

# Anisotropic Flow at the LHC as measured by ALICE



«ETTORE MAJORANA» FOUNDATION AND CENTRE FOR SCIENTIFIC CULTURE  
TO PAY A PERMANENT TRIBUTE TO GALILEO GALILEI, FOUNDER OF MODERN SCIENCE  
AND TO ENRICO FERMI, THE "ITALIAN NAVIGATOR", FATHER OF THE WEAK FORCES



## INTERNATIONAL SCHOOL OF NUCLEAR PHYSICS 34th Course: *PROBING THE EXTREMES OF MATTER WITH HEAVY IONS*

ERICE-SICILY: 16 – 24 SEPTEMBER 2012

Sponsored by the: • Deutsche Forschungsgemeinschaft • European Physical Society  
• Italian Ministry of University and Research • Sicilian Regional Government

### TOPICS AND LECTURERS

*Color Glass Condensate and the implications for the LHC*  
• J. ALBACETE, CEA/Saclay, Gif-sur-Yvette, FR

*New results from ALICE I*  
• P. BRAUN-MUNZINGER, GSI, Darmstadt, DE

*Penetrating probes for heavy-ion collisions*  
• T. HEMMICK, SUNY, Stony Brook, NY, US

*Hydrodynamic description of ultrarelativistic heavy-ion collisions*  
• T. HIRANO, University of Tokyo, JP

*Gluon saturation, geometric scaling and color glass condensates in heavy-ion collisions*  
• K. ITAKURA, KEK, Tsukuba, JP

*Recent results from PHENIX*  
• B. JACAK, Stony Brook, NY, US

*Dileptons and photons in heavy-ion collisions*  
• R. RAPP, College Station, Texas AM University, TX, US

*Sound propagation in the quark-gluon plasma*  
• E. SHURYAK, SUNY, Stony Brook, NY, US

*The planned NICA facility in Dubna*  
• A. SORIN, Joint Institute for Nuclear Research, Dubna, RU

*Collective flow at the LHC*  
• R. SNELLINGS, Utrecht University, NL

*New results from ALICE II*  
• J. STACHEL, University of Heidelberg, DE

*Recent results from the HADES experiment*  
• J. STROTH, University of Frankfurt, DE

*The equation of state in weak coupling*  
• A. VUORINEN, University of Bielefeld, DE

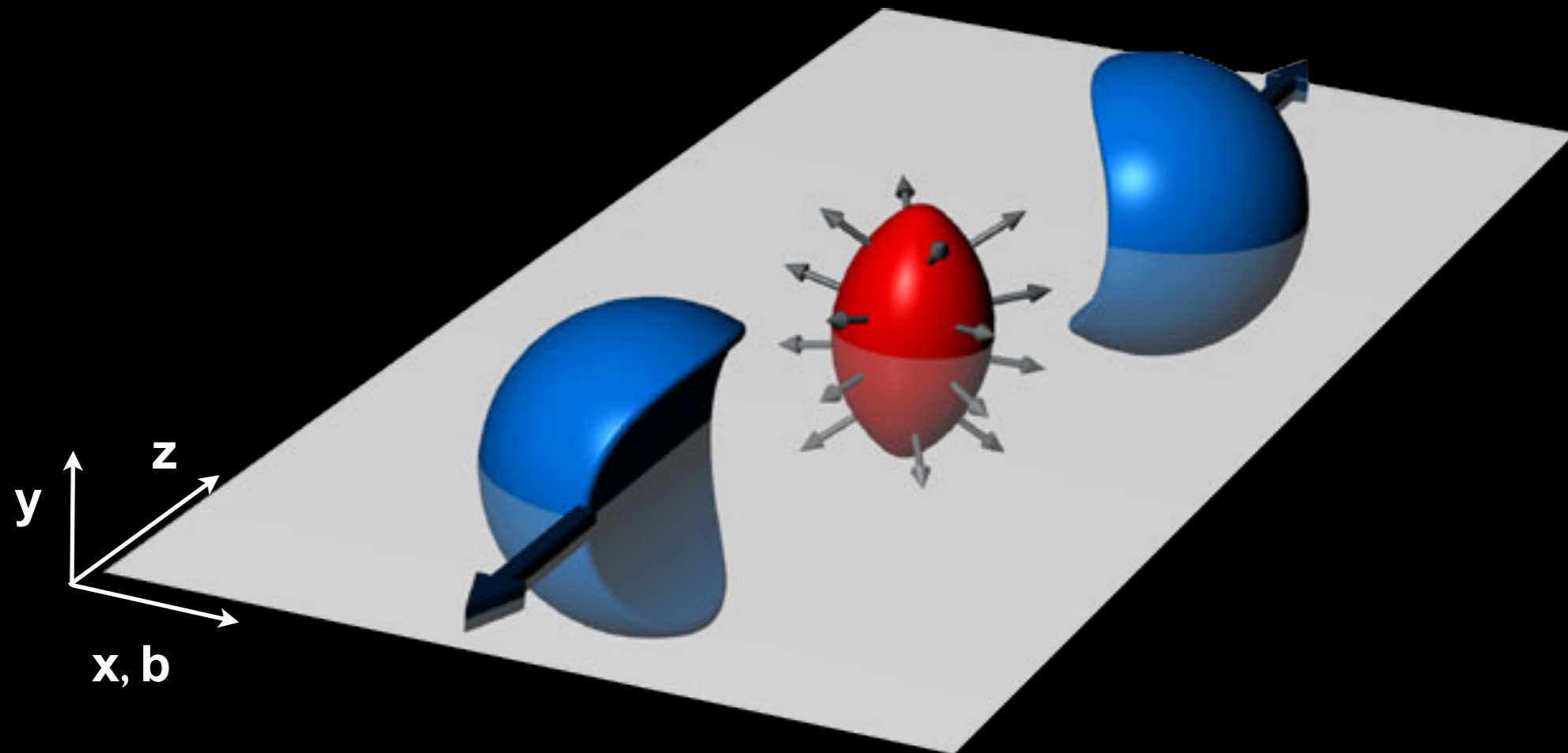
*Quarkonia production in heavy-ion collisions*  
• P. ZHUANG, Tsinghua University, Beijing, CH

## Raimond Snellings

# Content

- 1) Elliptic Flow
- 2) What do we learn from various particle species?
- 3) Higher harmonics
- 4) What's next?

# In a Heavy Ion Collision



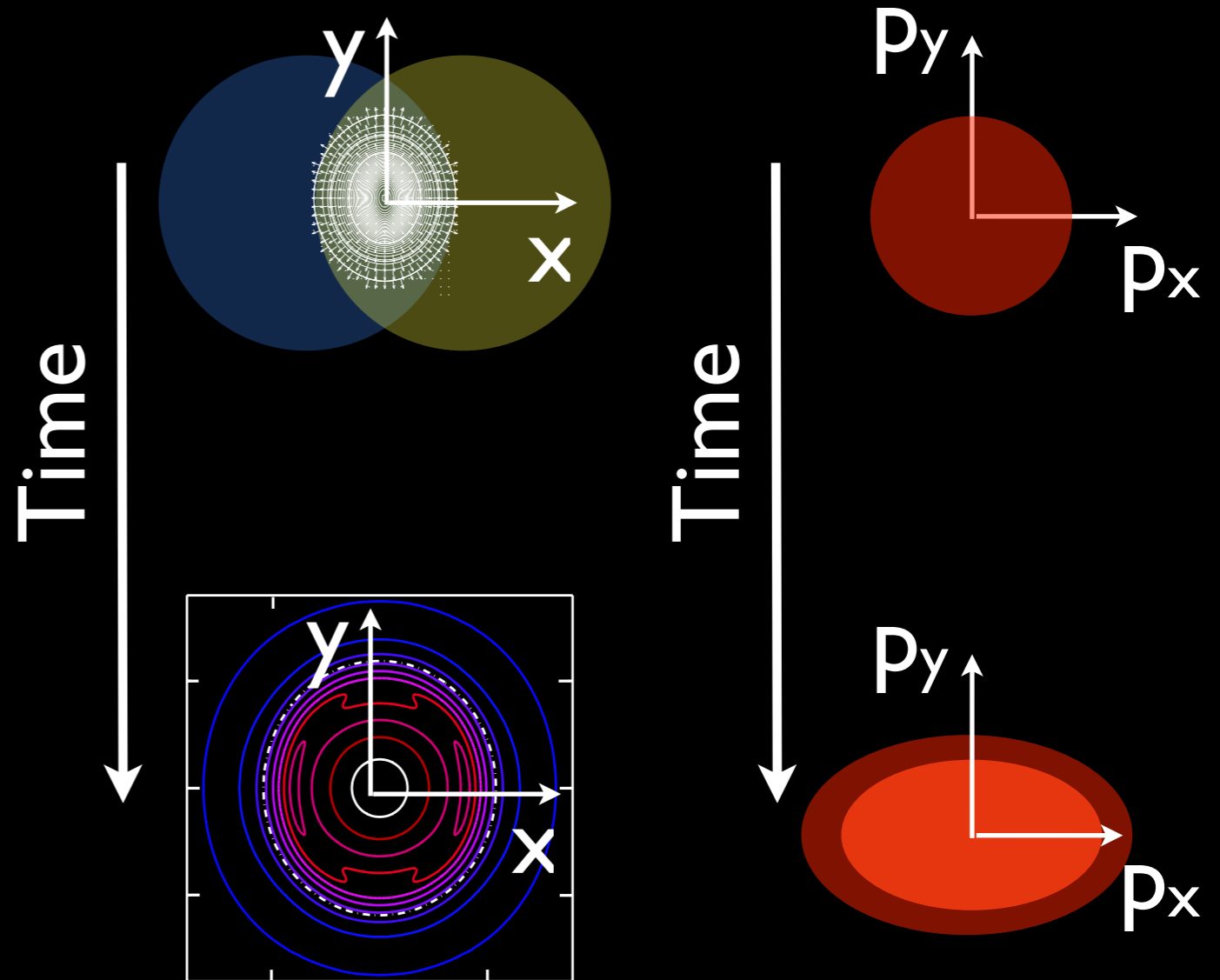
an anisotropic system is created

# Elliptic Flow

$$\varepsilon = \frac{\langle y^2 - x^2 \rangle}{\langle y^2 + x^2 \rangle}$$

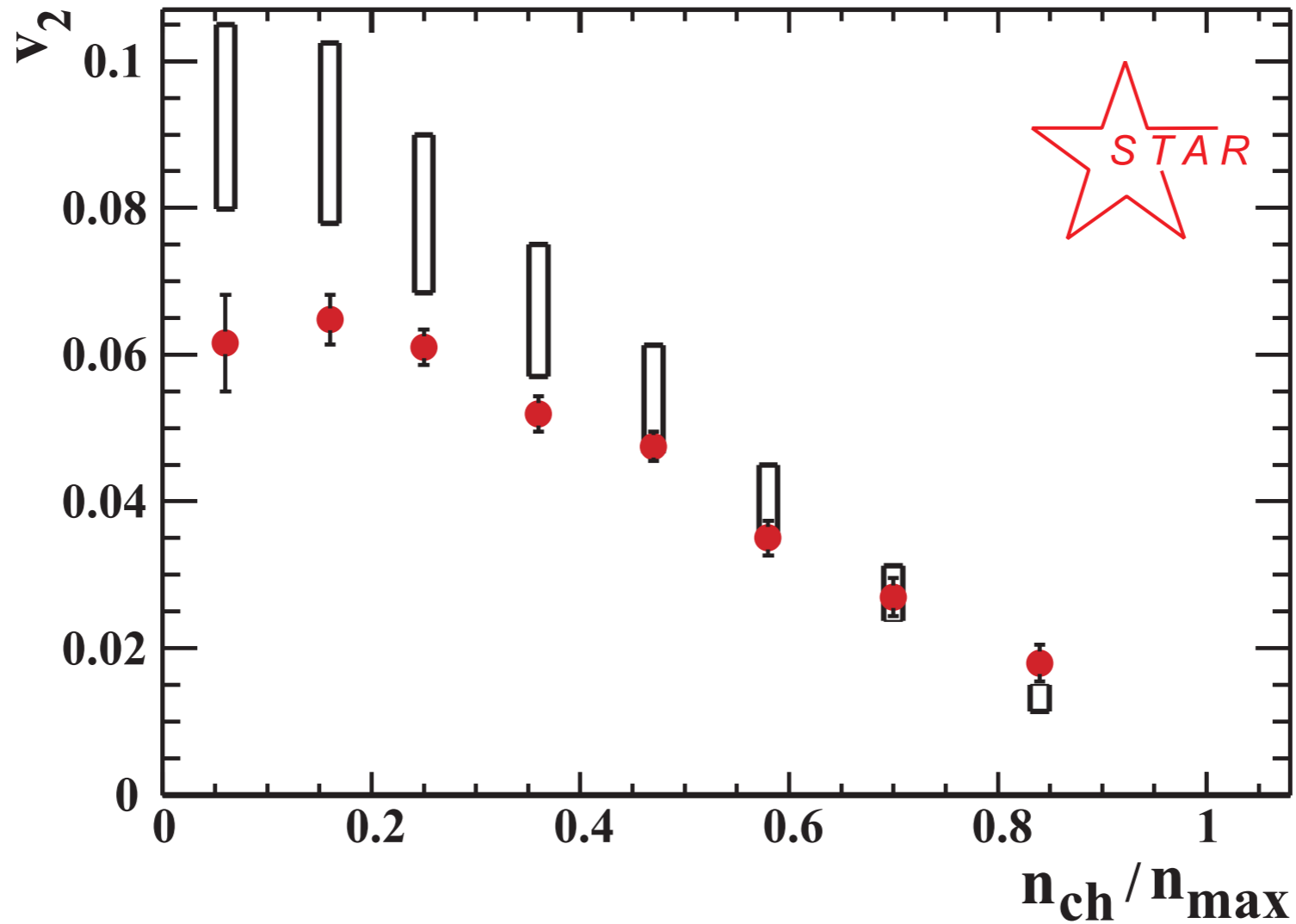
$$v_2 = \langle \cos 2\phi \rangle$$

- the system in coordinate space configuration is anisotropic (for a non-central collision almond shape). However, initial momentum distribution isotropic (spherically symmetric)
- interactions among constituents generate a pressure gradient which transforms the initial coordinate space anisotropy into the observed momentum space anisotropy → anisotropic flow
- self-quenching → sensitive to early stage



# Flow at RHIC

STAR Phys. Rev. Lett. 86, 402–407 (2001)



Elliptic flow is large

Ideal hydro gets the magnitude for more central collisions

# RHIC Scientists Serve Up “Perfect” Liquid

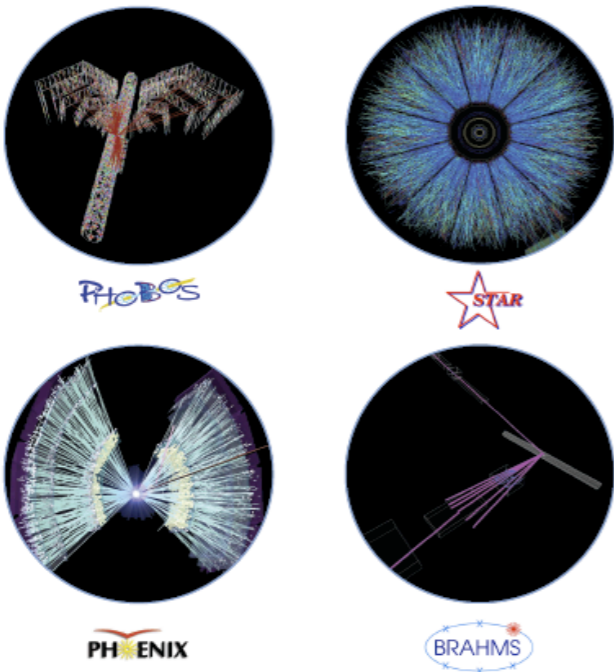
## New state of matter more remarkable than predicted -- raising many new questions

April 18, 2005

BNL -73847-2005  
Formal Report

### Hunting the Quark Gluon Plasma

RESULTS FROM THE FIRST 3 YEARS AT RHIC  
ASSESSMENTS BY THE EXPERIMENTAL COLLABORATIONS  
April 18, 2005




PHOBOS

STAR

PHENIX

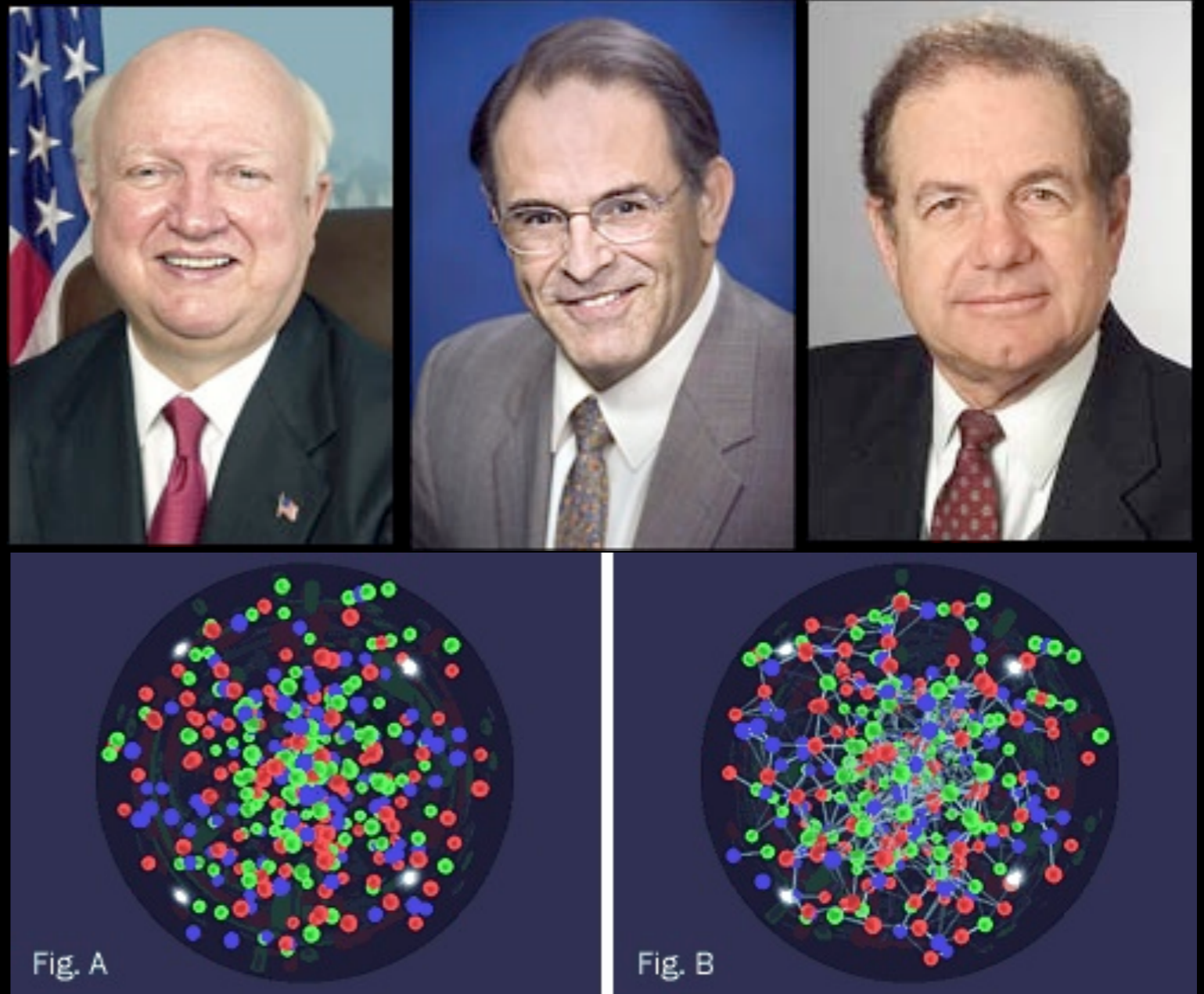
BRAHMS

Relativistic Heavy Ion Collider (RHIC) • Brookhaven National Laboratory, Upton, NY 11974-5000

