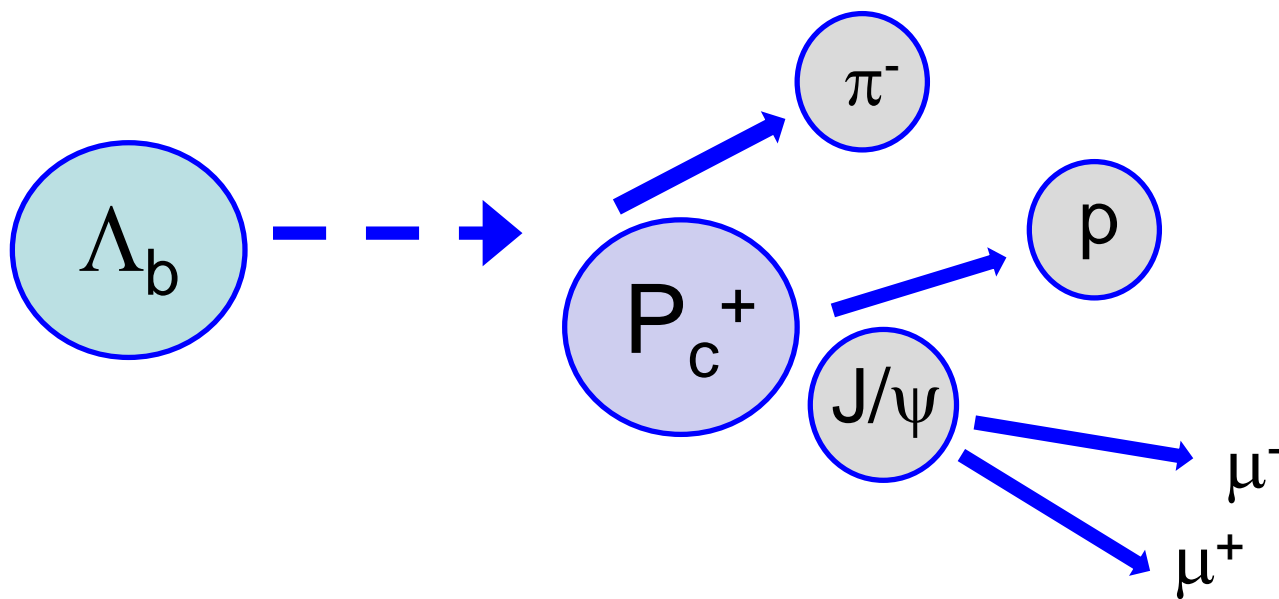


Exotic Hadron Spectroscopy at LHCb: Candidates for Tetra- and Pentaquark States



Ulrich Uwer
Heidelberg University
On behalf of the LHCb Collaboration

Supported by



Bundesministerium
für Bildung
und Forschung

Multi-Quark States in Quark Model

A SCHEMATIC MODEL OF BARYONS AND MESONS *

M. GELL-MANN

California Institute of Technology, Pasadena, California

Received 4 January 1964



AN SU_3 MODEL FOR STRONG INTERACTION SYMMETRY AND ITS BREAKING

8182/TH. 401

17 January 1964

G. Zweig *)

CERN - Geneva



Both papers mentioned explicitly the possibility for tetra and penta-quark states: $qq\bar{q}\bar{q}$, $qqqq\bar{q}$

Multiquark states would be short-lived $\sim 10^{-23}$ s “resonances” whose presences are detected by mass peaks & angular distributions showing unique J^{PC} .

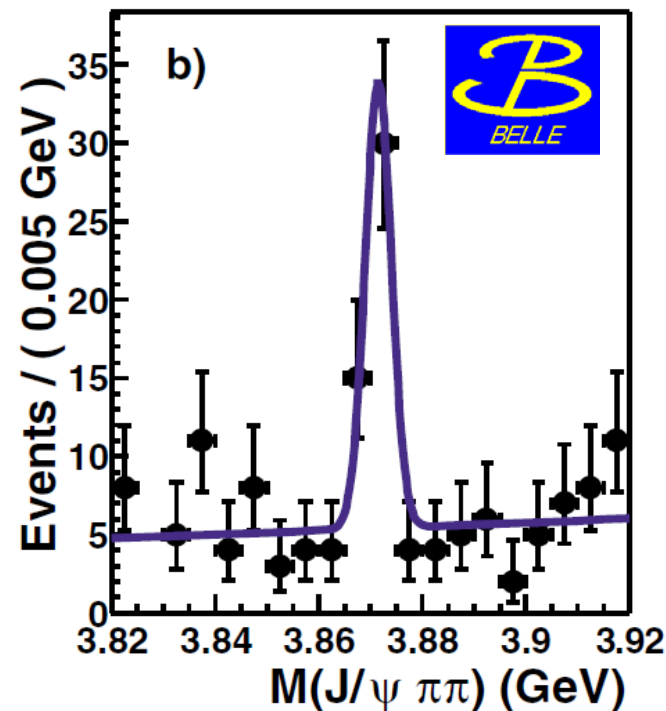
Searches for such states made from light quarks (u,d,s) are ~ 50 years old, but no undisputed experimental evidence has been found.

Discovery of X(3872)

Belle 2003, *Phys. Rev. Lett.* 91, 262001

$$B^{\pm} \rightarrow K^{\pm} \underbrace{J/\psi \pi^+ \pi^-}_{\text{X(3872)}} \Rightarrow$$

- Very narrow resonance ($\Gamma < 1.2$ MeV) close to $D^0 \bar{D}^{0*}$ threshold.
- Nature unclear: conventional charmonium state, exotic state ($D^0 \bar{D}^{0*}$ molecule, tetraquark), or a mixture
- Determination of J^{PC} important



PRL 110, 222001 (2013).

$B^+ \rightarrow X(3872) K^+$ w/ $X(3872) \rightarrow J/\psi \pi \pi$
 $\rightarrow J^{PC} = 1^{++}$, $J^{PC} = 2^{-+}$ rejected w/ $> 8\sigma$
 (analysis assumed lowest possible L)

PR D 92, 011102 (2015).

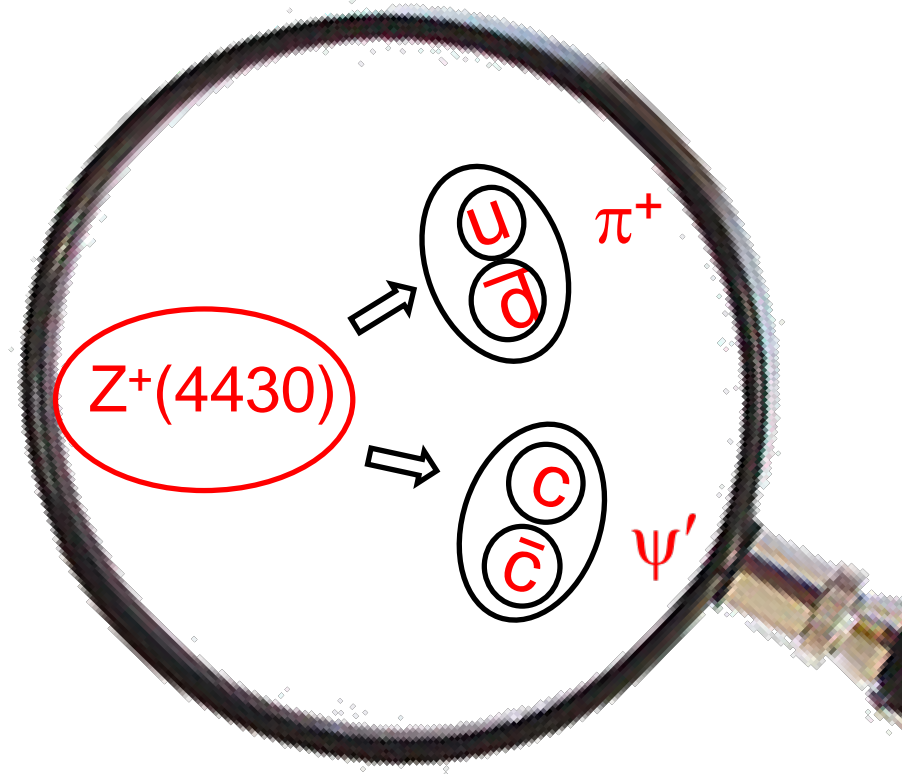
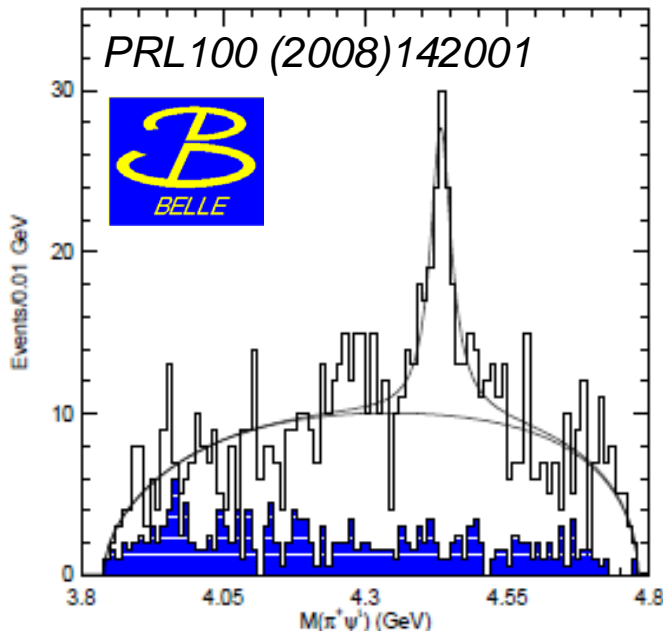
Update: w/o assumption on L
 Confirms $J^{PC} = 1^{++}$



Tetra-Quark Candidate

$$B \rightarrow \psi' \pi^+ K$$

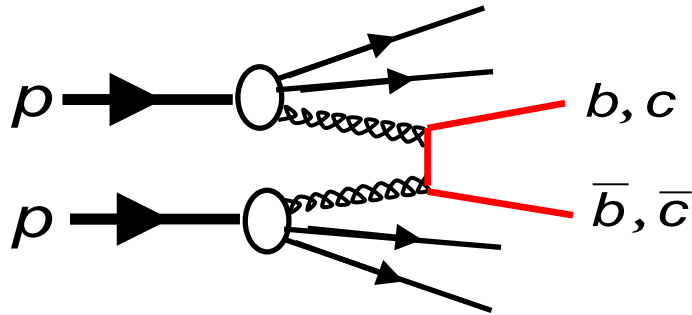
↓



Smoking gun for 4-quark effect. Confirmed only recently by LHCb.
LHCb also provides evidence for the resonant character – see later.

Supports the possibility for existence of pentaquark state.

LHCb-Experiment

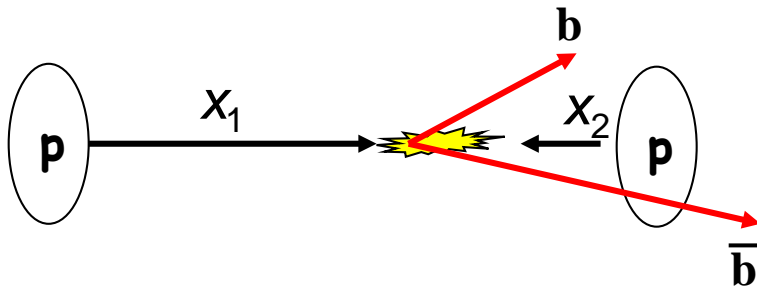


Run 2011-2012: 3 fb^{-1} (LHCb)

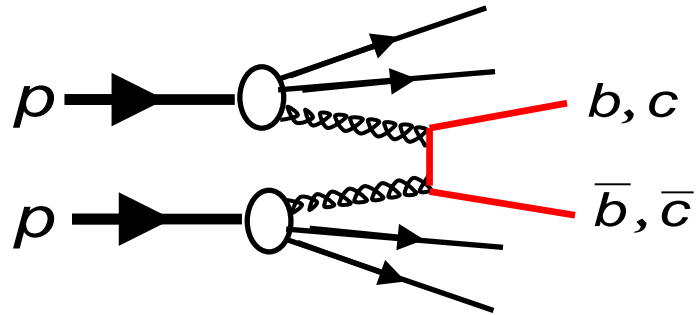
$200 \text{ kHz } b\bar{b} \rightarrow 2.6 \times 10^{11} b\bar{b}$

$4 \text{ MHz } c\bar{c} \rightarrow 5.9 \times 10^{12} c\bar{c}$

$\times O(5000)$ rates of B-factories.
Smaller background.



LHCb-Experiment

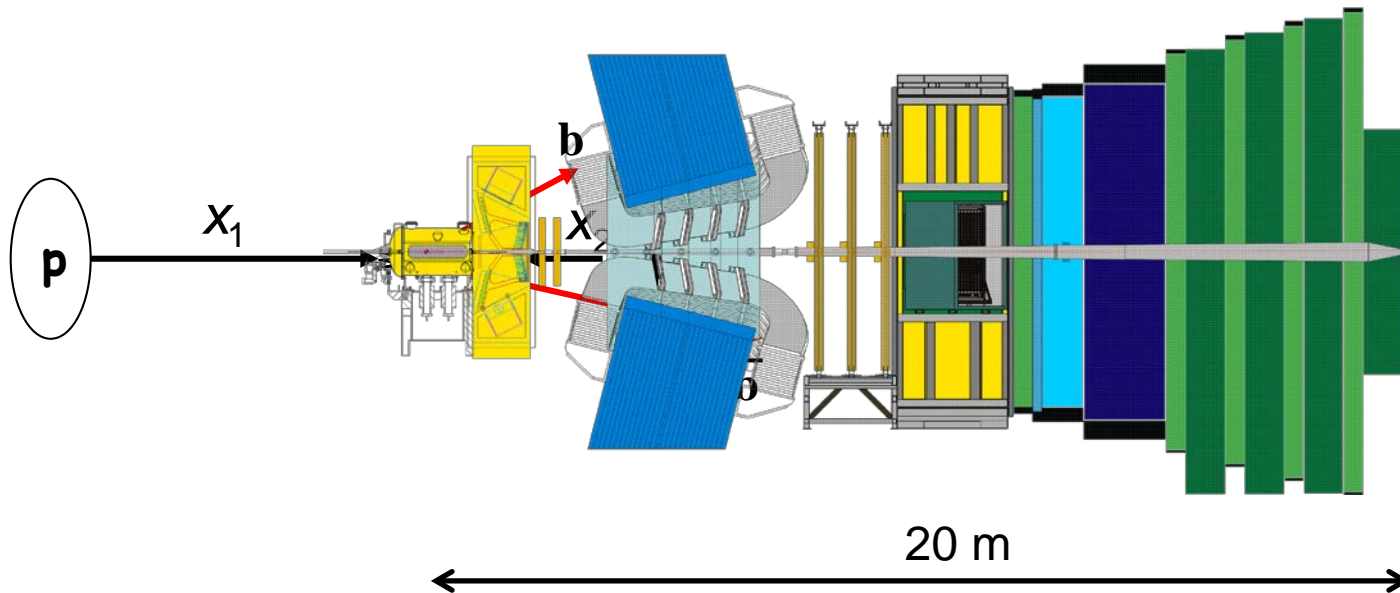


Run 2011-2012: 3 fb^{-1} (LHCb)

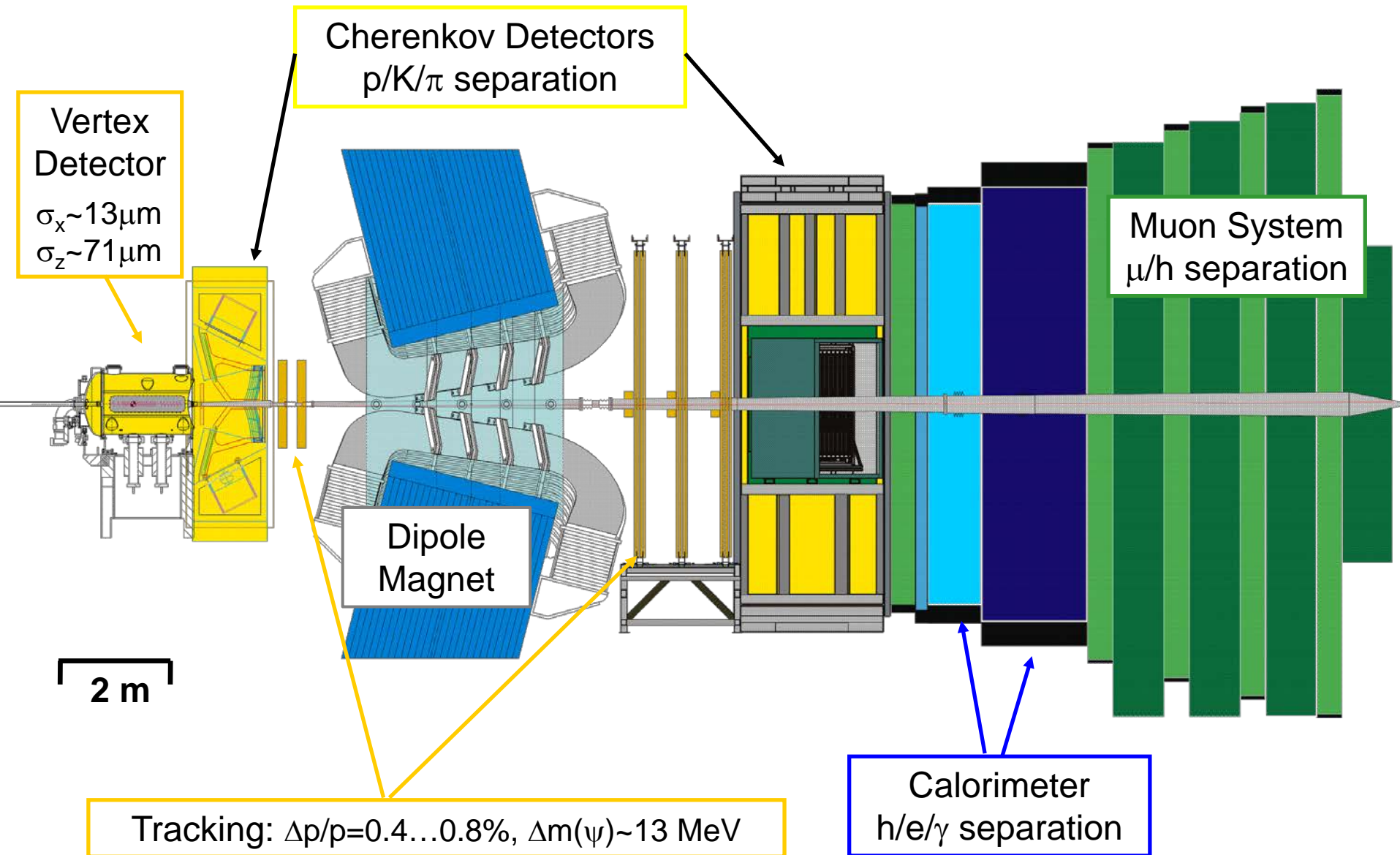
$200 \text{ kHz } b\bar{b} \rightarrow 2.6 \times 10^{11} b\bar{b}$

$4 \text{ MHz } c\bar{c} \rightarrow 5.9 \times 10^{12} c\bar{c}$

$\times O(5000)$ rates of B-factories.
Smaller background.

