

# Search for double beta decays of palladium isotopes into excited states



**INTERNATIONAL SCHOOL OF  
NUCLEAR PHYSICS  
35th Course  
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# Outline

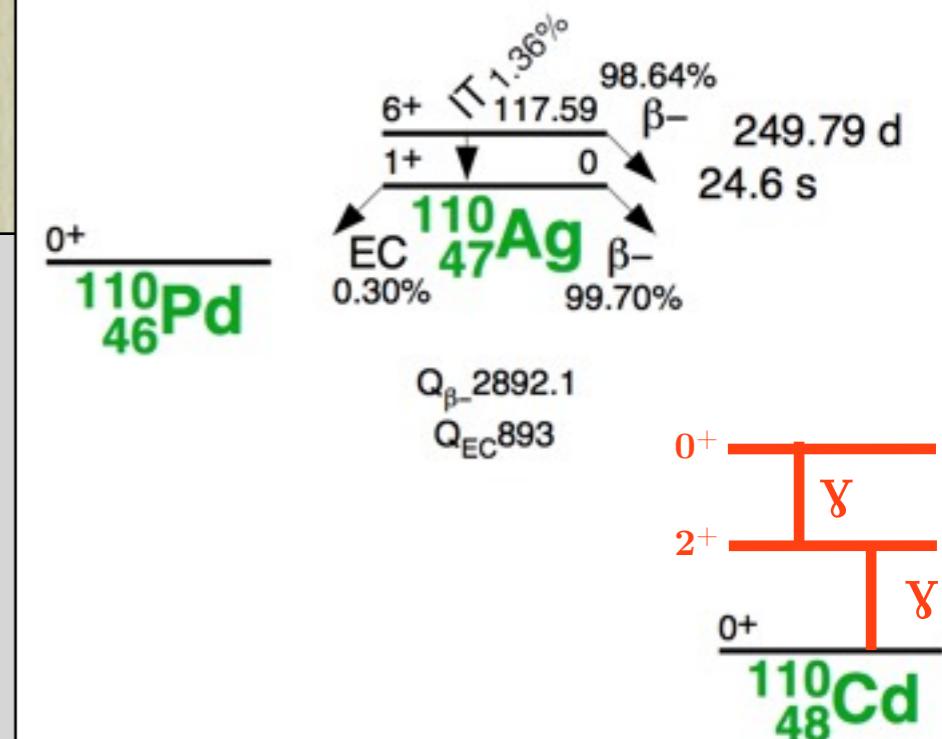
- Why double beta decays into excited states
- Palladium 101
- Three experiments...
- Outlook

## Experiments:

1. Felsenkeller              Physics Letters B 705 47–51 (2011)
2. HADES                      Physical Review C 87, 034312 (2013)
3. LNGS

# Why DBD into excited states?

- Adds nuclear structure information
- Eventually helps constraining NME calculations for  $0\nu\beta\beta$
- Potential resonance enhancement for  $0\nu ECEC$
- Convenient experimental signature ( $\gamma$ -lines)
- So far only discovered in  $^{100}\text{Mo}$  (1995) and  $^{150}\text{Nd}$  (2004)



Compilation of 2nubb  
 $0_1^+$  transitions

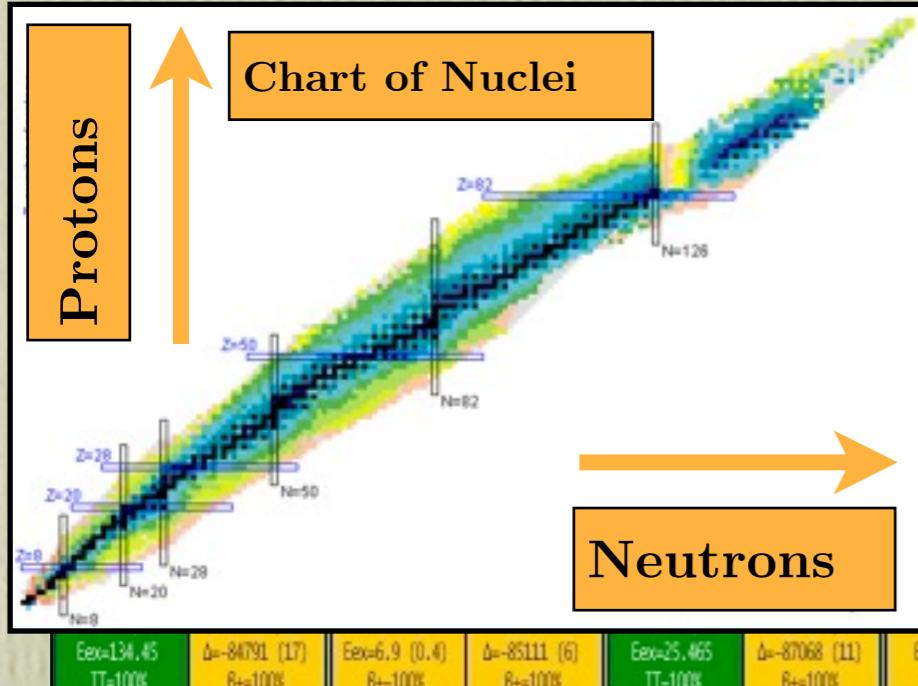
Nuclei	$E_{2\beta}$ , keV	Experiment $T_{1/2}, \gamma$	Theory [18, 19]	Theory [23]
$^{150}\text{Nd}$	2627.1	$= 1.4_{-0.4}^{+0.5} \times 10^{20}$ [8]	-	-
$^{96}\text{Zr}$	2202.5	$> 6.8 \times 10^{19}$ [22]	$(2.4 - 2.7) \times 10^{21}$	$3.8 \times 10^{21}$
$^{100}\text{Mo}$	1903.7	$= 6.2_{-0.7}^{+0.9} \times 10^{20}$	$1.6 \times 10^{21}$ [29]	$2.1 \times 10^{21}$
$^{82}\text{Se}$	1507.5	$> 3.0 \times 10^{21}$ [24]	$(1.5 - 3.3) \times 10^{21}$	-
$^{48}\text{Ca}$	1274.8	$> 1.5 \times 10^{20}$ [20]	-	-
$^{116}\text{Cd}$	1048.2	$> 2.0 \times 10^{21}$ [26]	$1.1 \times 10^{22}$	$1.1 \times 10^{21}$
$^{76}\text{Ge}$	916.7	$> 6.2 \times 10^{21}$ [30]	$(7.5 - 310) \times 10^{21}$	$4.5 \times 10^{21}$
$^{130}\text{Te}$	735.3	$> 2.3 \times 10^{21}$ [31]	$(5.1 - 14) \times 10^{22*}$	-

# Why and why not Palladium?

Isotope	Q (MeV)	Percent natural abund.	Element cost [5] (\$/kg)	$G^{0\nu}$ ( $10^{-14}/\text{yr}$ ) [6]	$M^{0\nu}$ (avg) [7]	Annual world production [5] (tons)	$0\nu/2\nu$ rate [2,8] ( $10^{-8}$ )
<sup>48</sup> Ca	4.27	0.19	0.16	6.06	1.6	$2.4 \times 10^8$	0.016
<sup>76</sup> Ge	2.04	7.8	1650	0.57	4.8	118	0.55
<sup>82</sup> Se	3.00	9.2	174	2.48	4.0	2000	0.092
<sup>96</sup> Zr	3.35	2.8	36	5.02	3.0	$1.4 \times 10^6$	0.025
<sup>100</sup> Mo	3.04	9.6	35	3.89	4.6	$2.5 \times 10^5$	0.014
<sup>110</sup> Pd	2.00	11.8	23000	1.18	6.0	207	0.16
<sup>116</sup> Cd	2.81	7.6	2.8	4.08	3.6	$2.2 \times 10^4$	0.035
<sup>124</sup> Sn	2.29	5.6	30	2.21	3.7	$2.5 \times 10^5$	0.072
<sup>130</sup> Te	2.53	34.5	360	3.47	4.0	$\sim 150$	0.92
<sup>136</sup> Xe	2.46	8.9	1000	3.56	2.9	50	1.51
<sup>150</sup> Nd	3.37	5.6	42	15.4	2.7	$\sim 10^4$	0.024

PHYSICAL REVIEW D  
87, 071301(R) (2013)

- <sup>110</sup>Pd is one out 11 DBD candidates with a Q-value above 2 MeV
- <sup>110</sup>Pd has the 2nd highest natural abundance
- <sup>102</sup>Pd is a double EC candidate
- But: Extremely expensive and no Pd detector technology



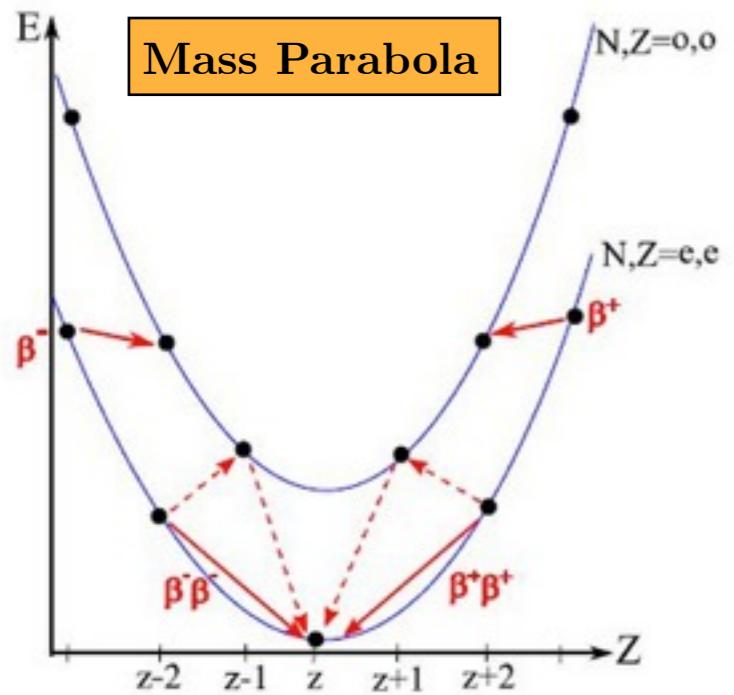
# Palladium: $^{110}\text{Pd}$ and $^{102}\text{Pd}$

