

Fundamental Constants
and their
Time Variation

Harald Fritzsch
LMU Munich

fundamental constants

the

problem of

modern science

Fritzschn

fundamental constants =>

particle

physics

nuclear

...

atomic

...

laser

...

solid state

...

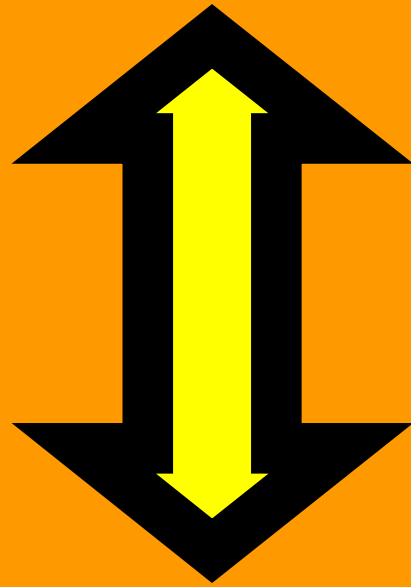
astro

...

cosmology

**==> chemistry,
biology, ...**

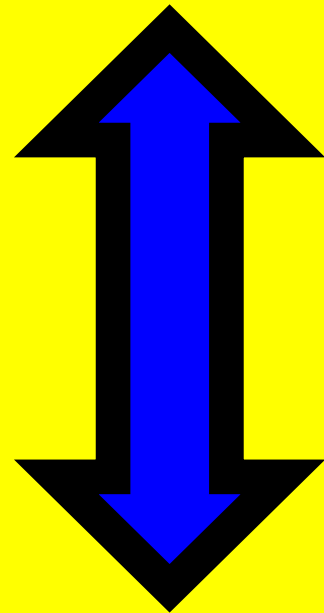
Fundamental constants



Standard Model

Fritzsch

Standard Model



gauge theories

Fritzsch

first gauge theory



Heisenberg

Pauli

Feynman

Schwinger

QED

Fritzsche

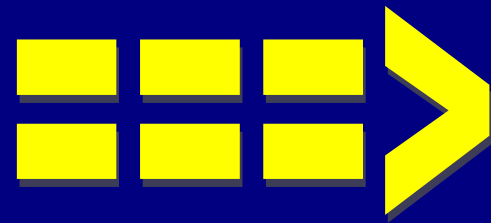
QED

2 fundamental constants

α

m_e

1964



electroweak
gauge theory

$U(1) \times SU(2)$

gauge theory
of the

**Strong
Interactions**



M. Gell-Mann



G. Zweig

1964

quarks

Fritzsch

**(p
n)**



**(u
d
s)**

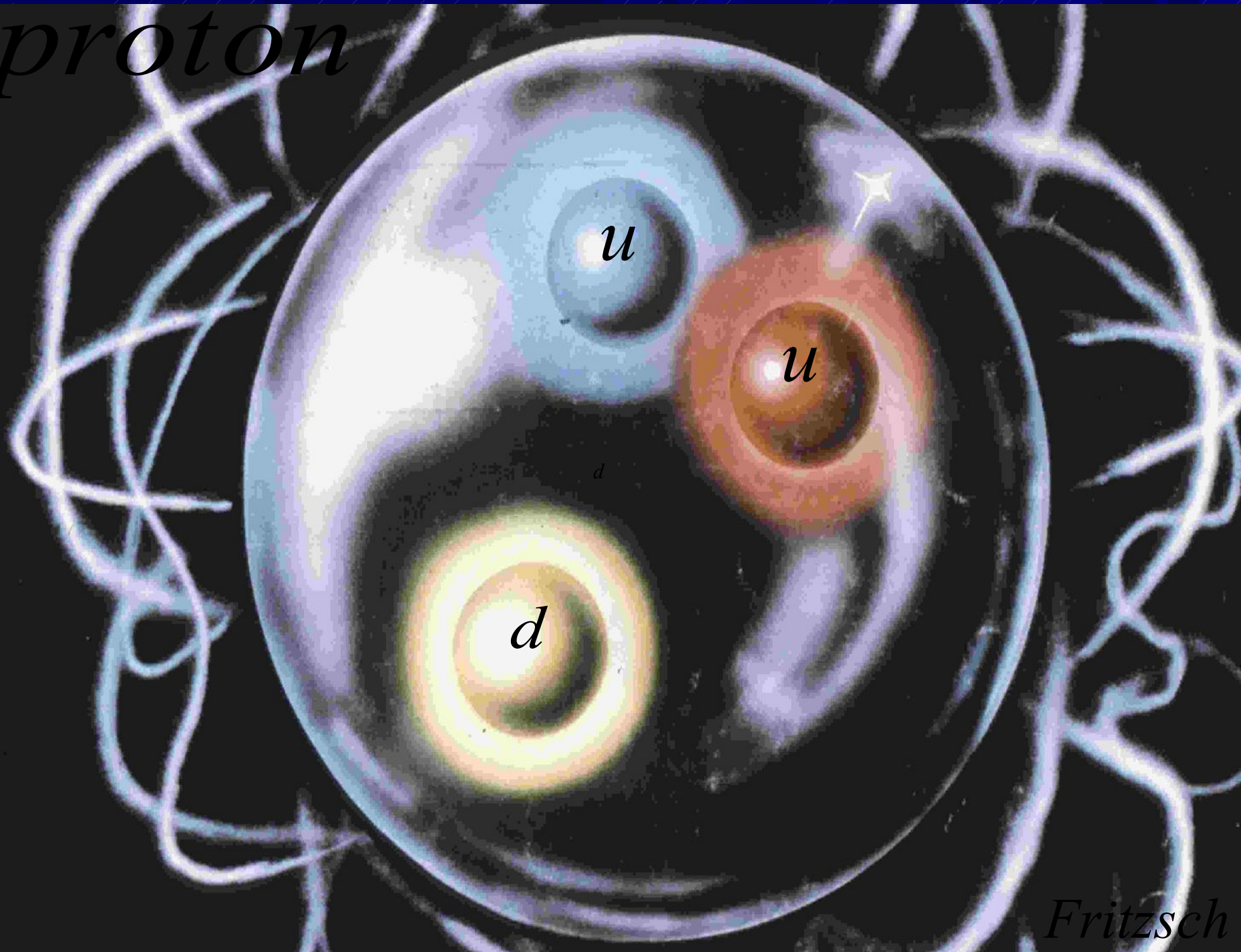
electric charge:

$$u : \frac{2}{3}e$$

$$d : -\frac{1}{3}e$$

$$s : -\frac{1}{3}e$$

proton



Fritzsch

1971

color

$q \Rightarrow \lambda$

q

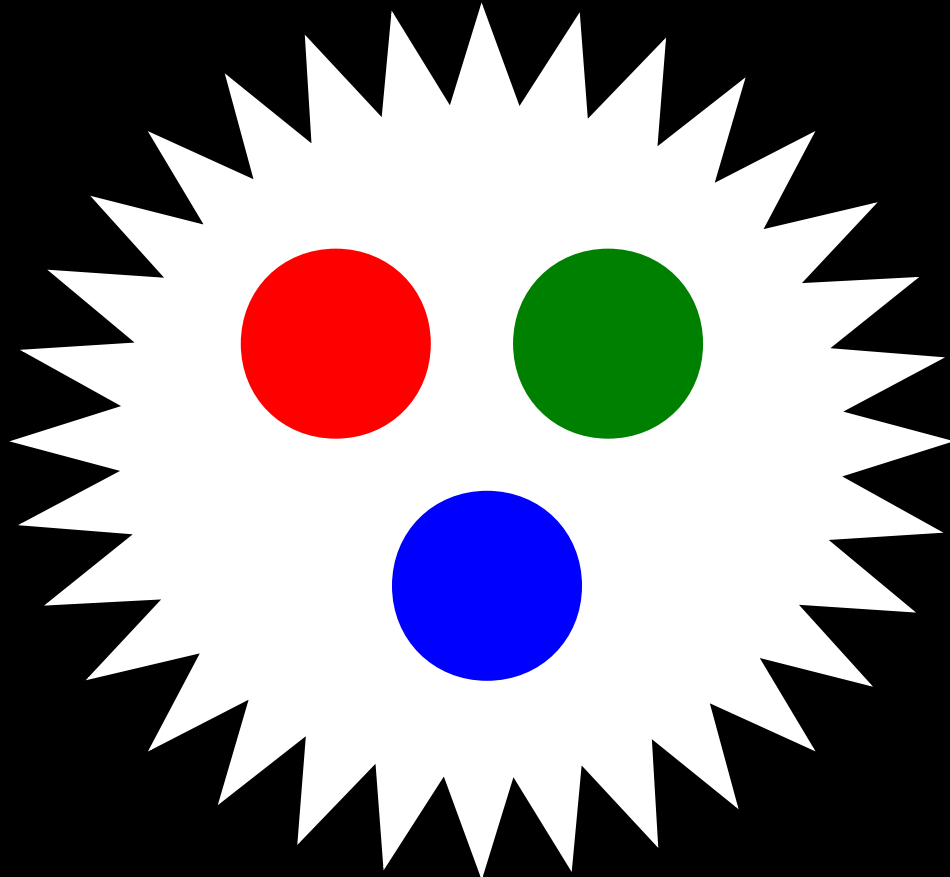
q

q

$SU(3, c)$

- Hadrons -

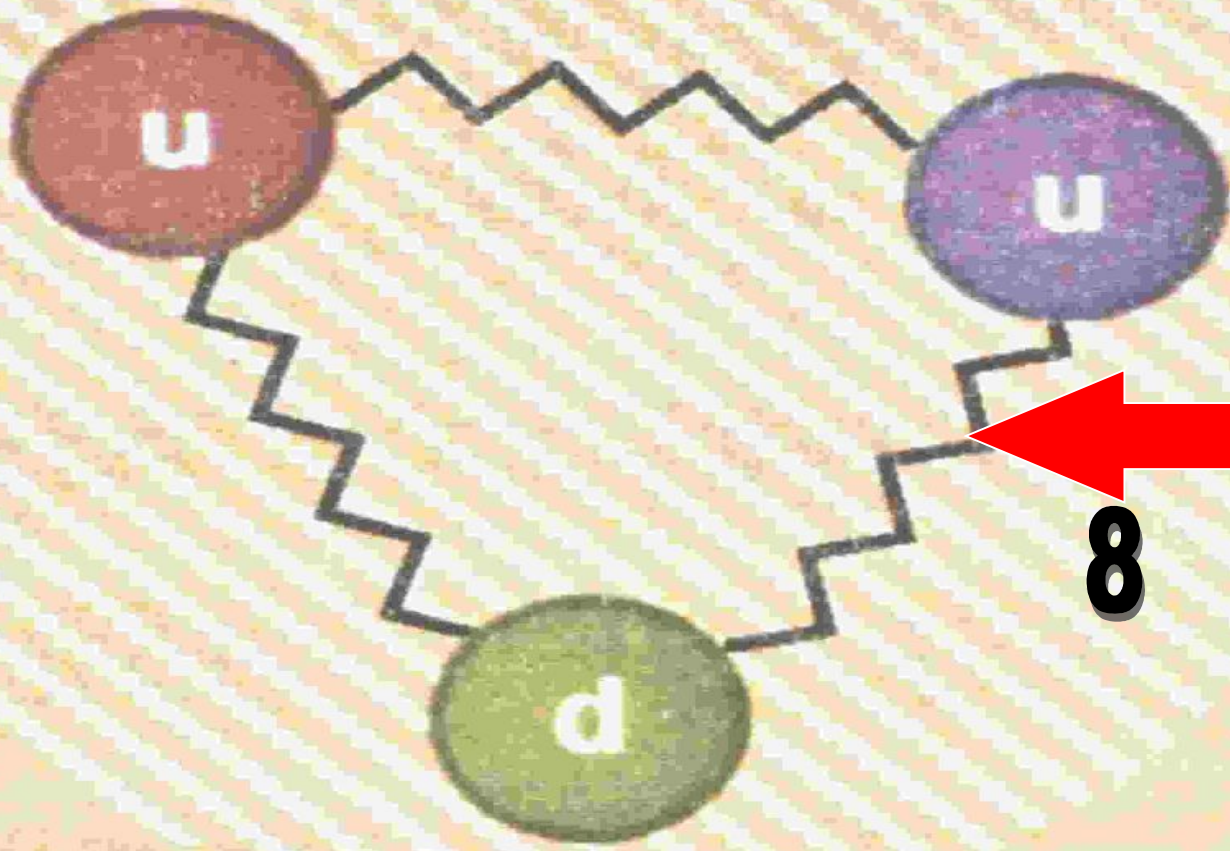
white states



1971 - 1972

QCD

Fritzsch & Gell-Mann



8 gluons

Proton

1973:

