

MASSIVE NEUTRINOS CIRCA 2017

Concha Gonzalez-Garcia

(ICREA U. Barcelona & YITP Stony Brook)

INTERNATIONAL SCHOOL OF NUCLEAR PHYSICS
Neutrinos in Cosmology, Astro-, Particle- and Nuclear Physics
Erice-Sicily: September 16-24, 2017

OUTLINE

The confirmed picture: 3ν Lepton Flavour Parameters

A partial list of Q&A

Neutrinos in the Standard Model

The SM is a gauge theory based on the symmetry group

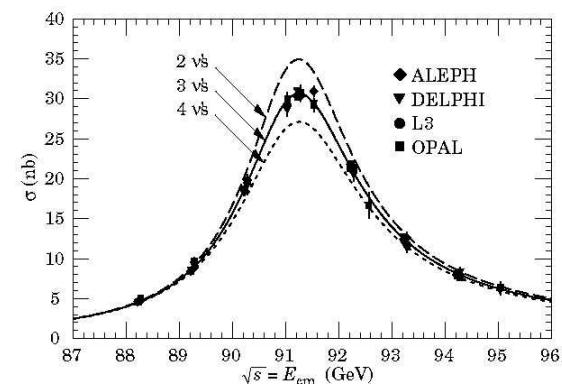
$$SU(3)_C \times SU(2)_L \times U(1)_Y \Rightarrow SU(3)_C \times U(1)_{EM}$$

With three generation of fermions

$(1, 2)_{-\frac{1}{2}}$	$(3, 2)_{\frac{1}{6}}$	$(1, 1)_{-1}$	$(3, 1)_{\frac{2}{3}}$	$(3, 1)_{-\frac{1}{3}}$
$\begin{pmatrix} \nu_e \\ e \end{pmatrix}_L \begin{pmatrix} u^i \\ d^i \end{pmatrix}_L$		e_R	u_R^i	d_R^i
$\begin{pmatrix} \nu_\mu \\ \mu \end{pmatrix}_L \begin{pmatrix} c^i \\ s^i \end{pmatrix}_L$		μ_R	c_R^i	s_R^i
$\begin{pmatrix} \nu_\tau \\ \tau \end{pmatrix}_L \begin{pmatrix} t^i \\ b^i \end{pmatrix}_L$		τ_R	t_R^i	b_R^i

There is no ν_R

Three and only three



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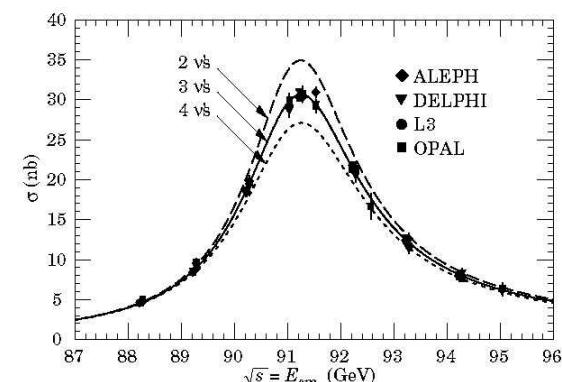


Accidental global symmetry: $B \times L_e \times L_\mu \times L_\tau$ (hence $L = L_e + L_\mu + L_\tau$)



ν strictly massless

Three and only three



- By 2017 we have observed with high (or good) precision:

- * Atmospheric ν_μ & $\bar{\nu}_\mu$ disappear most likely to ν_τ (**SK, MINOS, ICECUBE**)
- * Accel. ν_μ & $\bar{\nu}_\mu$ disappear at $L \sim 300/800$ Km (**K2K, T2K, MINOS, NO ν A**)
- * Some accelerator ν_μ appear as ν_e at $L \sim 300/800$ Km (**T2K, MINOS, NO ν A**)
- * Solar ν_e convert to ν_μ/ν_τ (**Cl, Ga, SK, SNO, Borexino**)
- * Reactor $\bar{\nu}_e$ disappear at $L \sim 200$ Km (**KamLAND**)
- * Reactor $\bar{\nu}_e$ disappear at $L \sim 1$ Km (**D-Chooz, Daya Bay, Reno**)

All this implies that L_α are violated

and There is Physics Beyond SM

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- The *starting* path:

Precise determination of the low energy parametrization

The New Minimal Standard Model

- Minimal Extension to allow for LFV \Rightarrow give Mass to the Neutrino

* Introduce ν_R AND impose L conservation \Rightarrow Dirac $\nu \neq \nu^c$:

$$\mathcal{L} = \mathcal{L}_{SM} - M_\nu \overline{\nu_L} \nu_R + h.c.$$

* NOT impose L conservation \Rightarrow Majorana $\nu = \nu^c$

$$\mathcal{L} = \mathcal{L}_{SM} - \frac{1}{2} M_\nu \overline{\nu_L} \nu_L^C + h.c.$$