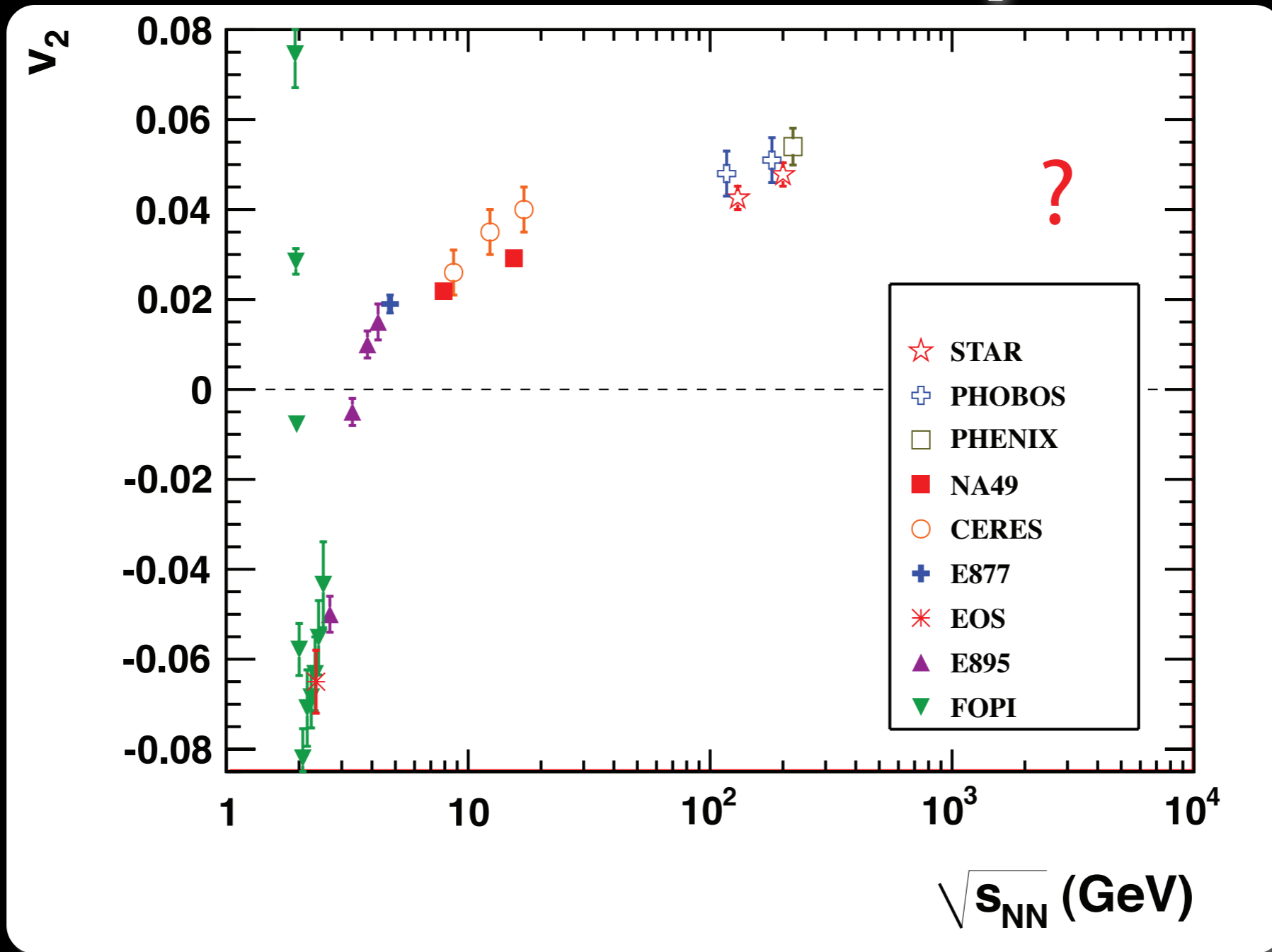


Office of Science  
U.S. DEPARTMENT OF ENERGY

BROOKHAVEN  
NATIONAL LABORATORY



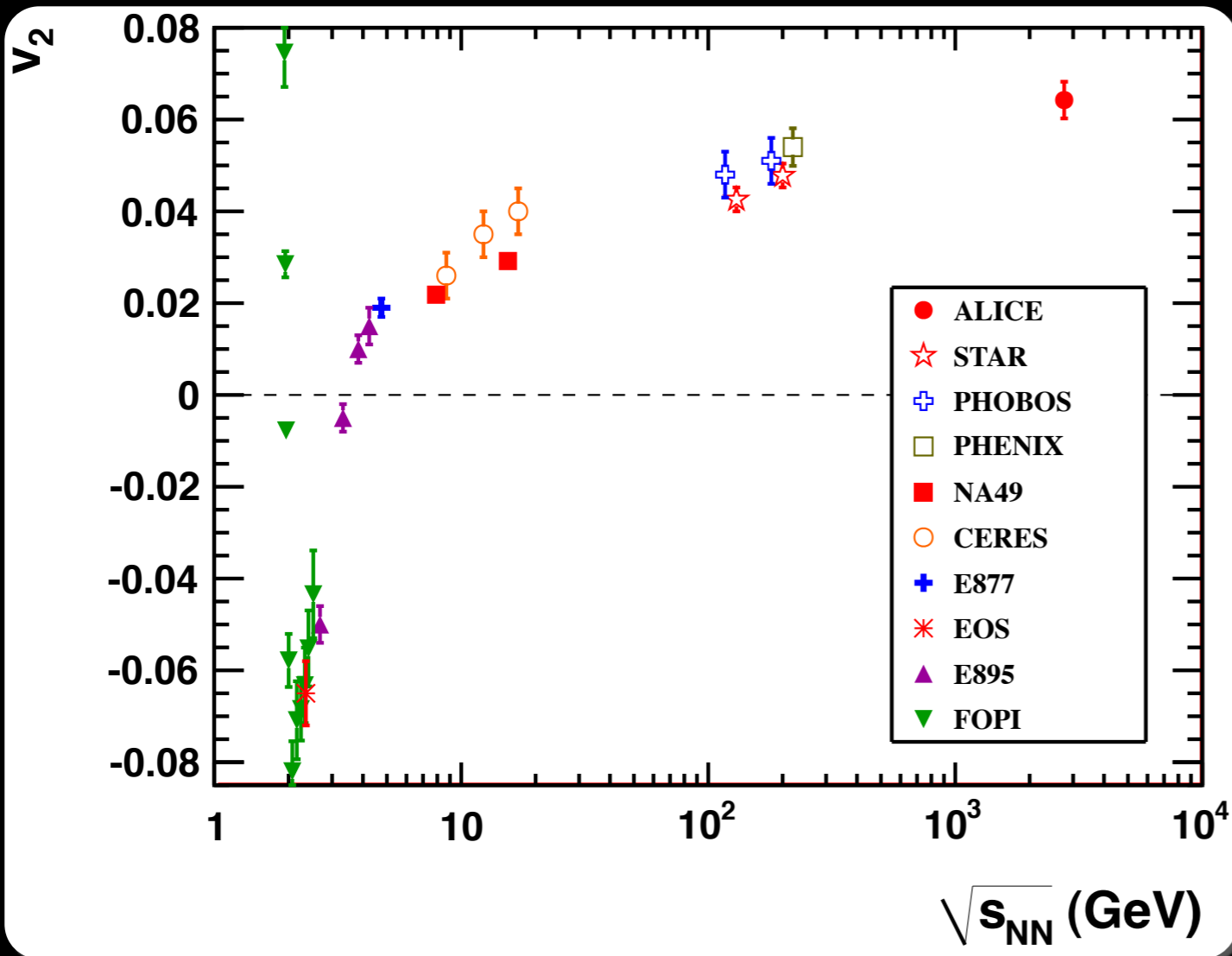
# The Perfect Liquid?



What to expect at the LHC: still the perfect liquid or approaching a viscous ideal gas?

# The Perfect Liquid?

K. Aamodt et al. (ALICE Collaboration) PRL 105, 252302 (2010)



Physics

Physics 3, 105 (2010)

## Viewpoint

### A "Little Bang" arrives at the LHC

Edward Shuryak

Department of Physics and Astronomy, Stony Brook University, Stony Brook, NY 11794, USA

Published December 13, 2010

*The first experiments to study the quark-gluon plasma at the LHC reveal that even at the hottest temperatures ever produced at a particle accelerator, this extreme state of matter remains the best example of an ideal liquid.*

Subject Areas: **Particles and Fields**

#### A Viewpoint on:

**Elliptic Flow of Charged Particles in Pb-Pb Collisions at  $\sqrt{s_{NN}} = 2.76$  TeV**

K. Aamodt et al. (ALICE Collaboration)

Phys. Rev. Lett. 105, 252302 (2010) – Published December 13, 2010

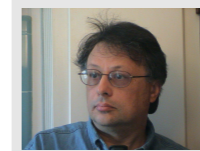
**Observation of a Centrality-Dependent Dijet Asymmetry in Lead-Lead Collisions at  $\sqrt{s_{NN}} = 2.76$  TeV with the ATLAS Detector at the LHC**

G. Aad et al. (ATLAS Collaboration)

Phys. Rev. Lett. 105, 252303 (2010) – Published December 13, 2010

## About the Author

### Edward Shuryak



Edward Shuryak received his Ph.D. in 1970 at Budker Institute of Nuclear Physics, Novosibirsk, Russia, where he later became a professor, before moving to the physics department at Stony Brook University in 1990. He has held visiting positions at CERN, Brookhaven National Laboratory, and several other institutions. He is a Fellow of the American Physical Society and has served on the Editorial Board of *Physical Review C*. In 2008 he was recognized as an Outstanding Referee by the American Physical Society. His research interests include the theoretical description of the quark-gluon plasma and high-energy ion collisions. In the late 1970s he introduced the term "quark-gluon plasma."

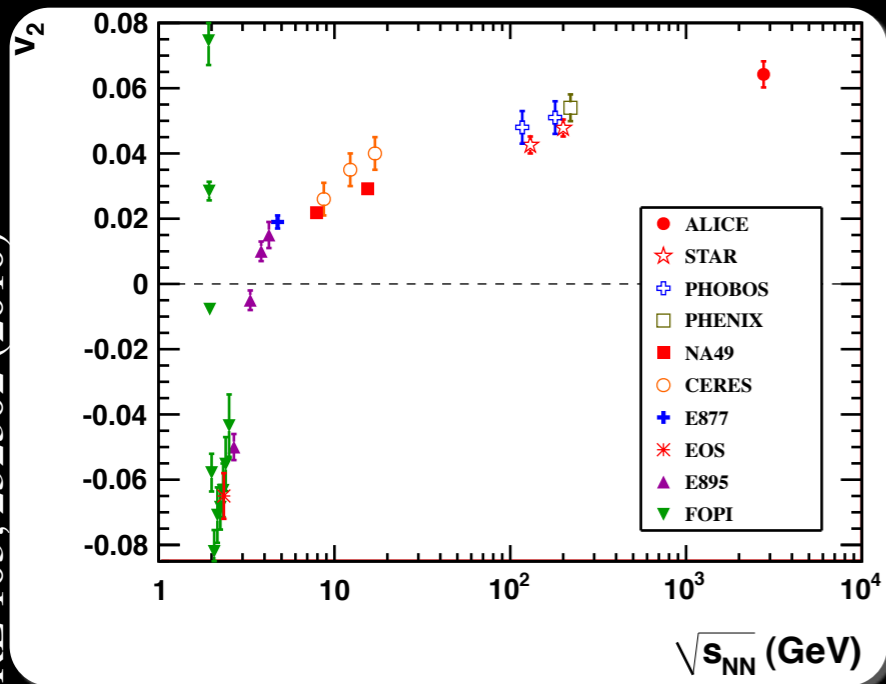
CERN, November 26, 2010:

'the much hotter plasma produced at the LHC behaves as a very low viscosity liquid (a perfect fluid)..'



# First LHC $v_2$ measurement

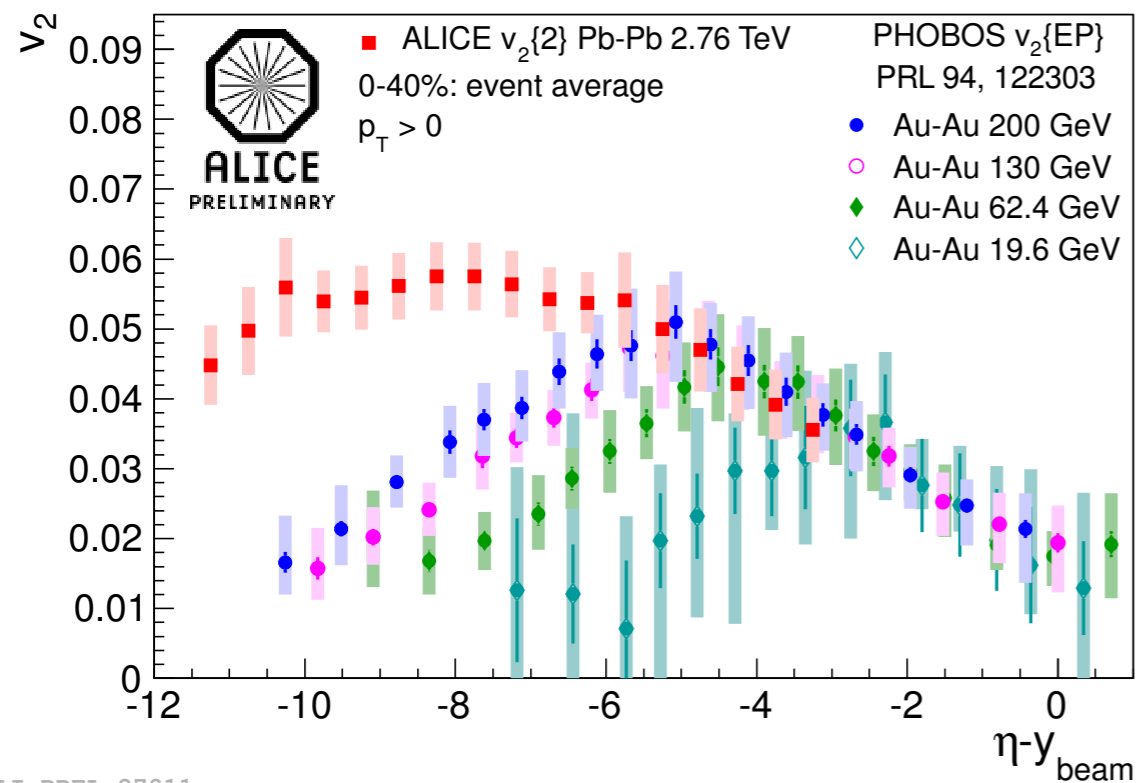
K. Aamodt et al. (ALICE Collaboration)  
PRL 105, 252302 (2010)



1) not in line with expectations from pure ideal hydro (measured  $v_2$  increased too much)

2) not in line with simple triangular scaling

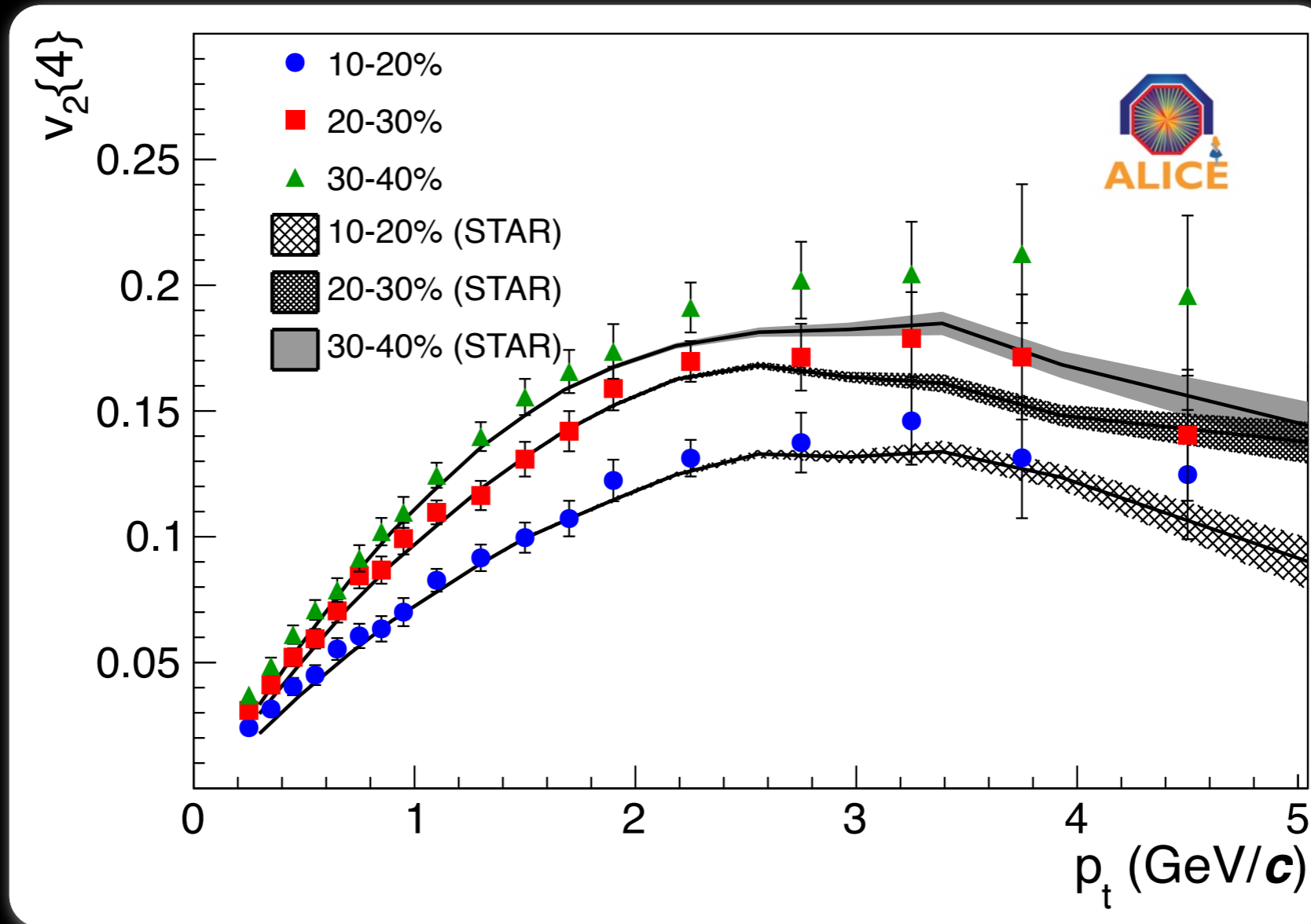
3) in line with expectations from models incorporating viscous corrections (viscous hydro, parton cascades, hybrid models)



# $v_2$ as function of $p_t$

K. Aamodt et al. (ALICE Collaboration)

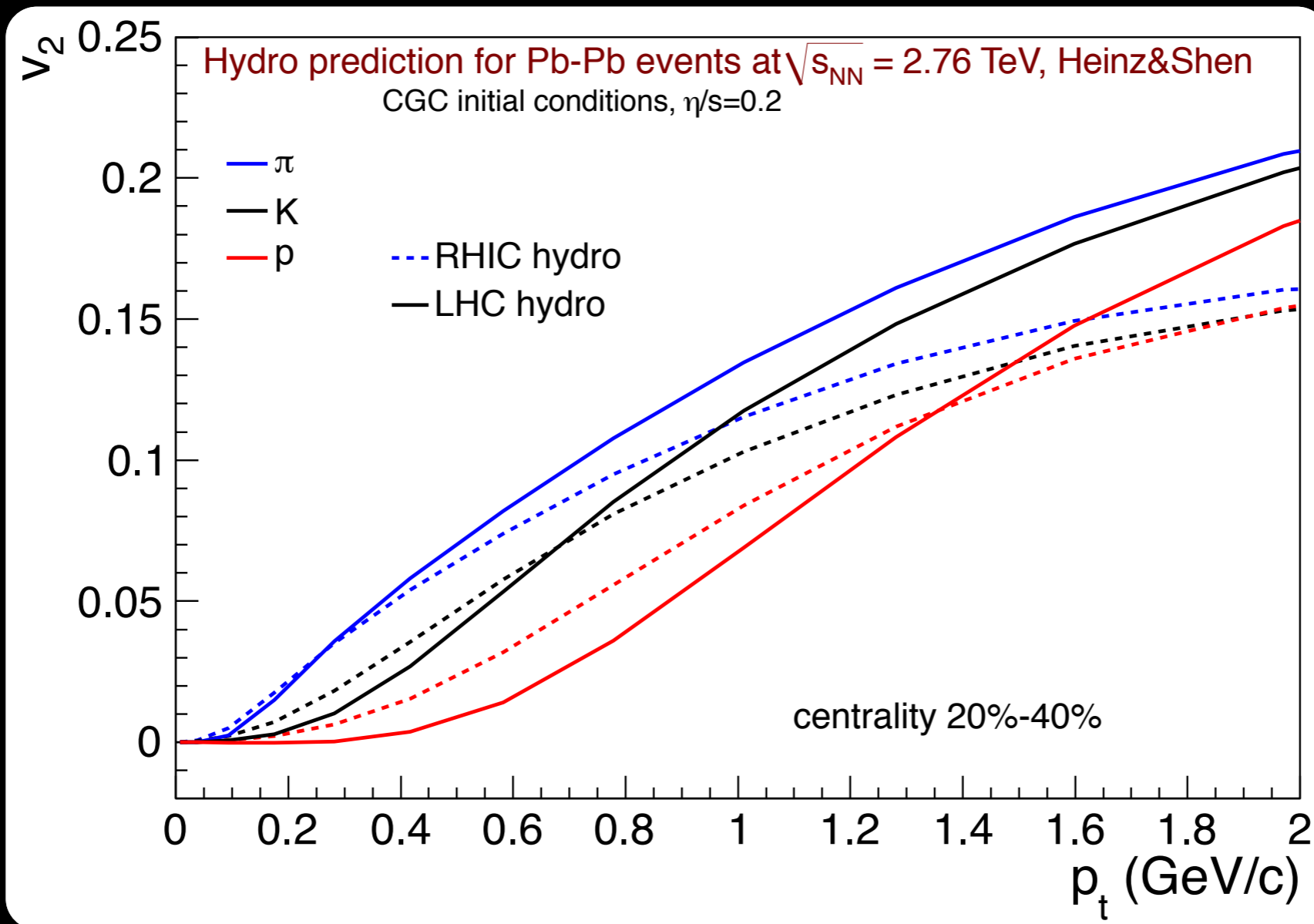
PRL 105, 252302 (2010)



Elliptic flow as function of transverse momentum does not change much from RHIC to LHC energies, can we understand that?