$^{108}\text{Cd}$ 59	$^{108}\text{Cd}$ 60	$^{109}\text{Cd}$ 61	$^{110}\text{Cd}$ 62	$^{111}\text{Cd}$ 63	$^{112}\text{Cd}$ 64
6.50 h $5/2^+$ $\Delta=-86985$ (6) $\beta+=100\%$	Stable $>410$ Py $0^+$ $\Delta=-89252$ (6) Abndnc=0.89% (3) $2\beta+ ?$	$12 \mu\text{s} 1/2^+$ $E_{\text{ex}}=59.6$ (0.4) IT=100% $\Delta=-88508$ (4) $\epsilon=100\%$	461.4 d $5/2^+$ $\Delta=-90353.0$ (2.7) Abndnc=12.49% (18)	$48.50 \pi 11/2^-$ $E_{\text{ex}}=396.214$ IT=100% $\Delta=-89257.5$ (2.7) Abndnc=12.80% (12)	Stable $1/2^+$ $\Delta=-90580.5$ (2.7) Abndnc=24.13% (21)
$^{107}\text{Ag}$ 59	$^{107}\text{Ag}$ 60	$^{108}\text{Ag}$ 61	$^{109}\text{Ag}$ 62	$^{111}\text{Ag}$ 63	$^{111}\text{Ag}$ 64
$8.3 \mu\text{s} 6^+$ $E_{\text{ex}}=89.66$ $\Delta=-89337$ (5) $\beta+=2\%$ $\beta=0.5\%$	$44.3 s 7/2^+$ $E_{\text{ex}}=93.125$ IT=100% $\Delta=-88402$ (4) Abndnc=51.83% (8)	$418 \gamma 6^+$ $E_{\text{ex}}=109.440$ $\beta=91.3\%$ (9) $\beta=2.8\%$ (20)	$2.37 \pi 1^+$ $E_{\text{ex}}=88.0341$ $\beta=97.15\%$ (20) $\beta=2.8\%$ (20)	$39.6 s 7/2^+$ $E_{\text{ex}}=88.0341$ IT=100% $\Delta=-88722.7$ (2.9) Abndnc=48.161% (8)	$249.950 d 6^+$ $E_{\text{ex}}=117.59$ $\beta=98.6\%$ (6) $\beta=1.3\%$ (6)
$^{102}\text{Pd}$ 56	$^{103}\text{Pd}$ 57	$^{104}\text{Pd}$ 58	$^{105}\text{Pd}$ 59	$^{106}\text{Pd}$ 60	$^{107}\text{Pd}$ 61
Stable $0^+$ $\Delta=-87925.1$ (3.0) Abndnc=1.02% (1) $2\beta+ ?$	$25 \pi 11/2^-$ $E_{\text{ex}}=784.79$ IT=100% $\Delta=-87479.1$ (2.9) $\epsilon=100\%$	$16.991 d 5/2^+$ $\Delta=-87479.1$ (2.9) $\epsilon=100\%$	Stable $0^+$ $\Delta=-89390$ (4) Abndnc=11.14% (8)	Stable $5/2^+$ $\Delta=-88413$ (4) Abndnc=22.33% (8)	Stable $0^+$ $\Delta=-89902$ (4) Abndnc=27.33% (3)
$^{101}\text{Rh}$ 56	$^{102}\text{Rh}$ 57	$^{103}\text{Rh}$ 58	$^{104}\text{Rh}$ 59	$^{105}\text{Rh}$ 60	$^{106}\text{Rh}$ 61
$4.34 d 9/2^+$ $E_{\text{ex}}=157.32$ $\beta=93.6\%$ (2) IT=6.4% (2)	$3.3 \gamma 1/2^-$ $\Delta=-87408$ (17) $\epsilon=100\%$	$3.742 \gamma 6^+$ $E_{\text{ex}}=140.75$ $\beta=100\%$ IT=0.233% (24)	$0 d (1,-2)$ $\Delta=-87375$ (2) $\beta=0\%$	$56.114 \pi 7/2^+$ $E_{\text{ex}}=39.756$ $\Delta=-88022.2$ (2.8) Abndnc=100.0%	$21.3 s 11/2^-$ $E_{\text{ex}}=214.6$ $\Delta=-88368$ (4) $\beta=100\%$
$^{100}\text{Ru}$ 56	$^{101}\text{Ru}$ 57	$^{102}\text{Ru}$ 58	$^{103}\text{Ru}$ 59	$^{104}\text{Ru}$ 60	$^{105}\text{Ru}$ 61
Stable $0^+$ $\Delta=-89219.0$ (2.0) Abndnc=12.60% (7)	$17.5 \mu\text{s} 11/2^-$ $E_{\text{ex}}=527.5$ IT=100% $\Delta=-87949.7$ (2.0) Abndnc=17.06% (7)	Stable $5/2^+$ $\Delta=-87949.7$ (2.0) Abndnc=17.06% (7)	Stable $0^+$ $\Delta=-89098.0$ (2.0) Abndnc=31.55% (14)	$1.69 \pi 11/2^-$ $E_{\text{ex}}=238.2$ IT=100% $\Delta=-87258.8$ (2.0) $\beta=100\%$	Stable $0^+$ $\Delta=-88089$ (3) Abndnc=18.62% (27) $2\beta^- ?$
$^{106}\text{Ru}$ 62	$^{107}\text{Ru}$ 63	$^{108}\text{Ru}$ 64	$^{109}\text{Ru}$ 65	$^{110}\text{Ru}$ 66	$^{111}\text{Ru}$ 67
$4.44 h 3/2^+$ $\Delta=-85928$ (3) $\beta=100\%$	$373.59 d 0^+$ $\Delta=-86322$ (8) $\beta=100\%$	$3.75 m (5/2)^+$ $\Delta=-83920$ (120) $\beta=100\%$	$4.55 m 0^+$ $\Delta=-83670$ (120) $\beta=100\%$		

- $^{102}\text{Pd}$ :  $2\nu\text{ECEC}$ ,  $2\nu\text{EC}\beta^+$
- nat abundance: 1.02 %
- Q-value: 1172 keV

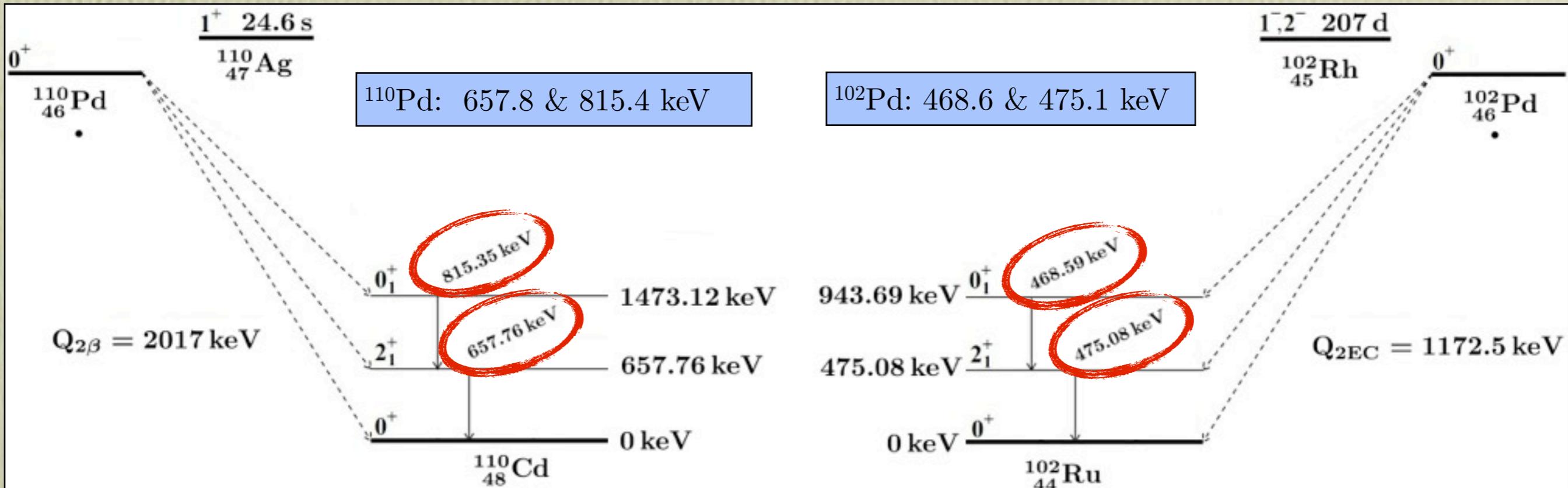
- $^{110}\text{Pd}$ :  $2\nu\beta^-\beta^-$
- nat abundance: 11.72 %
- Q-value 2017.9 keV

PRL 108, 062502 (2012)



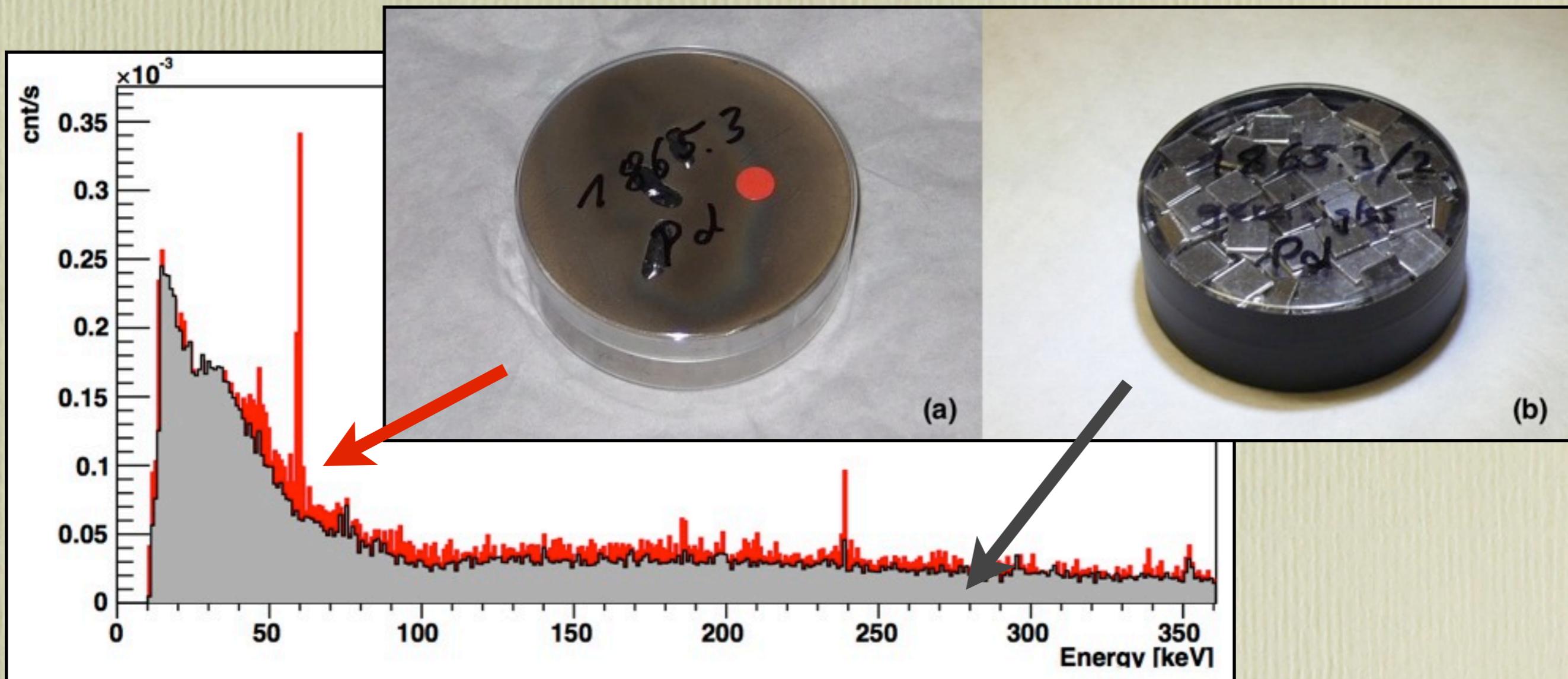
# Decay Schemes: $^{110}\text{Pd}$ and $^{102}\text{Pd}$

- $^{110}\text{Cd}$  and  $^{102}\text{Ru}$  have excited  $2^+$  and  $0^+$  states
- Probability depends on phase space and spin (highest rate expected from  $0_1^+$ )
- Expected  $\gamma$ -cascade



- Idea: Measure sample with HPGe  $\gamma$ -spectroscopy in low background env.
- Use  $\gamma$ -lines from excited state transitions as experimental signatures
- Not sensitive to g.s. transitions; No separation between  $2\nu\beta\beta$  and  $0\nu\beta\beta$

# Palladium Sample



- (a) Pd block from unknown origin
- Contaminated with  $^{241}\text{Am}$
- Cleaned by C. HAFNER GmbH+Co. KG >99.95% purity
- (b) 802.35 g Pd in 1cm x 1cm x 1mm plates ( $\rho_{\text{eff}} = 10.2 \text{ g/cm}^3$ )

