

EM STRUCTURE MODEL OF HYPERONS WITH GROUD STATE $\rho(770)$, $\omega(782)$, $\phi(1020)$ UNIVERSAL COUPLING CONSTANTS

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INTRODUCTION

According to $SU(3)$ classification of hadrons all $1/2^+$ hyperons are members of the $1/2^+$ baryon octet

$p, n, \Lambda, \Sigma^+, \Sigma^0, \Sigma^-, \Xi^0, \Xi^-$.

The electromagnetic (EM) structure of every of these particles is completely described by corresponding

electric $G_E(t)$

and **magnetic** $G_M(t)$

form factors (FFs), where $t = -Q^2$ is **squared momentum transferred by the virtual photon** γ^* .

INTRODUCTION

The FFs $G_E(t)$ and $G_M(t)$ are directly connected:

I.

with **experimentally measurable differential cross-section** of the elastic scattering of unpolarized electrons on unpolarized baryons $e^- B \rightarrow e^- B$ by the relation

$$\frac{d\sigma^{lab}(e^- B \rightarrow e^- B)}{d\Omega} = \frac{\alpha^2}{4E^2} \frac{\cos^2(\theta/2)}{\sin^4(\theta/2)} \frac{1}{1 + (\frac{2E}{m_B})\sin^2(\theta/2)} \times \left[\frac{G_E^2(t) - \frac{t}{4m_B^2} G_M^2(t)}{1 - \frac{t}{4m_B^2}} - 2 \frac{t}{4m_B^2} G_M^2(t) \tan^2(\theta/2) \right] \quad (1)$$

where $\alpha = 1/137$ is the fine structure constant, E is the incident electron energy and θ is scattering angle

INTRODUCTION

Ia.

the **specific measurement is the elastic scattering of the hyperon on atomic electrons**, by means of which the radius of the hyperon (i.e. Σ^- -hyperon) can be in principle determined.

INTRODUCTION

II.

with **experimentally measurable total cross-section** of electron-positron annihilation into baryon-antibaryon $e^+e^- \rightarrow B\bar{B}$ by the relation

$$\sigma_{tot}^{c.m.}(e^+e^- \rightarrow B\bar{B}) = \frac{4\pi\alpha^2\beta_B}{3t} [|G_M(t)|^2 + \frac{2m_B^2}{t} |G_E(t)|^2] \quad (2)$$

where $\beta_B = \sqrt{1 - \frac{4m_B^2}{t}}$

INTRODUCTION

III.

with **experimentally measurable total cross-section** of
antibaryon-baryon annihilation into electron-positron pair
 $\bar{B}B \rightarrow e^+e^-$ by the relation

$$\sigma_{tot}^{c.m.}(\bar{B}B \rightarrow e^+e^-) = \frac{2\pi\alpha^2}{3p_{c.m.}\sqrt{t}} [|G_M(t)|^2 + \frac{2m_B^2}{t} |G_E(t)|^2] \quad (3)$$

where $p_{c.m.}$ is the antibaryon momentum in the c.m. system

INTRODUCTION

IV.

with **experimentally measurable transverse component**

$$P_t = \frac{h}{I_0} (-2) \sqrt{\tau(1+\tau)} G_E(t) G_M(t) \tan(\theta/2) \quad (4)$$

and **longitudinal** component

$$P_l = \frac{h(E + E')}{I_0 m_B} \sqrt{\tau(1+\tau)} G_M^2(t) \tan^2(\theta/2) \quad (5)$$

of the **recoil baryon's polarization** in the electron scattering plane of the **polarization transfer process** $\vec{e}^- B \rightarrow e^- \vec{B}$
 where h is the electron **beam helicity**, I_0 is the **unpolarized cross-section excluding** σ_{Mott} and $\tau = \frac{Q^2}{4m_B^2}$.

INTRODUCTION

By measuring P_t and P_I **simultaneously** one can obtain experimental information on the ratio

$$\mu_B \frac{G_E(t)}{G_M(t)} = -\frac{P_t}{P_I} \frac{E + E'}{2m_B} \tan(\theta/2). \quad (6)$$

NOTE:

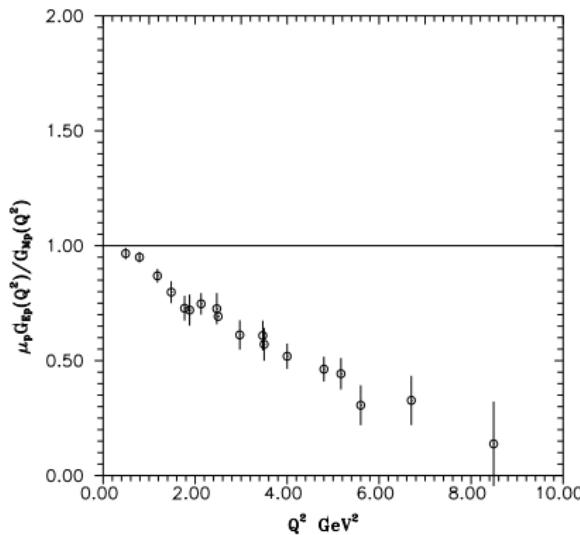
Due to the problem with hyperon targets - the measurements I., III. and IV. for **HYPERONS** are excluded!

The most data on electric and magnetic FFs, by means of the above mentioned experimentally measurable quantities, exist **for the proton**, and to some extent also **for the neutron to be obtained by light nuclei targets**.

Experimental status on protons and neutrons

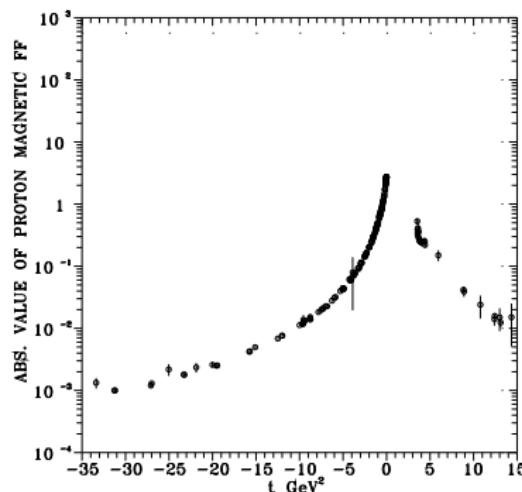
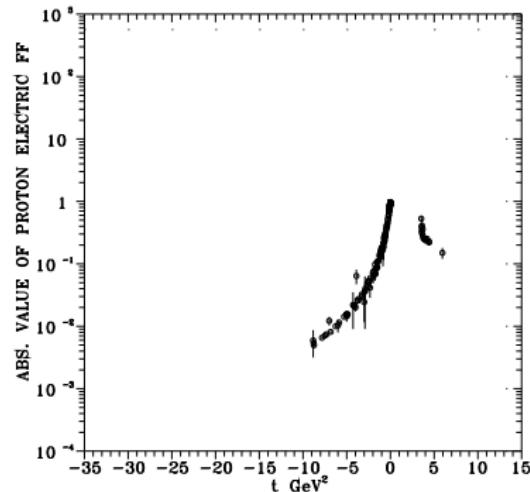
Present-day experimental information on the nucleon EM FFs $G_E^p(t)$, $G_M^p(t)$, $G_E^n(t)$, $G_M^n(t)$ consists of **10 different sets of data in various regions** - they are graphically presented in the following Figs.

Experimental status on protons and neutrons



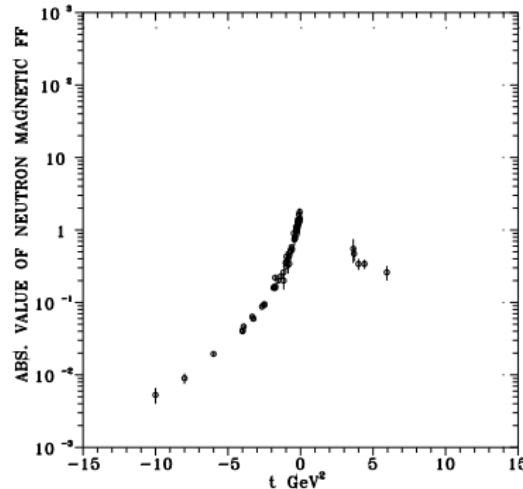
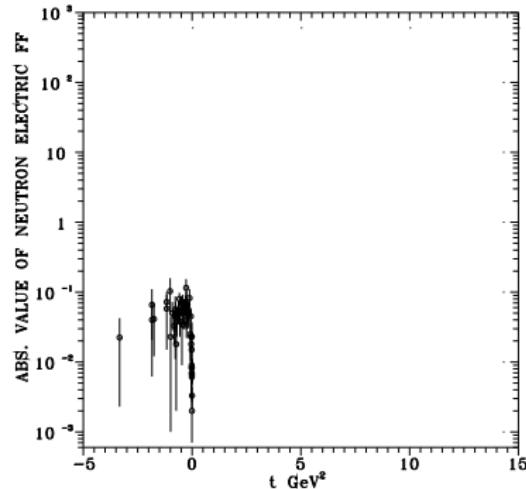
New JLab proton polarization data on the **ratio** $\mu_p G_E^p(t)/G_M^p(t)$, which **clearly demonstrate violation of the dipole behavior of** $G_E^p(t)$ **in space-like region.**

Experimental status on protons and neutrons



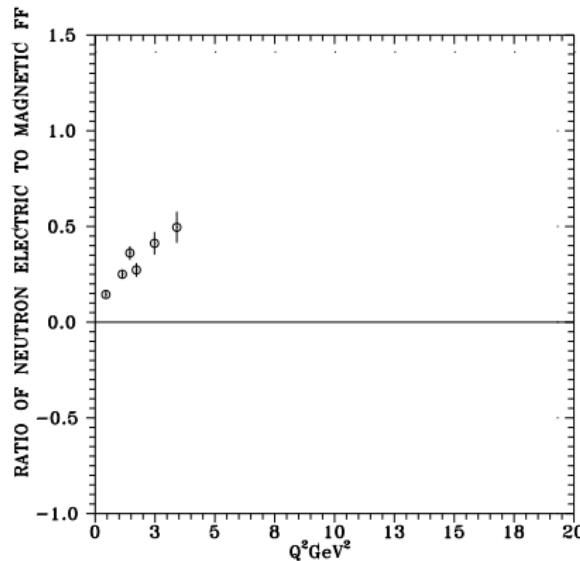
Experimental data on **proton electric and magnetic FFs** in space-like and time-like regions.

Experimental status on protons and neutrons



Experimental data on **neutron electric and magnetic FFs** in space-like and time-like regions.

Experimental status on protons and neutrons



Neutron polarization data on the ratio $\mu_n G_E^n(t)/G_M^n(t)$.

