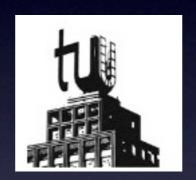
Flavor Symmetries: Finding tests & alternatives

Heinrich Päs



Erice School on Nuclear Physics, 2013

- The Higgs as a harbinger of S3 flavor symmetry
- Novel signatures of the Higgs sector from S3 flavor symmetry
 G. Bhattacharyya, P. Leser, H.Päs, PRD 83 (2011) and PRD 86 (2012) 036009
- Knotted strings & leptonic flavor structure
 T.W. Kephart, P. Leser, H. Päs, Mod. Phys. Lett. A 27 (2012) 1250224

Puzzling Flavor structures

Fact:

- Large/Maximal lepton vs. small quark mixing
- Mild lepton vs. strong quark hierarchies

Discrete Flavor symmetry?

S₃, A₄, S₄, D₄, Q₄, D₅, D₆, Q₆, D₇,...

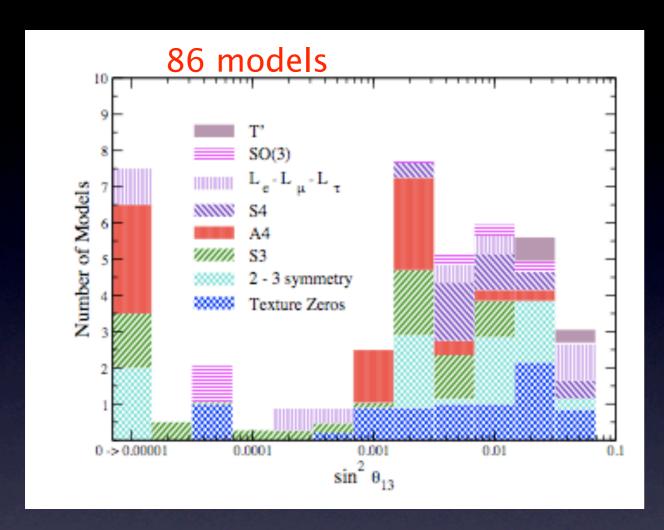
[e.g. Ma, Altarelli, Feruglio, King, Ross, Varzielas,...]

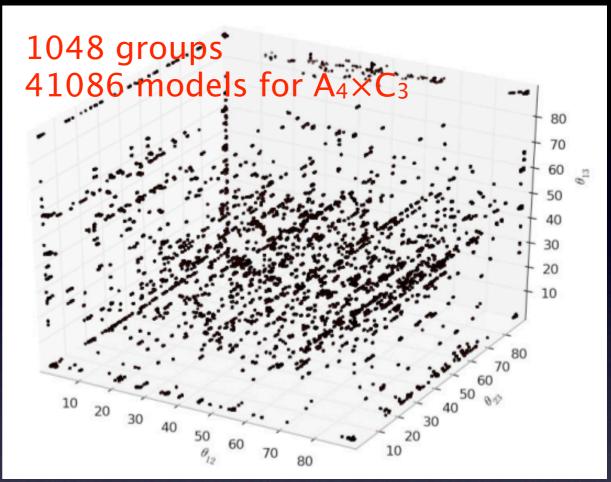
Anarchy?

Masses and Mixings random numbers?

[Hall, Murayama, Weiner, Haber, de Gouvea, '99, '00, '03]

A landscape of Flavor symmetry

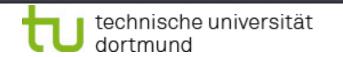




[Albright, Chen, Rodejohann; '06,'08]

[Parattu, Wingerter, SUSY'10, FLASY'12]

- Huge variety of models
- Predictions spanning a large part of the parameter space
- Search for new tests of Flavor symmetry
- Search for alternatives of Flavor symmetry



Probing flavor symmetry models

A typical flavor model:

- Choose a symmetry group
- Assign matter to irreducible representations
- Write down Lagrangian allowed by symmetry
- Find minima of Higgs potential

If Higgses responsible for flavor structure also break electroweak symmetry:

Maximal v mixing can translate into Higgs couplings

→extraordinary Higgs phenomenology!

