

Sterile neutrinos from low energy to the GUT scale

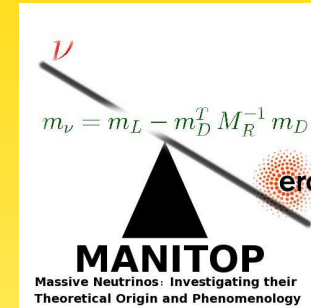


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17/09/13



Outline

- General aspects and phenomenology
 - What is a sterile neutrino?
 - What is its mass?
 - 3 (4) well motivated scales and some phenomenology
 - * eV
 - * keV
 - * (TeV)
 - * heavy
- Models for light sterile neutrinos: 3 ways to make them light

What is a sterile neutrino?

SM contains 3 active neutrinos with isospin $\frac{1}{2}$

$$\begin{pmatrix} \nu_e \\ e^- \end{pmatrix}_L, \quad \begin{pmatrix} \nu_\mu \\ \mu^- \end{pmatrix}_L, \quad \begin{pmatrix} \nu_\tau \\ \tau^- \end{pmatrix}_L$$

their CP -partners are also active:

$$\begin{pmatrix} e^+ \\ \bar{\nu}_e \end{pmatrix}_R, \quad \begin{pmatrix} \mu^+ \\ \bar{\nu}_\mu \end{pmatrix}_R, \quad \begin{pmatrix} \tau^+ \\ \bar{\nu}_\tau \end{pmatrix}_R$$

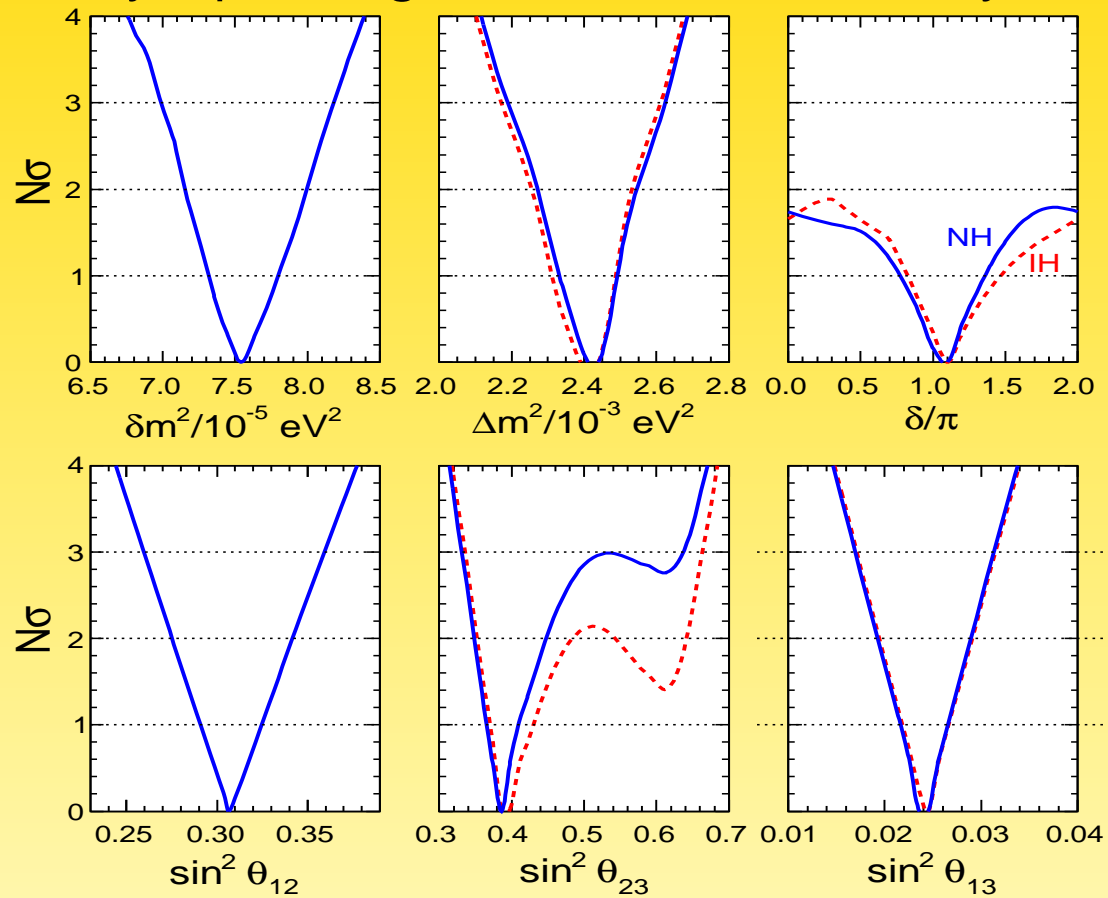
the $(\nu_{e,\mu,\tau})_L$ and $(\bar{\nu}_{e,\mu,\tau})_R$ take part in weak interactions = couple to W, Z

What is a sterile neutrino?

- add a fourth state to the game, but don't give it isospin!
⇒ **a sterile neutrino** ν_s
- a sterile neutrino ν_s does NOT take part in weak interactions = does NOT couple to W, Z
- can mix with active neutrinos
- can couple to Higgs
- can couple to BSM physics

Neutrino Physics: Status of global fits

Synopsis of global 3ν oscillation analysis



Fogli, Lisi *et al.*, June 2012

Lessons

- consistent picture emerging
- there are 3 generation effects!
- about 2σ hint for $\theta_{23} < \pi/4$
- about 1σ hint for $\delta \neq 0$
- no hint for hierarchy
- future program of LBL experiments to pin down, make more precise
- all is well...?

Light Sterile Neutrinos

\leftrightarrow is there an additional **sterile** state at $\Delta m^2 \sim \text{eV}^2$ and mixing $\mathcal{O}(0.1)$?

- LSND ($\bar{\nu}_\mu \rightarrow \bar{\nu}_e$) 3.8σ
- MiniBooNE ($\bar{\nu}_\mu \rightarrow \bar{\nu}_e$ and $\nu_\mu \rightarrow \nu_e$) 3.8σ
- Gallium anomaly ($\nu_e \rightarrow \nu_e$) 2.9σ
- reactor anomaly ($\bar{\nu}_e \rightarrow \bar{\nu}_e$) 2.8σ
- cosmology and astroparticle physics

Sterile Neutrinos: Disappearance vs. Appearance

$$U = \begin{pmatrix} U_{e1} & U_{e2} & U_{e3} & U_{e4} \\ U_{\mu1} & U_{\mu2} & U_{\mu3} & U_{\mu4} \\ U_{\tau1} & U_{\tau2} & U_{\tau3} & U_{\tau4} \\ U_{s1} & U_{s2} & U_{s3} & U_{s4} \end{pmatrix}$$

$$P(\nu_{\mu} \rightarrow \nu_e) = 4 |U_{e4}|^2 |U_{\mu4}|^2 \sin^2 \frac{\Delta m_{41}^2 L}{4E}$$

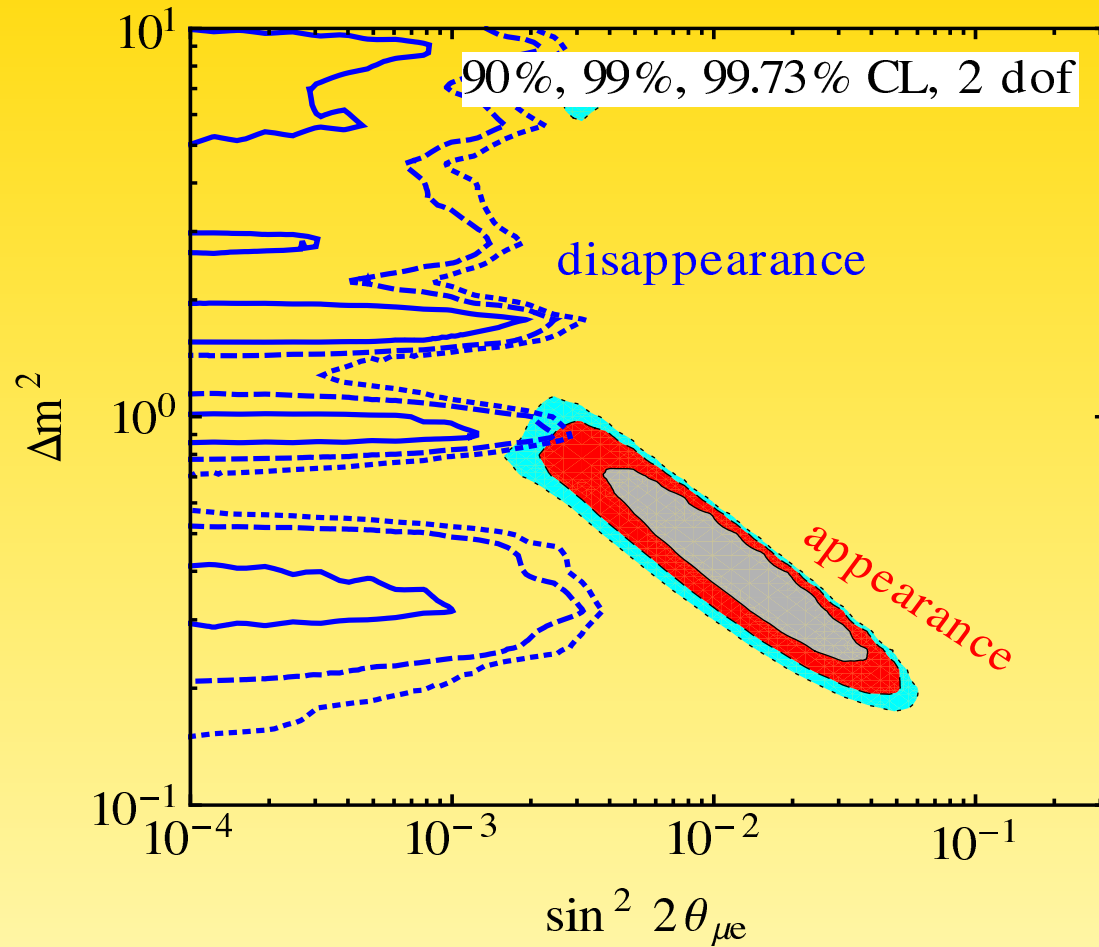
$$P(\nu_e \rightarrow \nu_e) = 1 - 4 |U_{e4}|^2 (1 - |U_{e4}|^2) \sin^2 \frac{\Delta m_{41}^2 L}{4E}$$

$$P(\nu_{\mu} \rightarrow \nu_{\mu}) = 1 - 4 |U_{\mu4}|^2 (1 - |U_{\mu4}|^2) \sin^2 \frac{\Delta m_{41}^2 L}{4E}$$

\Rightarrow if $\nu_{\mu} \rightarrow \nu_e$, then there should be $\nu_e \rightarrow \nu_e$ and $\nu_{\mu} \rightarrow \nu_{\mu}$

\Leftrightarrow tension between appearance and disappearance data...