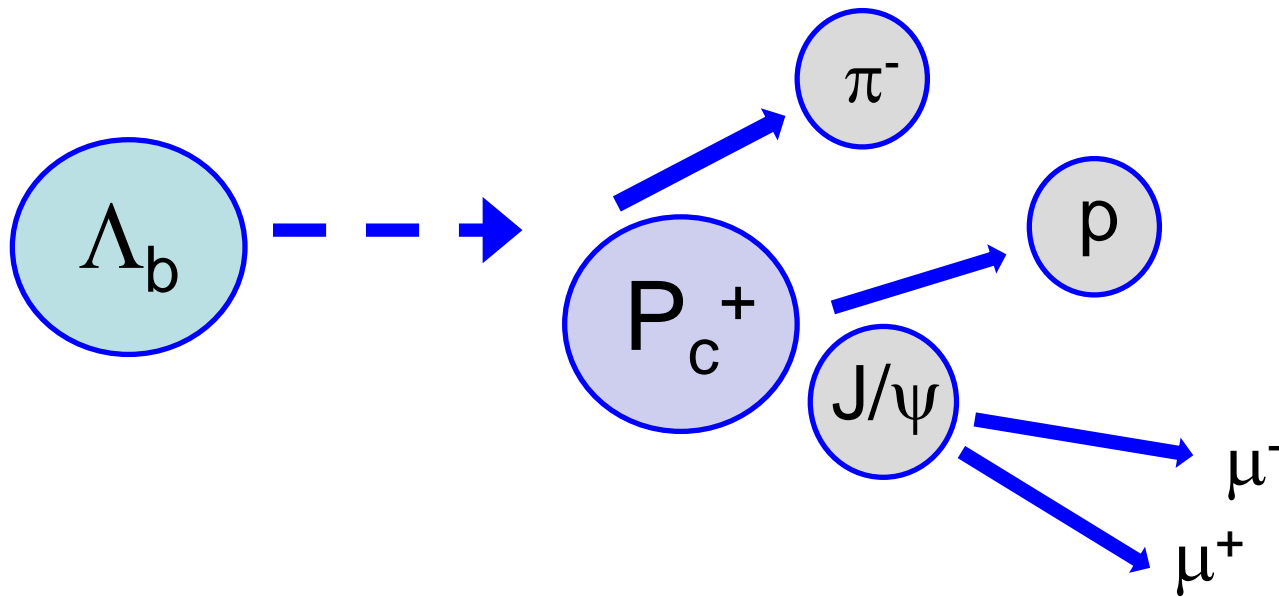


LHCb Detector



Observation of J/ψ resonances consistent with pentaquark states

PRL 115, 07201, arXiv:1507.03414

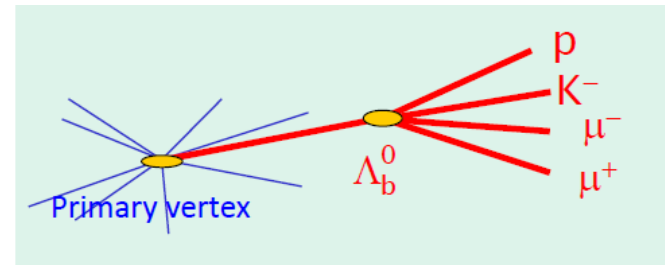


$\Lambda_b^0 \rightarrow J/\psi \, p \, K^-$ data sample

$\Lambda_b^0 \rightarrow J/\psi \, p \, K^-$ first observed by LHCb; used for Λ_b^0 lifetime.

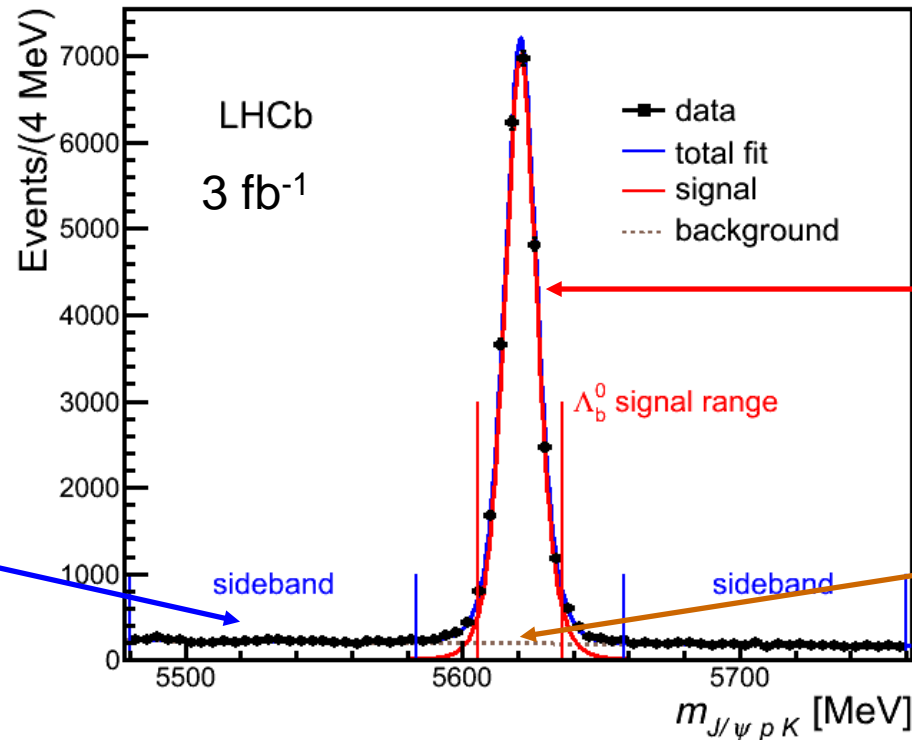
$$\mathcal{B} = (3.04 \pm 0.04^{+0.55}_{-0.43}) \times 10^{-4}$$

arXiv:1509.00292



PRL 115, 07201, arXiv:1507.03414

Flat sidebands
→ no major
reflections from
other b-hadrons



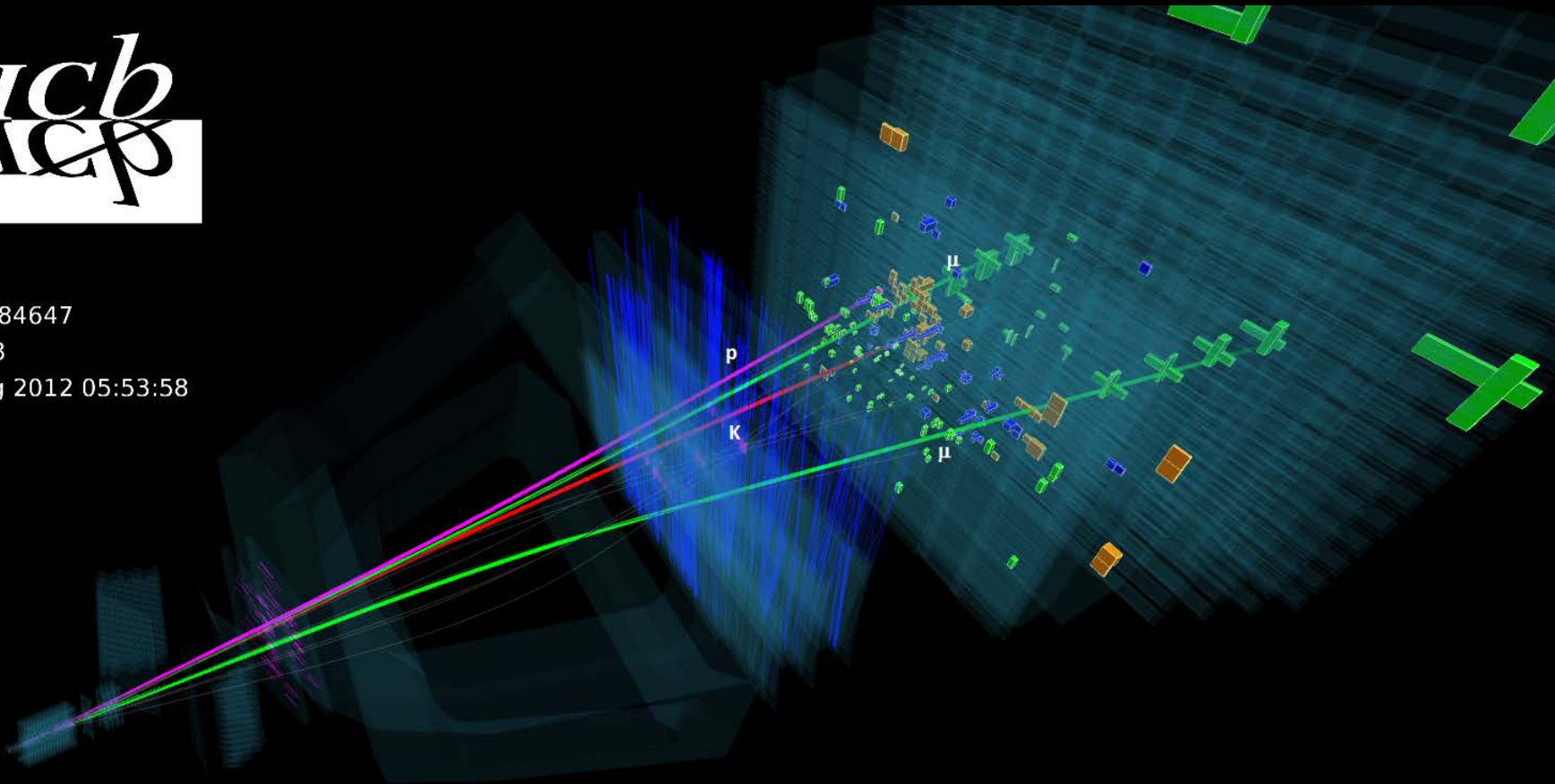
26000 Λ_b
decays

background
only 5.4% in
signal region

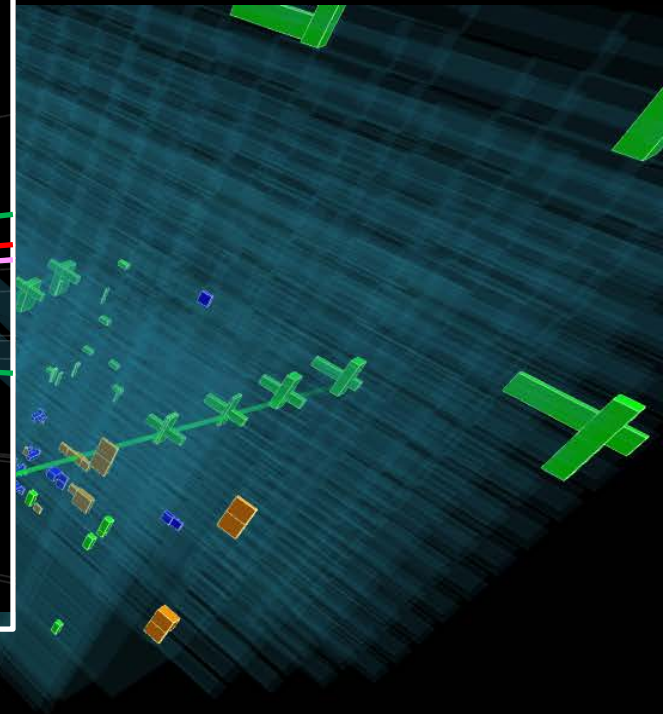
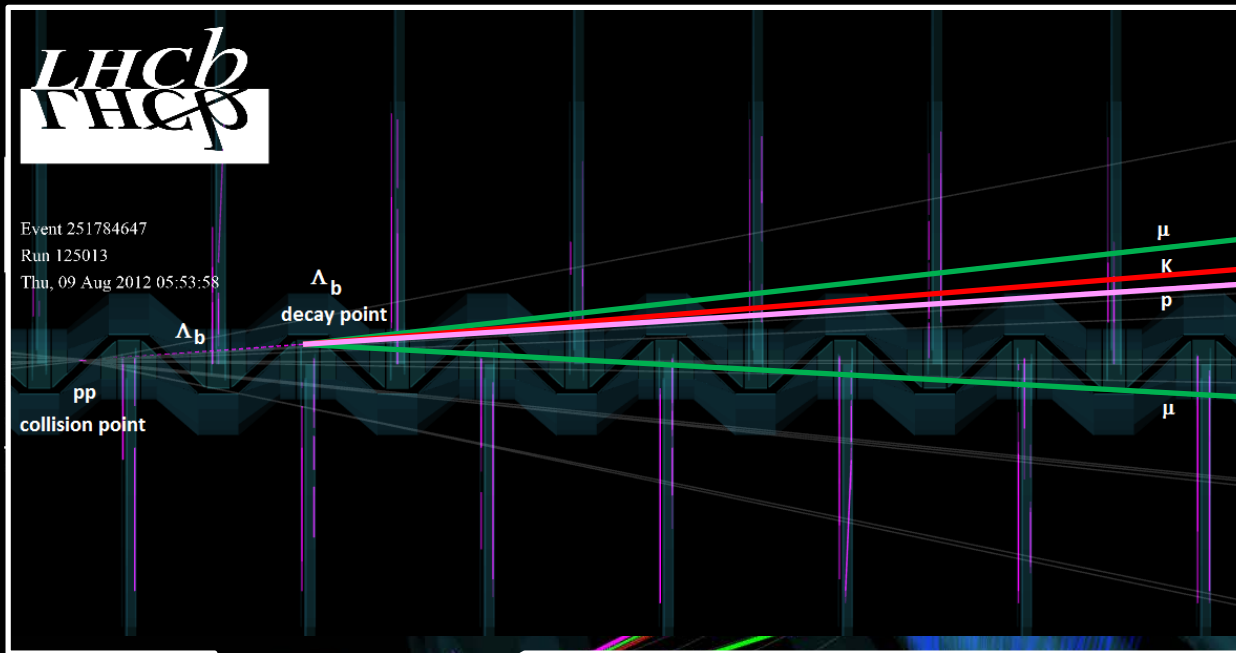
$\Lambda_b^0 \rightarrow J/\psi \text{ p } K^-$ candidate