U&A MODEL OF 1/2⁺ OCTET BARYON EM STRUCTURE

In a construction of the *U&A MODEL OF 1/2⁺ OCTET BARYON EM STRUCTURE* we shall apply the *U&A approach*, which already appeared to be **very powerful in a description of the EM structure of the complete nonet of pseudoscalar mesons** $\pi^-, \pi^0, \pi^+, K^-, K^0, \bar{K}^0, K^+, \eta, \eta'$

S.Dubnicka and A.Z.Dubnickova: Eur. Phys. J. Web of Conference 37 (2012) 01003

and to some extent also in a **description of the EM structure of vector meson nonet**

$\rho^-, \rho^0, \rho^+, K^{*-}, K^{*0}, \bar{K}^{*0}, K^{*+}, \omega, \phi$

C.Adamuscin, S.Dubnicka and A.Z.Dubnickova: contribution to MESON'14 Conference

U&A MODEL OF $1/2^+$ OCTET BARYON EM STRUCTURE

The model **respects all known theoretical properties** of the baryon EM FFs, like

- assumed analyticity
- unitarity conditions
- normalizations
- experimental fact of a creation of vector-meson resonances in e^+e^- -annihilation processes into hadrons - **to every vector meson under consideration correspond a complex conjugate pair of poles placed always on un-physical sheets**
- and asymptotic behaviors

U&A MODEL OF 1/2⁺ OCTET BARYON EM STRUCTURE

Electric and magnetic FFs, $G_E(t)$ and $G_M(t)$, - **very suitable for extraction of experimental data** from the measured physical quantities.

However, for construction of various baryon EM structure models the flavor-independent **iso-scalar and iso-vector parts** of the **Dirac and Pauli FFs** to be defined by a parametrization of the baryon EM current

$$\langle B | J_\mu^{EM} | B \rangle = \bar{u}(p') \{ \gamma_\mu F_1^B(t) + i \frac{\sigma_{\mu\nu} q_\nu}{2m_B^2} F_2^B(t) \} u(p) \quad (7)$$

are more suitable.

U&A MODEL OF $1/2^+$ OCTET BARYON EM STRUCTURE

Both sets of FFs are related

$$G_E^P(t) = [F_{1s}^N(t) + F_{1v}^N(t)] + \frac{t}{4m_p^2} [F_{2s}^N(t) + F_{2v}^N(t)]$$

$$G_M^P(t) = [F_{1s}^N(t) + F_{1v}^N(t)] + [F_{2s}^N(t) + F_{2v}^N(t)]$$

$$G_E^n(t) = [F_{1s}^N(t) - F_{1v}^N(t)] + \frac{t}{4m_n^2} [F_{2s}^N(t) - F_{2v}^N(t)]$$

$$G_M^n(t) = [F_{1s}^N(t) - F_{1v}^N(t)] + [F_{2s}^N(t) - F_{2v}^N(t)]$$

$$G_E^\Lambda(t) = F_{1s}^\Lambda(t) + \frac{t}{4m_\Lambda^2} F_{2s}^\Lambda(t)$$

$$G_M^\Lambda(t) = F_{1s}^\Lambda(t) + F_{2s}^\Lambda(t)$$

$$G_E^{\Sigma^0}(t) = F_{1s}^\Sigma(t) + \frac{t}{4m_\Sigma^2} F_{2s}^\Sigma(t)$$

$$G_M^{\Sigma^0}(t) = F_{1s}^\Sigma(t) + F_{2s}^\Sigma(t)$$

U&A MODEL OF $1/2^+$ OCTET BARYON EM STRUCTURE

$$G_E^{\Sigma^+, \Sigma^-}(t) = [F_{1s}^\Sigma(t) \pm F_{1v}^\Sigma(t)] + \frac{t}{4m_\Sigma^2} [F_{2s}^\Sigma(t) \pm F_{2v}^\Sigma(t)]$$

$$G_M^{\Sigma^+, \Sigma^-}(t) = [F_{1s}^\Sigma(t) \pm F_{1v}^\Sigma(t)] + [F_{2s}^\Sigma(t) \pm F_{2v}^\Sigma(t)]$$

$$G_E^{\Xi^0, \Xi^-}(t) = [F_{1s}^{\Xi}(t) \pm F_{1v}^{\Xi}(t)] + \frac{t}{4m_\Xi^2} [F_{2s}^{\Xi}(t) \pm F_{2v}^{\Xi}(t)]$$

$$G_M^{\Xi^0, \Xi^-}(t) = [F_{1s}^{\Xi}(t) \pm F_{1v}^{\Xi}(t)] + [F_{2s}^{\Xi}(t) \pm F_{2v}^{\Xi}(t)].$$

U&A MODEL OF $1/2^+$ OCTET BARYON EM STRUCTURE

whereby **experimental fact of a creation of vector-meson resonances in $e^+e^- \rightarrow had$** is taken into account:

- **in saturation of $F_{1B}^s(t), F_{2B}^s(t)$ by iso-scalar vector mesons**
- **in saturation of $F_{1B}^v(t), F_{2B}^v(t)$ by iso-vector vector meson resonances**

in the corresponding **zero width approximation** of *VMD* parametrizations.

U&A MODEL OF 1/2⁺ OCTET BARYON EM STRUCTURE

Consideration of the $SU(3)$ symmetry in EM structure model means - always complete trinity of vector-mesons $(\rho, \omega, \phi; \rho', \omega', \phi'; \text{etc.})$ has to be taken into account !

The **Review of Particle Physics**

J.Beringer et al (Particle Data Group), Phys. Rev. D86 (2012) 010001.

provides just 3 complete trinities of such vector-meson resonances

$\rho(770), \omega(782), \phi(1020)$

$\omega'(1420), \rho'(1450)), \phi'(1680)$

$\omega''(1650), \rho''(1700), \phi''(2170).$

then also OZI rule violation is fulfilled.

U&A MODEL OF NUCLEON EM STRUCTURE

Then starting point of a construction of the *U&A* model is
9-resonance (3 iso-vectors and 6 iso-scalars) VMD model

$$\begin{aligned}
 F_{1s}^N(t) = & \frac{1}{2} \frac{m_\omega^2 m_\phi^2}{(m_\omega^2 - t)(m_\phi^2 - t)} + \\
 & + \left\{ \frac{m_\phi^2 m_{\omega'}^2}{(m_\phi^2 - t)(m_{\omega'}^2 - t)} \frac{(m_\phi^2 - m_{\omega'}^2)}{(m_\phi^2 - m_\omega^2)} + \frac{m_\omega^2 m_{\omega'}^2}{(m_\omega^2 - t)(m_{\omega'}^2 - t)} \frac{(m_\omega^2 - m_{\omega'}^2)}{(m_\omega^2 - m_\phi^2)} - \right. \\
 & \quad \left. - \frac{m_\omega^2 m_\phi^2}{(m_\omega^2 - t)(m_\phi^2 - t)} \right\} (f_{\omega' NN}^{(1)} / f_{\omega'}) + \\
 & + \left\{ \frac{m_\phi^2 m_{\phi'}^2}{(m_\phi^2 - t)(m_{\phi'}^2 - t)} \frac{(m_\phi^2 - m_{\phi'}^2)}{(m_\phi^2 - m_\omega^2)} + \frac{m_\omega^2 m_{\phi'}^2}{(m_\omega^2 - t)(m_{\phi'}^2 - t)} \frac{(m_\omega^2 - m_{\phi'}^2)}{(m_\omega^2 - m_\phi^2)} - \right. \\
 & \quad \left. - \frac{m_\omega^2 m_\phi^2}{(m_\omega^2 - t)(m_\phi^2 - t)} \right\} (f_{\phi' NN}^{(1)} / f_{\phi'}) +
 \end{aligned}$$

U&A MODEL OF NUCLEON EM STRUCTURE

$$\begin{aligned}
 & + \left\{ \frac{m_\phi^2 m_{\omega''}^2}{(m_\phi^2 - t)(m_{\omega''}^2 - t)} \frac{(m_\phi^2 - m_{\omega''}^2)}{(m_\phi^2 - m_\omega^2)} + \frac{m_\omega^2 m_{\omega''}^2}{(m_\omega^2 - t)(m_{\omega''}^2 - t)} \frac{(m_\omega^2 - m_{\omega''}^2)}{(m_\omega^2 - m_\phi^2)} - \right. \\
 & \quad \left. - \frac{m_\omega^2 m_\phi^2}{(m_\omega^2 - t)(m_\phi^2 - t)} \right\} (f_{\omega'' NN}^{(1)} / f_{\omega''}) + \\
 & + \left\{ \frac{m_\phi^2 m_{\phi''}^2}{(m_\phi^2 - t)(m_{\phi''}^2 - t)} \frac{(m_\phi^2 - m_{\phi''}^2)}{(m_\phi^2 - m_\omega^2)} + \frac{m_\omega^2 m_{\phi''}^2}{(m_\omega^2 - t)(m_{\phi''}^2 - t)} \frac{(m_\omega^2 - m_{\phi''}^2)}{(m_\omega^2 - m_\phi^2)} - \right. \\
 & \quad \left. - \frac{m_\omega^2 m_\phi^2}{(m_\omega^2 - t)(m_\phi^2 - t)} \right\} (f_{\phi'' NN}^{(1)} / f_{\phi''}).
 \end{aligned}$$

U&A MODEL OF NUCLEON EM STRUCTURE

$$\begin{aligned}
 F_{1\nu}^N(t) = & \frac{1}{2} \frac{m_\rho^2 m_{\rho'}^2}{(m_\rho^2 - t)(m_{\rho'}^2 - t)} + \\
 & + \left\{ \frac{m_{\rho'}^2 m_{\rho''}^2}{(m_{\rho'}^2 - t)(m_{\rho''}^2 - t)} \frac{(m_{\rho'}^2 - m_{\rho''}^2)}{(m_{\rho'}^2 - m_\rho^2)} + \frac{m_\rho^2 m_{\rho''}^2}{(m_\rho^2 - t)(m_{\rho''}^2 - t)} \frac{(m_\rho^2 - m_{\rho''}^2)}{(m_\rho^2 - m_{\rho'}^2)} - \right. \\
 & \left. - \frac{m_\rho^2 m_{\rho'}^2}{(m_\rho^2 - t)(m_{\rho'}^2 - t)} \right\} (f_{\rho'' NN}^{(1)} / f_{\rho''}).
 \end{aligned}$$