# Pd DBD Knowledge

## $^{110}\text{Pd}$

- Best & only experimental half-life limit for g.s. transition from 1952
- No previous experimental limit for excited state transitions
- Theoretical expectations starting with half-lives  $\mathcal{O}(10^{23})$  for  $0_1^+$

## $^{102}\text{Pd}$

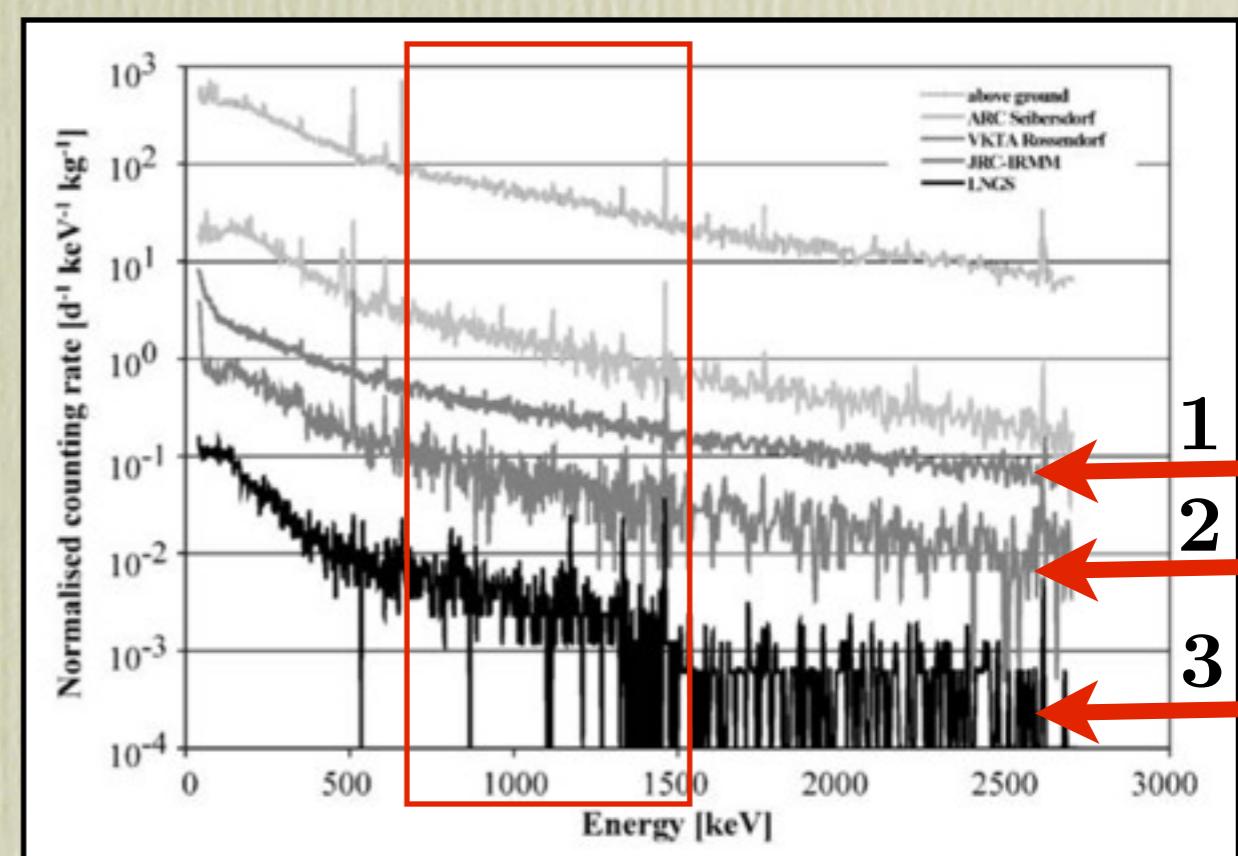
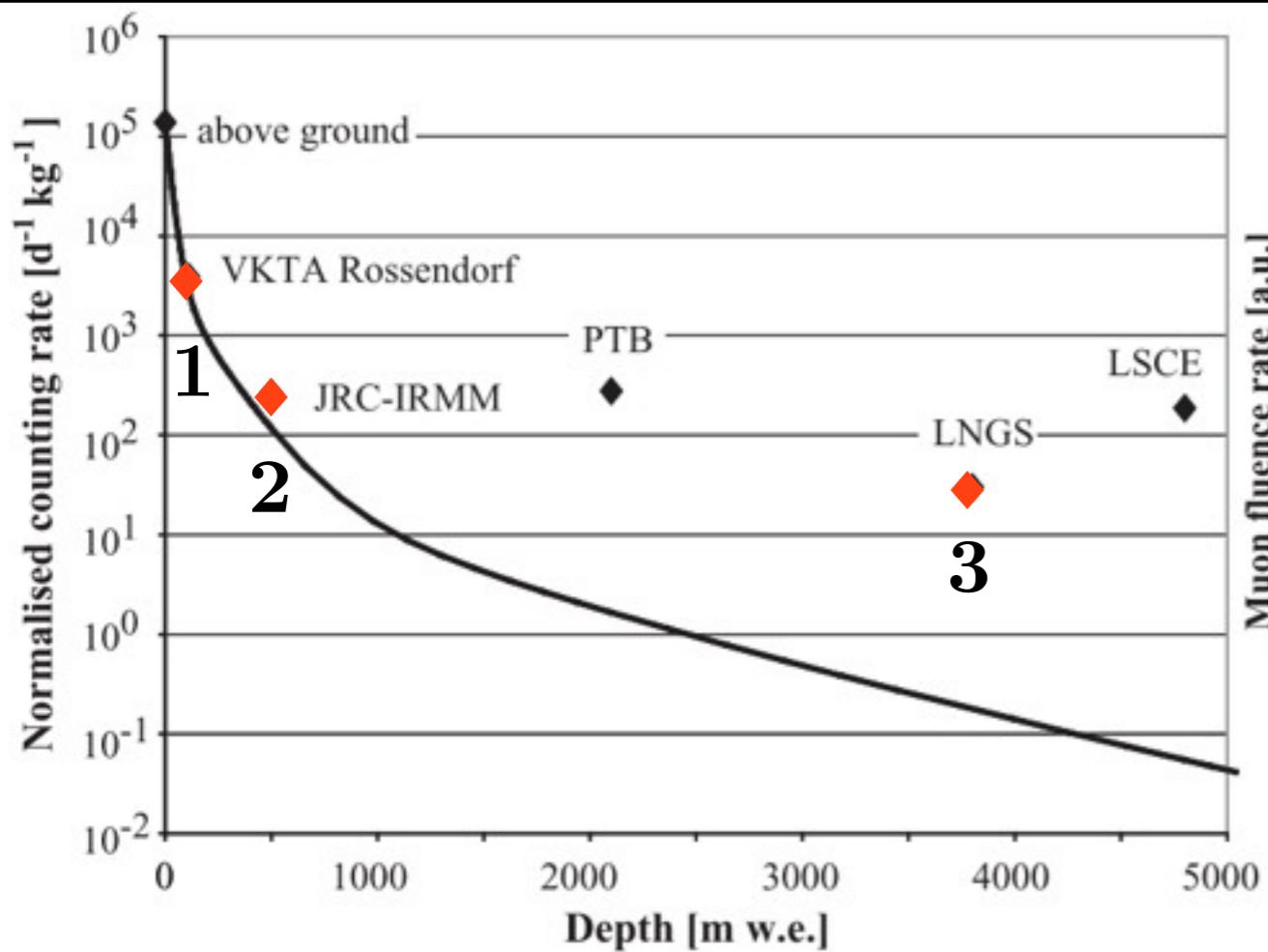
- No previous experimental limit
- No theoretical calculation

Expt./Th. model	Lower limit $T_{1/2}$ (yr)	Reference	Year of publication
<b><math>^{110}\text{Pd}</math> ground state</b>			
Expt.	$1 \times 10^{17}$ (68% CL)	[24]	1952
PHFM	$1.41 \times 10^{20}$ and $3.44 \times 10^{20}$ <sup>a</sup>	[26]	2005
SSDH	$1.75 \times 10^{20}$	[27]	2000
SSDH	$1.2\text{--}1.8 \times 10^{20}$ <sup>b</sup>	[28]	1998
SRPA	$1.6 \times 10^{20}$	[29]	1994
OEM	$1.24 \times 10^{21}$	[30]	1994
QRPA	$1.16 \times 10^{19}$	[31]	1990
SSD	$1.2 \times 10^{20}$	[32]	2005
<i>pnQRPA</i>	$1.1 \times 10^{20}$ and $0.91 \times 10^{20}$ <sup>c</sup>	[33]	2011
<b><math>^{110}\text{Pd}</math> <math>2_1^+</math></b> @ 657.76 keV			
Expt.	$4.40 \times 10^{19}$ (95% CL)	[25]	2011
SSD	$4.4 \times 10^{25}$	[32]	2005
SRPA	$8.37 \times 10^{25}$	[29]	1994
<i>pnQRPA</i>	$1.48 \times 10^{25}$	[34]	2007
<i>pnQRPA</i>	$0.62 \times 10^{25}$ and $1.3 \times 10^{25}$ <sup>c</sup>	[33]	2011
<b><math>^{110}\text{Pd}</math> <math>0_1^+</math></b> @ 1473.12 keV			
Expt.	$5.89 \times 10^{19}$ (95% CL)	[25]	2011
SSD	$2.4 \times 10^{26}$	[32]	2005
<i>pnQRPA</i>	$4.2 \times 10^{23}$ and $9.1 \times 10^{23}$ <sup>c</sup>	[33]	2011
<b><math>^{110}\text{Pd}</math> <math>2_2^+</math></b> @ 1475.80 keV			
SSD	$3.8 \times 10^{31}$	[32]	2005
<i>pnQRPA</i>	$11 \times 10^{30}$ and $7.4 \times 10^{30}$ <sup>c</sup>	[33]	2011
<b><math>^{110}\text{Pd}</math> <math>0_2^+</math></b> @ 1731.33 keV			
SSD	$5.3 \times 10^{29}$	[32]	2005
<b><math>^{110}\text{Pd}</math> <math>2_3^+</math></b> @ 1783.48 keV			
SSD	$1.3 \times 10^{35}$	[32]	2005
		8	

# Three Experiments

## The Palladium world tour:

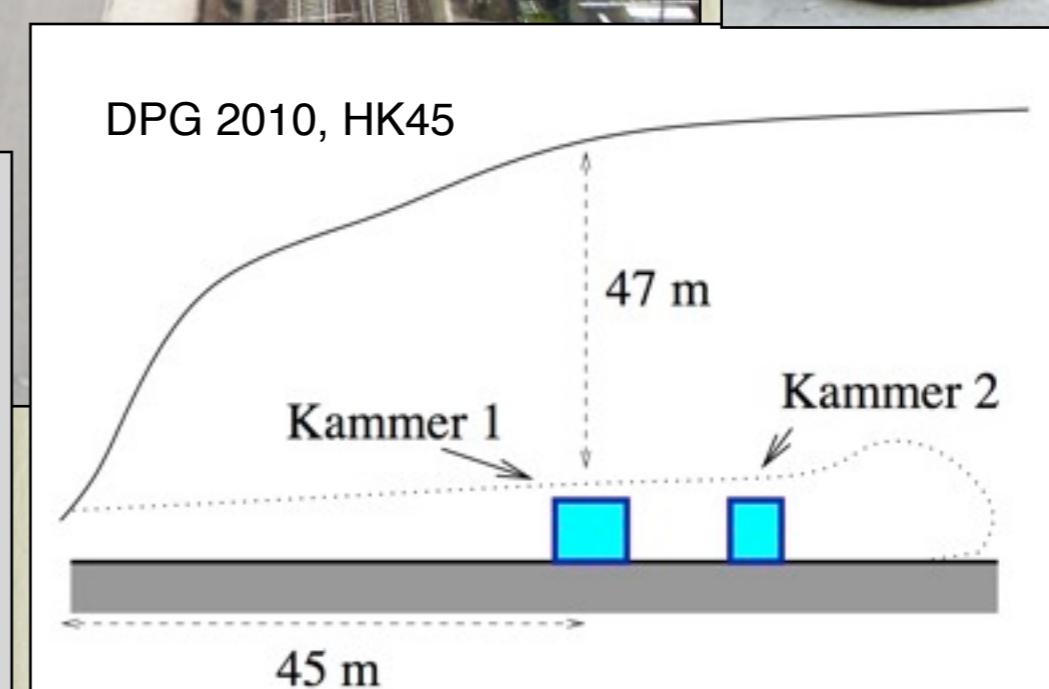
1. Felsenkeller (Dresden, Germany)
2. HADES (Mol, Belgium)
3. LNGS (L'Aquila, Italy)