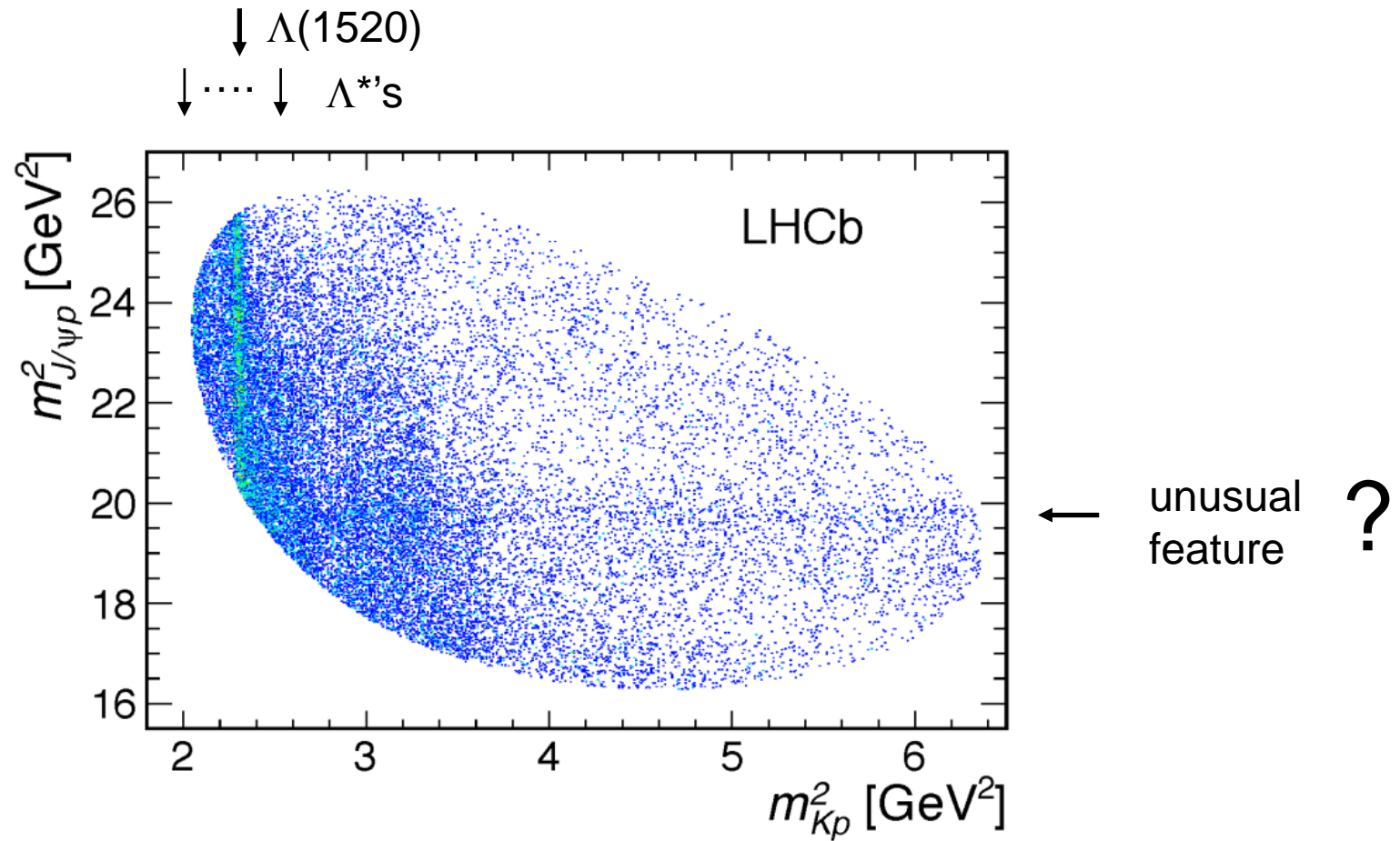


Event 251784647
Run 125013
Thu, 09 Aug 2012 05:53:58



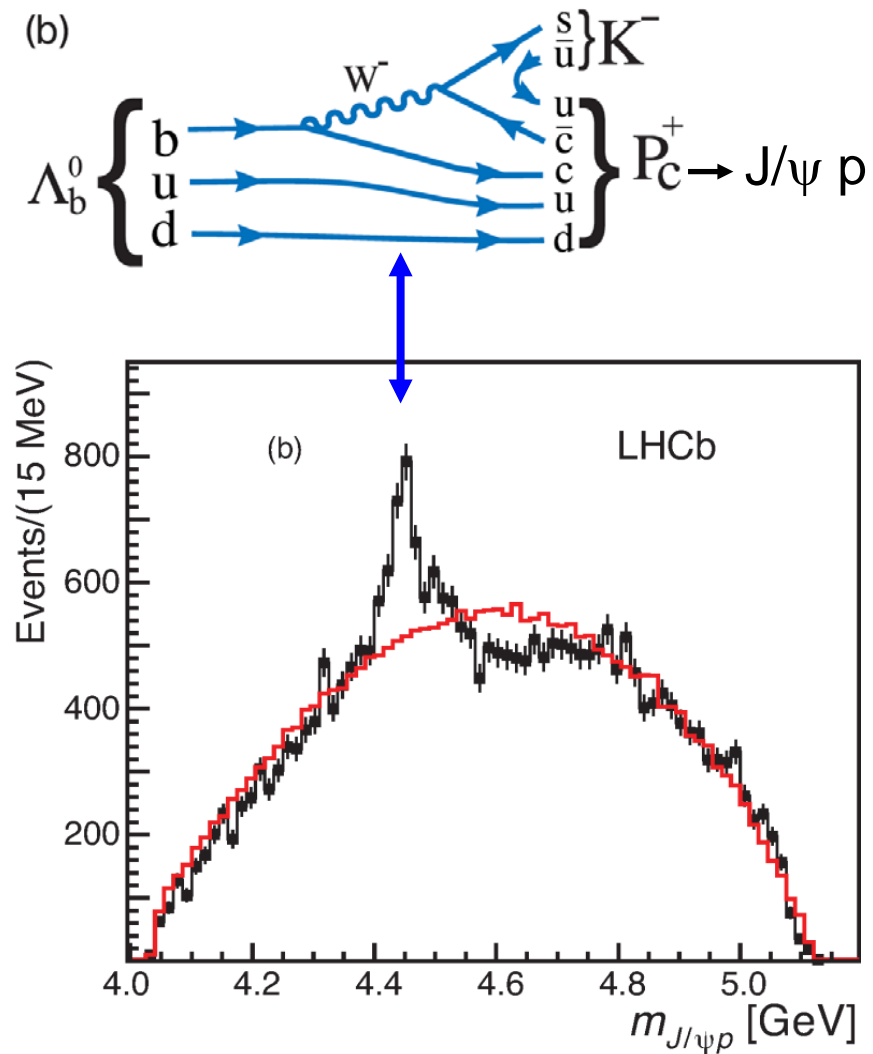
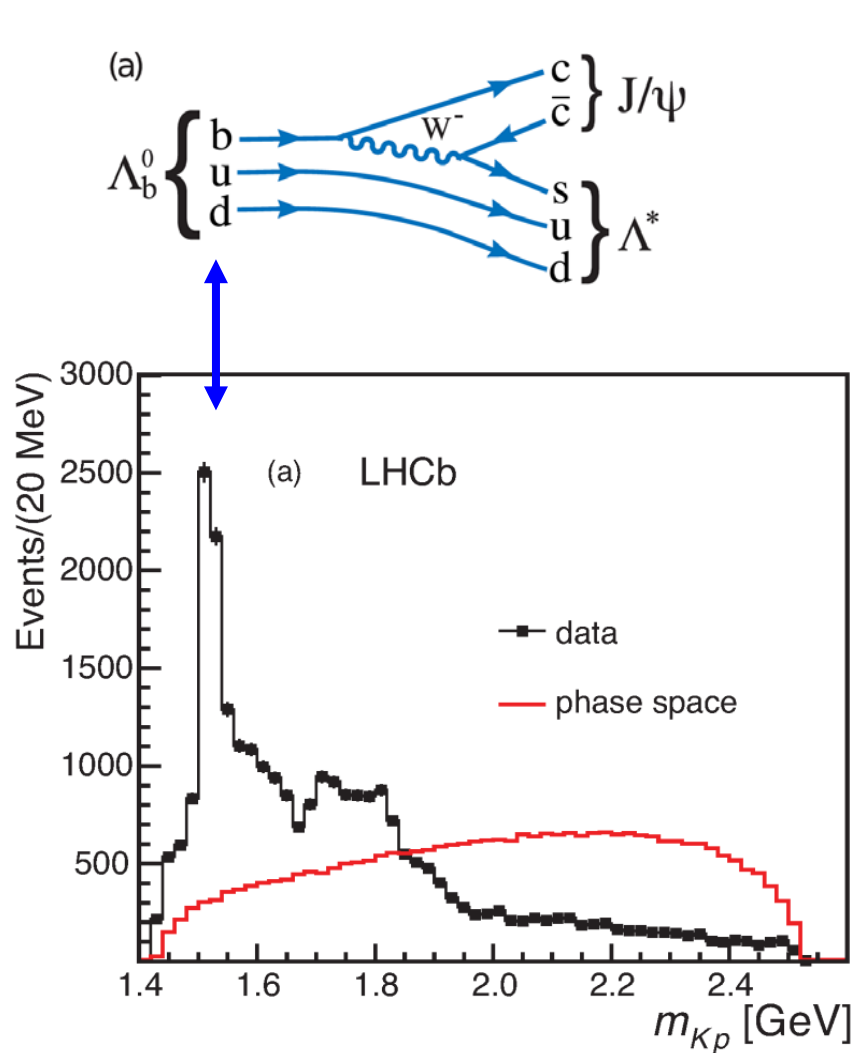
$\Lambda_b^0 \rightarrow J/\psi \text{ p } K^-$ candidate





Projections

PRL 115, 07201, arXiv:1507.03414

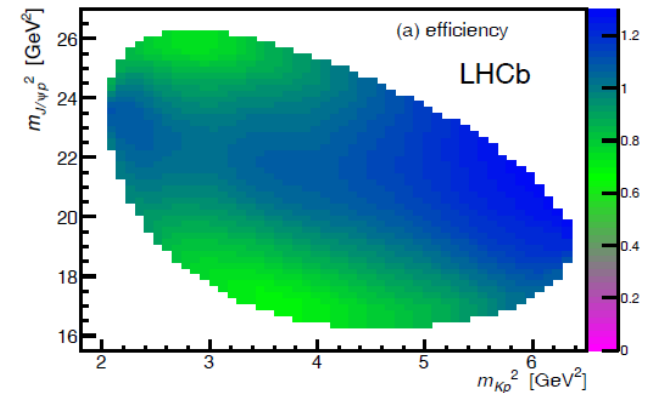


Origin of narrow peak in $m_{J/\psi p}$

PRL 115, 07201, arXiv:1507.03414

Checks to ensure that it is not an artifact of the selection:

- Reflections of $B^0 \rightarrow J/\psi K\pi$ & $B_s \rightarrow J/\psi KK$ are vetoed
- Ξ_b decays checked
- Efficiency is smooth, cannot create a peak
- Λ_b sideband background does not peak
- Clones and ghost tracks are eliminated



Can interference between Λ^* resonances generate peak in $(J/\psi p)$ mass?

If not, can data be described in all relevant kinematic variables with the addition of $(J/\psi p)$ resonances?




Full amplitude analysis using all known Λ^* 's .


Helicity formalism

Each sequential decay $A \rightarrow BC$ contributes to the amplitude:


$$\mathcal{H}_{\lambda_B, \lambda_C}^{A \rightarrow BC} D_{\lambda_A, \lambda_B - \lambda_C}^{J_A}(\phi_B, \theta_A, 0)^* R_A(m_{BC})$$



Complex helicity
coupling amplitude



Wigner D-matrices:
rotation of quantization axis



Complex function for
mass shape (BW)

Express helicity couplings via LS couplings (Clebsch-Gordon coeff.):

$$\mathcal{H}_{\lambda_B, \lambda_C}^{A \rightarrow BC} = \sum_L \sum_S \sqrt{\frac{2L+1}{2J_A+1}} B_{L,S} \left(\begin{array}{cc|c} J_B & J_C & S \\ \lambda_B & -\lambda_C & \lambda_B - \lambda_C \end{array} \right) \times \left(\begin{array}{cc|c} L & S & J_A \\ 0 & \lambda_B - \lambda_C & \lambda_B - \lambda_C \end{array} \right),$$

⇒ Easily consider parity conservation $P_A = P_B P_C (-1)^L$ and restrict L_{\max}

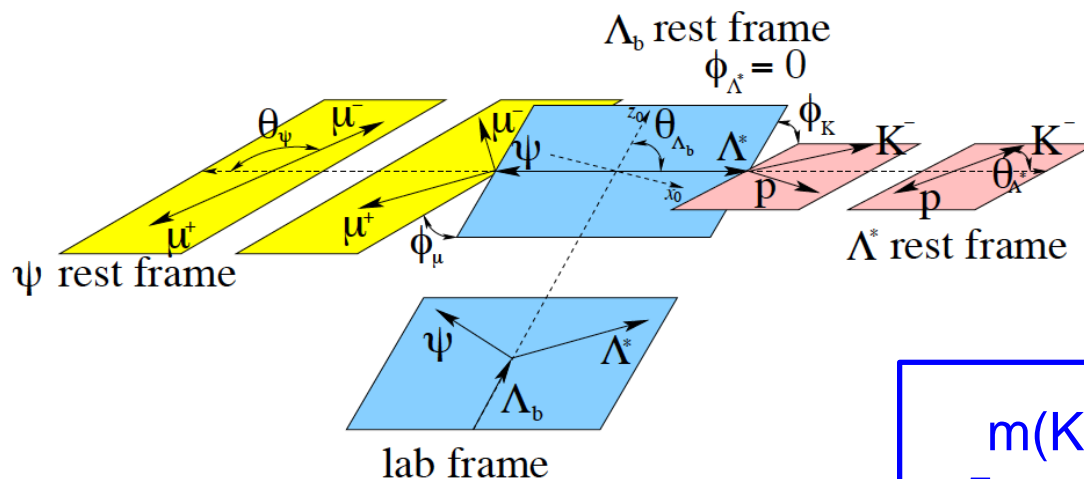
Amplitude Analysis

Consider two interfering processes with two distinct decay chains:

$$\Lambda_b^0 \rightarrow J/\psi \Lambda^*$$

$$\Lambda^* \rightarrow p K^-$$

$$J/\psi \rightarrow \mu\mu$$

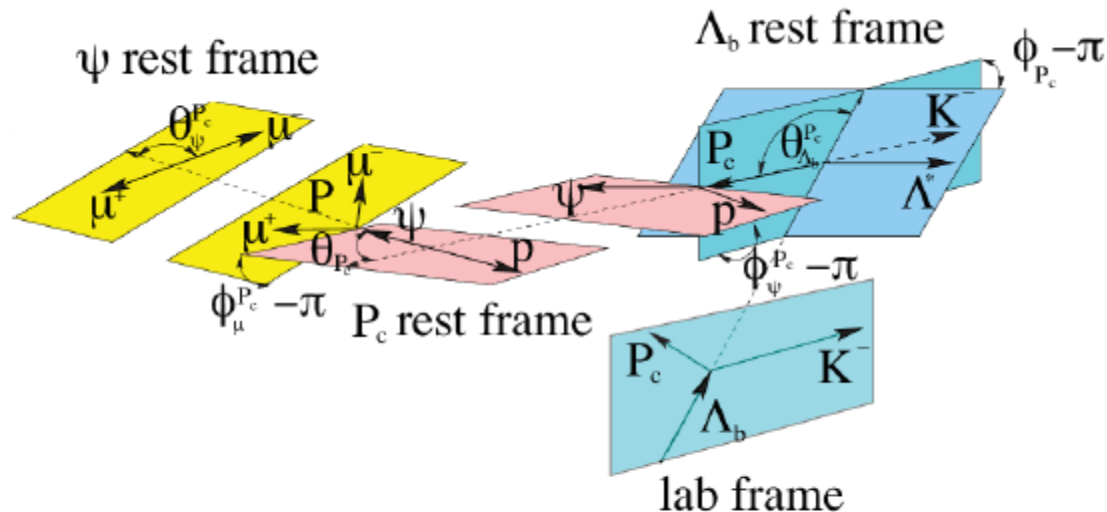


$m(K^-p)$
5 angles

$$\Lambda_b^0 \rightarrow P_c^+ K^-$$

$$P_c^+ \rightarrow J/\psi p$$

$$J/\psi \rightarrow \mu\mu$$



Λ^* resonance model

PRL 115, 07201, arXiv:1507.03414

Extended model:

- All known Λ^* resonances.
Masses and widths fixed to PDG.
- All possible L values.