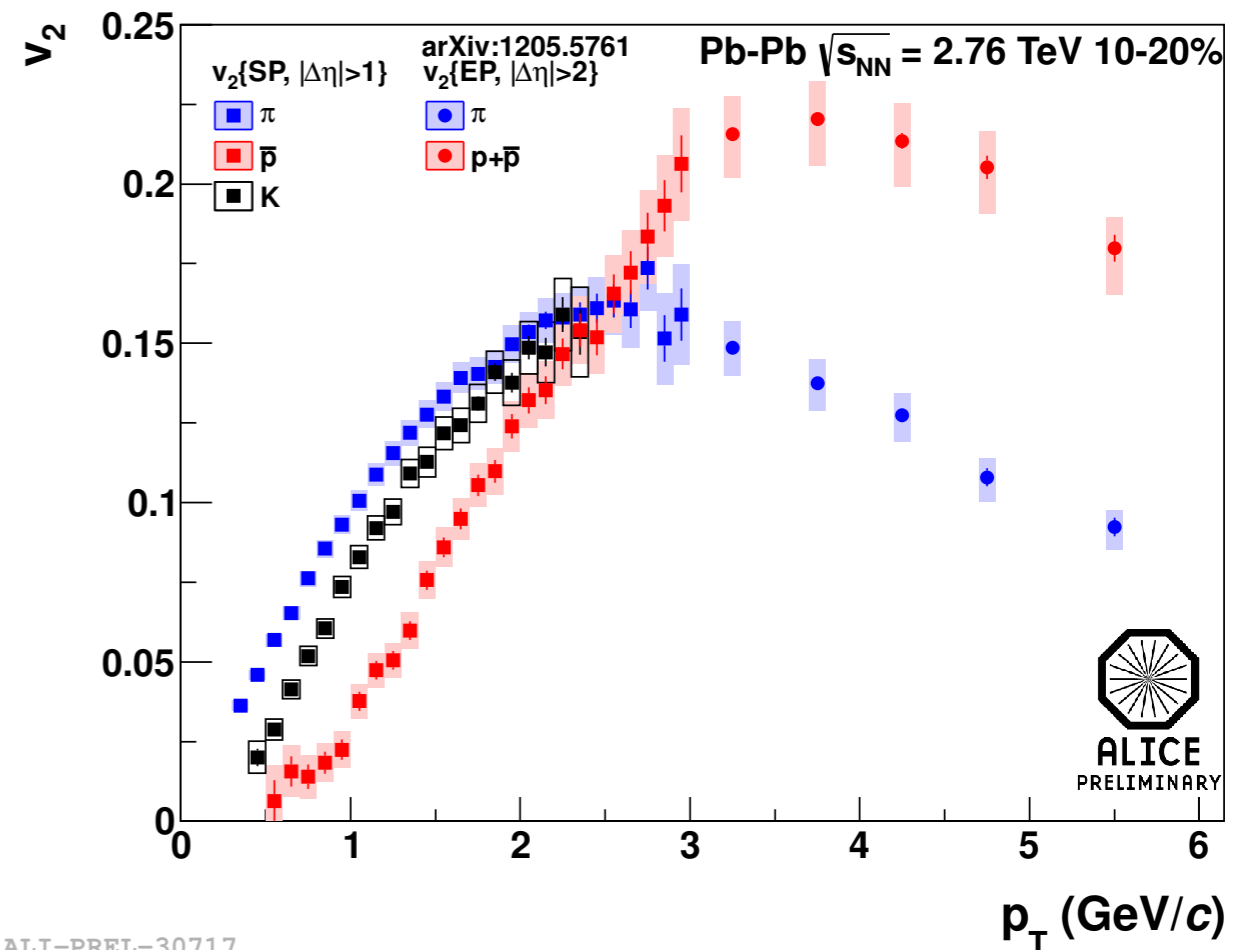
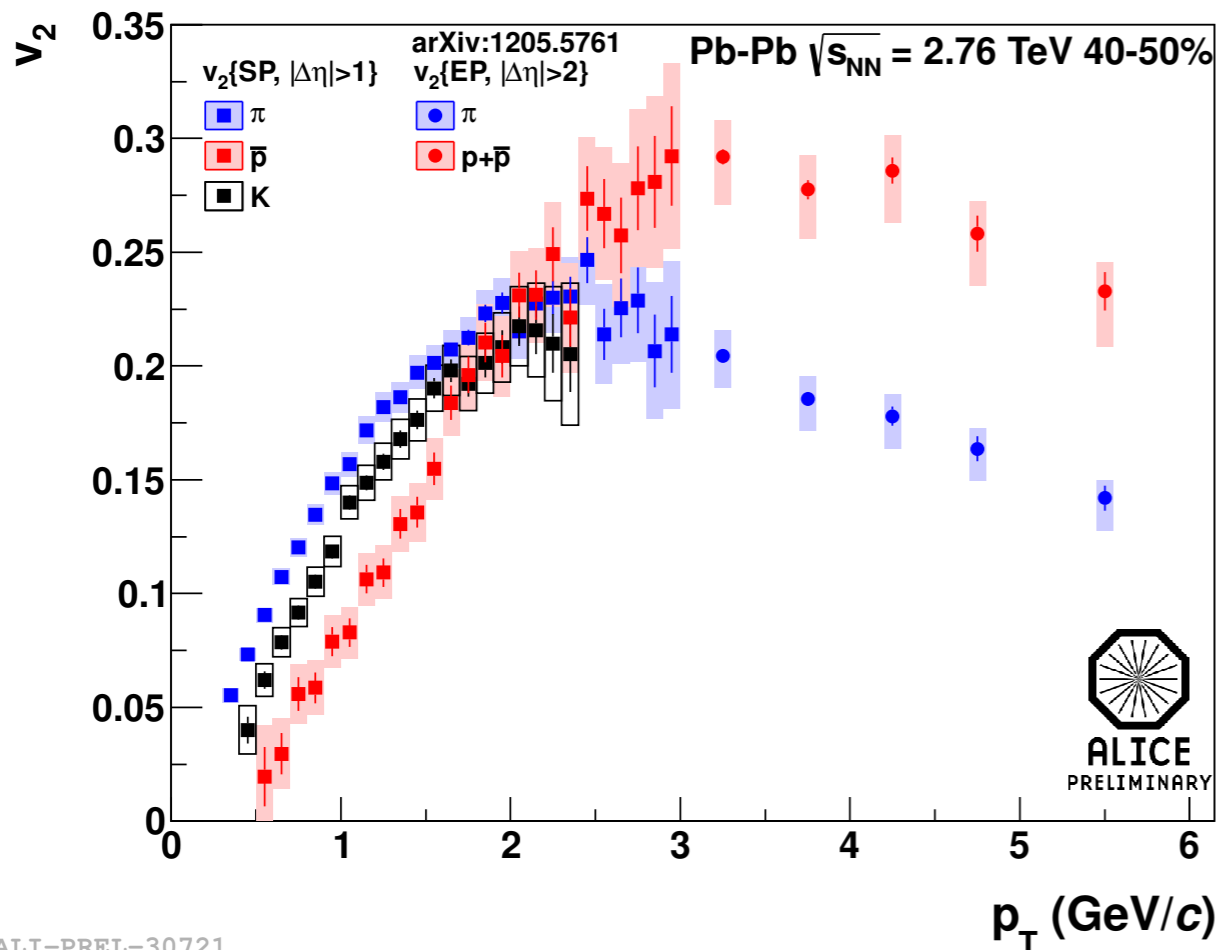
# $v_2$ as function of $p_t$

Hydro: Shen, Heinz, Huovinen & Song, arXiv:1105.3226



Charged particle flow sums contributions of different mass particles which do individually change significantly as function of beam energy according to hydro  
This prediction we can test

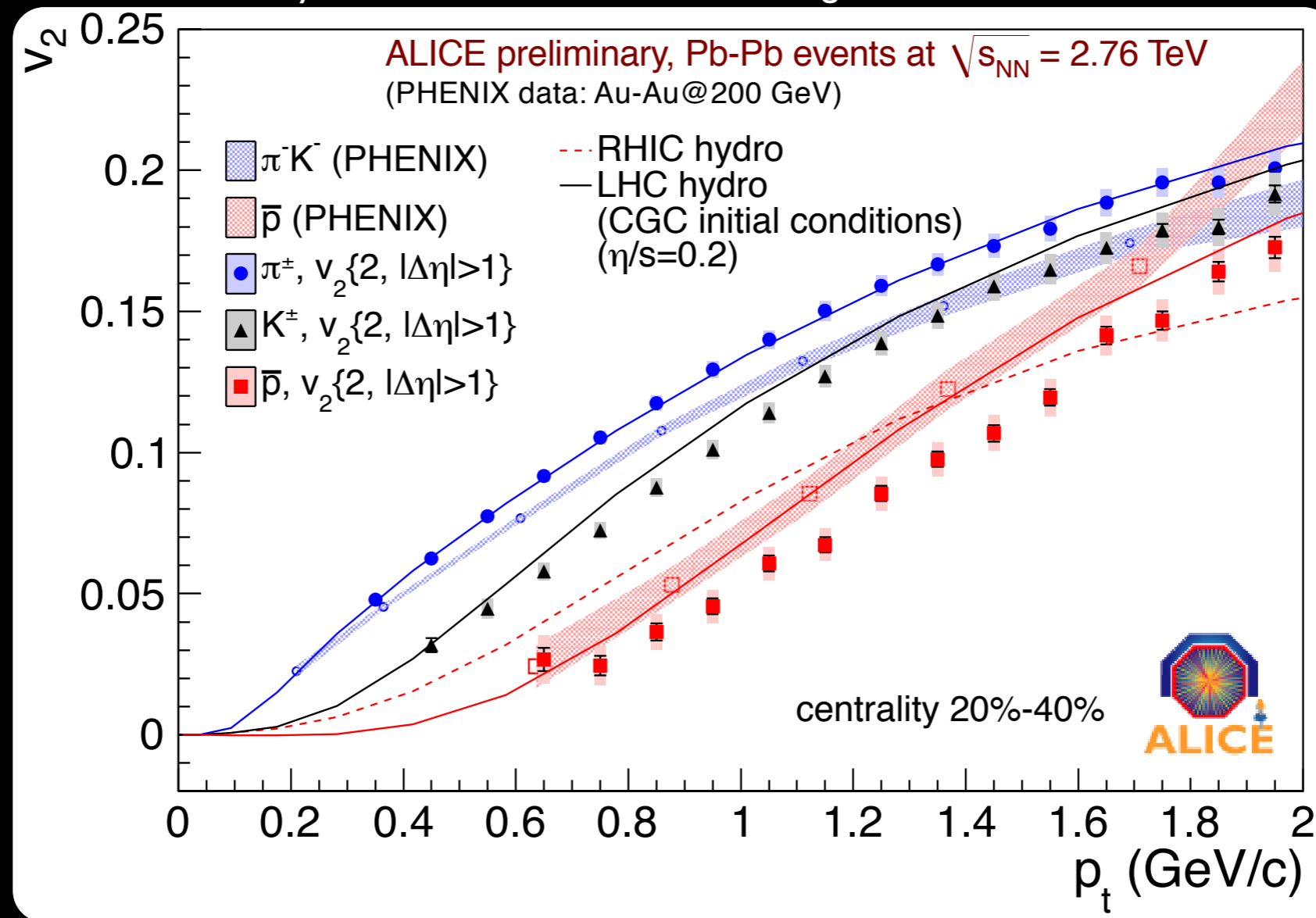
# Mass dependence of $v_2(p_T)$



centrality dependence clearly shows the effect of increasing radial flow

# Mass dependence of $v_2(p_t)$

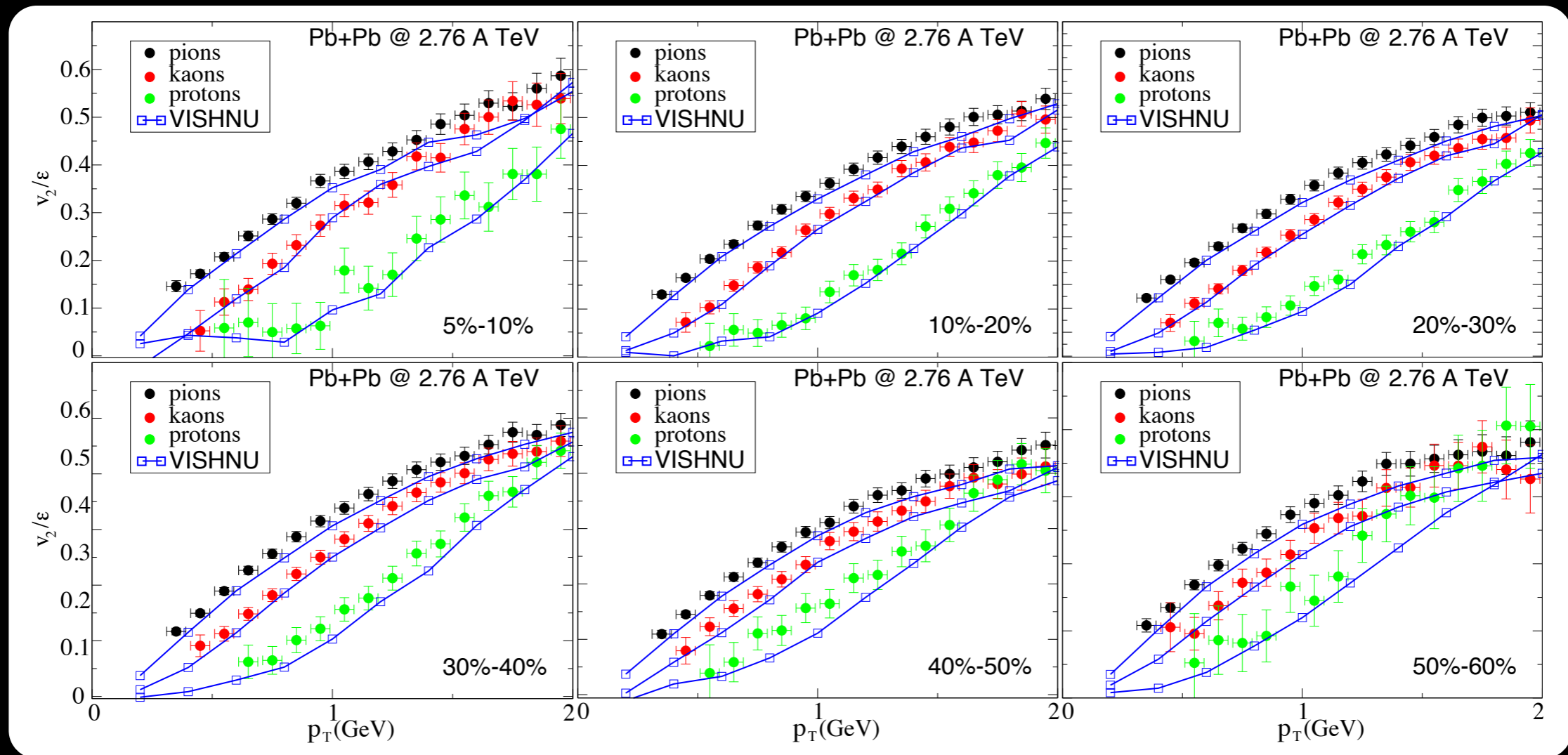
Hydro: Shen, Heinz, Huovinen & Song, arXiv:1105.3226



viscous hydro does capture energy dependence but fails quantitatively for the protons in more central collisions (both for RHIC and the LHC!)

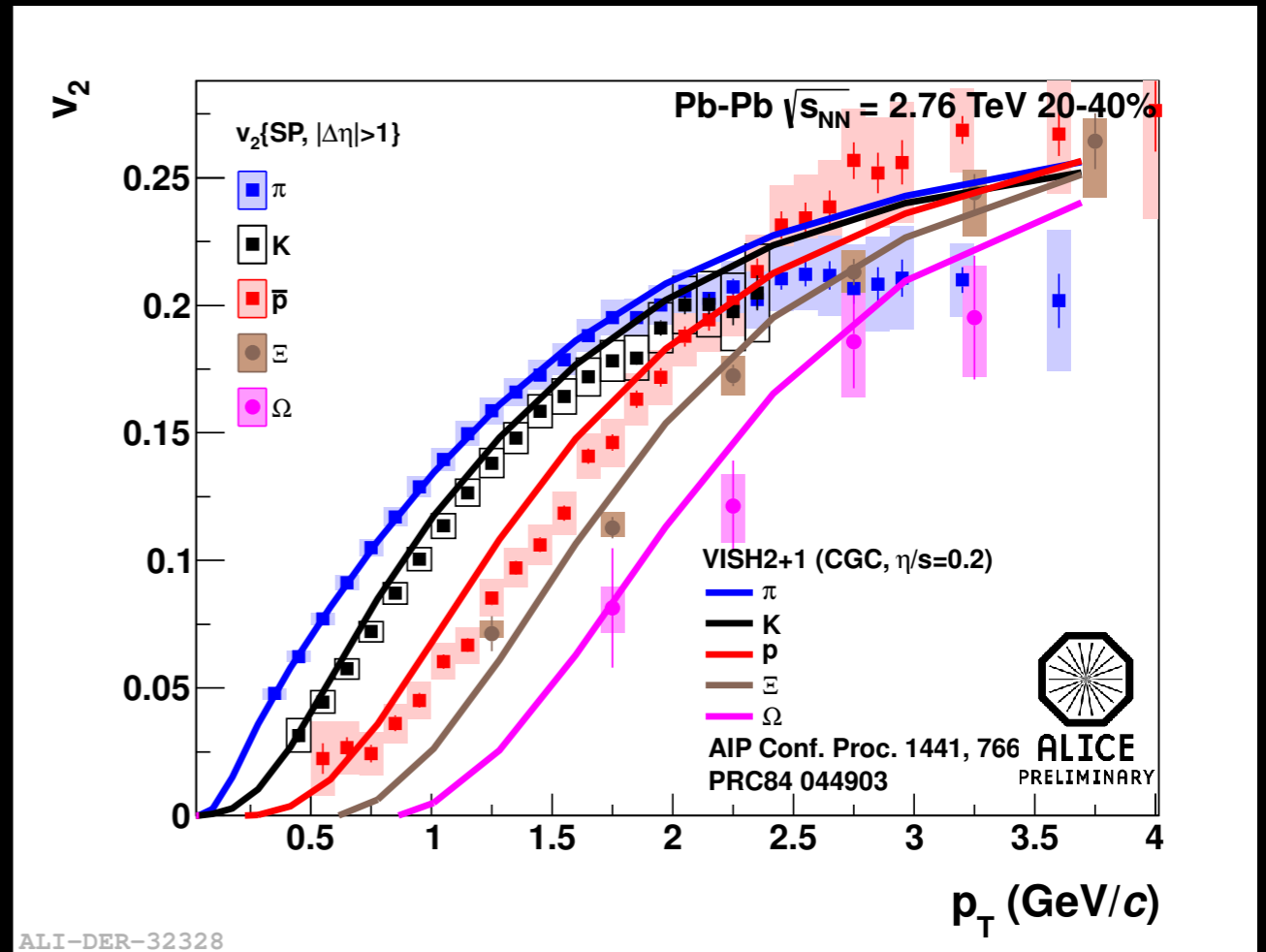
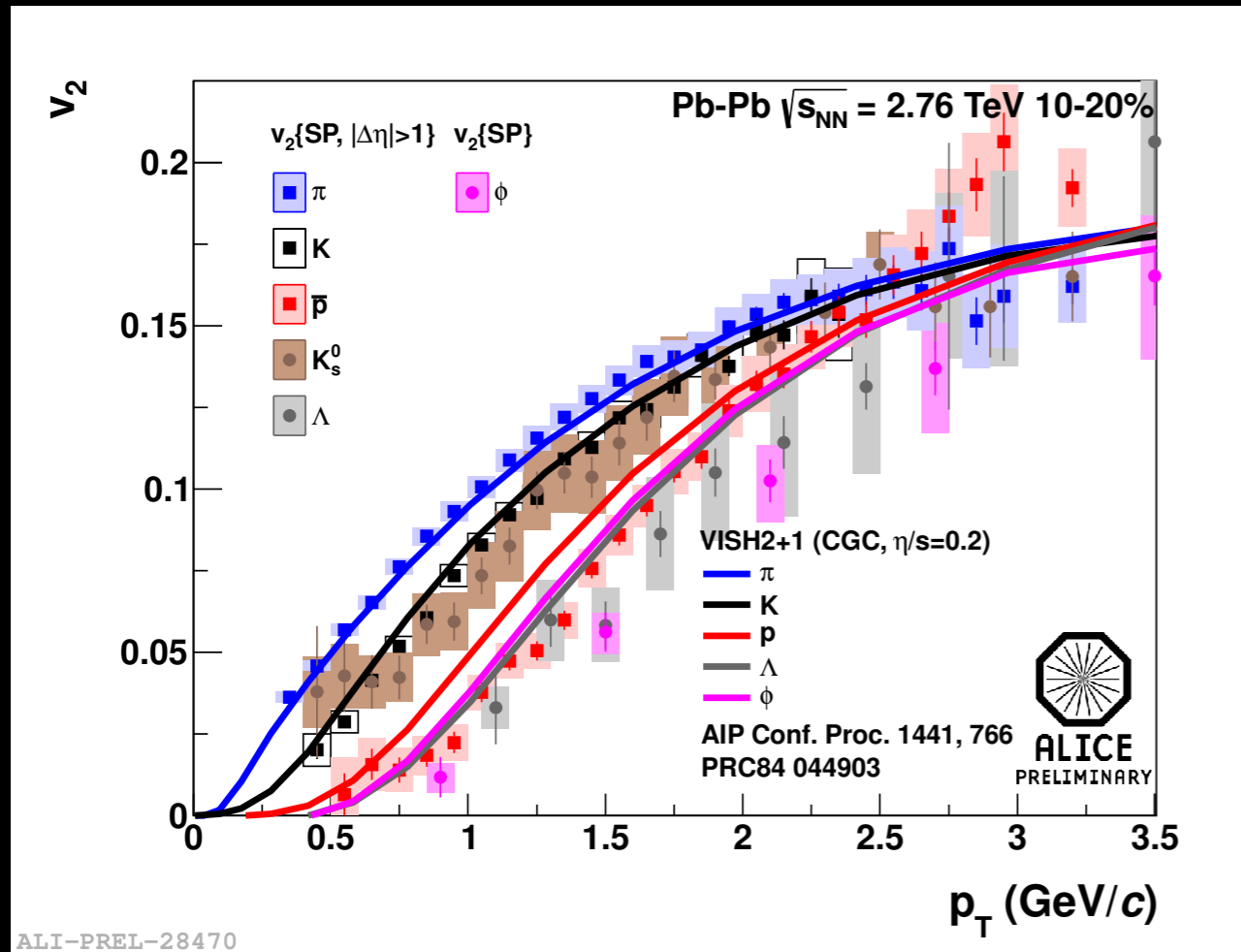
# Mass dependence of $v_2(p_t)$