A prototypical flavor model based on S₃:

[Chen, Frigerio, Ma, '04]

Symmetry group of the permutation of 3 objects. (equivalent to symmetry group of **equilateral triangle**)

More attractive again for sizable θ_{13} !

- Contains 6 **elements**: (123), (312), (231), (132), (321), (213)
- 3 irreducible representations: 1, 1', 2
- Basic multiplication rules: $1' \times 1' = 1$ and $2 \times 2 = 1 + 1' + 2$
- Assign matter fields to irreps as follows:

$$(L_1, L_2) \propto \mathbf{2}$$
 $L_3, l_3^c, l_1^c \propto \mathbf{1}$ $l_2^c \propto \mathbf{1}'$ $(Q_1, Q_2) \propto \mathbf{2}$ $Q_3, u_3^c, u_1^c, d_3^c, d_1^c \propto \mathbf{1}$ $u_2^c, d_2^c \propto \mathbf{1}'$ $(\phi_1, \phi_2) \propto \mathbf{2}$ $\phi_3 \propto \mathbf{1}$

- the same Higgses breaking EWSB also break Flavor!
- 3 Higgs SU(2) doublets necessary
- Vaccum alignment v₁=v₂=v for maximal atmospheric v mixing (extremum
- Large Flavor violating terms cancel between up and down-type quarks
- Neutrino masses generated by additional Higgs SU(2) triplet
- Large Flavor violation translates as mismatch between charged leptons and neutrinos directly into PMNS matrix

$$\mathcal{M}_{\ell} = \begin{pmatrix} f_4 v_3 & f_5 v_3 & 0 \\ 0 & f_1 v & -f_2 v \\ 0 & f_1 v & f_2 v \end{pmatrix}$$

→Such models exhibit an extraordinary Higgs phenomenology!

S3 invariant potential:

- Correct W and Z masses
- Maximal atmospheric mixing:
- Minimize scalar potential
- Diagonalization of mass matrix

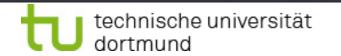
Realistic models

Consider a 125 GeV SM-like Higgs Include the complete set of scalars and pseudoscalars

[Bhattacharyya, Leser, Päs, '12]

3 CP even, 2 CP odd and 2 charged scalars

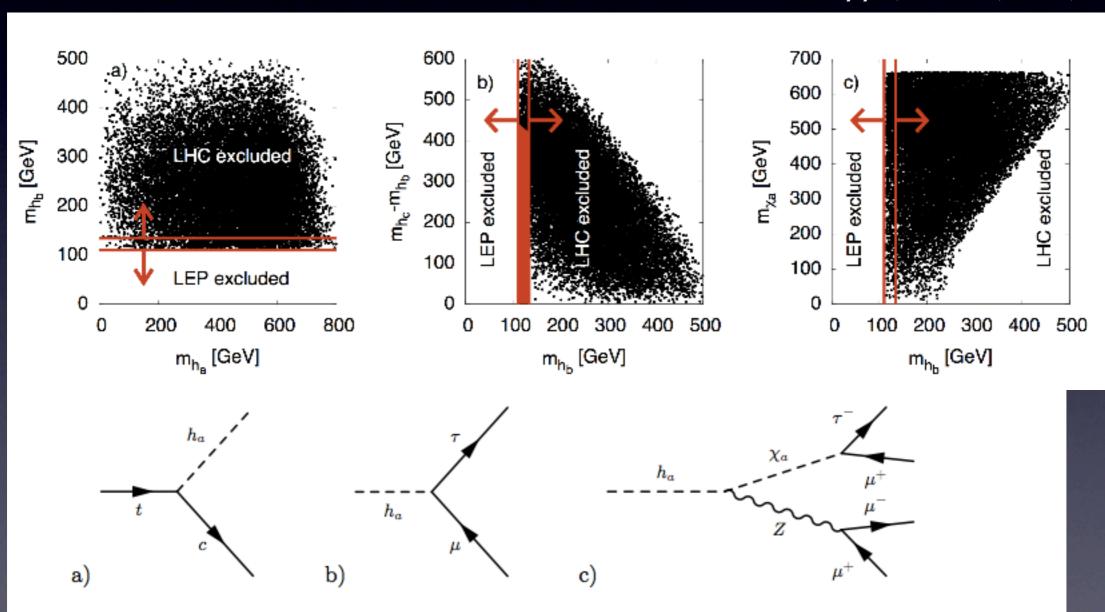
- h_{b,c} have SM-like couplings except for decay into h_a
- ha and Xa have no WW or ZZ interactions
- h_a /X_a have only flavor off-diagonal Yukawa couplings with 3rd generation
- ha /Xa can be hidden from standard searches and thus can be very light
- All other scalar/pseudoscalars can have masses above 550 GeV



