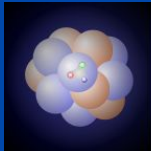


# Neutrino Interactions with Nucleons and Nuclei

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# Motivation and Contents

- Determination of neutrino oscillation parameters and axial properties of nucleons and resonances in accelerator experiments requires knowledge of neutrino energy, but the neutrino beam is broad in energy
- Modern experiments use nuclear targets
- Will show:  
Nuclear effects affect event characterization and neutrino energy reconstruction and limit oscillation parameter determination



# Neutrino Oscillations

$$\begin{aligned}
 P(\nu_\mu \rightarrow \nu_e) &\simeq \sin^2 2\theta_{13} \sin^2 \theta_{23} \frac{\sin^2[(1 - \hat{A})\Delta]}{(1 - \hat{A})^2} \\
 &- \alpha \sin 2\theta_{13} \xi \sin \delta \sin(\Delta) \frac{\sin(\hat{A}\Delta)}{\hat{A}} \frac{\sin[(1 - \hat{A})\Delta]}{(1 - \hat{A})} \\
 &+ \alpha \sin 2\theta_{13} \xi \cos \delta \cos(\Delta) \frac{\sin(\hat{A}\Delta)}{\hat{A}} \frac{\sin[(1 - \hat{A})\Delta]}{(1 - \hat{A})} \\
 &+ \alpha^2 \cos^2 \theta_{23} \sin^2 2\theta_{12} \frac{\sin^2(\hat{A}\Delta)}{\hat{A}^2} \\
 &\equiv O_1 + O_2(\delta) + O_3(\delta) + O_4 .
 \end{aligned}$$