U. Heinz, C. Shen, and H. Song arXiv:1108.5323



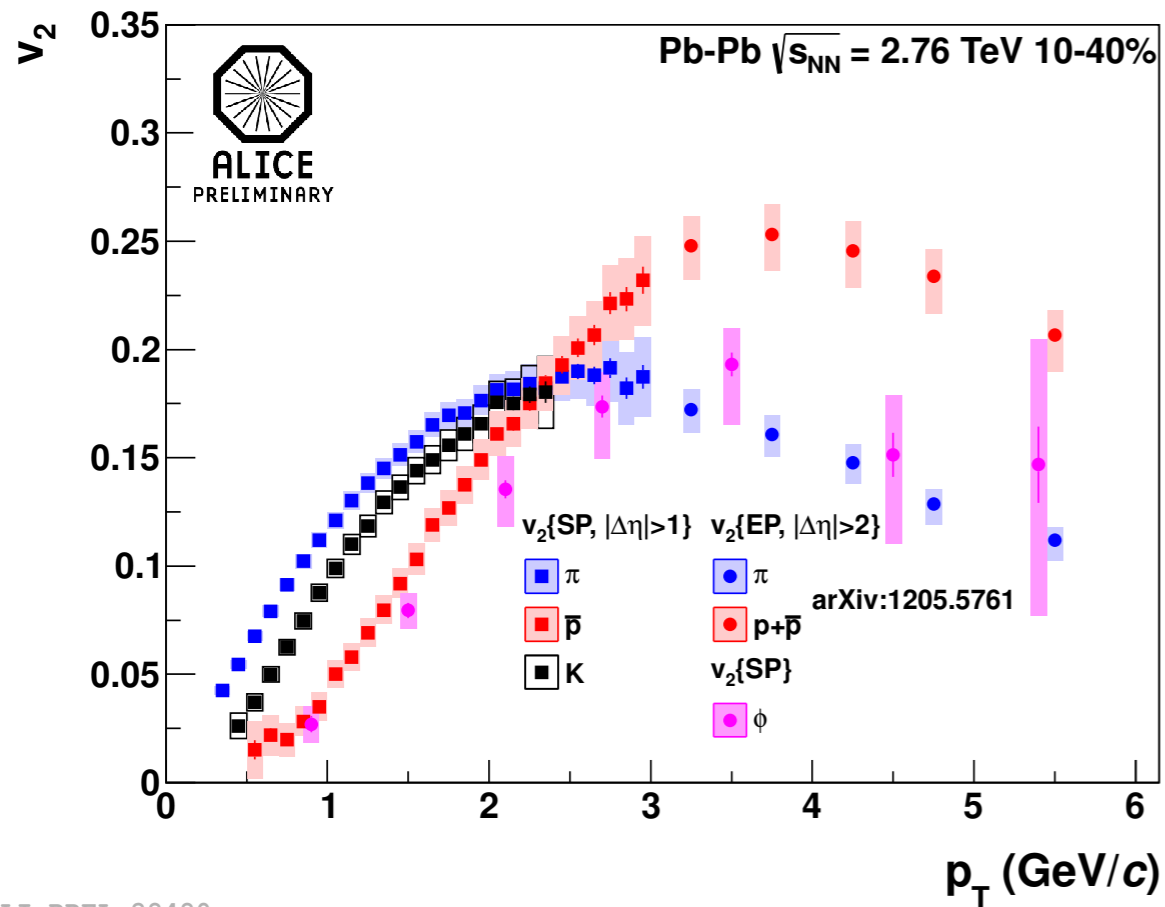
Hybrid calculations (VISHNU) fix the more central collisions  
Is there a strong contribution from the hadronic phase?

# Mass dependence of $v_2(p_T)$

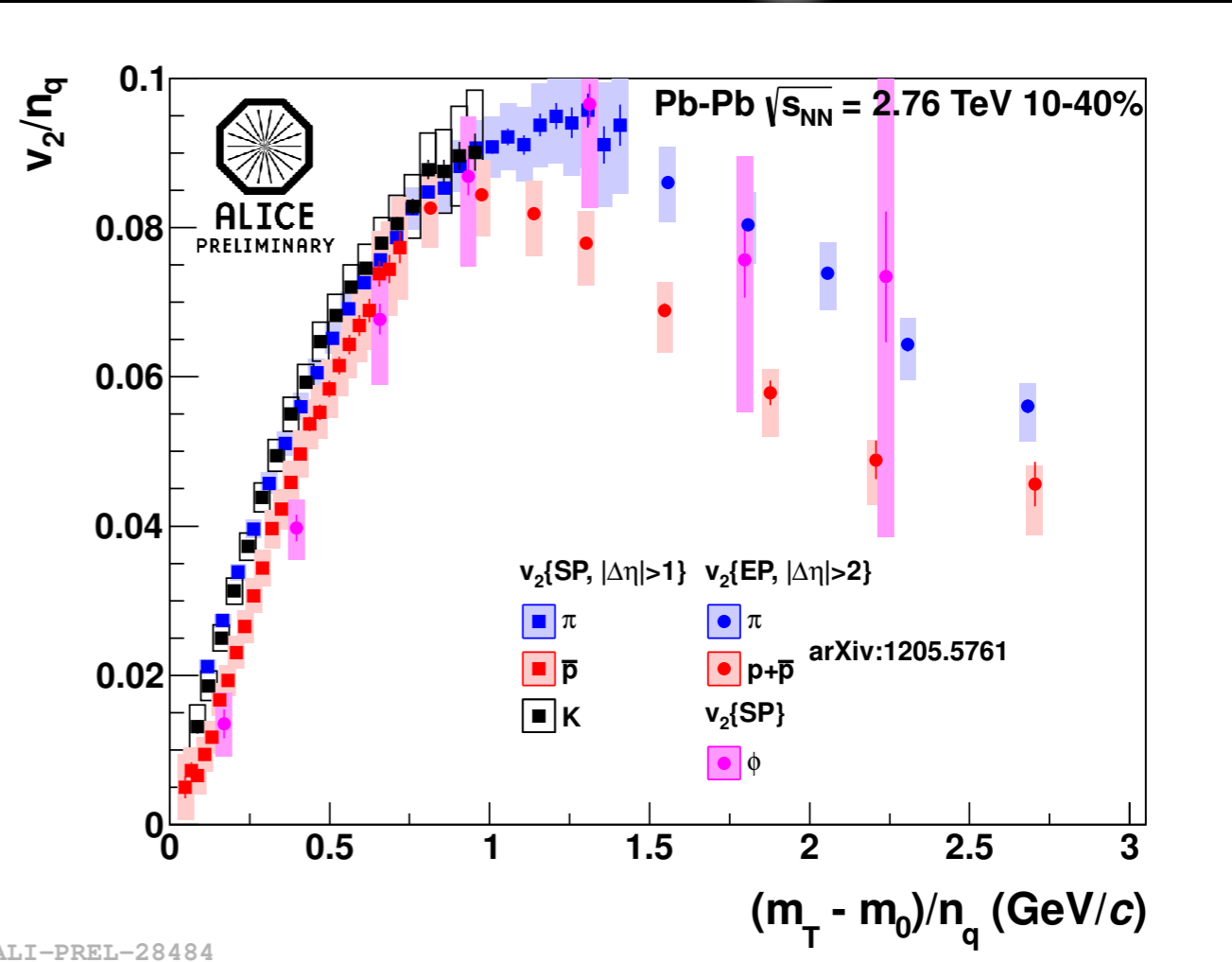


The phi meson is also not described by pure viscous hydro  
 The multi-strange baryons are closer to viscous hydro  
 Is this in line with expectations from an hadronic contribution?

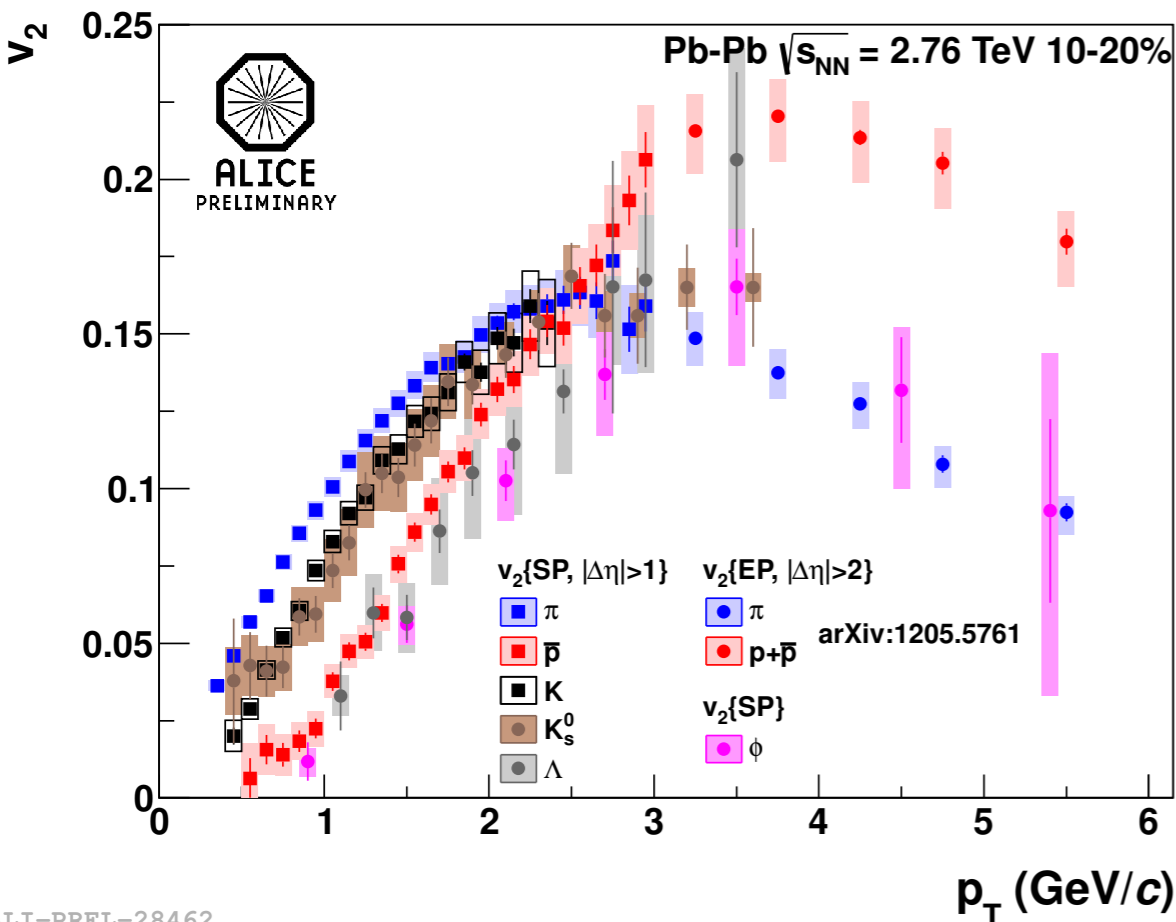
# Scaling?



ALI-PREL-28480



ALI-PREL-28484



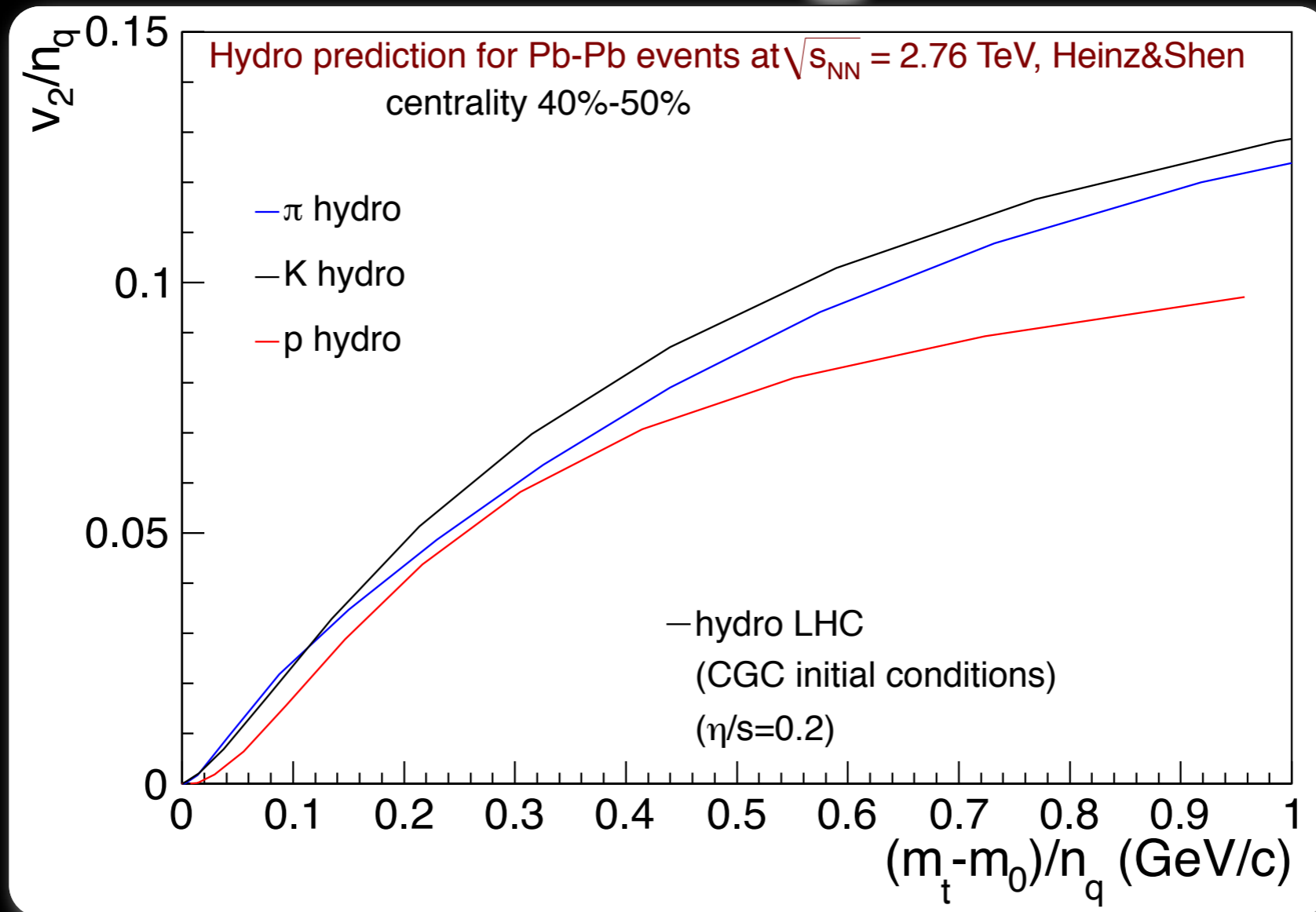
ALI-PREL-28462

The phi meson follows at low- $p_T$  the mass scaling while at intermediate  $p_T$  follows the pions as would be expected in a reco picture  
 No KET scaling observed