Sterile Neutrinos: Disappearance vs. Appearance

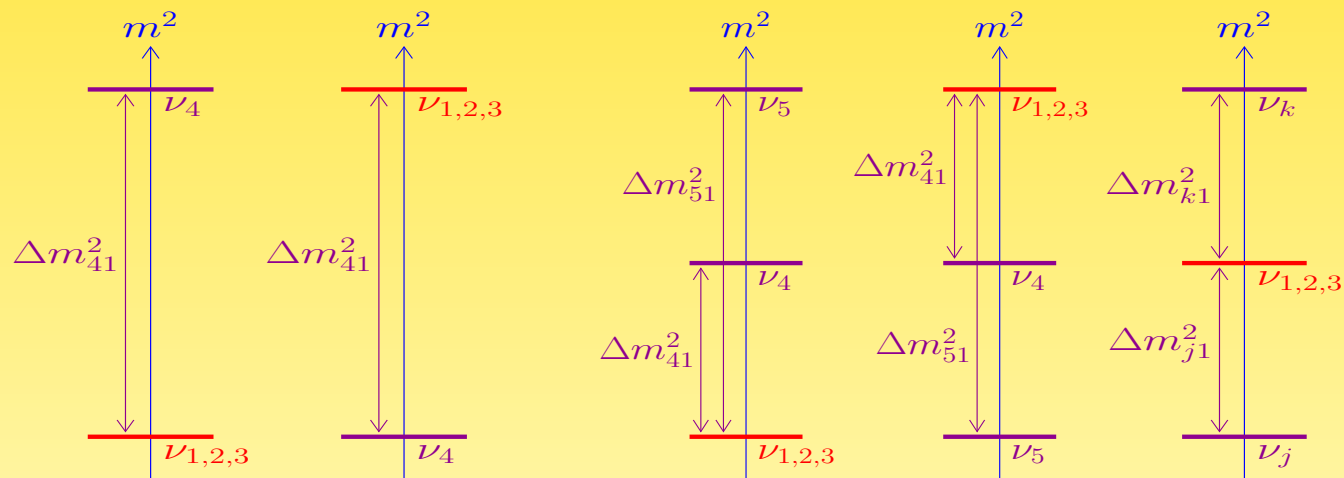


some overlap at 99 % CL, consistency has p -value $\simeq 10^{-4}$...

Kopp, Machado, Maltoni, Schwetz, 1303.3031

Sterile Neutrinos: more than one?

- does not help much for tension between appearance and disappearance
- mass ordering? 3+2 or 1+3+1



Sterile Neutrinos: Typical Values

	Δm_{41}^2	$ U_{e4} $	$ U_{\mu 4} $	Δm_{51}^2	$ U_{e5} $	$ U_{\mu 5} $	$\gamma_{\mu e}$	$p(\text{app./dis.})$
3+1	0.93	0.15	0.17					1.2×10^{-4}
3+2	0.47	0.13	0.15	0.87	0.14	0.13	-0.15π	3.4×10^{-5}
1+3+1	-0.87	0.15	0.13	0.47	0.13	0.17	0.06π	2.1×10^{-3}

Kopp, Machado, Maltoni, Schwetz, 1303.3031

$$P_{\nu_\alpha \rightarrow \nu_\beta}^{\text{SBL}} = 4 |U_{\alpha 4}|^2 |U_{\beta 4}|^2 \sin^2 \phi_{41} + 4 |U_{\alpha 5}|^2 |U_{\beta 5}|^2 \sin^2 \phi_{51} \\ + 8 |U_{\alpha 4} U_{\beta 4} U_{\alpha 5} U_{\beta 5}| \sin \phi_{41} \sin \phi_{51} \cos(\phi_{54} - \gamma_{\alpha\beta})$$

$$\phi_{ij} \equiv \frac{\Delta m_{ij}^2 L}{4E}, \quad \gamma_{\alpha\beta} \equiv \arg(I_{\alpha\beta 54}), \quad I_{\alpha\beta ij} \equiv U_{\alpha i}^* U_{\beta i} U_{\alpha j} U_{\beta j}^*$$

experimental tests: talk by Karsten Heeger...

Experiments...

Important: New Sterile Experiments & Plans

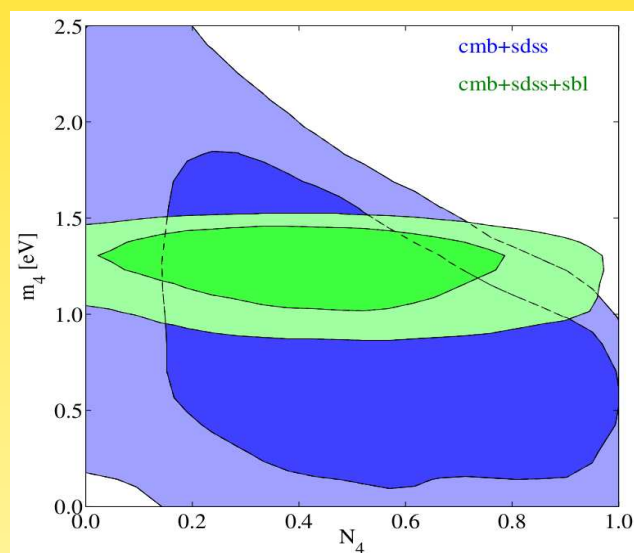
Experiment Type	Appearance / Disappearance	Oscillation Channel	Projects
Reactor	Disappearance	$\bar{\nu}_e \rightarrow \bar{\nu}_e$	Nucifer, Stéréo, Scraam, Neutrino-4, DANSS, Poséidon, MARS, ...
Radioactive Source	Disappearance	$\bar{\nu}_e \rightarrow \bar{\nu}_e$ $\nu_e \rightarrow \nu_e$	CeLAND, SOX (Cr & Ce), Sage2, SNO+, LENS-s
Cyclotron	Disappearance	$\bar{\nu}_e \rightarrow \bar{\nu}_e$	IsoDAR
Pion / Kaon Decay-at-Rest	Apparition & Disappearance	$\bar{\nu}_\mu \rightarrow \bar{\nu}_e$ $\nu_e \rightarrow \nu_e$	OscSNS, CLEAR, DAEΔALUS, KDAR
Pion Decay-in-Flight (Beam)	Appearance & Disappearance	$\nu_\mu \rightarrow \nu_e$ $\bar{\nu}_\mu \rightarrow \bar{\nu}_e$ $\nu_\mu \rightarrow \nu_\mu$ $\nu_e \rightarrow \nu_e$	MINOS+, MicroBooNE, LAr1kton+MicroBooNE, Icarus/Nessie@CERN
Low-E Neutrino Factory	Appearance & Disappearance	$\nu_e \rightarrow \nu_\mu$ $\bar{\nu}_e \rightarrow \bar{\nu}_\mu$ $\nu_\mu \rightarrow \nu_\mu$ $\bar{\nu}_e \rightarrow \bar{\nu}_e$	vSTORM@Fermilab

Potential \leftrightarrow hints, speed, cost \leftrightarrow funding, challenges, ...

See also [Light Sterile Neutrinos: A White Paper, 1204.5379](#)

Motivation for Sterile Neutrinos: Cosmology

- CMB and power matter spectrum prefer $N_{\text{eff}} > 3$
- BBN prefers $N_{\text{eff}} > 3$
- Planck: $N_{\text{eff}} = 3.5 \pm 0.5$



Giunti, Hannestad *et al.*, 1302.6720, talk by Steen Hannestad

model-dependent, inconsistent data sets?

can be avoided by asymmetries, new interactions,...

Phenomenology of eV steriles: β -decays

with non-zero U_{e4} and m_4 :

- Kurie-plot experiments:

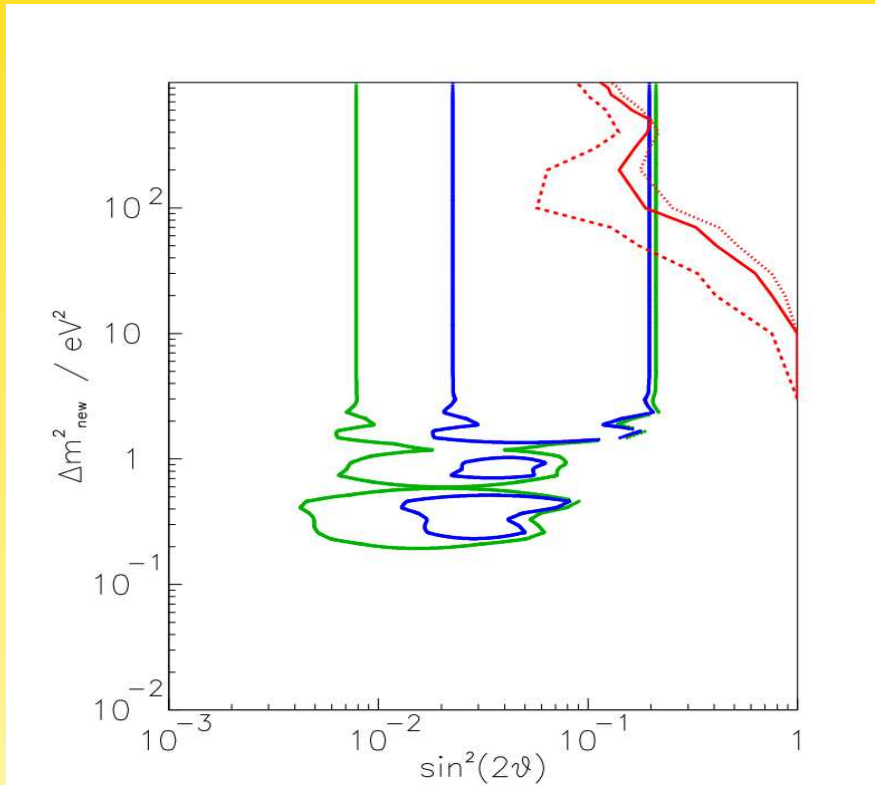
$$m_\beta^2 = |U_{e1}|^2 m_1^2 + |U_{e2}|^2 m_2^2 + |U_{e3}|^2 m_3^2 + |U_{e4}|^2 m_4^2 \leq (2.2 \text{ eV})^2$$

- neutrinoless double beta decay experiments:

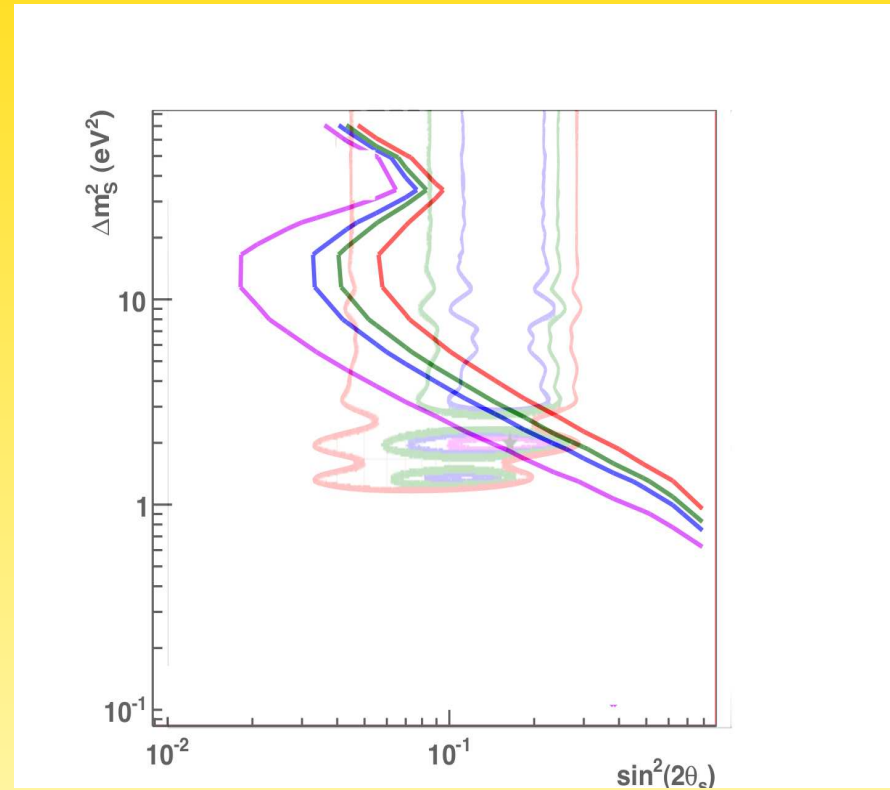
$$|m_{ee}| = |U_{e1}^2 m_1 + U_{e2}^2 m_2 + U_{e3}^2 m_3 + U_{e4}^2 m_4| \leq 0.3 \text{ eV}$$