$$\Delta = \frac{\Delta m_{21}^2 L}{4E}$$

$$\alpha = \frac{\Delta m_{21}^2}{\Delta m_{31}^2}$$

$$\xi = \cos \theta_{13} \sin(2\theta_{12}) \sin(2\theta_{23})$$

$$\hat{A} = \frac{2\sqrt{2}G_F n_e E}{\Delta m_{31}^2}$$

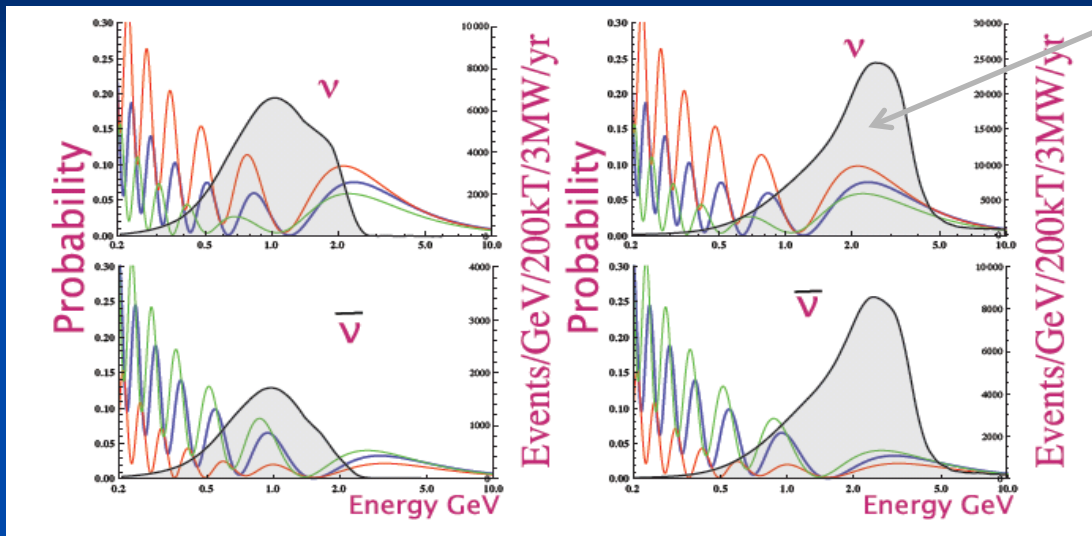
$\delta =$  CP violating phase

Vacuum  
oscillation

Matter effects,  
 $n_e =$  electron density

# LBNE, $\delta_{CP}$ sensitivity

From: Bishai et al., hep-ex 12034090



Flux distribution

From:  
Bishai et al  
arXiv:1203.409

$$\delta_{CP} = 0$$

$$\delta_{CP} = \pi/2$$

$$\delta_{CP} = -\pi/2$$

8 GeV

60 GeV

proton energy

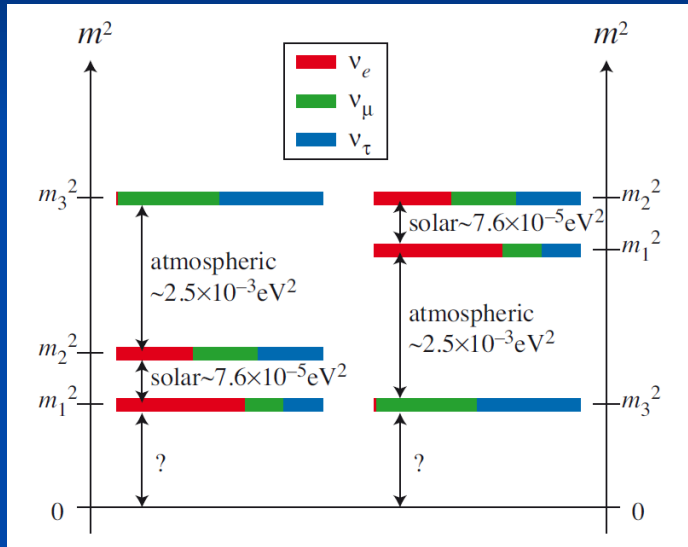
Need energy to distinguish between different  $\delta_{CP}$





# Oscillation Signal

## Dependence on Hierarchy and Mixing Angle



Energy has to be known better than 100 MeV  
 Shape sensitive to hierarchy and sign of  
 mixing angle

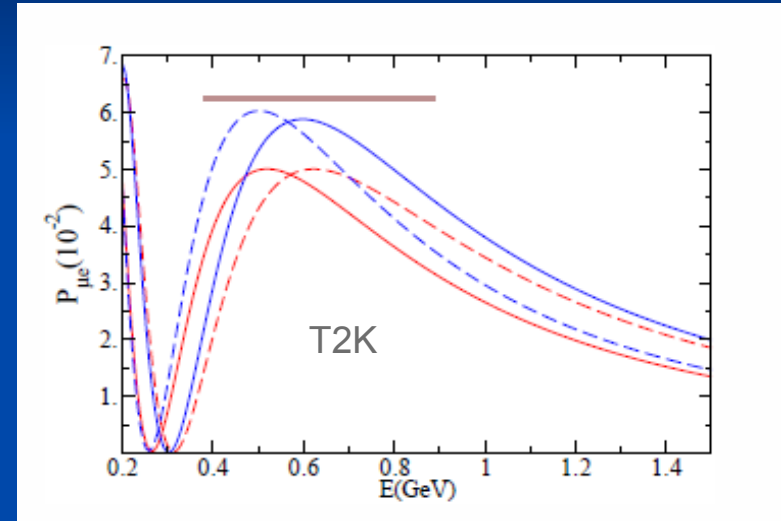
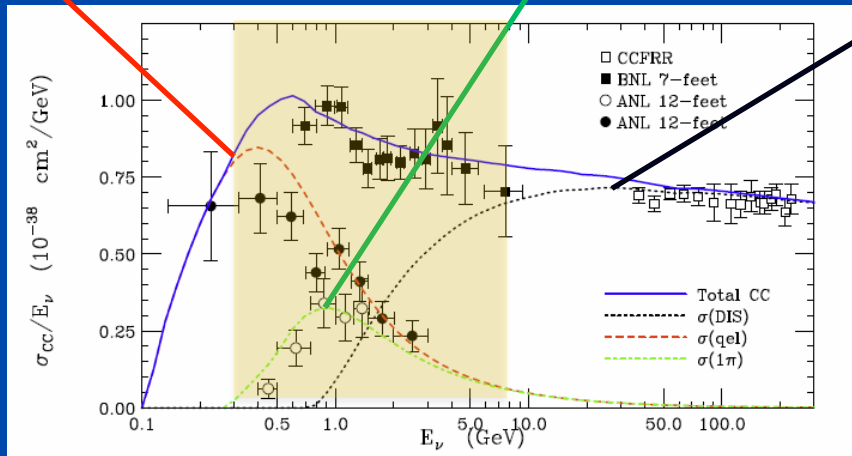
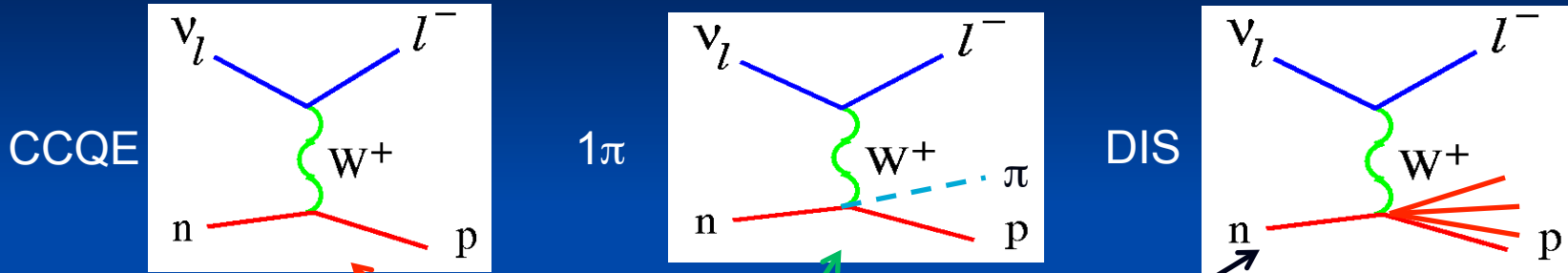