# Scaling?

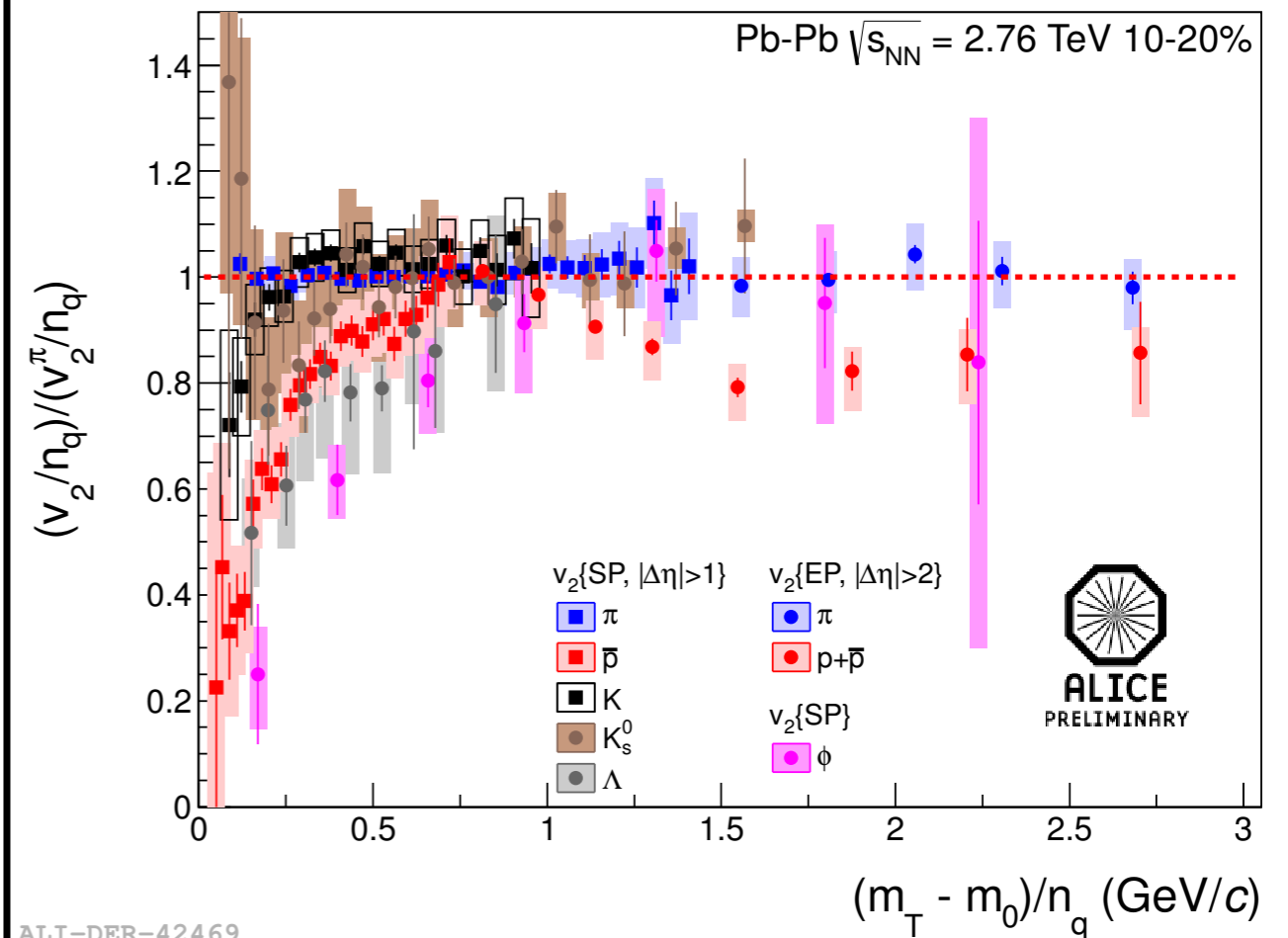
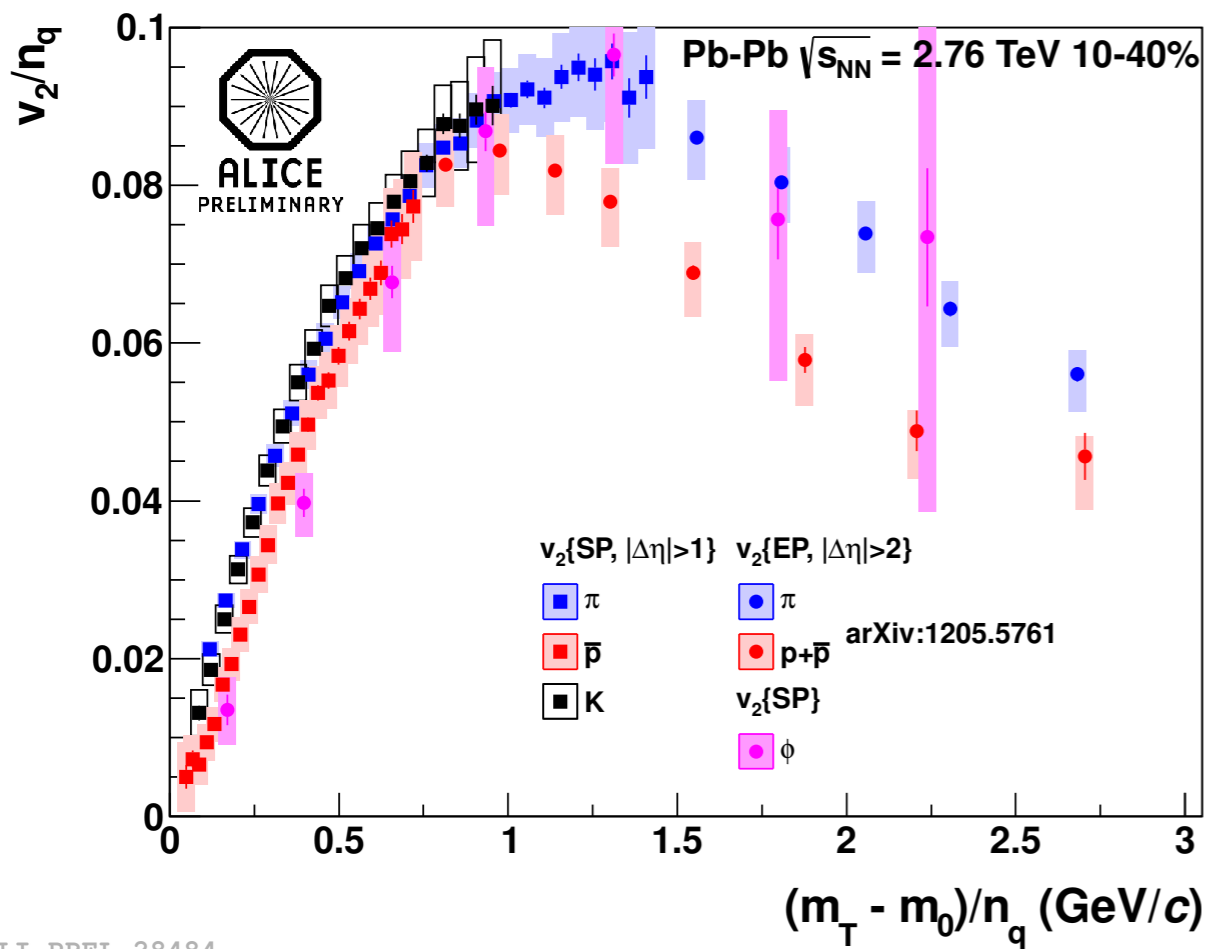
Hydro: Shen, Heinz, Huovinen & Song, arXiv:1105.3226



Viscous hydro and many (most?) models do not show a universal scaling versus KET

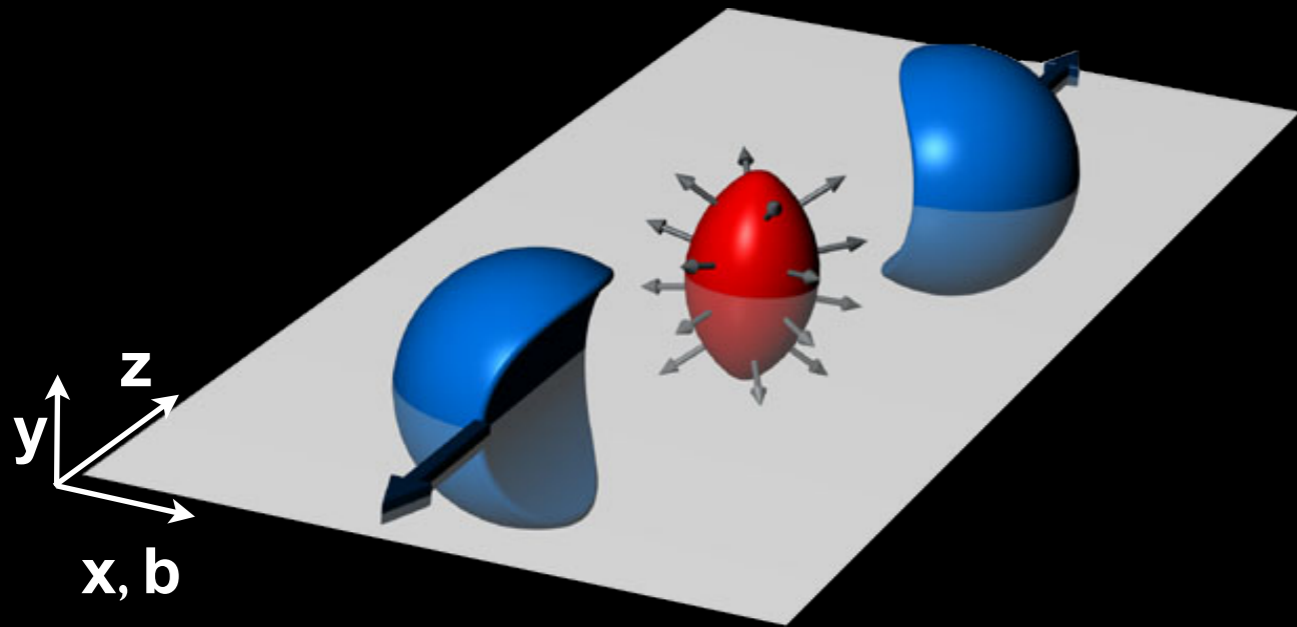
In a simple blast-wave model how well the scaling works depends on the magnitude of the transverse flow

# Scaling?



At low  $p_t$  the mass ordering of the breaking of the KET scaling in the data is in agreement with that in viscous hydro

# Anisotropic Flow



Azimuthal distributions of particles measured with respect to the reaction plane (spanned by impact parameter vector and beam axis) are not isotropic.

$$E \frac{d^3 N}{d^3 \vec{p}} = \frac{1}{2\pi} \frac{d^2 N}{p_T dp_T dy} \left( 1 + \sum_{n=1}^{\infty} 2v_n \cos(n(\phi - \Psi_{RP})) \right)$$

$$v_n = \langle \cos n(\phi - \Psi_{RP}) \rangle$$

harmonics  $v_n$  quantify anisotropic flow

S.Voloshin and Y. Zhang (1996)

# $v_n$ is not an observable

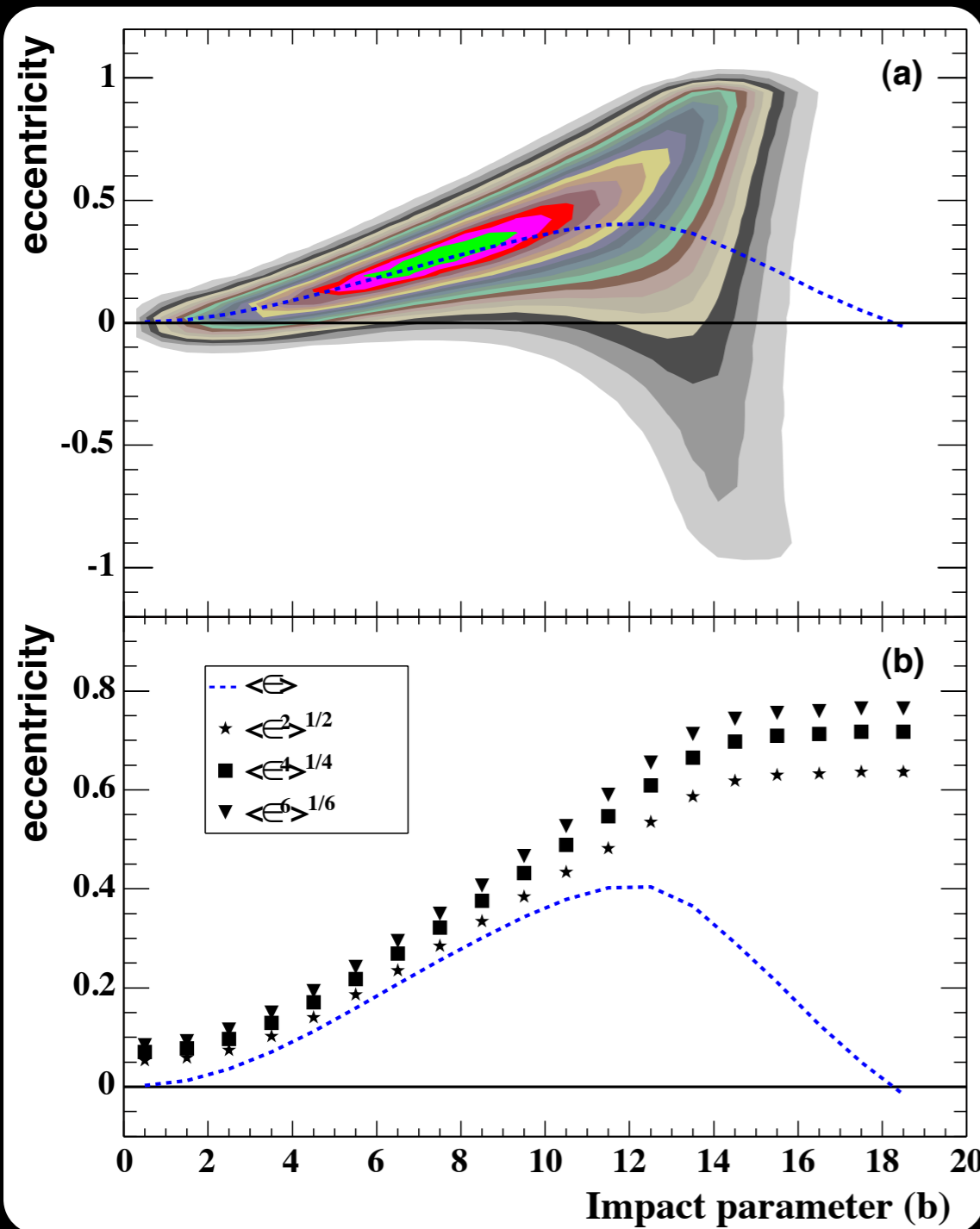
$$\langle v_n \rangle = \langle \langle e^{in(\phi_1 - \Psi_n)} \rangle \rangle$$

- since the common symmetry planes cannot be measured event-by-event, we measure quantities which do not depend on it's orientation: multi-particle azimuthal correlations

$$\begin{aligned} \langle \langle e^{in(\phi_1 - \phi_2)} \rangle \rangle &= \langle \langle e^{in(\phi_1 - \Psi_n - (\phi_2 - \Psi_n))} \rangle \rangle \\ &= \langle \langle e^{in(\phi_1 - \Psi_n)} \rangle \langle e^{-in(\phi_2 - \Psi_n)} \rangle \rangle \\ &= \langle v_n^2 \rangle \end{aligned}$$

- **assuming** that **only** correlations with the symmetry plane are present - not a very good assumption (jets, resonances, etc)!

# $v_2$ fluctuations



M. Miller and RS, arXiv:nucl-ex/0312008

- If  $v_2$  fluctuates

$$\langle v_2 \rangle \neq \sqrt{\langle (v_2)^2 \rangle}$$

- If

$$v_2 \propto \epsilon$$

- $\rightarrow$  fluctuations in the initial conditions change our various observables related to  $v_2$

eccentricity fluctuations and its possible effect on  $v_2$  measurements:

M. Miller and RS, arXiv:nucl-ex/0312008 (2003)

participant eccentricity

PHOBOS QM2005: Nucl. Phys. A774: 523 (2006)

# Flow Fluctuations

when (2-particle) nonflow is corrected for or negligible!

in limit of “small” (not necessarily Gaussian) fluctuations

$$v_n^2\{2\} = \bar{v}_n^2 + \sigma_v^2$$

$$v_n^2\{4\} = \bar{v}_n^2 - \sigma_v^2$$

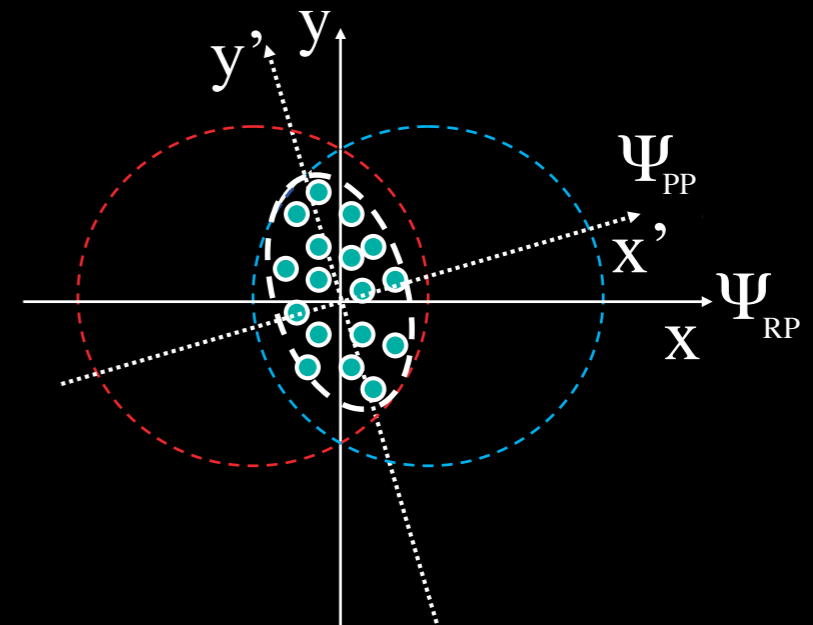
$$v_n^2\{2\} + v_n^2\{4\} = 2\bar{v}_n^2$$