U&A MODEL OF NUCLEON EM STRUCTURE

$$\begin{aligned}
 F_{2s}^N(t) = & \frac{1}{2}(\mu_p + \mu_n - 1) \frac{m_\omega^2 m_\phi^2 m_{\omega'}^2}{(m_\omega^2 - t)(m_\phi^2 - t)(m_{\omega'}^2 - t)} + \\
 & + \left\{ \frac{m_\phi^2 m_\omega^2 m_{\phi'}^2}{(m_\phi^2 - t)(m_\omega^2 - t)(m_{\phi'}^2 - t)} \frac{(m_\phi^2 - m_{\phi'}^2)(m_{\omega'}^2 - m_{\phi'}^2)}{(m_\phi^2 - m_\omega^2)(m_{\omega'}^2 - m_\omega^2)} + \right. \\
 & + \frac{m_\omega^2 m_\omega^2 m_{\phi'}^2}{(m_\omega^2 - t)(m_\omega^2 - t)(m_{\phi'}^2 - t)} \frac{(m_\omega^2 - m_{\phi'}^2)(m_{\omega'}^2 - m_{\phi'}^2)}{(m_\omega^2 - m_\phi^2)(m_{\omega'}^2 - m_\phi^2)} + \\
 & + \frac{m_\omega^2 m_\phi^2 m_{\phi'}^2}{(m_\omega^2 - t)(m_\phi^2 - t)(m_{\phi'}^2 - t)} \frac{(m_\omega^2 - m_{\phi'}^2)(m_\phi^2 - m_{\phi'}^2)}{(m_\omega^2 - m_{\omega'}^2)(m_\phi^2 - m_{\omega'}^2)} - \\
 & \left. - \frac{m_\omega^2 m_\phi^2 m_{\omega'}^2}{(m_\omega^2 - t)(m_\phi^2 - t)(m_{\omega'}^2 - t)} \right\} (f_{\phi' NN}^{(2)} / f_{\phi'}) +
 \end{aligned}$$

U&A MODEL OF NUCLEON EM STRUCTURE

$$\begin{aligned}
 & + \left\{ \frac{m_\phi^2 m_\omega^2, m_{\omega''}^2}{(m_\phi^2 - t)(m_{\omega'}^2 - t)(m_{\omega''}^2 - t)} \frac{(m_\phi^2 - m_{\omega''}^2)(m_{\omega'}^2 - m_{\omega''}^2)}{(m_\phi^2 - m_\omega^2)(m_{\omega'}^2 - m_\omega^2)} + \right. \\
 & + \frac{m_\omega^2 m_\omega^2, m_{\omega''}^2}{(m_\omega^2 - t)(m_{\omega'}^2 - t)(m_{\omega''}^2 - t)} \frac{(m_\omega^2 - m_{\omega''}^2)(m_{\omega'}^2 - m_{\omega''}^2)}{(m_\omega^2 - m_\phi^2)(m_{\omega'}^2 - m_\phi^2)} + \\
 & + \frac{m_\omega^2 m_\phi^2 m_{\omega''}^2}{(m_\omega^2 - t)(m_\phi^2 - t)(m_{\omega''}^2 - t)} \frac{(m_\omega^2 - m_{\omega''}^2)(m_\phi^2 - m_{\omega''}^2)}{(m_\omega^2 - m_{\omega'}^2)(m_\phi^2 - m_{\omega'}^2)} - \\
 & \left. - \frac{m_\omega^2 m_\phi^2 m_{\omega'}^2}{(m_\omega^2 - t)(m_\phi^2 - t)(m_{\omega'}^2 - t)} \right\} (f_{\omega'' NN}^{(2)} / f_{\omega''}) +
 \end{aligned}$$

U&A MODEL OF NUCLEON EM STRUCTURE

$$\begin{aligned}
 & + \left\{ \frac{m_\phi^2 m_{\omega'}^2 m_{\phi''}^2}{(m_\phi^2 - t)(m_{\omega'}^2 - t)(m_{\phi''}^2 - t)} \frac{(m_\phi^2 - m_{\phi''}^2)(m_{\omega'}^2 - m_{\phi''}^2)}{(m_\phi^2 - m_\omega^2)(m_{\omega'}^2 - m_\omega^2)} + \right. \\
 & + \frac{m_\omega^2 m_{\omega'}^2 m_{\phi''}^2}{(m_\omega^2 - t)(m_{\omega'}^2 - t)(m_{\phi''}^2 - t)} \frac{(m_\omega^2 - m_{\phi''}^2)(m_{\omega'}^2 - m_{\phi''}^2)}{(m_\omega^2 - m_\phi^2)(m_{\omega'}^2 - m_\phi^2)} + \\
 & + \frac{m_\omega^2 m_\phi^2 m_{\phi''}^2}{(m_\omega^2 - t)(m_\phi^2 - t)(m_{\phi''}^2 - t)} \frac{(m_\omega^2 - m_{\phi''}^2)(m_\phi^2 - m_{\phi''}^2)}{(m_\omega^2 - m_{\omega'}^2)(m_\phi^2 - m_{\omega'}^2)} - \\
 & \left. - \frac{m_\omega^2 m_\phi^2 m_{\omega'}^2}{(m_\omega^2 - t)(m_\phi^2 - t)(m_{\omega'}^2 - t)} \right\} (f_{\phi'' NN}^{(2)} / f_{\phi''})
 \end{aligned}$$

U&A MODEL OF NUCLEON EM STRUCTURE

$$F_{2\nu}^N(t) = \frac{1}{2}(\mu_p - \mu_n - 1) \frac{m_\rho^2 m_{\rho'}^2 m_{\rho''}^2}{(m_\rho^2 - t)(m_{\rho'}^2 - t)(m_{\rho''}^2 - t)}$$

to be **automatically normalized** and governing the **asymptotic behaviors** as predicted by the quark model of hadrons.

By the non-linear transformations

$$t = t_0^s + \frac{4(t_{in}^{1s} - t_0^s)}{[1/V(t) - V(t)]^2}; \quad t = t_0^\nu + \frac{4(t_{in}^{1\nu} - t_0^\nu)}{[1/W(t) - W(t)]^2};$$

$$t = t_0^s + \frac{4(t_{in}^{2s} - t_0^s)}{[1/U(t) - U(t)]^2}; \quad t = t_0^\nu + \frac{4(t_{in}^{2\nu} - t_0^\nu)}{[1/X(t) - X(t)]^2}.$$

and a subsequent **inclusion of the nonzero values of vector-meson widths**, for every iso-scalar and iso-vector Dirac and Pauli FF, one obtains just **one analytic and smooth from $-\infty$ to $+\infty$ function** in the form

U&A MODEL OF NUCLEON EM STRUCTURE

$$\begin{aligned}
 F_{1s}^N[V(t)] = & \left(\frac{1 - V^2}{1 - V_N^2} \right)^4 \frac{1}{2} L_\omega(V) L_\phi(V) + \\
 & + \left(\frac{1 - V^2}{1 - V_N^2} \right)^4 \left[L_\phi(V) L_{\omega'}(V) \frac{(C_\phi^{1s} - C_{\omega'}^{1s})}{(C_\phi^{1s} - C_\omega^{1s})} + L_\omega(V) L_{\omega'}(V) \frac{(C_\omega^{1s} - C_{\omega'}^{1s})}{(C_\omega^{1s} - C_\phi^{1s})} - \right. \\
 & \quad \left. - L_\omega(V) L_\phi(V) \right] (f_{\omega' NN}^{(1)} / f_{\omega'}) + \\
 & + \left(\frac{1 - V^2}{1 - V_N^2} \right)^4 \left[L_\phi(V) H_{\phi'}(V) \frac{(C_\phi^{1s} - C_{\phi'}^{1s})}{(C_\phi^{1s} - C_\omega^{1s})} + L_\omega(V) H_{\phi'}(V) \frac{(C_\omega^{1s} - C_{\phi'}^{1s})}{(C_\omega^{1s} - C_\phi^{1s})} - \right. \\
 & \quad \left. - L_\omega(V) L_\phi(V) \right] (f_{\phi' NN}^{(1)} / f_{\phi'}) +
 \end{aligned}$$

U&A MODEL OF NUCLEON EM STRUCTURE

$$\begin{aligned} & + \left(\frac{1 - V^2}{1 - V_N^2} \right)^4 \left[L_\phi(V) H_{\omega''}(V) \frac{(C_\phi^{1s} - C_{\omega''}^{1s})}{(C_\phi^{1s} - C_\omega^{1s})} + L_\omega(V) H_{\omega''}(V) \frac{(C_\omega^{1s} - C_{\omega''}^{1s})}{(C_\omega^{1s} - C_\phi^{1s})} - \right. \\ & \quad \left. - L_\omega(V) L_\phi(V) \right] (f_{\omega''NN}^{(1)} / f_{\omega''}) + \\ & + \left(\frac{1 - V^2}{1 - V_N^2} \right)^4 \left[L_\phi(V) H_{\phi''}(V) \frac{(C_\phi^{1s} - C_{\phi''}^{1s})}{(C_\phi^{1s} - C_\omega^{1s})} + L_\omega(V) H_{\phi''}(V) \frac{(C_\omega^{1s} - C_{\phi''}^{1s})}{(C_\omega^{1s} - C_\phi^{1s})} - \right. \\ & \quad \left. - L_\omega(V) L_\phi(V) \right] (f_{\phi''NN}^{(1)} / f_{\phi''}) \end{aligned}$$

U&A MODEL OF NUCLEON EM STRUCTURE

$$\begin{aligned}
 F_{1\nu}^N[W(t)] = & \left(\frac{1 - W^2}{1 - W_N^2} \right)^4 \left\{ \frac{1}{2} L_\rho(W) L_{\rho'}(W) + \right. \\
 & + \left[L_{\rho'}(W) H_{\rho''}(W) \frac{(C_{\rho'}^{1\nu} - C_{\rho''}^{1\nu})}{(C_{\rho'}^{1\nu} - C_\rho^{1\nu})} + L_\rho(W) H_{\rho''}(W) \frac{(C_\rho^{1\nu} - C_{\rho''}^{1\nu})}{(C_\rho^{1\nu} - C_{\rho'}^{1\nu})} - \right. \\
 & \quad \left. \left. - L_\rho(W) L_{\rho'}(W) \right] (f_{\rho''NN}^{(1)} / f_{\rho''}) \right\}
 \end{aligned}$$