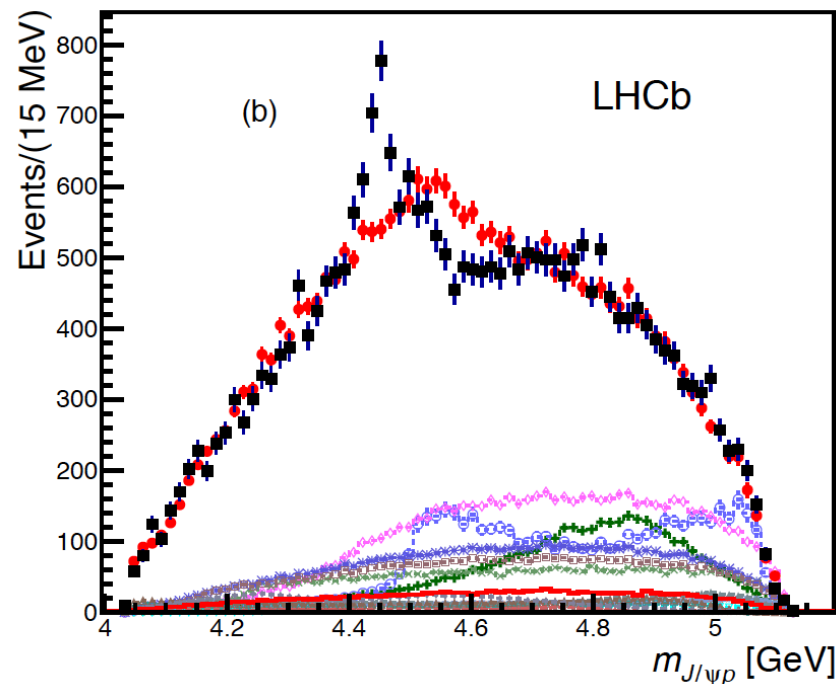
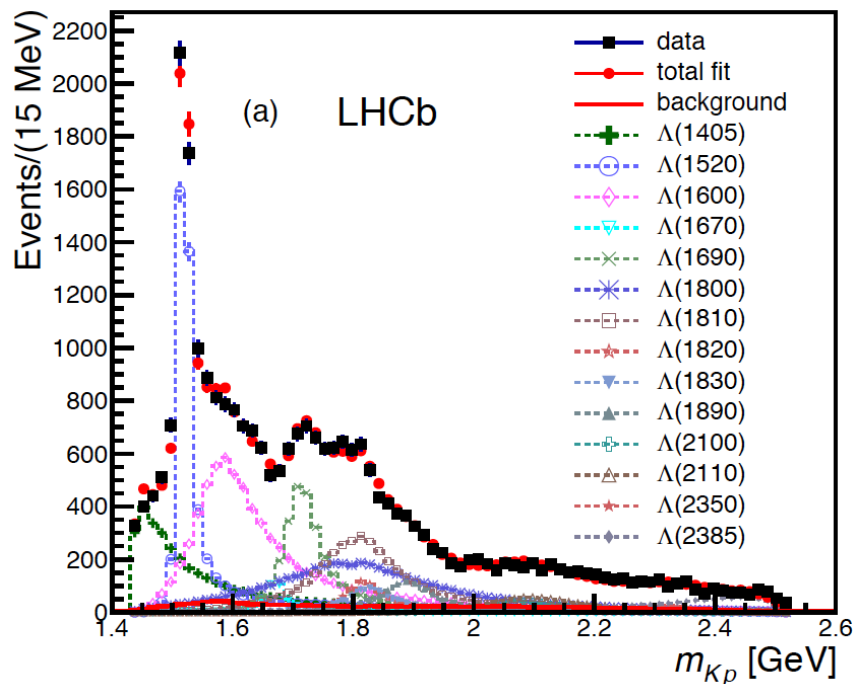
Reduced model:

- Drop $\Lambda(2350)$ and $\Lambda(2585)$
- Remove high L contributions.

	State	J^P	M_0 (MeV)	Γ_0 (MeV)	# Reduced	# Extended	
14 Λ^* states	$\Lambda(1405)$	$1/2^-$	$1405.1^{+1.3}_{-1.0}$	50.5 ± 2.0	3	4	Fit parameters
	$\Lambda(1520)$	$3/2^-$	1519.5 ± 1.0	15.6 ± 1.0	5	6	
	$\Lambda(1600)$	$1/2^+$	1600	150	3	4	
	$\Lambda(1670)$	$1/2^-$	1670	35	3	4	
	$\Lambda(1690)$	$3/2^-$	1690	60	5	6	
	$\Lambda(1800)$	$1/2^-$	1800	300	4	4	
	$\Lambda(1810)$	$1/2^+$	1810	150	3	4	
	$\Lambda(1820)$	$5/2^+$	1820	80	1	6	
	$\Lambda(1830)$	$5/2^-$	1830	95	1	6	
	$\Lambda(1890)$	$3/2^+$	1890	100	3	6	
	$\Lambda(2100)$	$7/2^-$	2100	200	1	6	
	$\Lambda(2110)$	$5/2^+$	2110	200	1	6	
	$\Lambda(2350)$	$9/2^+$	2350	150	0	6	
	$\Lambda(2585)$?	≈ 2585	200	0	6	
					<u>64</u>	<u>146</u>	

Fit with extended Λ^* model (no P_C^+)

PRL 115, 07201, arXiv:1507.03414

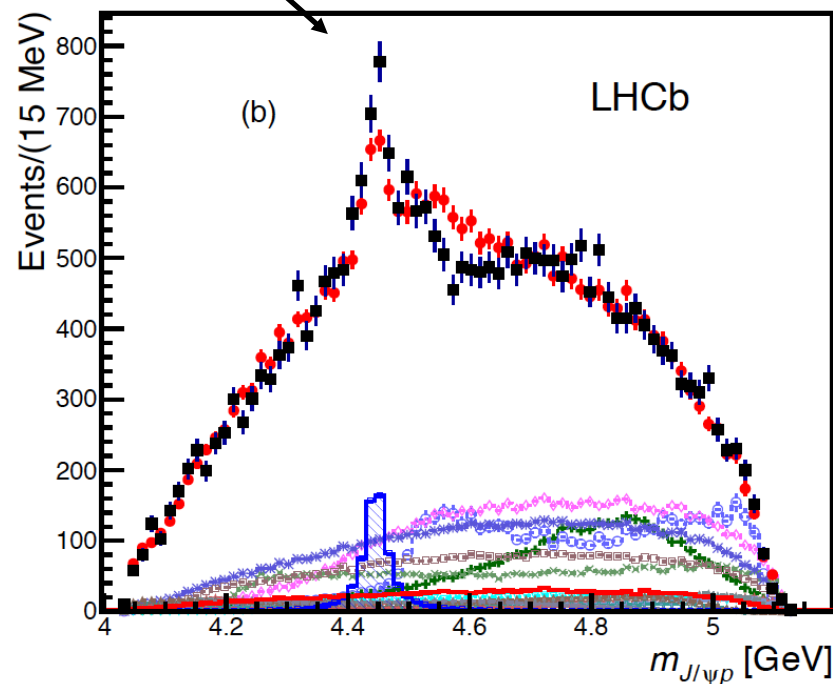
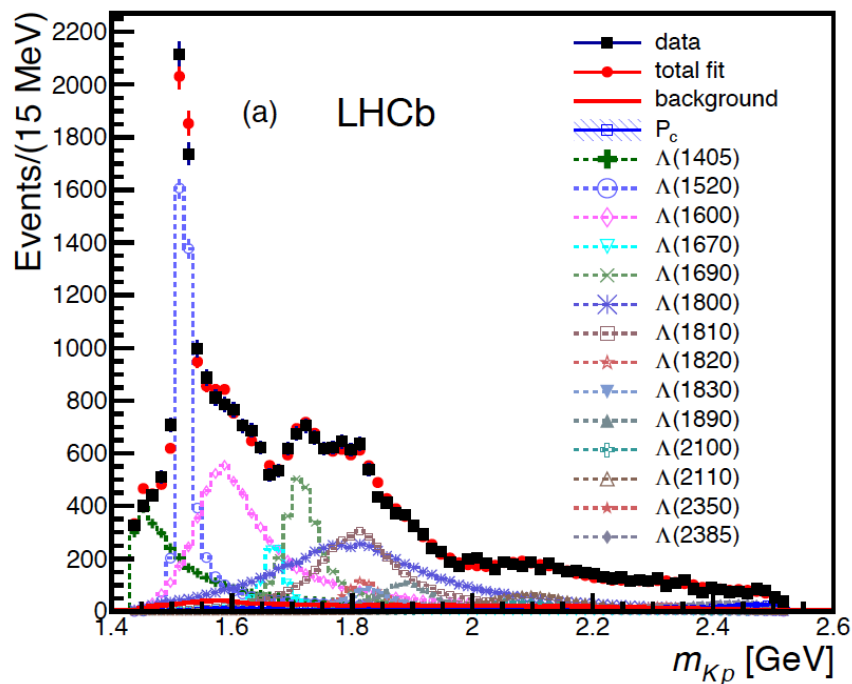


- m_{Kp} looks fine, $m_{J/\psi p}$ not described
- Additional terms do not help:
 - Σ^* 's (expect small contribution: $\Delta I=1$)
 - Λ^* with free mass and widths
 - Non-resonant terms w/ $J^P=1/2^\pm, 3/2^\pm$

Fit with one additional P_C^+ state

PRL 115, 07201, arXiv:1507.03414

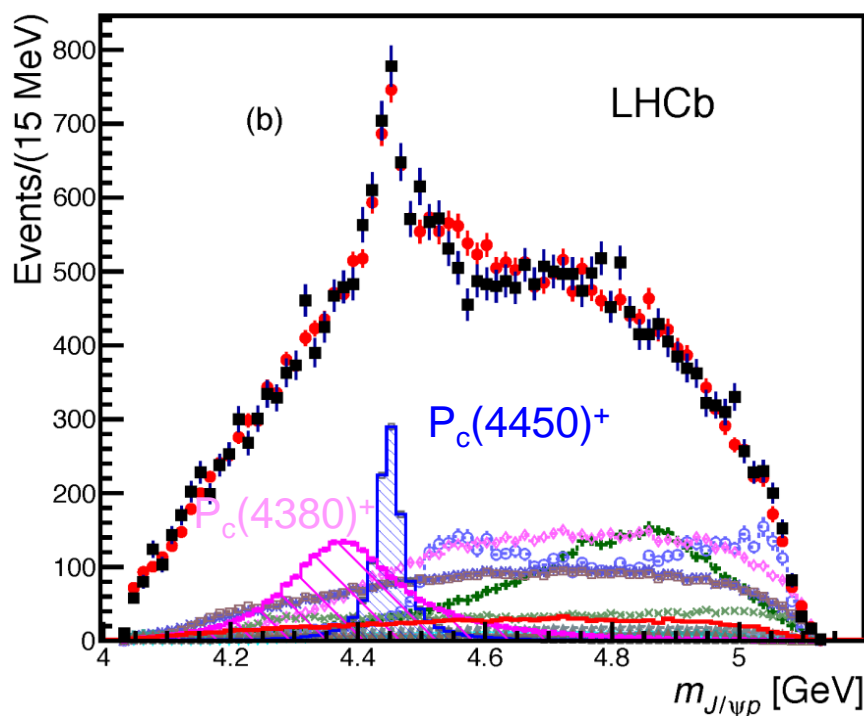
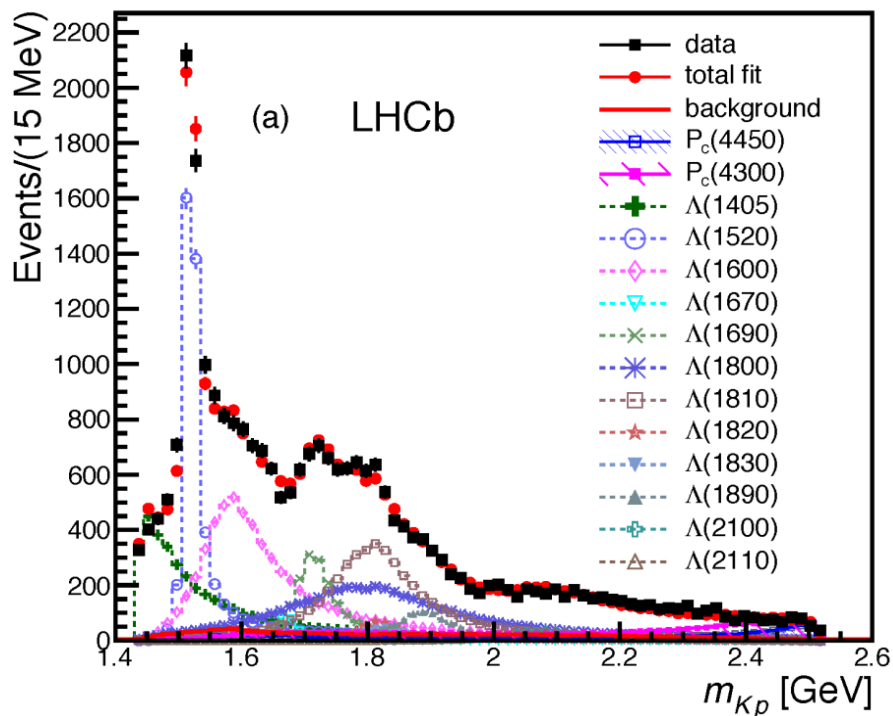
- Extended Λ^* model
- Try all J^P (P_C^+) up to $7/2^\pm$
- Best fit for $J^P(P_C^+)=5/2^\pm$. Still not a good fit.



Fit with two additional P_c^+ states

PRL 115, 07201, arXiv:1507.03414

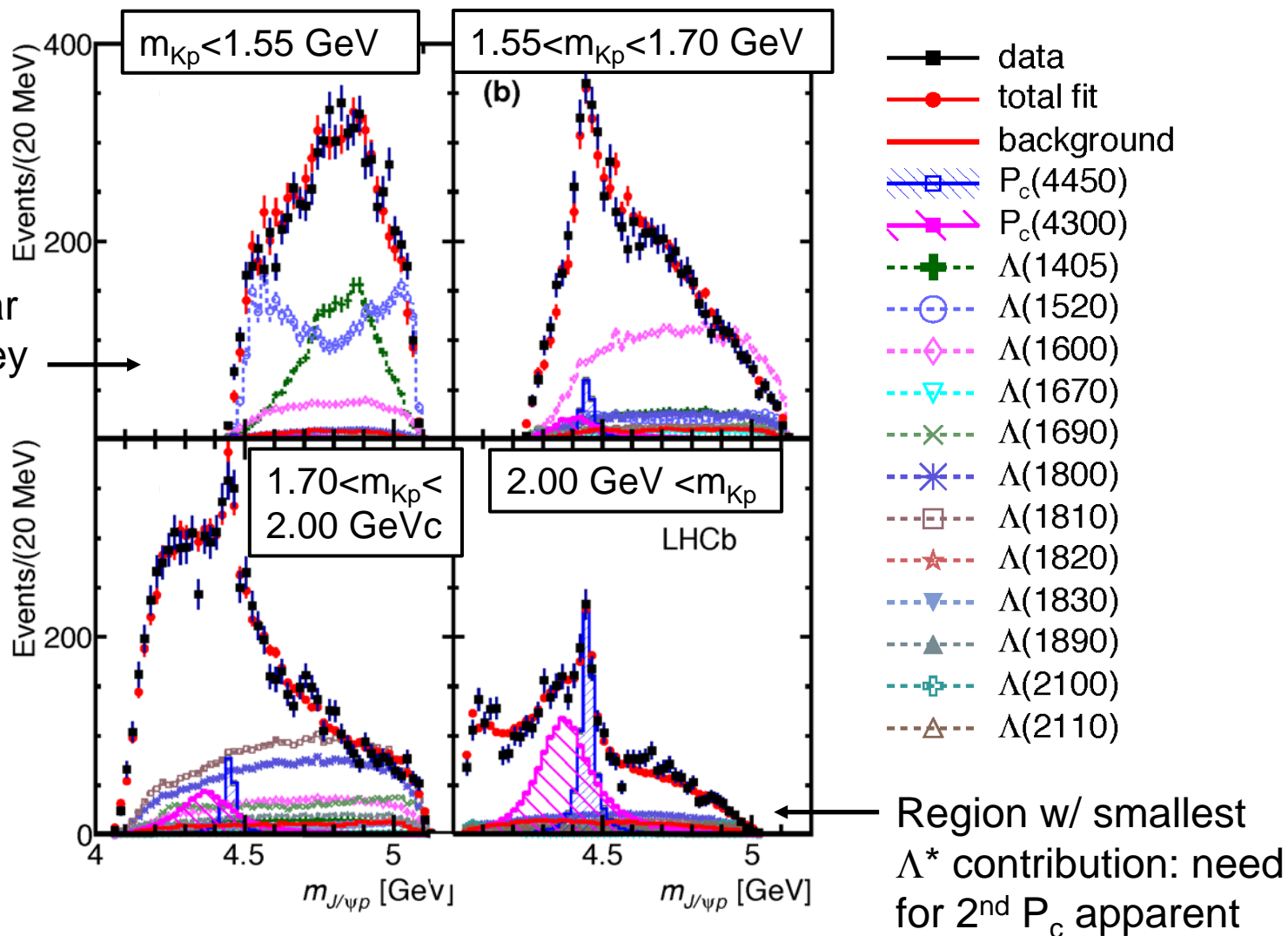
- Obtain good fits even with the reduced Λ^* model (use reduced Λ^* model when determining the P_c^+ parameters)
- Best fit has $J^P=(3/2^-, 5/2^+)$, also $J^P=(3/2^+, 5/2^-)$ and $J^P=(5/2^+, 3/2^-)$ possible ($\Delta(-2\ln\mathcal{L})=1, 2.3^2$). Other combinations up to $7/2$ disfavored. Opposite parity needed to explain P_c^+ decay angle distribution.