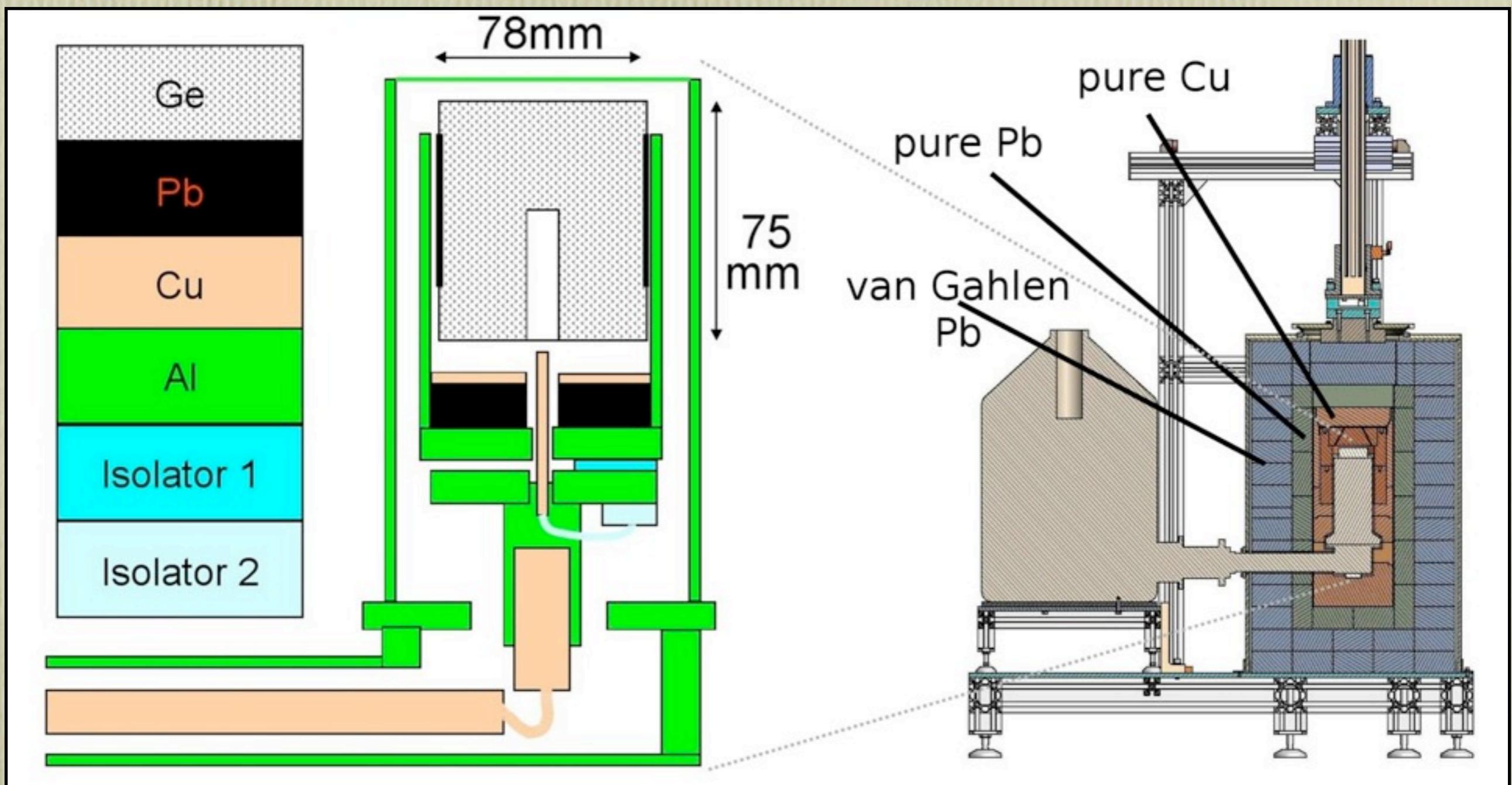
# VKTA Rossendorf - The Felsenkeller



- Built in 1982 in cavity of old brewery in Dresden, Germany
- Used to help decommissioning nuclear facilities
- 47 m Monzonite (120 m w.e.)
- $\mu$ -flux reduced by factor 20
- Up to 10 experimental HPGe setups in 2 chambers



# The Detector



- HPGe Canberra 90 % efficiency
- Detector simulation with AMOS (Radiat. Protect. Dosim. 119 (2006) 479)

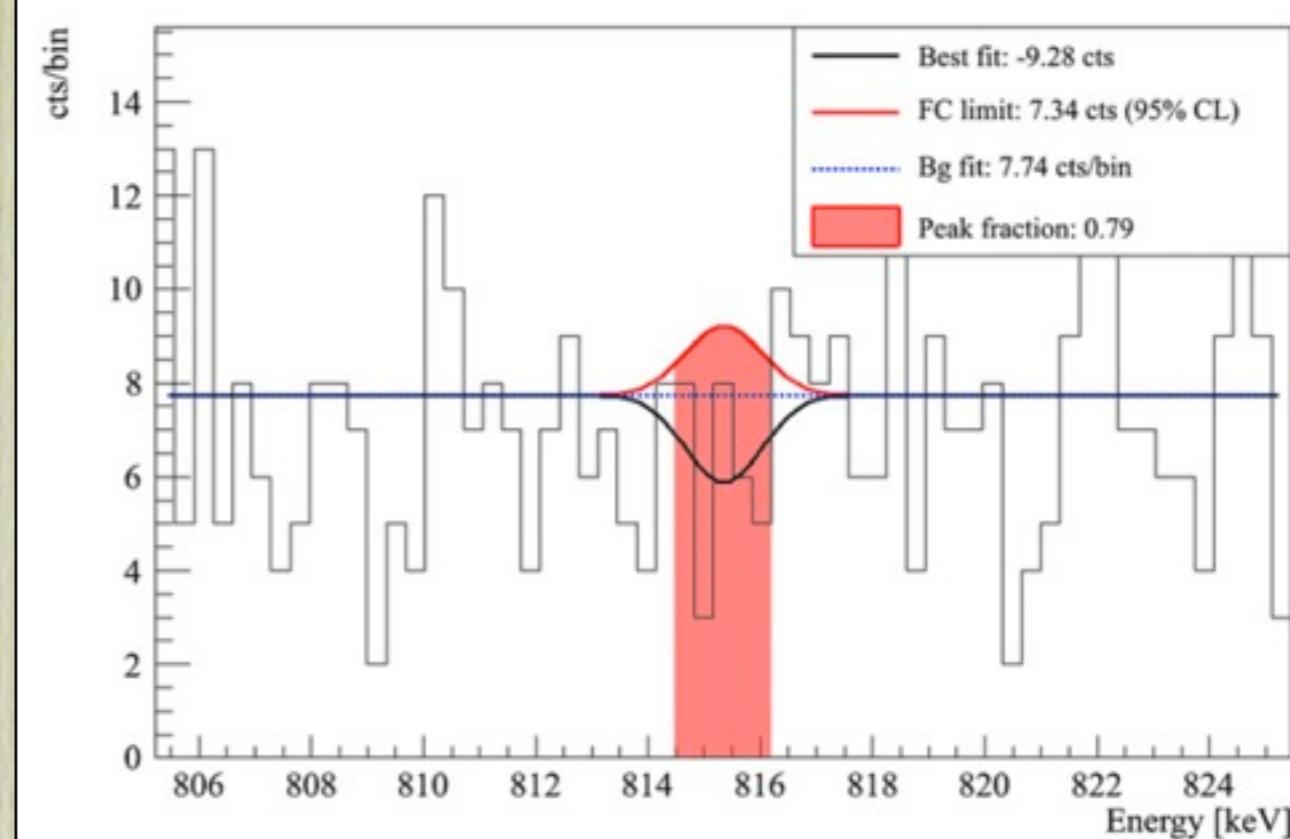
# Analysis: Felsenkeller

- 16.2 d measurement
- 13.0 kg · y exposure

- Energy and efficiency calibration with 8 nuclides in SiO<sub>2</sub> sample geometry
- Correction for self-absorption with MC simulations with AMOS code
  - 1.6 keV FWHM @ 815 keV
  - 3.9 % FEP efficiency @ 815 keV

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- Background model: Constant likelihood fit in side bands w/o γ-line
- Fit of gaussian signal can result in under-fluctuation
- Limit calculation using Feldman-Cousins in single analysis bin
- Quoting half-life limit for γ-line with best limit
- No systematic uncertainties considered for limit

## Results:

Lower T<sub>1/2</sub> limits (95 % CL)

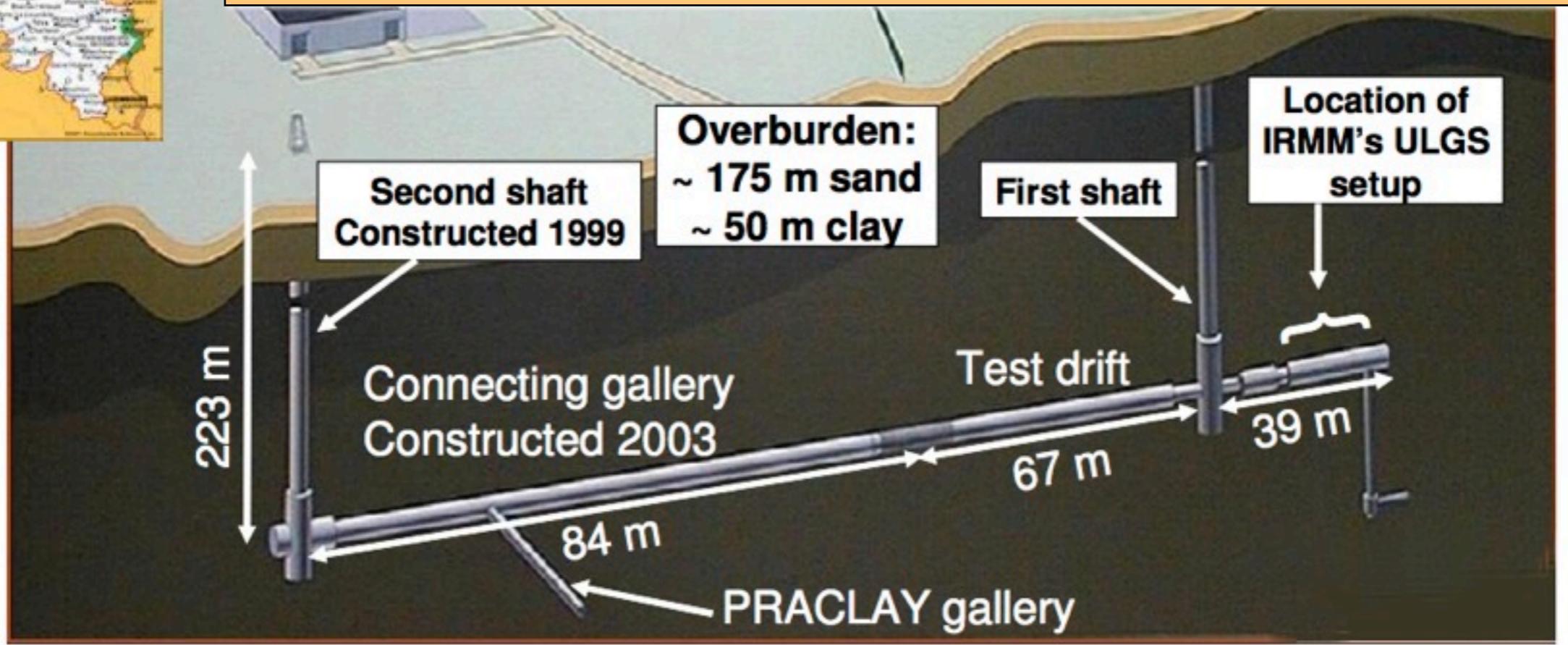
<sup>110</sup>Pd 0<sub>1</sub><sup>+</sup>: > 5.89 · 10<sup>19</sup> yr