LHC signatures

Full scalar and pseudoscalar spectrum and couplings

[Bhattacharyya, Leser, Päs, '12]

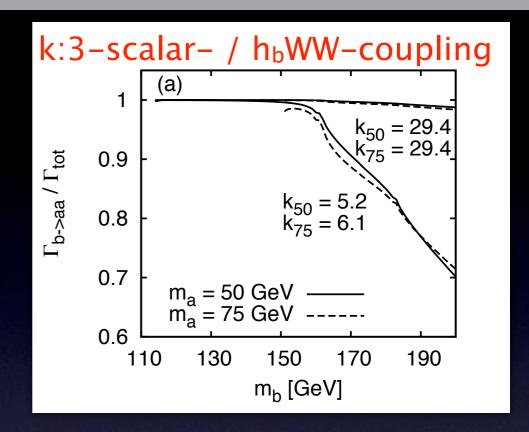


Feynman graphs for dominant sources of h_a production and decays which might be relevant at the LHC.

Phenomenology of CP-even scalars

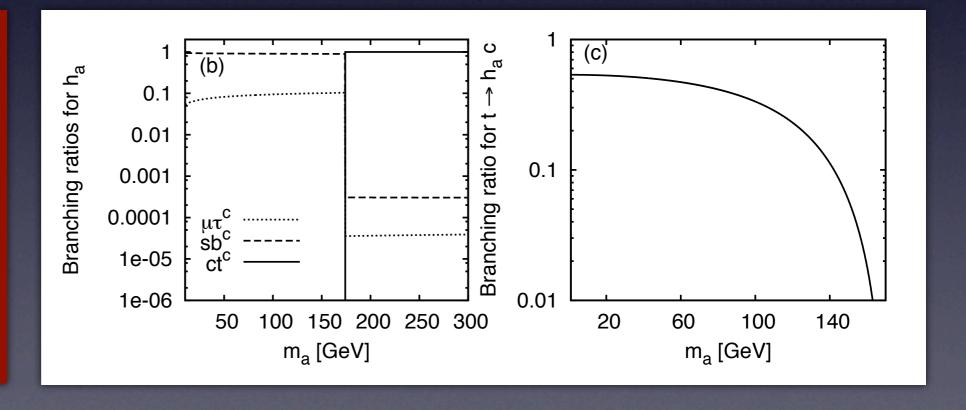
- Dominant decay for a light $h_{a:}$ $h_{b/c} \rightarrow h_a h_a$
- Production of h_a possible through $t \rightarrow h_a$ c with subsequent decay $h_{a->}$ $\mu \tau$
- h_a decays dominantly off-diagonally into jets (sb^c, $m_a < m_t$) or ct^c ($m_a > m_t$)

[Bhattacharyya, Leser, Päs, '10]



Interesting signals at the LHC!

ha, hb might already be buried in existing LEP or Tevatron data!



