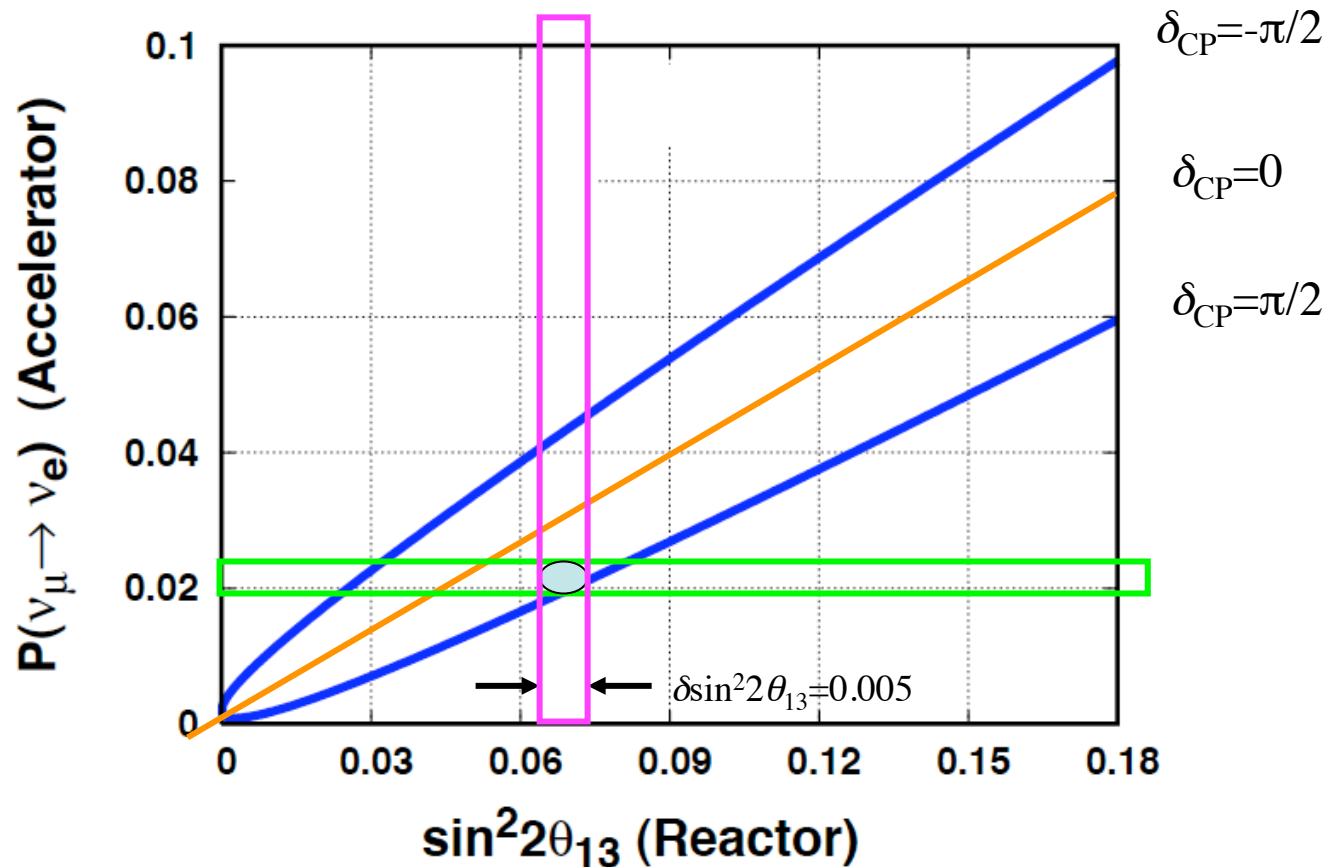


3rd Generation; More Precise θ_{13}

For higher statistics, θ_{13} can be measured by energy spectrum distortion and $\delta \sin^2 2\theta_{13} < 0.01$ is possible