Fig. 2.  $P_{\mu e}$  in matter versus neutrino energy for the T2K experiment. The blue curves depict the normal hierarchy, red the inverse hierarchy. Solid curves depict positive  $\theta_{13}$ , dashed curves negative  $\theta_{13}$

D.J. Ernst et al., arXiv:1303.4790 [nucl-th]

# Neutrino-nucleon cross section



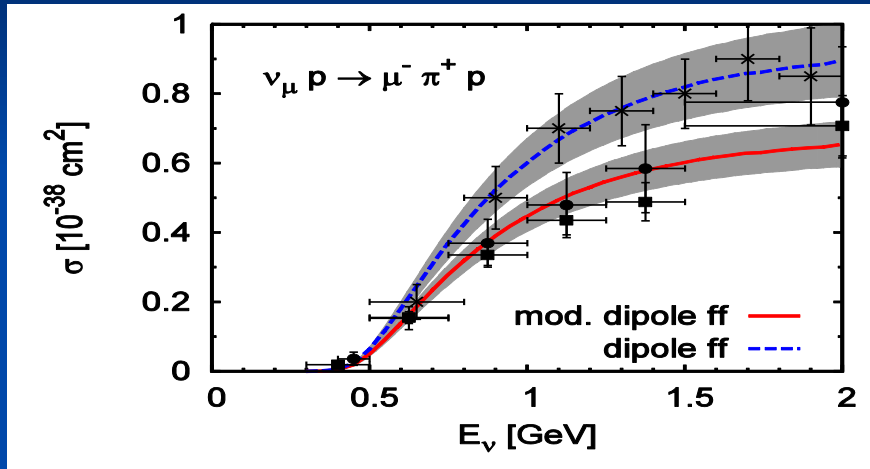
note:

$$10^{-38} \text{ cm}^2 = 10^{-11} \text{ mb}$$

In the region of most experiments (0.5 – 10 GeV) all 3 mechanisms overlap



# Pion Production



10 % error in  $C_5^A(0)$

data:  
PRD 25, 1161 (1982), PRD 34, 2554 (1986)

discrepancy between elementary data sets

→ impossible to determine 3 axial formfactors from these data

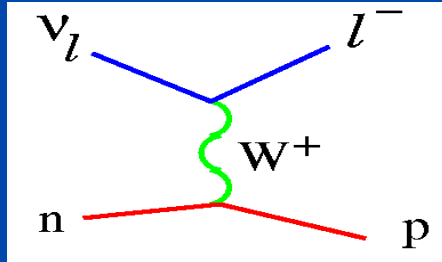
# Energy Reconstruction

- Energy reconstruction
  1. Through QE: needs event identification
  2. Calorimetric: needs simulation of thresholds and non-measured events
- In both methods nuclear many-body structure and reaction theory are needed



# Energy Reconstruction by QE

- In QE scattering on nucleon at rest outgoing lepton determines neutrino energy:

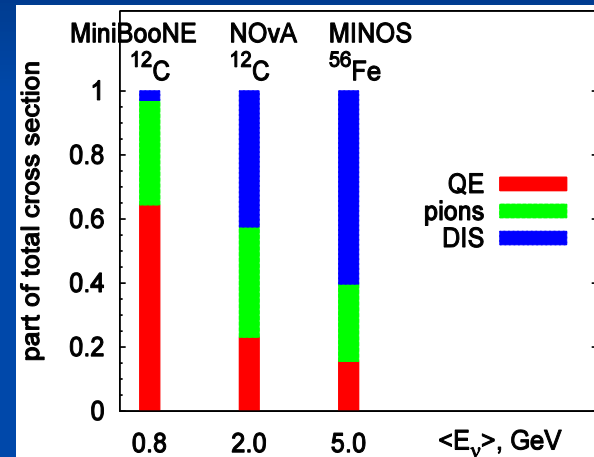
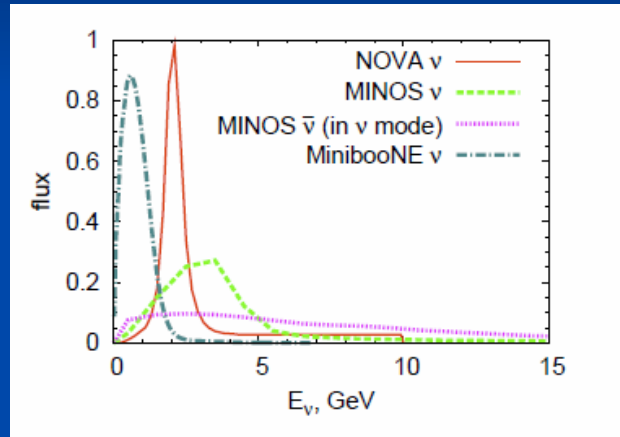