<sup>110</sup>Pd 2<sub>1</sub><sup>+</sup>: > 4.40 · 10<sup>19</sup> yr

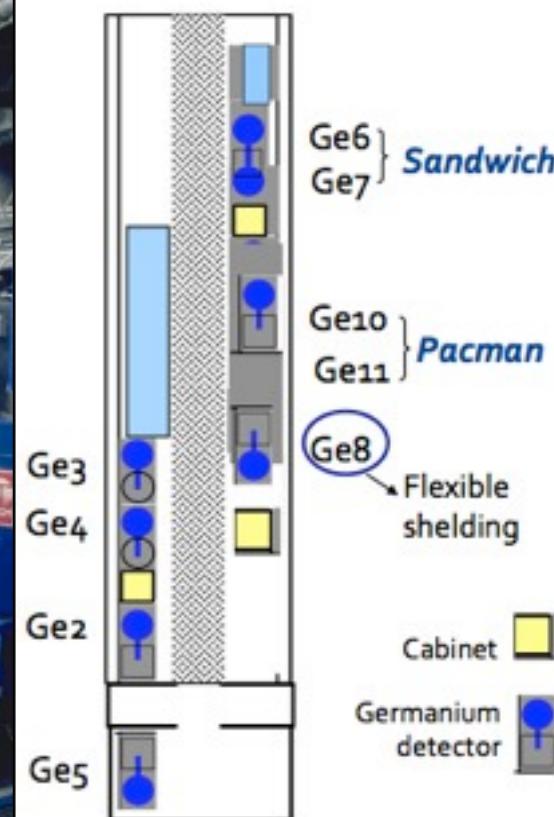
<sup>102</sup>Pd 0<sub>1</sub><sup>+</sup>: > 7.64 · 10<sup>18</sup> yr

<sup>102</sup>Pd 2<sub>1</sub><sup>+</sup>: > 2.68 · 10<sup>18</sup> yr

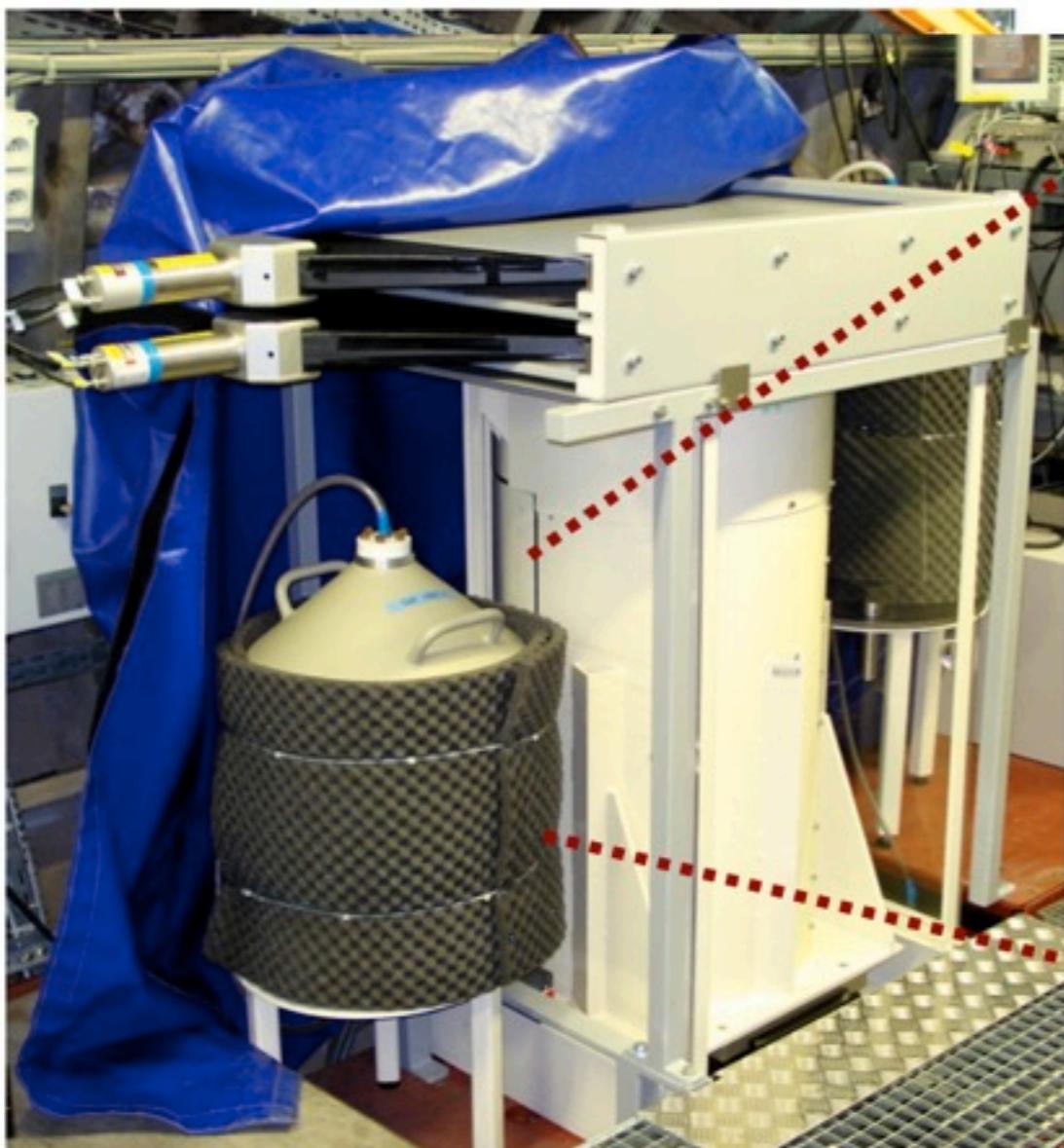
# HADES - High Activity Disposal Experimental Site



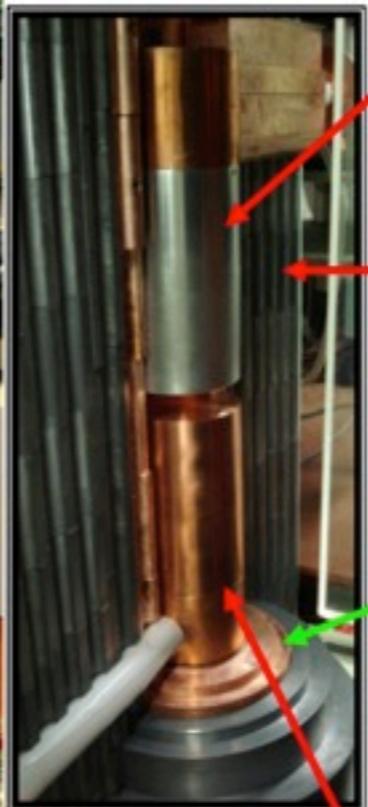
- Operated by SCK · CEN in Mol, Belgium
- Used to study disposal of nuclear waste in clay
- IRMM low-background laboratory
- 175 m overburden (500 m w.e.)
- $\mu$ -flux reduced by factor 1000



# IRMM Sandwich Spectrometer



Increased solid angle



Ge-7

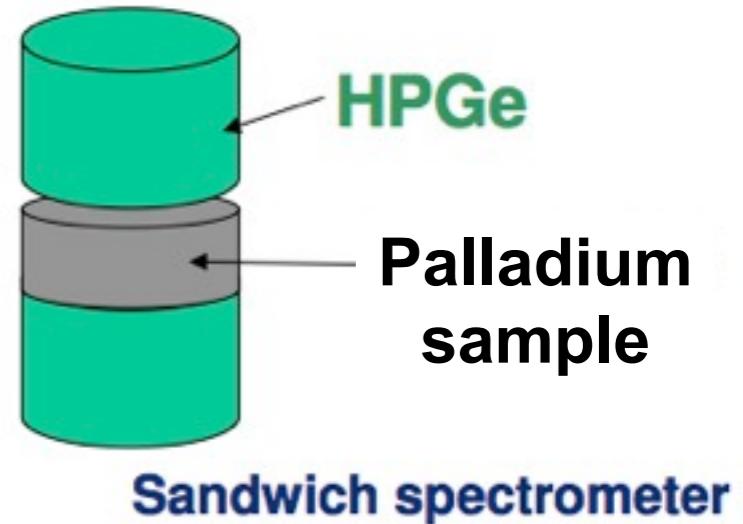
Pb shield = radiopure  
lead, 4 cm, 2.5 Bq/kg

+14.5 cm lead, 20 Bq/kg

Cu lining = radiopure  
copper, 3.5 cm

Ge-6

Detector mass ~ 1.9 kg each



- 2 HPGe Canberra p-type with 80% and 90% efficiency; Muon-veto above detector
- Two DAQ:
  - Multi parameter system in list mode (offline)
  - MCA in histogram mode
- Detector simulation with EGS4