$$v_n^2\{2\} - v_n^2\{4\} = 2\sigma_v^2$$

in limit of only (Gaussian) fluctuations

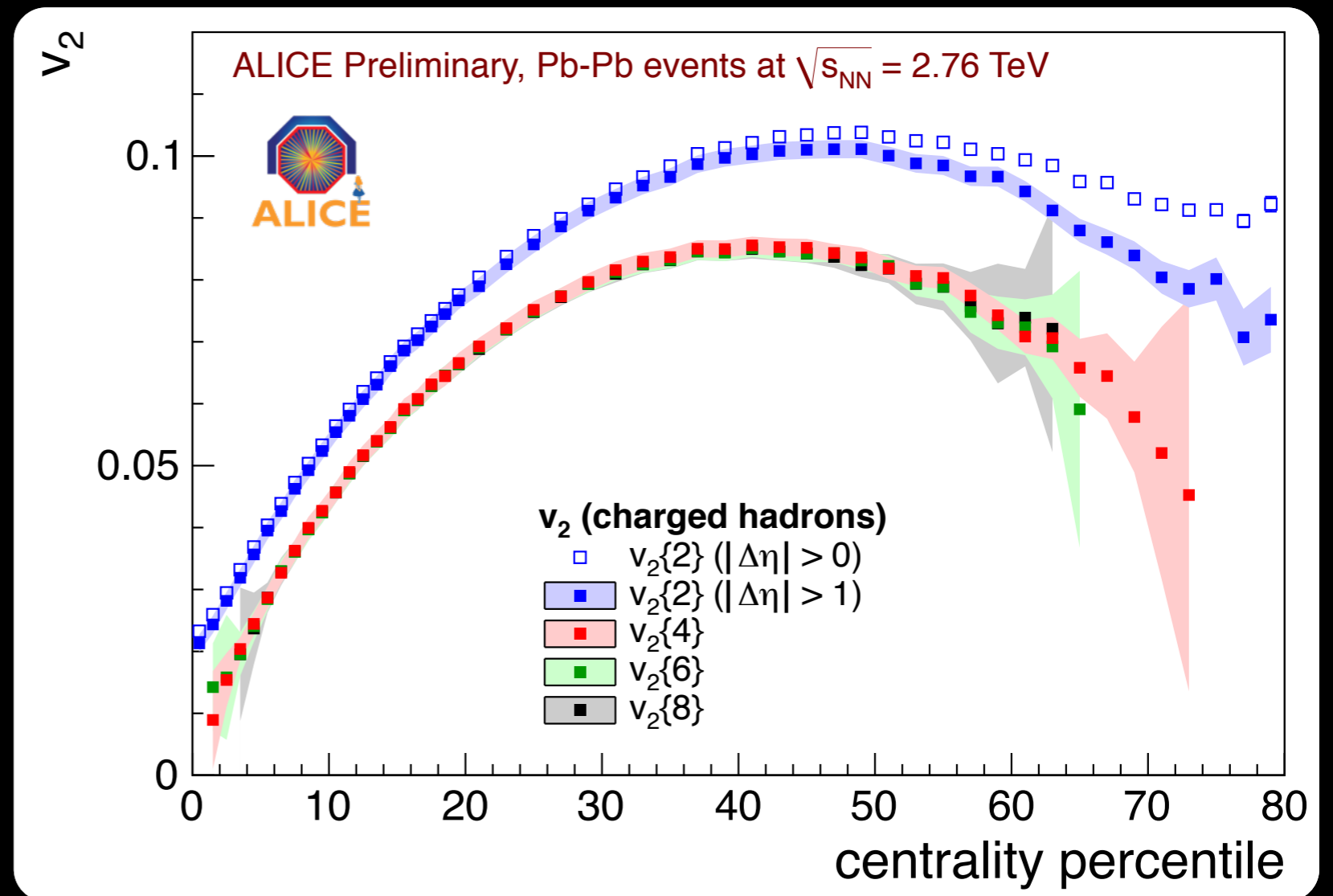
$$v_n\{4\} = 0$$

$$v_n\{2\} = \frac{2}{\sqrt{\pi}}\bar{v}_n$$



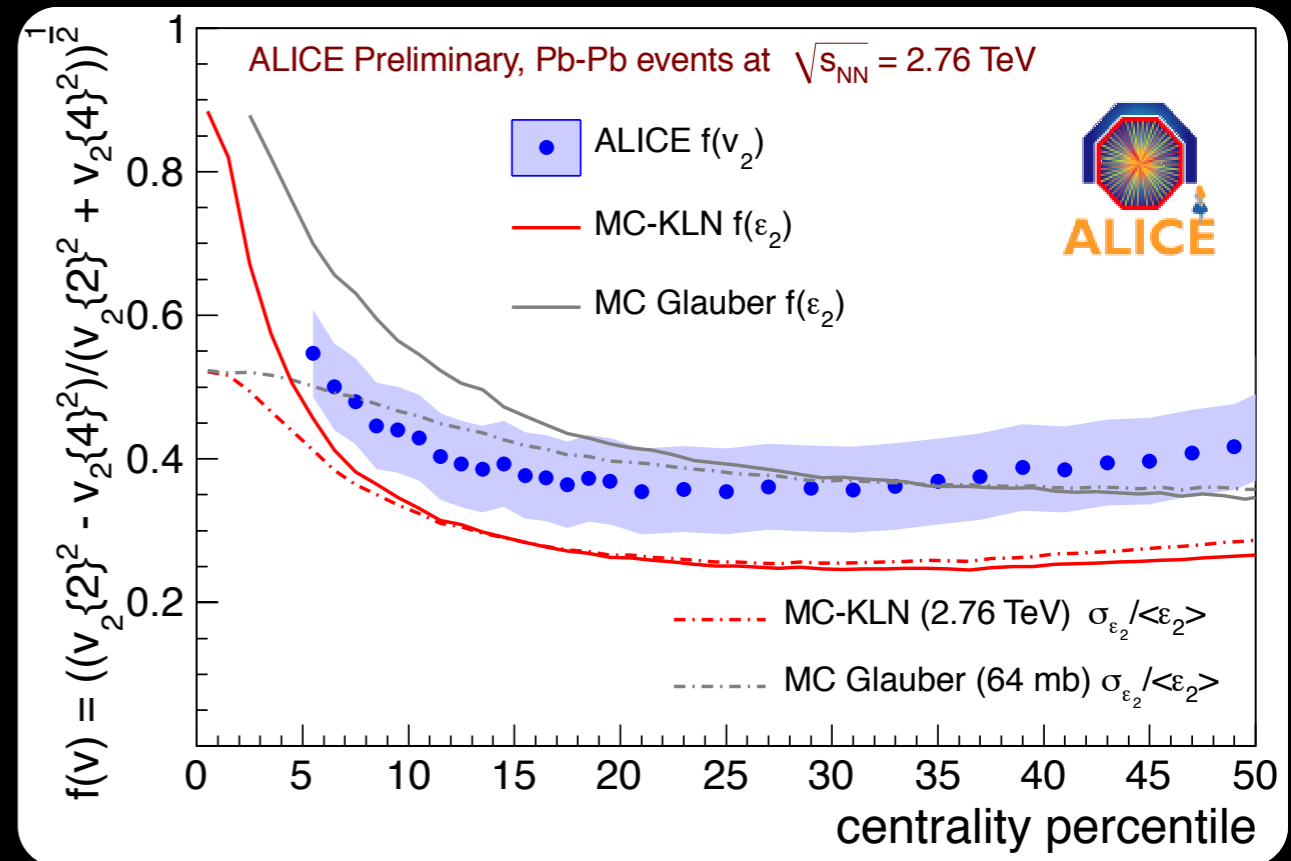
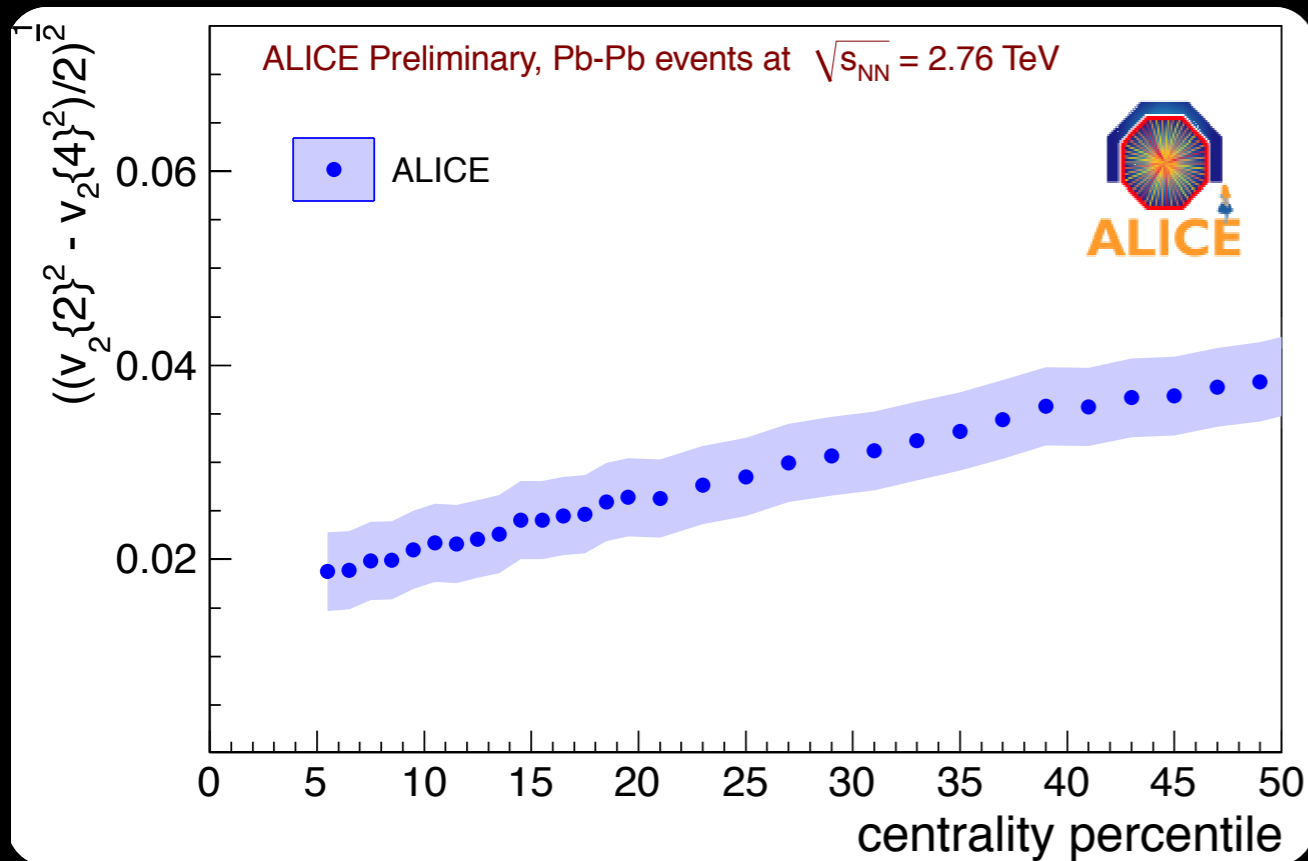
# $v_2$ versus centrality in ALICE

$$\begin{aligned}v\{2\} &= \langle v \rangle + \frac{1}{2} \frac{\sigma_v^2}{\langle v \rangle} \\v\{4\} &= \langle v \rangle - \frac{1}{2} \frac{\sigma_v^2}{\langle v \rangle} \\v\{6\} &= \langle v \rangle - \frac{1}{2} \frac{\sigma_v^2}{\langle v \rangle} \\v\{8\} &= \langle v \rangle - \frac{1}{2} \frac{\sigma_v^2}{\langle v \rangle}\end{aligned}$$



Clear separation between  $v_2\{2\}$  and higher order cumulants  
Higher order cumulant  $v_2$  estimates are consistent within uncertainties

# $v_2$ fluctuations



$$\sigma_{v_n} \simeq \left[ \frac{1}{2} (v_n^2\{2\} - v_n^2\{4\}) \right]^{1/2}$$

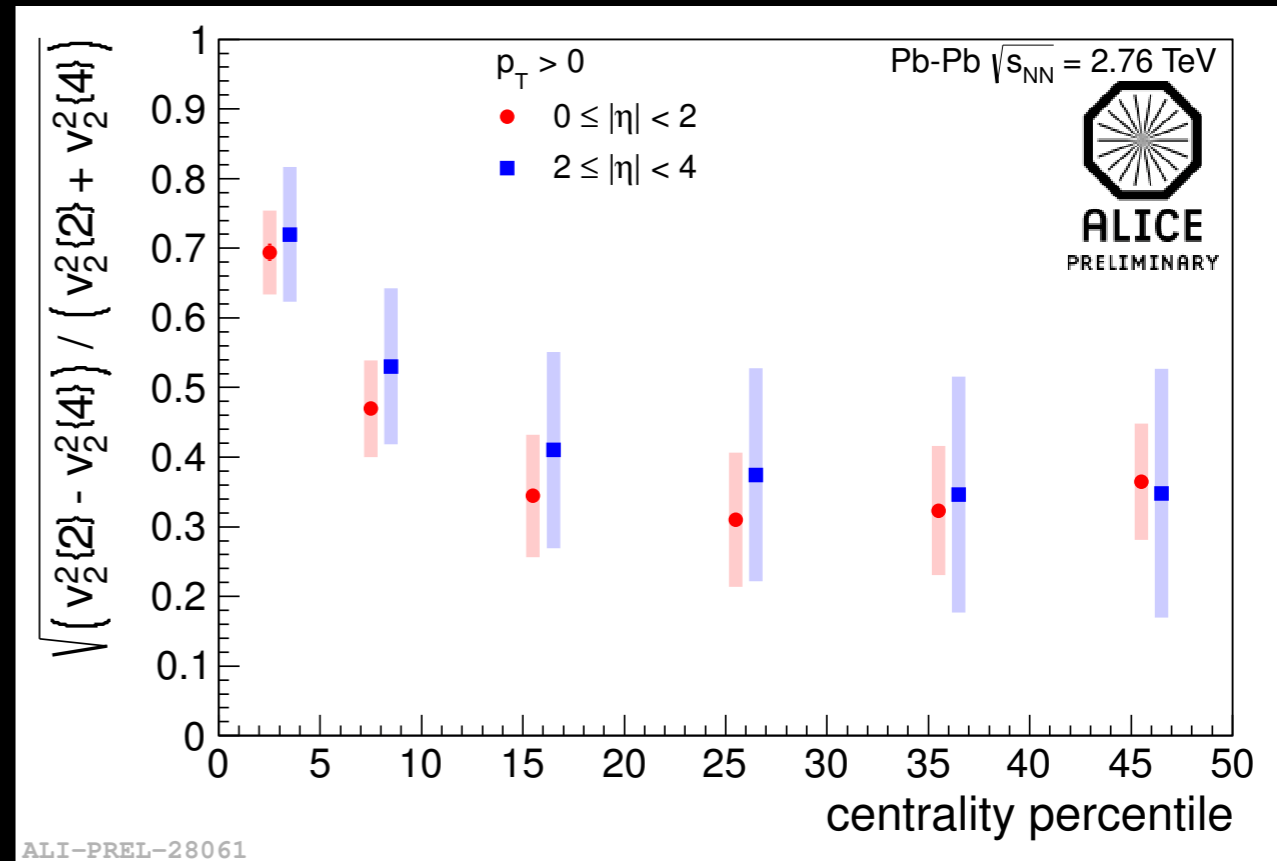
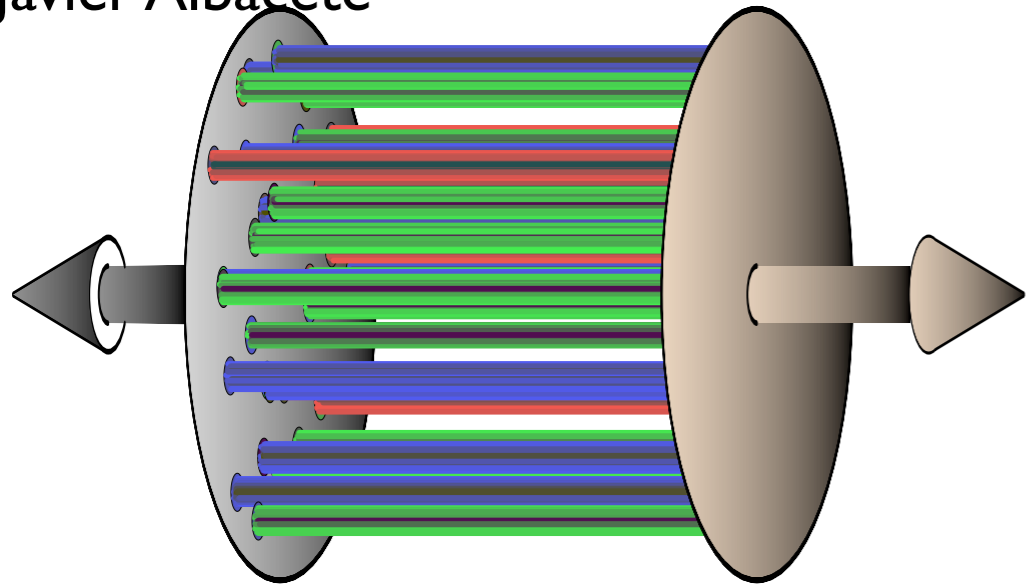
$$\frac{\sigma_{v_n}}{v_n} \simeq \left( \frac{v_n^2\{2\} - v_n^2\{4\}}{v_n^2\{2\} + v_n^2\{4\}} \right)^{1/2}$$

For more central collisions the data is between  
MC Glauber and MC-KLN CGC



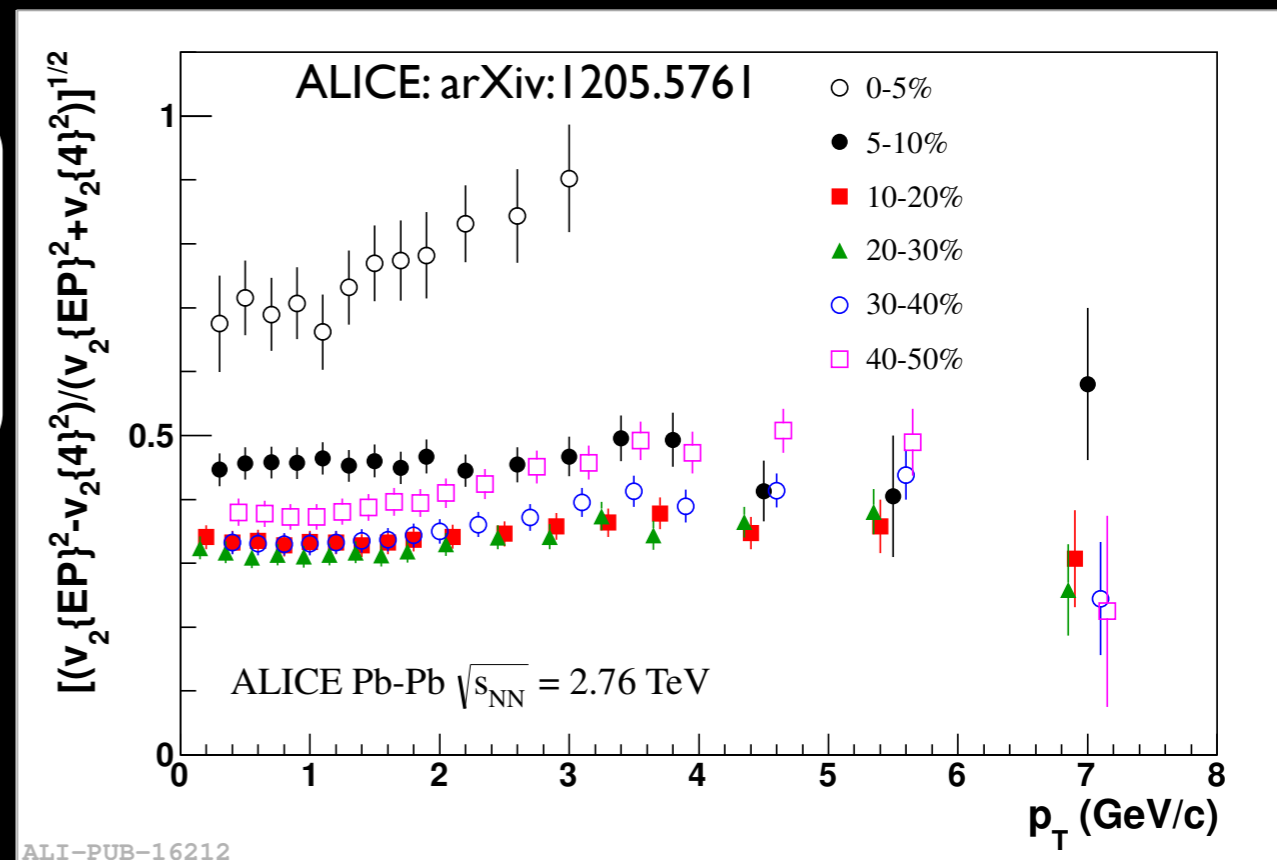
# $v_2$ fluctuations

Javier Albacete



ALI-PREL-28061

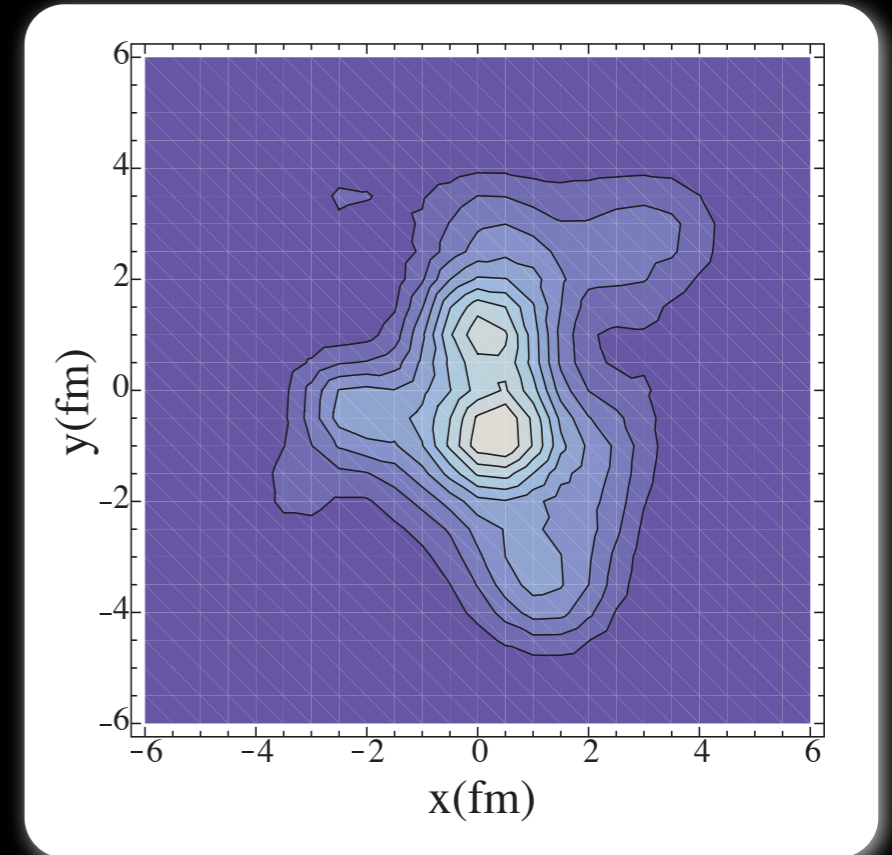
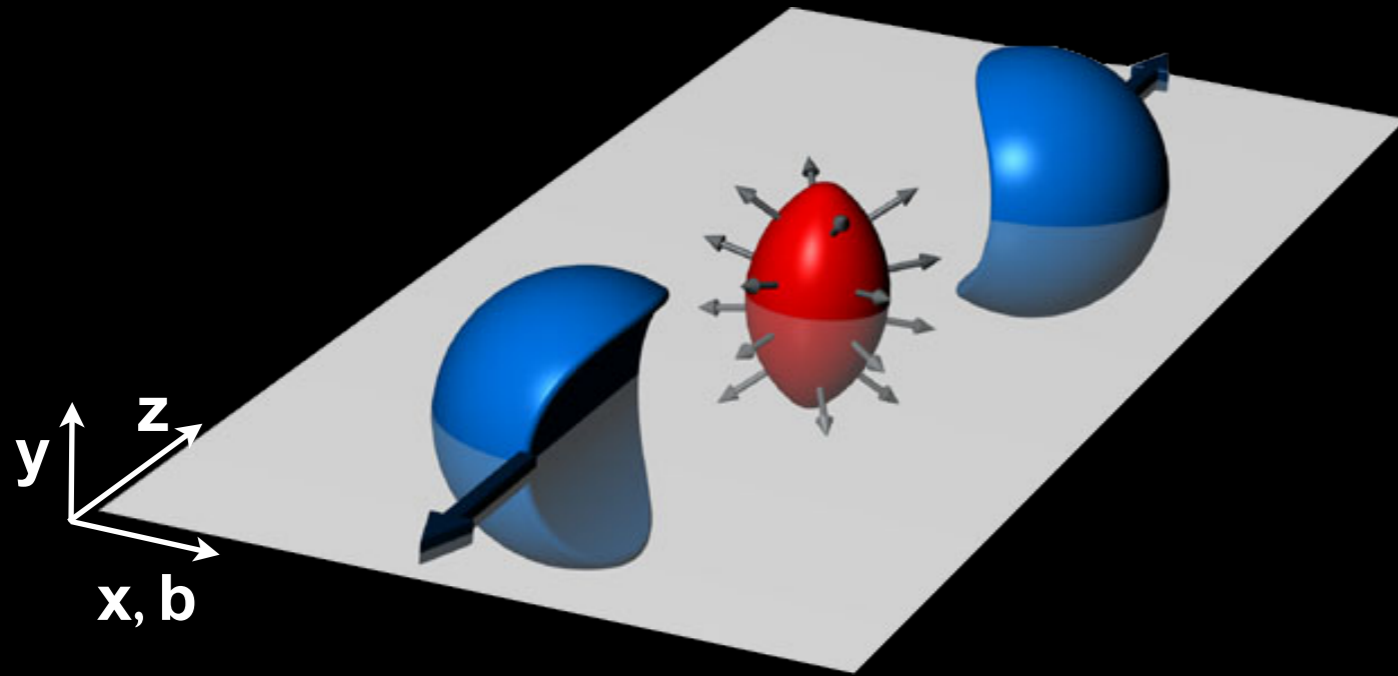
The  $v_2$  fluctuations are very similar as function of  $\eta$  and  $p_t$