$$E_\nu = \frac{2M_N E_\mu - m_\mu^2}{2(M_N - E_\mu + p_\mu \cos \theta_\mu)}$$

- **Trouble:** all presently running exps use nuclear targets
  1. Nucleons are Fermi-moving
  2. Final state interactions may hinder correct event identification

# Neutrino Beams

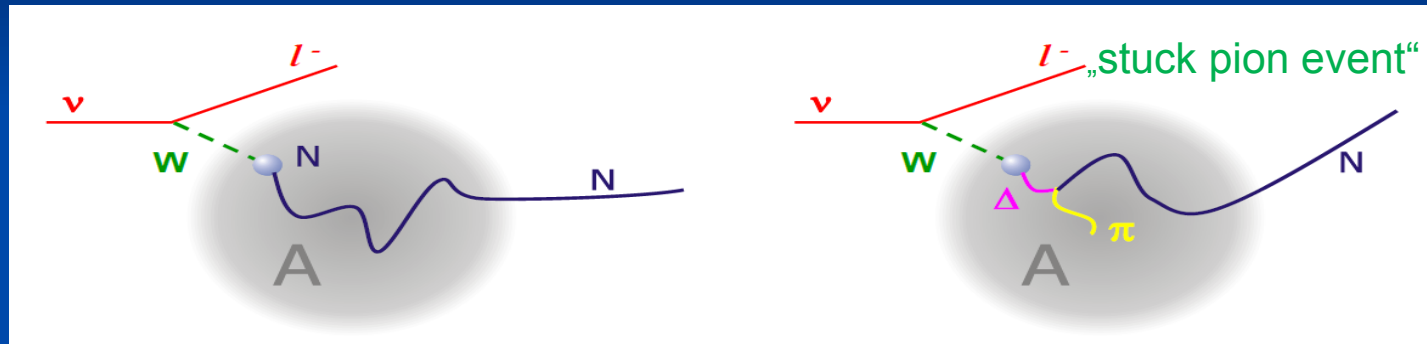
- Neutrinos do not have fixed energy nor just one reaction mechanism



Have to reconstruct energy from final state of reaction

Different initial processes entangled: can lead to same final states!

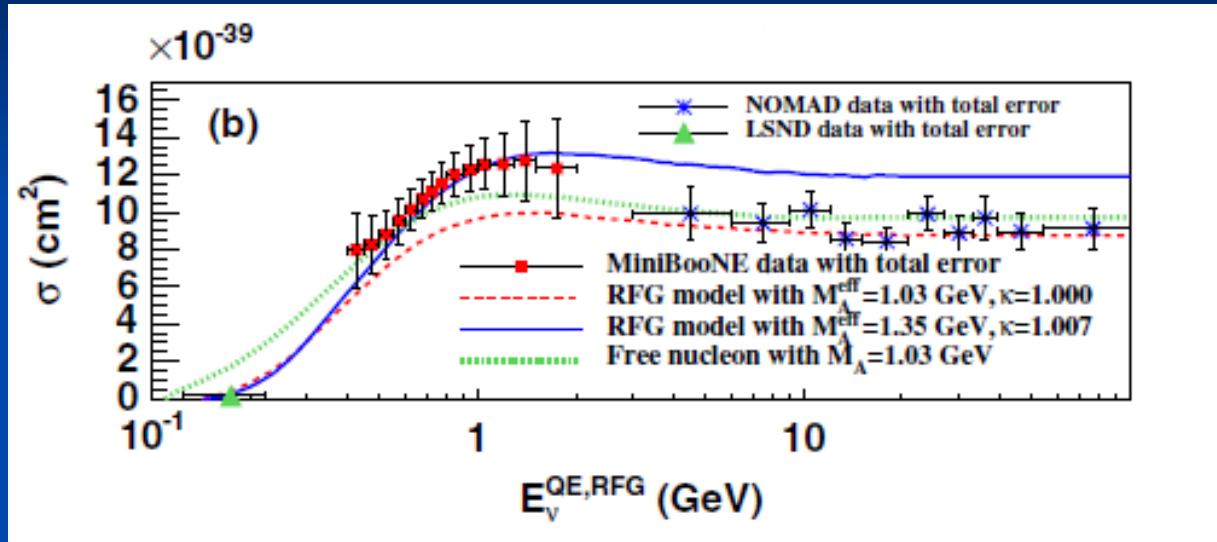
# Final State Interactions in Nuclear Targets



Complication to identify QE, entangled with  $\pi$  production

Nuclear Targets (K2K, MiniBooNE, T2K, MINOS, Minerva, ....)