U&A MODEL OF NUCLEON EM STRUCTURE

$$\begin{aligned}
 F_{2s}^N[U(t)] = & \left(\frac{1 - U^2}{1 - U_N^2} \right)^6 \frac{1}{2} (\mu_p + \mu_n - 1) L_\omega(U) L_\phi(U) L_{\omega'}(U) + \\
 & + \left(\frac{1 - U^2}{1 - U_N^2} \right)^6 \left[L_\phi(U) L_{\omega'}(U) H_{\phi'}(U) \frac{(C_\phi^{2s} - C_{\phi'}^{2s})(C_{\omega'}^{2s} - C_\phi^{2s})}{(C_\phi^{2s} - C_\omega^{2s})(C_{\omega'}^{2s} - C_\omega^{2s})} + \right. \\
 & + L_\omega(U) L_{\omega'}(U) H_{\phi'}(U) \frac{(C_\omega^{2s} - C_{\phi'}^{2s})(C_{\omega'}^{2s} - C_{\phi'}^{2s})}{(C_\omega^{2s} - C_\phi^{2s})(C_{\omega'}^{2s} - C_\phi^{2s})} + \\
 & + L_\omega(U) L_\phi(U) H_{\phi'}(U) \frac{(C_\omega^{2s} - C_{\phi'}^{2s})(C_\phi^{2s} - C_{\phi'}^{2s})}{(C_\omega^{2s} - C_{\omega'}^{2s})(C_\phi^{2s} - C_{\omega'}^{2s})} - \\
 & \left. - L_\omega(U) L_\phi(U) L_{\omega'}(U) \right] (f_{\phi' NN}^{(2)} / f_{\phi'}) +
 \end{aligned}$$

U&A MODEL OF NUCLEON EM STRUCTURE

$$\begin{aligned}
 & + \left(\frac{1 - U^2}{1 - U_N^2} \right)^6 \left[L_\phi(U) L_{\omega'}(U) H_{\omega''}(U) \frac{(C_\phi^{2s} - C_{\omega''}^{2s})(C_{\omega'}^{2s} - C_{\omega''}^{2s})}{(C_\phi^{2s} - C_\omega^{2s})(C_{\omega'}^{2s} - C_\omega^{2s})} + \right. \\
 & + L_\omega(U) L_{\omega'}(U) H_{\omega''}(U) \frac{(C_\omega^{2s} - C_{\omega''}^{2s})(C_{\omega'}^{2s} - C_{\omega''}^{2s})}{(C_\omega^{2s} - C_{\omega'}^{2s})(C_{\omega'}^{2s} - C_\phi^{2s})} + \\
 & + L_\omega(U) L_\phi(U) H_{\omega''}(U) \frac{(C_\omega^{2s} - C_{\omega''}^{2s})(C_\phi^{2s} - C_{\omega''}^{2s})}{(C_\omega^{2s} - C_{\omega'}^{2s})(C_\phi^{2s} - C_{\omega'}^{2s})} - \\
 & \left. - L_\omega(U) L_\phi(U) L_{\omega'}(U) \right] \left(f_{\omega'' NN}^{(2)} / f_{\omega''} \right) +
 \end{aligned}$$

U&A MODEL OF NUCLEON EM STRUCTURE

$$\begin{aligned}
 & + \left(\frac{1 - U^2}{1 - U_N^2} \right)^6 \left[L_\phi(U) L_{\omega'}(U) H_{\phi''}(U) \frac{(C_\phi^{2s} - C_{\phi''}^{2s})(C_{\omega'}^{2s} - C_{\phi''}^{2s})}{(C_\phi^{2s} - C_\omega^{2s})(C_{\omega'}^{2s} - C_\omega^{2s})} + \right. \\
 & + L_\omega(U) L_{\omega'}(U) H_{\phi''}(U) \frac{(C_\omega^{2s} - C_{\phi''}^{2s})(C_{\omega'}^{2s} - C_{\phi''}^{2s})}{(C_\omega^{2s} - C_\phi^{2s})(C_{\omega'}^{2s} - C_\phi^{2s})} + \\
 & + L_\omega(U) L_\phi(U) H_{\phi''}(U) \frac{(C_\omega^{2s} - C_{\phi''}^{2s})(C_\phi^{2s} - C_{\phi''}^{2s})}{(C_\omega^{2s} - C_{\omega'}^{2s})(C_\phi^{2s} - C_{\omega'}^{2s})} - \\
 & \left. - L_\omega(U) L_\phi(U) L_{\omega'}(U) \right] (f_{\phi''NN}^{(2)} / f_{\phi''})
 \end{aligned}$$

U&A MODEL OF NUCLEON EM STRUCTURE

$$F_{2\nu}^N[X(t)] = \left(\frac{1-X^2}{1-X_N^2}\right)^6 \left\{ \frac{1}{2}(\mu_p - \mu_n - 1)L_\rho(U)L_{\rho'}(U)H_{\rho''}(U) \right\}$$

where

$$L_r(V) = \frac{(V_N - V_r)(V_N - V_r^*)(V_N - 1/V_r)(V_N - 1/V_r^*)}{(V - V_r)(V - V_r^*)(V - 1/V_r)(V - 1/V_r^*)},$$

$$C_r^{1s} = \frac{(V_N - V_r)(V_N - V_r^*)(V_N - 1/V_r)(V_N - 1/V_r^*)}{-(V_r - 1/V_r)(V_r - 1/V_r^*)}, r = \omega, \phi, \omega'$$

U&A MODEL OF NUCLEON EM STRUCTURE

$$H_I(V) = \frac{(V_N - V_I)(V_N - V_I^*)(V_N + V_I)(V_N + V_I^*)}{(V - V_I)(V - V_I^*)(V + V_I)(V + V_I^*)},$$

$$C_I^{1s} = \frac{(V_N - V_I)(V_N - V_I^*)(V_N + V_I)(V_N + V_I^*)}{-(V_I - 1/V_I)(V_I - 1/V_I^*)}, I = \phi', \omega''\phi''$$

$$L_k(W) = \frac{(W_N - W_k)(W_N - W_k^*)(W_N - 1/W_k)(W_N - 1/W_k^*)}{(W - W_k)(W - W_k^*)(W - 1/W_k)(W - 1/W_k^*)},$$

$$C_k^{1v} = \frac{(W_N - W_k)(W_N - W_k^*)(W_N - 1/W_k)(W_N - 1/W_k^*)}{-(W_k - 1/W_k)(W_k - 1/W_k^*)}, k = \rho, \rho'$$

U&A MODEL OF NUCLEON EM STRUCTURE

$$H_{\rho''}(W) = \frac{(W_N - W_{\rho''})(W_N - W_{\rho''}^*)(W_N + W_{\rho''})(W_N + W_{\rho''}^*)}{(W - W_{\rho''})(W - W_{\rho''}^*)(W + W_{\rho''})(W + W_{\rho''}^*)},$$

$$C_{\rho''}^{1v} = \frac{(W_N - W_{\rho''})(W_N - W_{\rho''}^*)(W_N + W_{\rho''})(W_N + W_{\rho''}^*)}{-(W_{\rho''} - 1/W_{\rho''})(W_{\rho''} - 1/W_{\rho''}^*)},$$

$$L_r(U) = \frac{(U_N - U_r)(U_N - U_r^*)(U_N - 1/U_r)(U_N - 1/U_r^*)}{(U - U_r)(U - U_r^*)(U - 1/U_r)(U - 1/U_r^*)},$$

$$C_r^{2s} = \frac{(U_N - U_r)(U_N - U_r^*)(U_N - 1/U_r)(U_N - 1/U_r^*)}{-(U_r - 1/U_r)(U_r - 1/U_r^*)}, r = \omega, \phi, \omega'$$

$$H_I(U) = \frac{(U_N - U_I)(U_N - U_I^*)(U_N + U_I)(U_N + U_I^*)}{(U - U_I)(U - U_I^*)(U + U_I)(U + U_I^*)},$$

$$C_I^{2s} = \frac{(U_N - U_I)(U_N - U_I^*)(U_N + U_I)(U_N + U_I^*)}{-(U_I - 1/U_I)(U_I - 1/U_I^*)}, I = \phi', \omega'' \phi''$$

U&A MODEL OF NUCLEON EM STRUCTURE

$$L_k(X) = \frac{(X_N - X_k)(X_N - X_k^*)(X_N - 1/X_k)(X_N - 1/X_k^*)}{(X - X_k)(X - X_k^*)(X - 1/X_k)(X - 1/X_k^*)},$$

$$C_k^{2v} = \frac{(X_N - X_k)(X_N - X_k^*)(X_N - 1/X_k)(X_N - 1/X_k^*)}{-(X_k - 1/X_k)(X_k - 1/X_k^*)}, k = \rho, \rho'$$

$$H_{\rho''}(X) = \frac{(X_N - X_{\rho''})(X_N - X_{\rho''}^*)(X_N + X_{\rho''})(X_N + X_{\rho''}^*)}{(X - X_{\rho''})(X - X_{\rho''}^*)(X + X_{\rho''})(X + X_{\rho''}^*)},$$

$$C_{\rho''}^{2v} = \frac{(X_N - X_{\rho''})(X_N - X_{\rho''}^*)(X_N + X_{\rho''})(W_X + X_{\rho''}^*)}{-(X_{\rho''} - 1/X_{\rho''})(X_{\rho''} - 1/X_{\rho''}^*)}.$$

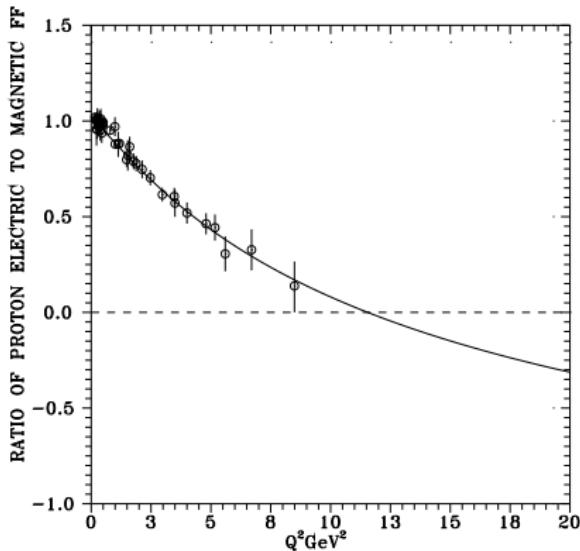
U&A MODEL OF NUCLEON EM STRUCTURE

This advanced model is **defined on four-sheeted Riemann surface** and one can simply verify that it includes all required properties like

- **experimental fact of a creation of unstable vector-meson resonances** in e^+e^- annihilation processes into hadrons
- the **analytic properties** of FFs
- the **reality conditions**
- the **unitarity conditions** of FFs
- the **normalizations** of FFs
- the **asymptotic behaviors** of FFs as predicted by quark model of hadrons

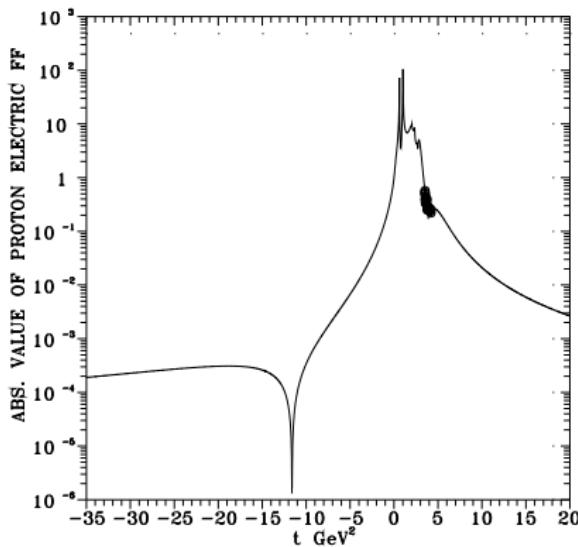
By its comparison with present-day nucleon EM FFs data in space-like and time-like regions simultaneously(see Figs.)