ALI-PUB-16212

# Initial conditions and $v_n$

G. Qin, H. Petersen, S. Bass, and B. Muller



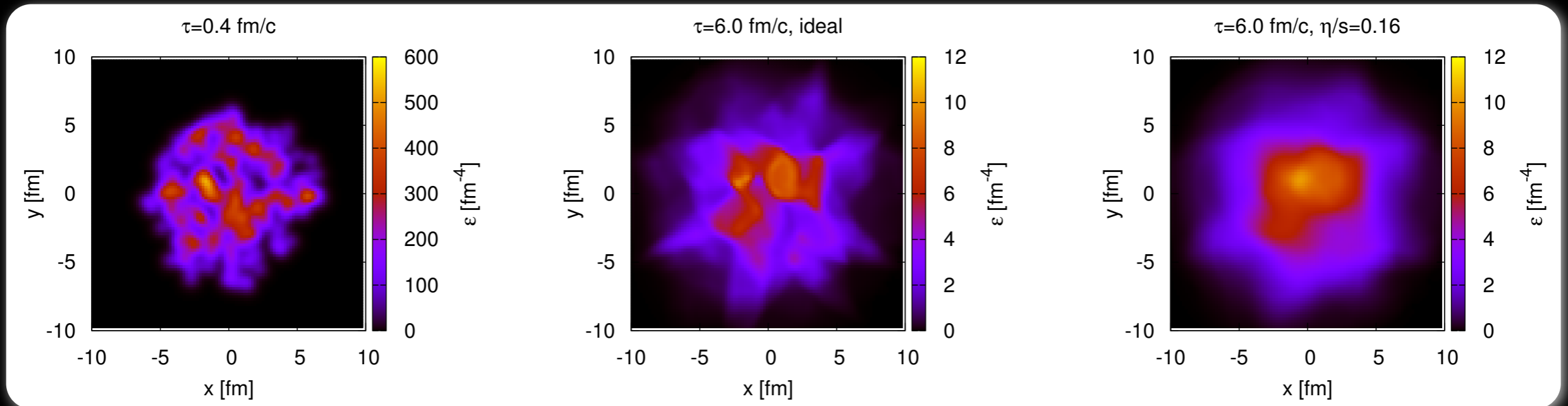
$$\frac{2\pi}{N} \frac{dN}{d\phi} = 1 + \sum_{n=2,4,6,\dots}^{\infty} 2v_n \cos n(\phi - \Psi_R)$$

$$\frac{2\pi}{N} \frac{dN}{d\phi} = 1 + \sum_{n=1}^{\infty} 2v_n \cos n(\phi - \Psi_n)$$

initial spatial geometry not a smooth almond (for which all odd harmonics are zero due to reflection symmetry)  
 may give rise to higher odd harmonics versus their planes of symmetry

# Shear Viscosity

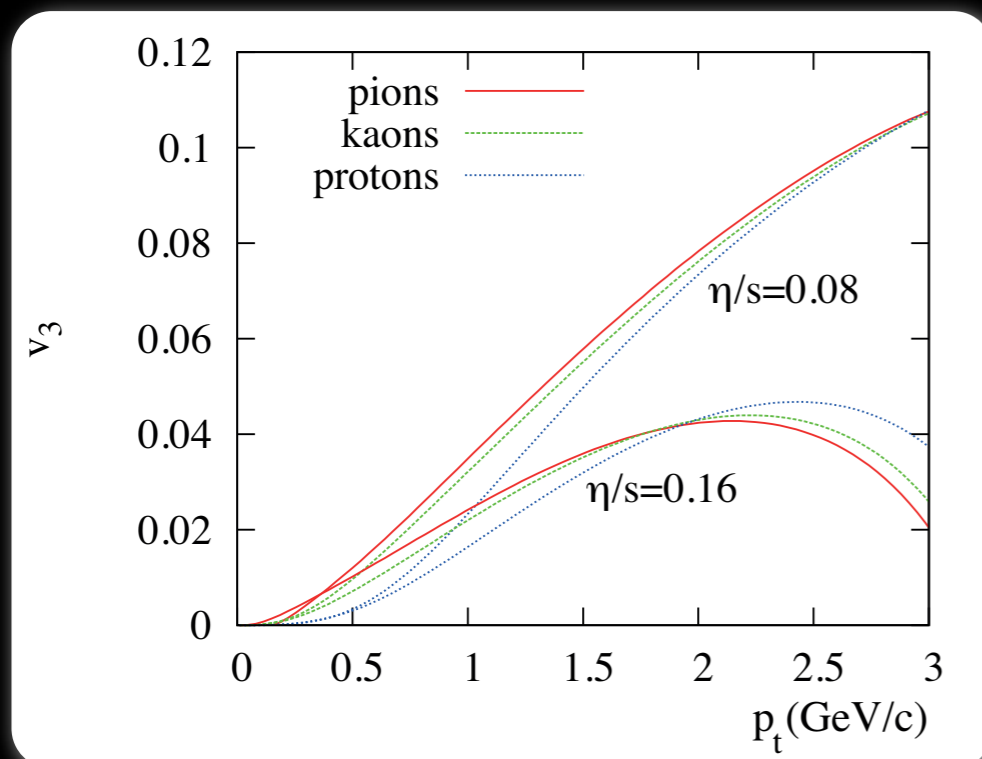
Music, Sangyong Jeon



initial conditions

ideal hydro  $\eta/s=0$

viscous hydro  $\eta/s=0.16$

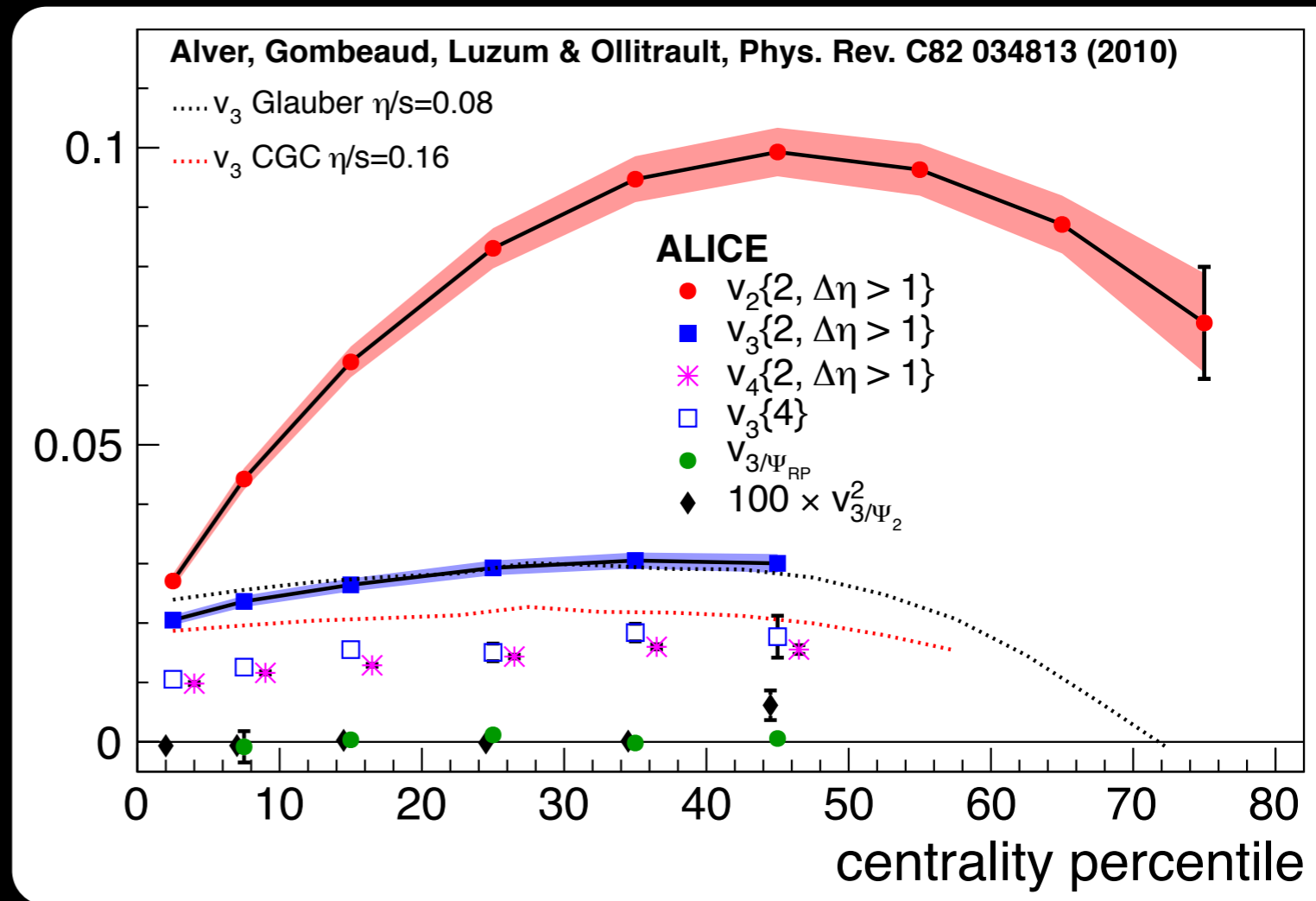


Larger  $\eta/s$  clearly smoothes the distributions and suppresses the higher harmonics (e.g.  $v_3$ )

# the $v_n$ 's

The  $v_3$  with respect to the reaction plane determined in the ZDC and with the  $v_2$  participant plane is consistent with zero as expected if  $v_3$  is due to fluctuations of the initial eccentricity

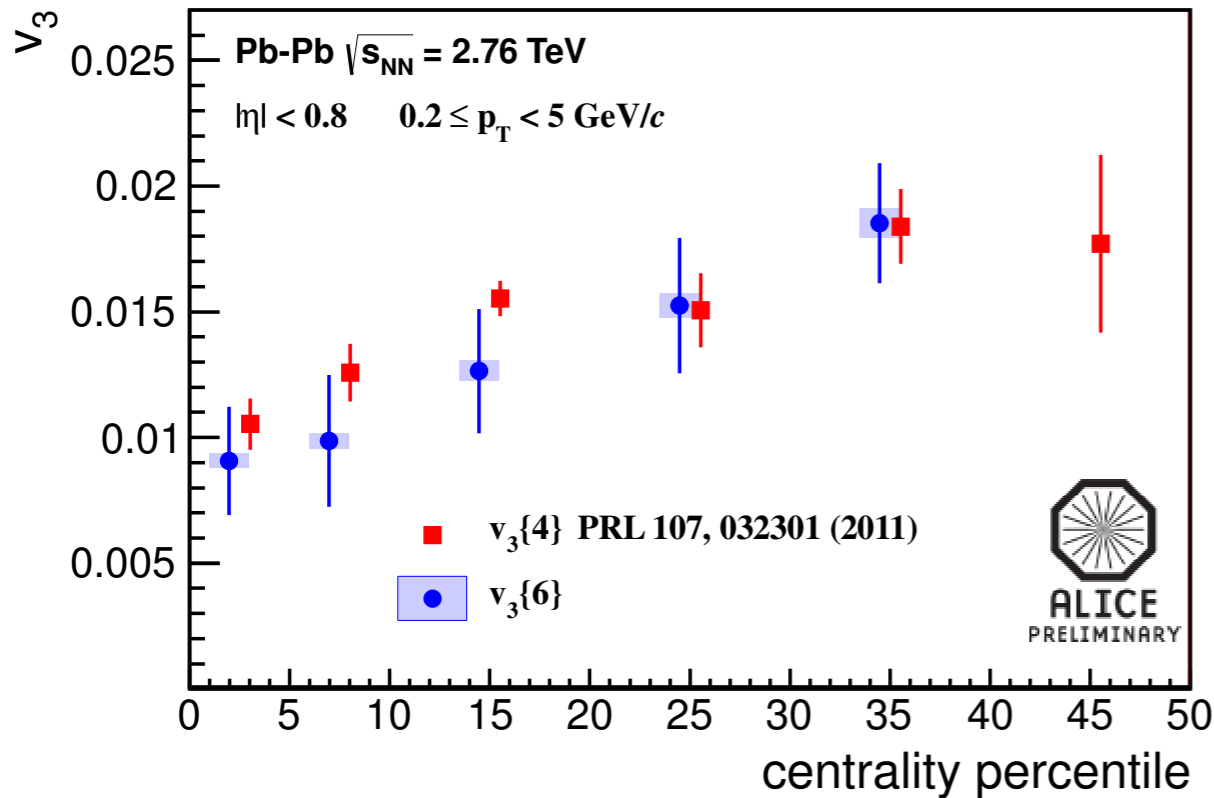
The  $v_3\{2\}$  is about two times larger than  $v_3\{4\}$  which is also consistent with expectations based on initial eccentricity fluctuations



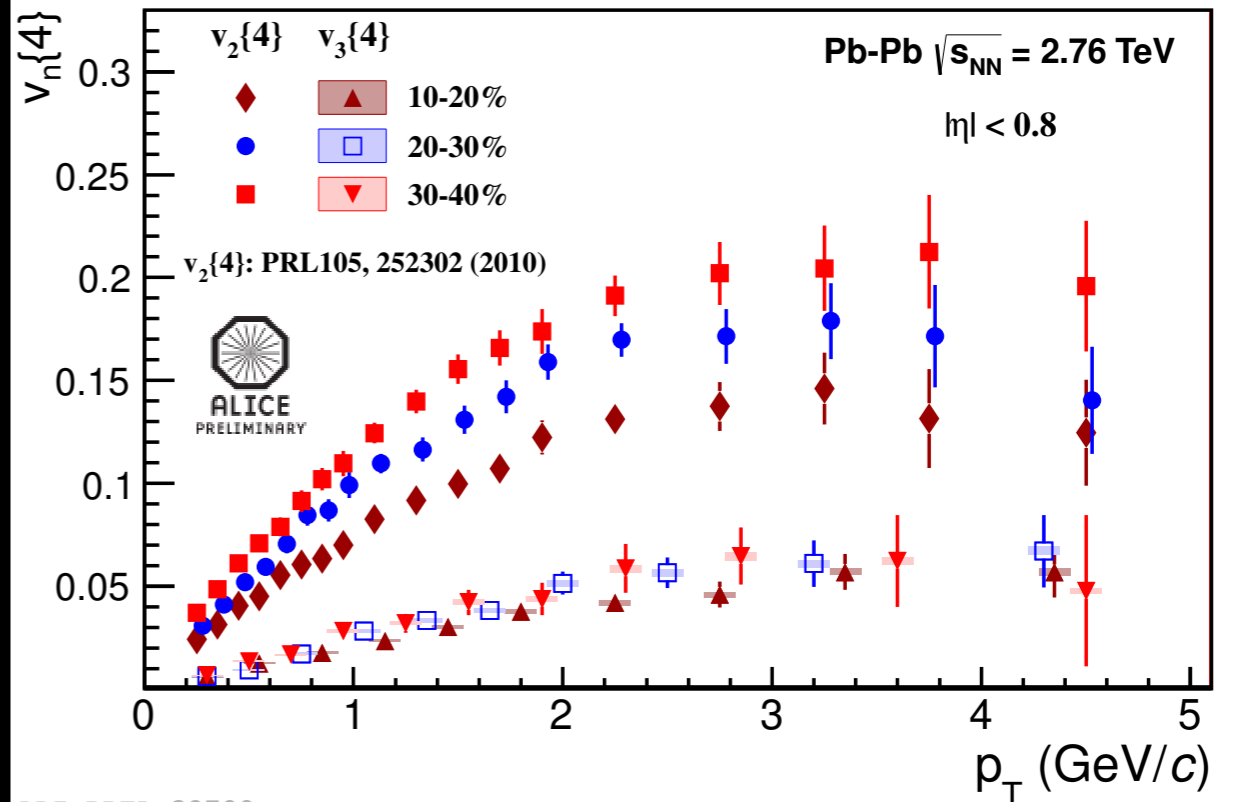
ALICE Collaboration, arXiv:1105.3865  
PRL 107 (2011) 032301

We observe significant  $v_3$  and  $v_4$  which compared to  $v_2$  has a different centrality dependence (strong constrain for  $\eta/s$ )

# V3



ALI-PREL-29357

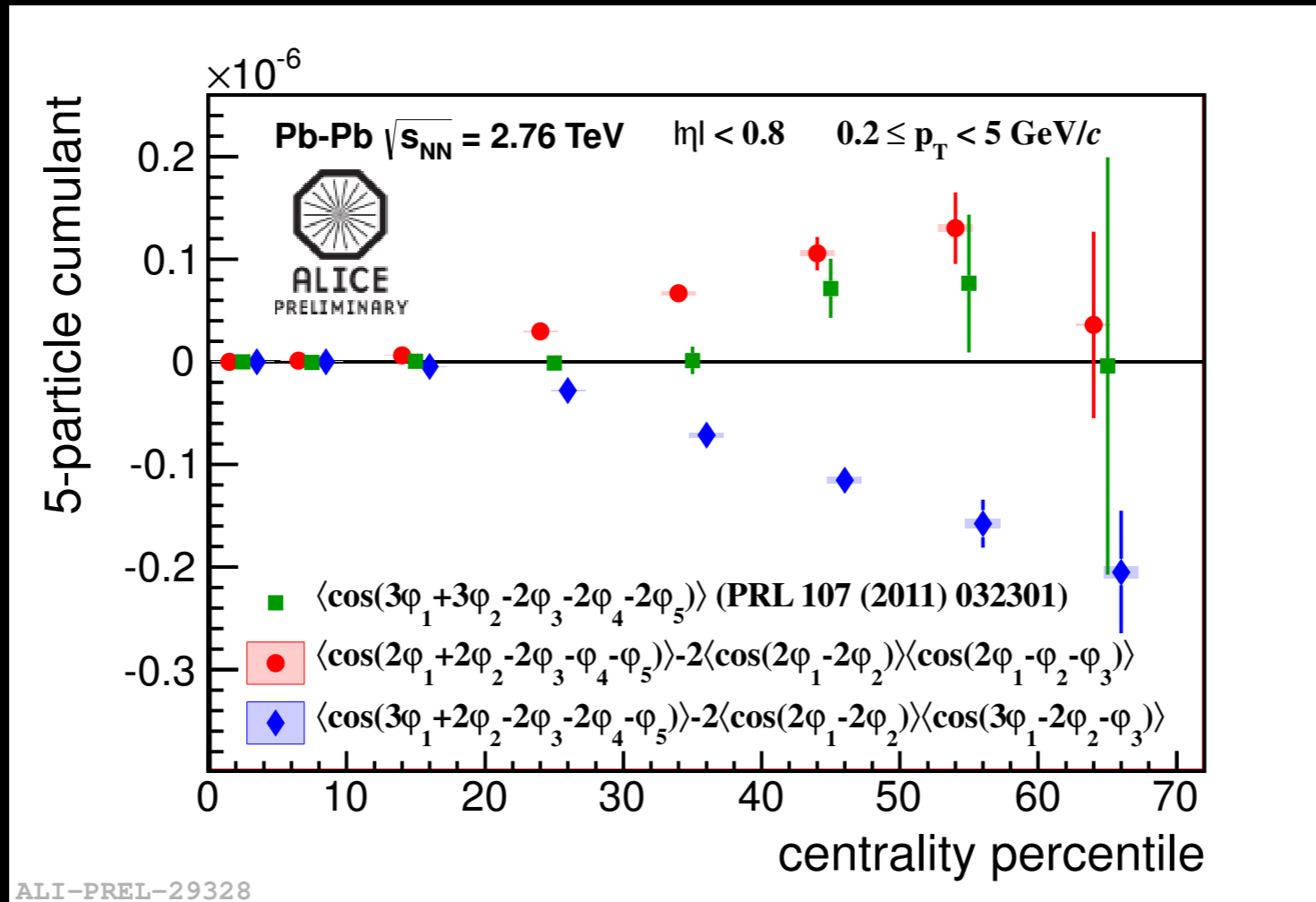


ALI-PREL-32788

We observe as for  $v_2$  that  $v_3\{4\}$  and  $v_3\{6\}$  agree within errors and the difference of about a factor 2 between  $v_3\{2\}$  and  $v_3\{4\}$  and  $v_3\{6\}$  matches that observed in Glauber calculations (indication of the number of sources?)