# MiniBooNE QE puzzle



World average  
axial mass:  
 $M_A = 1.03$  GeV

MB employs Cerenkov counter: identifies QE by muon and 0 pion,  
corrects for 'stuck pions'



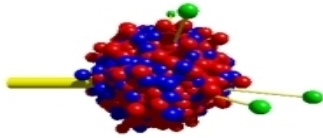
# FSI and Transport Theory

- All modern experiments use nuclear targets
- Need to model final state interactions
  1. to identify reaction mechanism
  2. to reconstruct incoming neutrino energy from final state

Quantum mechanical description not possible to describe

$\nu + A \rightarrow X + \text{many hadrons}$

→ Need Transport Theory (event generators)



- **GiBUU : Theory and Event Generator**  
based on a Botermans-Malfliet solution of Kadanoff-Baym equations
- Physics content: **Phys. Rept. 512 (2012) 1**  
Code available from <http://gibuu.hepforge.org>
- **GiBUU** describes (within the same unified theory and code)
  - heavy ion reactions, particle production and flow
  - pion and proton induced reactions
  - low and high energy photon and electron induced reactions
  - **neutrino induced reactions**

.....using the same physics input! And the same code!



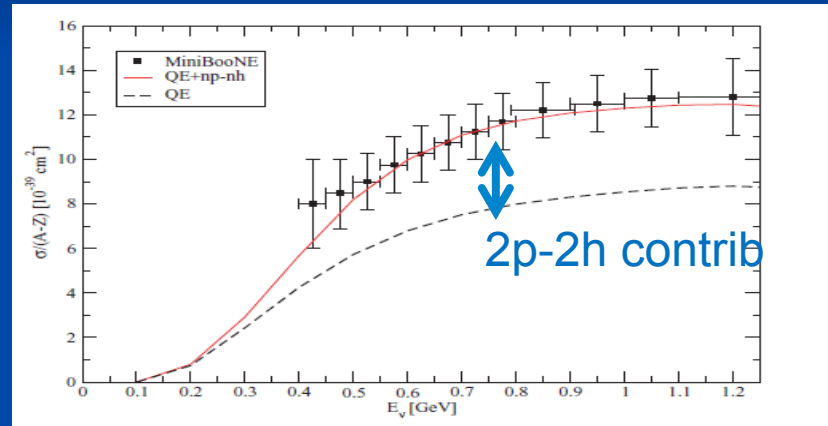
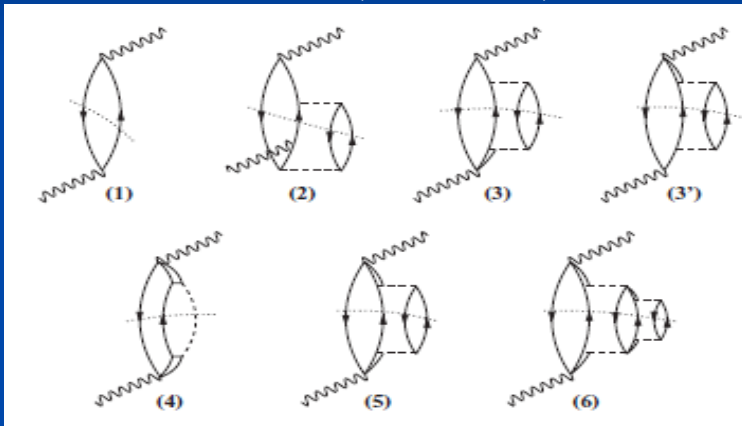
# Nuclear Effects

- Impulse approximation,  
local Fermi gas or spectral functions
- RPA essential up to about 0.7 GeV and  
small  $Q^2$ , rather irrelevant for most exps.
- Coherent X-section negligeably small:  
 $\sigma \approx 10^{-40} \text{ cm}^2$ , per cent level



# The MiniBooNE QE Puzzle Explanations

Martini et al, PRC80, 2009



Exp: both  $\sigma$  and  $E_\nu$  are reconstructed!