Phenomenology of eV steriles

Neutrino mass observables: β decays



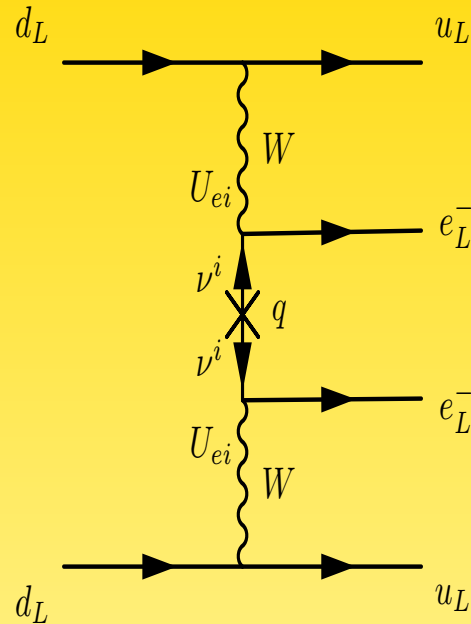
Mainz



Sejersen Riis, Hannestad;

Formaggio, Barret

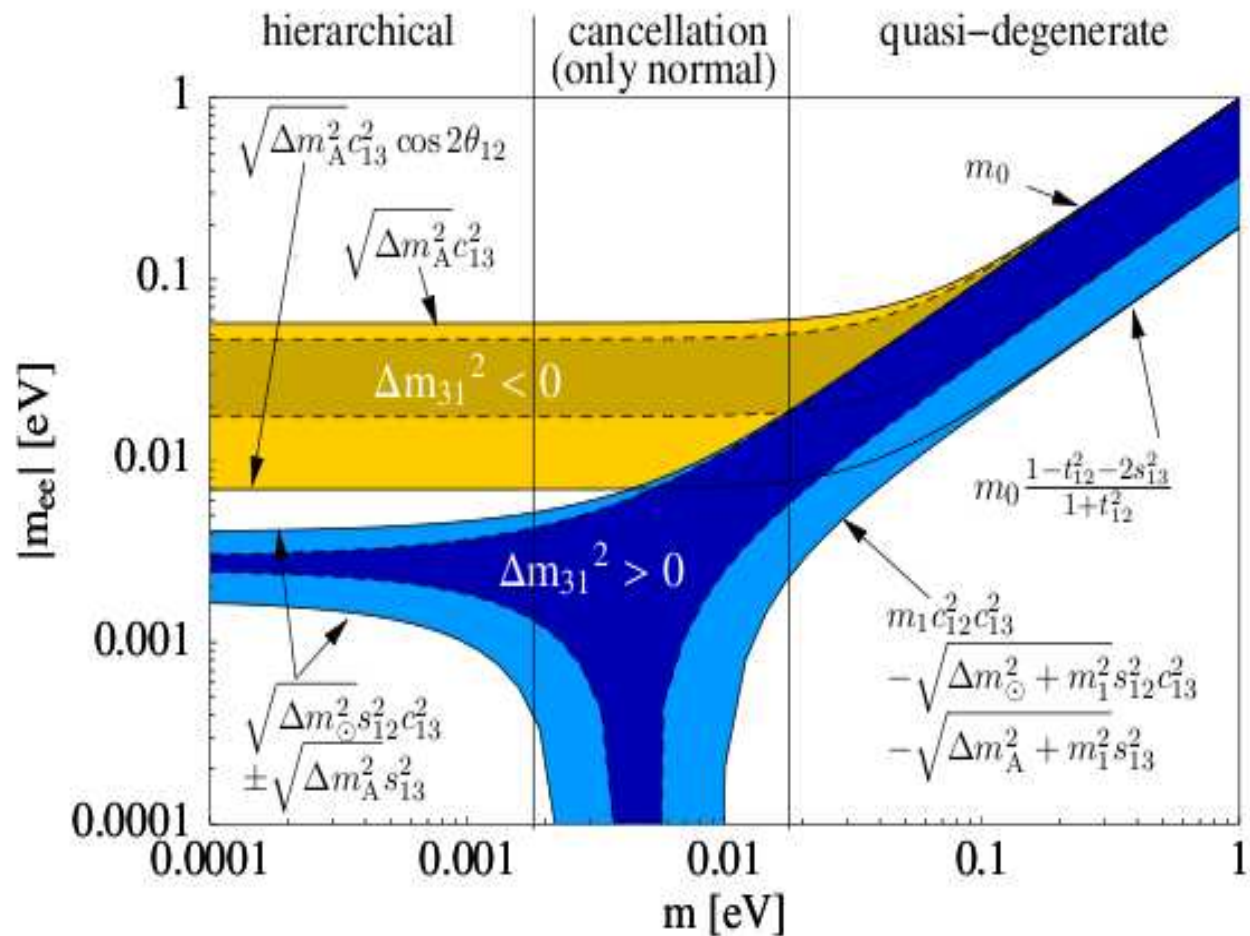
Neutrinoless double beta decay: $nn \rightarrow pp e^- e^-$



Amplitude proportional to

$$\frac{U_{ei}^2 m_i}{q^2 - m_i^2} \propto \begin{cases} U_{ei}^2 m_i & \text{for light neutrinos } q^2 \gg m_i^2 \\ \frac{U_{ei}^2}{m_i} & \text{for heavy neutrinos } q^2 \ll m_i^2 \end{cases}$$

The usual plot for double beta decay...



Sterile Neutrinos and $0\nu\beta\beta$

- recall $|m_{ee}|_{\text{NH}}^{\text{act}}$ can vanish and $|m_{ee}|_{\text{IH}}^{\text{act}}$ cannot vanish

- $|m_{ee}| = \underbrace{||U_{e1}|^2 m_1 + |U_{e2}|^2 m_2 e^{2i\alpha} + |U_{e3}|^2 m_3 e^{2i\beta}}_{m_{ee}^{\text{act}}} + \underbrace{|U_{e4}|^2 m_4 e^{2i\Phi_1}}_{m_{ee}^{\text{st}}}$

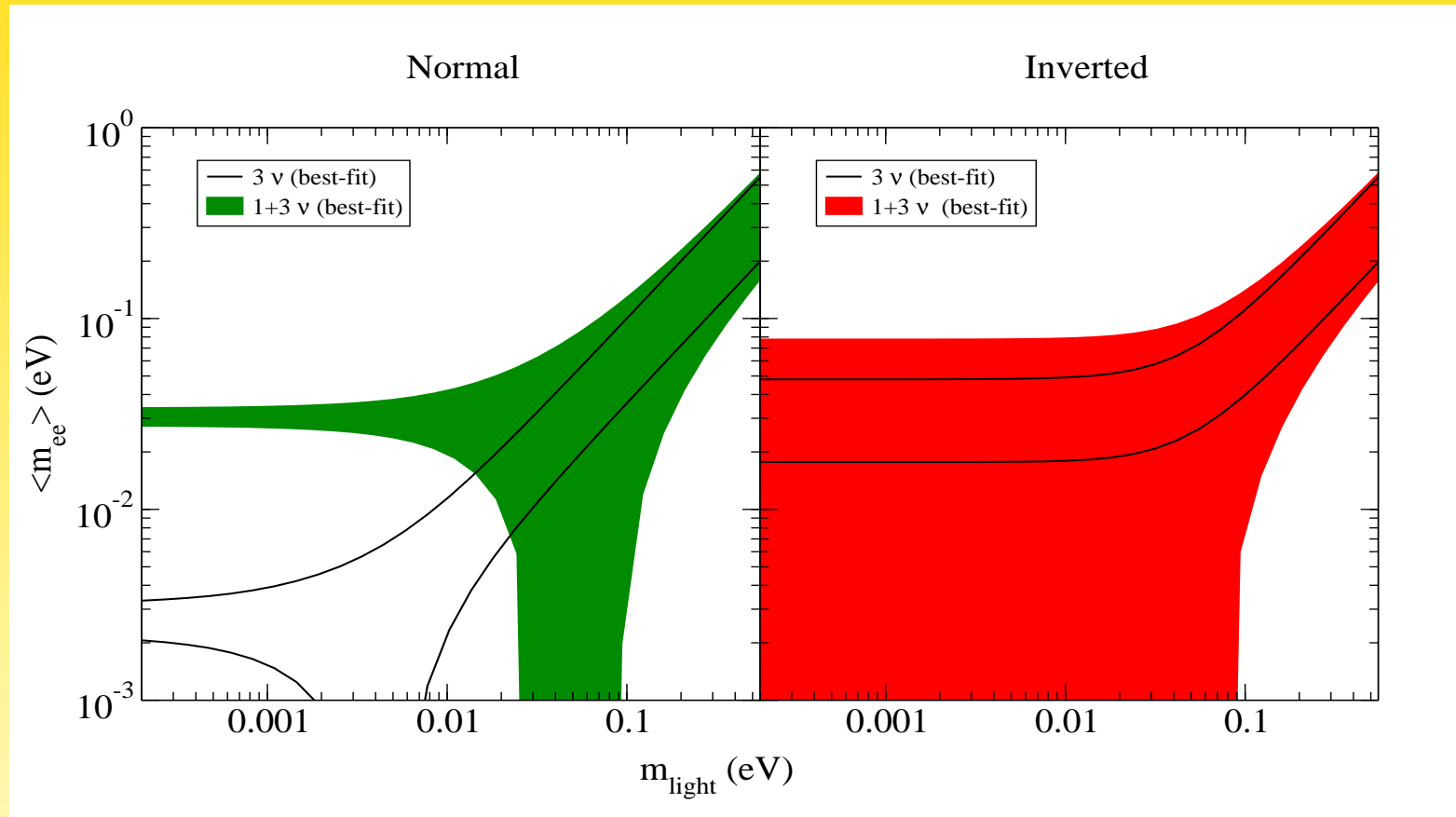
- sterile contribution to $0\nu\beta\beta$:

$$|m_{ee}|^{\text{st}} \simeq \sqrt{\Delta m_{\text{st}}^2} |U_{e4}|^2 \begin{cases} \gg |m_{ee}|_{\text{NH}}^{\text{act}} \\ \simeq |m_{ee}|_{\text{IH}}^{\text{act}} \end{cases}$$

- $\Rightarrow |m_{ee}|_{\text{NH}}$ cannot vanish and $|m_{ee}|_{\text{IH}}$ can vanish!

Barry, W.R., Zhang, JHEP 1107; Giunti *et al.*, PRD **87**; Girardi, Meroni,
Petcov, 1308.5802

The usual plot for double beta decay...
... gets completely turned around!



Barry, W.R., Zhang, JHEP 1107; Giunti *et al.*, PRD **87**; Girardi, Meroni,
Petcov, 1308.5802

Other Sterile Neutrinos

- very light \ll eV (\leftrightarrow missing upturn of P_{ee}^{\odot})
- keV (\leftrightarrow Warm Dark Matter)
- $10^{10} \dots 10^{15}$ GeV (\leftrightarrow GUTs, leptogenesis)
- [TeV (\leftrightarrow LHC)]

What is a sterile neutrino?

- add a fourth state to the game, but don't give it isospin!