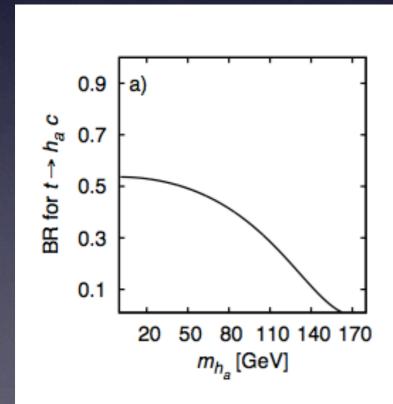
Exploiting the full scalar/pseudoscalar sector

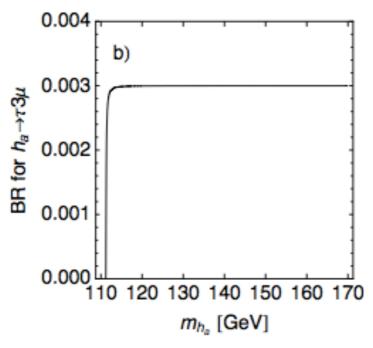
Signatures of the pseudoscalar χ_a

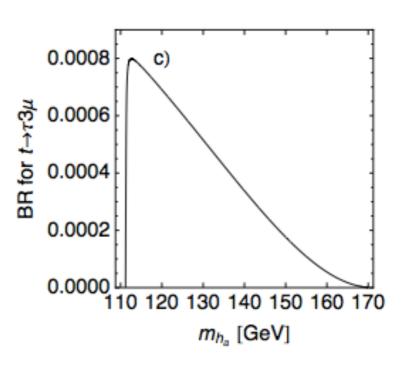
 $h_a \, o \, \chi_a Z$ with BR~100 % followed by

 $Z
ightarrow \mu \mu ~{
m BR} ~{
m of} \sim 3\%$ and $\chi_a
ightarrow au \mu ~{
m with} ~{
m a} ~{
m BR} ~{
m of} \sim 10\%$

 \Rightarrow $h_a o \chi_a Z o au \mu \mu \mu$ signature







"The Higgs as a harbinger of flavor symmetry"

Discrete symmetries employed to explain flavor mixing and mass hierarchies can be associated with an enlarged scalar sector which might lead to exotic Higgs decay modes. In this paper, we explore such a possibility in a scenario

[Bhattacharyya, Leser, Päs, '10]

If neutrino tribimaximal mixing is explained by a non-Abelian discrete symmetry such as A_4 , T_7 , $\Delta(27)$, etc., the charged-lepton Higgs sector has a Z_3 residual symmetry (lepton flavor triality), which may be observed directly in the decay chain $H^0 \to \psi_2^0 \bar{\psi}_2^0$, then $\psi_2^0(\bar{\psi}_2^0) \to l_i^+ l_j^-$ ($i \neq j$), where H^0 is a standard-model-like Higgs boson and ψ_2^0 is a scalar particle needed for realizing the original discrete symmetry. If kinematically allowed, this unusual and easily detectable decay is observable at the LHC with 1 fb⁻¹ for $E_{\rm cm} = 7$ TeV.

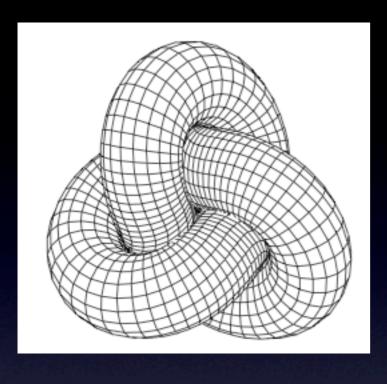
[Cao, Damanik, Ma, Wegman, '11]