# Analysis: HADES

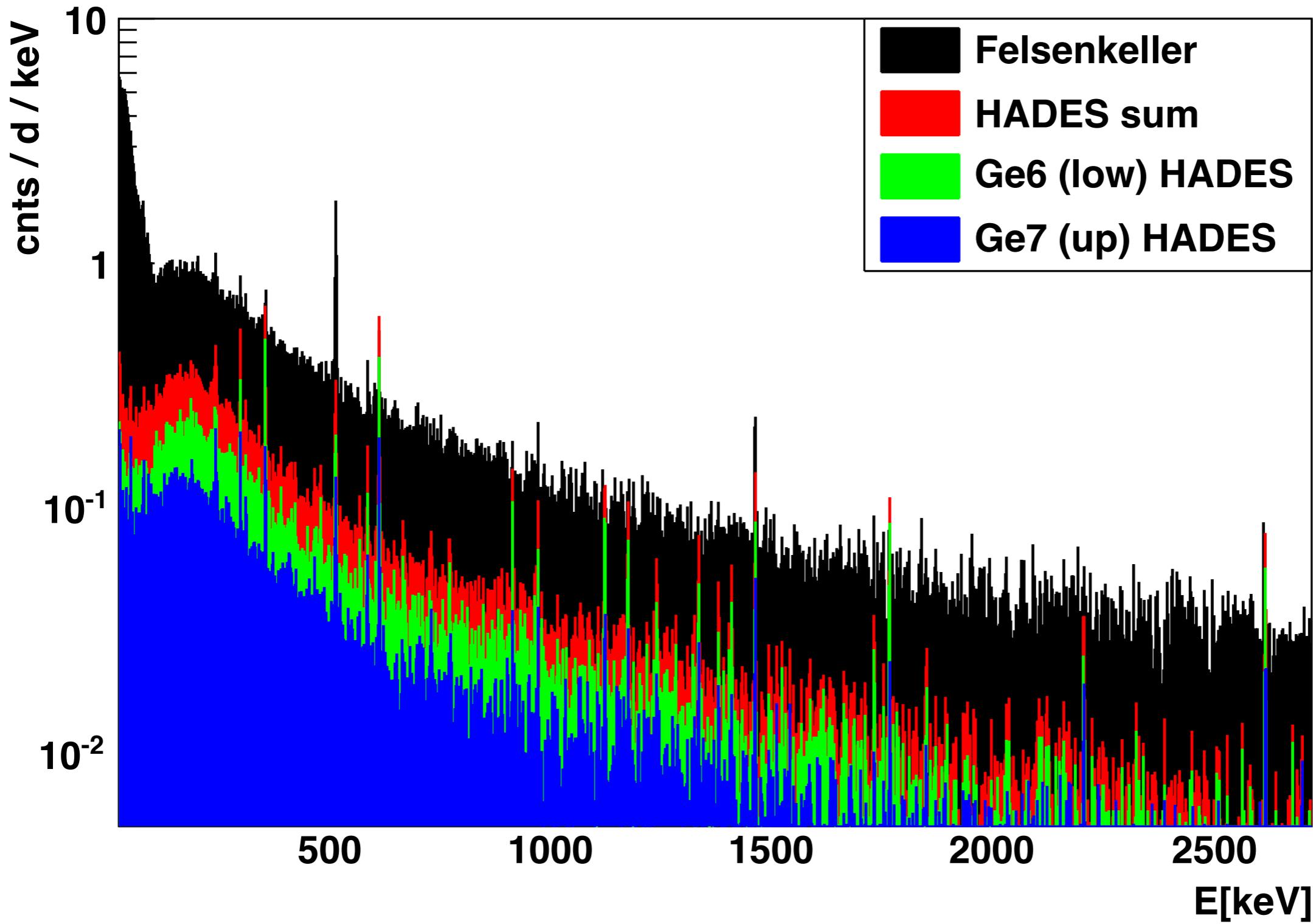
Physical Review C 87, 034312 (2013)  
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- Analysis only with single detector spectra (no coincidence possible)
- 46.5 d measurement; 35.9 kg y exposure
- Analysis analog to Felsenkeller measurement
- Limits for all possible decay branches were calculated
- Limit of best decay branch was quoted as limit of decay mode

Decay mode	$\gamma$ line energy (keV)	Emission probability	Detection efficiency	Signal count limit	$T_{1/2}$ limit (yr)
$^{110}\text{Pd } 2_1^+$ 657.76 keV	657.76 keV	100%	4.70%	12.4	$1.72 \times 10^{20}$
$^{110}\text{Pd } 0_1^+$ 1473.12 keV	815.33 keV	100%	3.84%	8.4	$1.98 \times 10^{20}$
	657.76 keV	100%	3.94%	12.4	$1.44 \times 10^{20}$
$^{110}\text{Pd } 2_2^+$ 1475.80 keV	1475.80 keV	35.25%	1.32%	11.5	$5.17 \times 10^{19}$
	818.02 keV	64.75%	2.40%	16.3	$6.67 \times 10^{19}$
	657.76 keV	64.75%	2.53%	12.4	$9.26 \times 10^{19}$
$^{110}\text{Pd } 0_2^+$ 1731.33 keV	1073.7 keV	86.73%	1.89%	10.1	$8.50 \times 10^{19}$
	657.76 keV <sup>a</sup>	95.32%	3.78%	12.4	$1.38 \times 10^{20}$
	255.49 keV	13.27%	0.36%	25.3	$6.46 \times 10^{18}$
	1475.80 keV	4.68%	0.12%	11.5	$4.87 \times 10^{18}$
	818.02 keV	8.59%	0.24%	16.3	$6.63 \times 10^{18}$
$^{110}\text{Pd } 2_3^+$ 1783.48 keV	1783.48 keV	21.57%	0.88%	6.2	$6.45 \times 10^{19}$
	1125.71 keV	78.43%	2.48%	12.0	$9.41 \times 10^{19}$
	657.76 keV	78.43%	2.99%	12.4	$1.09 \times 10^{20}$