We can now even measure the  $p_t$  dependence of  $v_3$  using higher order cumulants

# Correlations between $v_n$



$$\langle \cos(3\phi_1 + 3\phi_2 - 2\phi_3 - 2\phi_4 - 2\phi_5) \rangle = v_3^2 v_2^3 \cos[6(\Psi_3 - \Psi_2)]$$

$$\langle \cos(2\phi_1 + 2\phi_2 - 2\phi_3 - \phi_4 - \phi_5) \rangle - 2\langle \cos(2\phi_1 - \phi_2 - \phi_3) \rangle \langle \cos(2\phi_1 - 2\phi_2) \rangle = -v_2^3 v_1^2 \cos[2(\Psi_2 - \Psi_1)]$$

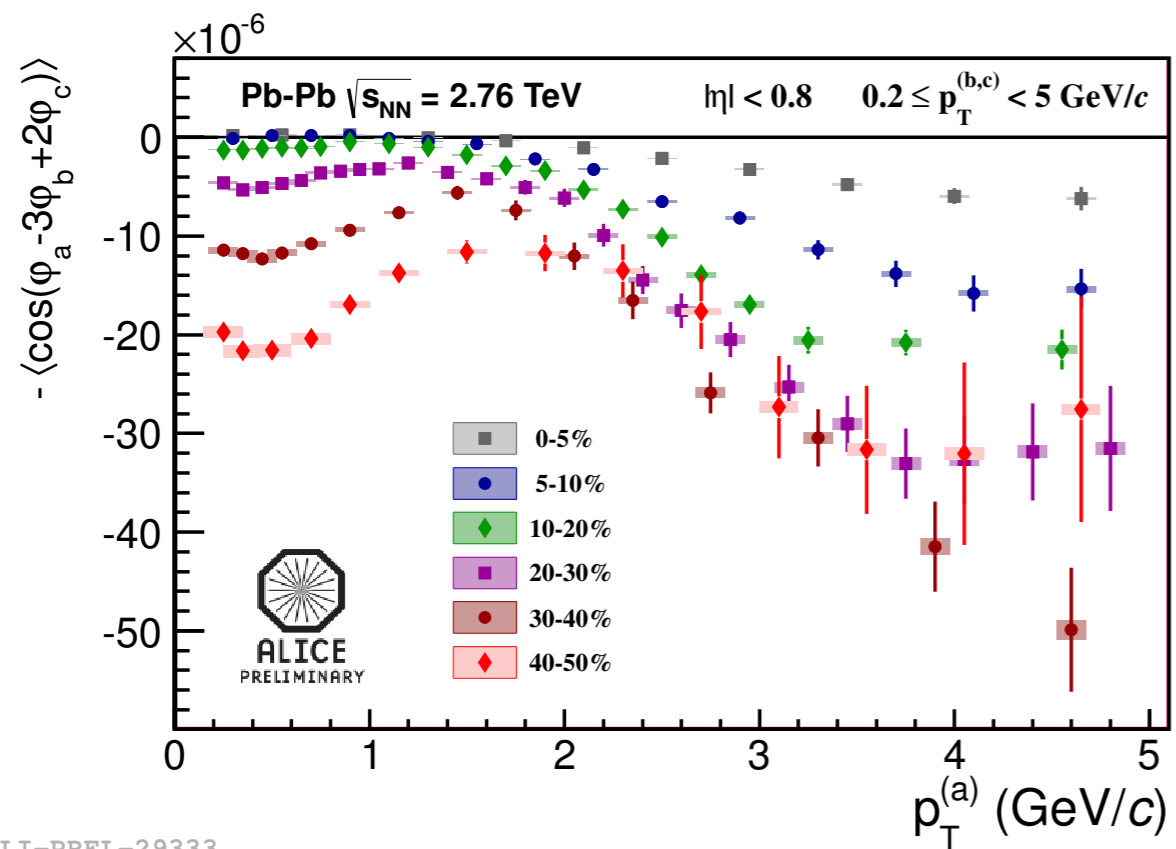
$$\langle \cos(3\phi_1 + 2\phi_2 - 2\phi_3 - 2\phi_4 - \phi_5) \rangle - 2\langle \cos(3\phi_1 - 2\phi_2 - \phi_3) \rangle \langle \cos(2\phi_1 - 2\phi_2) \rangle = -v_3 v_2^3 v_1 \cos[3\Psi_3 - 2\Psi_2 - \Psi_1]$$

The 5 particle cumulants allow us to cleanly measure if there is a correlations between the various planes

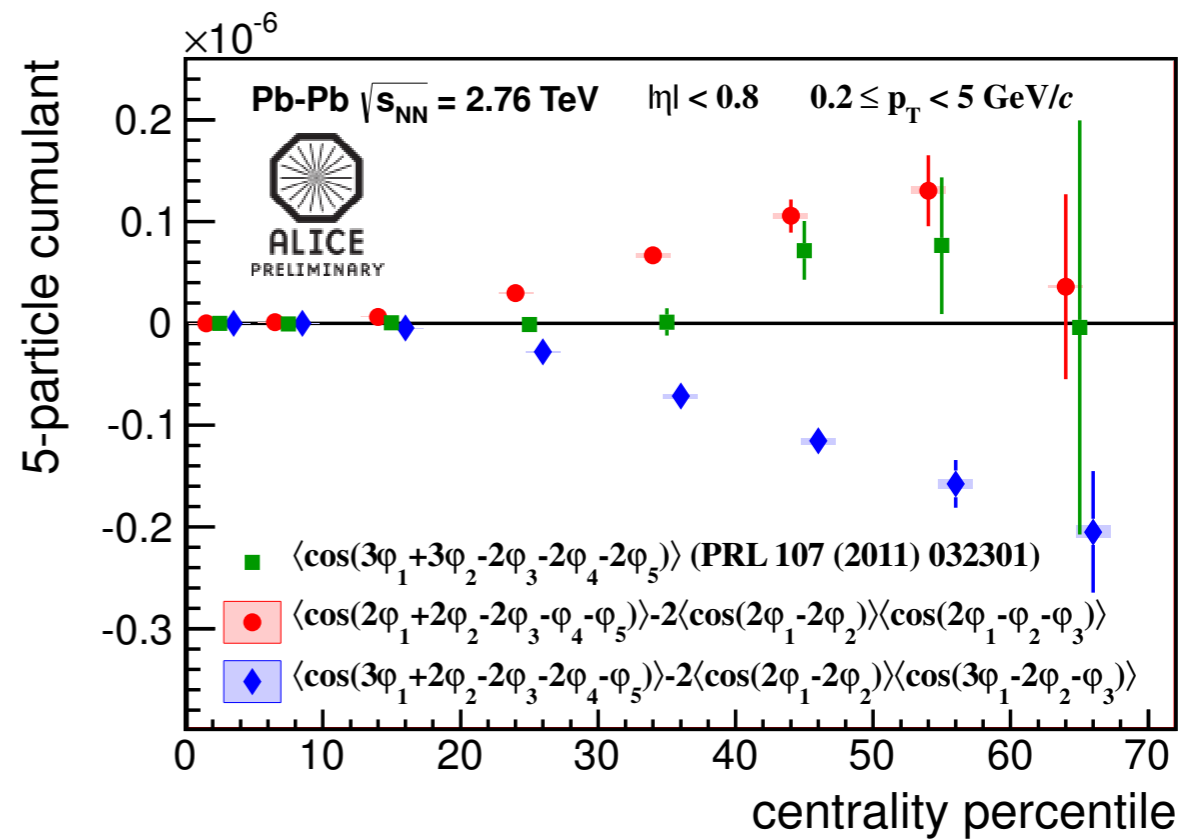
# Conclusions

- Elliptic flow measurements provided strong constraints on the bulk properties of hot and dense matter produced at RHIC and LHC energies and have led to the new paradigm of the QGP as the so called perfect liquid
- At the LHC we observe even stronger flow than at RHIC which is expected for almost perfect fluid behavior
- viscous hydro calculations fail to describe proton  $v_2$  while hybrid models do a much better job
- does this hadronic contribution also explain the  $v_2$  of the phi meson and multi-strange baryons?
- At the LHC KET scaling is broken (but was it ever a well founded scaling?)
- $v_2$  fluctuations are in qualitative agreement with expectations from Glauber models and rather independent of  $\eta$  and  $p_t$
- The measurements of  $v_3$  and higher  $v_n$ 's at RHIC and at the LHC indicate that these flow coefficients behave as expected from a created system which has a small  $\eta/s$
- The fluctuations can be used to do “event shape engineering” which provides new ways to compare to models

# multi-particles



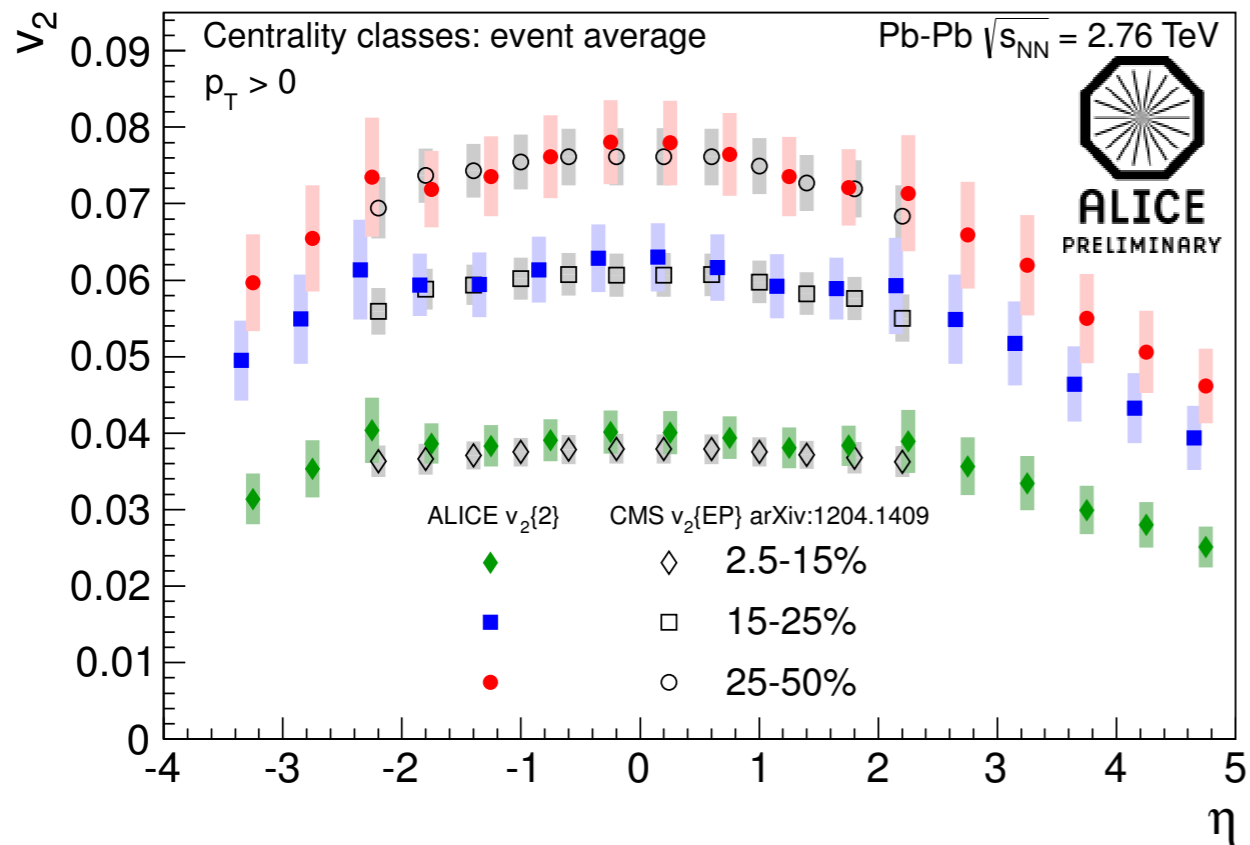
ALI-PREL-29333



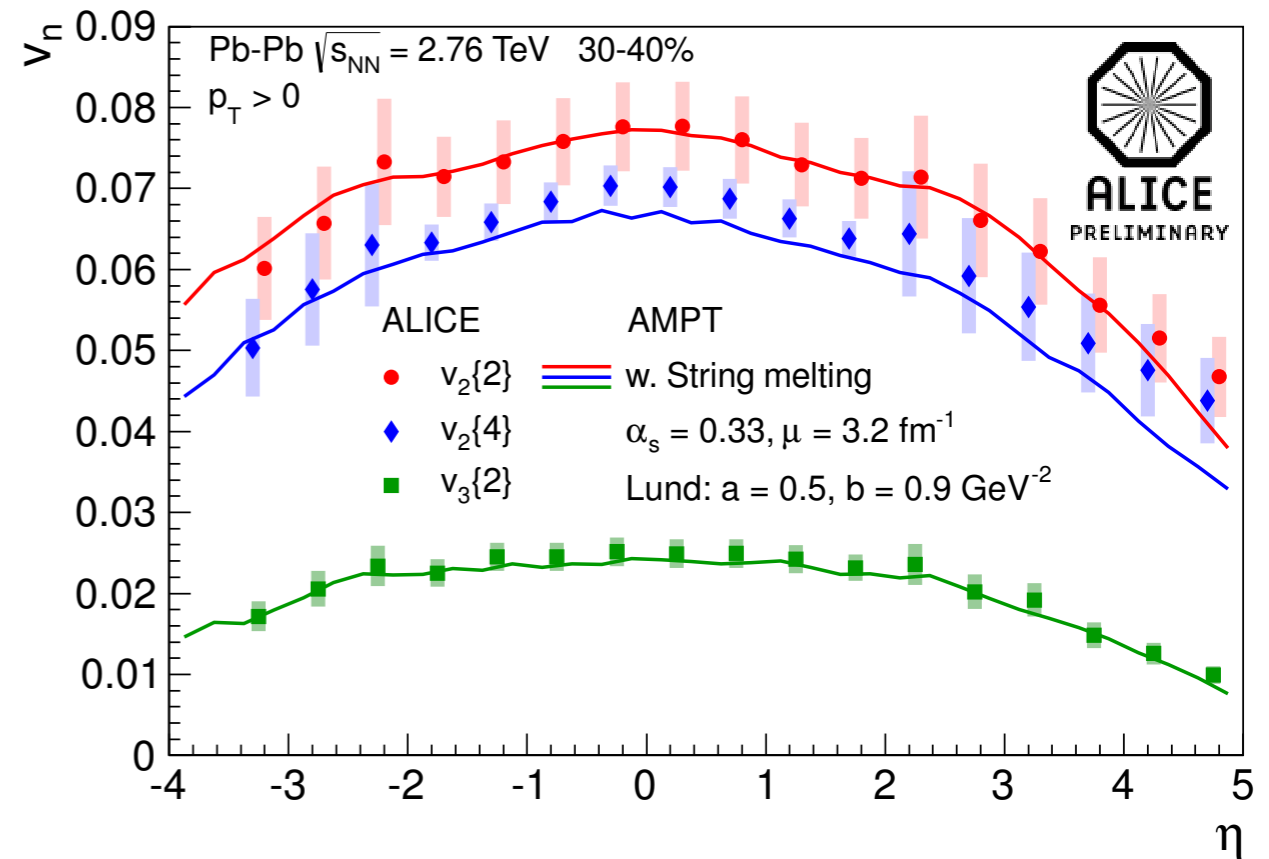
ALI-PREL-29328



# $v_2$ and $v_3$

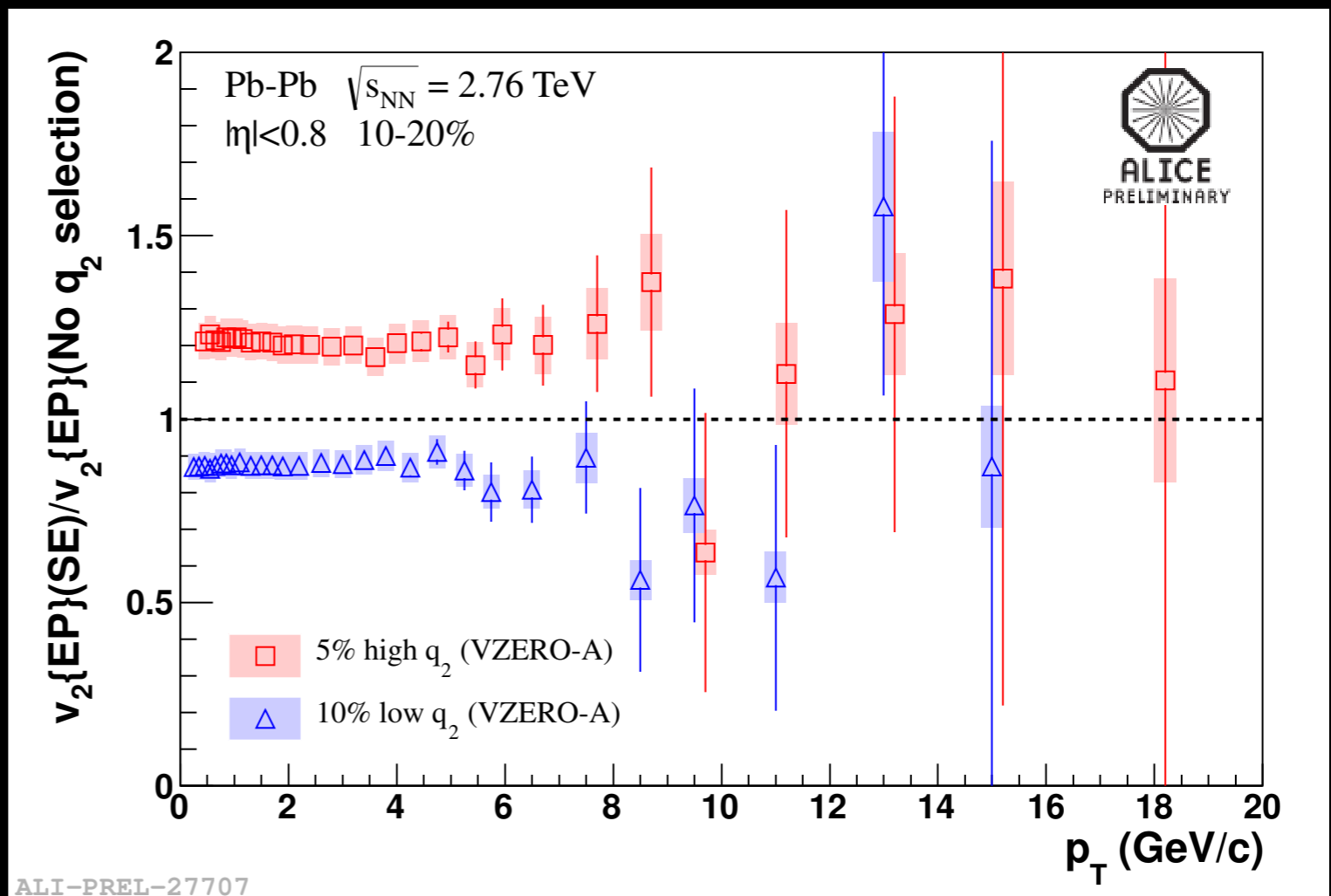


ALI-PREL-27803



ALI-PREL-28053

# Event shape engineering



# Flow Fluctuations

$$v\{2\} = \langle v \rangle + \frac{1}{2} \frac{\sigma_v^2}{\langle v \rangle}$$

$$v\{4\} = \langle v \rangle - \frac{1}{2} \frac{\sigma_v^2}{\langle v \rangle}$$

$$v\{6\} = \langle v \rangle - \frac{1}{2} \frac{\sigma_v^2}{\langle v \rangle}$$

$$v\{8\} = \langle v \rangle - \frac{1}{2} \frac{\sigma_v^2}{\langle v \rangle}$$

- for  $\sigma_v \ll \langle v \rangle$  this is a general result to order  $\sigma^2$