⇒ **a sterile neutrino** ν_s

- a sterile neutrino ν_s does NOT take part in weak interactions = does NOT couple to W, Z
- can mix with active neutrinos
- can couple to Higgs
- can couple to BSM physics

we discuss N_R , the right-handed neutrino of the seesaw mechanism, and assume that it is Majorana, and assume that no other New Physics is there

Seesaw: Formalism

$$\mathcal{L} = \frac{1}{2} (\bar{\nu}_L, \bar{N}_R^c) \begin{pmatrix} 0 & m_D \\ m_D^T & M_R \end{pmatrix} \begin{pmatrix} \nu_L^c \\ N_R \end{pmatrix}$$

6×6 mass matrix diagonalized by

$$U_\nu \simeq \begin{pmatrix} 1 - \frac{1}{2} B B^\dagger & B \\ -B^\dagger & 1 - \frac{1}{2} B^\dagger B \end{pmatrix} \begin{pmatrix} U & 0 \\ 0 & V_R \end{pmatrix} \quad \text{with } B = m_D M_R^{-1}$$

light neutrino mass matrix:

$$m_\nu = -m_D M_R^{-1} m_D^T = U \text{diag}(m_1, m_2, m_3) U^T$$

heavy neutrino mass matrix:

$$M_R = V_R \text{diag}(M_1, M_2, M_3) V_R^T$$

N_R is a sterile neutrino

What is the mass of a Sterile Neutrino?

total mass term for active neutrinos and sterile neutrino(s):

$$\mathcal{L} = \frac{1}{2} (\bar{\nu}_L, \bar{N}_R^c) \begin{pmatrix} 0 & m_D \\ m_D^T & M_R \end{pmatrix} \begin{pmatrix} \nu_L^c \\ N_R \end{pmatrix}$$

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- SM singlet, not protected by v , hence GUT-scale, or $B - L$ breaking scale, or Planck-scale \Rightarrow naturally large
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so, what now?

What is the mass of a Sterile Neutrino?

$$\mathcal{L} = \frac{1}{2} (\bar{\nu}_L, \bar{N}_R^c) \begin{pmatrix} 0 & m_D \\ m_D^T & M_R \end{pmatrix} \begin{pmatrix} \nu_L^c \\ N_R \end{pmatrix}$$

special cases:

- $m_D = 0$; **pure Majorana case**
- $M_R = 0$; **pure Dirac case**
- $M_R \gg m_D$; **seesaw case**
- $m_D \gg M_R$; **pseudo-Dirac case**
- $M_D \sim M_R$; **ugly case**

What is the mass of a Sterile Neutrino?

The seesaw limit $M_R \gg m_D$

$$m_\nu = \frac{m_D^2}{M_R}$$

does this fix everything?

No, multiply m_D with x and M_R with x^2 : leaves m_ν invariant

Formalism

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3 active neutrinos mix with each other through

$$N \equiv U \left(1 - \frac{1}{2} B B^\dagger \right) \text{ with } B = m_D M_R^{-1}$$

3 active neutrinos mix with sterile neutrinos via

$$\theta_{\alpha i} = (m_D M_R^{-1} V_R)_{\alpha i} = \frac{[m_D V_R^*]_{\alpha i}}{M_i} = \mathcal{O}(\sqrt{m_\nu / M_R})$$

Consequences

- unitarity violation of PMNS matrix of order $(m_D/M_R)^2$

$$\epsilon_\alpha \equiv \sum_{i \geq 4} |(\mathcal{U}_\nu)_{\alpha i}|^2 \Rightarrow \begin{cases} \epsilon_e - \epsilon_\mu & = 0.0022 \pm 0.0025 \\ \epsilon_\mu - \epsilon_\tau & = 0.0017 \pm 0.0038 \\ \epsilon_e - \epsilon_\tau & = 0.0039 \pm 0.0040 \end{cases}$$

Loinaz *et al.*, PRD **70**

- Lepton flavor violation

$$\text{BR}(\mu \rightarrow e\gamma) \propto |N_{\mu i}^* N_{ei} f(m_i/m_W) + \theta_{\mu i}^* \theta_{ei} g(M_i/m_W)|^2 \lesssim 1.1 \times 10^{-8}$$

- neutrinoless double beta decay

$$\sum N_{ei}^2 m_i \lesssim 0.3 \text{ eV} \text{ and } \sum \frac{\theta_{ei}^2}{M_i} \lesssim 2 \times 10^{-8} \text{ GeV}^{-1}$$

Sterile Neutrinos, Seesaw and $0\nu\beta\beta$

- if the eV-steriles are from seesaw: individual cancellations in flavor symmetry models, e.g.:

$$U_{e2}^2 m_2 + U_{e4}^2 m_4 = 0$$

Barry, W.R., Zhang, JCAP 1201

- if seesaw scale is below 100 MeV: No double beta decay!

$$\sum_{i=1}^6 U_{ei}^2 m_i = 0 \text{ since } \mathcal{M} = \begin{pmatrix} 0 & m_D \\ m_D^T & M_R \end{pmatrix} = U \begin{pmatrix} m_\nu^{\text{diag}} & 0 \\ 0 & M_R^{\text{diag}} \end{pmatrix} U^T$$

de Gouvea, Jenkins, Vasudevan, PRD 75

keV steriles as Warm Dark Matter

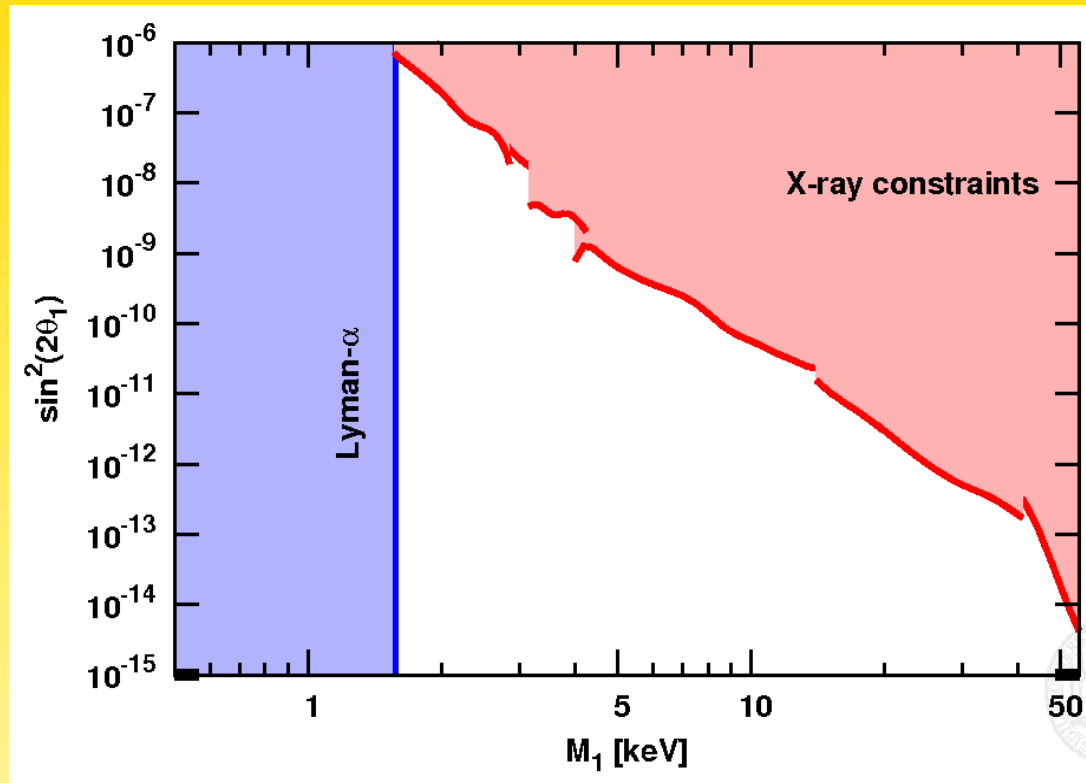
→ WDM has same large scale structure formation as CDM, but suppresses small scale formations

⇒ predicts less cuspy (=smoother) DM profiles, and less dwarf satellites

keV sterile is excellent candidate

parameters: mass M_1 and mixing θ

- X-ray searches $\Gamma \sim G_F^2 M_1^5 \theta^2$
- Ly- α : structure formation at low scales \sim Mpc
- Tremaine-Gunn
- $\tau \sim \tau_U$
- etc.



$m_\nu = \theta^2 M \Rightarrow$ one massless active neutrino! (unless strong cancellations)

talk by Viollier

TeV seesaw

naively, $m_\nu = m_D^2/M_R$ and mixing m_D/M_R

\Rightarrow TeV neutrinos have mixing of order 10^{-7}

But, matrices are involved...e.g. (Kersten, Smirnov)

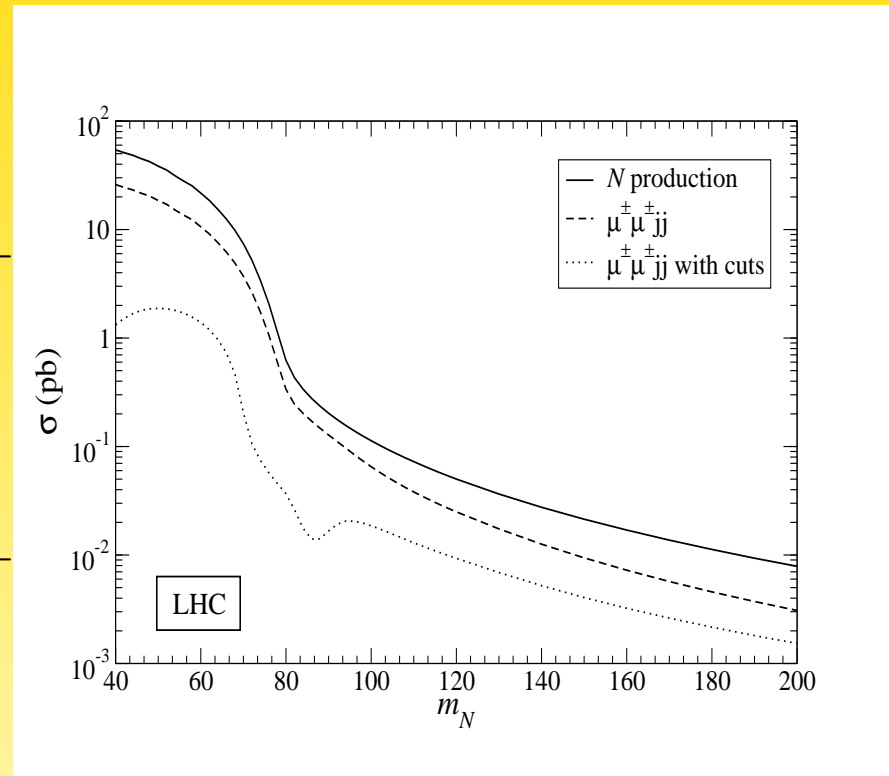
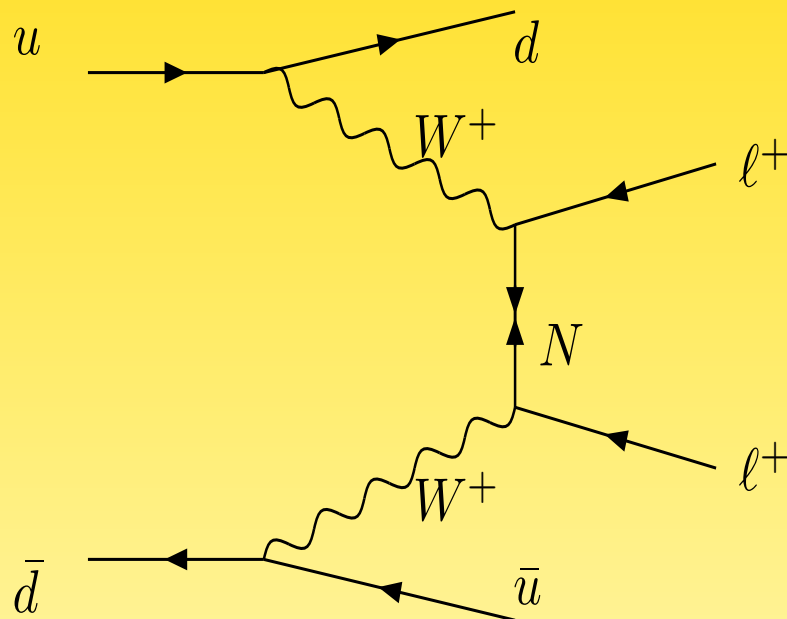
$$m_D = v \begin{pmatrix} h_1 & h_2 & h_3 \\ \omega h_1 & \omega h_2 & \omega h_3 \\ \omega^2 h_1 & \omega^2 h_2 & \omega^2 h_3 \end{pmatrix} = \mathcal{O}(v) \text{ and } M_R = M_0 \mathbb{1} = \mathcal{O}(\text{TeV})$$

gives $m_\nu = 0$, add (very) small corrections

first pointed out: Korner, Pilaftsis, Schilcher (1993)

works with $Y_\nu = \mathcal{O}(1)$, mixing $m_D/M_R = \mathcal{O}(0.1)$ and $M_0 \lesssim \text{TeV}$!