Standard Model

$SU(3) \times SU(2) \times U(1)$

2 \Rightarrow 28

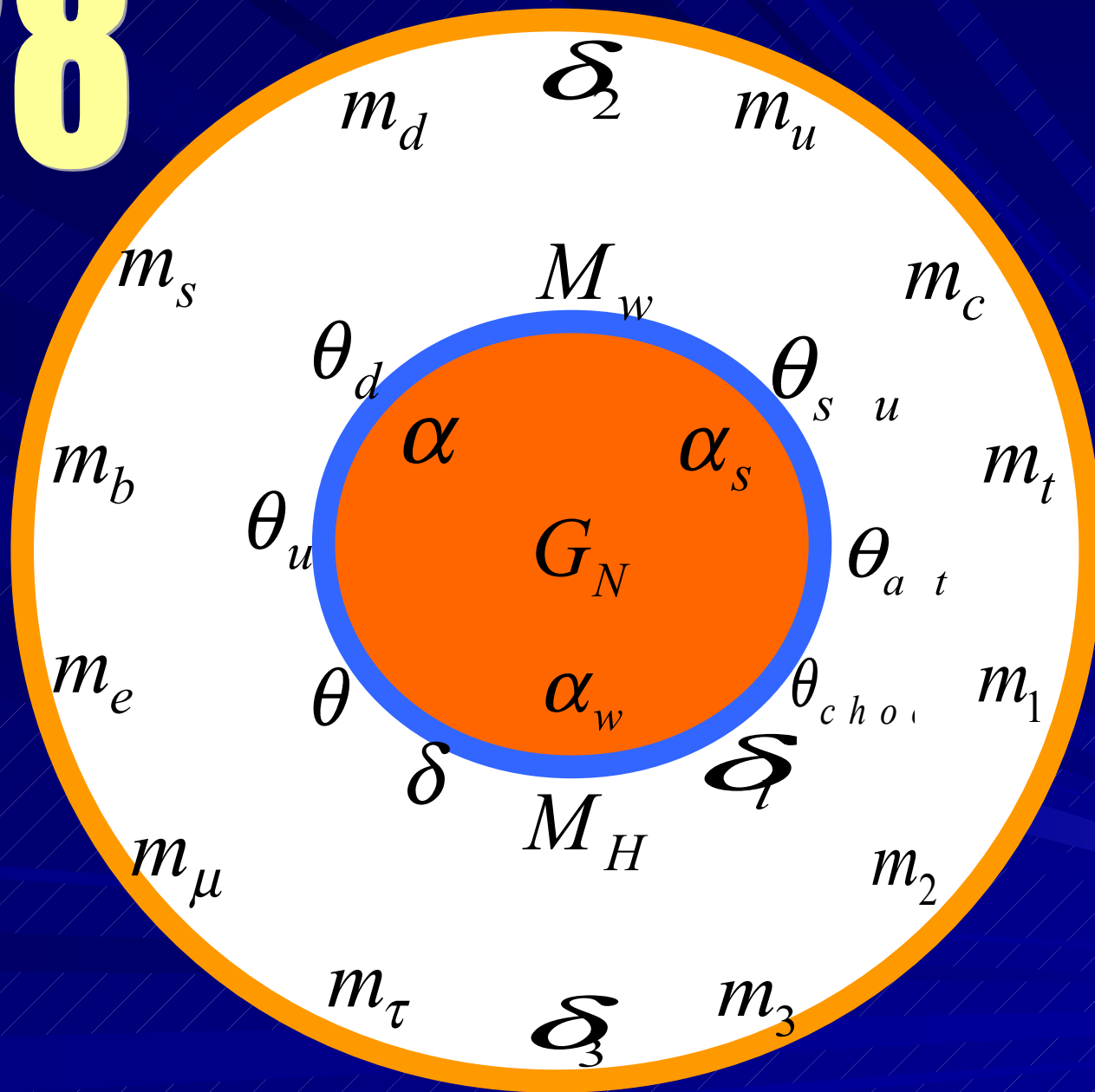
=== > problem

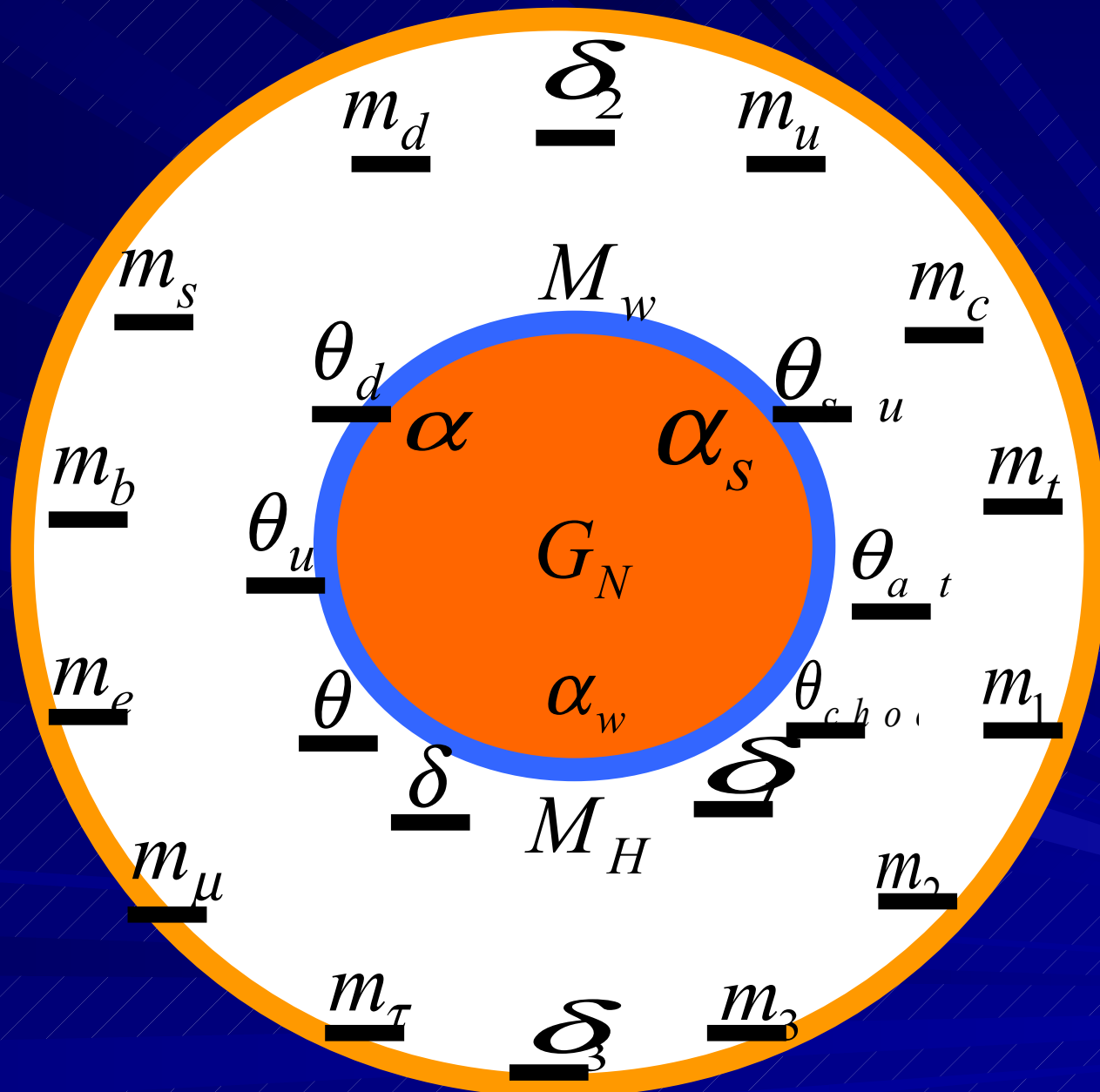
28

**fundamental
constants**

Newton's constant G	1
fine structure constant	1
coupling constant of strong interaction	1
coupling constant of weak interaction	1
mass of W boson	1
mass of Higgs boson	1
masses of 6 quarks and 6 leptons	12
flavor mixing of quarks	4
flavor mixing of leptons	

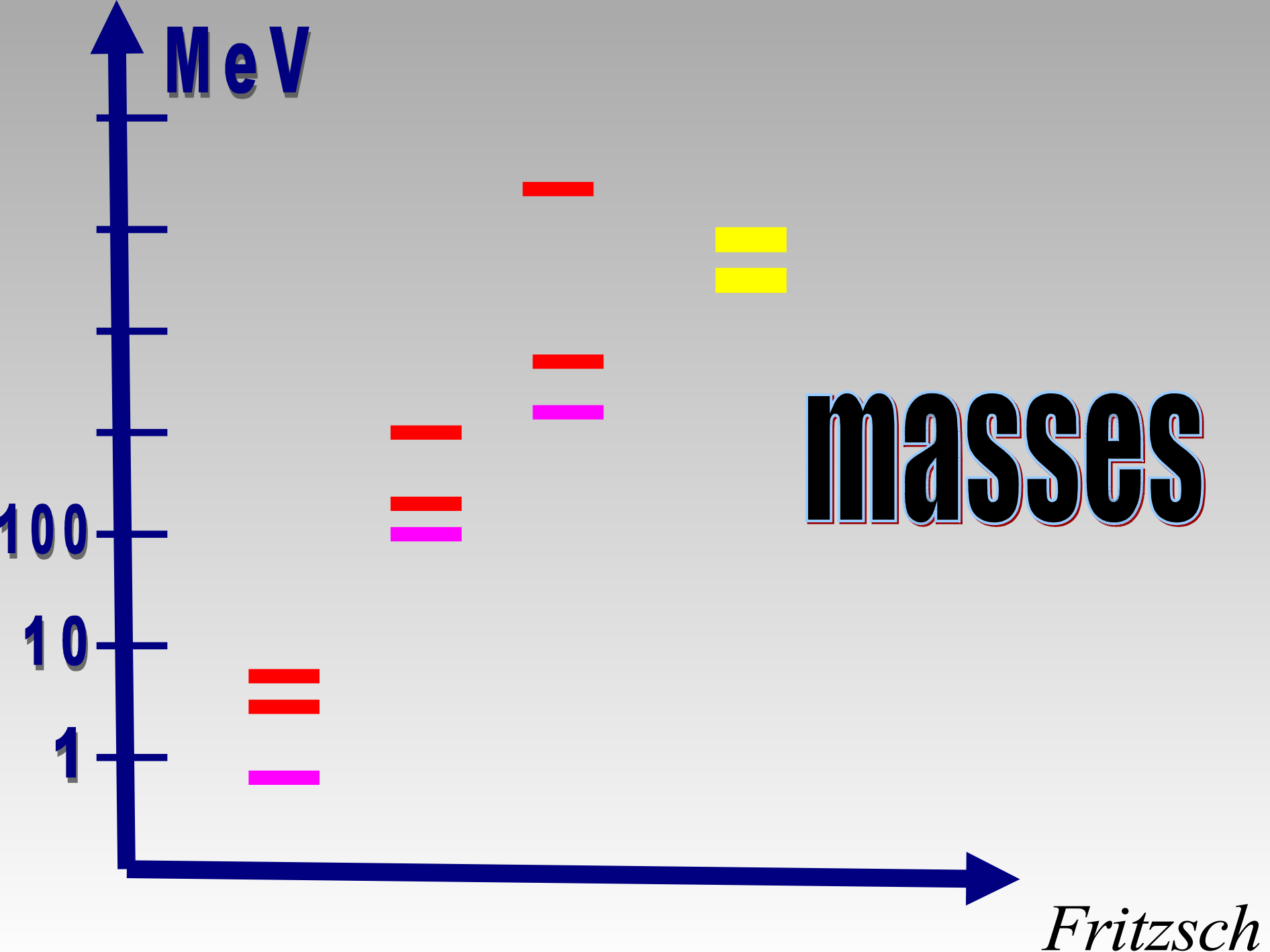
28





(22 related to fermion masses)