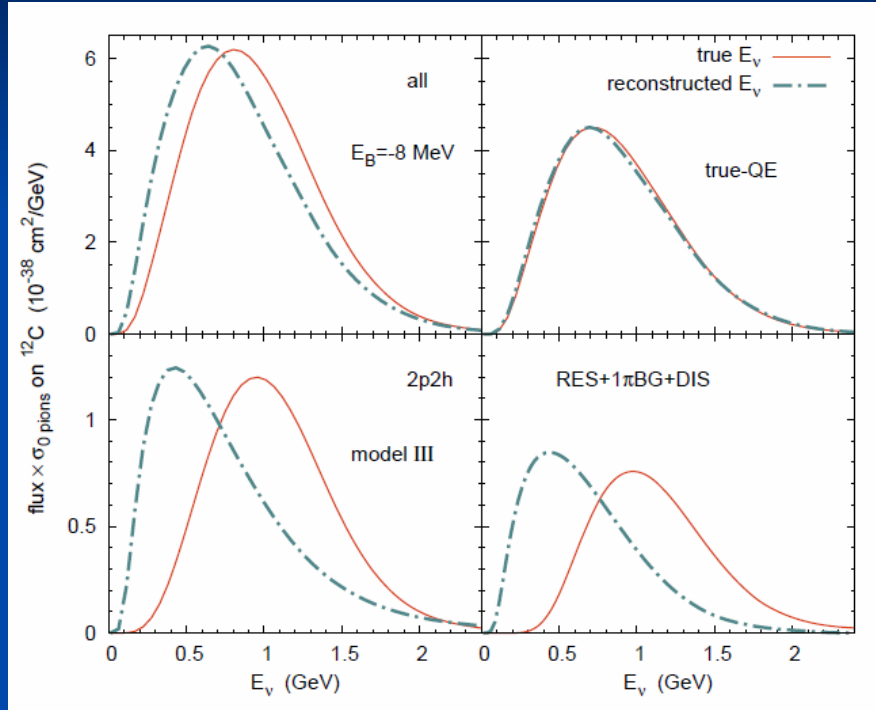
# Energy reconstruction analysis

- Assume: GiBUU is nature
- Smear all cross sections (QE, 2p2h, pion production, DIS) with exp. flux distribution to get measured distributions
- Assume QE kinematics to reconstruct  $E_\nu$



# Energy reconstruction in MB

Event rates = flux x crosssection

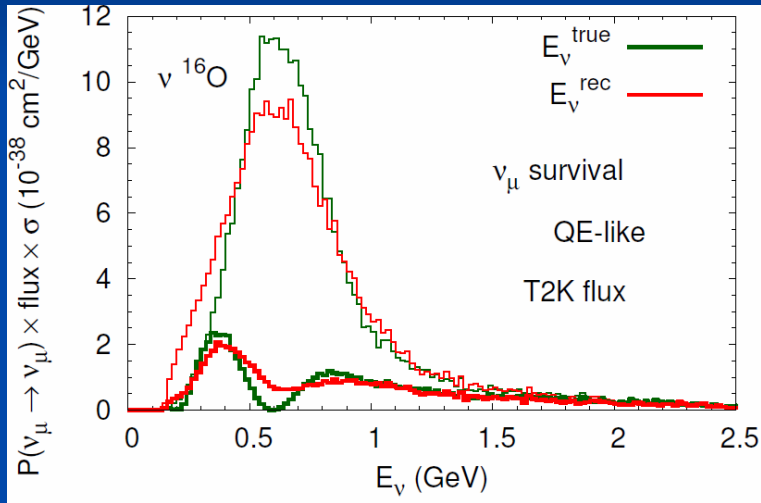


MiniBooNE flux

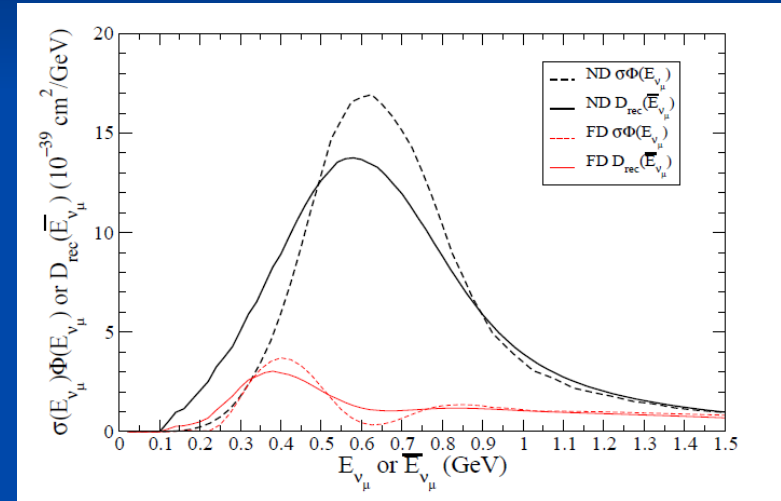
Reconstructed energy shifted to lower energies for all processes beyond QE  
Reconstruction must be done for 0 pion events