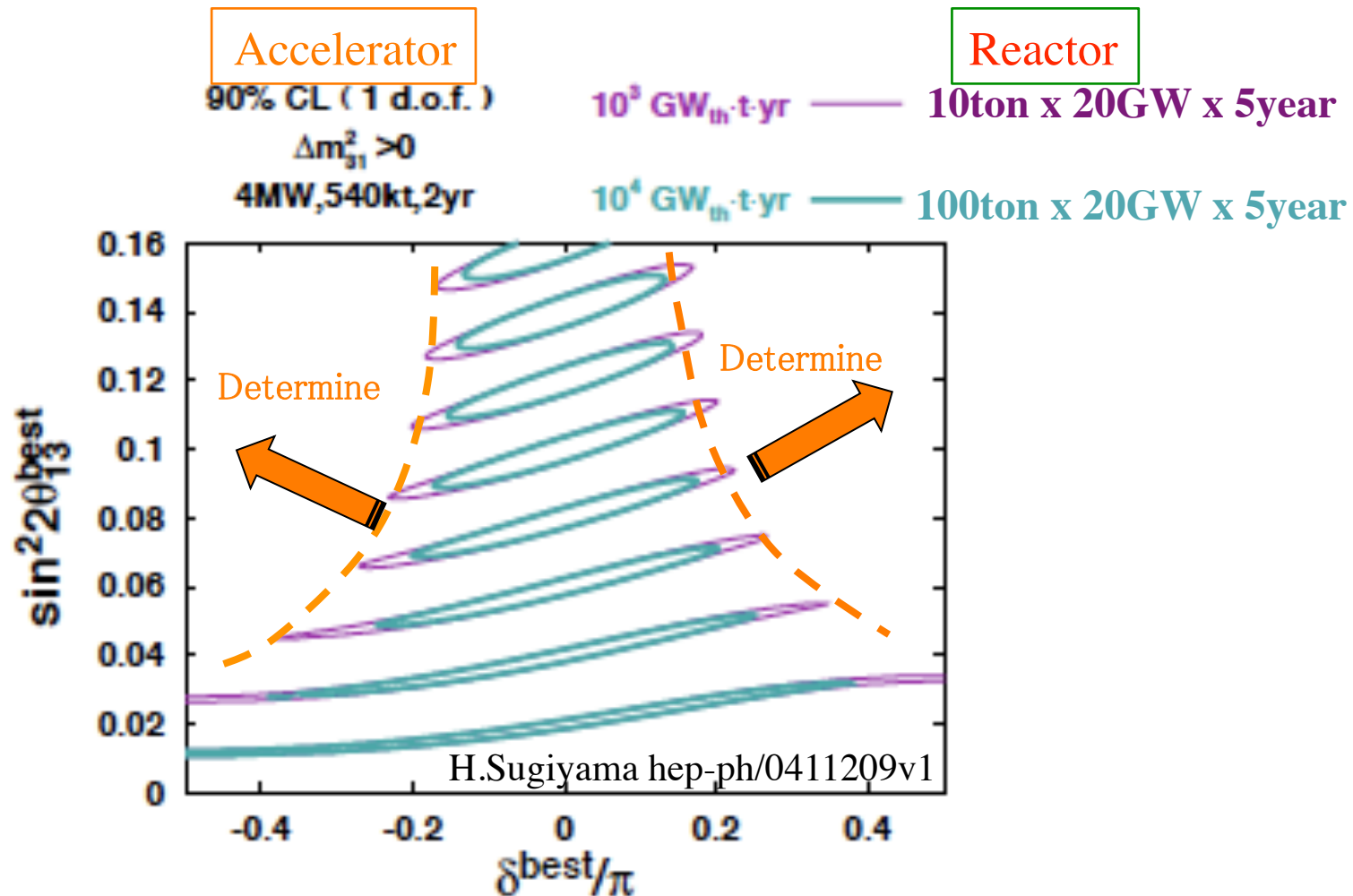
Quick Access to δ_{CP}



If θ_{23} degeneracy and Mass Hierarchy are solved, only δ remains to be solved.

Combination of high **precision Reactor- θ_{13}** and **Accelerator ν_e appearance** may determine **non-0 δ** before anti-neutrino mode operation.

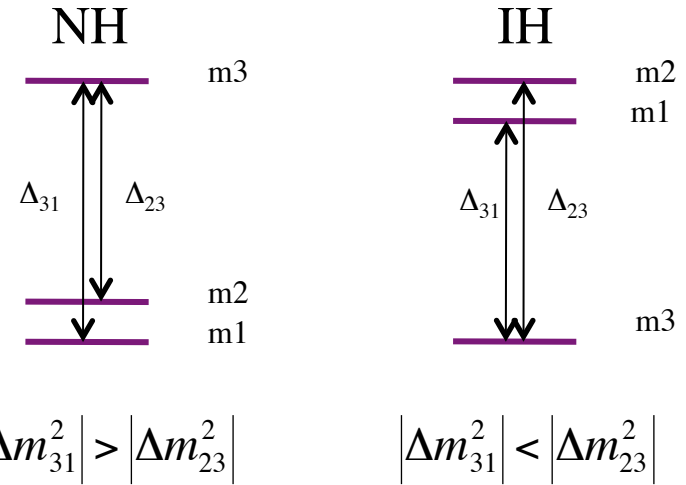
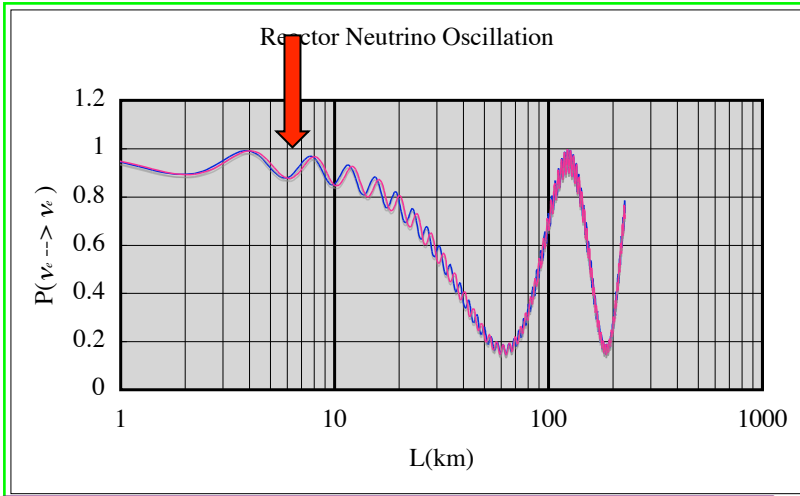
Parameter region to determine non-0 δ



If $\sin^2 2\theta_{13} > 0.05$ there is a possibility to determine non-0 δ

Physics @ Δm_{13}^2 2nd Maximum (L~5km)

($|\Delta m_{13}^2|$ measurement)



$$P_R(\bar{\nu}_e \rightarrow \bar{\nu}_e) \approx 1 - \sin^2 2\theta_{13} \sin^2 \Delta_{31}$$