Major achievement of Flavor models: motivate degenerate mass matrix entries to fit TBM:

$$m_
u = egin{pmatrix} x & y & y \ y & x+v & y-v \ y & y-v & x+v \end{pmatrix}$$

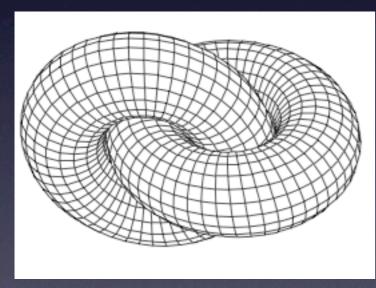
[e.g. Altarelli, Feruglio]

- Alternative: Anarchy....
- Anything else?
- Other phenomena in Nature with close numbers?

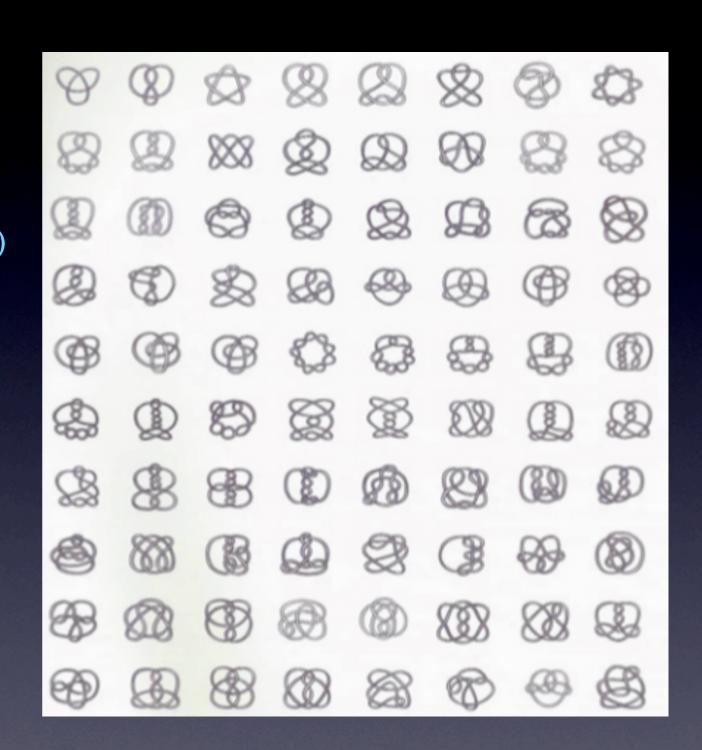


3₁ knot

(3 crossings, 1 component)



3²_I link (3 crossings, 2 components)
[Buniy, Kephart '03]



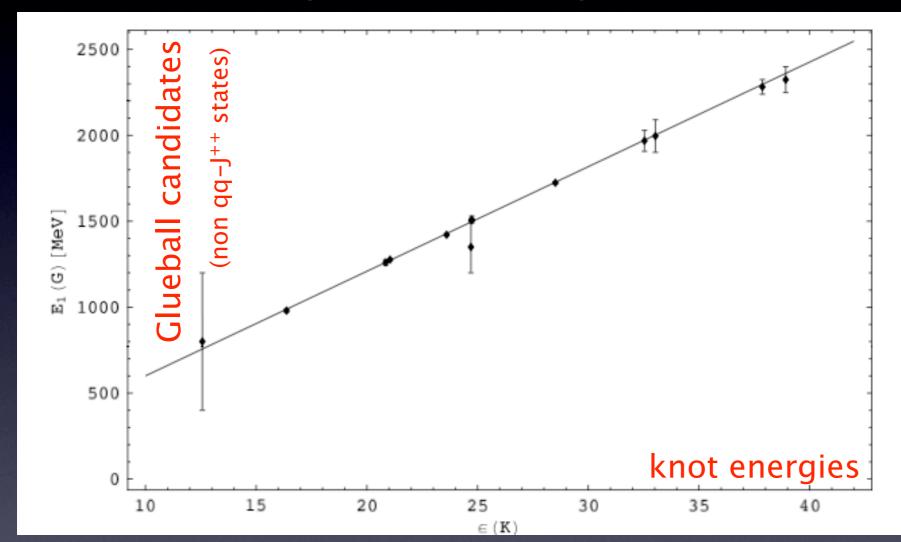
[Dale Rolfson: Knots and Links]

- Lengths of the smallest knots and links
- Several numbers lying closeby!
- Numerology?