# Oscillation signal in T2K

## $\nu_\mu$ disappearance



GiBUU

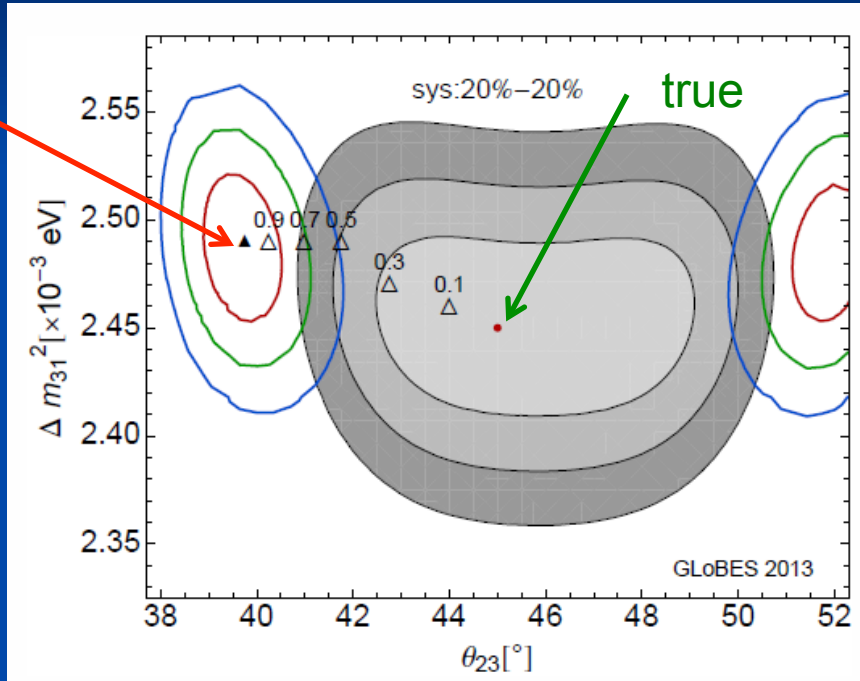


Martini. Chanfray et al



# Sensitivity of oscillation parameters to nuclear model

reconstructed



P. Coloma, P. Huber,  
arXiv:1308.6822

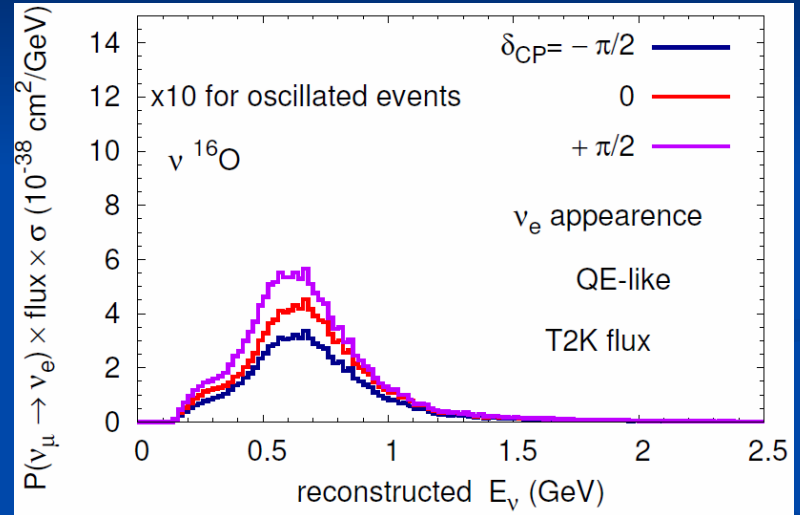
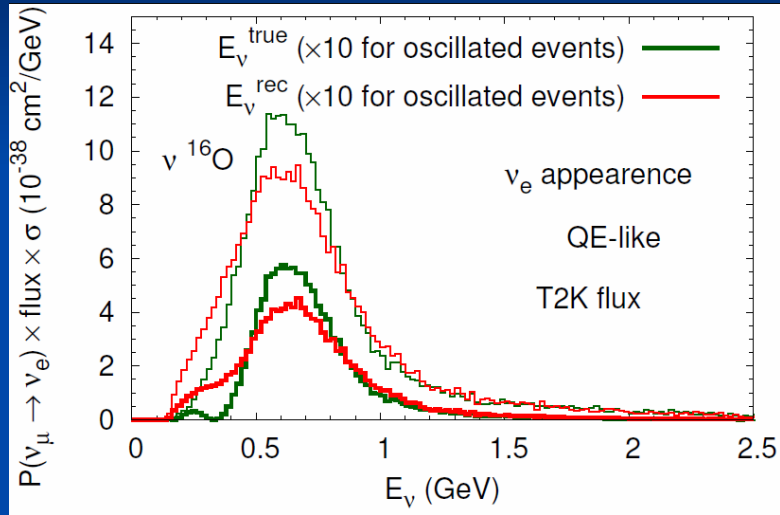
Analysis based on GiBUU