$m_{J/\psi p}$ projection for different m_{Kp} bins

PRL 115, 07201, arXiv:1507.03414

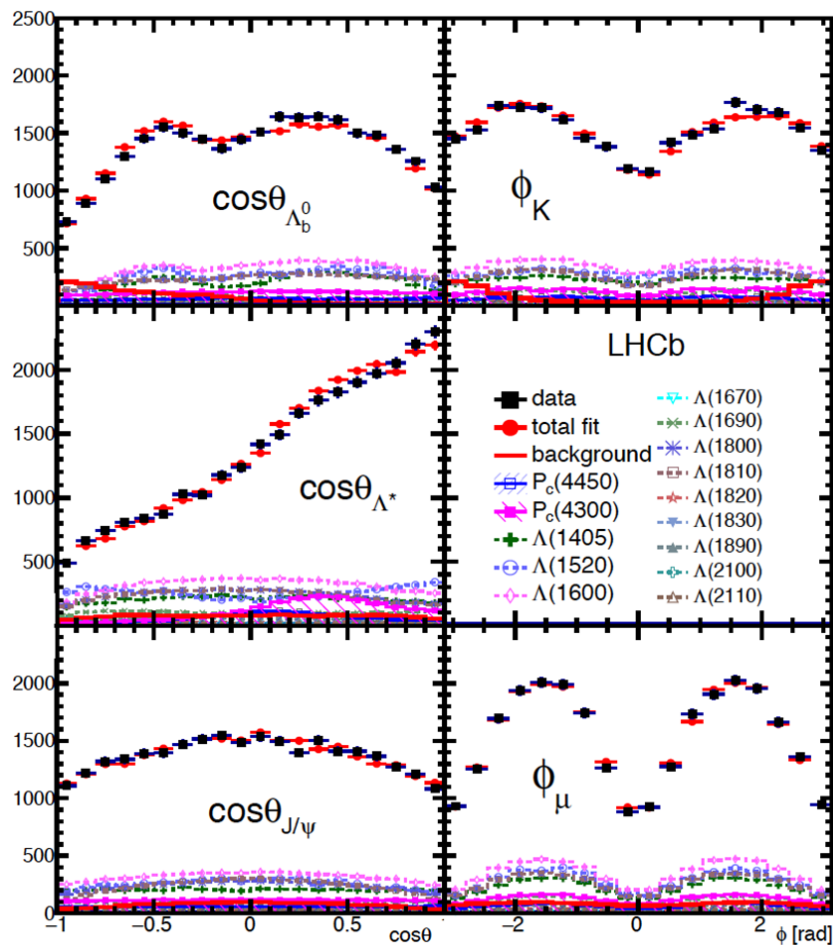
P_c 's cannot appear in first interval: they would be outside Dalitz boundary



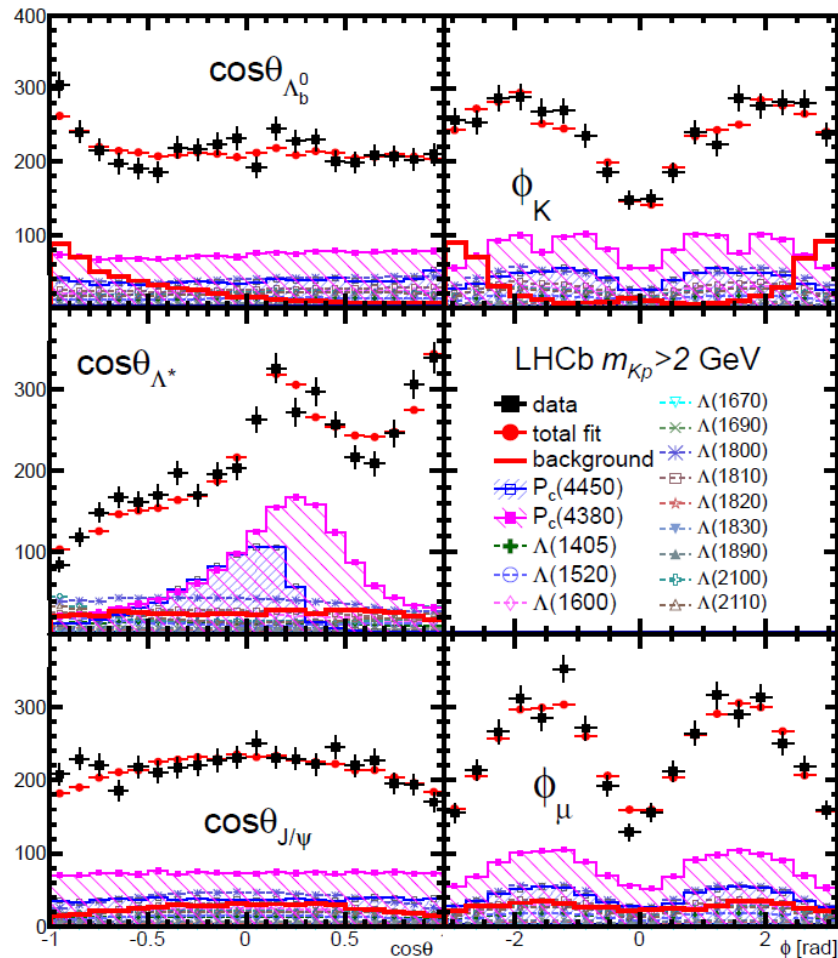
Angular distributions

PRL 115, 07201, arXiv:1507.03414

All data



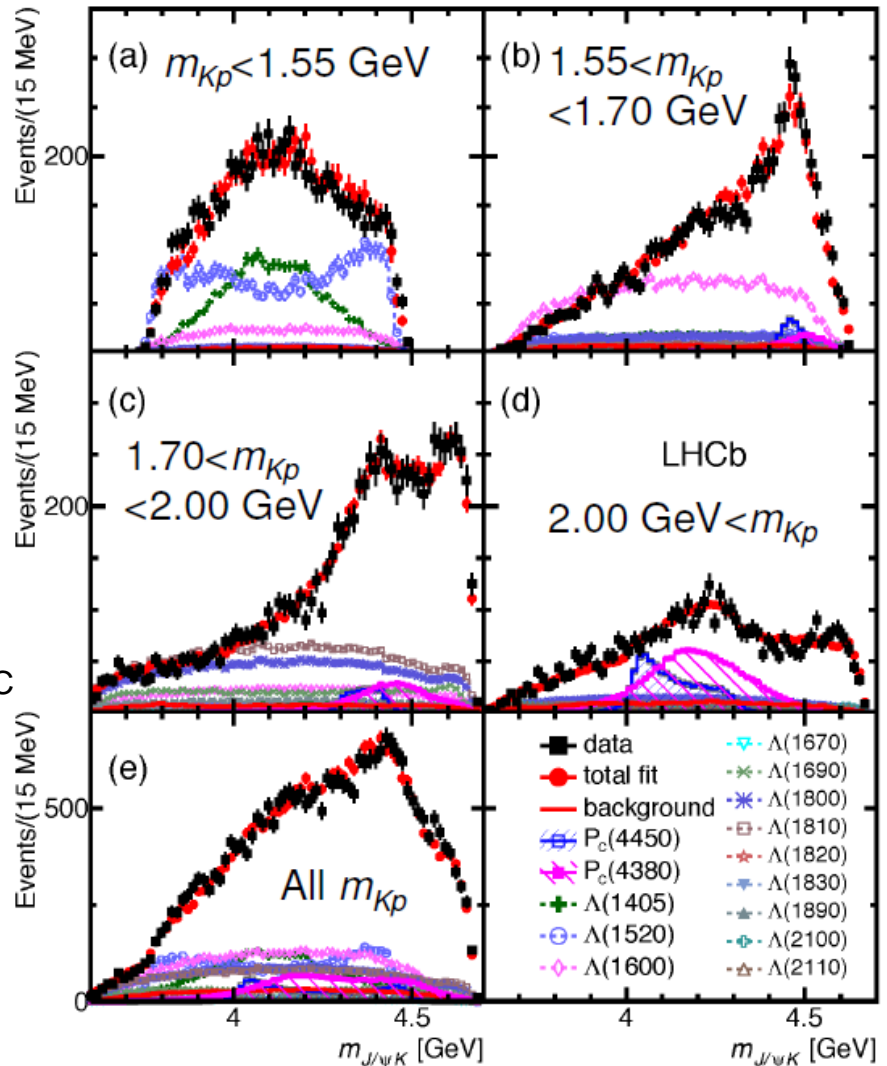
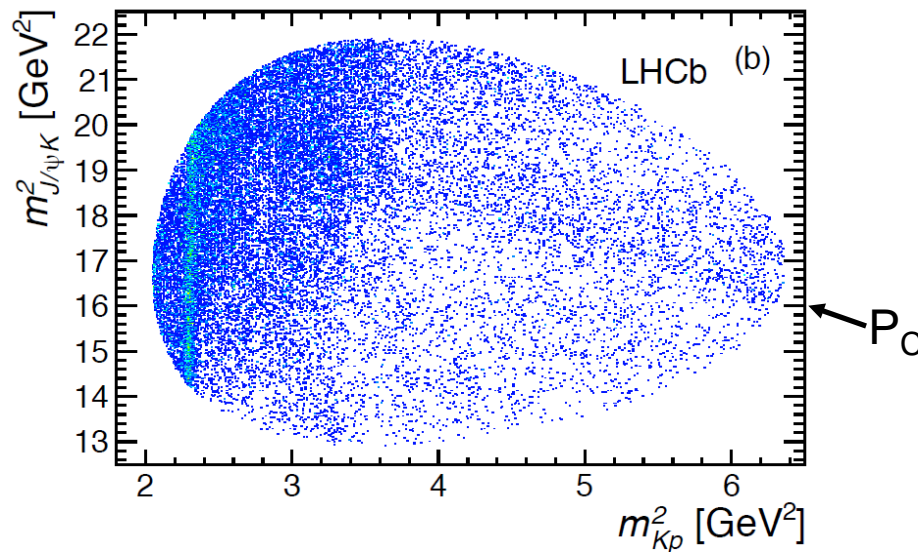
P_C^+ enriched ($m_{Kp} > 2$ GeV)



No need for exotic $J/\psi K^-$ contributions

PRL 115, 07201, arXiv:1507.03414

$J/\psi K^-$ structure well described by the Λ^* and P_c^+ reflections.



Significances and Fit Results

PRL 115, 07201, arXiv:1507.03414

Improvement
of fit quality:

Fit w/ only Λ^* model

+ 1st P_c^+

+ 2nd P_c^+

$$\Delta(-2\ln\mathcal{L}) = 14.7^2$$

$$\Delta(-2\ln\mathcal{L}) = 11.6^2$$

$$\Delta(-2\ln\mathcal{L}) = 18.7^2$$

Simulation of pseudo-experiments used
to turn $\Delta(-2\ln\mathcal{L})$ values into significances:

(includes dominant systematics: difference
between extended and reduced Λ^* model)

$P_c(4450)^+$	12σ
$P_c(4380)^+$	9σ
$P_c(4450) \text{ \& } P_c(4380)$	15σ

State	Mass (MeV)	Width (MeV)	Fit Fraction (%)
$P_c(4380)^+$	$4380 \pm 8 \pm 29$	$205 \pm 18 \pm 86$	$8.4 \pm 0.7 \pm 4.2$
$P_c(4450)^+$	$4449.8 \pm 1.7 \pm 2.5$	$39 \pm 5 \pm 19$	$4.1 \pm 0.5 \pm 1.1$
$\Lambda(1405)$	<i>PRL 115, 07201, arXiv:1507.03414</i>		$15 \pm 1 \pm 6$
$\Lambda(1520)$			$19 \pm 1 \pm 4$

Systematic uncertainties

Source	M_0 (MeV)		Γ_0 (MeV)		Fit fractions (%)			
	low	high	low	high	low	high	$\Lambda(1405)$	$\Lambda(1520)$
Extended vs. reduced	21	0.2	54	10	3.14	0.32	1.37	0.15
Λ^* masses & widths	7	0.7	20	4	0.58	0.37	2.49	2.45
Proton ID	2	0.3	1	2	0.27	0.14	0.20	0.05
$10 < p_p < 100$ GeV	0	1.2	1	1	0.09	0.03	0.31	0.01
Nonresonant	3	0.3	34	2	2.35	0.13	3.28	0.39
Separate sidebands	0	0	5	0	0.24	0.14	0.02	0.03
J^P ($3/2^+$, $5/2^-$) or ($5/2^+$, $3/2^-$)	10	1.2	34	10	0.76	0.44		
$d = 1.5 - 4.5$ GeV $^{-1}$	9	0.6	19	3	0.29	0.42	0.36	1.91
$L_{\Lambda_b^0}^{P_c} \Lambda_b^0 \rightarrow P_c^+ (\text{low/high}) K^-$	6	0.7	4	8	0.37	0.16		
$L_{P_c} P_c^+ (\text{low/high}) \rightarrow J/\psi p$	4	0.4	31	7	0.63	0.37		
$L_{\Lambda_b^0}^{\Lambda^*} \Lambda_b^0 \rightarrow J/\psi \Lambda^*$	11	0.3	20	2	0.81	0.53	3.34	2.31
Efficiencies	1	0.4	4	0	0.13	0.02	0.26	0.23
Change $\Lambda(1405)$ coupling	0	0	0	0	0	0	1.90	0
Overall	29	2.5	86	19	4.21	1.05	5.82	3.89
sFit/cFit cross check	5	1.0	11	3	0.46	0.01	0.45	0.13

- Λ^* modeling is largest uncertainty
- Fits w/ alternative J^P assignment
- Parameters for description of mass dependence

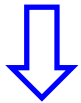
Cross checks

- Two independently coded max. log likelihood fitters using different background subtractions (cFit [default] & sFit):
 - Signal and background described by PDFs
 - background subtraction using sPlot technique*)
- Split data to check consistency: 2011/2012, magnet up/down, $\Lambda_b/\bar{\Lambda}_b$, $\Lambda_b(p_T \text{ low})/\Lambda_b(p_T \text{ high})$
- Extended model fits tried without P_c states, but two additional high mass Λ^* resonances allowing masses & widths to vary, or 4 non-resonant terms of J up to 3/2

*) sPlot: *M.Pivk and F.R. Le Diberder, NIM A555 (2005) 356.*

Phase motion across the resonance

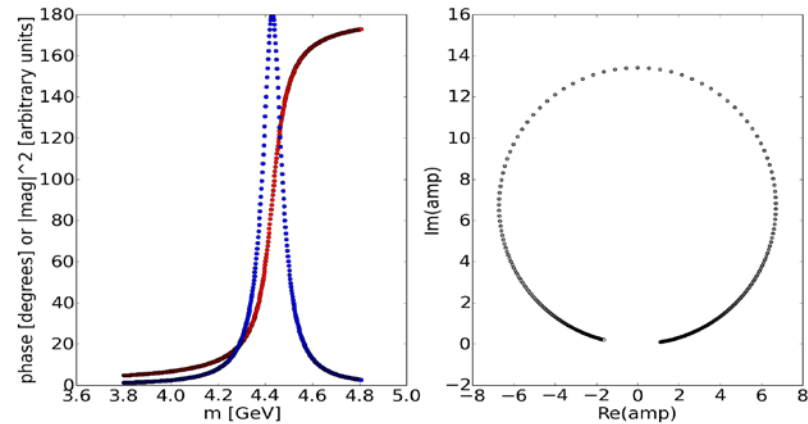
For a Breit-Wigner resonance we expect a phase variation over the resonance:



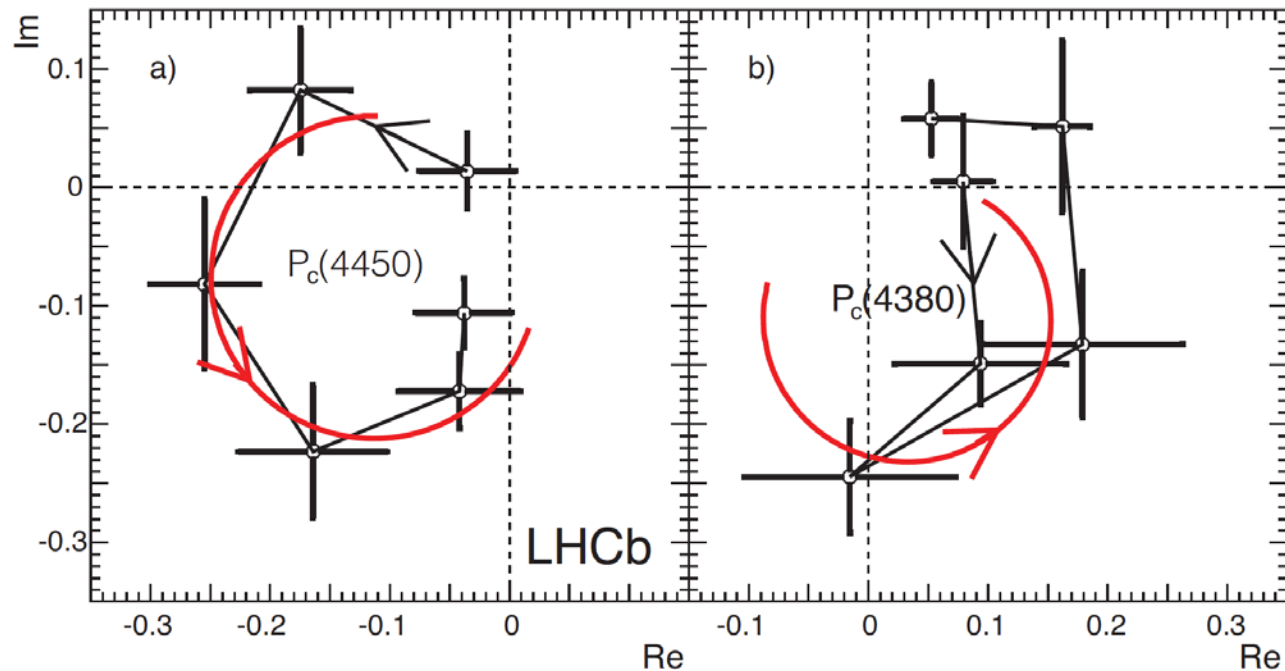
Fit Re and Im part of amplitudes for 6 individual mass bins in $M_0 \pm \Gamma_0$

$P_c(4450)$: clock-wise phase change across pole.