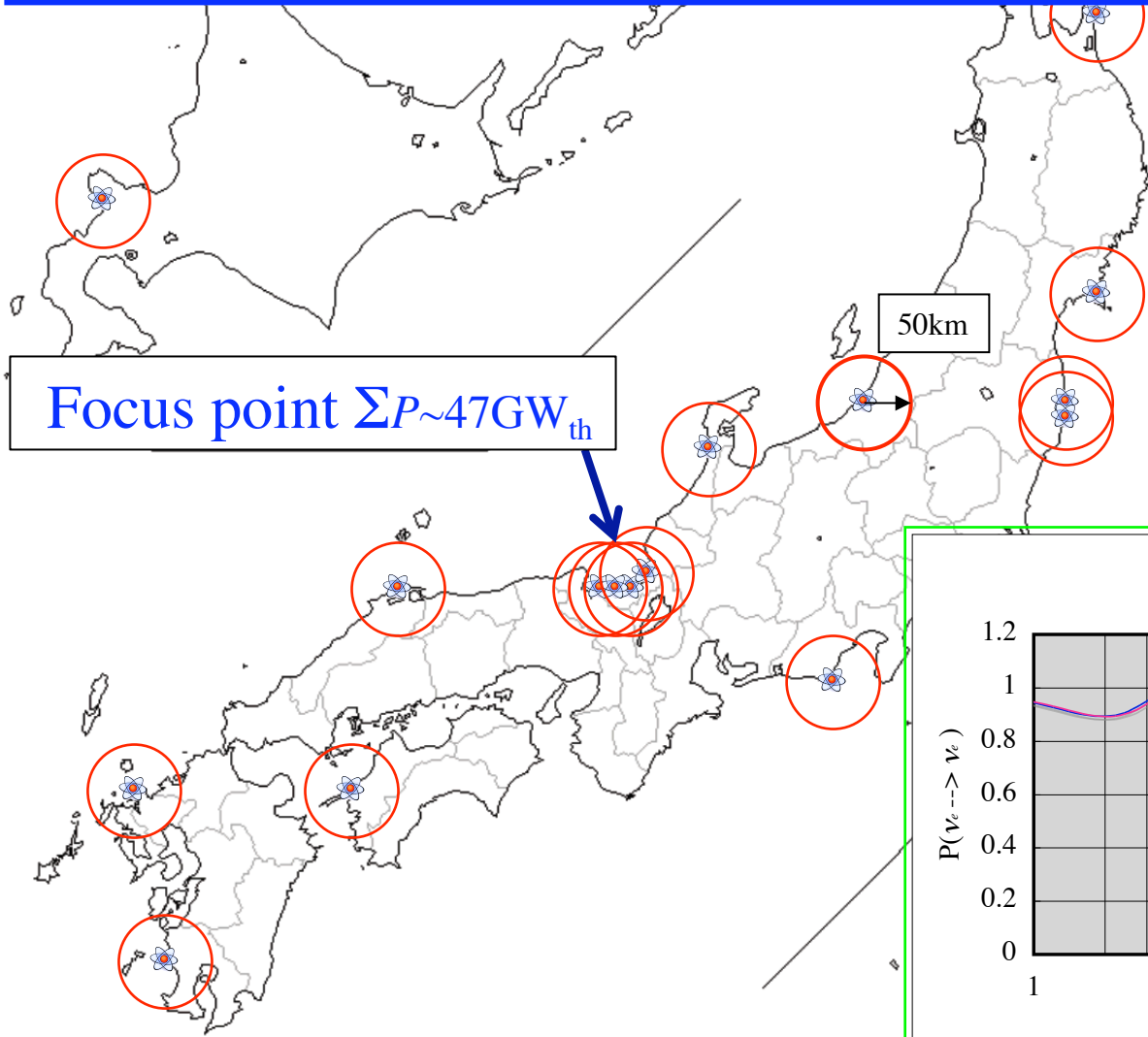
In principle, Mass Hierarchy is accessible

However, accuracy of $\frac{\delta|\Delta m_{31}^2|}{|\Delta m_{31}^2|}, \frac{\delta|\Delta m_{23}^2|}{|\Delta m_{23}^2|} \ll \frac{|\Delta m_{12}^2|}{|\Delta m_{23}^2|} \sim 3\%$ are necessary.

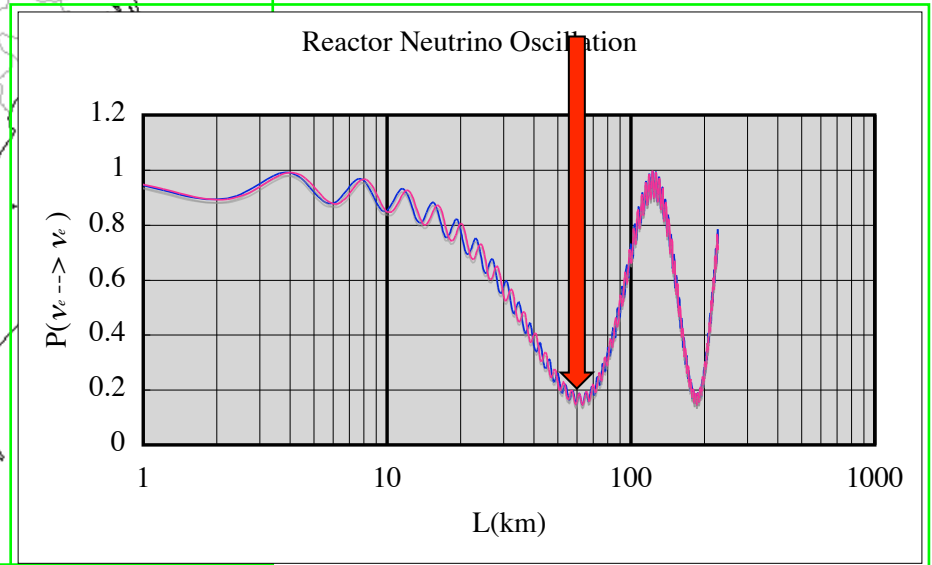
T2K & Nova expected $\delta|\Delta m_{23}^2|/|\Delta m_{23}^2| \sim 4\%$ \longrightarrow Need to improve
 θ_{13} is necessary to evaluate $\delta|\Delta m_{13}^2|$ (KamLAND case; $\delta|\Delta m_{12}^2|/|\Delta m_{12}^2| \sim 2.6\%$)

Physics @ 1st Δm^2_{12} Maximum ($L \sim 50\text{km}$)

(Very Precise θ_{12} & Mass Hierarchy)