Fritzsch



Arnold *Sommerfeld*, 1916

**fine-structure
constant**

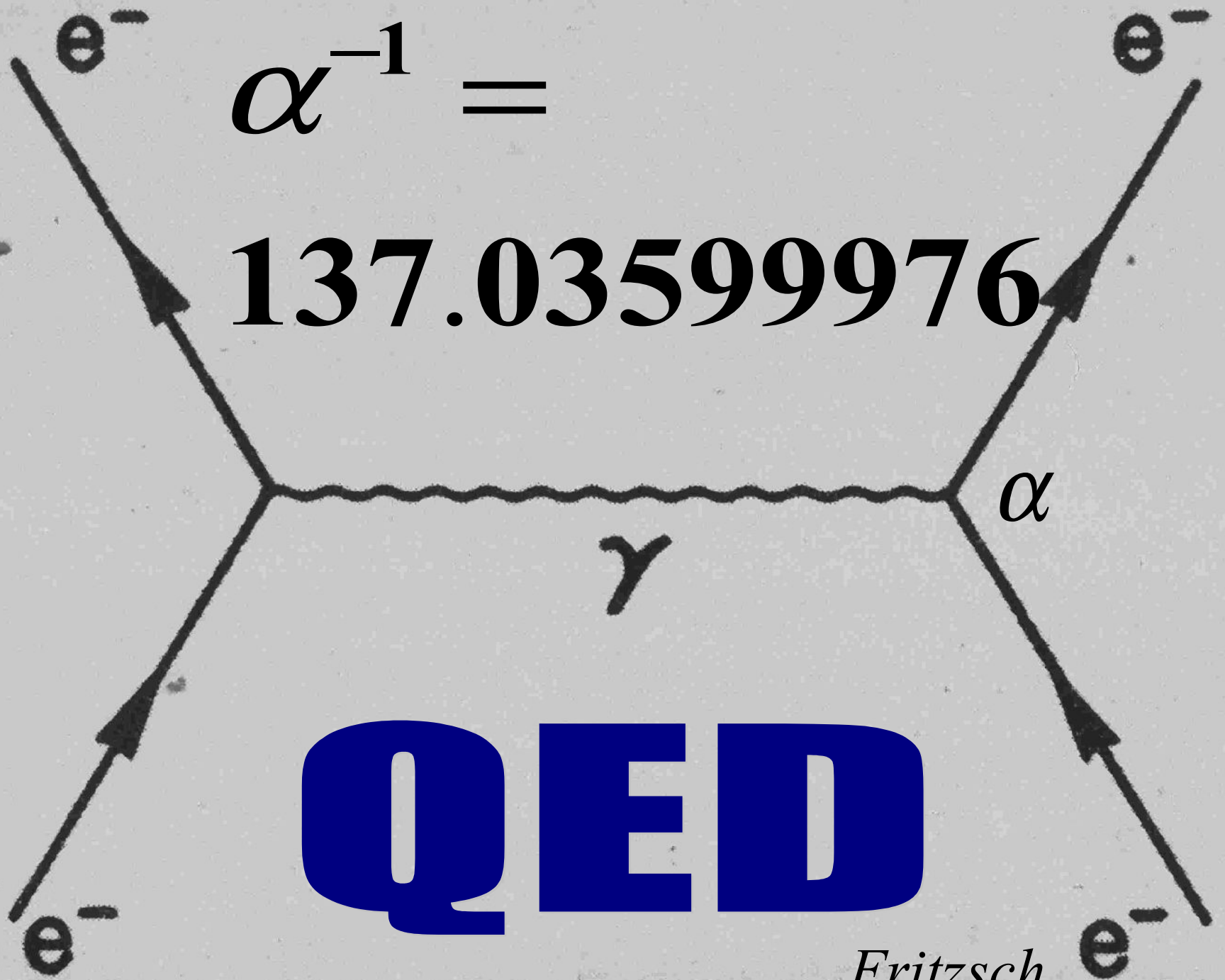
$$\alpha = e^2 2\pi / hc$$



Fritzsch

$$\alpha = \frac{e^2}{\hbar c} \approx \frac{1}{137}$$

***electrodynamics +
relativity +
quantum theory***



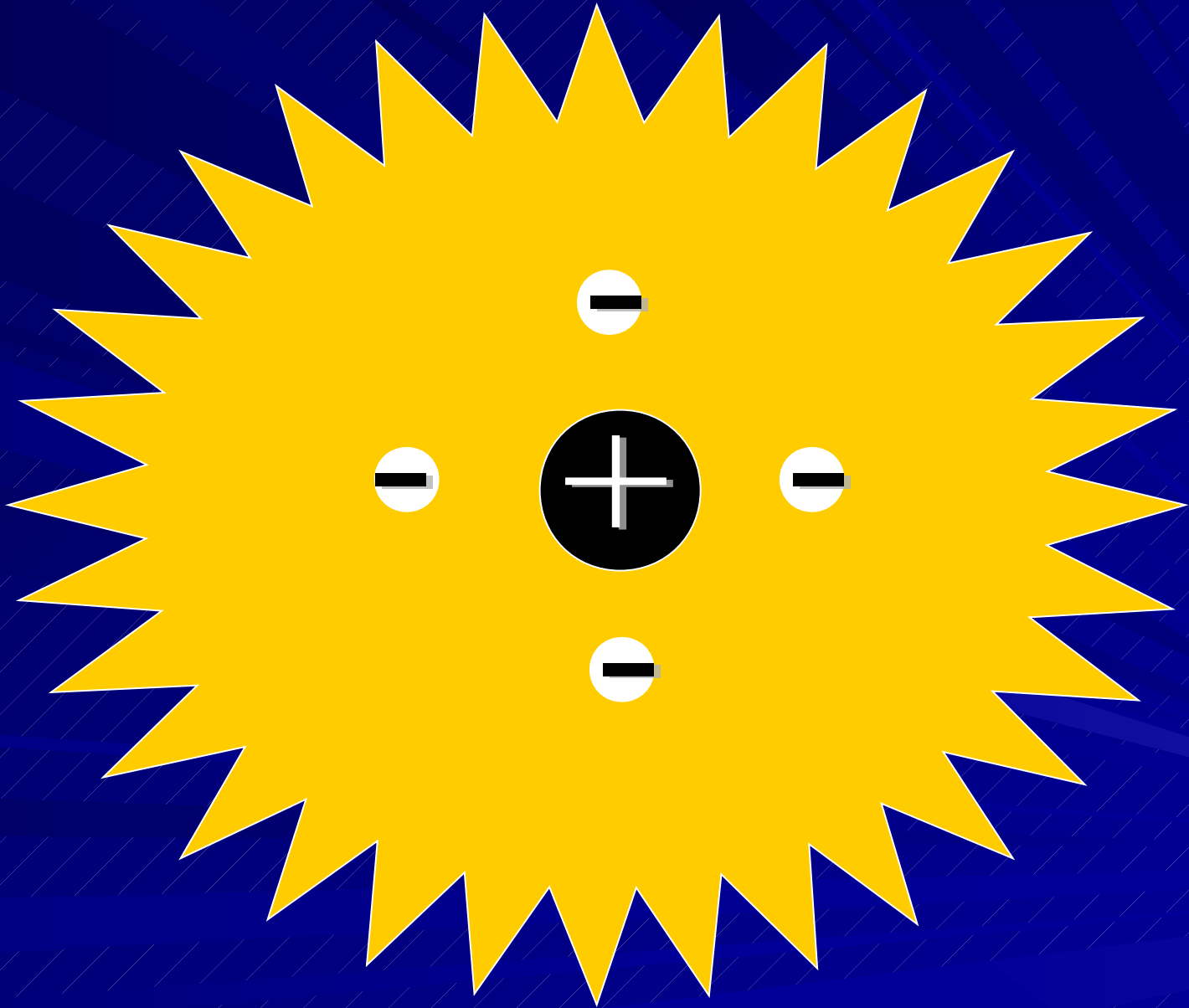
$$\alpha^{-1} =$$

137.03599976

QED

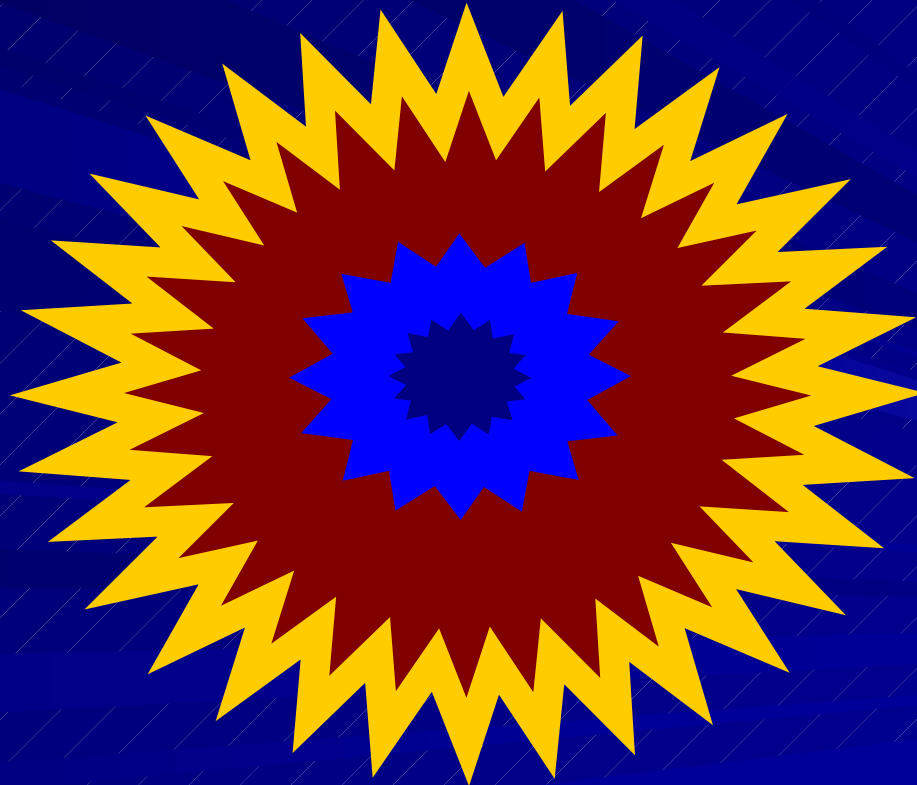
Fritzsche

partial screening



**fine-structure
constant ==>**

function of energy



$$\alpha(\gamma, G, e)$$

$$\text{LEP: } \sim 1/127$$

$$\alpha(M_Z) \neq \frac{1}{127}$$

nucleon mass

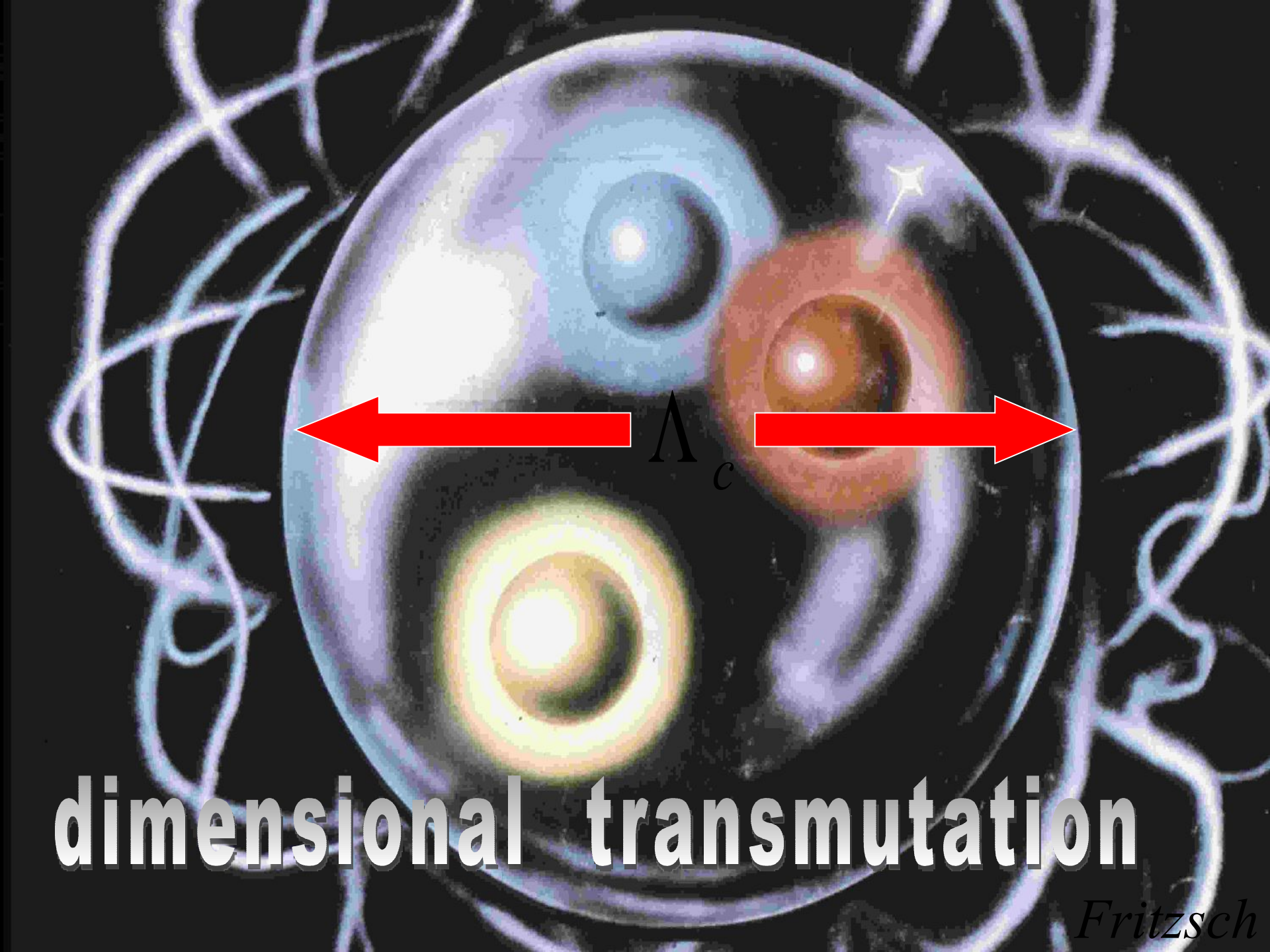
fundamental constant?

⇒ QCD

quark masses $\implies 0$

$$M_p = E(\text{gluons, quarks}) / c^2$$

mass \Leftrightarrow field energy



dimensional transmutation

Fritzsch

nucleon mass

(quark masses $\Rightarrow 0 =$

$$M = \text{const.} \cdot \Lambda_c$$

Experiments:

$$\Lambda_c \sim 250 \text{ MeV}$$

mass \Leftrightarrow confined field energy

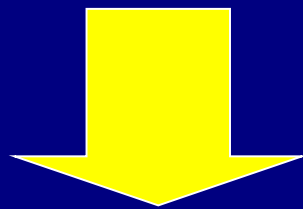
real world:

$$M_n = c_u \Lambda \left(\frac{m_d}{c_d} + \frac{m_s}{c_s} \right) + c_e \Lambda \left(\frac{m_l}{c_l} + \frac{m_m}{c_m} \right)$$

$$M(\text{proton}) = \begin{matrix} \text{QCD} & u & d & s & \text{QED} \\ 860 & + 21 & + 19 & + 36 & + 2 \end{matrix}$$

Standard Model:

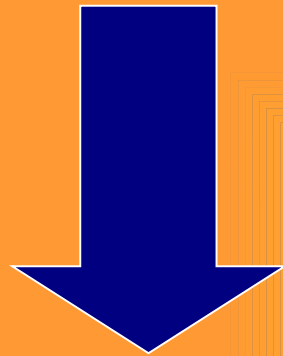
*fundamental constants
in our universe*



universal

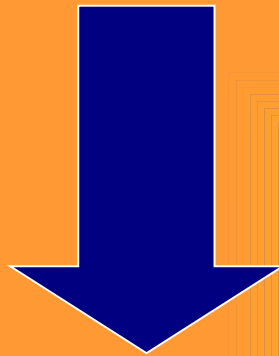
**Are the fundamental
constants
functions of time
and space?**

α :



function of energy

α :



? function of time?

Oklo Phenomenon

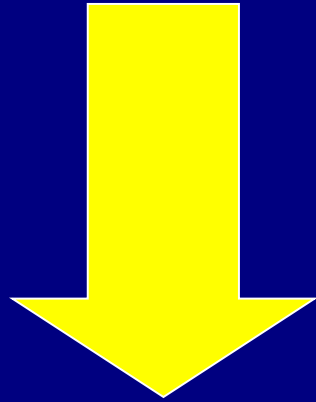
About 1.8 billion years ago, in Gabon, Westafrika.

Natural Reactor, which operated about 100 million years.