$P_c(4380)$: large changes, not conclusive



PRL 115, 07201, arXiv:1507.03414



Interpretation

- Kinematic effects in non-perturbative rescattering processes (cusps)

e.g. arXiv:1507.04950, 1507.05359,
1507.06552, 1507.07478

- bound states (or resonances) formed from open-charm baryon and meson constituents

e.g. arXiv:1507.03717, 1507.03704,
1507.05200, 1507.04249, 1508.00924

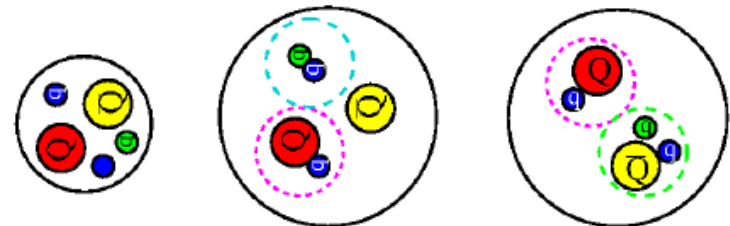
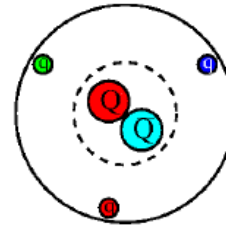
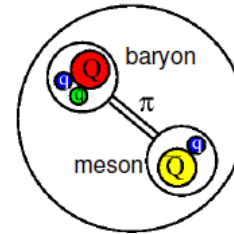
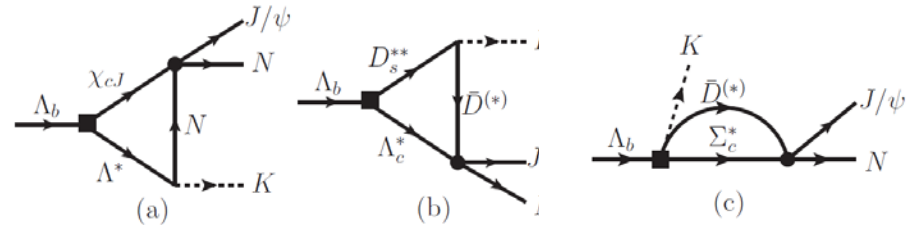
- Baryocharmonia

e.g. arXiv:1508.00888

- Tightly bound pentaquark states

e.g. arXiv:1201.0807, 1507.04980,
1507.07652, 1508.00356, 1507.05867,
1507.08252, 1508.01468, 1508.04189

from arXiv:1507.05359

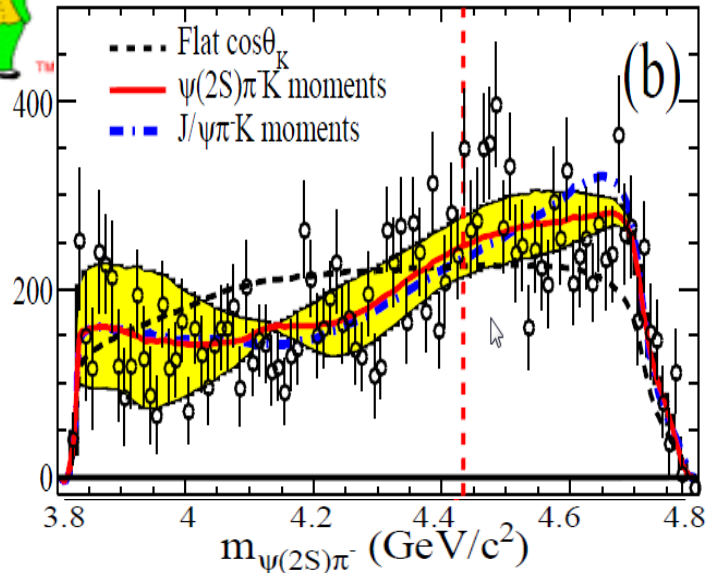


The $Z^+(4430)$ – a Tetraquark Candidate

After the first observation by Belle in 2008 using simple 1D mass fit:



PRD 79, 112001 (2009)

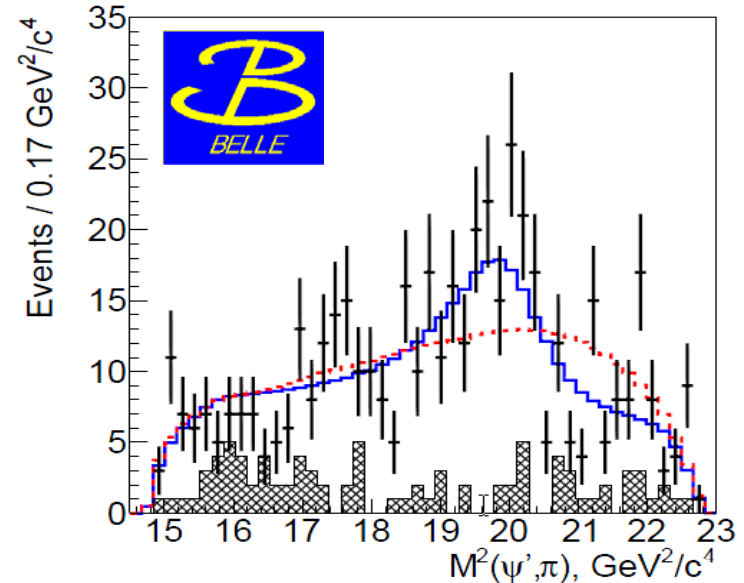


2D analysis. Harmonic moments for K^* reflected to $m(\psi'\pi^+)$: model independent description of $K^* \rightarrow K\pi$



BaBar did not confirm $Z(4430)^+$

PRD 88, 074026 (2013)



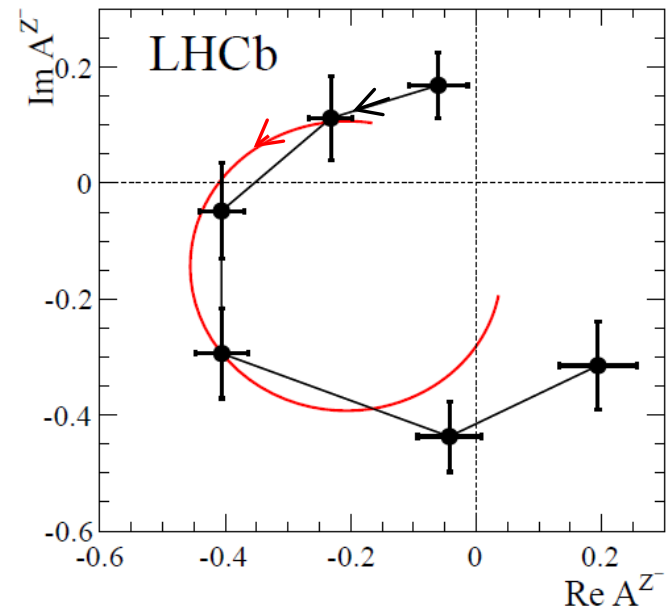
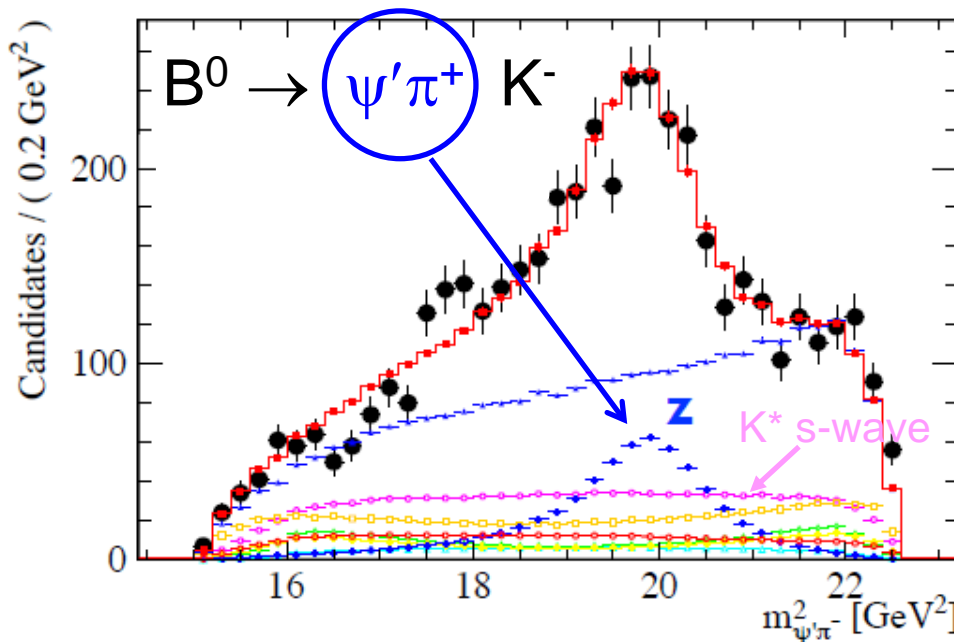
4D amplitude fit: model dependent description of $K^* \rightarrow K\pi$ resonances.

6.4σ (5.6σ w/ syst.) observation,
 $J^P=1^+$ preferred by $>3.4\sigma$

Z(4430)⁺ confirmation by LHCb

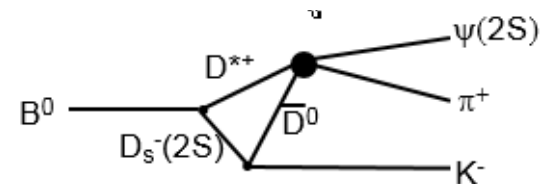
PRL 112, 222002 (2014), arXiv:1404.1903

LHCb: more data and smaller backgrounds



4D amplitude analysis:

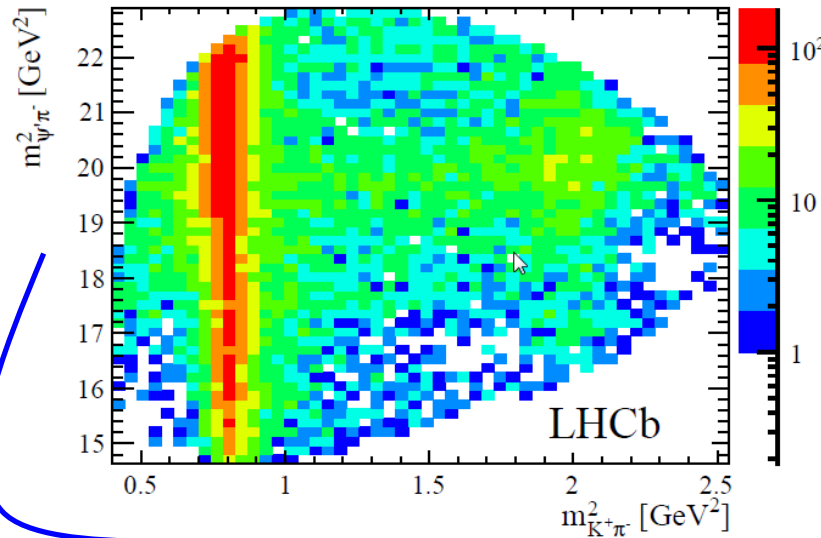
- Clear confirmation of $Z(4430)^+$
- Resonance phase motion
- Quantum number: $J^P = 1^+$
- Rescattering \rightarrow diff. phase behavior



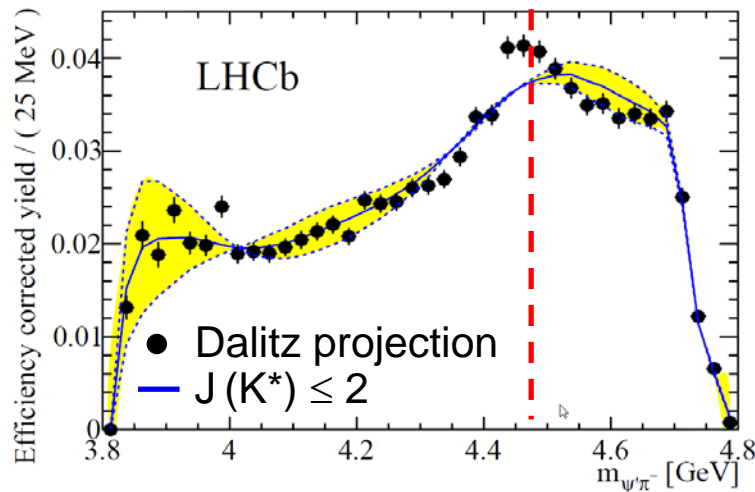
*P. Pakhlov, T. Uglov
PLB 748, 183 (2015)*

2D model independent analysis

PRL 112, 222002 (2014), arXiv:1404.1903

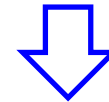


4D Belle



Describe the K^* angular distribution ($\cos\theta_{K^*}$) and thus the reflection in $m_{\psi'\pi}$ using Legendre polynoms.

The maximum moment l_{\max} of the Legendre polynoms depends on max. $J(K^*)$.



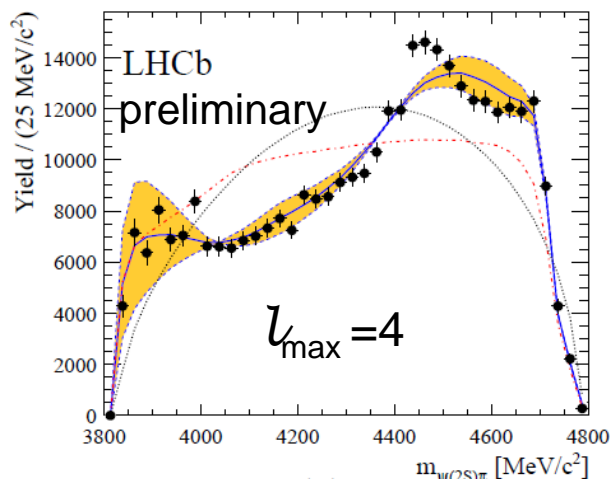
K^* contribution filtered w/ $J(K^*) \leq 2$ ($l_{\max} \leq 4$):
Cannot describe the “Z(4430) region”

Quantitative Analysis

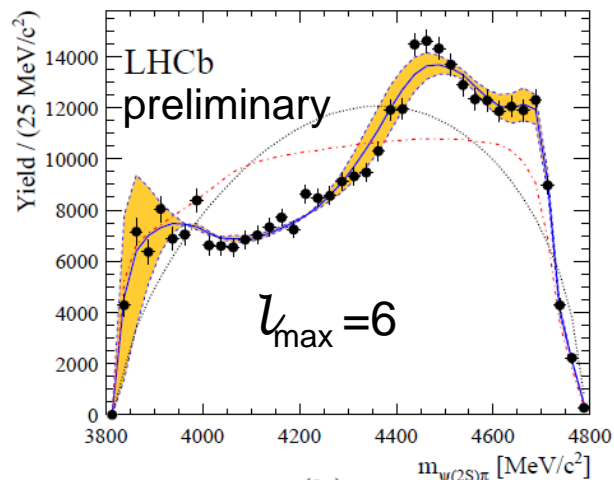
LHCb-Paper-2015-038
(in preparation)

..... phase space
..... $m_{K\pi}$ weighting

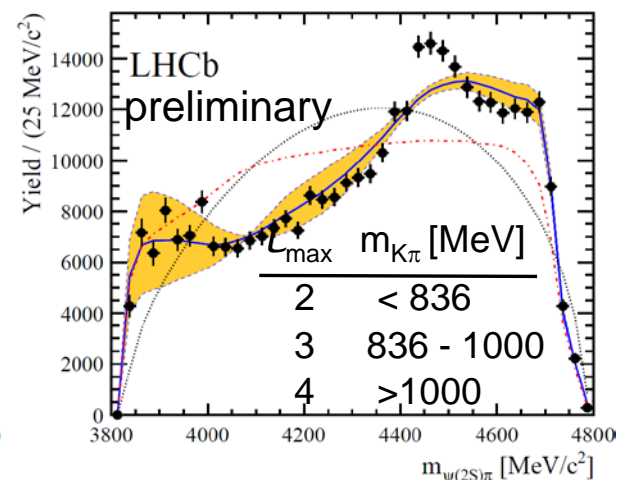
■ experimental (stat.) uncertainty of moments



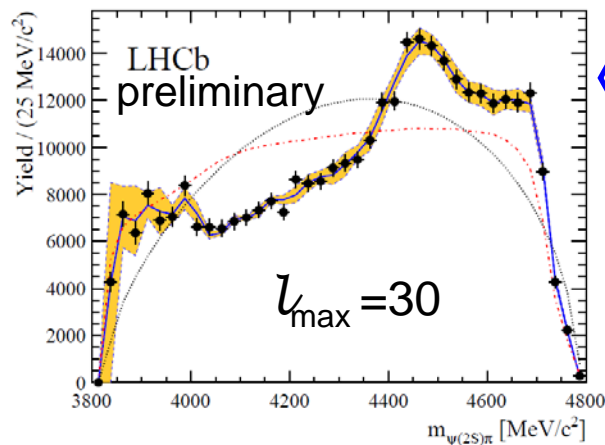
Significance 13.3σ



Significance 8.0σ



Significance 15.2σ



To calculate significance from pseudo-experiments we compare to test-statistics obtained with implausible high $l_{\max} = 30$.