[Ashton, Cantarella, Piatek, Rawdon, arXiv:1002.1723]

$\begin{array}{cccccccccccccccccccccccccccccccccccc$	Link	Rop_p	Rop
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	2_1^2	25.1415	25.1334
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	31	32.7437	32.7436
$egin{array}{cccccccccccccccccccccccccccccccccccc$	41	42.0971	42.0887
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	4_1^2	40.0203	40.0122
$egin{array}{cccccccccccccccccccccccccccccccccccc$			
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$\frac{5_2}{}$	49.4820	49.4701
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	5_1^2	49.7864	49.7716
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	6_{1}	56.7178	56.7058
$egin{array}{cccccccccccccccccccccccccccccccccccc$	6_2	57.0381	57.0235
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	63	57.8531	57.8392
$6_3^{\overline{2}}$ 58.1142 58.1013 $6_1^{\overline{3}}$ 57.8286 57.8141 $6_2^{\overline{3}}$ 58.0112 58.0070 $6_3^{\overline{3}}$ 50.5602 50.5539 7_1 61.4234 61.4067 7_2 63.8684 63.8556 7_3 63.9430 63.9285 7_4 64.2836 64.2687 7_5 65.2705 65.2560 7_6 65.7068 65.6924	6^2_1	54.3919	54.3768
$egin{array}{cccccccccccccccccccccccccccccccccccc$		56.7087	56.7000
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$\frac{6_3^2}{}$	58.1142	58.1013
$egin{array}{cccccccccccccccccccccccccccccccccccc$	6^{3}_{1}	57.8286	57.8141
7_1 61.4234 61.4067 7_2 63.8684 63.8556 7_3 63.9430 63.9285 7_4 64.2836 64.2687 7_5 65.2705 65.2560 7_6 65.7068 65.6924	6_{2}^{3}	58.0112	58.0070
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	6_3^3	50.5602	50.5539
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	71	61.4234	61.4067
$egin{array}{cccccccccccccccccccccccccccccccccccc$	7_2	63.8684	63.8556
7 ₅ 65.2705 65.2560 7 ₆ 65.7068 65.6924	7_3	63.9430	63.9285
7 ₆ 65.7068 65.6924			
ė.	-	65.2705	65.2560
77 65.6235 65.6086		65.7068	65.6924
	7_7	65.6235	65.6086

- What's relating know lengths and particle physics?
- Assume knot length \propto knot energy (flux tube model)



[Buniy, Kephart '03,'05; Buniy, Holmes, Kephart '09]

Excellent fit to the spectrum of glueball candidates!

- String theory (+ AdS/QCD duality): glueballs, gravitons and modulinos are open strings
- [Arkani-Hamed, Dvali, Dimopoulos, March-Russell + some 400 cites]: Right-handed neutrinos can be closed string modulinos

→Obtain Leptonic flavor structures by assuming right-handed neutrino masses are dominated by knot and link energies?

6×6 seesaw matrix:

$$m_{
u} = \left(egin{array}{ccc} 0 & m_D^{
m diag} \\ m_D^{
m diag} & M_R \end{array}
ight)$$
 $Mixing purely from right-handed sector!
$$M_R = \left(egin{array}{ccc} {
m knot}_1 & {
m link}_1 & {
m link}_2 \\ {
m link}_1 & {
m knot}_2 & {
m link}_3 \\ {
m link}_2 & {
m link}_3 & {
m knot}_3 \end{array}
ight)$$$

[Kephart, Leser, Päs, 2011]