**High concentration of uranium
3.7% U 235 at that time (today 0.72 %)**

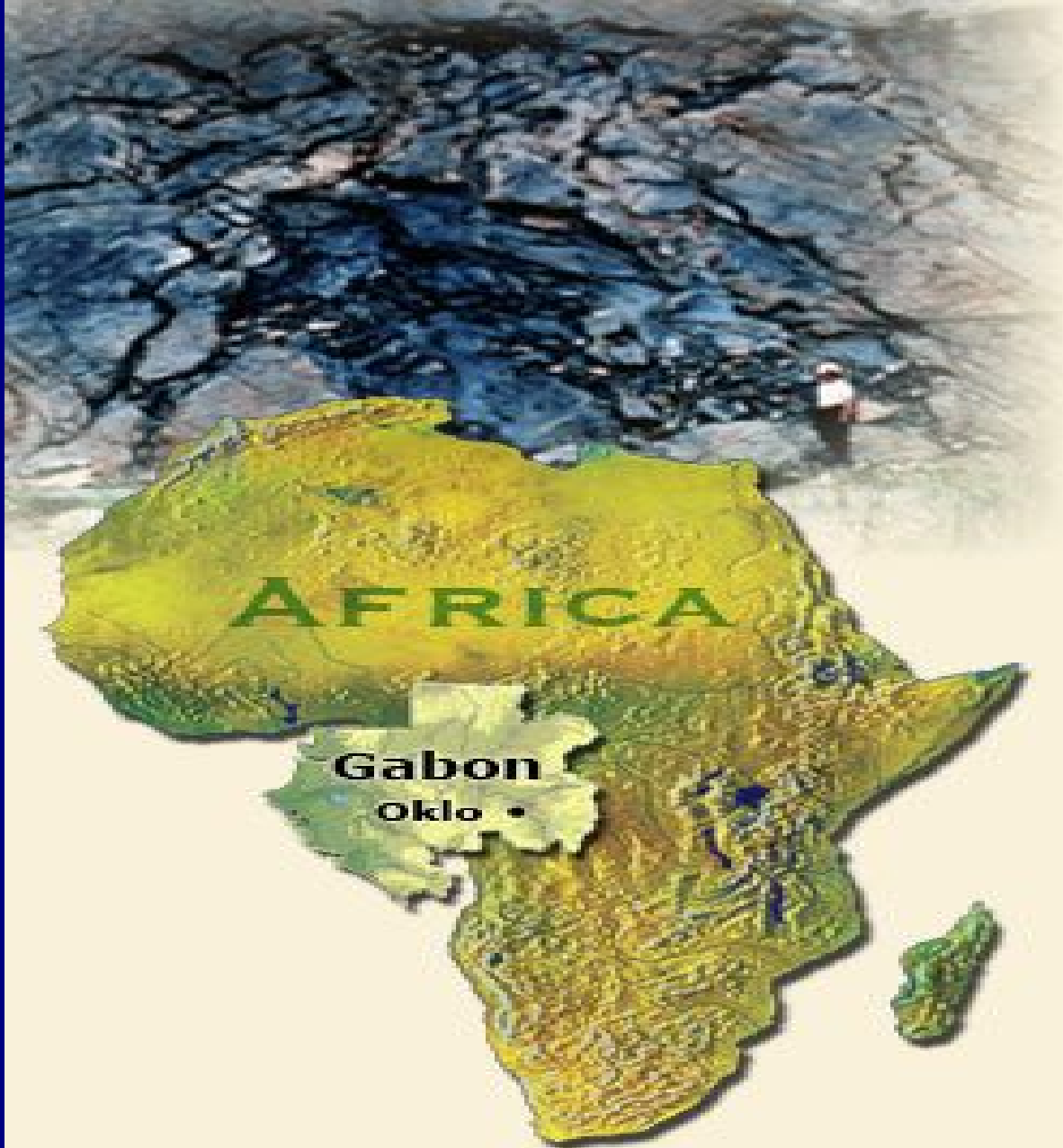
Moderator: water from river Oklo

discovery: 1972



Natural reactor

(output: ~ 100 kw)



The uranium isotopes found at Oklo strongly resemble those in the spent nuclear fuel generated by today's nuclear power plants.

Fritzschn



Libreville

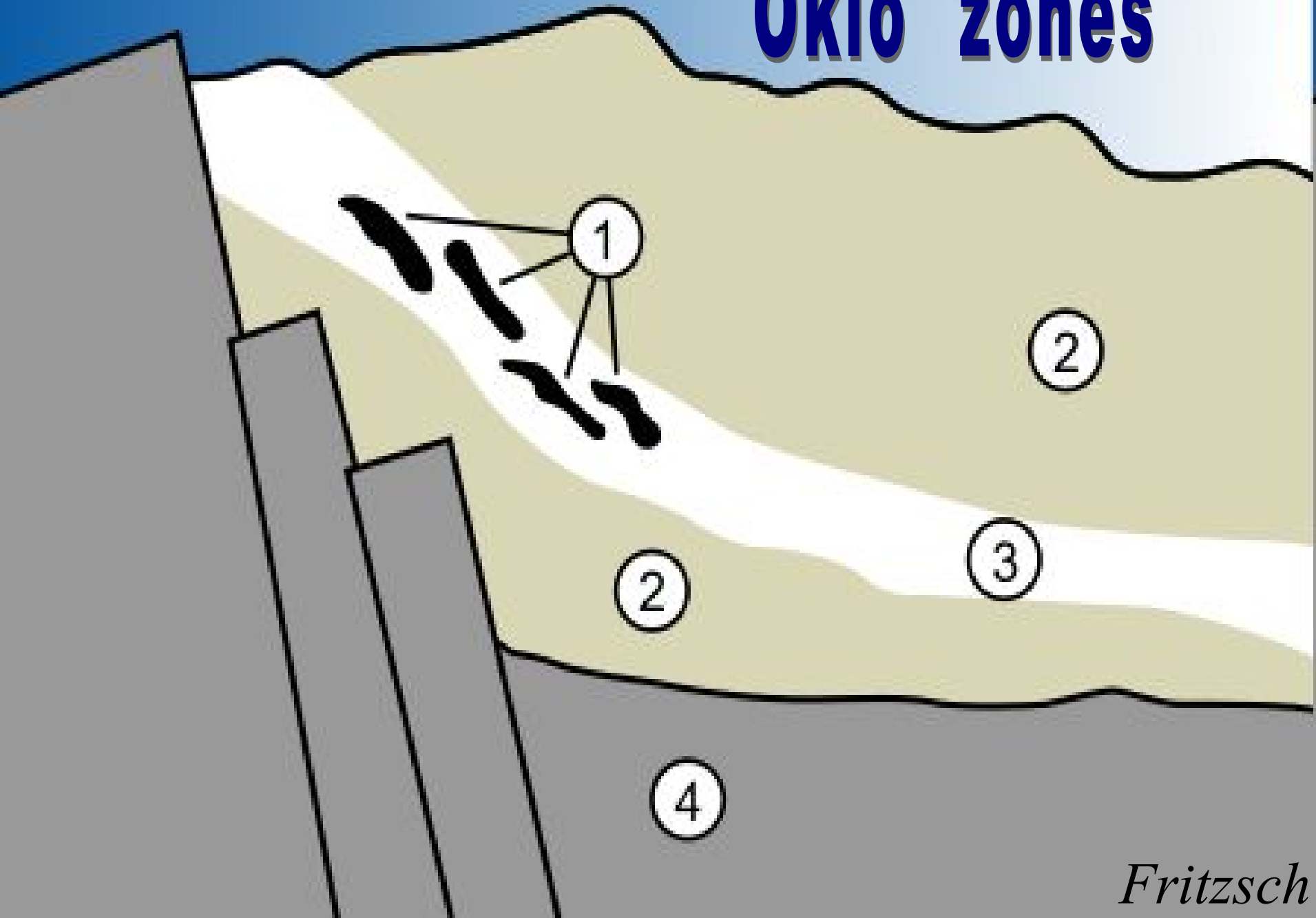
Natural reactor

Kinshasa

Brazzaville

Fritzsche

Oklo zones



samarium:

neutron capture



cross section about 80 kb

nuclear resonance: $E = 0.0973 \text{ eV}$

**change of resonance
position less than 0.1 eV
in 2 billion years**

***constraint for
fine-structure constant:***

$$\left(\frac{\alpha(\text{Oklo}) - \alpha(\text{now})}{\alpha} \right) \leq 10^{-7}$$

(Dyson, Damour)

***Change of alpha per year
must be less than***

$$10^{-16}$$

per year

(if no other parameters change)

==>constraint questionable

**limits on time variation
of constantes, related to
stable matter:**

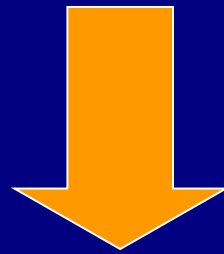
**fine-structure constant
mass of electron
QCD scale
quark masses**

time variation of QCD scale:

$$\dot{\Lambda} / \Lambda \leq 10^{-15} / \textit{year}$$

u / d - quarks

~ 20 MeV of proton mass



$$\dot{m}_{u,d} / m_{u,d} \leq 10^{-15} / \text{year}$$

unstable particles

*mass of muon, tauon,
c-quark, b-quark and t-quark*

**flavor mixing angles
mass of weak boson**

***b*-quarks**

$$\text{change}(m_b) \leq 10^{-6} / \text{year}$$

t-quark:

$$m = 171.3 \pm 2.3 \text{ MeV}$$

$$\text{change}(m_t) \leq 0.002 / \text{year}$$

1686

**Newtons
constant
of gravity**



Fritzsche

1686

PHILOSOPHIÆ
NATURALIS
PRINCIPIA
MATHEMATICA.

^{Autore} ^{ac} S. NEWTON^{Equite Aurato,}
Professore ^{Trin. Coll. Cantab. Soc. Mathefeos} ^{& Societatis Regalis Sodali.}
^{et Societatis Regie Societatis}

IMPRIMATUR.
S. PEPYS, Reg. Soc. PRÆSES.
Julii 5. 1686.

LONDINI,

Jussu Societatis Regie ac Typis Josephi Streater. Prostat apud
plures Bibliopolas. Anno MDCLXXXVII.

Dirac

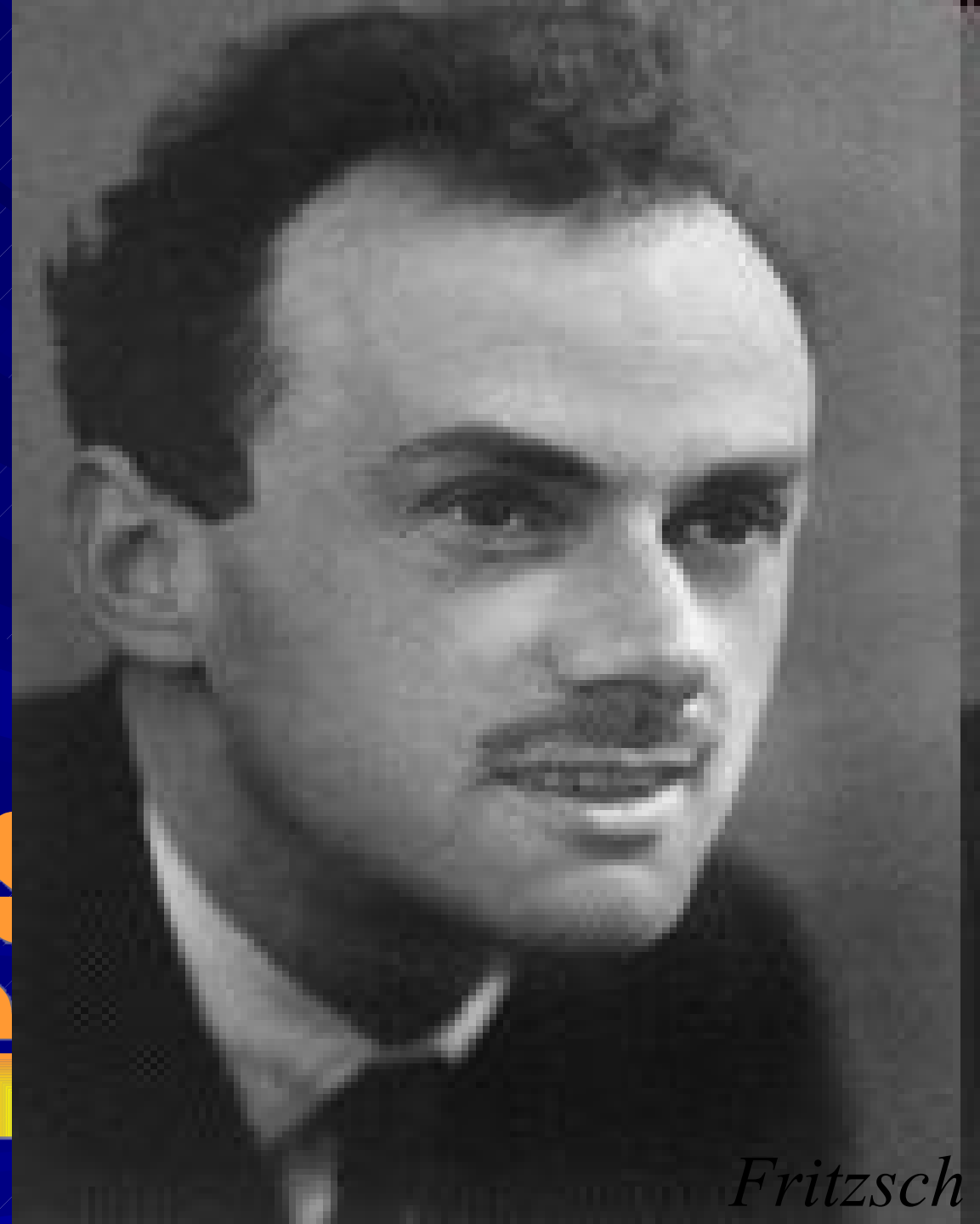
(~1930)