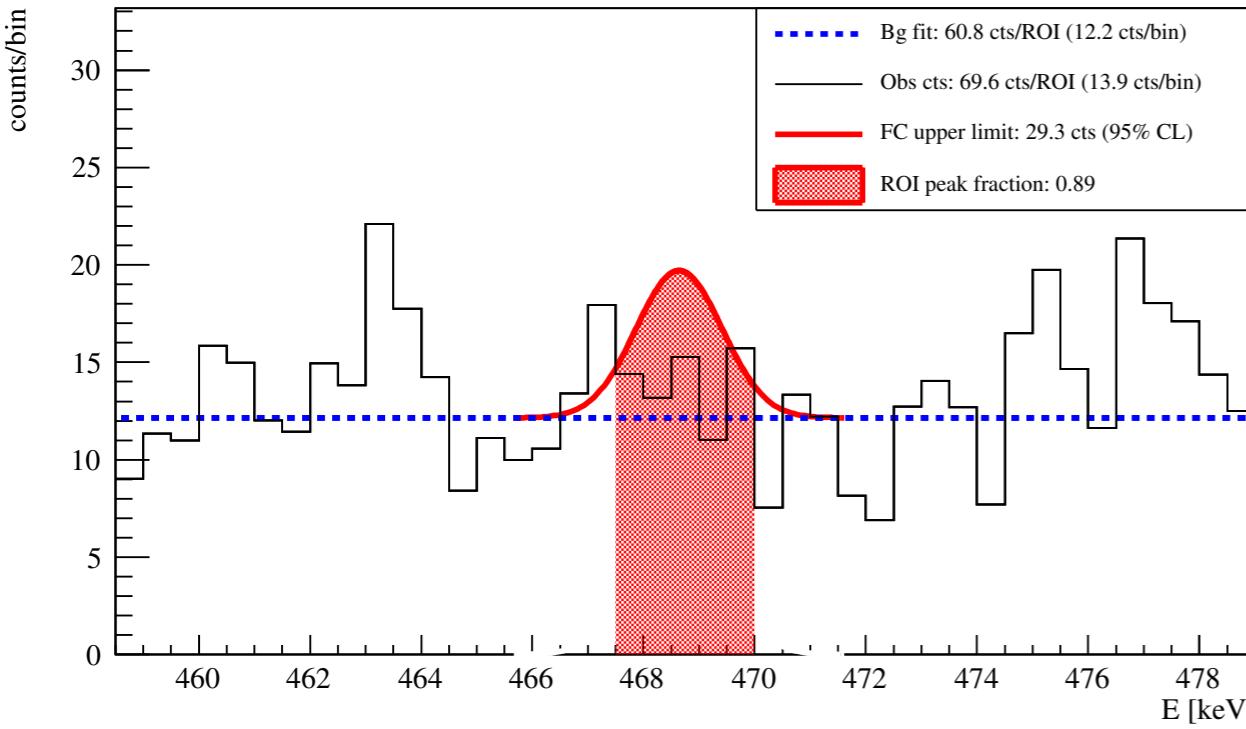
# Full Spectra Comparison

Pd: HADES-Felsenkeller Comparison

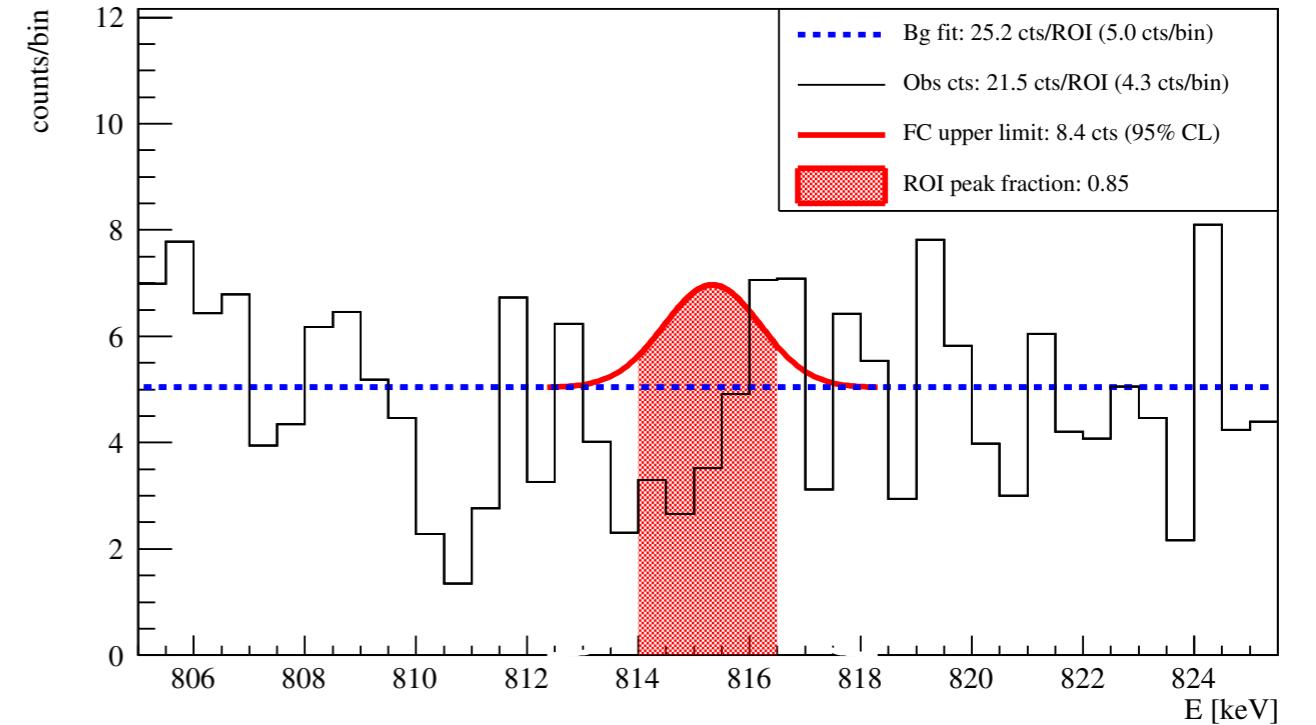
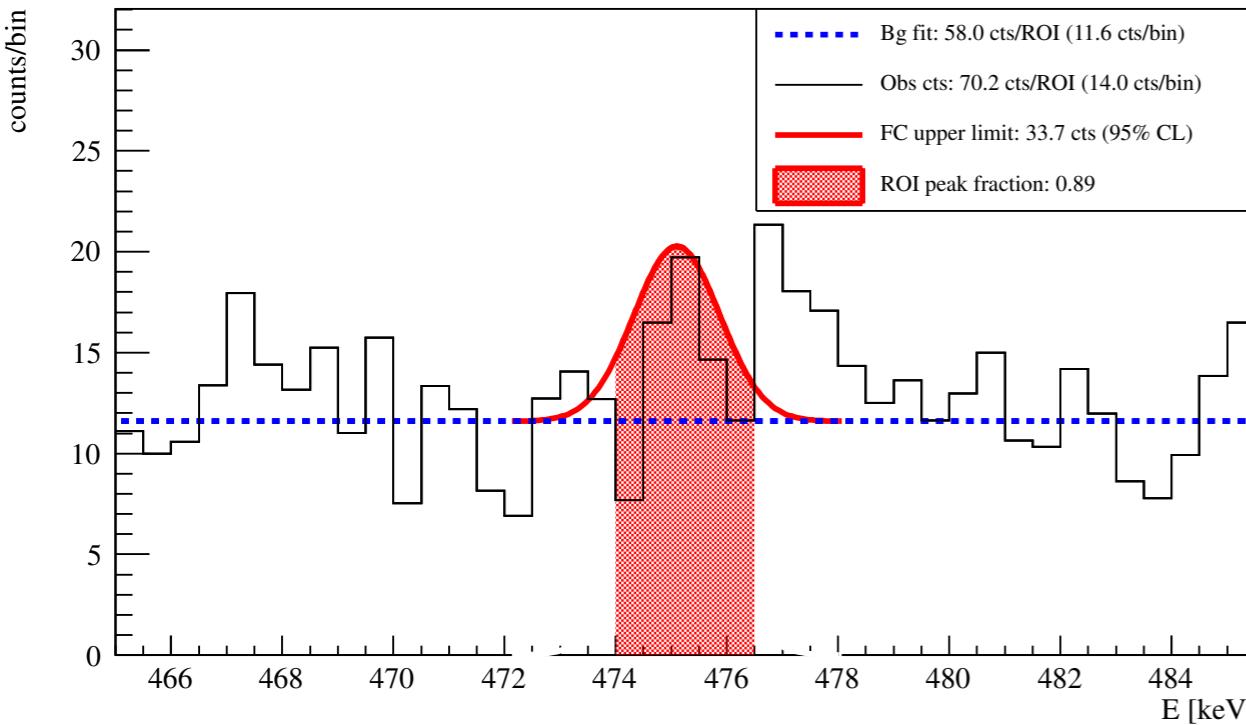
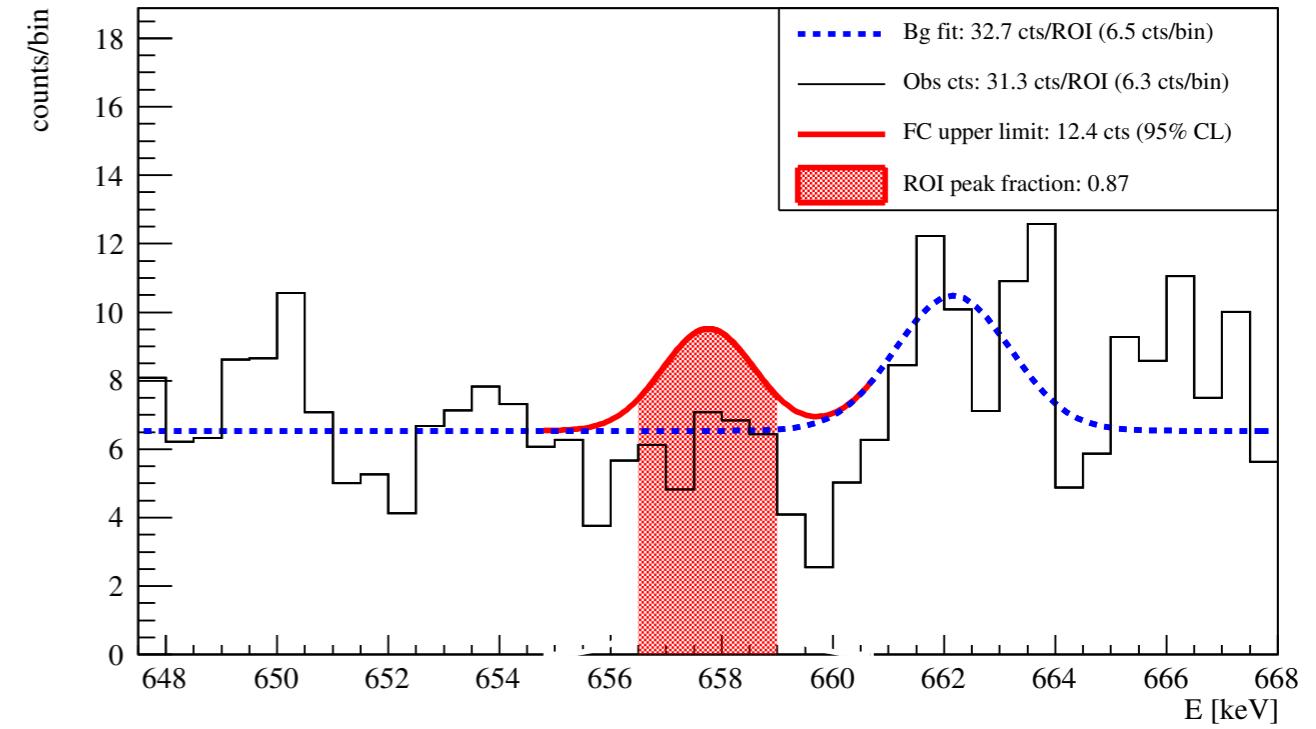


# Region of Interests

$^{102}\text{Pd}$

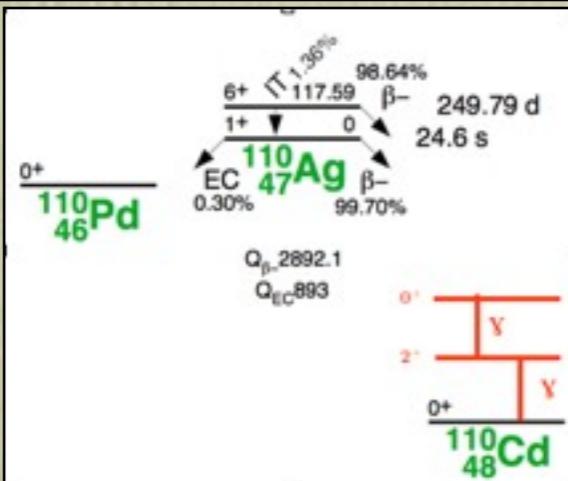


$^{110}\text{Pd}$

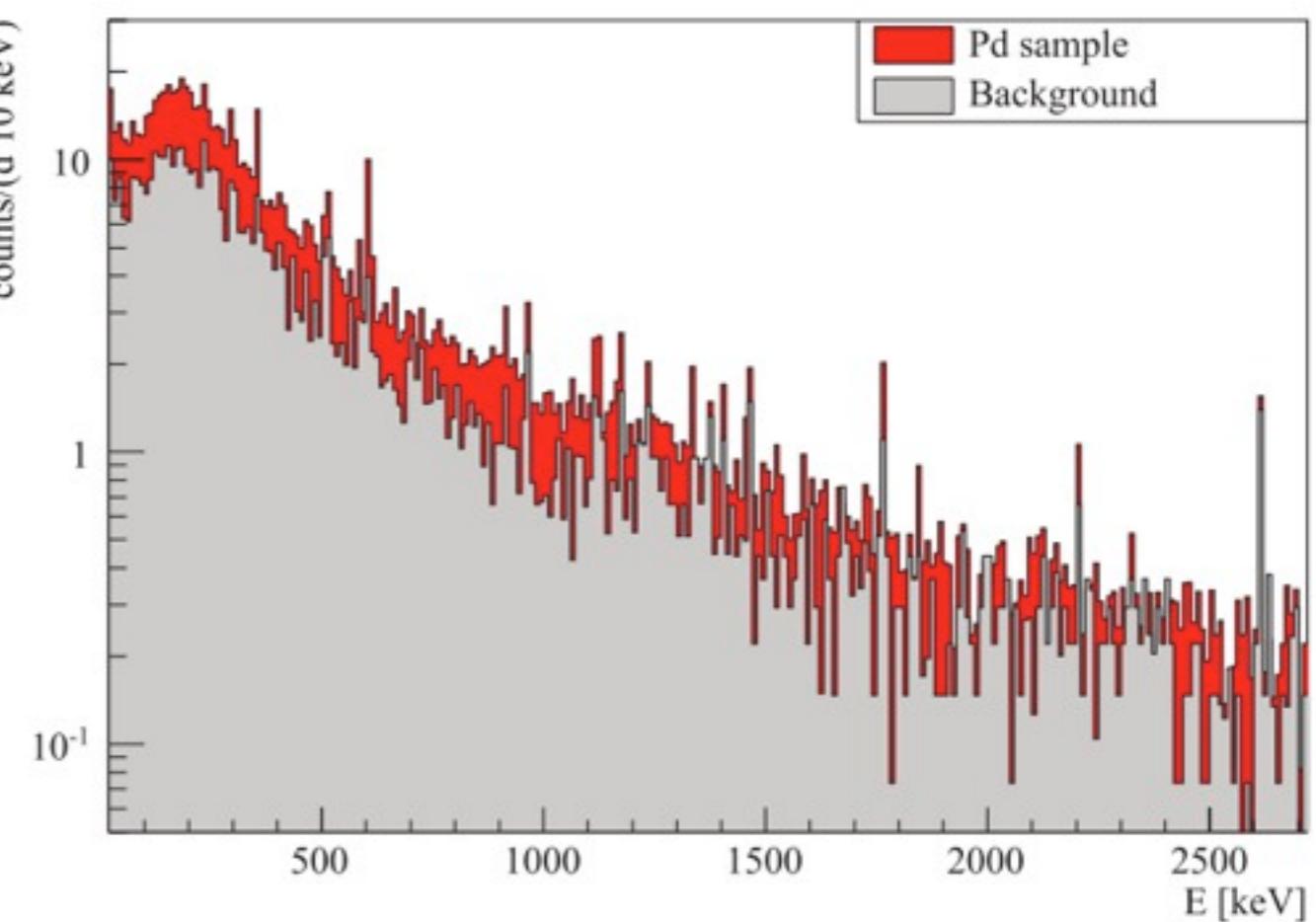


# Background of Pd Sample

Nuclide	$E$ (keV)	Massic activity (mBq/kg)	Decision threshold ( $\alpha = 95\%$ ) (mBq/kg)	Weighted mean massic activity (mBq/kg)
$^{214}\text{Pb}$	295.22	$1.9 \pm 1.0$	1.4	$1.4 \pm 0.4$
	351.93	$1.3 \pm 0.5$	0.6	
$^{214}\text{Bi}$	609.32	$1.9 \pm 0.4$	0.4	$1.9 \pm 0.4$
	1120.29	$2.0 \pm 0.8$	0.9	
	1238.11	—	2.2	
	1377.67	—	2.7	
	1764.54	—	3.2	
$^{210}\text{Pb}$	46.54	—	414.3	
$^{228}\text{Ac}$	911.20	—	0.5	
	968.97	—	0.9	
$^{212}\text{Pb}$	238.63	—	0.7	
$^{208}\text{Tl}$	583.19	—	0.6	
	2614.51	—	0.3	
$^{40}\text{K}$	1460.82	—	1.0	
$^{137}\text{Cs}$	661.66	—	0.2	
$^{60}\text{Co}$	1173.23	—	0.2	
	1332.49	—	0.1	



- Only  $^{214}\text{Pb}$  and  $^{214}\text{Bi}$  with measured activity
- Background dominated by environment and not by sample
- No indication for irreducible background of  $^{110m}\text{Ag}$ ,  $^{102}\text{Rh}$ ,  $^{102m}\text{Rh}$
- Improvement possible external bg reduction