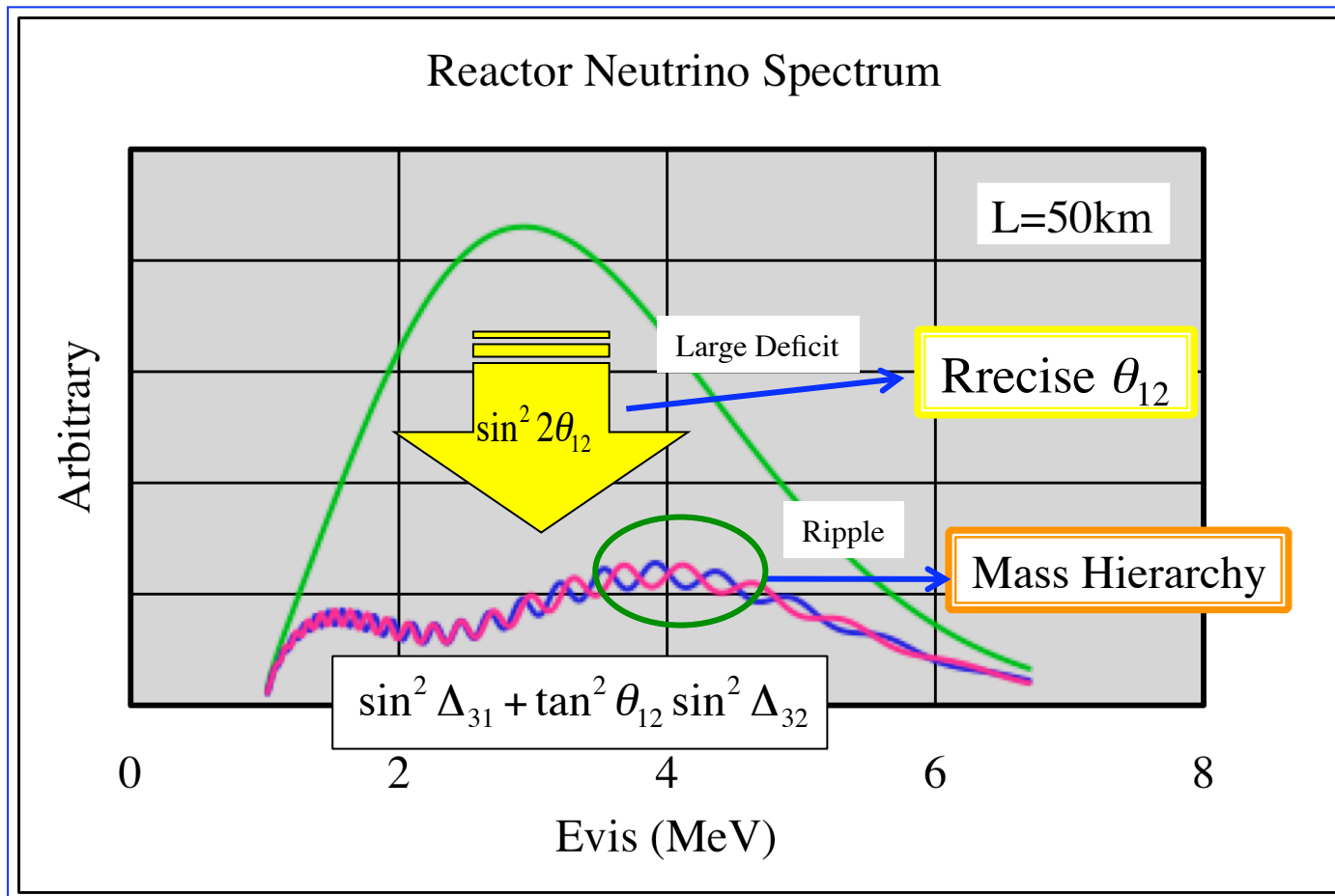


Example of Japan case



Physics @ 1st Δm^2_{12} Maximum

$$P_R(\bar{\nu}_e \rightarrow \bar{\nu}_e) = 1 - \left\{ \begin{array}{l} \cos^4 \theta_{13} \sin^2 2\theta_{12} \sin^2 \Delta_{21} \\ + \sin^2 2\theta_{13} \cos^2 \theta_{12} (\sin^2 \Delta_{31} + \tan^2 \theta_{12} \sin^2 \Delta_{32}) \end{array} \right\}$$



Precise θ_{12}

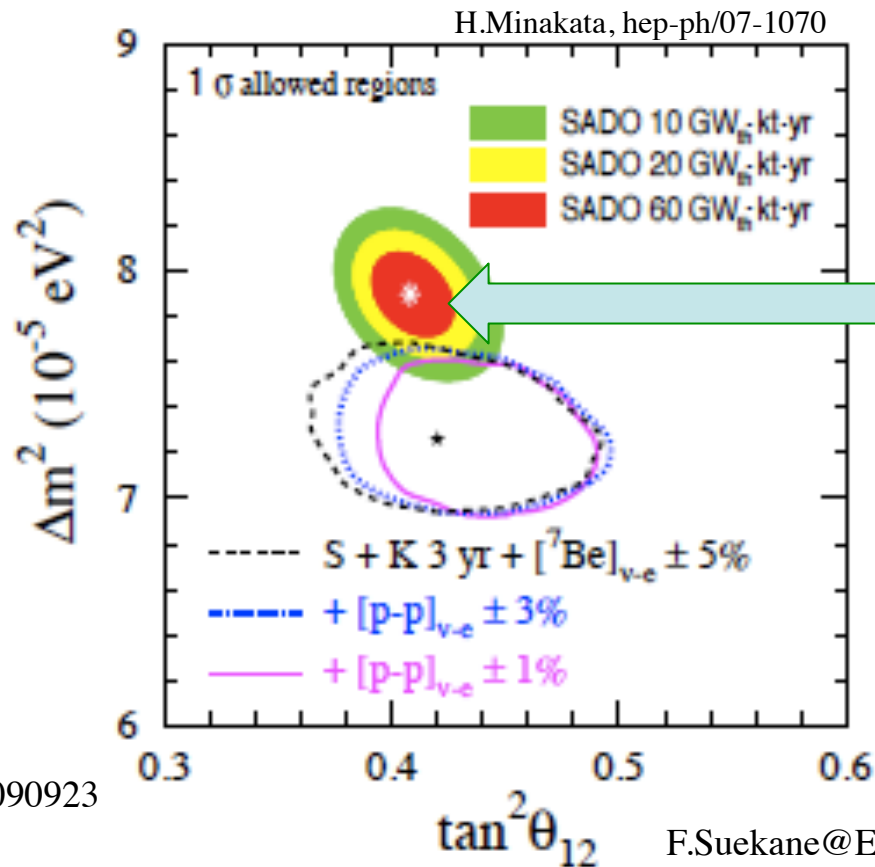
$$P(\bar{\nu}_e \rightarrow \bar{\nu}_e) \sim \cos^4 \theta_{13} \left(1 - \sin^2 2\theta_{12} \sin^2 \Delta_{21} \right)$$

$$\delta \sin^2 2\theta_{12} \propto \frac{1}{\Lambda(L)}, \quad \Lambda = \text{Deficit probability};$$

$$\Lambda(L) = \frac{\int f_\nu(E) \sin^2 \Delta_{21} dE}{\int f_\nu(E) dE}$$

$$\left. \begin{array}{l} \Lambda(50\text{km}) \sim 0.8 \\ \Lambda(180\text{km}) \sim 0.4 \text{ (KamLAND)} \end{array} \right\} \Rightarrow \delta \sin^2 2\theta_{12} \sim \frac{1}{2} (\delta \sin^2 2\theta_{12})_{\text{KamLAND}}$$