TeV seesaw

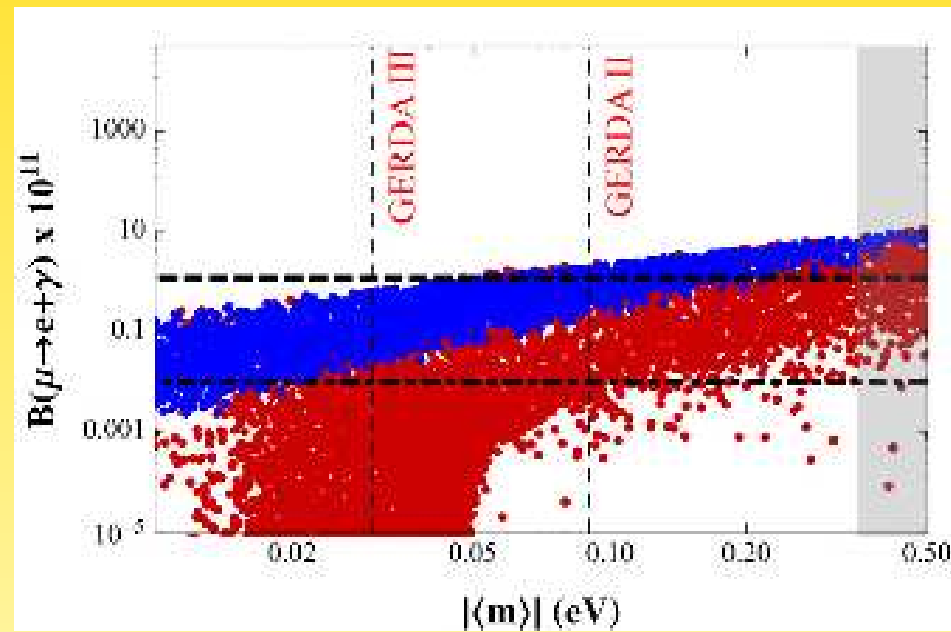


at most $M_i \lesssim 400$ GeV

Han, Zhang; del Aguila, Aguilar-Saavedra, Pittau

TeV scale seesaw with sizable mixing

can saturate LFV and LNV



Ibarra, Molinaro, Petcov

TeV scale seesaw with sizable mixing

$$m_D = m \begin{pmatrix} f\epsilon^2 & 0 & 0 \\ 0 & g\epsilon & 0 \\ 0 & 0 & 1 \end{pmatrix} \quad \text{and} \quad M_R^{-1} = M^{-1} \begin{pmatrix} a & b & k \\ b & c & d\epsilon \\ k & d\epsilon & e\epsilon^2 \end{pmatrix}$$

M/GeV	m/MeV	ϵ	a	k	b	c	d	e	f	g
5.00	0.935	0.02	1.00	1.35	0.90	1.4576	0.7942	0.2898	0.0948	0.485

gives successful m_ν and for double beta decay:

$$\frac{T_{1/2}(\text{light})}{T_{1/2}(\text{heavy})} \simeq 10^4$$

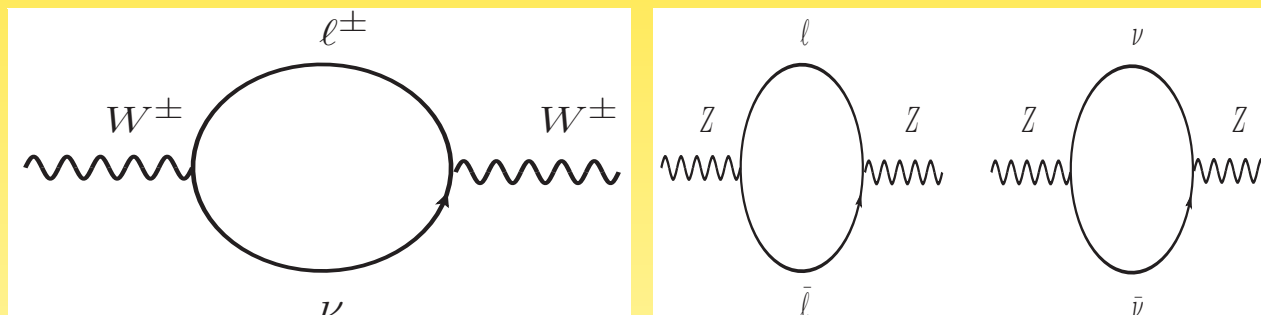
Mittra, Senjanovic, Vissani

New motivation for TeV neutrinos?

$$\Gamma_{\text{inv}} = \frac{1}{3} \Gamma_{\text{inv}}^{\text{SM}} \sum (1 - \epsilon_\alpha)^2$$

$$\sigma(\nu_\alpha q)_{\text{CC}} = \sigma(\nu_\alpha q)_{\text{CC}}^{\text{SM}} (1 - \epsilon_\alpha)$$

$$\sigma(\nu_\alpha q)_{\text{NC}} = \sigma(\nu_\alpha q)_{\text{NC}}^{\text{SM}} (1 - \epsilon_\alpha)^2$$



Fit to EWPO: TeV-scale neutrinos with $\epsilon \lesssim 10^{-3}$

Akhmedov, Kartavtsev, Michaels, Lindner, Smirnov, 1302.1872

Seesaw with not too diverse mass scales

if m_D/M_R is sizable, NLO corrections to seesaw become relevant:

$$\begin{aligned}\tilde{m}_\nu &= -m_D^T M_R^{-1} m_D + \frac{1}{2} m_D^T M_R^{-1} X M_R^{-1} m_D \\ \tilde{M}_R &= M_R + \frac{1}{2} X\end{aligned}$$

with $X = A + A^T$ where $A = m_D m_D^\dagger (M_R^*)^{-1}$

Grimus, Lavoura, JHEP 0011; Hettmansperger, Lindner, W.R., JHEP 1104

Examples:

- no correction to $U_{e3} = 0$ and $\theta_{23} = \pi/4$ for μ - τ symmetry
- no correction to $U_{\alpha i}$ if one light neutrino m_i massless
- relevant for inverse, linear, double seesaw

Phenomenology of heavy singlets

recall: for small quartic Higgs coupling $\lambda = m_h/(v\sqrt{2})$ is driven to negative values by top Yukawa:

$$\beta_\lambda \propto -24 \text{Tr} (Y_u^\dagger Y_u)^2 \Rightarrow m_h \geq f(\Lambda)$$

vacuum stability bound

currently unclear situation:

- could be $\lambda(M_{\text{Pl}}) = 0$
- vacuum could be stable
- vacuum could be unstable
- vacuum could be metastable

(Holthausen, Lim, Lindner; Bezrukov *et al.*; Strumia *et al.*; Masina)

strong dependence on top mass, threshold corrections, α_s

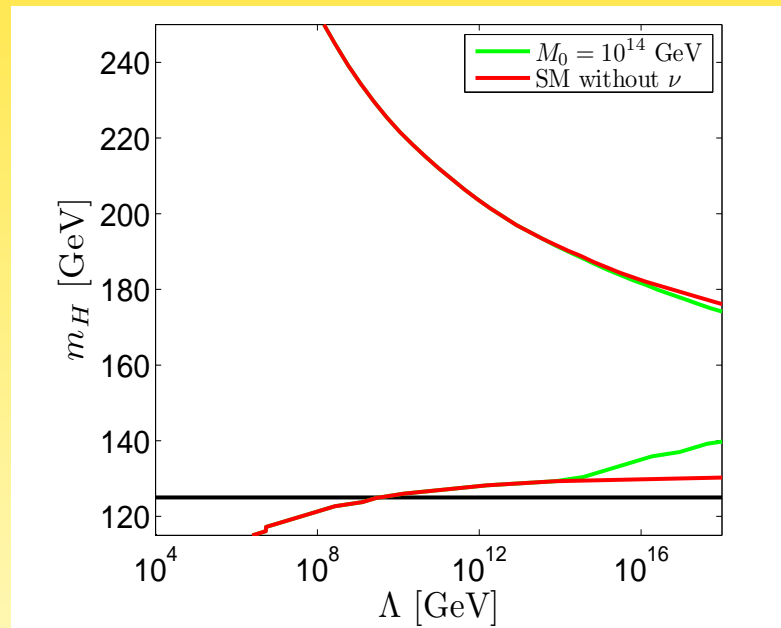
Phenomenology of heavy singlets

often overlooked: Dirac Yukawa $\bar{\nu}_L Y_\nu N_R$ contribution to λ :