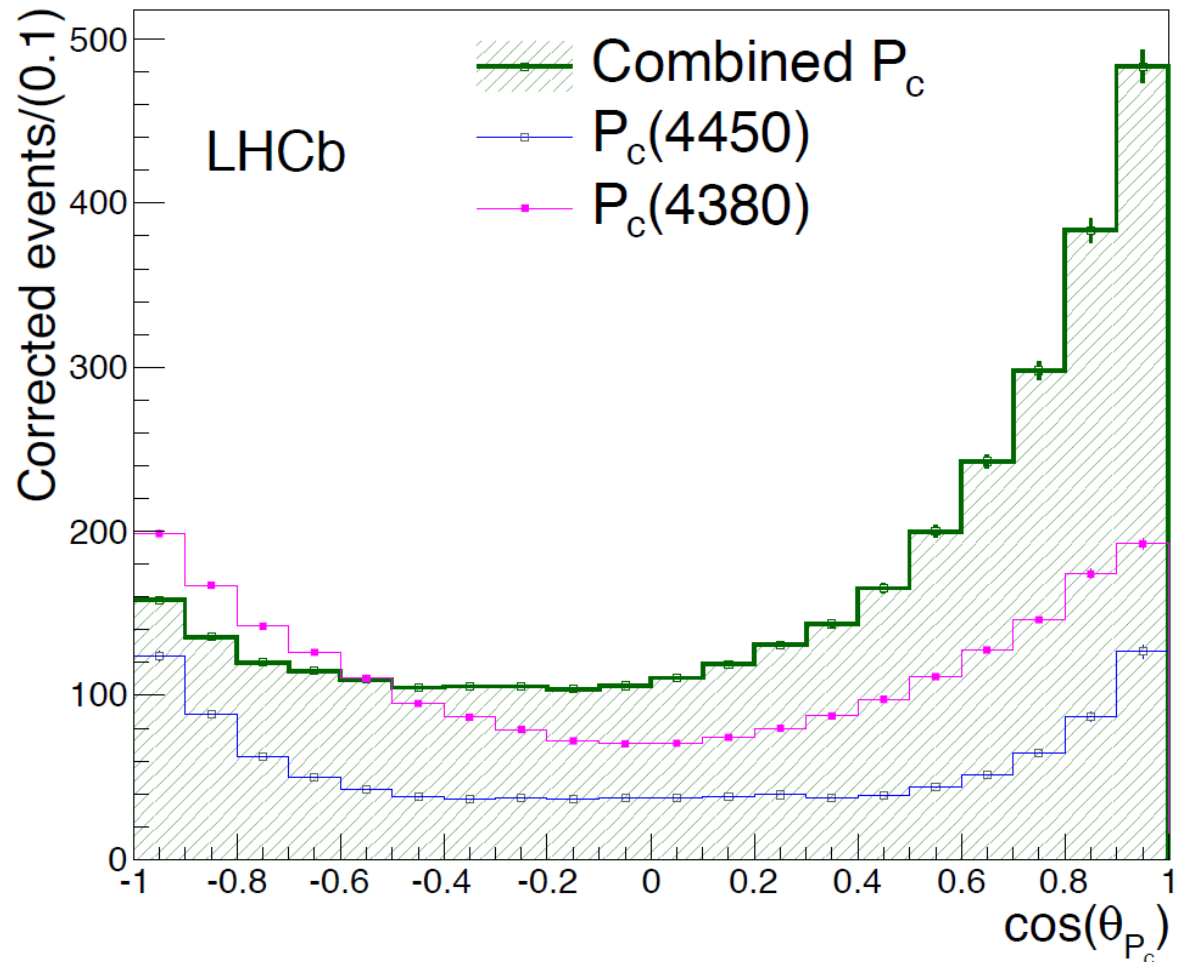
Explanation of data by plausible K^* contributions is ruled out with $>8.0\sigma$ w/o assuming anything about the K^* model.

Conclusion

- Two states decaying to $J/\psi p$ have been observed in Λ_b decays which are consistent with pentaquarks. To better understand the origin:
 - Search for diff. final-states (e.g. $\Lambda_b \rightarrow J/\psi p \pi^-, \chi_c p K^-, \eta_c p K^-, \Lambda_c^+ D^0 K^-$)
 - Look in different b-hadron decays (e.g. Ξ_b)
 - Look for isospin partners (e.g. $\Lambda_b \rightarrow [ccddu] K^0$)
 - Study $\chi_c \Lambda^*, \Sigma_c^* D, \dots$ to check rescattering
- The 2014 model dependent amplitude analysis confirmed the $Z(4430)$ tetraquark state from Belle and established its resonance character via the phase behavior.

A new model independent analysis also demonstrates the need of an exotic tetraquark contributions with significances $>8\sigma$.
- We look forward to the discovery of more exotic hadrons and learning about their internal structure.

P_c^+ Angular distribution



Helicity Formalism

D -matrix,

$$|J_A, m_A\rangle = \sum_{m'_A} D_{m_A, m'_A}^{J_A}(\alpha, \beta, \gamma)^* |J_A, m'_A\rangle,$$

where,

$$D_{m, m'}^J(\alpha, \beta, \gamma)^* = \langle J, m | \mathcal{R}(\alpha, \beta, \gamma) | J, m' \rangle^* = e^{im\alpha} d_{m, m'}^J(\beta) e^{im'\gamma},$$

$$D_{m' m}^j(\alpha, \beta, \gamma) \equiv \langle jm' | \mathcal{R}(\alpha, \beta, \gamma) | jm \rangle = e^{-im'\gamma} d_{m' m}^j(\beta) e^{-im\alpha}.$$

Amplitude Analysis II

- The matrix element for the Λ^* decay is:

$$\mathcal{M}_{\lambda_{\Lambda_b^0}, \lambda_p, \Delta\lambda_\mu}^{\Lambda^*} \equiv \sum_n \sum_{\lambda_{\Lambda^*}} \sum_{\lambda_\psi} \mathcal{H}_{\lambda_{\Lambda^*}, \lambda_\psi}^{\Lambda_b^0 \rightarrow \Lambda_n^* \psi} D_{\lambda_{\Lambda_b^0}, \lambda_{\Lambda^*} - \lambda_\psi}^{\frac{1}{2}}(0, \theta_{\Lambda_b^0}, 0)^* \\ \mathcal{H}_{\lambda_p, 0}^{\Lambda_n^* \rightarrow Kp} D_{\lambda_{\Lambda^*}, \lambda_p}^{J_{\Lambda_n^*}}(\phi_K, \theta_{\Lambda^*}, 0)^* R_n(m_{Kp}) D_{\lambda_\psi, \Delta\lambda_\mu}^1(\phi_\mu, \theta_\psi, 0)^*$$

- And for the P_c :

$$\mathcal{M}_{\lambda_{\Lambda_b^0}, \lambda_p^{P_c}, \Delta\lambda_\mu^{P_c}}^{P_c} \equiv \sum_j \sum_{\lambda_{P_c}} \sum_{\lambda_\psi^{P_c}} \mathcal{H}_{\lambda_{P_c}, 0}^{\Lambda_b^0 \rightarrow P_{cj} K} D_{\lambda_{\Lambda_b^0}, \lambda_{P_c}}^{\frac{1}{2}}(\phi_{P_c}, \theta_{\Lambda_b^0}^{P_c}, 0)^* \\ \mathcal{H}_{\lambda_\psi^{P_c}, \lambda_p^{P_c}}^{P_{cj} \rightarrow \psi p} D_{\lambda_{P_c}, \lambda_\psi^{P_c} - \lambda_p^{P_c}}^{J_{P_{cj}}}(\phi_\psi, \theta_{P_c}, 0)^* R_j(m_{\psi p}) D_{\lambda_\psi^{P_c}, \Delta\lambda_\mu^{P_c}}^1(\phi_\mu^{P_c}, \theta_\psi^{P_c}, 0)^*$$

$$R_X(m) = B'_{L_{\Lambda_b^0}^X}(p, p_0, d) \left(\frac{p}{M_{\Lambda_b^0}} \right)^{L_{\Lambda_b^0}^X} \text{BW}(m|M_{0X}, \Gamma_{0X}) B'_{L_X}(q, q_0, d) \left(\frac{q}{M_{0X}} \right)^{L_X}.$$

Orbital momentum barrier factor (Blatt-Weisskopf functions)

Amplitude Analysis III

- They are added together as:

$$|\mathcal{M}|^2 = \sum_{\lambda_{\Lambda_b^0}} \sum_{\lambda_p} \sum_{\Delta\lambda_\mu} \left| \mathcal{M}_{\lambda_{\Lambda_b^0}, \lambda_p, \Delta\lambda_\mu}^{A*} + e^{i\Delta\lambda_\mu \alpha_\mu} \sum_{\lambda_p^{P_c}} d_{\lambda_p^{P_c}, \lambda_p}^{\frac{1}{2}}(\theta_p) \mathcal{M}_{\lambda_{\Lambda_b^0}, \lambda_p^{P_c}, \Delta\lambda_\mu}^{P_c} \right|^2$$

- α_μ and θ_p are rotation angles to align the final state helicity axes of the μ and p , as helicity frames used are different for the two decay chains.

cFit

- cFit uses events in $\pm 2\sigma$ window ($\sigma=7.52\text{MeV}$)
- Total PDF $\mathcal{P}(m_{Kp}, \Omega | \vec{\omega}) = (1 - \beta) \mathcal{P}_{\text{sig}}(m_{Kp}, \Omega | \vec{\omega}) + \beta \mathcal{P}_{\text{bkg}}(m_{Kp}, \Omega)$
- Background is described by sidebands 5σ - 13.5σ
- cFit minimizes

Background fraction $\beta=5.4\%$

$$-\ln \mathcal{L}(\vec{\omega}) = \sum_i \ln \left[|\mathcal{M}(m_{Kp\ i}, \Omega_i | \vec{\omega})|^2 + \frac{\beta I(\vec{\omega})}{(1 - \beta) I_{\text{bkg}}} \frac{\mathcal{P}_{\text{bkg}}^u(m_{Kp\ i}, \Omega_i)}{\Phi(m_{Kp\ i}) \epsilon(m_{Kp\ i}, \Omega_i)} \right] + N \ln I(\vec{\omega}) + \text{constant},$$

$$I_{\text{bkg}} \propto \sum_j w_j^{\text{MC}} \frac{\mathcal{P}_{\text{bkg}}^u(m_{Kp\ j}, \Omega_j)}{\Phi(m_{Kp\ i}) \epsilon(m_{Kp\ j}, \Omega_j)}$$

Signal efficiency parameterization becomes part of background parameterization,

effects only a tiny part of total PDF because of small β

sFit

- Signal PDF

$$\mathcal{P}_{\text{sig}}(m_{Kp}, \Omega | \vec{\omega}) = \frac{1}{I(\vec{\omega})} |\mathcal{M}(m_{Kp}, \Omega | \vec{\omega})|^2 \Phi(m_{Kp}) \epsilon(m_{Kp}, \Omega)$$

$\vec{\omega}$: fitting parameters
 Φ : phase-space = pq
 ϵ : efficiency

$$I(\vec{\omega}) \propto \sum_j^{N_{\text{MC}}} w_j^{\text{MC}} |\mathcal{M}(m_{Kpj}, \Omega_j | \vec{\omega})|^2$$

- Normalization calculated using simulated PHSP MC ($\Phi\epsilon$ included)
- w^{MC} discuss later

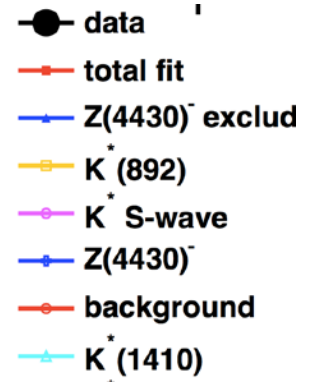
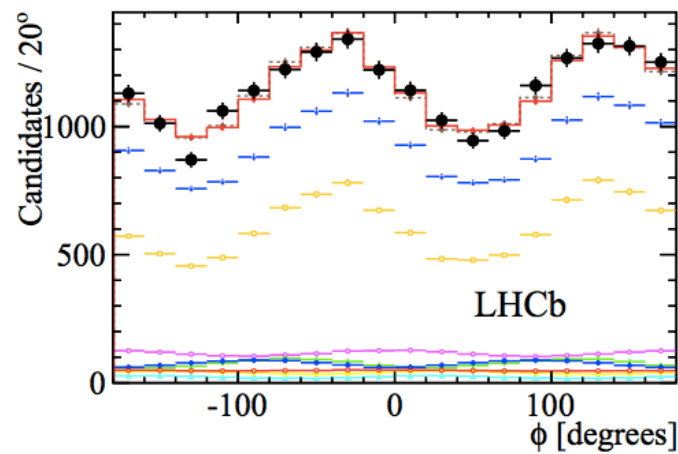
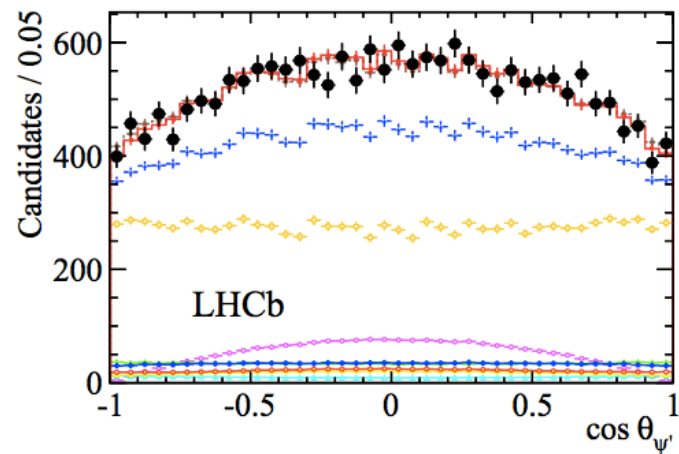
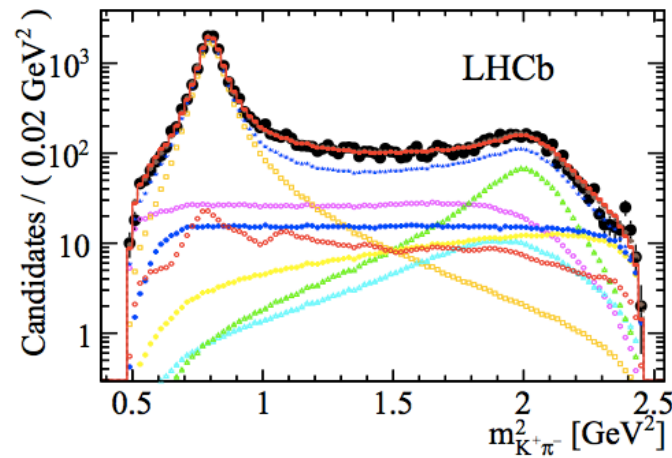
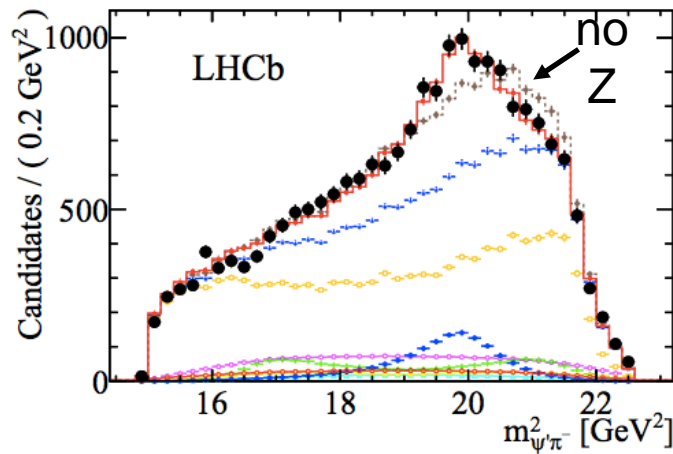
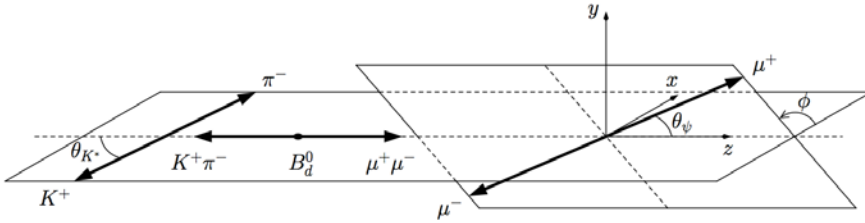
- sFit minimizes

$$\begin{aligned}
 -2 \ln \mathcal{L}(\vec{\omega}) &= -2s_W \sum_i W_i \ln \mathcal{P}_{\text{sig}}(m_{Kp\ i}, \Omega_i | \vec{\omega}) \\
 &= -2s_W \sum_i W_i \ln |\mathcal{M}(m_{Kp\ i}, \Omega_i | \vec{\omega})|^2 + 2s_W \ln I(\vec{\omega}) \sum_i W_i \\
 &\quad - 2s_W \sum_i W_i \ln [\Phi(m_{Kp\ i}) \epsilon(m_{Kp\ i}, \Omega_i)].
 \end{aligned}$$