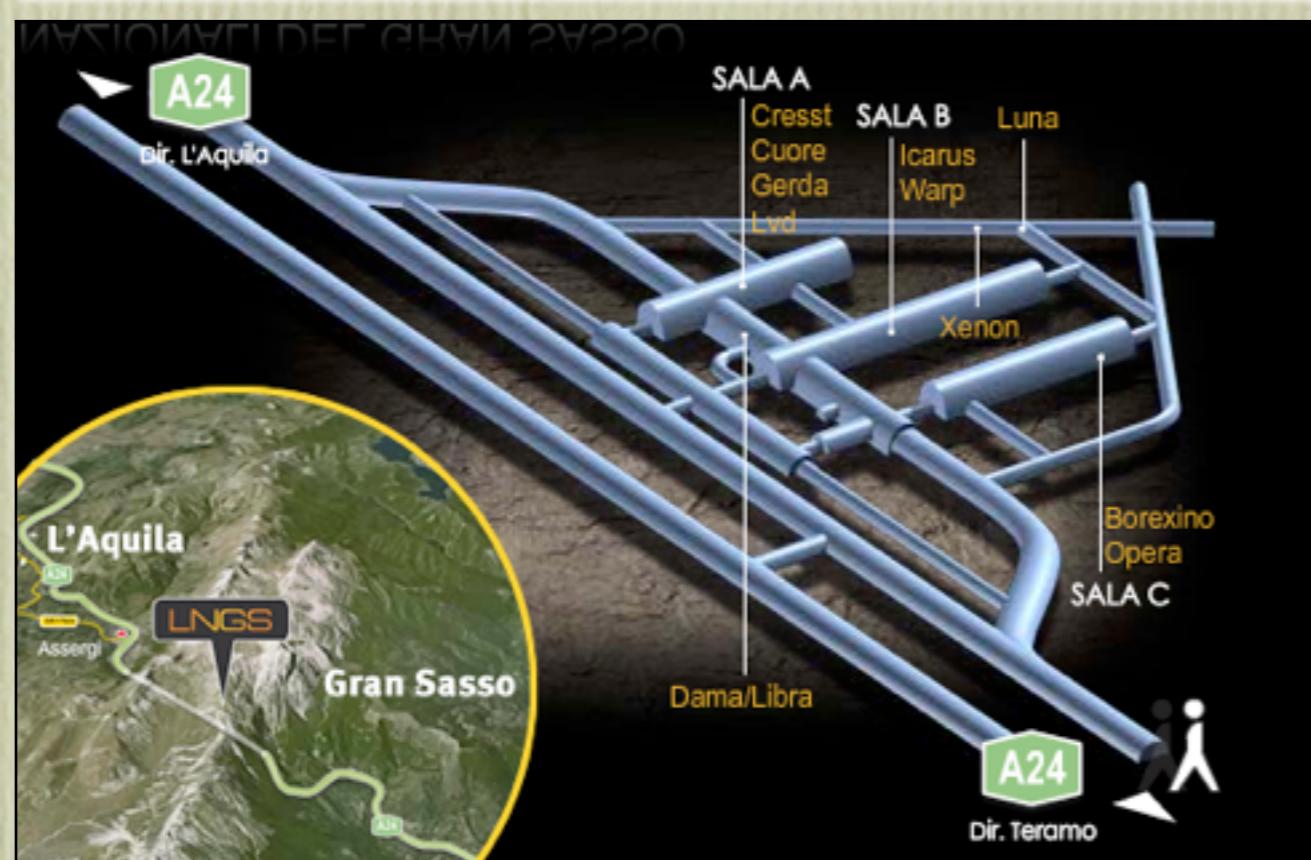
# New Half-Life Limits for $^{110}\text{Pd}$ and $^{102}\text{Pd}$

TABLE VI. Summary of measured half-life limits for all  $^{110}\text{Pd}$  and  $^{102}\text{Pd}$  double- $\beta$ -decay excited-state transitions.

Decay mode	$T_{1/2}$ limit (yr) (95%)
$^{110}\text{Pd } 2_1^+ \text{ 657.76 keV}$	$1.72 \times 10^{20}$
$^{110}\text{Pd } 0_1^+ \text{ 1473.12 keV}$	$1.98 \times 10^{20}$
$^{110}\text{Pd } 2_2^+ \text{ 1475.80 keV}$	$9.26 \times 10^{19}$
$^{110}\text{Pd } 0_2^+ \text{ 1731.33 keV}$	$1.38 \times 10^{20}$
$^{110}\text{Pd } 2_3^+ \text{ 1783.48 keV}$	$1.09 \times 10^{20}$
$^{102}\text{Pd } 2_1^+ \text{ 475.10 keV}$	$5.95 \times 10^{18}$
$^{102}\text{Pd } 0_1^+ \text{ 943.69 keV}$	$5.81 \times 10^{18}$
$^{102}\text{Pd } 2_2^+ \text{ 1103.05 keV}$	$8.55 \times 10^{18}$

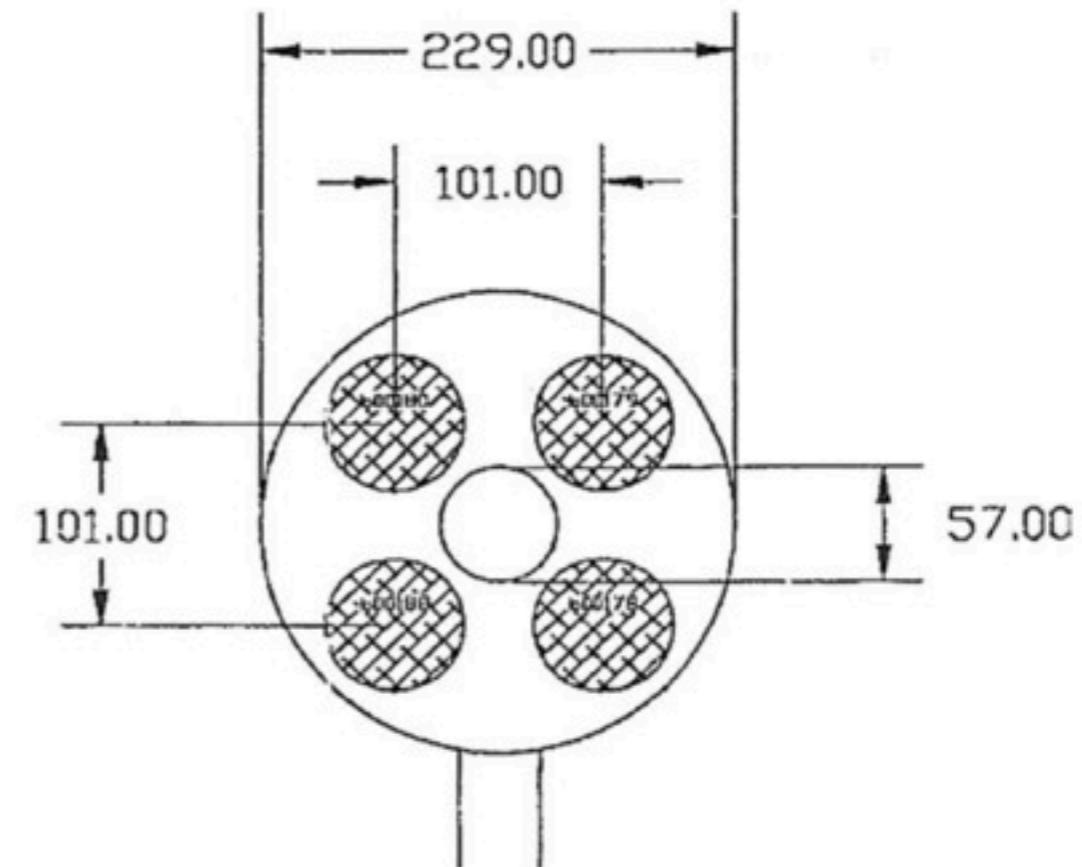
- Limit improved by factor 3 for  $0_1^+$  and  $2_1^+$  state in  $^{110}\text{Pd}$
- Experimental limits for all possible excited state transitions in  $^{110}\text{Pd}$  and  $^{102}\text{Pd}$

# Outlook @ LNGS



	Detectors			
	ge178	ge179	ge180	ge188
Volume (cm <sup>3</sup> )	225.2	225.0	225.0	220.7
Endcap and holder material				Electrolytical copper
Energy resolution (FWHM) at 1332 keV	2.1	2.0	2.0	2.0

- 85 d with 4-HPGe setup @ LNGS
- $\mu$ -flux reduced by factor  $10^6$
- Higher efficiency
- True coincidence analysis will reduce the background significantly
- Further measurement planned with Pd plates in thin layer around n-type HPGe: Detection of EC X-rays



# Conclusions

- World first experimental limits for DBD into excited states in  $^{110}\text{Pd}$  and  $^{102}\text{Pd}$
- Measurements in three state of the art underground gamma spectrometers
- Two measurements finished and published
- Third analysis is ongoing
- Challenge: 3 orders of magnitude improvement if theory is right

$0_1^+$ state		Nuclei	$E_{2\beta}$ , keV	Experiment $T_{1/2}, \text{y}$	Theory [18, 19]	Theory [23]
$^{150}\text{Nd}$	2627.1		$= 1.4_{-0.4}^{+0.5} \times 10^{20}$ [8]		-	-
$^{96}\text{Zr}$	2202.5		$> 6.8 \times 10^{19}$ [22]	$(2.4 - 2.7) \times 10^{21}$	$3.8 \times 10^{21}$	
$^{100}\text{Mo}$	1903.7		$= 6.2_{-0.7}^{+0.9} \times 10^{20}$	$1.6 \times 10^{21}$ [29]	$2.1 \times 10^{21}$	
$^{82}\text{Se}$	1507.5		$> 3.0 \times 10^{21}$ [24]	$(1.5 - 3.3) \times 10^{21}$	-	
$^{48}\text{Ca}$	1274.8		$> 1.5 \times 10^{20}$ [20]		-	
$^{116}\text{Cd}$	1048.2		$> 2.0 \times 10^{21}$ [26]		$1.1 \times 10^{22}$	$1.1 \times 10^{21}$
$^{76}\text{Ge}$	916.7		$> 6.2 \times 10^{21}$ [30]	$(7.5 - 310) \times 10^{21}$	$4.5 \times 10^{21}$	
$^{130}\text{Te}$	735.3		$> 2.3 \times 10^{21}$ [31]	$(5.1 - 14) \times 10^{22*}$	-	
$^{110}\text{Pd}$	544.8		$> 2.0 \times 10^{20}$	$(4.2 - 9.1) \times 10^{23}$	-	
$2_1^+$ state						arXiv:0710.2194
Nuclei	$E_{2\beta}$ , keV	Experiment		Theory [17]	Theory [18, 19]	
			$T_{1/2}, \text{y}$			
$^{48}\text{Ca}$	3288.5	$> 1.8 \times 10^{20}$ [20]	$1.7 \times 10^{24}$		-	
$^{150}\text{Nd}$	3033.6	$> 9.1 \times 10^{19}$ [21]		-	-	
$^{96}\text{Zr}$	2572.2	$> 7.9 \times 10^{19}$ [22]	$2.3 \times 10^{25}$	$(3.8 - 4.8) \times 10^{21}$		
$^{100}\text{Mo}$	2494.5	$> 1.6 \times 10^{21}$ [4]	$1.2 \times 10^{25}$	$3.4 \times 10^{22}$ [23]		
$^{82}\text{Se}$	2218.5	$> 1.4 \times 10^{21}$ [24]	-	$2.8 \times 10^{23}$ - $3.3 \times 10^{26}$		
$^{130}\text{Te}$	1992.7	$> 2.8 \times 10^{21}$ [25]	$6.9 \times 10^{26}$	$(3.0 - 27) \times 10^{22}$		
$^{116}\text{Cd}$	1511.5	$> 2.3 \times 10^{21}$ [26]	$3.4 \times 10^{26}$	$1.1 \times 10^{24}$		
$^{76}\text{Ge}$	1480	$> 1.1 \times 10^{21}$ [27]	$5.8 \times 10^{28}$	$(7.8 - 10) \times 10^{25}$		
$^{110}\text{Pd}$	1360.1	$> 1.7 \times 10^{20}$		$0.6 - 1.3 \times 10^{25}$		

# BACKUP

# Angular Correlation

$$W(\theta) = \frac{5}{4}(1 - 3\cos^2\theta + 4\cos^4\theta).$$

Angular Correlation of  $0+ \rightarrow 2+ \rightarrow 0+$  Transitions