$$\Delta\beta_\lambda = -8 \text{Tr} (Y_\nu^\dagger Y_\nu)^2$$

Casas *et al.*; Strumia *et al.*; W.R., Zhang

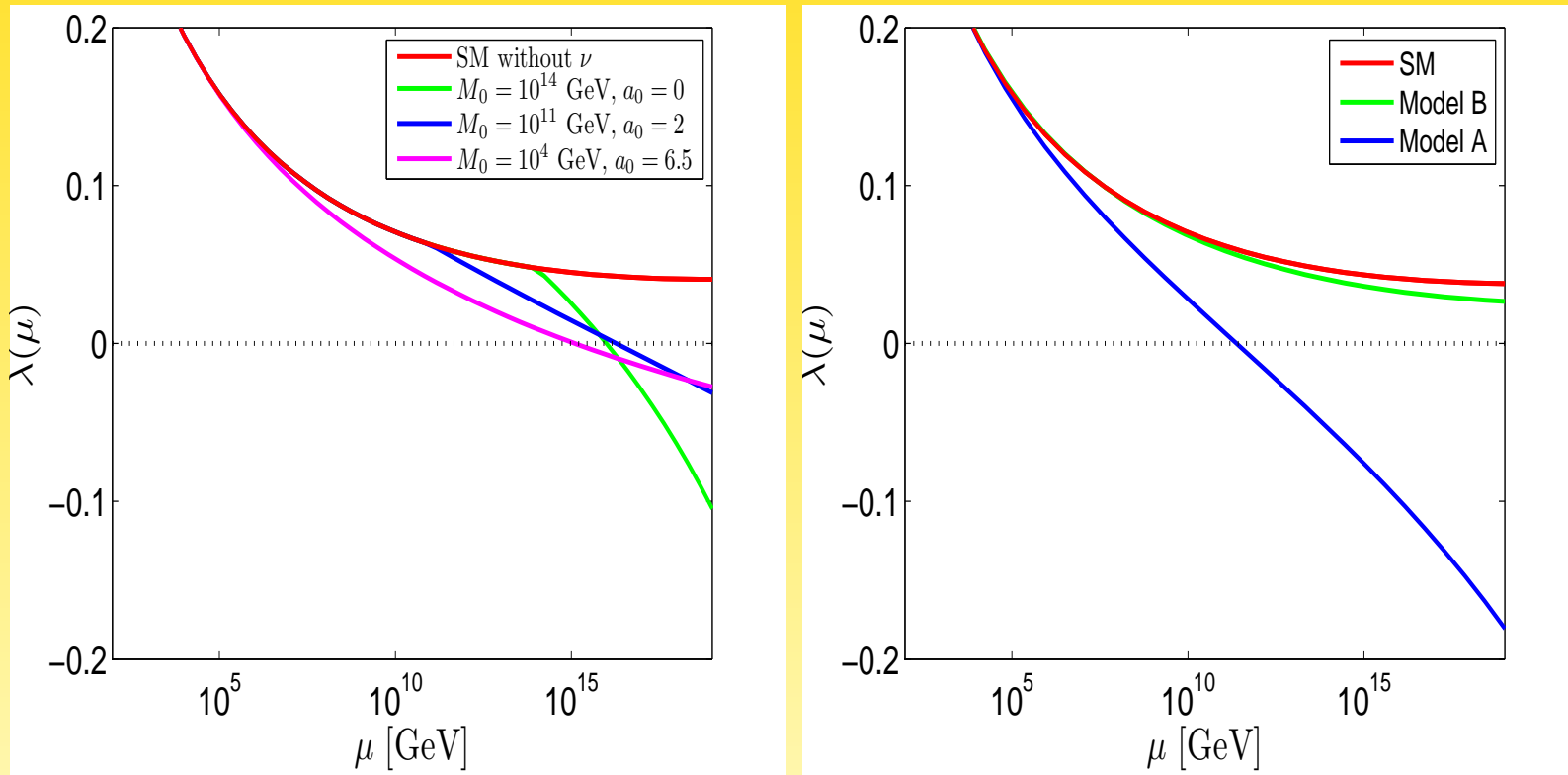
makes vacuum stability condition worse!



naively, if M_R goes down, Y_ν goes down and effect is negligible

Higgs physics and sterile neutrinos

if neutrinos are made accessible at colliders, Dirac Yukawa is large even for TeV neutrinos \Rightarrow influences vacuum stability bound



W.R., Zhang, JHEP 1206

$10^9 \dots 10^{15}$ GeV: The case of very heavy $M_R \dots$

- ... gives correct neutrino masses for $m_D \simeq v$
- ... gives successful thermal leptogenesis
- ... is a generic GUT prediction

this is the scale where one would expect M_R

$10^9 \dots 10^{15}$ GeV: The case of very heavy $M_R \dots$

... gives correct neutrino masses for $m_D \simeq v$

... gives successful thermal leptogenesis (lecture by Ibarra)

... is a generic GUT prediction

this is the scale where one would expect M_R

Recall: theorists also expected small neutrino mixing...

Predictions of $SO(10)$ theories

Model	Fit	M_3 [GeV]	M_2 [GeV]	M_2 [GeV]	χ^2
$10_H + \overline{126}_H$	NH	3.6×10^{12}	2.0×10^{11}	1.2×10^{11}	23.0
$10_H + \overline{126}_H + SS$	NH	1.1×10^{12}	5.7×10^{10}	1.5×10^{10}	3.29
$10_H + \overline{126}_H + 120_H$	NH	9.9×10^{14}	7.3×10^{13}	1.2×10^{13}	11.2
$10_H + \overline{126}_H + 120_H + SS$	NH	4.2×10^{13}	4.9×10^{11}	4.9×10^{11}	6.9×10^{-6}
$10_H + \overline{126}_H + 120_H$	IH	1.1×10^{13}	3.5×10^{12}	5.5×10^{11}	13.3
$10_H + \overline{126}_H + 120_H + SS$	IH	1.2×10^{13}	3.1×10^{11}	2.0×10^{03}	0.6

Fit to $SO(10)$ models including θ_{13} , Higgs, seesaw RG, etc.

Dueck, W.R., 1306.4468

Phenomenology of (high scale) Leptogenesis

little

(would expect leptonic CP violation and neutrinoless double beta decay)

But note:

- bread and butter leptogenesis requires $M_1 \gtrsim 10^9$ GeV
- *resonant* leptogenesis works even at weak scale
- *flavor oscillation* of sterile neutrinos with mass around few GeV

3 well motivated scales

there are three well-motivated mass values of M_R :

- eV
- keV
- $\gtrsim 10^9$ GeV

what if all three are there?

N_1	N_2	N_3	BAU	eV-anomalies	DM
eV	GUT	GUT	✓	✓	—
eV	keV	GUT	—	✓	✓
keV	GUT or GeV	GUT or GeV	✓	—	✓

(last row is called ν MSM, [Shaposhnikov *et al.*](#))

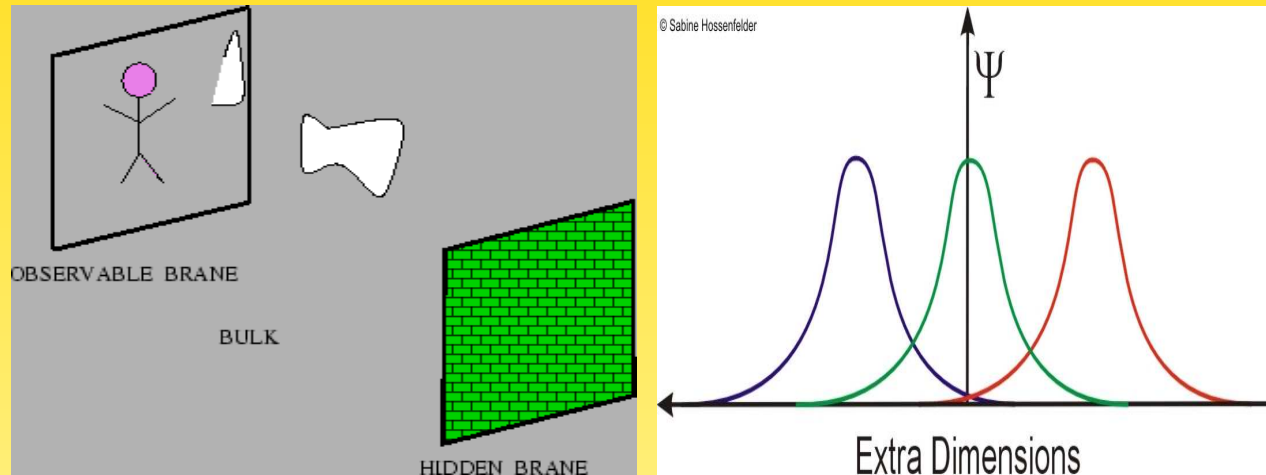
Models for light sterile neutrinos

how to bring one (or all) of the singlet neutrinos down to (k)eV ?

- extra dimensions (Kusenko, Takahashi, Yanagida)
- zero mass plus corrections (Mohapatra; Shaposhnikov; Lindner, Merle, Niro; Araki, Li)
- Froggatt-Nielsen (Merle, Niro; Barry, W.R., Zhang)

Light sterile neutrinos from extra dimensions

localize one heavy neutrino N_1 on distant brane, separated from the SM brane, where we live



small wave function overlap between this field and the other ones

$$M_s \propto e^{-2ml}, \quad m_D \propto e^{-ml} \Rightarrow m_D^2/M_R = \text{const}$$

(m mass of 5D spinor, l size of ED)

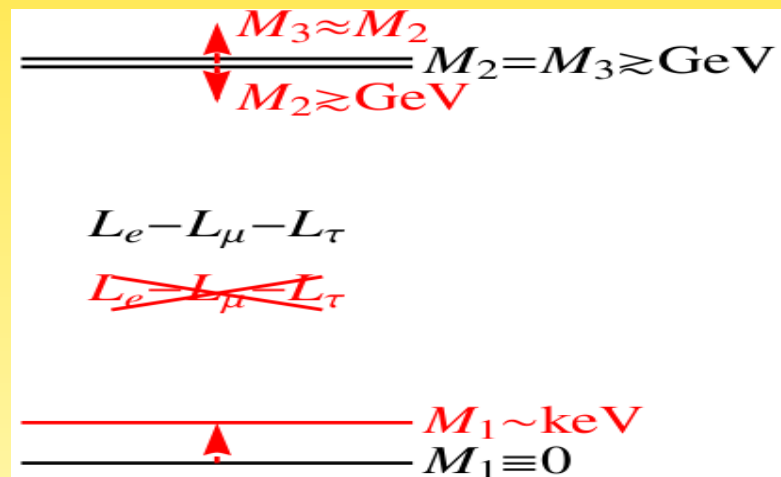
“Split seesaw”

Kusenko, Takahashi, Yanagida

Light sterile neutrinos from slightly broken flavor symmetry

introduce flavor symmetry leading to one massless neutrino, e.g.

$$M_R^{L_e - L_\mu - L_\tau} = \begin{pmatrix} 0 & a & b \\ \cdot & 0 & 0 \\ \cdot & \cdot & 0 \end{pmatrix} \Rightarrow M_1 = 0, \quad M_{2,3} = \pm \sqrt{a^2 + b^2}$$



small breaking to lift M_1

Mohapatra; Shaposhnikov; Lindner, Merle, Niro; Araki, Li

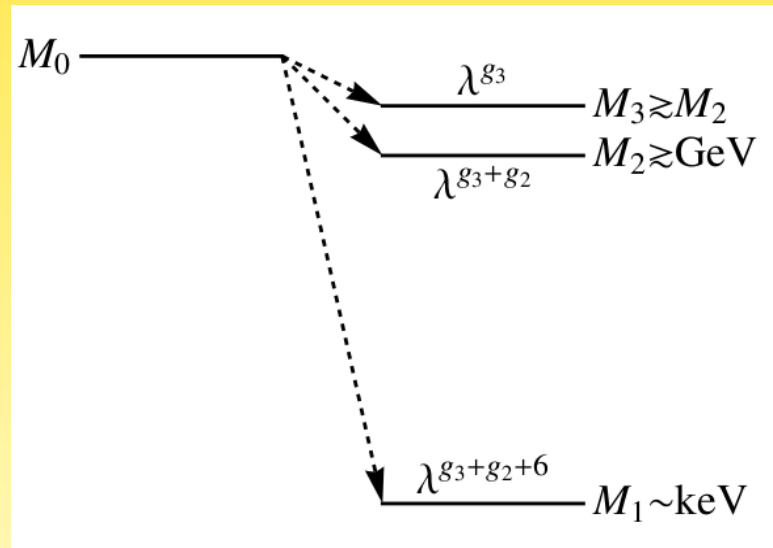
Light sterile neutrinos from Froggatt-Nielsen

introduce new $U(1)$ and field Θ with charge -1

N_R has charge m and ν_L has charge n :

$$m_D \bar{\nu}_L N_R \left(\frac{\Theta}{\Lambda} \right)^{n+m} + M_R \bar{N}_R^c N_R \left(\frac{\Theta}{\Lambda} \right)^{2m}, \quad \frac{\Theta}{\Lambda} \simeq \lambda$$