& Low geo neutrino BKG
(high ν flux)



$$\frac{\delta \sin^2 \theta_{12}}{\sin^2 \theta_{12}} \sim 2.4\% (1\sigma)$$

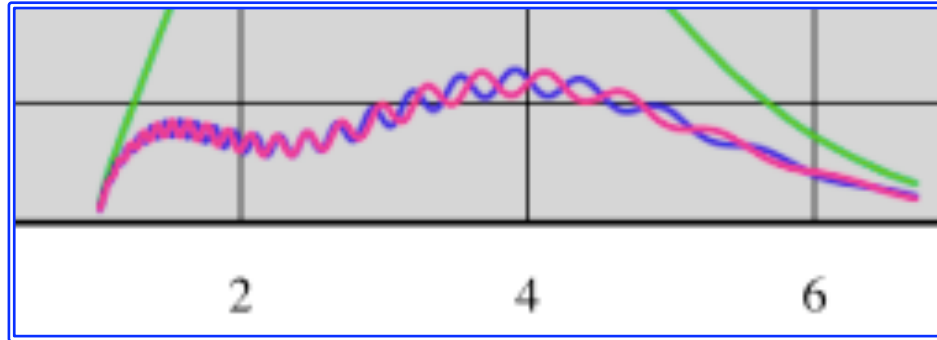
Current Global fit

$$\frac{\delta \sin^2 \theta_{12}}{\sin^2 \theta_{12}} \sim 6.3\% (1\sigma)$$

Determination of Mass Hierarchy @ 50km

Principle

Petcov et al., Phys. Lett. B 533, 94 (2002)
 S.Choubey et al., Phys. Rev. D 68,113006 (2003)
 J. Learned et al., hep-ex/062022
 L.Zhan et al., hep-ex/0807.3203
 M.Batygov et al., hep-ex/0810.2508

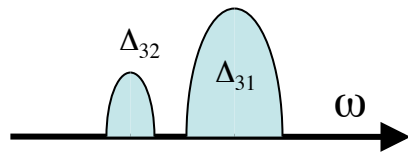


$$\text{Ripple} \propto \sin^2 2\theta_{13} \left(\sin^2 \Delta_{31} + \tan^2 \theta_{12} \sin^2 \Delta_{32} \right)$$

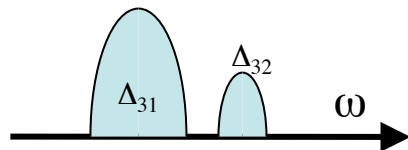
It is essential that θ_{12} is not maximum ($\tan^2 \theta_{12} \sim 0.4$)

Fourier Analysis \Rightarrow Power Spectrum Peaks at $\omega = |\Delta m_{31}^2|, |\Delta m_{32}^2|$

The smaller peak is $|\Delta m_{32}^2|$ and larger peak is $|\Delta m_{31}^2|$,



$$\Rightarrow |\Delta m_{31}^2| > |\Delta m_{32}^2| \quad : \text{Normal Hierarchy}$$



$$\Rightarrow |\Delta m_{31}^2| < |\Delta m_{32}^2| \quad : \text{Inverted Hierarchy}$$

J.Learned et al. arXive-0612022

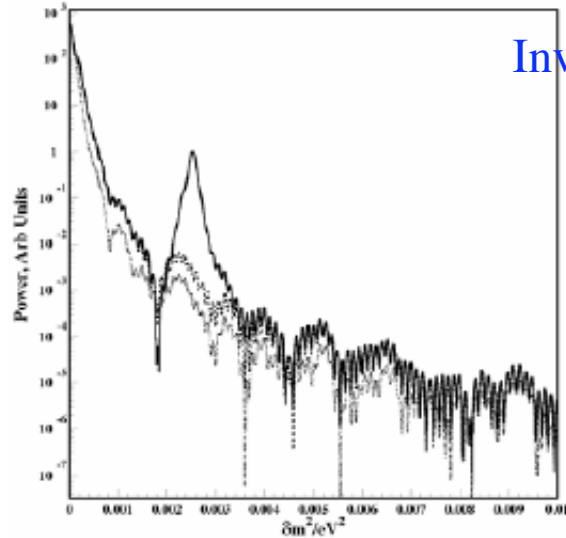
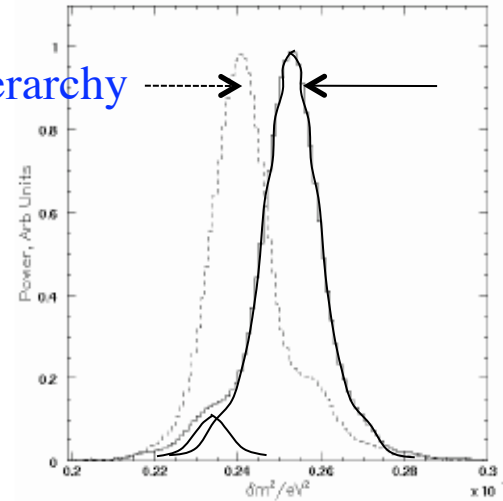


FIG. 2: Fourier power spectrum with modulation in units of eV^2 and power in arbitrary units on the logarithmic scale. The peak due to Δ_{31} with $\sin^2(2\theta_{13})=0.1$ is prominent.

Inverted Hierarchy



Normal Hierarchy

FIG. 3: Neutrino mass hierarchy (normal=solid; inverted=dashed) is determined by the position of the small shoulder on the main peak.

Simulation of power spectrum

If $\sin^2 2\theta_{13}=0.05$, **3kton x24GW x5yr**,

Mass Hierarchy can be determined with 1σ significance.

L.Zhan et al.=> Mass Hierarchy could be determined if $\sin^2 2\theta_{13}>0.005$.

Merit & Issues of this method.

* Need not to know absolute $|m_{23}^2|$ so precisely.
It is enough only to separate two peak positions.