U&A MODEL OF NUCLEON EM STRUCTURE



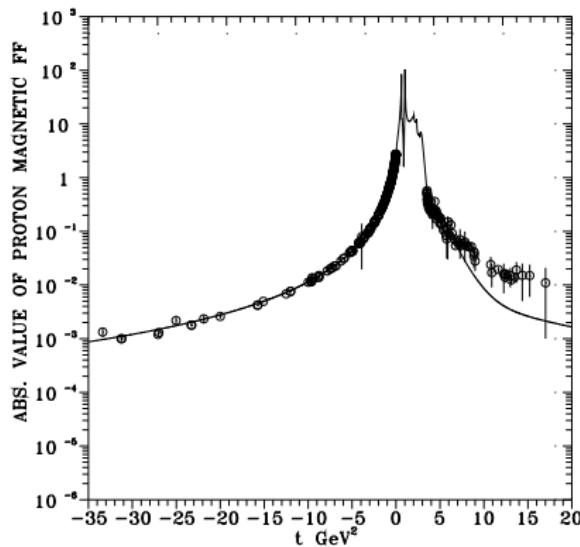
Prediction of **proton electric to magnetic FFs ratio** behavior by
U&A model respecting $SU(3)$ symmetry and OZI rule violation

U&A MODEL OF NUCLEON EM STRUCTURE



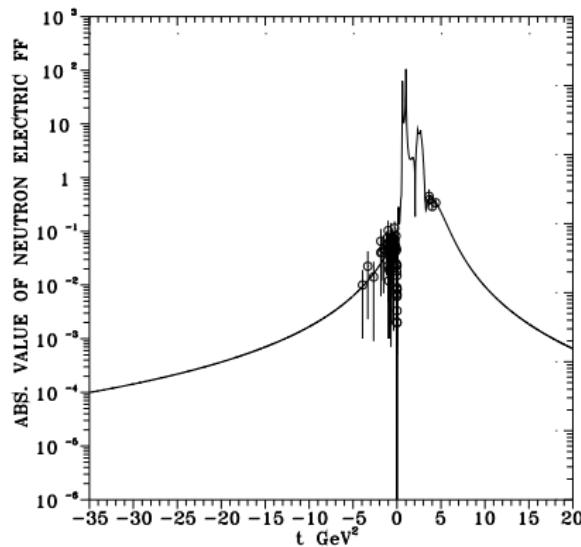
Prediction of **proton electric FF** behavior by *U&A* model respecting *SU(3)* symmetry and OZI rule violation

U&A MODEL OF NUCLEON EM STRUCTURE



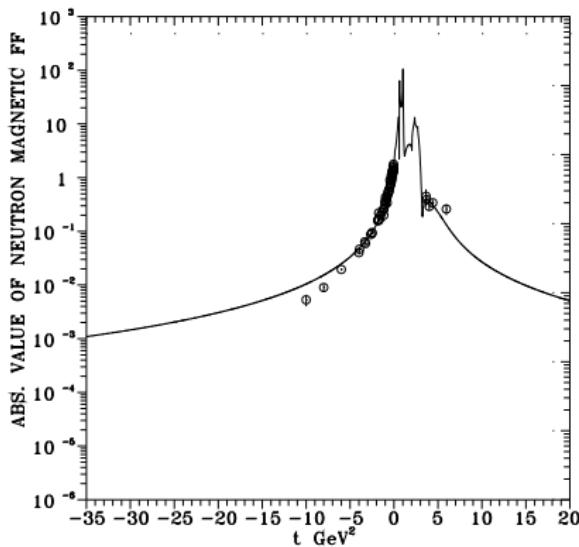
Prediction of **proton magnetic FF** behavior by *U&A* model respecting *SU(3)* symmetry and OZI rule violation

U&A MODEL OF NUCLEON EM STRUCTURE



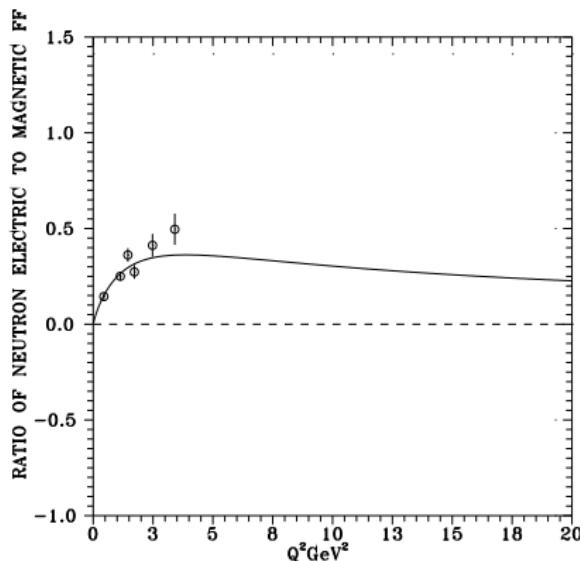
Prediction of **neutron electric FF** behavior by $U\&A$ model respecting $SU(3)$ symmetry and OZI rule violation

U&A MODEL OF NUCLEON EM STRUCTURE



Prediction of **neutron magnetic FF** behavior by *U&A* model respecting *SU(3)* symmetry and OZI rule violation

U&A MODEL OF NUCLEON EM STRUCTURE



Prediction of **neutron electric to magnetic FFs ratio** behavior by *U&A* model respecting *SU(3)* symmetry and OZI rule violation

U&A MODEL OF NUCLEON EM STRUCTURE

one determines **all free parameters of the model**

$$F_{1s}^N : (f_{\omega' NN}^{(1)} / f_{\omega'}), (f_{\phi' NN}^{(1)} / f_{\phi'}), (f_{\omega'' NN}^{(1)} / f_{\omega''}), (f_{\phi'' NN}^{(1)} / f_{\phi''})$$

$$F_{1v}^N : (f_{\rho'' NN}^{(1)} / f_{\rho''})$$

$$F_{2s}^N : (f_{\phi' NN}^{(2)} / f_{\phi'}), (f_{\omega'' NN}^{(2)} / f_{\omega''}), (f_{\phi'' NN}^{(2)} / f_{\phi''})$$

$$F_{2v}^N : 0$$

NOTE: One does not see here coupling constants ratios

$(f_{\omega NN}^{(1)} / f_{\omega}), (f_{\phi NN}^{(1)} / f_{\phi}), (f_{\rho NN}^{(1)} / f_{\rho}), (f_{\rho' NN}^{(1)} / f_{\rho'}), (f_{\omega NN}^{(2)} / f_{\omega}), (f_{\phi NN}^{(2)} / f_{\phi}),$
 $(f_{\omega' NN}^{(2)} / f_{\omega'}), (f_{\rho NN}^{(2)} / f_{\rho}), (f_{\rho' NN}^{(2)} / f_{\rho'}), (f_{\rho'' NN}^{(2)} / f_{\rho''})$, which by
 demanding in constructed model correct norms and the asymptotic
 behaviors of FFs have been **expressed through special
 combinations of vector meson masses.**

HYPERONS EM STRUCTURE MODEL

Similarly to nucleons, one can construct also the **advanced U&A model of hyperon EM FFs** to be completely described by the Sachs electric $G_E^h(t)$ and magnetic $G_M^h(t)$ FFs.

$$F_{1s}^\Lambda[V(t)] = \left(\frac{1-V^2}{1-V_\Lambda^2}\right)^4 \left[L_\phi(V)L_{\omega'}(V) \frac{(C_\phi^{1s} - C_{\omega'}^{1s})}{(C_\phi^{1s} - C_\omega^{1s})} + L_\omega(V)L_{\omega'}(V) \frac{(C_\omega^{1s} - C_{\omega'}^{1s})}{(C_\omega^{1s} - C_\phi^{1s})} - L_\omega(V)L_\phi(V) \right] (f_{\omega'\Lambda\Lambda}^{(1)} / f_{\omega'}) + \\ + \left(\frac{1-V^2}{1-V_\Lambda^2}\right)^4 \left[L_\phi(V)H_{\phi'}(V) \frac{(C_\phi^{1s} - C_{\phi'}^{1s})}{(C_\phi^{1s} - C_\omega^{1s})} + L_\omega(V)H_{\phi'}(V) \frac{(C_\omega^{1s} - C_{\phi'}^{1s})}{(C_\omega^{1s} - C_\phi^{1s})} - L_\omega(V)L_\phi(V) \right] (f_{\phi'\Lambda\Lambda}^{(1)} / f_{\phi'}) +$$

HYPERONS EM STRUCTURE MODEL

$$\begin{aligned} & + \left(\frac{1 - V^2}{1 - V_\Lambda^2} \right)^4 \left[L_\phi(V) H_{\omega''}(V) \frac{(C_\phi^{1s} - C_{\omega''}^{1s})}{(C_\phi^{1s} - C_\omega^{1s})} + L_\omega(V) H_{\omega''}(V) \frac{(C_\omega^{1s} - C_{\omega''}^{1s})}{(C_\omega^{1s} - C_\phi^{1s})} - \right. \\ & \quad \left. - L_\omega(V) L_\phi(V) \right] (f_{\omega''\Lambda\Lambda}^{(1)} / f_{\omega''}) + \\ & + \left(\frac{1 - V^2}{1 - V_\Lambda^2} \right)^4 \left[L_\phi(V) H_{\phi''}(V) \frac{(C_\phi^{1s} - C_{\phi''}^{1s})}{(C_\phi^{1s} - C_\omega^{1s})} + L_\omega(V) H_{\phi''}(V) \frac{(C_\omega^{1s} - C_{\phi''}^{1s})}{(C_\omega^{1s} - C_\phi^{1s})} - \right. \\ & \quad \left. - L_\omega(V) L_\phi(V) \right] (f_{\phi''\Lambda\Lambda}^{(1)} / f_{\phi''}) \end{aligned}$$