Time

Variation

of Newton's

constant G



Fritzsch

Dirac:

$$\frac{1}{G} \frac{dG}{dt} = H \approx 6 \cdot 10^{-11} / \text{year}$$

**excluded recently by
satellite experiments
- NASA -**

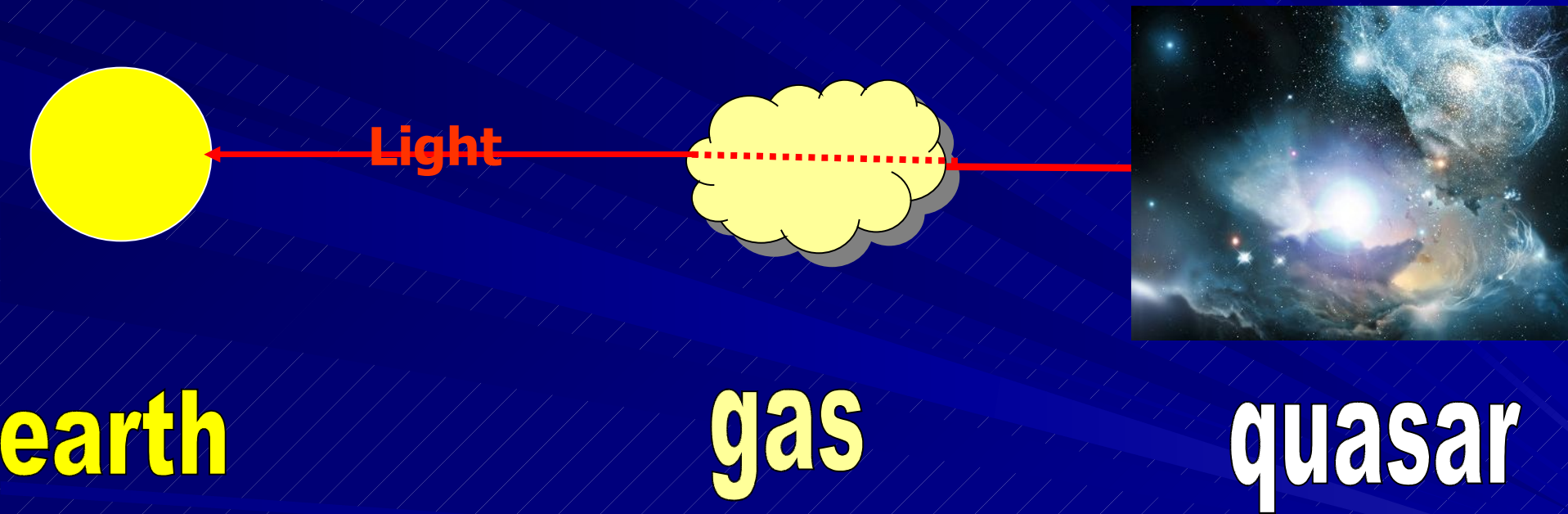
Time Variation of alpha?

*Observation of
fine structure of
atomic levels*

*Quasars
5-7 billion years back*



Quasar absorption spectra



Keck telescope

Hawäii



Fritsch

Experiment at Keck telescope (Australia, England, USA)

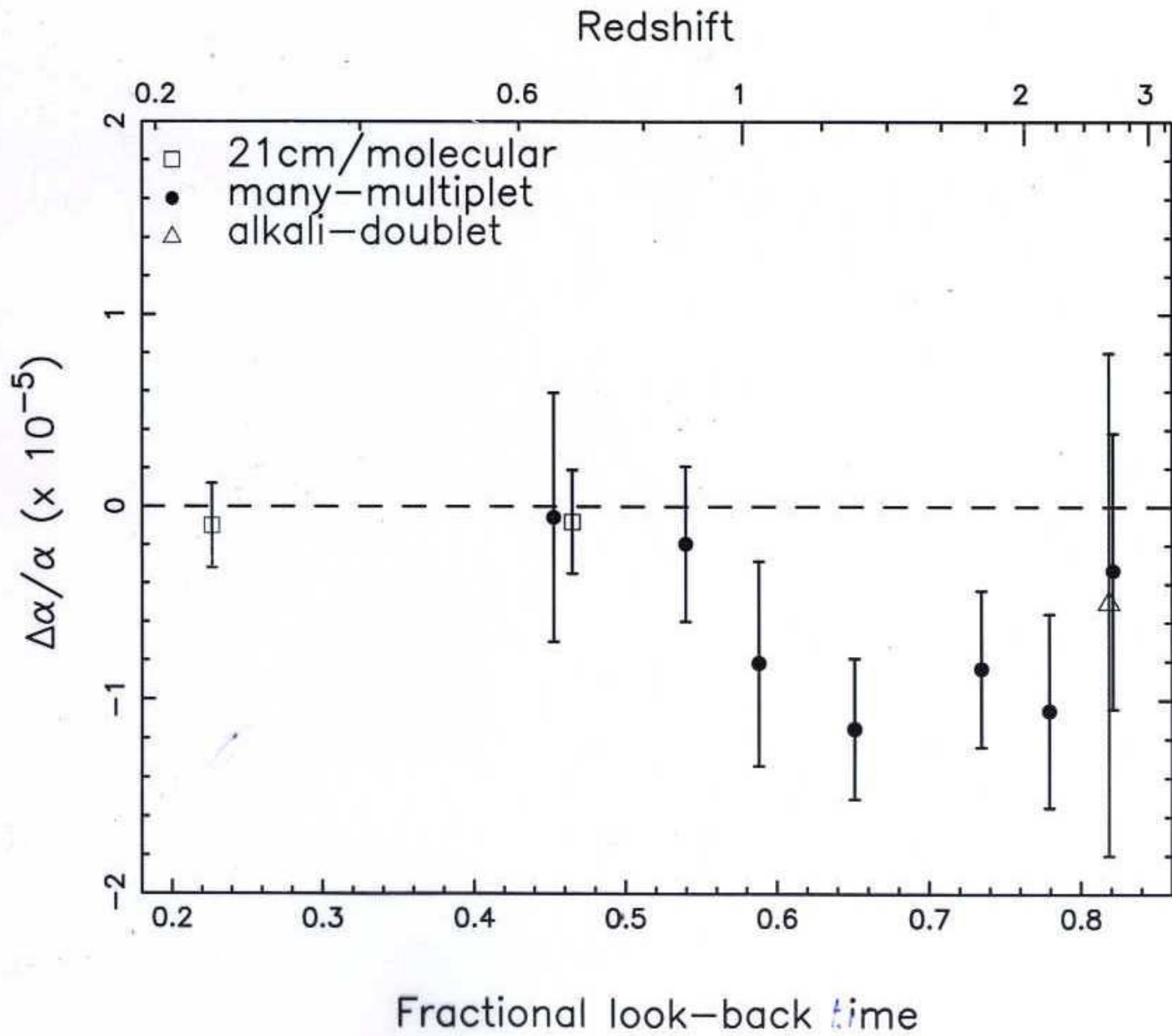
(Webb, Wolf, Flambaum...)

Fine structure of Fe, Ni, Mg, Sn, A -
Quasars, back to 11 bn years in time

$$\Delta\alpha/\alpha \approx (-5.4 \pm 0.12) \times 10^{-5}$$

Linearly decreasing

**N. Kanekar et al.
(May 2010)
arXiv:1004.5383
same result as
Webb et al.**



Fritzsche

grand unification:

$SU(3) \times SU(2) \times U(1)$

$\Rightarrow SO(10)$

(Fritzsch - Minkowski; Georgi - 1975)

Fritzsch

$SO(10)$



$SO(6)$

\times

$SO(4)$



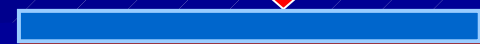
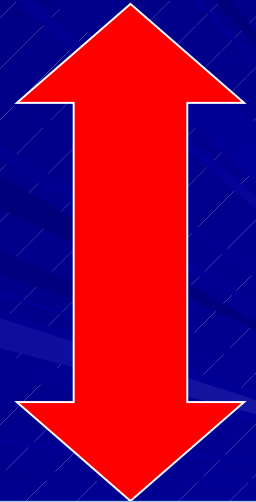
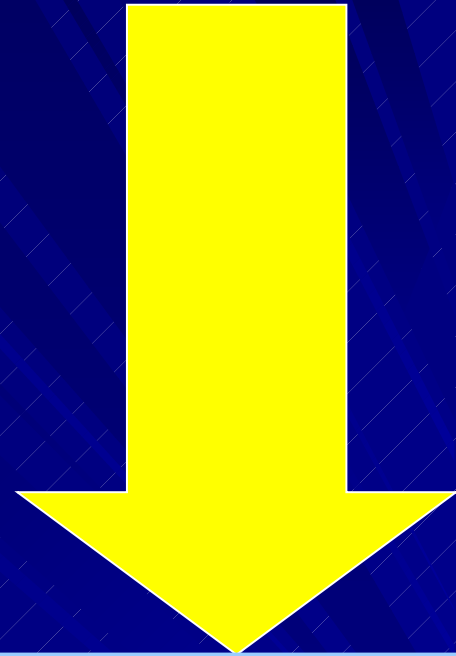
$SU(4)$

\times

$SU(2,L) \times SU(2,R)$



$SU(3) \times SU(2,L) \times U(1)$



Fritzsche

Grand Unification

3 coupling constants

electromagnetic, weak and strong interactions

reduced to two parameters:

unification scale
and

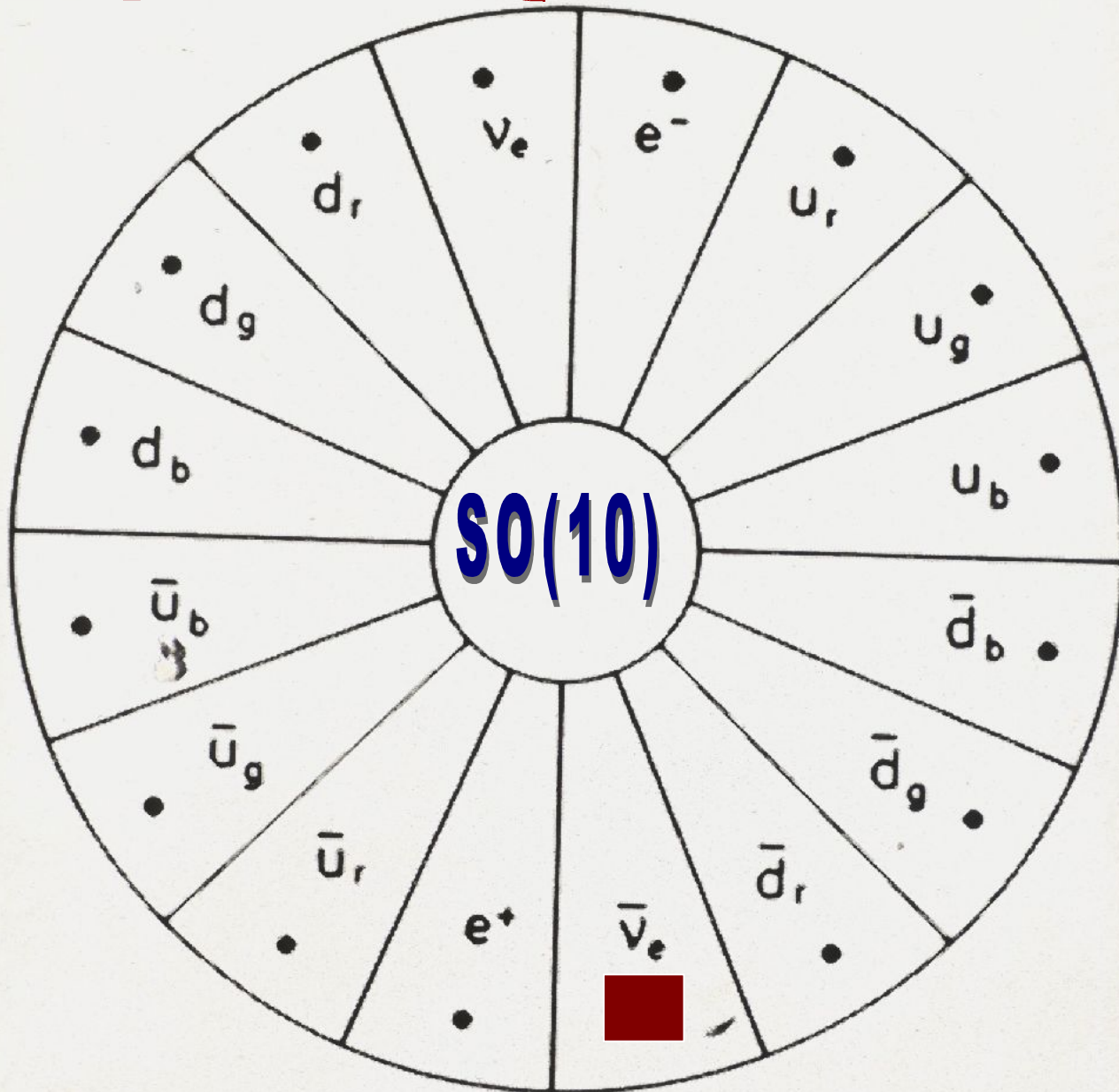
unified coupling

SU(6)