* However, a good energy resolution; $\frac{\delta E}{E} < \frac{3\%}{\sqrt{E(\text{MeV})}}$ is necessary.

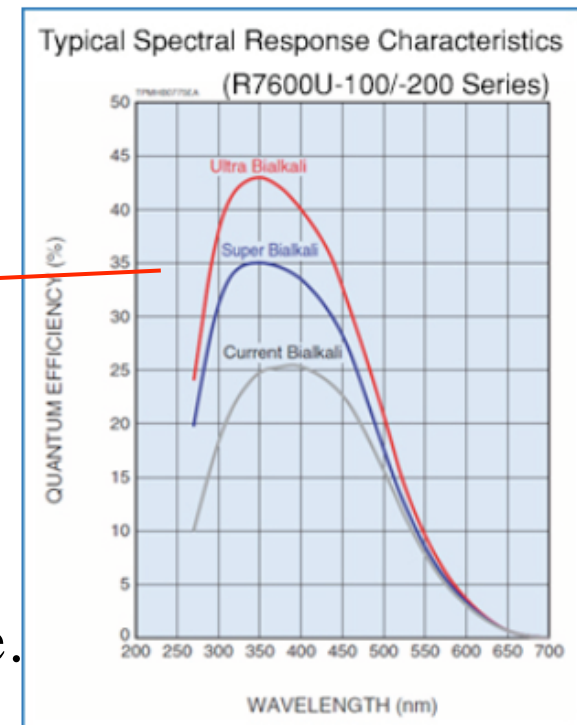
Borexino case $\frac{\delta E}{E} \sim \frac{5\%}{\sqrt{E(\text{MeV})}}$

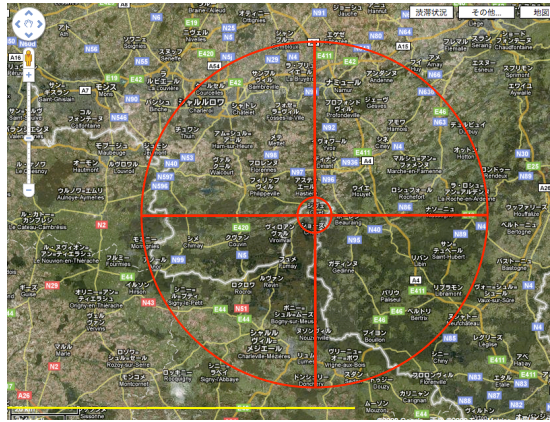
improvement of light yield:
x1.5 more PMT
x1.8 with UltraBialkali photocathode

$\Rightarrow \frac{\delta E}{E} = \frac{3\%}{\sqrt{E(\text{MeV})}}$ can be achieved

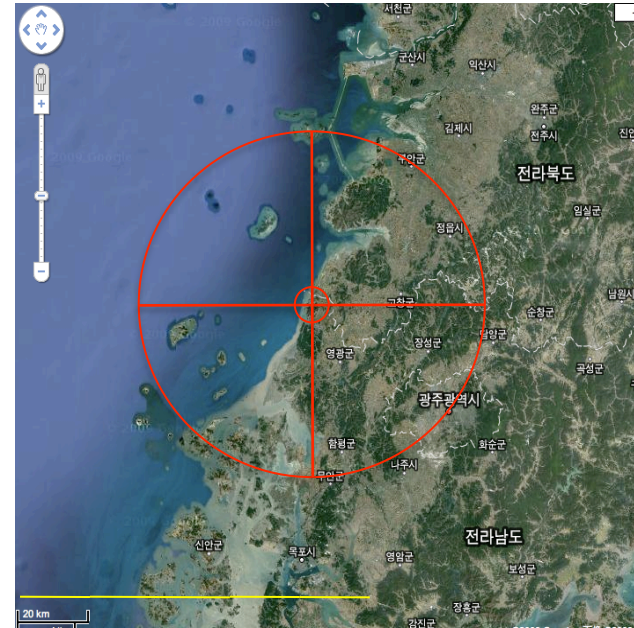
* Energy smearing due to recoil neutron energy & baseline difference may degrade performance.