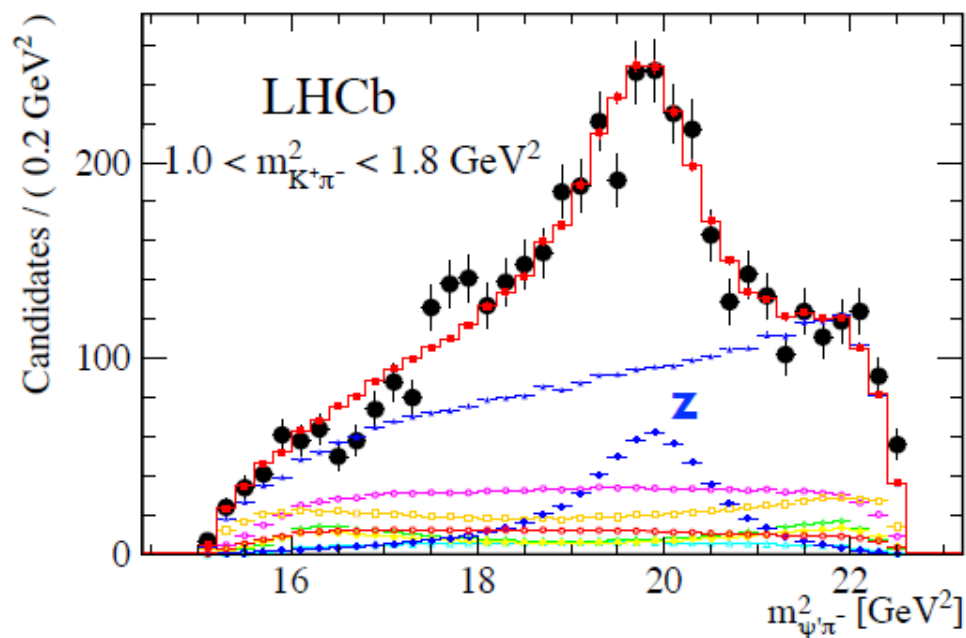
W_i is sWeights from m(J/ψKp) fits
 $s_W = \sum_i W_i / \sum_i W_i^2$ constant factor to correct uncertainty

Constant (invariant of $\vec{\omega}$), is dropped
 No need to know $\Phi\epsilon$ parameterization

4D Dalitz-Fit

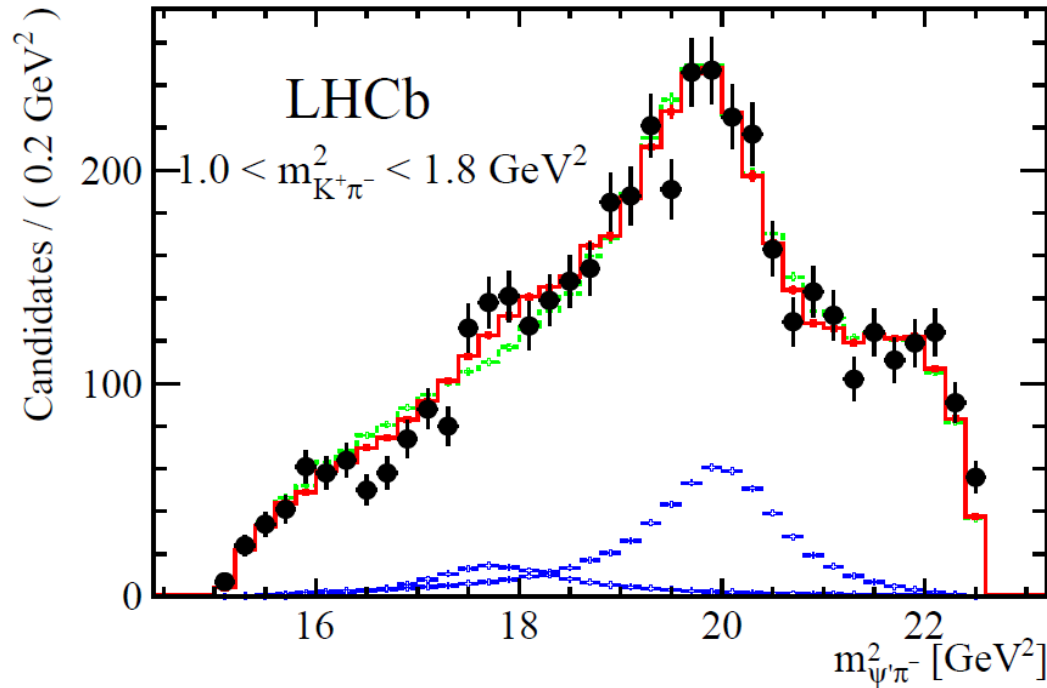


Resonances



State	Mass (MeV)	Width (MeV)	Fit Fraction (%)
Z_1^+	$4475 \pm 7^{+15}_{-25}$	$172 \pm 13^{+37}_{-34}$	$5.9 \pm 0.9^{+1.5}_{-3.3}$

Allowing two resonances



— 2 resonances: $J^P = 0^-$ and 1^+

— 1 resonance: $J^P = 1^+$

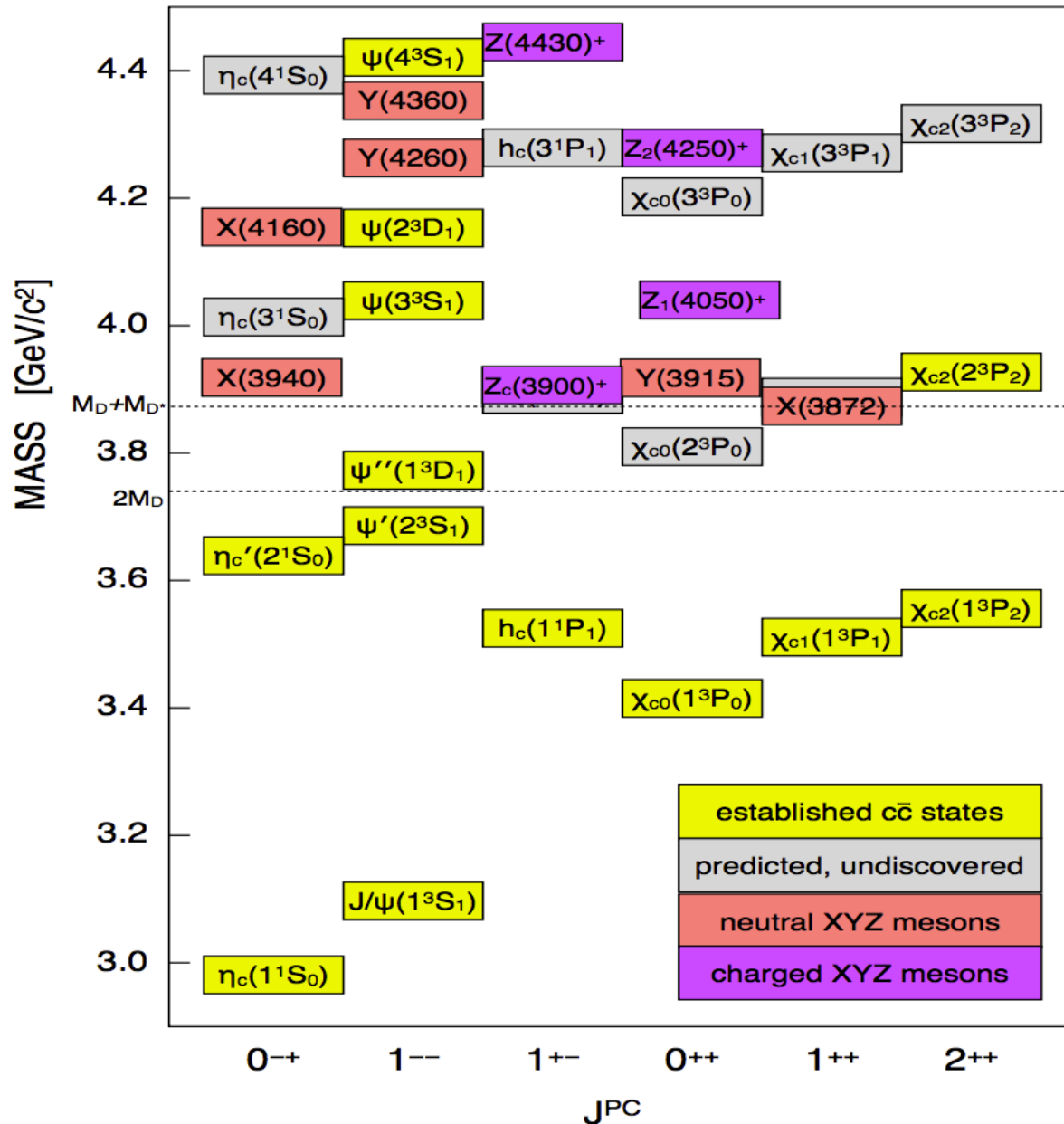
State	Mass (MeV)	Width (MeV)	Fit Fraction (%)
Z_0^+	$4239 \pm 18 \text{ }^{+45}_{-10}$	$220 \pm 47 \text{ }^{+108}_{-74}$	$1.6 \pm 0.5 \text{ }^{+1.9}_{-0.4}$

Open questions $Z^+(4430)$

Disfavoured J^P	Rejection level relative to 1^+ LHCb	Belle
0^-	9.7σ	3.4σ
1^-	15.8σ	3.7σ
2^+	16.1σ	5.1σ
2^-	14.6σ	4.7σ

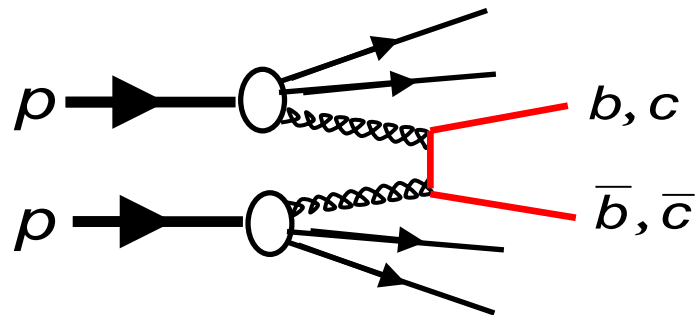
- $P=+$ rules out interpretation in terms of $\bar{D}^*(2010)D^*1(2420)$ molecule or threshold effect (cusp).
- Potential neutral **isospin partner?** $Z(4430)^0$ in $B^+ \rightarrow \psi' \pi^0 K^+$
- No clear picture of the complex system of charmonium-like exotic resonances.
- Further constraints will come from observing $Z(4430)^\pm$ and other exotics in alternative decay modes and/or production mechanisms.
- Look for synergies with the $s\bar{s}$ and $b\bar{b}$ sectors.

$c\bar{c}$ states



B-Physics at the Intensity Frontier

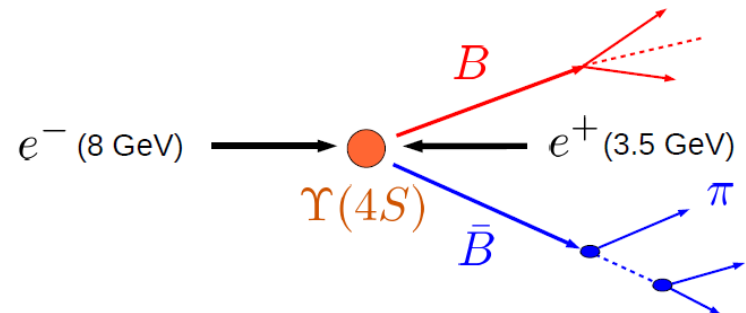
LHC @ 14 (13) TeV



$$\sigma_{bb}(14 \text{ TeV}) \approx 500 \mu\text{b}$$

$$\rightarrow 10^{10} b\bar{b} \text{ events/fb}^{-1}$$

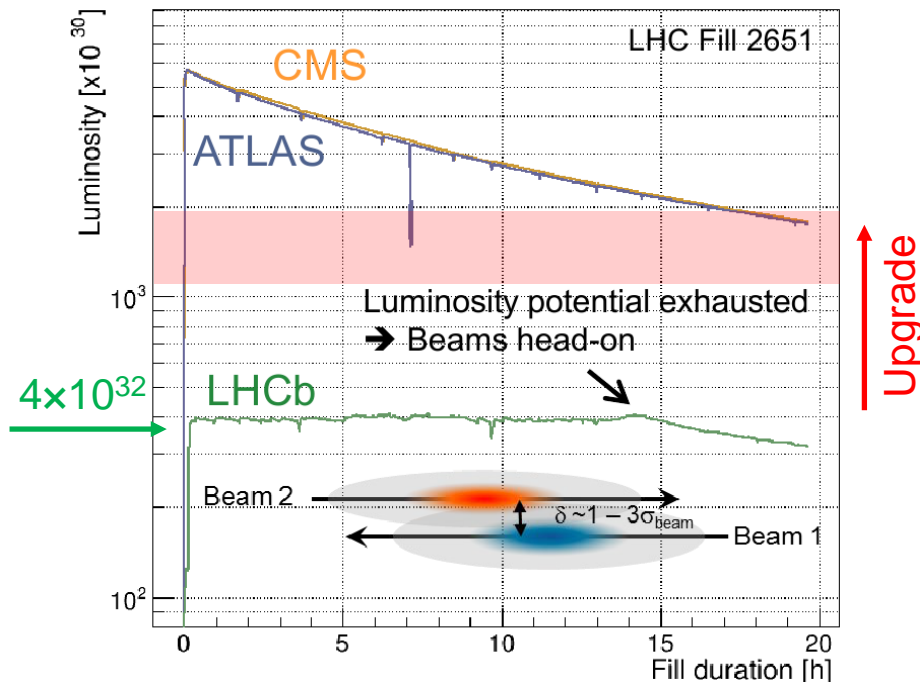
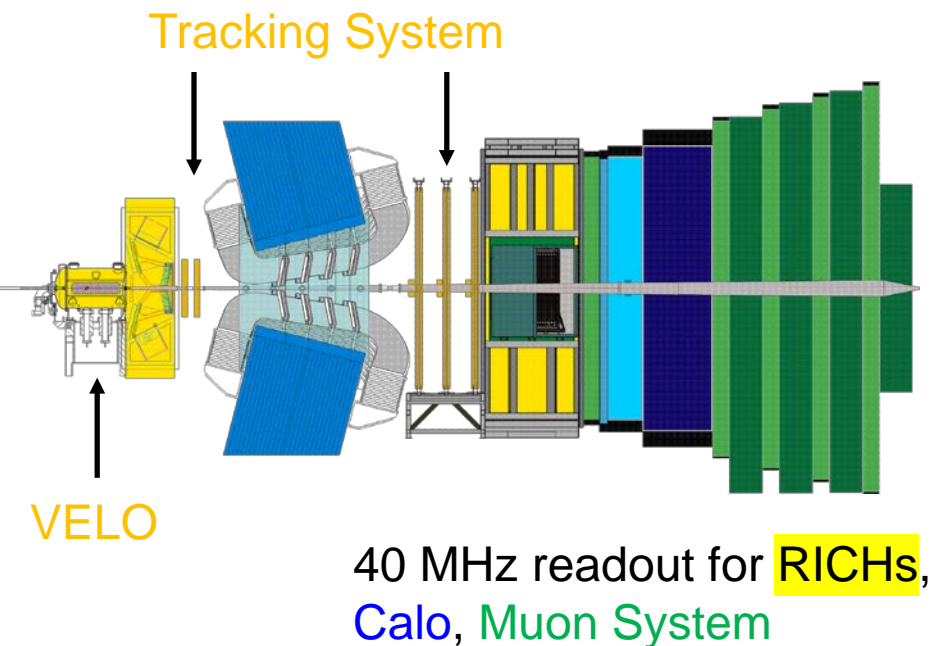
SuperKEKB & Belle II



$$\sigma_{BB} \approx 1 \text{ nb}$$

$$\rightarrow 10^9 B\bar{B} \text{ events/ab}^{-1}$$

	LHC era		High-lumi LHC era		
	2010-2012	2015-2018	2020-2022	2025-2028	2030+
ATLAS & CMS	25 fb ⁻¹	100 fb ⁻¹	300 fb ⁻¹	→	3000 fb ⁻¹
LHCb	3 fb ⁻¹	8 fb ⁻¹	23 fb ⁻¹	46 fb ⁻¹	100 fb ⁻¹
Belle II		0.5 ab ⁻¹	25 ab ⁻¹	50 ab ⁻¹	-



LHCb Upgrade:

- Increase levelled luminosity up to $2 \times 10^{33} \text{ cm}^{-2}\text{s}^{-1}$ (pile-up ~ 8):
- Fully flexible & efficient software trigger up to 40 MHz input
- Record 20 – 100 kHz
- Upgrade VELO and Tracker (adapt to higher occupancy and radiation load)

See also talk by Wander Baldini

Physics Complementarity*)

LHCb

ATLAS & CMS

- Rare decays: $B_{d,s} \rightarrow \mu\mu$
- B_s system
- b-baryons

- Spectroscopy

- CKM phases (β, γ)
 - Gluonic penguins
 - EW penguins
 - Charm physics
 - Semileptonics: Mixing, A_{SL}
- } Some only LHCb,
some only Belle II

On-going

Belle II

- Semileptonics: V_{xb}
- $B \rightarrow \tau \nu$, $D \tau \mu$,
- $B \rightarrow K^* \nu \nu$
- τ -physics

*) Caveat: I am probably missing “your” favored channel/field

Typical $b\bar{b}$ event