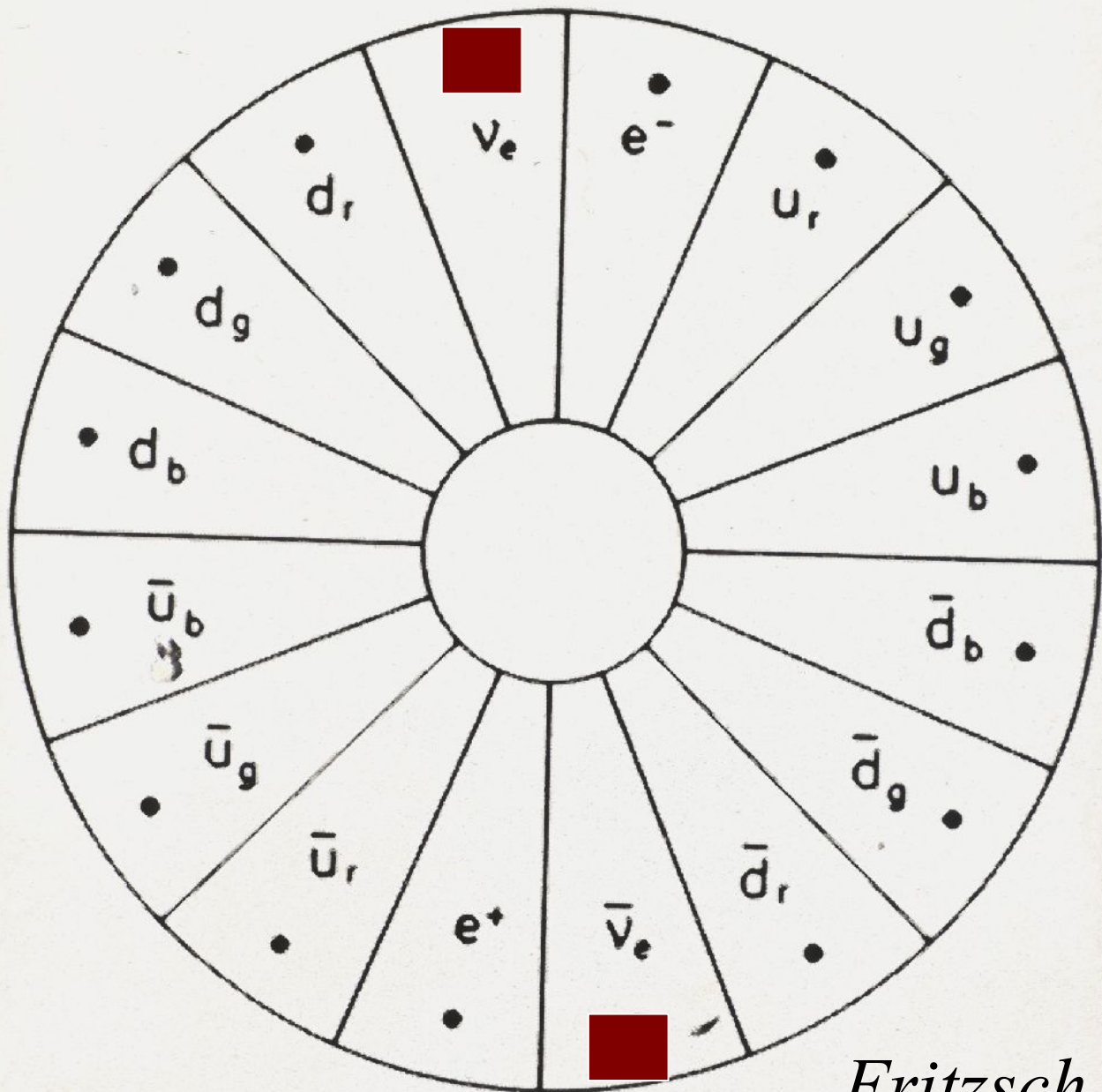
Fermions in 16-plet

(incl. righthanded neutrinos)

Leptons and Quarks in $SO(10)$

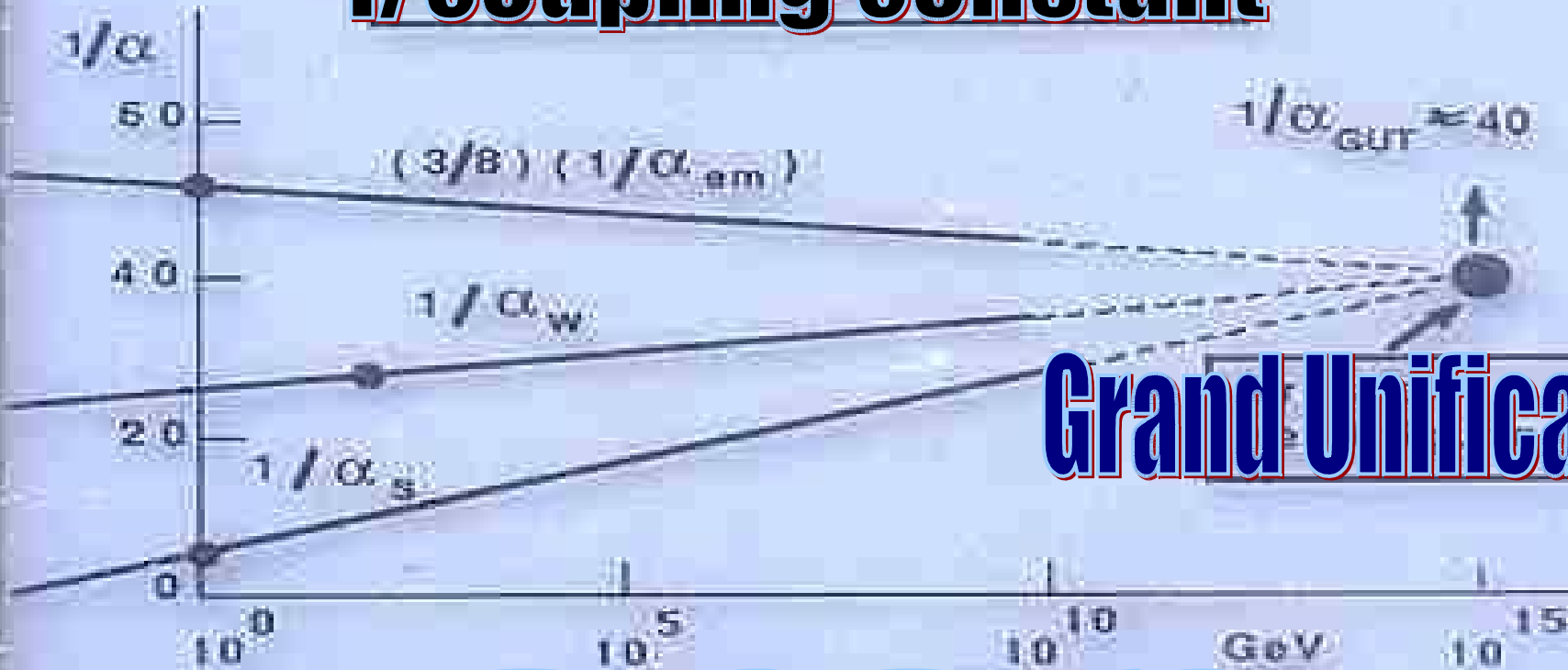


**Neutrinos
have a
mass**



Fritzsch

1/coupling constant



Grand Unification

energy



time change of

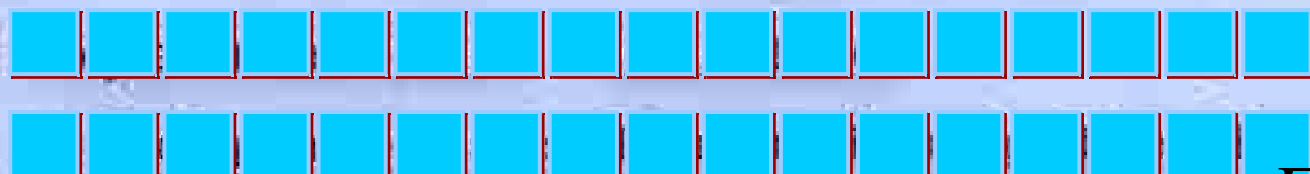
α ?