HYPERONS EM STRUCTURE MODEL

$$\begin{aligned}
 F_{2s}^\Lambda[U(t)] = & \left(\frac{1 - U^2}{1 - U_\Lambda^2} \right)^6 \mu_\Lambda L_\omega(U) L_\phi(U) L_{\omega'}(U) + \\
 & + \left(\frac{1 - U^2}{1 - U_N^2} \right)^6 \left[L_\phi(U) L_{\omega'}(U) H_{\phi'}(U) \frac{(C_\phi^{2s} - C_{\phi'}^{2s})(C_{\omega'}^{2s} - C_{\phi'}^{2s})}{(C_\phi^{2s} - C_\omega^{2s})(C_{\omega'}^{2s} - C_\omega^{2s})} + \right. \\
 & + L_\omega(U) L_{\omega'}(U) H_{\phi'}(U) \frac{(C_\omega^{2s} - C_{\phi'}^{2s})(C_{\omega'}^{2s} - C_{\phi'}^{2s})}{(C_\omega^{2s} - C_\phi^{2s})(C_{\omega'}^{2s} - C_\phi^{2s})} + \\
 & + L_\omega(U) L_\phi(U) H_{\phi'}(U) \frac{(C_\omega^{2s} - C_{\phi'}^{2s})(C_\phi^{2s} - C_{\phi'}^{2s})}{(C_\omega^{2s} - C_{\omega'}^{2s})(C_\phi^{2s} - C_{\omega'}^{2s})} - \\
 & \left. - L_\omega(U) L_\phi(U) L_{\omega'}(U) \right] \left(f_{\phi' \Lambda \Lambda}^{(2)} / f_{\phi'} \right) +
 \end{aligned}$$

HYPERONS EM STRUCTURE MODEL

$$\begin{aligned}
 & + \left(\frac{1 - U^2}{1 - U_\Lambda^2} \right)^6 \left[L_\phi(U) L_{\omega'}(U) H_{\omega''}(U) \frac{(C_\phi^{2s} - C_{\omega''}^{2s})(C_{\omega'}^{2s} - C_{\omega''}^{2s})}{(C_\phi^{2s} - C_\omega^{2s})(C_{\omega'}^{2s} - C_\omega^{2s})} + \right. \\
 & + L_\omega(U) L_{\omega'}(U) H_{\omega''}(U) \frac{(C_\omega^{2s} - C_{\omega''}^{2s})(C_{\omega'}^{2s} - C_{\omega''}^{2s})}{(C_\omega^{2s} - C_\phi^{2s})(C_{\omega'}^{2s} - C_\phi^{2s})} + \\
 & + L_\omega(U) L_\phi(U) H_{\omega''}(U) \frac{(C_\omega^{2s} - C_{\omega''}^{2s})(C_\phi^{2s} - C_{\omega''}^{2s})}{(C_\omega^{2s} - C_{\omega'}^{2s})(C_\phi^{2s} - C_{\omega'}^{2s})} - \\
 & \left. - L_\omega(U) L_\phi(U) L_{\omega'}(U) \right] \left(f_{\omega''\Lambda\Lambda}^{(2)} / f_{\omega''} \right) +
 \end{aligned}$$

HYPERONS EM STRUCTURE MODEL

$$\begin{aligned} & + \left(\frac{1 - U^2}{1 - U_\Lambda^2} \right)^6 \left[L_\phi(U) L_{\omega'}(U) H_{\phi''}(U) \frac{(C_\phi^{2s} - C_{\phi''}^{2s})(C_{\omega'}^{2s} - C_{\phi''}^{2s})}{(C_\phi^{2s} - C_\omega^{2s})(C_{\omega'}^{2s} - C_\omega^{2s})} + \right. \\ & \quad + L_\omega(U) L_{\omega'}(U) H_{\phi''}(U) \frac{(C_\omega^{2s} - C_{\phi''}^{2s})(C_{\omega'}^{2s} - C_{\phi''}^{2s})}{(C_\omega^{2s} - C_\phi^{2s})(C_{\omega'}^{2s} - C_\phi^{2s})} + \\ & \quad + L_\omega(U) L_\phi(U) H_{\phi''}(U) \frac{(C_\omega^{2s} - C_{\phi''}^{2s})(C_\phi^{2s} - C_{\phi''}^{2s})}{(C_\omega^{2s} - C_{\omega'}^{2s})(C_\phi^{2s} - C_{\omega'}^{2s})} - \\ & \quad \left. - L_\omega(U) L_\phi(U) L_{\omega'}(U) \right] (f_{\phi''\Lambda}^{(2)} / f_{\phi''}) \end{aligned}$$

HYPERONS EM STRUCTURE MODEL

$$F_{1s}^{\Sigma}[V(t)] = \left(\frac{1-V^2}{1-V_{\Sigma}^2}\right)^4 \left[L_{\phi}(V)L_{\omega'}(V) \frac{(C_{\phi}^{1s} - C_{\omega'}^{1s})}{(C_{\phi}^{1s} - C_{\omega}^{1s})} + L_{\omega}(V)L_{\omega'}(V) \frac{(C_{\omega}^{1s} - C_{\omega'}^{1s})}{(C_{\omega}^{1s} - C_{\phi}^{1s})} - L_{\omega}(V)L_{\phi}(V) \right] (f_{\omega' \Sigma\Sigma}^{(1)} / f_{\omega'}) +$$
$$+ \left(\frac{1-V^2}{1-V_{\Sigma}^2}\right)^4 \left[L_{\phi}(V)H_{\phi'}(V) \frac{(C_{\phi}^{1s} - C_{\phi'}^{1s})}{(C_{\phi}^{1s} - C_{\omega}^{1s})} + L_{\omega}(V)H_{\phi'}(V) \frac{(C_{\omega}^{1s} - C_{\phi'}^{1s})}{(C_{\omega}^{1s} - C_{\phi}^{1s})} - L_{\omega}(V)L_{\phi}(V) \right] (f_{\phi' \Sigma\Sigma}^{(1)} / f_{\phi'}) +$$

HYPERONS EM STRUCTURE MODEL

$$\begin{aligned} & + \left(\frac{1 - V^2}{1 - V_\Sigma^2} \right)^4 \left[L_\phi(V) H_{\omega''}(V) \frac{(C_\phi^{1s} - C_{\omega''}^{1s})}{(C_\phi^{1s} - C_\omega^{1s})} + L_\omega(V) H_{\omega''}(V) \frac{(C_\omega^{1s} - C_{\omega''}^{1s})}{(C_\omega^{1s} - C_\phi^{1s})} - \right. \\ & \quad \left. - L_\omega(V) L_\phi(V) \right] (f_{\omega''\Sigma\Sigma}^{(1)} / f_{\omega''}) + \\ & + \left(\frac{1 - V^2}{1 - V_\Sigma^2} \right)^4 \left[L_\phi(V) H_{\phi''}(V) \frac{(C_\phi^{1s} - C_{\phi''}^{1s})}{(C_\phi^{1s} - C_\omega^{1s})} + L_\omega(V) H_{\phi''}(V) \frac{(C_\omega^{1s} - C_{\phi''}^{1s})}{(C_\omega^{1s} - C_\phi^{1s})} - \right. \\ & \quad \left. - L_\omega(V) L_\phi(V) \right] (f_{\phi''\Sigma\Sigma}^{(1)} / f_{\phi''}) \end{aligned}$$

HYPERONS EM STRUCTURE MODEL

$$F_{1\nu}^{\Sigma}[W(t)] = \left(\frac{1 - W^2}{1 - W_{\Sigma}^2} \right)^4 \left\{ L_{\rho}(W)L_{\rho'}(W) + \right. \\ \left. + \left[L_{\rho'}(W)H_{\rho''}(W) \frac{(C_{\rho'}^{1\nu} - C_{\rho''}^{1\nu})}{(C_{\rho'}^{1\nu} - C_{\rho}^{1\nu})} + L_{\rho}(W)H_{\rho''}(W) \frac{(C_{\rho}^{1\nu} - C_{\rho''}^{1\nu})}{(C_{\rho}^{1\nu} - C_{\rho'}^{1\nu})} - \right. \right. \\ \left. \left. - L_{\rho}(W)L_{\rho'}(W) \right] (f_{\rho''\Sigma\Sigma}^{(1)} / f_{\rho''}) \right\}$$

HYPERONS EM STRUCTURE MODEL

$$\begin{aligned}
 F_{2s}^\Sigma[U(t)] = & \left(\frac{1 - U^2}{1 - U_\Sigma^2} \right)^6 \frac{1}{2} (\mu_{\Sigma^+} + \mu_{\Sigma^-}) L_\omega(U) L_\phi(U) L_{\omega'}(U) + \\
 & + \left(\frac{1 - U^2}{1 - U_N^2} \right)^6 \left[L_\phi(U) L_{\omega'}(U) H_{\phi'}(U) \frac{(C_\phi^{2s} - C_{\phi'}^{2s})(C_{\omega'}^{2s} - C_{\phi'}^{2s})}{(C_\phi^{2s} - C_\omega^{2s})(C_{\omega'}^{2s} - C_\omega^{2s})} + \right. \\
 & + L_\omega(U) L_{\omega'}(U) H_{\phi'}(U) \frac{(C_\omega^{2s} - C_{\phi'}^{2s})(C_{\omega'}^{2s} - C_{\phi'}^{2s})}{(C_\omega^{2s} - C_{\phi'}^{2s})(C_{\omega'}^{2s} - C_\phi^{2s})} + \\
 & + L_\omega(U) L_\phi(U) H_{\phi'}(U) \frac{(C_\omega^{2s} - C_{\phi'}^{2s})(C_\phi^{2s} - C_{\phi'}^{2s})}{(C_\omega^{2s} - C_{\omega'}^{2s})(C_\phi^{2s} - C_{\omega'}^{2s})} - \\
 & \left. - L_\omega(U) L_\phi(U) L_{\omega'}(U) \right] (f_{\phi' \Sigma \Sigma}^{(2)} / f_{\phi'}) +
 \end{aligned}$$

HYPERONS EM STRUCTURE MODEL

$$\begin{aligned}
 & + \left(\frac{1 - U^2}{1 - U_{\Sigma}^2} \right)^6 \left[L_{\phi}(U) L_{\omega'}(U) H_{\omega''}(U) \frac{(C_{\phi}^{2s} - C_{\omega''}^{2s})(C_{\omega'}^{2s} - C_{\omega''}^{2s})}{(C_{\phi}^{2s} - C_{\omega}^{2s})(C_{\omega'}^{2s} - C_{\omega}^{2s})} + \right. \\
 & + L_{\omega}(U) L_{\omega'}(U) H_{\omega''}(U) \frac{(C_{\omega}^{2s} - C_{\omega''}^{2s})(C_{\omega'}^{2s} - C_{\omega''}^{2s})}{(C_{\omega}^{2s} - C_{\omega'}^{2s})(C_{\omega'}^{2s} - C_{\phi}^{2s})} + \\
 & + L_{\omega}(U) L_{\phi}(U) H_{\omega''}(U) \frac{(C_{\omega}^{2s} - C_{\omega''}^{2s})(C_{\phi}^{2s} - C_{\omega''}^{2s})}{(C_{\omega}^{2s} - C_{\omega'}^{2s})(C_{\phi}^{2s} - C_{\omega'}^{2s})} - \\
 & \left. - L_{\omega}(U) L_{\phi}(U) L_{\omega'}(U) \right] \left(f_{\omega''/\Sigma\Sigma}^{(2)} / f_{\omega''} \right) +
 \end{aligned}$$