\Rightarrow FN charge of N_R drops out in m_D^2/M_R



Merle, Niro; Barry, W.R., Zhang

Flavor Symmetries

add ν_s to bread and butter A_4 model and use FN to control mass:

	l	e^c	μ^c	τ^c	ν^c	$h_{u,d}$	ν_s
A_4	3	1	$1''$	$1'$	3	1	1
Z_3	ω	ω^2	ω^2	ω^2	ω^2	1	1
$U(1)$	0	4	2	0	0	0	6 (8)

active neutrino terms of order $llhh(\xi, \varphi')/\Lambda^2$

active-sterile terms of order $l\xi\varphi'h\nu_s\lambda^6/\Lambda^2$

sterile-sterile terms of order $\varphi^2\nu_s\nu_s\lambda^{12}/\Lambda$

generate tri-bimaximal mixing and mixing of order 0.1 with eV-steriles
(or 10^{-4} with keV)

Barry, W.R., Zhang, JHEP 1107

Flavor Symmetries

$$M_\nu^{4 \times 4} = \begin{pmatrix} a + \frac{2d}{3} & -\frac{d}{3} & -\frac{d}{3} & e \\ \cdot & \frac{2d}{3} & a - \frac{d}{3} & e \\ \cdot & \cdot & \frac{2d}{3} & e \\ \cdot & \cdot & \cdot & m_s \end{pmatrix} \quad \text{with} \quad \begin{array}{ll} a, d \simeq 10^{-2} \text{ eV} \\ e/m_s \simeq 0.1 & (10^{-4}) \\ m_s \simeq \text{eV} & (\text{keV}) \end{array}$$

diagonalized by

$$U \simeq \begin{pmatrix} \frac{2}{\sqrt{6}} & \frac{1}{\sqrt{3}} & 0 & 0 \\ -\frac{1}{\sqrt{6}} & \frac{1}{\sqrt{3}} & -\frac{1}{\sqrt{2}} & 0 \\ -\frac{1}{\sqrt{6}} & \frac{1}{\sqrt{3}} & \frac{1}{\sqrt{2}} & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix} + \begin{pmatrix} 0 & 0 & 0 & \frac{e}{m_s} \\ 0 & 0 & 0 & \frac{e}{m_s} \\ 0 & 0 & 0 & \frac{e}{m_s} \\ 0 & -\frac{\sqrt{3}e}{m_s} & 0 & 0 \end{pmatrix} + \begin{pmatrix} 0 & -\frac{\sqrt{3}e^2}{2m_s^2} & 0 & 0 \\ 0 & -\frac{\sqrt{3}e^2}{2m_s^2} & 0 & 0 \\ 0 & -\frac{\sqrt{3}e^2}{2m_s^2} & 0 & 0 \\ 0 & 0 & 0 & -\frac{3e^2}{2m_s^2} \end{pmatrix}$$

A₄ Seesaw Model with light steriles (Barry, W.R., Zhang, JCAP 1201)

Field	L	e^c	μ^c	τ^c	$h_{u,d}$	φ	φ'	φ''	ξ	ξ'	ξ''	Θ	ν_1^c	ν_2^c	ν_3^c
$SU(2)_L$	2	1	1	1	2	1	1	1	1	1	1	1	1	1	1
A_4	$\underline{3}$	$\underline{1}$	$\underline{1}''$	$\underline{1}'$	$\underline{1}$	$\underline{3}$	$\underline{3}$	$\underline{3}$	$\underline{1}$	$\underline{1}'$	$\underline{1}$	$\underline{1}$	$\underline{1}$	$\underline{1}'$	$\underline{1}$
Z_3	ω	ω^2	ω^2	ω^2	1	1	ω	ω^2	ω^2	ω	1	1	ω^2	ω	1
$U(1)$	-	3	1	0	-	-	-	-	-	-	-	-1	F_1	F_2	F_3

various possibilities for the FN-charges:

	F_1, F_2, F_3	Mass spectrum	$ U_{\alpha 4} $	$ U_{\alpha 5} $	m_{ee}		Phenomenology
					NO	IO	
I	9, 10, 10	$M_{2,3} = \mathcal{O}(\text{eV})$	$\mathcal{O}(0.1)$	$\mathcal{O}(0.1)$	0	0	3 + 2 mixing
IIA	9, 10, 0	$M_2 = \mathcal{O}(\text{eV})$ $M_3 = \mathcal{O}(10^{11} \text{ GeV})$	$\mathcal{O}(0.1)$	$\mathcal{O}(10^{-11})$	0	$\frac{2\sqrt{\Delta m_A^2}}{3}$	3 + 1 mixing
IIB	9, 0, 10	$M_2 = \mathcal{O}(10^{11} \text{ GeV})$ $M_3 = \mathcal{O}(\text{eV})$	$\mathcal{O}(10^{-11})$	$\mathcal{O}(0.1)$	$\frac{\sqrt{\Delta m_\odot^2}}{3}$	$\frac{\sqrt{\Delta m_A^2}}{3}$	
III	9, 5, 5	$M_{2,3} = \mathcal{O}(10 \text{ GeV})$	$\mathcal{O}(10^{-6})$	$\mathcal{O}(10^{-6})$	$\frac{\sqrt{\Delta m_\odot^2}}{3}$	$\sqrt{\Delta m_A^2}$	Leptogenesis

Final Remarks

Steriles have a number of consequences:

- oscillations
- astrophysics
- cosmology
- beta decays, neutrinoless double beta decay
- Higgs physics
- Lepton flavor violation
- ...

would be extraordinary discovery!

Summary

- Are there sterile neutrinos?
-
-
-

Summary

- Are there sterile neutrinos? Maybe!
-
-
-

Summary

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- if there are steriles, are they light?
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-

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Summary

- Are there sterile neutrinos? Maybe!
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- experimental input necessary
-

Summary

- Are there sterile neutrinos? Maybe!
- if there are steriles, are they light? Maybe!
- experimental input necessary
- if (light) steriles necessary, we know what to do

EXTRA SLIDES FROM HERE ON

Predictions of $SO(10)$ theories

Yukawa structure of $SO(10)$ models depends on Higgs representations

$$10_H (\leftrightarrow H), \overline{126}_H (\leftrightarrow F), 120_H (\leftrightarrow G)$$

Gives relation for mass matrices:

$$m_{\text{up}} \propto r(H + sF + it_u G)$$

$$m_{\text{down}} \propto H + F + iG$$

$$m_D \propto r(H - 3sF + it_D G)$$

$$m_\ell \propto H - 3F + it_\ell G$$

$$M_R \propto r_R^{-1} F$$

Numerical fit including RG, Higgs, θ_{13}

Dueck, W.R., 1306.4468

Froggatt-Nielsen mechanism

effective theory

introduce new scalar field θ with charge -1 under new $U(1)$; acquires VEV $\langle\theta\rangle$

L_e and Φ have charge 0, e_R has charge 4, thus the term

$$\overline{L}_e \Phi e_R \frac{\theta^4}{\Lambda^4} \rightarrow \overline{L}_e \Phi e_R \frac{\langle\theta\rangle^4}{\Lambda^4}$$

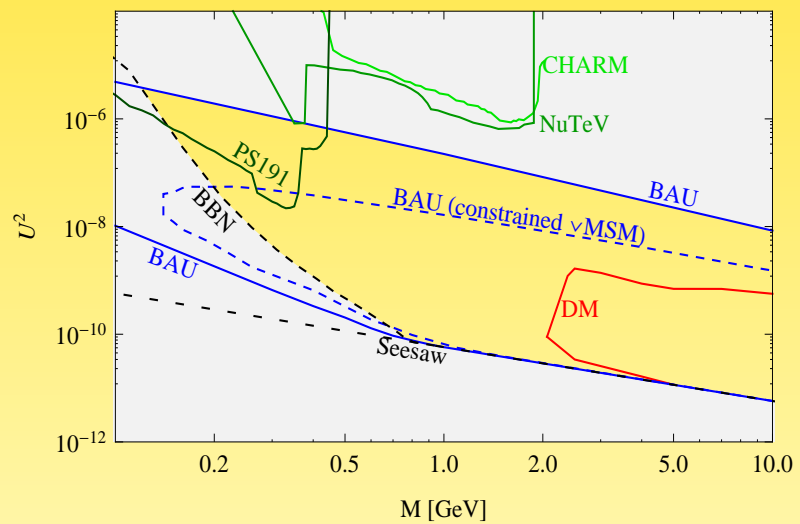
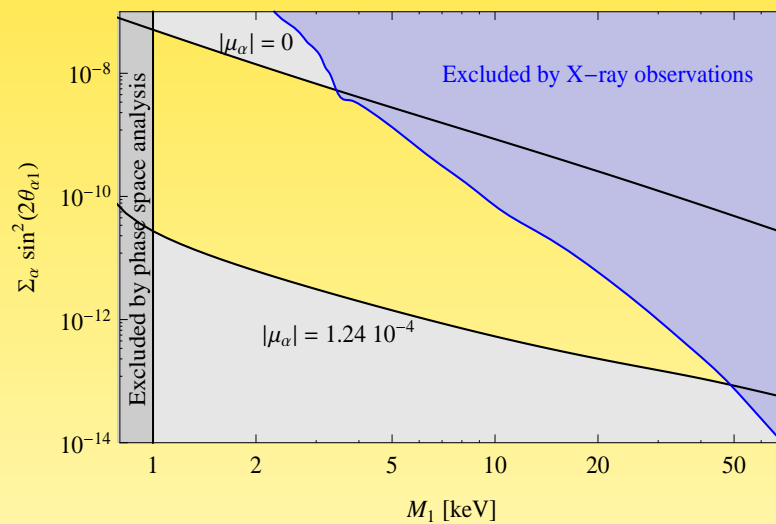
is allowed

tau mass can go as $\overline{L}_\tau \Phi \tau_R$

With $\langle\theta\rangle/\Lambda \simeq \lambda$: $m_e \simeq \lambda^4 m_\tau$

ν MSM

- no new scale beyond ν and Planck scale
- no new particles except 3 right-handed neutrinos
 - one is keV and is Warm Dark Matter
 - two are few GeV, almost degenerate, and do leptogenesis via oscillations



Shaposhnikov *et al.*; Shaposhnikov *et al.*; Shaposhnikov *et al.*; Shaposhnikov *et al.*; Shaposhnikov *et al.*; Shaposhnikov *et al.*,...