T2K



# Oscillation signal in T2K

## $\delta_{CP}$ sensitivity of appearance expts



Uncertainties due to energy reconstruction  
as large as  $\delta_{CP}$  dependence

# Sensitivity of T2K to Energy Reconstruction

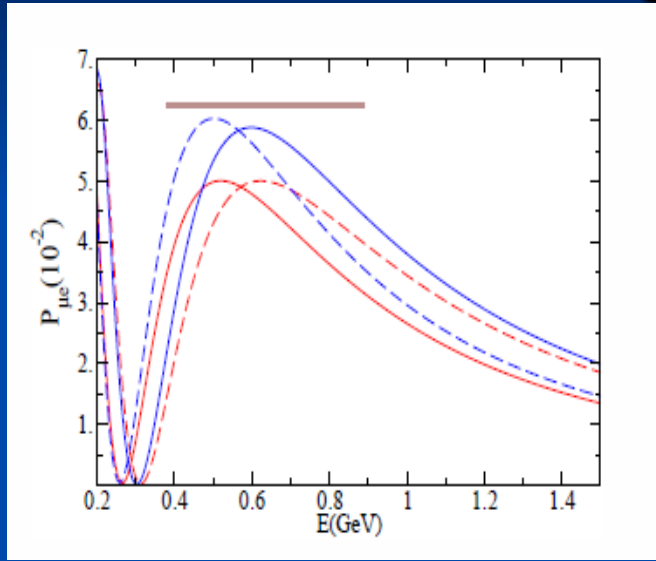
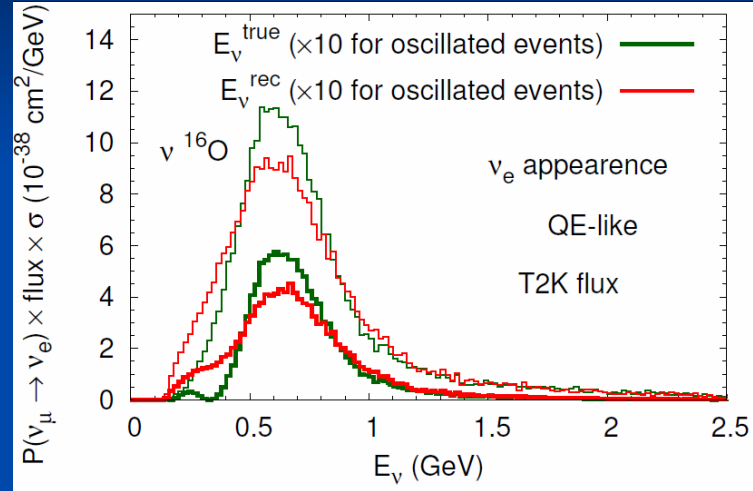


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D.J. Ernst et al., arXiv:1303.4790 [nucl-th]



# Summary

- Event generators for neutrino-nucleus interactions have to describe QE,  $\pi$  production and DIS simultaneously
- Energy reconstruction based on QE leads to downward shift of reconstructed distribution
- $\delta_{CP}$  determination depends crucially on energy reconstruct.
- Precision era of neutrino physics requires much more sophisticated generators and a dedicated effort in theory



A wake-up call for the high-energy physics community:



Low-Energy  
Nuclear Physics  
determines response  
of nuclei to high-energy  
neutrinos

# Relevant Refs

- *Pion production in the MiniBooNE experiment.*

Olga Lalakulich, Ulrich Mosel (Giessen U.). Oct 2012. 21 pp.

Published in Phys.Rev. C87 (2013) 014602

- *Energy reconstruction in quasielastic scattering in the MiniBooNE and T2K experiments.*

O. Lalakulich, U. Mosel (Giessen U.). Aug 2012. 15 pp.

Published in Phys.Rev. C86 (2012) 054606

- *Neutrino- and antineutrino-induced reactions with nuclei between 1 and 50 GeV.*

O. Lalakulich (Giessen U.), K. Gallmeister (Frankfurt U.), U. Mosel (Giessen U.). May 2012.

Published in Phys.Rev. C86 (2012) 014607

- *Many-Body Interactions of Neutrinos with Nuclei - Observables.*

O. Lalakulich (Giessen U.), K. Gallmeister (Frankfurt U.), U. Mosel (Giessen U.). Mar 2012. 22 pp.

Published in Phys.Rev. C86 (2012) 014614

- *Transport-theoretical Description of Nuclear Reactions.*

O. Buss, T. Gaitanos, K. Gallmeister, H. van Hees, M. Kaskulov, O. Lalakulich, A.B. Larionov, T. Leitner, J. Weil, U. Mosel (Giessen U.). Jun 2011. 170 pp.

Published in Phys.Rept. 512 (2012) 1-124