HYPERONS EM STRUCTURE MODEL

$$\begin{aligned} & + \left(\frac{1 - U^2}{1 - U_\Sigma^2} \right)^6 \left[L_\phi(U) L_{\omega'}(U) H_{\phi''}(U) \frac{(C_\phi^{2s} - C_{\phi''}^{2s})(C_{\omega'}^{2s} - C_{\phi''}^{2s})}{(C_\phi^{2s} - C_\omega^{2s})(C_{\omega'}^{2s} - C_\omega^{2s})} + \right. \\ & \quad + L_\omega(U) L_{\omega'}(U) H_{\phi''}(U) \frac{(C_\omega^{2s} - C_{\phi''}^{2s})(C_{\omega'}^{2s} - C_{\phi''}^{2s})}{(C_\omega^{2s} - C_\phi^{2s})(C_{\omega'}^{2s} - C_\phi^{2s})} + \\ & \quad + L_\omega(U) L_\phi(U) H_{\phi''}(U) \frac{(C_\omega^{2s} - C_{\phi''}^{2s})(C_\phi^{2s} - C_{\phi''}^{2s})}{(C_\omega^{2s} - C_{\omega'}^{2s})(C_\phi^{2s} - C_{\omega'}^{2s})} - \\ & \quad \left. - L_\omega(U) L_\phi(U) L_{\omega'}(U) \right] (f_{\phi''/\Sigma\Sigma}^{(2)} / f_{\phi''}) \end{aligned}$$

HYPERONS EM STRUCTURE MODEL

$$F_{2v}^\Sigma[X(t)] = \left(\frac{1-X^2}{1-X_\Sigma^2}\right)^6 \left\{ \frac{1}{2}(\mu_{\Sigma^+} - \mu_{\Sigma^-} - 2)L_\rho(U)L_{\rho'}(U)H_{\rho''}(U) \right\}$$

HYPERONS EM STRUCTURE MODEL

$$\begin{aligned}
 F_{1s}^{\Xi}[V(t)] = & -\left(\frac{1-V^2}{1-V_{\Xi}^2}\right)^4 \frac{1}{2} L_{\omega}(V)L_{\phi}(V) + \\
 & + \left(\frac{1-V^2}{1-V_{\Xi}^2}\right)^4 \left[L_{\phi}(V)L_{\omega'}(V) \frac{(C_{\phi}^{1s} - C_{\omega'}^{1s})}{(C_{\phi}^{1s} - C_{\omega}^{1s})} + L_{\omega}(V)L_{\omega'}(V) \frac{(C_{\omega}^{1s} - C_{\omega'}^{1s})}{(C_{\omega}^{1s} - C_{\phi}^{1s})} - \right. \\
 & \quad \left. - L_{\omega}(V)L_{\phi}(V) \right] (f_{\omega' \Xi \Xi}^{(1)} / f_{\omega'}) + \\
 & + \left(\frac{1-V^2}{1-V_{\Xi}^2}\right)^4 \left[L_{\phi}(V)H_{\phi'}(V) \frac{(C_{\phi}^{1s} - C_{\phi'}^{1s})}{(C_{\phi}^{1s} - C_{\omega}^{1s})} + L_{\omega}(V)H_{\phi'}(V) \frac{(C_{\omega}^{1s} - C_{\phi'}^{1s})}{(C_{\omega}^{1s} - C_{\phi}^{1s})} - \right. \\
 & \quad \left. - L_{\omega}(V)L_{\phi}(V) \right] (f_{\phi' \Xi \Xi}^{(1)} / f_{\phi'}) +
 \end{aligned}$$

HYPERONS EM STRUCTURE MODEL

$$\begin{aligned} & + \left(\frac{1 - V^2}{1 - V_{\Xi}^2} \right)^4 \left[L_{\phi}(V) H_{\omega''}(V) \frac{(C_{\phi}^{1s} - C_{\omega''}^{1s})}{(C_{\phi}^{1s} - C_{\omega}^{1s})} + L_{\omega}(V) H_{\omega''}(V) \frac{(C_{\omega}^{1s} - C_{\omega''}^{1s})}{(C_{\omega}^{1s} - C_{\phi}^{1s})} - \right. \\ & \quad \left. - L_{\omega}(V) L_{\phi}(V) \right] (f_{\omega''/\Xi\Xi}^{(1)} / f_{\omega''}) + \\ & + \left(\frac{1 - V^2}{1 - V_{\Xi}^2} \right)^4 \left[L_{\phi}(V) H_{\phi''}(V) \frac{(C_{\phi}^{1s} - C_{\phi''}^{1s})}{(C_{\phi}^{1s} - C_{\omega}^{1s})} + L_{\omega}(V) H_{\phi''}(V) \frac{(C_{\omega}^{1s} - C_{\phi''}^{1s})}{(C_{\omega}^{1s} - C_{\phi}^{1s})} - \right. \\ & \quad \left. - L_{\omega}(V) L_{\phi}(V) \right] (f_{\phi''/\Xi\Xi}^{(1)} / f_{\phi''}) \end{aligned}$$

HYPERONS EM STRUCTURE MODEL

$$F_{1\nu}^{\Xi}[W(t)] = \left(\frac{1 - W^2}{1 - W_{\Xi}^2} \right)^4 \left\{ \frac{1}{2} L_{\rho}(W) L_{\rho'}(W) + \right.$$
$$+ \left[L_{\rho'}(W) H_{\rho''}(W) \frac{(C_{\rho'}^{1\nu} - C_{\rho''}^{1\nu})}{(C_{\rho'}^{1\nu} - C_{\rho}^{1\nu})} + L_{\rho}(W) H_{\rho''}(W) \frac{(C_{\rho}^{1\nu} - C_{\rho''}^{1\nu})}{(C_{\rho}^{1\nu} - C_{\rho'}^{1\nu})} - \right.$$
$$\left. \left. - L_{\rho}(W) L_{\rho'}(W) \right] (f_{\rho''\Xi\Xi}^{(1)} / f_{\rho''}) \right\}$$

HYPERONS EM STRUCTURE MODEL

$$\begin{aligned}
 F_{2s}^{\Xi}[U(t)] = & \left(\frac{1 - U^2}{1 - U_{\Xi}^2} \right)^6 \frac{1}{2} (\mu_{\Xi^0} + \mu_{\Xi^-} + 1) L_{\omega}(U) L_{\phi}(U) L_{\omega'}(U) + \\
 & + \left(\frac{1 - U^2}{1 - U_N^2} \right)^6 \left[L_{\phi}(U) L_{\omega'}(U) H_{\phi'}(U) \frac{(C_{\phi}^{2s} - C_{\phi'}^{2s})(C_{\omega'}^{2s} - C_{\phi'}^{2s})}{(C_{\phi}^{2s} - C_{\omega}^{2s})(C_{\omega'}^{2s} - C_{\omega}^{2s})} + \right. \\
 & + L_{\omega}(U) L_{\omega'}(U) H_{\phi'}(U) \frac{(C_{\omega}^{2s} - C_{\phi'}^{2s})(C_{\omega'}^{2s} - C_{\phi'}^{2s})}{(C_{\omega}^{2s} - C_{\phi}^{2s})(C_{\omega'}^{2s} - C_{\phi}^{2s})} + \\
 & + L_{\omega}(U) L_{\phi}(U) H_{\phi'}(U) \frac{(C_{\omega}^{2s} - C_{\phi'}^{2s})(C_{\phi}^{2s} - C_{\phi'}^{2s})}{(C_{\omega}^{2s} - C_{\omega'}^{2s})(C_{\phi}^{2s} - C_{\omega'}^{2s})} - \\
 & \left. - L_{\omega}(U) L_{\phi}(U) L_{\omega'}(U) \right] (f_{\phi' \Xi \Xi}^{(2)} / f_{\phi'}) +
 \end{aligned}$$

HYPERONS EM STRUCTURE MODEL

$$\begin{aligned} & + \left(\frac{1 - U^2}{1 - U_{\Xi}^2} \right)^6 \left[L_{\phi}(U) L_{\omega'}(U) H_{\omega''}(U) \frac{(C_{\phi}^{2s} - C_{\omega''}^{2s})(C_{\omega'}^{2s} - C_{\omega''}^{2s})}{(C_{\phi}^{2s} - C_{\omega}^{2s})(C_{\omega'}^{2s} - C_{\omega}^{2s})} + \right. \\ & + L_{\omega}(U) L_{\omega'}(U) H_{\omega''}(U) \frac{(C_{\omega}^{2s} - C_{\omega''}^{2s})(C_{\omega'}^{2s} - C_{\omega''}^{2s})}{(C_{\omega}^{2s} - C_{\omega'}^{2s})(C_{\omega'}^{2s} - C_{\phi}^{2s})} + \\ & + L_{\omega}(U) L_{\phi}(U) H_{\omega''}(U) \frac{(C_{\omega}^{2s} - C_{\omega''}^{2s})(C_{\phi}^{2s} - C_{\omega''}^{2s})}{(C_{\omega}^{2s} - C_{\omega'}^{2s})(C_{\phi}^{2s} - C_{\omega'}^{2s})} - \\ & \left. - L_{\omega}(U) L_{\phi}(U) L_{\omega'}(U) \right] (f_{\omega''\Xi\Xi}^{(2)} / f_{\omega''}) + \end{aligned}$$

HYPERONS EM STRUCTURE MODEL

$$\begin{aligned}
 & + \left(\frac{1 - U^2}{1 - U_{\Xi}^2} \right)^6 \left[L_\phi(U) L_{\omega'}(U) H_{\phi''}(U) \frac{(C_\phi^{2s} - C_{\phi''}^{2s})(C_{\omega'}^{2s} - C_{\phi''}^{2s})}{(C_\phi^{2s} - C_\omega^{2s})(C_{\omega'}^{2s} - C_\omega^{2s})} + \right. \\
 & \quad + L_\omega(U) L_{\omega'}(U) H_{\phi''}(U) \frac{(C_\omega^{2s} - C_{\phi''}^{2s})(C_{\omega'}^{2s} - C_{\phi''}^{2s})}{(C_\omega^{2s} - C_\phi^{2s})(C_{\omega'}^{2s} - C_\phi^{2s})} + \\
 & \quad + L_\omega(U) L_\phi(U) H_{\phi''}(U) \frac{(C_\omega^{2s} - C_{\phi''}^{2s})(C_\phi^{2s} - C_{\phi''}^{2s})}{(C_\omega^{2s} - C_{\omega'}^{2s})(C_\phi^{2s} - C_{\omega'}^{2s})} - \\
 & \quad \left. - L_\omega(U) L_\phi(U) L_{\omega'}(U) \right] (f_{\phi''/\Xi\Xi}^{(2)} / f_{\phi''})
 \end{aligned}$$