Comparing model with data: back on the envelope

Diagonalizing the seesaw formula:

$$M_{\mathrm{flv}}^{
u}=m_{\mathrm{D}}^{T}M^{-1}m_{\mathrm{D}}$$

$$M_{\mathrm{flv}}^{\nu} = \frac{1}{\Delta^{3}} \begin{pmatrix} \left[m_{2}^{\mathrm{K}} m_{3}^{\mathrm{K}} - \left(m_{3}^{\mathrm{L}} \right)^{2} \right] \left(m_{1}^{\mathrm{D}} \right)^{2} & \left(m_{2}^{\mathrm{L}} m_{3}^{\mathrm{L}} - m_{3}^{\mathrm{K}} m_{1}^{\mathrm{L}} \right) m_{1}^{\mathrm{D}} m_{2}^{\mathrm{D}} & \left(m_{1}^{\mathrm{L}} m_{3}^{\mathrm{L}} - m_{2}^{\mathrm{K}} m_{2}^{\mathrm{L}} \right) m_{1}^{\mathrm{D}} m_{3}^{\mathrm{D}} \\ \left(m_{2}^{\mathrm{L}} m_{3}^{\mathrm{L}} - m_{3}^{\mathrm{K}} m_{1}^{\mathrm{L}} \right) m_{1}^{\mathrm{D}} m_{2}^{\mathrm{D}} & \left[m_{1}^{\mathrm{K}} m_{3}^{\mathrm{K}} - \left(m_{2}^{\mathrm{L}} \right)^{2} \right] \left(m_{2}^{\mathrm{D}} \right)^{2} & \left(m_{1}^{\mathrm{L}} m_{2}^{\mathrm{L}} - m_{1}^{\mathrm{K}} m_{3}^{\mathrm{L}} \right) m_{2}^{\mathrm{D}} m_{3}^{\mathrm{D}} \\ \left(m_{1}^{\mathrm{L}} m_{3}^{\mathrm{L}} - m_{2}^{\mathrm{K}} m_{2}^{\mathrm{L}} \right) m_{1}^{\mathrm{D}} m_{3}^{\mathrm{D}} & \left(m_{1}^{\mathrm{L}} m_{2}^{\mathrm{L}} - m_{1}^{\mathrm{K}} m_{3}^{\mathrm{L}} \right) m_{2}^{\mathrm{D}} m_{3}^{\mathrm{D}} & \left[m_{1}^{\mathrm{K}} m_{2}^{\mathrm{K}} - \left(m_{1}^{\mathrm{L}} \right)^{2} \right] \left(m_{3}^{\mathrm{D}} \right)^{2} \end{pmatrix}$$

with

$$\Delta^{3} = -m_{3}^{ ext{K}} \left(m_{1}^{ ext{L}}
ight)^{2} + 2m_{1}^{ ext{L}} m_{2}^{ ext{L}} m_{3}^{ ext{L}} - m_{2}^{ ext{K}} \left(m_{2}^{ ext{L}}
ight)^{2} - m_{1}^{ ext{K}} \left(m_{3}^{ ext{L}}
ight)^{2} + \hspace{0.2cm} m_{1}^{ ext{K}} m_{2}^{ ext{K}} m_{3}^{ ext{K}}$$

and compare with TBM mixing for various hierarchies

Comparing model with data: back on the envelope

$$\mathrm{diag}(0,0,\tilde{m})$$

$$ilde{m} \cdot egin{pmatrix} 0 & 0 & 0 \ 0 & rac{1}{2} & -rac{1}{2} \ 0 & -rac{1}{2} & rac{1}{2} \end{pmatrix}$$

$$m_3^{
m K}/m_2^{
m K} = \left(m_2^{
m D}
ight)^2/\left(m_3^{
m D}
ight)^2, \; m_2^{
m L}/m_1^{
m L} = m_3^{
m D}/m_2^{
m D}, \; m_2^{
m K}m_2^{
m L} = m_1^{
m L}m_3^{
m L}, \; m_2^{
m L}m_3^{
m L}$$