1/coupling constant

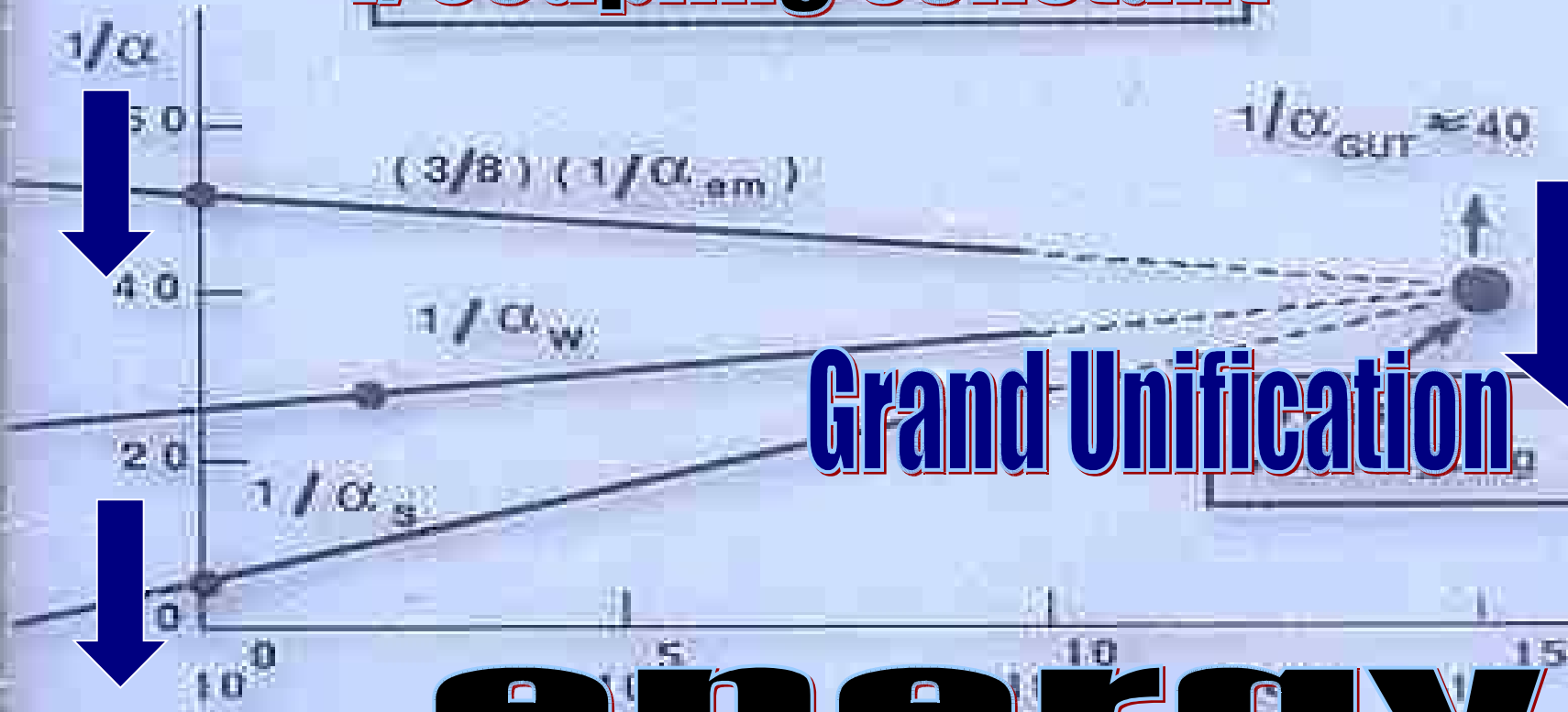


Grand Unification

energy

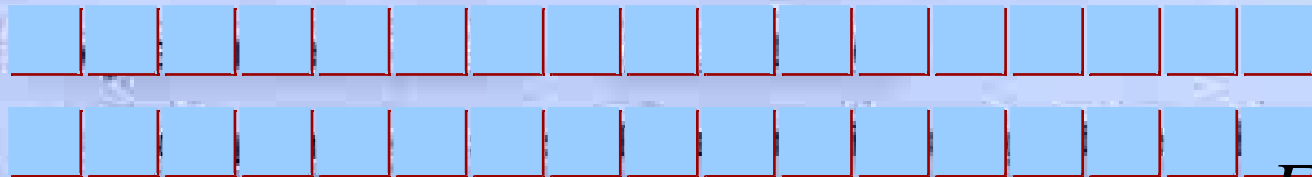


1/coupling constant



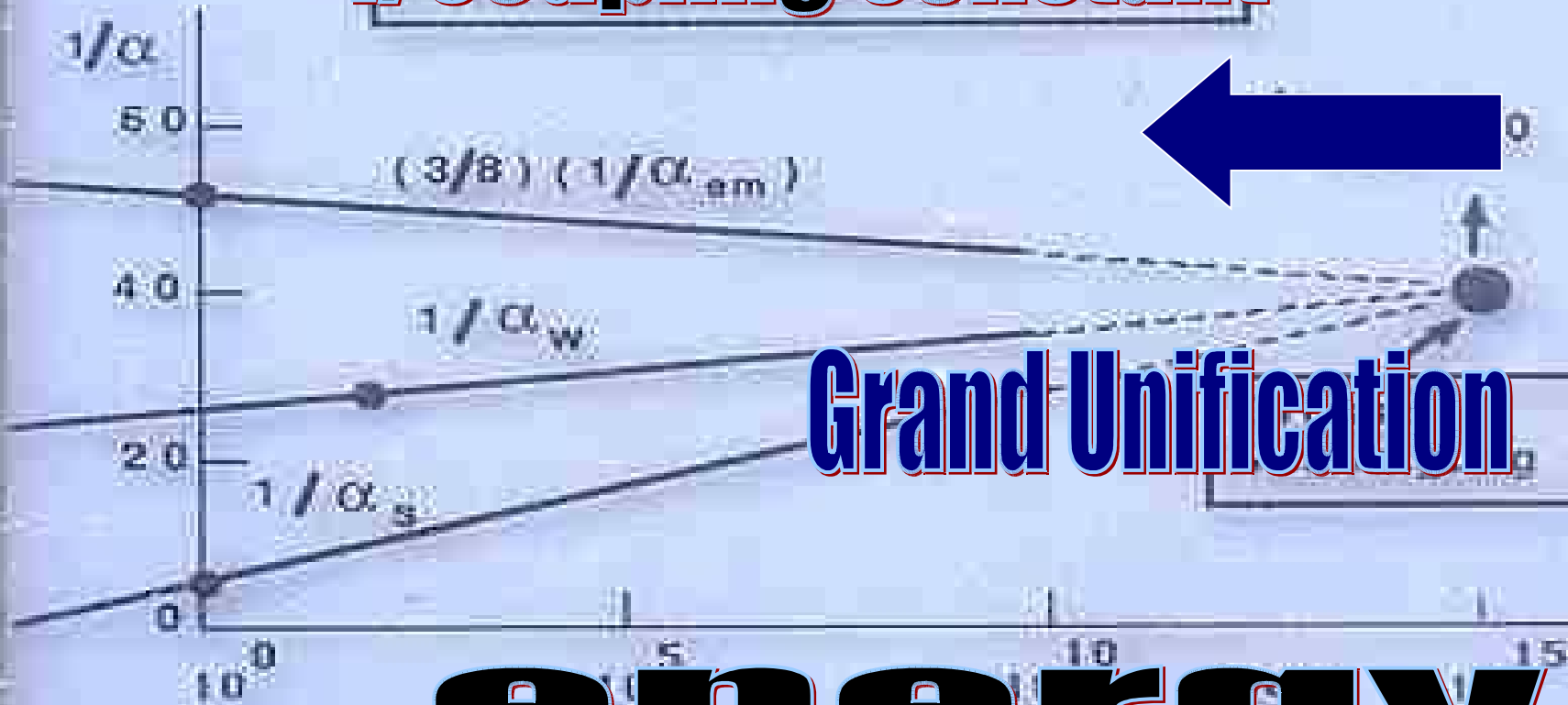
Grand Unification

energy



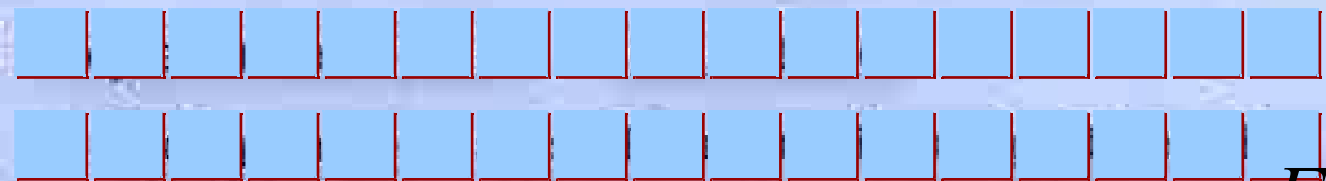
Fritzsch

1/coupling constant



Grand Unification

energy



Fritzsche

1/coupling constant



Grand Unification

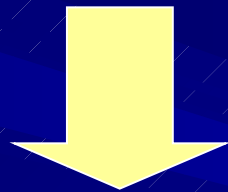
energy



$$d\alpha/dt = \frac{8}{3} \alpha^2 \left(\sum_s c_s - \frac{1}{2} \sum_u s_u \right) \frac{\Delta d}{\Delta t}$$

**Calmet, Fritzsche
Langacker, Segre 2002**

no change of unification scale



$$d\alpha/dt = \frac{8}{3} \alpha^2 \sum_s c_s \frac{d\alpha_s/dt}{\alpha}$$

$$d\Lambda / d\Lambda \approx t \delta \quad d \delta \approx d \alpha$$

Magnetic moments of atomic nuclei would change accordingly, per year

$$3, *9 \quad \Gamma^1 \quad ($$

change of unification scale

$$\dot{\Lambda} / \Lambda \approx (-31) \dot{\alpha} / \alpha$$

experiments:

MPQ Munich

NIST Boulder

Time:

measured by Cesium clocks

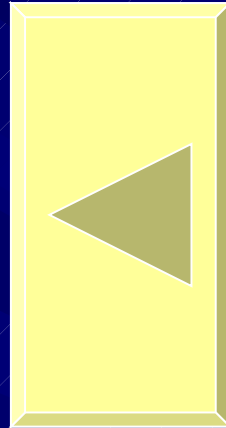
Hyperfine transition \rightarrow magnetic moment of the cesium nucleus.

Would be affected by time change of QCD scale

Cesium: 9 192 631 770 Hz

(definition of time)

comparison:



difference: 3 Cs oscillations per day

**Experiment
(T. Hänsch, MPQ)**



T. Hänsch

Fritzsche

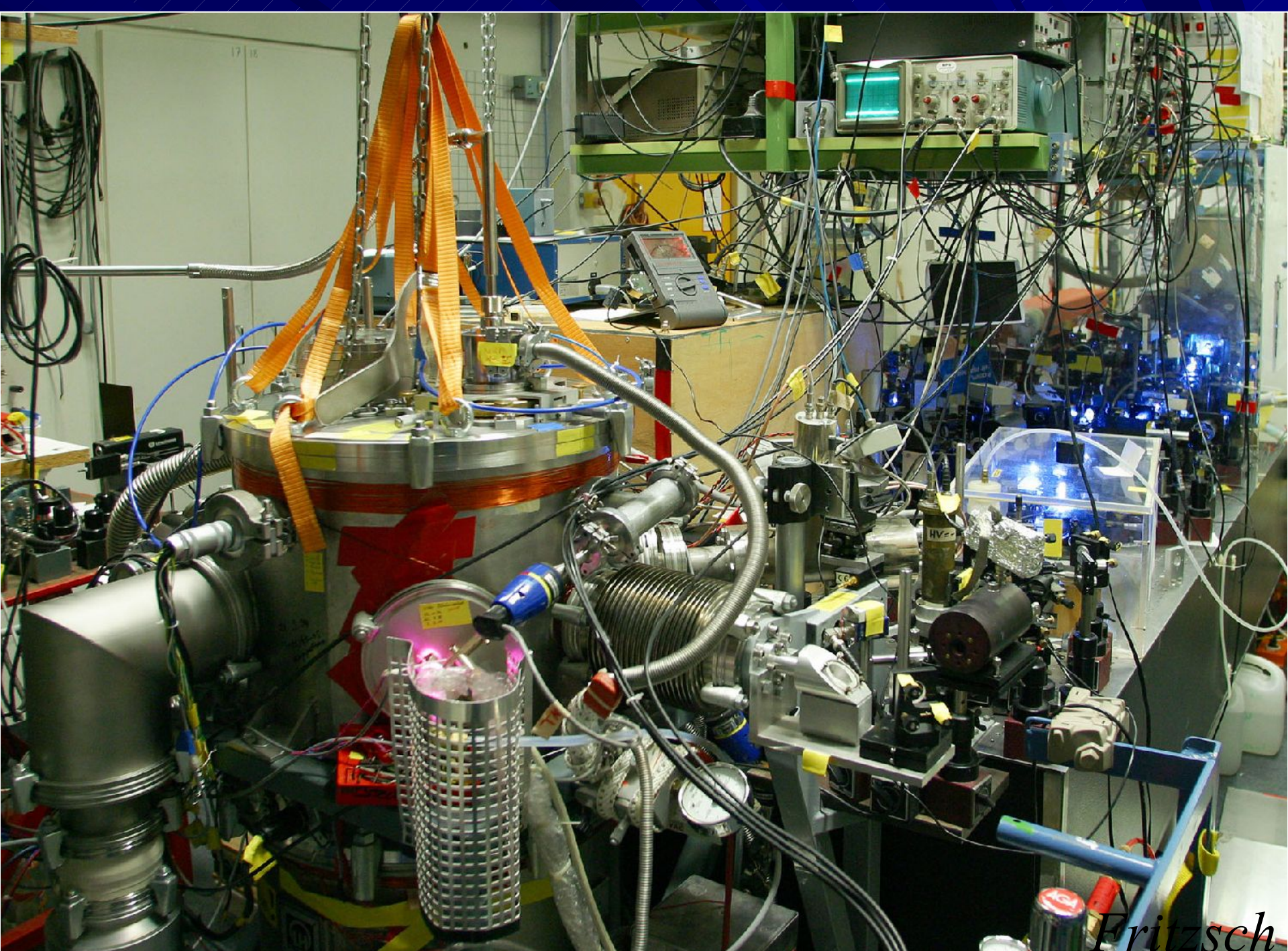
MPQ-experiment

*486 nm dye laser in hydrogen
spectrometer*

*Reference: cesium clock Pharao LPTF
Paris*

Hydrogen: 1s-2s transition

2 466 061 413 187 127 (18) Hz



Fritzsch

result of Haensch:

$$d\mu / : (\mu D = \xi \quad 4 \quad 6 \quad . \quad 8 \quad) \quad y^1 \quad 0^{5-}$$

experiment :

$$d\mu / d : \mu \neq 2 \quad 4 \quad 6 \quad . \quad 8 \quad) \quad y^1 \quad 0^{5-}$$

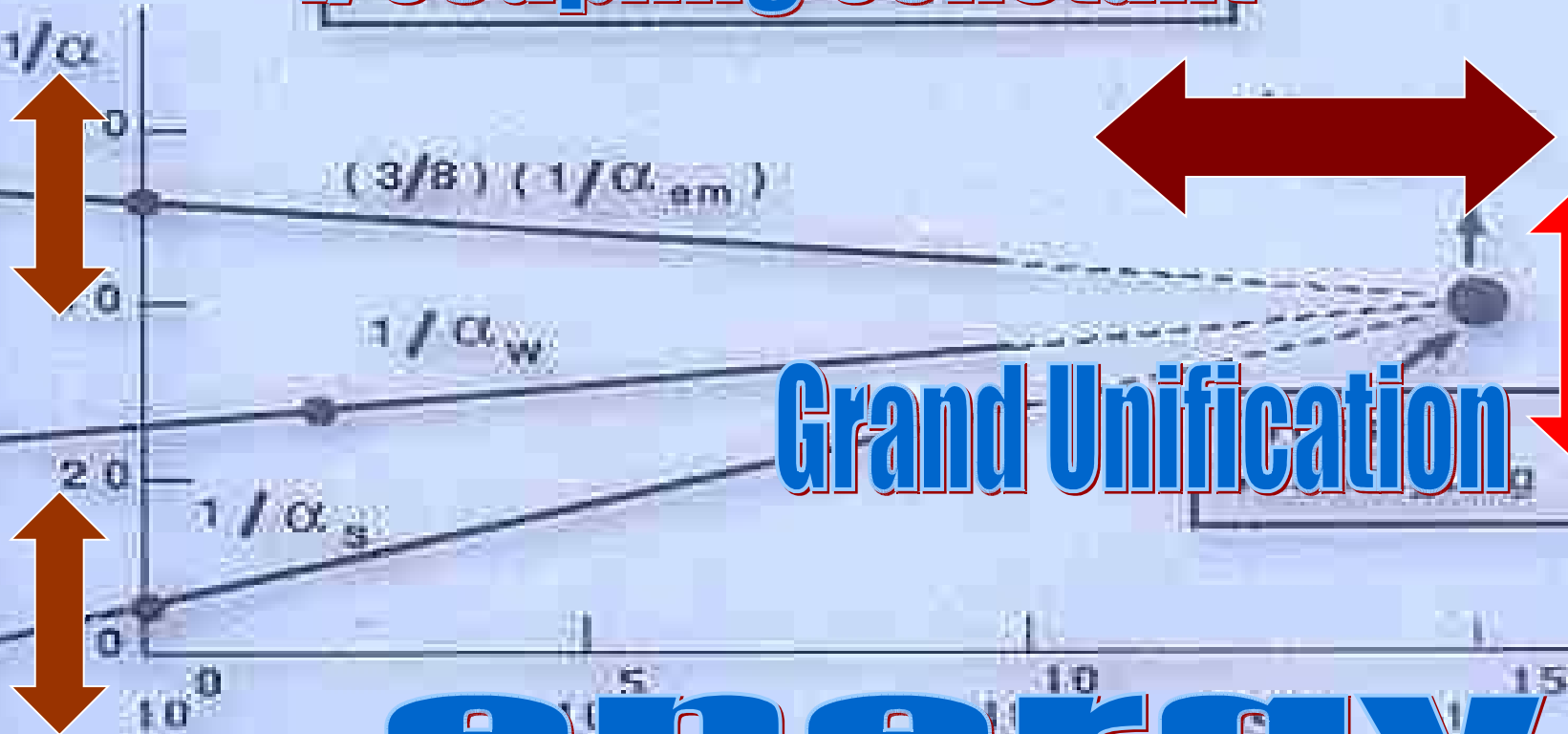
expected:

$$d\mu / d : \mu \neq 2 \quad 1^{-1} ($$

==> excluded!

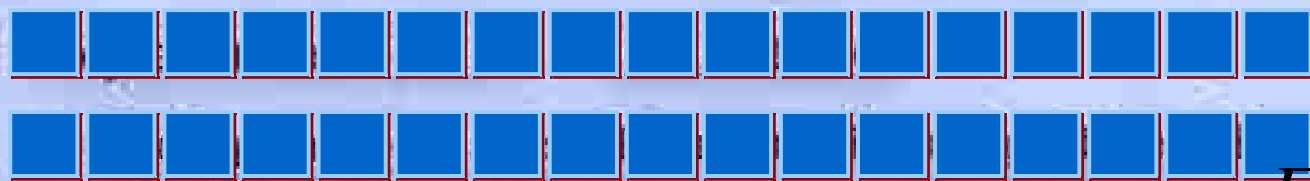
Simultaneous change
of the unified coupling
constant and the
unification scale?