\Rightarrow Need more studies for specific sites

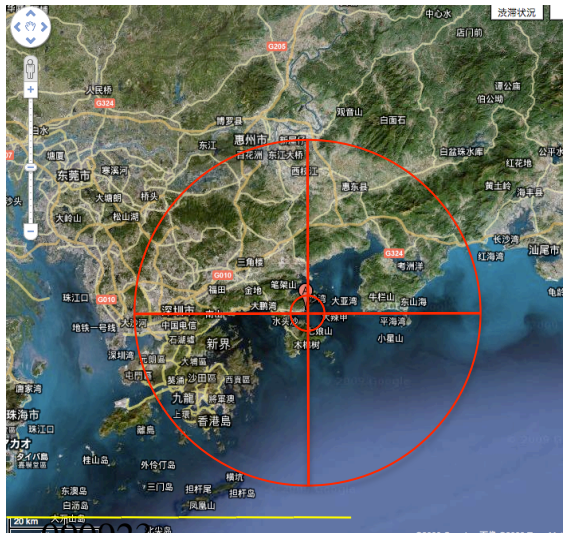




DoubleChooz-50



RENO-50



090923
DayaBay-50

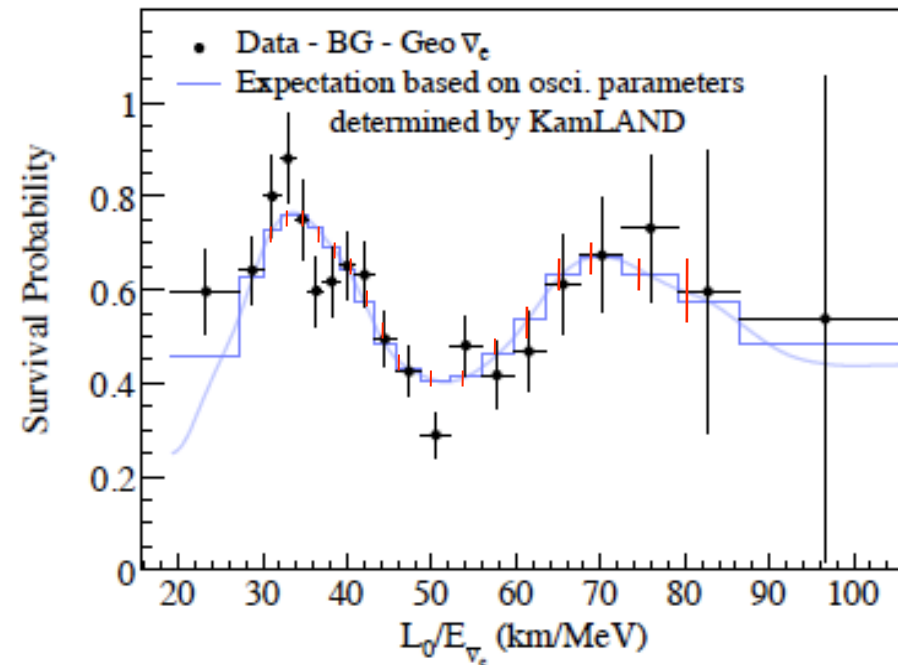
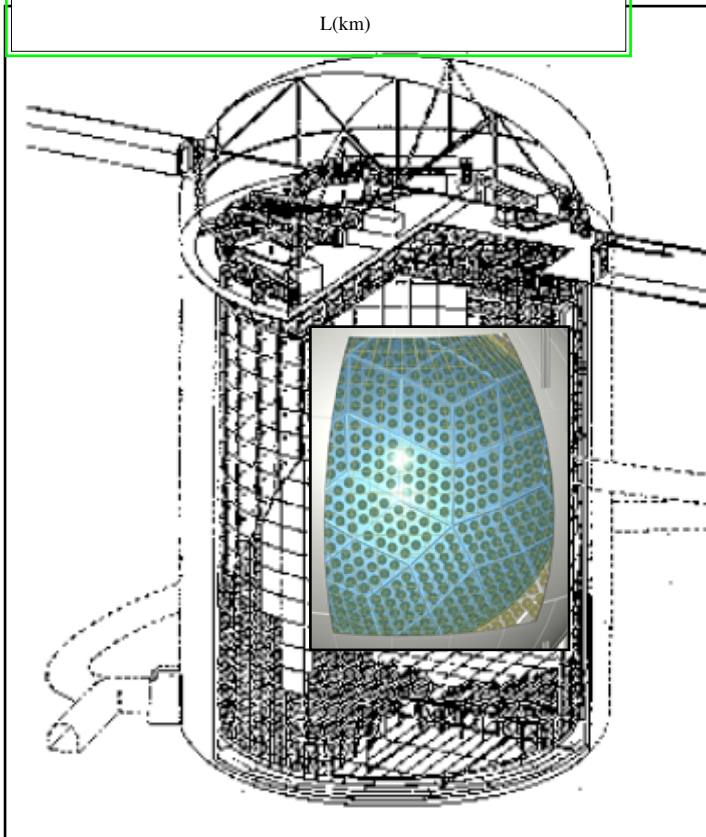
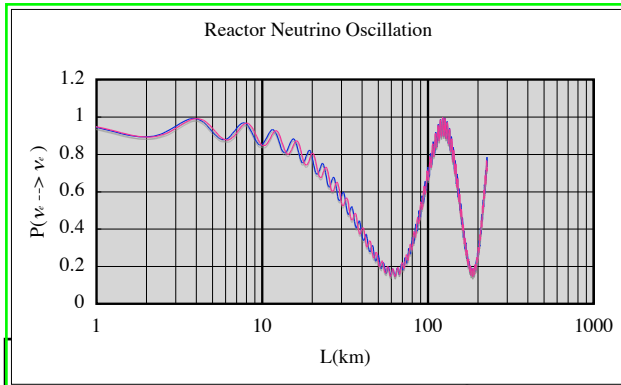
L~50km experiment may be a natural extension of current Reactor- θ_{13} Experiments

- * θ_{13} detectors can be used as near detector
- * Small background from other reactors.

Physics @ Δm^2_{12} 2nd Maximum (L~150km)

If SK detector is filled with LS,

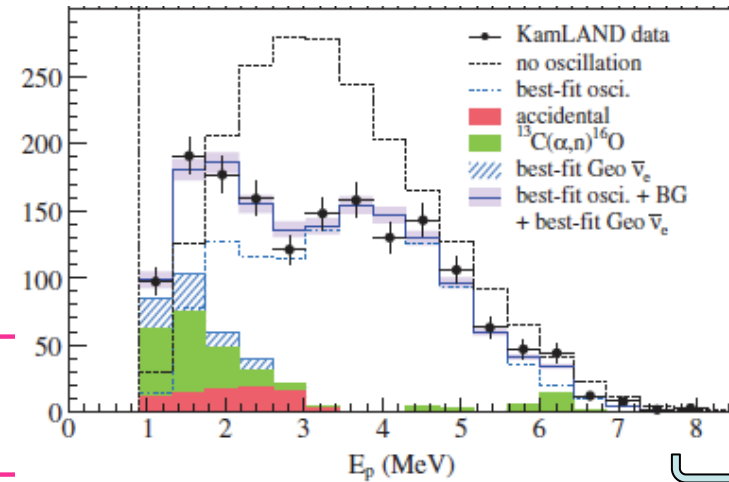
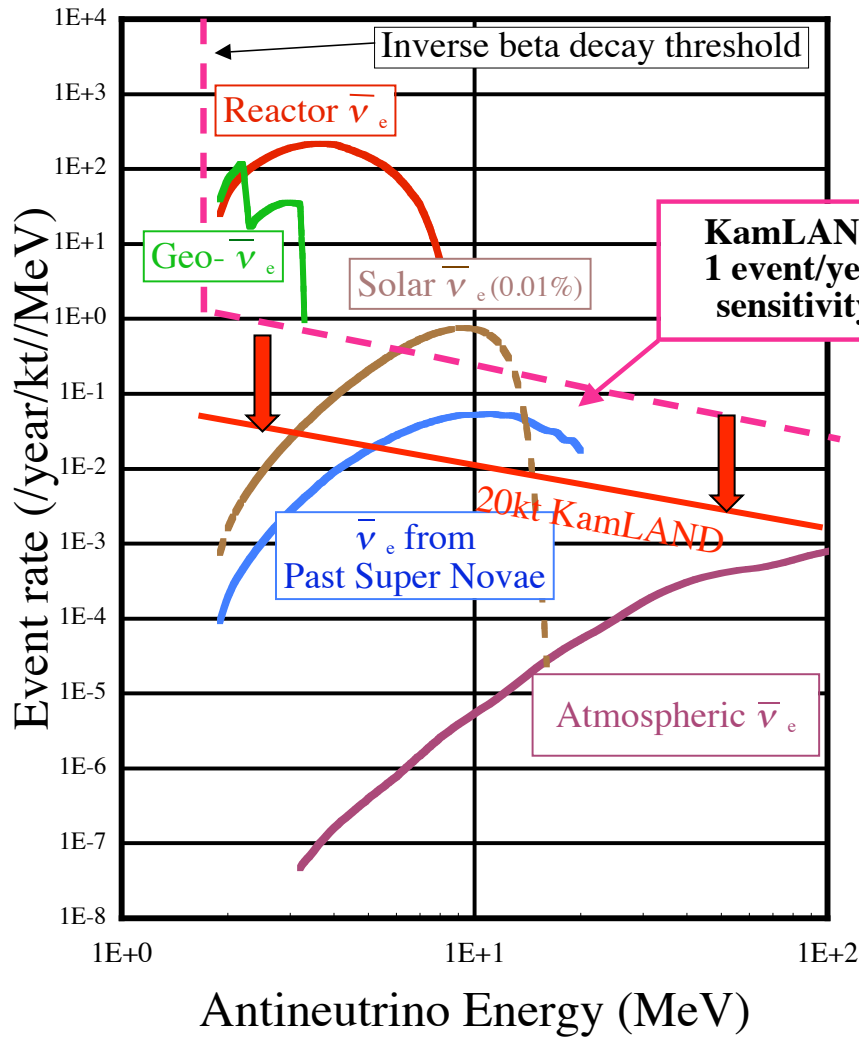
>20 times more statistics
than KamLAND