ν MSM

- $N_{2,3}$ produced thermally at $T \gtrsim T_{\text{EW}}$
- oscillate and generate lepton asymmetry
- $\mu \simeq 10^{-10}$ at $T = T_{\text{EW}}$
- $N_{2,3}$ freeze out, decay at $T \lesssim \text{GeV}$ and generate lepton asymmetry $\mu \simeq 10^{-7}$ at $T \simeq 100 \text{ MeV}$
- resonant WDM production at $T \simeq 100 \text{ MeV}$

Higgs physics and sterile neutrinos (W.R., Zhang)

$$m_\nu = v^2 Y_\nu^T M_R^{-1} Y_\nu \quad \text{with} \quad Y_\nu = \frac{1}{v} \sqrt{M_R^{\text{diag}}} R \sqrt{m_\nu^{\text{diag}}} U^\dagger$$

useful parametrization:

$$R = O e^{iA} \quad \text{with} \quad A = \begin{pmatrix} 0 & a & b \\ -a & 0 & c \\ -b & -c & 0 \end{pmatrix}$$

degenerate heavy and light neutrinos:

$$\text{tr} (Y_\nu^\dagger Y_\nu) \simeq \frac{M_0 m_0}{v^2} (1 + 2 \cosh r) \quad \text{with} \quad r = 2\sqrt{a^2 + b^2 + c^2}$$

for instance, $M_0 = 1 \text{ TeV}$, $m_0 = 0.1 \text{ eV}$, $r = 25$ gives $\text{tr} (Y_\nu^\dagger Y_\nu) = \mathcal{O}(0.1)$

(compare to naive estimate $Y_\nu \simeq m_0 M_0 / v^2 \sim 10^{-11}$)

Seesaw parameters and sterile neutrinos: eV scale



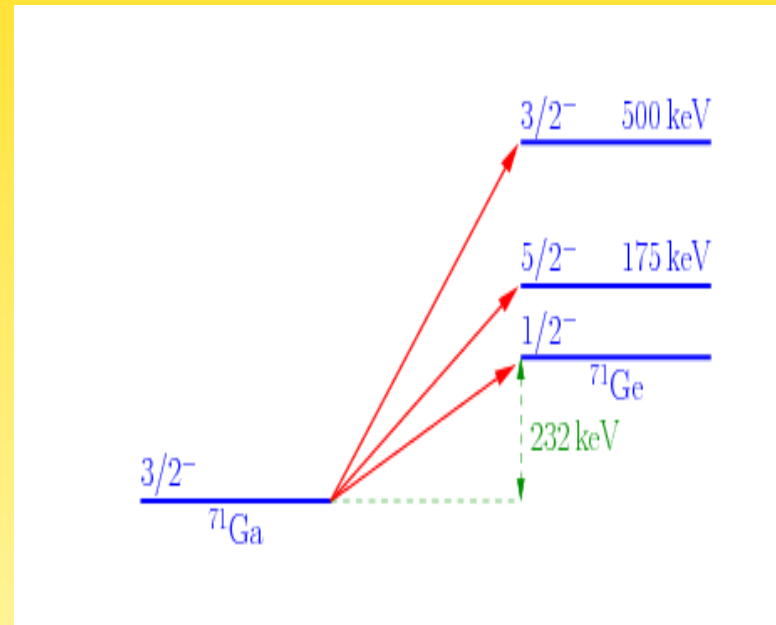
- 3+2 scenario: m_ν is 5×5 matrix, with a total of 5 masses, 9 mixing angles, 6 Dirac and 4 Majorana phases, 24 parameters
- seesaw with 2 singlet neutrinos has 11 parameters

But: no problem, seesaw fits work as well

Donini *et al.*; Blennow, Fernandez-Martinez; Fan, Langacker

Motivation for Sterile Neutrinos: Gallium Anomaly

- overestimate of detection process $\sigma(\nu_e + {}^{71}\text{Ga} \rightarrow e^- + {}^{71}\text{Ge})$?



- small contributions of excited states confirmed by ${}^{71}\text{Ga}({}^3\text{He}, t){}^{71}\text{Ge}$ measurements

Motivation for Sterile Neutrinos: Reactor Anomaly

- 200 MeV energy per fission, 6 neutrinos generated in β -decay chain
 $\Rightarrow 2 \times 10^{20} \nu/s$ per GW thermal power
- U and Pu chains have $\mathcal{O}(10^2)$ nuclei, with $\mathcal{O}(10)$ branches each
- high energy part (shortest lifetime, i.e. least known) most important
- \Leftrightarrow measurement of e^- spectrum at ILL
- sophisticated translation into $\bar{\nu}_e$ spectra, taking into account
 - new neutron lifetime ($\sigma_{\text{fission}} \propto 1/\tau_n$)
 - corrections to Fermi theory
 - * nuclear charge distribution (\leftrightarrow QED corrections)
 - * weak magnetism (\leftrightarrow magn. moment and axial current interference)
 - * off-equilibrium effects (\leftrightarrow evolution of reactor)
 - * radiative corrections
 - * more branches

$$S_\beta(Z, A, E_e) = \underbrace{K}_{\text{Norm.}} \times \underbrace{\mathcal{F}(Z, A, E_e)}_{\text{Fermi function}} \times \underbrace{p_e E_e (E_e - E_0)^2}_{\text{Phase space}} \times \underbrace{\left(1 + \delta(Z, A, E_e)\right)}_{\text{Correction}}$$

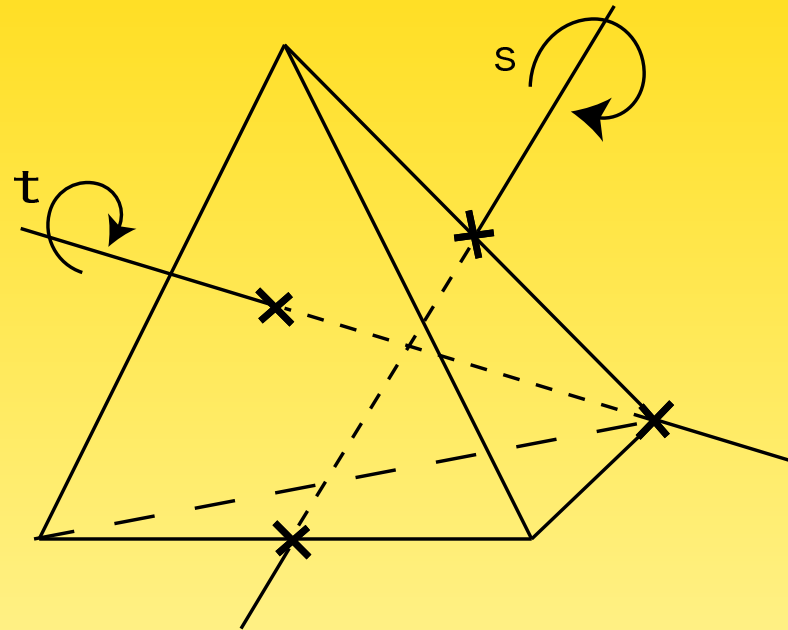
Origin of m_ν

$\mathcal{L}_M = \frac{1}{2} \overline{\nu}_L m_\nu \nu_L^c$ or $\mathcal{L}_D = \overline{\nu}_L m_\nu \nu_R$ are necessarily BSM

Ansatz	content	\mathcal{L}	m_ν	scale
“SM” (Dirac mass)	singlet	$y \overline{L} H N_R$	yv	$y = \mathcal{O}(10^{-12})$
“effective” (dim 5 operator)	new scale + LNF	$\frac{1}{\Lambda} \overline{L} H H^T L^c$	$\frac{v^2}{\Lambda}$	$\Lambda = \left(\frac{0.1 \text{ eV}}{m_\nu} \right) 10^{14} \text{ GeV}$
“direct” (Type II See-Saw)	Higgs triplet + LNV	$y \overline{L} \Delta L^c + \mu H H \Delta$	yv_T	$\Lambda = \frac{1}{y\mu} M_\Delta^2$
“indirect 1” (Type I see-saw)	Singlet + LNV	$y \overline{L} H N_R + \overline{N}_R^c M_R N_R$	$\frac{(yv)^2}{M_R}$	$\Lambda = \frac{1}{y} M_R$
“indirect 2” (Type III see-saw)	Fermion triplet + LNV	$y \overline{L} \Sigma H + \text{Tr} \overline{\Sigma} M_\Sigma \Sigma$	$\frac{(yv)^2}{M_\Sigma}$	$\Lambda = \frac{1}{y} M_\Sigma$

focus here on type I see-saw mechanism

How to generate lepton mixing: Flavor Symmetries...

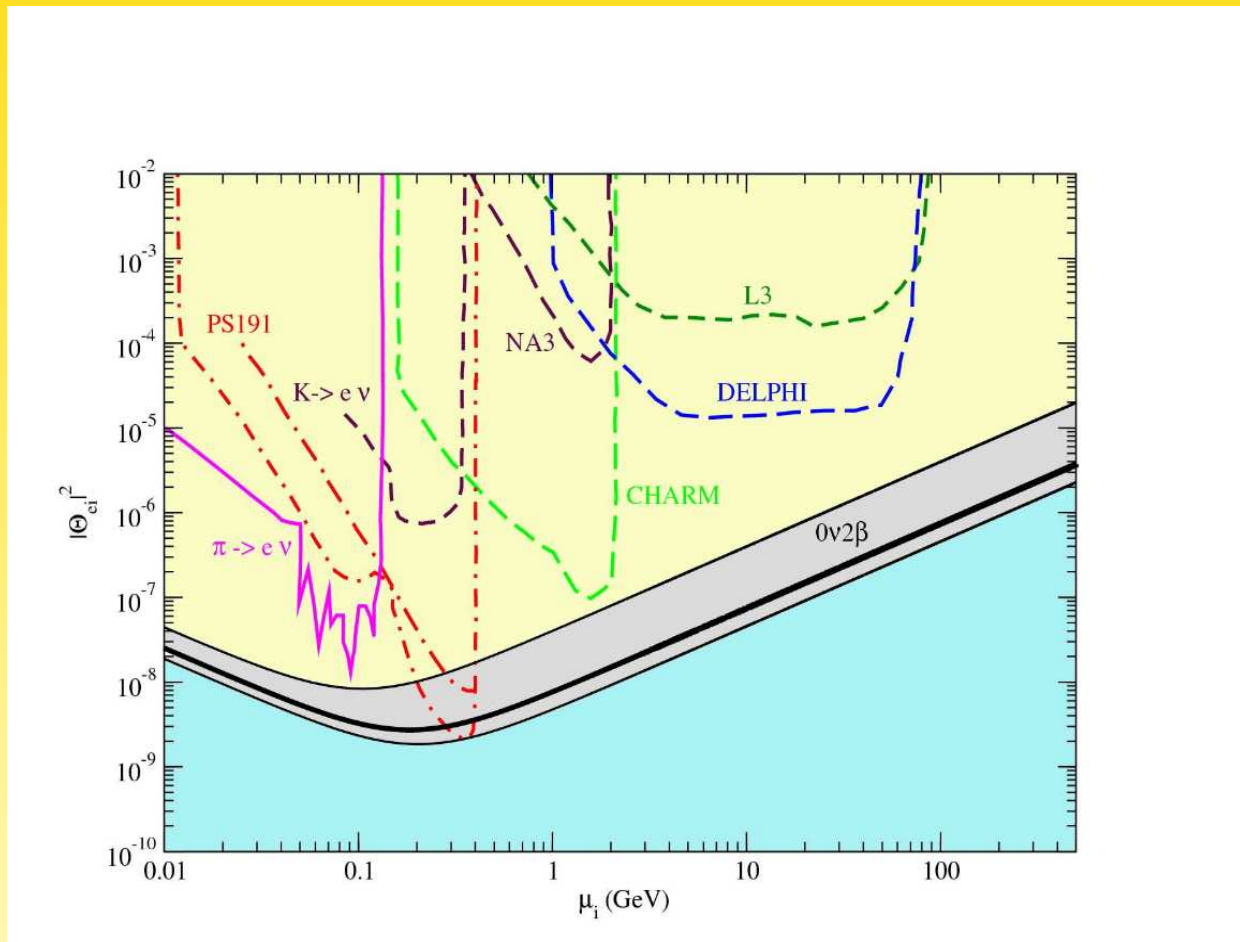


A_4 smallest group with irreducible $3 \leftrightarrow 3$ generations

$$3 \times 3 = 1 + 1' + 1'' + 3 + 3$$

$$1 \times 1 = 1, 1' \times 1'' = 1, 1'' \times 1' = 1, 1' \times 1' = 1'', 1'' \times 1'' = 1', 3 \times 1 = 3, \dots$$

Heavy neutrinos



Mitra, Senjanovic, Vissani