1/coupling constant



Grand Unification

energy



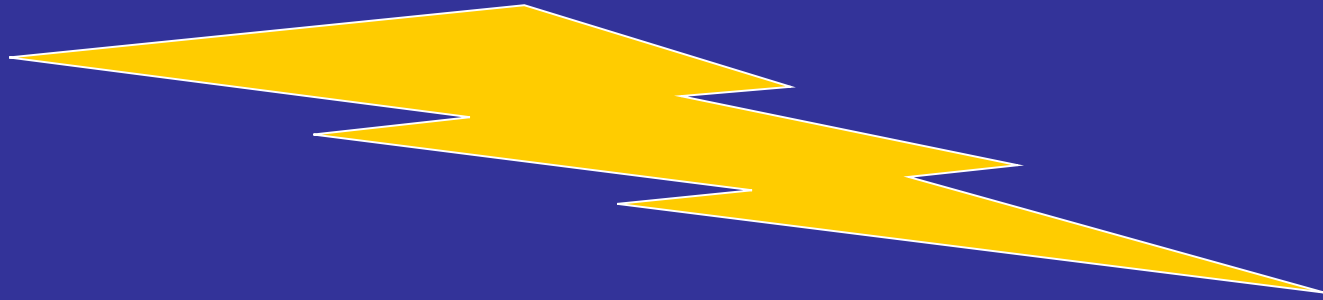
Simultaneous change of unif. coupling and
unif. scale

Partial Cancellation of effect?
(expected in superstring models)

$$\frac{8}{3} d\alpha_s dt + \alpha_s^2 dt + \log d_G + t \alpha c^2 \left(-\frac{\theta}{\pi} - \frac{1}{2} n_t \right) + t_G \Lambda - d \quad d_u \Lambda t :$$



cancellation



$$\dot{\Lambda} / \Lambda \leq 10^{-14} \quad / \textit{year}$$

Hänsch et al.



$$\sim 3 \times 10^{-15} / \text{year}$$

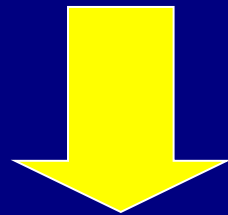
Reinhold et al., 2006

VLT Chile

Fritzschn

Reinhold et al. PRL 96 (2006)
2 quasars, 12 bn. years away

time variation of ratio
proton mass / electron mass



$$\Delta\mu/\mu = (2.0 \pm 0.6) \times 10^{-5}$$

$$\Rightarrow \Delta\Lambda / \Lambda \approx 10^{-5} \text{ yr}^{-1} e^{-1}$$

(if the electron mass
is taken to be constant)

$\Rightarrow \Delta\Lambda / \Lambda 03 \quad 1^{-1} 0^5 y \notin$

\Rightarrow Hänsch



*The masses of atomic nuclei
will depend on time!*

energy not strictly conserved

A deep space photograph showing a vast field of stars and galaxies. A faint constellation outline is visible in the upper half of the image, with a prominent bright blue star at its center. The background is filled with numerous smaller stars and distant galaxies in various colors and sizes.

does alpha depend on space?

Webb et al, 2010:

VLT and Keck

**small space dependence of
fine-structure constant**

Conclusions:

28 constants of nature

24 constants → mass parameters

**Grand unification relates the elm.,
strong and weak interactions.**

The time variation of alpha leads to a time variation of the QCD scale.

The MPQ Experiment rules out the simplest model.

An effect seems to be present, about a factor 10 less than naively expected, consistent with the observed variation of the electron-proton mass ratio.

Necessary:

Both unification scale and
unified coupling
must change in time.

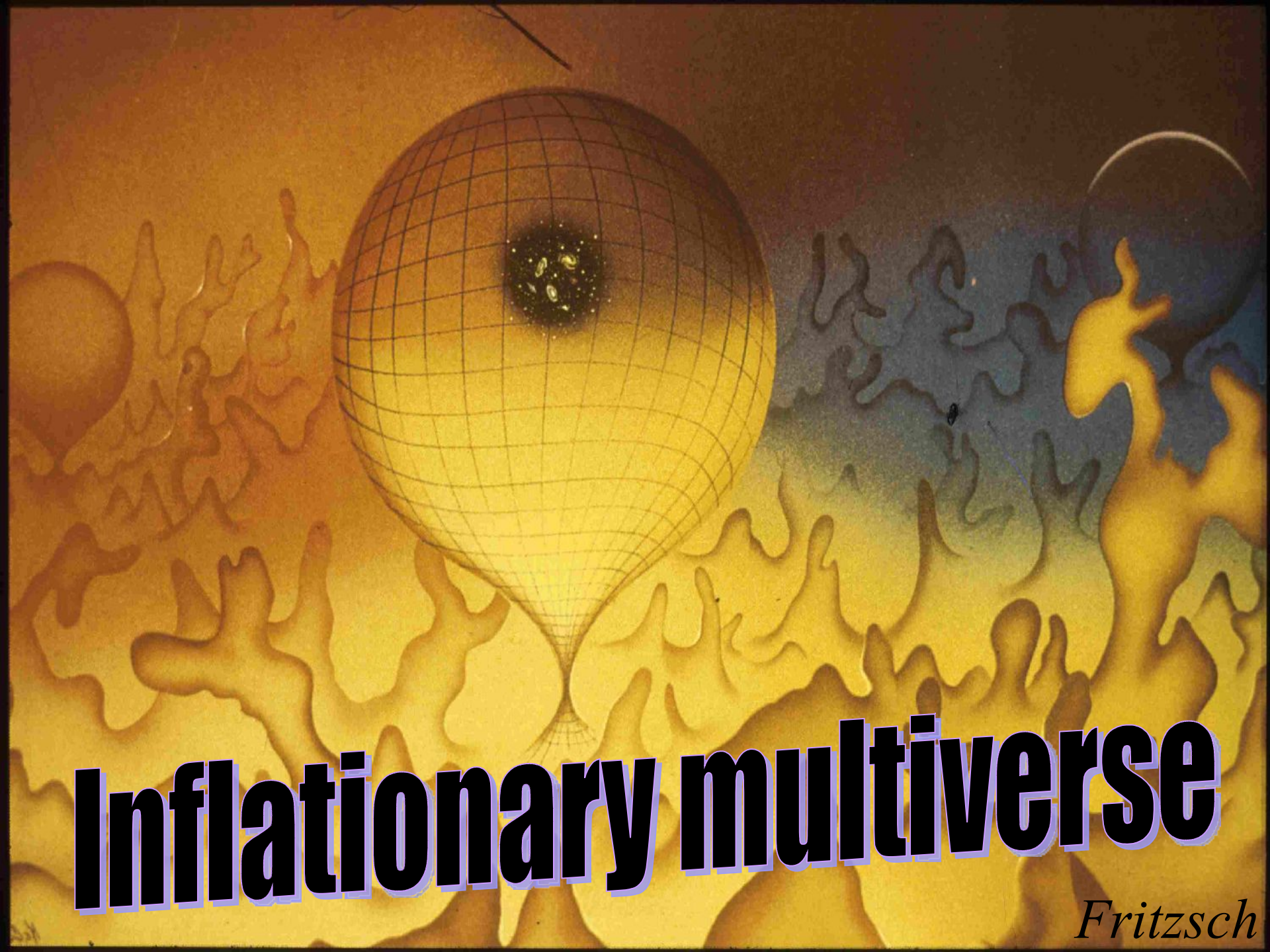
(expected in superstring
models)

Perhaps all fundamental constants are not constant, but functions of time?

⇒ cosmology?

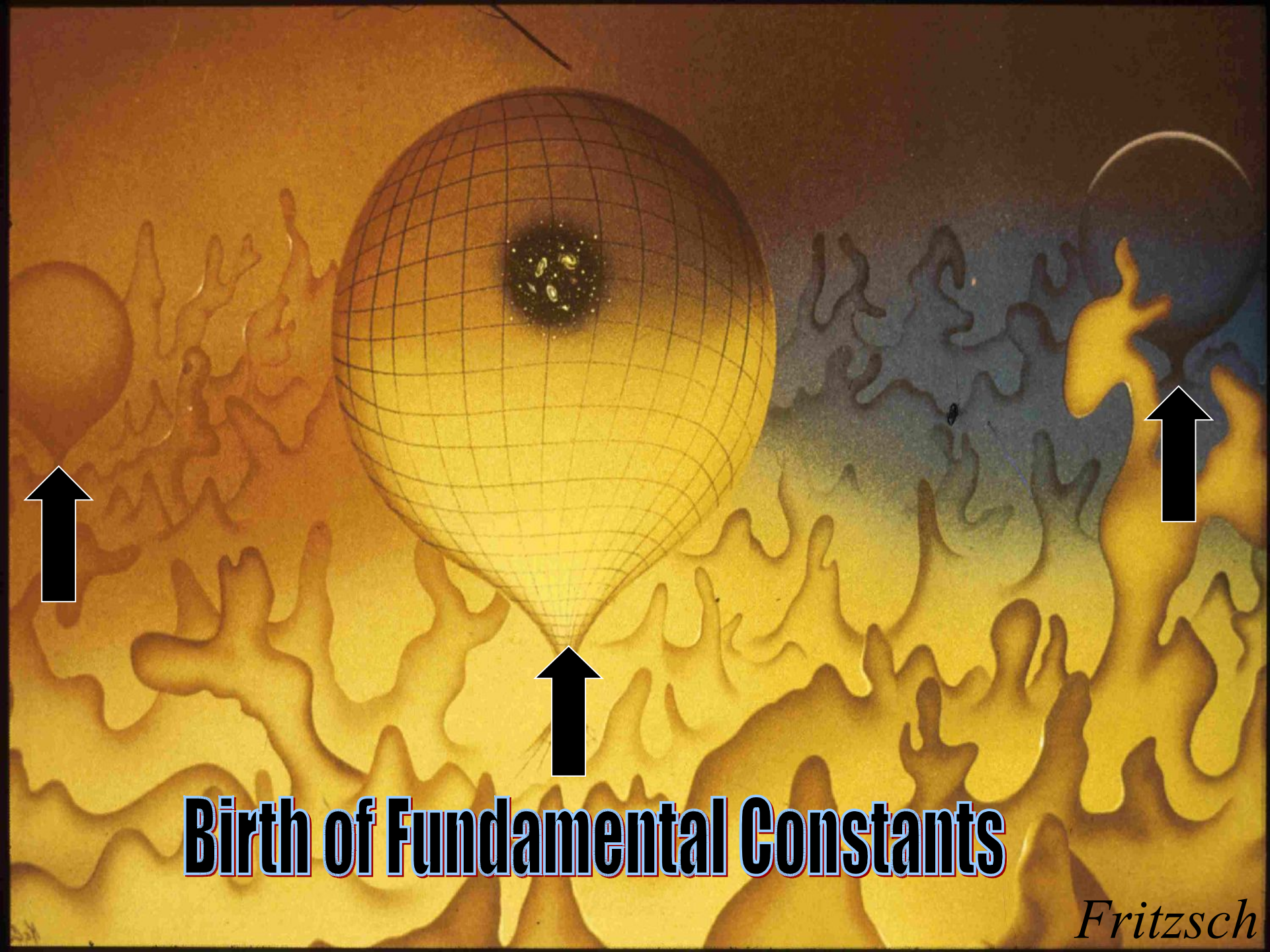
Universe

⇒ Multiverse



Inflationary multiverse

Fritzs



Birth of Fundamental Constants

Fritzsche

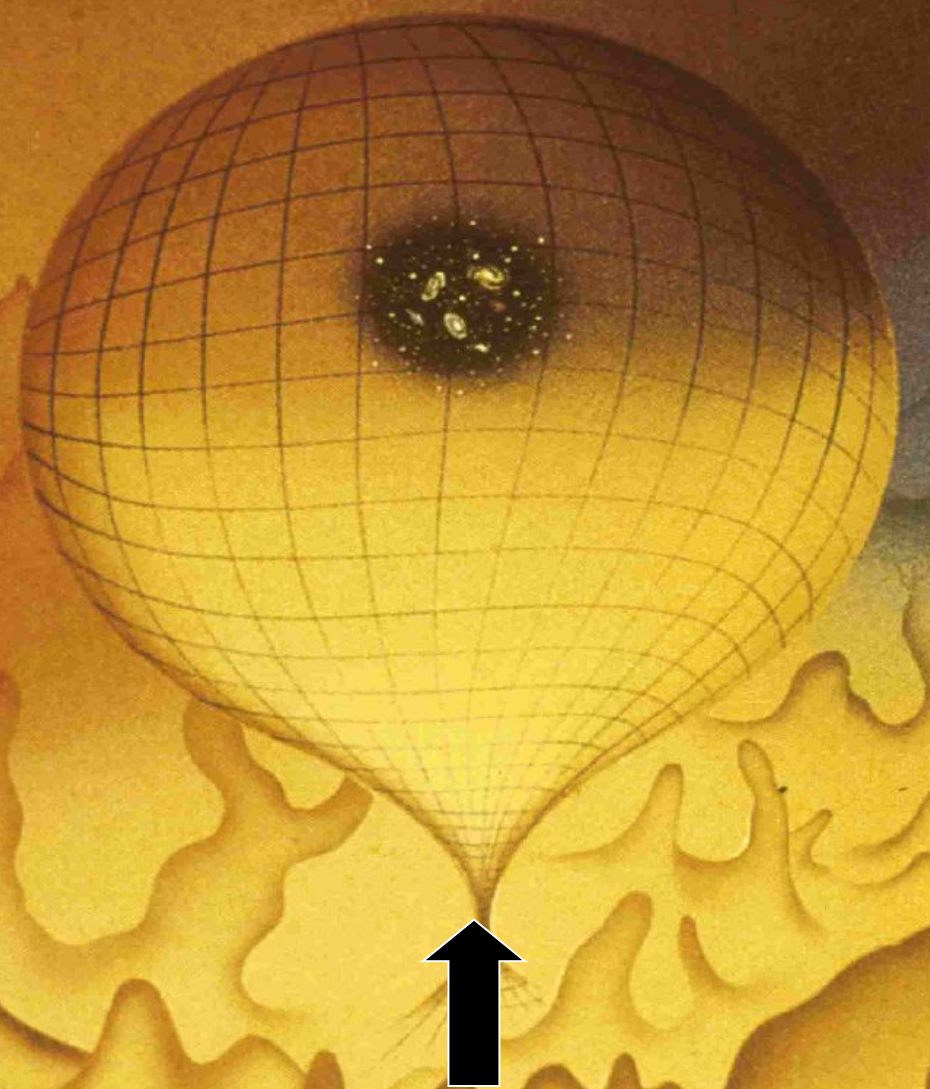


Fundamental constants

cosmic accidents?



G_n m_e
 α α_s



COSMIC accidents

Fritzs