$$\left\{ \begin{array}{l} \Delta m^2_{21} = 7.58^{+0.14}_{-0.13} (\text{stat})^{+0.15}_{-0.15} (\text{syst}) \Rightarrow 7.58^{+0.03}_{-0.03} (\text{stat})^{+0.15}_{-0.15} (\text{syst}) \\ \tan^2 \theta_{12} = 0.56^{+0.10}_{-0.07} (\text{stat})^{+0.10}_{-0.06} (\text{syst}) \Rightarrow 0.56^{+0.2}_{-0.014} (\text{stat})^{+0.10}_{-0.06} (\text{syst}) \end{array} \right.$$

$$f_\nu(E_\nu) \times \sigma_{\bar{\nu}_p \rightarrow e^+ n}(E_\nu)$$

Electron Antineutrino Event Rate at Kamioka



No Backgrounds >8MeV

KamLAND detects any $\bar{\nu}_e$ with $E > 1.8 \text{ MeV}$

20Kton KamLAND pushes the limit 20 times better and may reach Relic SN $\bar{\nu}_e$.

Summary

= Current =

θ_{13} : DoubleChooz, RENO, Dayabay are going to start in 2010.

$\delta\sin^2 2\theta_{13}=0.01\sim 0.03$ in a few years.

= Future =

* $L\sim 1.8\text{km}$, High Precision θ_{13} ;

$M\sim 100\text{ton} \times 24\text{GW}_{\text{th}} \Rightarrow \delta\sin^2 2\theta_{13}<0.01$

→ θ_{23} Degeneracy with accelerator

→ early $\sin\delta$ detection with accelerator

* $L=50\text{km}$, $M\sim 3\text{Kton} \times 24\text{GW}_{\text{th}}$,

→ High Precision θ_{12} ;

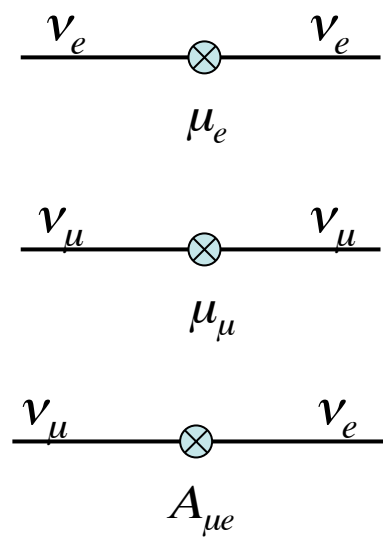
→ Mass hierarchy determination

* $L=180\text{km}$ 20Kton KamLAND???

It is important to discuss about the future strategy taking into account the reactor-accelerator complementarity after the 1st phase θ_{13} measurements.

Back up slides

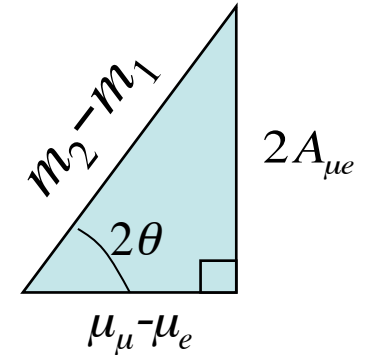
Relation of mass, mixing & transition amplitudes



$$\begin{cases} m_1 = \frac{1}{2} \left(\mu_\mu + \mu_e - \sqrt{(\mu_\mu - \mu_e)^2 + 4A_{\mu e}^2} \right) \\ m_2 = \frac{1}{2} \left(\mu_\mu + \mu_e + \sqrt{(\mu_\mu - \mu_e)^2 + 4A_{\mu e}^2} \right) \end{cases}$$

$$\tan 2\theta = \frac{2A_{\mu e}}{\mu_\mu - \mu_e}$$

$$\Delta m^2 = (\mu_\mu + \mu_e) \sqrt{(\mu_\mu - \mu_e)^2 + 4A_{\mu e}^2}$$



$$P_{Accel}(\nu_\mu \rightarrow \nu_e) \oplus P_{Accel}(\bar{\nu}_\mu \rightarrow \bar{\nu}_e) \oplus P_{Reactor}(\bar{\nu}_e \rightarrow \bar{\nu}_e)$$

Reactor θ_{13} helps to pin down parameters