$$m_1^{
m K} m_2^{
m K}
eq (m_1^{
m L})^2, \ ilde{m} = 2 \left(m_3^{
m D}
ight)^2 \left(\left(m_1^{
m L}
ight)^2 - m_1^{
m K} m_2^{
m K}
ight)/\Delta^3.$$

$$m_i^{\rm D}$$
 are assumed to be roughly equal

$$m_i^{
m K/L} = \ell_i^{
m K/L} \cdot m_{
m S}$$

$$\ell_i^{\mathrm{K}}$$
 and ℓ_i^{L} are close to each other.

$$\Rightarrow$$

Knots and links fit better than random numbers!

Comparing model with data: back on the envelope

Inverse hierarchy

$$\operatorname{diag}(ilde{m}, ilde{m},0)$$



$$ilde{m} \cdot egin{pmatrix} 1 & 0 & 0 \ 0 & rac{1}{2} & rac{1}{2} \ 0 & rac{1}{2} & rac{1}{2} \end{pmatrix}$$

- \Rightarrow can only be solved if $\tilde{m} = 0$
- ⇒ Disfavored for knots and links!

Degenerate neutrinos

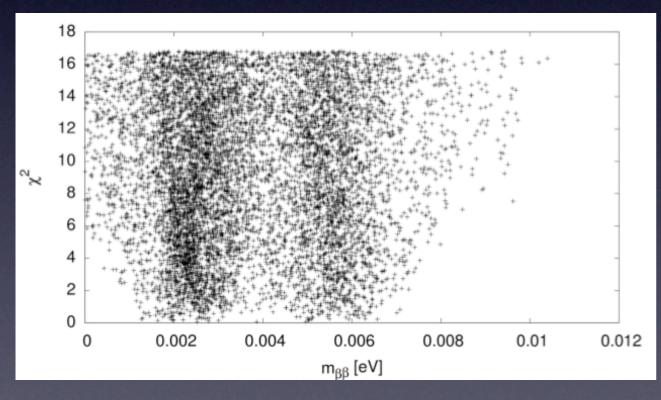
$$\operatorname{diag}(ilde{m}, ilde{m}, ilde{m}, ilde{m}) \Rightarrow m_1^{\operatorname{L}} = m_2^{\operatorname{L}} = m_3^{\operatorname{L}} = 0,$$

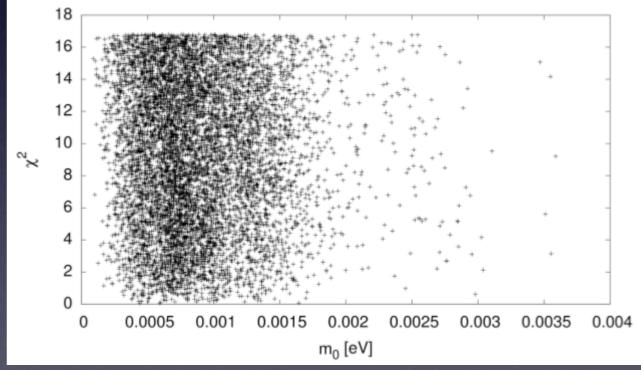
⇒ Disfavored for knots and links!

Results:

To be done: implement θ_{13}

- Excellent fit: $\chi^2 \approx 0.04$
- Comparison with random numbers favorable
- Normal hierarchy preferred (bad news for 0νββ decay search)





[Kephart, Leser, Päs, 2011]

Conclusions

- Huge variety of flavor models
- Neither generic predictions nor discriminators in the v sector
- Flavor models where the same Higgses break EW and Flavor symmetry: characteristic Higgs sectors
- Spectacular LFV signals at the LHC
- But also: Symmetry and Anarchy are not the only explanation for the leptonic Flavor structure
- Example: seesaw models with right-handed v's as knotted strings