HYPERONS EM STRUCTURE MODEL

$$F_{2\nu}^{\Xi}[X(t)] = \left(\frac{1-X^2}{1-X_{\Xi}^2}\right)^6 \left\{ \frac{1}{2}(\mu_{\Xi^0} - \mu_{\Xi^-} - 1)L_{\rho}(U)L_{\rho'}(U)H_{\rho''}(U) \right\}$$

HYPERONS EM STRUCTURE MODEL

But this hyperon EM structure model contains the
vector-meson-hyperon coupling constant ratios

$$F_{1s}^h : (f_{\omega'hh}^{(1)} / f_{\omega'}), (f_{\phi'hh}^{(1)} / f_{\phi'}), (f_{\omega''hh}^{(1)} / f_{\omega''}), (f_{\phi''hh}^{(1)} / f_{\phi''})$$

$$F_{1v}^h : (f_{\rho''hh}^{(1)} / f_{\rho''})$$

$$F_{2s}^h : (f_{\phi'hh}^{(2)} / f_{\phi'}), (f_{\omega''hh}^{(2)} / f_{\omega''}), (f_{\phi''hh}^{(2)} / f_{\phi''})$$

$$F_{2v}^h : 0$$

as **free parameters**. Again coupling constants $(f_{\omega hh}^{(1)} / f_{\omega}), (f_{\phi hh}^{(1)} / f_{\phi}),$
 $(f_{\rho hh}^{(1)} / f_{\rho}), (f_{\rho' hh}^{(1)} / f_{\rho'}), (f_{\omega hh}^{(2)} / f_{\omega}), (f_{\phi hh}^{(2)} / f_{\phi}), (f_{\omega' hh}^{(2)} / f_{\omega'}), (f_{\rho hh}^{(2)} / f_{\rho}),$
 $(f_{\rho' hh}^{(2)} / f_{\rho'}), (f_{\rho'' hh}^{(2)} / f_{\rho''})$, are absent among these free parameters,
because they have been **expressed through vector meson masses**.

HYPERONS EM STRUCTURE MODEL

These free parameters, in principle, could be determined by a comparison of the model with some data on the hyperon EM FFs, like in the case of nucleons.

However, **there are no such data**, except two experiments with elastic scattering of Σ^- hyperons on atomic electrons for very small momentum transfer squared values in the space-like region **giving just the value of the corresponding charge mean square radius of the Σ^- hyperon** and few experimental points **on the total cross section of electron-positron annihilation into HYPERON-ANTIHYPERON pairs.**

HYPERONS EM STRUCTURE MODEL

Nevertheless also **in such case one finds the solution.**

Unknown parameters of the hyperon EM structure model can be predicted theoretically:

- by using $SU(3)$ invariant vector-meson-baryon Lagrangian
- results from the analysis of nucleons
- provided that the **universal vector-meson coupling constants f_V in all considered coupling constants ratios are known numerically.**

HYPERONS EM STRUCTURE MODEL

The **$SU(3)$ invariant Lagrangian** of vector meson-baryon interactions

$$\begin{aligned} Tr(L_{VB\bar{B}}) = & \frac{i}{\sqrt{2}} f^F [\bar{B}_\beta^\alpha \gamma_\mu B_\gamma^\beta - \bar{B}_\gamma^\beta \gamma_\mu B_\beta^\alpha] (V_\mu)_\alpha^\gamma + \\ & \frac{i}{\sqrt{2}} f^D [\bar{B}_\gamma^\beta \gamma_\mu B_\beta^\alpha + \bar{B}_\gamma^\alpha \gamma_\mu B_\gamma^\beta] (V_\mu)_\alpha^\gamma + \\ & \frac{i}{\sqrt{2}} f^S \bar{B}_\beta^\alpha \gamma_\mu B_\alpha^\beta \omega_\mu^0 \end{aligned}$$

provides the relations

HYPERONS EM STRUCTURE MODEL

$$f_{\rho NN}^{1,2} = \frac{1}{2}(f_{1,2}^D + f_{1,2}^F)$$

$$f_{\omega NN}^{1,2} = \frac{1}{\sqrt{2}}\cos\theta f_{1,2}^S - \frac{1}{2\sqrt{3}}\sin\theta(3f_{1,2}^F - f_{1,2}^D)$$

$$f_{\phi NN}^{1,2} = \frac{1}{\sqrt{2}}\sin\theta f_{1,2}^S + \frac{1}{2\sqrt{3}}\cos\theta(3f_{1,2}^F - f_{1,2}^D)$$

where the **left hand side is known**, if we take **numerical values of the nucleon coupling constant ratios** from nucleon EM FF data analysis and the **universal vector meson coupling constants** f_ρ , f_ω , f_ϕ **from data on** $\Gamma(V \rightarrow e^+e^-)$ to be determined by the relation $\Gamma(V \rightarrow e^+e^-) = \frac{\alpha^2 m_V}{4\pi} \left(\frac{f_V^2}{4\pi}\right)^{-1}$.

HYPERONS EM STRUCTURE MODEL

The solution of the last system of algebraic equations according to $f_{1,2}^D$, $f_{1,2}^F$, $f_{1,2}^S$ with numerical values of $f_{\rho NN}^{1,2}$, $f_{\omega NN}^{1,2}$ and $f_{\phi NN}^{1,2}$, **enables to predict all following vector-meson-hyperon coupling constants**

HYPERONS EM STRUCTURE MODEL

$$f_{\omega \Lambda \Lambda}^{1,2} = \frac{1}{\sqrt{2}} \cos \theta f_{1,2}^S + \frac{1}{\sqrt{3}} \sin \theta f_{1,2}^D$$

$$f_{\phi \Lambda \Lambda}^{1,2} = \frac{1}{\sqrt{2}} \sin \theta f_{1,2}^S - \frac{1}{\sqrt{3}} \cos \theta f_{1,2}^D$$

$$f_{\rho \Sigma \Sigma}^{1,2} = -f_{1,2}^F$$

$$f_{\omega \Sigma \Sigma}^{1,2} = \frac{1}{\sqrt{2}} \cos \theta f_{1,2}^S - \frac{1}{\sqrt{3}} \sin \theta f_{1,2}^D$$

$$f_{\phi \Sigma \Sigma}^{1,2} = \frac{1}{\sqrt{2}} \sin \theta f_{1,2}^S + \frac{1}{\sqrt{3}} \cos \theta f_{1,2}^D$$

$$f_{\rho \Xi \Xi}^{1,2} = \frac{1}{2} (f_{1,2}^D - f_{1,2}^F)$$

$$f_{\omega \Xi \Xi}^{1,2} = \frac{1}{\sqrt{2}} \cos \theta f_{1,2}^S + \frac{1}{2\sqrt{3}} \sin \theta (3f_{1,2}^F + f_{1,2}^D)$$

$$f_{\phi \Xi \Xi}^{1,2} = \frac{1}{\sqrt{2}} \sin \theta f_{1,2}^S - \frac{1}{2\sqrt{3}} \cos \theta (3f_{1,2}^F + f_{1,2}^D)$$

HYPERONS EM STRUCTURE MODEL

where $\theta = 39.83^\circ$ is the **mixing angle** to be determined by the **Gell-Mann-Okubo quadratic mass formula**

$$m_\phi^2 \cos^2 \theta + m_\omega^2 \sin^2 \theta = \frac{4m_{K^*}^2 - m_\rho^2}{3}.$$

HYPERONS EM STRUCTURE MODEL

Finally, dividing the determined vector-meson-hyperon coupling constants by the corresponding universal vector-meson coupling constants f_ρ , f_ω , f_ϕ , **one finds searched vector-meson-hyperon coupling constant ratios.**

Similarly one can proceed in a **determination of the first excited and the second excited vector-meson-hyperon coupling constants ratios.**

Here **big problem appeared**. There are no data on $\Gamma(V \rightarrow e^+e^-)$ for $\omega'(1420)$, $\rho'(1450)$), $\phi'(1680)$ and $\omega''(1650)$, $\rho''(1700)$, $\phi''(2170)$, in order to determine f'_ρ , f'_ω , f'_ϕ and f''_ρ , f''_ω , f''_ϕ .

HYPERONS EM STRUCTURE MODEL

In order to avoid this problem to some extent, we have constructed the *U&A* model with explicit coupling constants ratios

$(f_{\omega hh}^{(1,2)} / f_\omega), (f_{\phi hh}^{(1,2)} / f_\phi), (f_{\rho hh}^{(1)} / f_\rho)$, where we know numerical values of f_ρ , f_ω , f_ϕ and $(f_{\omega' hh}^{(1,2)} / f_{\omega'}), (f_{\phi' hh}^{(1,2)} / f_{\phi'})$, where one can find f'_ω , f'_ϕ by exploiting some model considerations.

The results are in progress.

As a first approximation, we have calculated at least 1/2⁺ octet baryon mean square charge radii in the framework of the **hyperon EM structure *U&A* model** to be compared with χPT predictions and existing experimental determinations (see Table).

HYPERONS EM STRUCTURE MODEL

baryon	<i>U&A model</i>	χ PT	Exp.
p	0.727	0.717	0.769
n	-.205	-.113	-.116
Λ	-.068	-.112	
Σ^+	1.090	0.602	
Σ^0	-.093	-.031	
Σ^-	0.536	0.673	0.915
Ξ^0	-.221	0.133	
Ξ^-	0.876	0.495	

Conclusions

- All existing data on the proton and neutron electric and magnetic FFs, $G_E^P(t)$, $G_M^P(t)$ and $G_E^n(t)$, $G_M^n(t)$, have been reviewed.
- The advanced *U&A nucleon EM structure model*, which successfully describes all today's experimental data in space-like and time-like regions simultaneously, was elaborated.
- The results of the *U&A nucleon EM structure model with a combination of SU(3) symmetry* have been used for a construction of the *U&A EM structure model of the 1/2⁺ octet hyperons*.
- By means of the latter the **charge mean square radii of 1/2⁺ octet hyperons** have been calculated and compared with χ PT predictions.

Thank you