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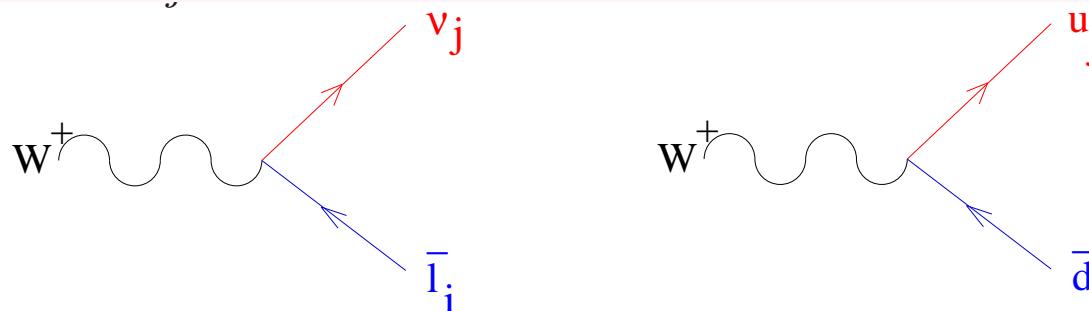
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- The charged current interactions of leptons are not diagonal (same as quarks)

$$\frac{g}{\sqrt{2}} W_\mu^+ \sum_{i,j} (U_{\text{LEP}}^{ij} \bar{\ell}^i \gamma^\mu L \nu^j + U_{\text{CKM}}^{ij} \bar{U}^i \gamma^\mu L D^j) + h.c.$$



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- In general for $N = 3 + s$ massive neutrinos U_{LEP} is $3 \times N$ matrix

$$U_{\text{LEP}} U_{\text{LEP}}^\dagger = I_{3 \times 3} \quad \text{but in general} \quad U_{\text{LEP}}^\dagger U_{\text{LEP}} \neq I_{N \times N}$$

- U_{LEP} : $3 + 3s$ angles + $2s + 1$ Dirac phases + $s + 2$ Majorana phases

ν Mass Oscillations in Vacuum

- If neutrinos have mass, a weak eigenstate $|\nu_\alpha\rangle$ produced in $l_\alpha + N \rightarrow \nu_\alpha + N'$

is a linear combination of the mass eigenstates ($|\nu_i\rangle$) : $|\nu_\alpha\rangle = \sum_{i=1}^n U_{\alpha i} |\nu_i\rangle$

- After a distance L it can be detected with flavour β with probability

$$P_{\alpha\beta} = \delta_{\alpha\beta} - 4 \sum_{j \neq i} \text{Re}[U_{\alpha i}^* U_{\beta i} U_{\alpha j} U_{\beta j}^*] \sin^2 \left(\frac{\Delta_{ij}}{2} \right) + 2 \sum_{j \neq i} \text{Im}[U_{\alpha i}^* U_{\beta i} U_{\alpha j} U_{\beta j}^*] \sin(\Delta_{ij})$$

$$\frac{\Delta_{ij}}{2} = \frac{(E_i - E_j)L}{2} = 1.27 \frac{(m_i^2 - m_j^2)}{\text{eV}^2} \frac{L/E}{\text{Km/GeV}}$$

No information on ν mass scale nor Majorana versus Dirac

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- When osc between 2- ν dominates:

$$P_{\alpha\alpha} = 1 - P_{osc} \quad \text{Disappear}$$

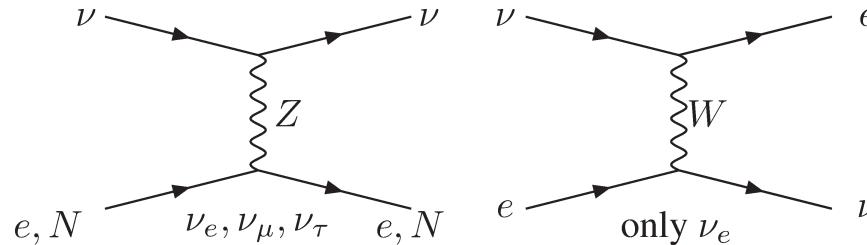
$$P_{osc} = \sin^2(2\theta) \sin^2 \left(1.27 \frac{\Delta m^2 L}{E} \right) \quad \text{Appear}$$

\Rightarrow No info on sign of Δm^2 and θ octant

Matter Effects

- If ν cross matter regions (Sun, Earth...) it interacts *coherently*

– But Different flavours
have different interactions :



\Rightarrow Effective potential in ν evolution : $V_e \neq V_{\mu, \tau} \Rightarrow \Delta V^\nu = -\Delta V^{\bar{\nu}} = \sqrt{2}G_F N_e$

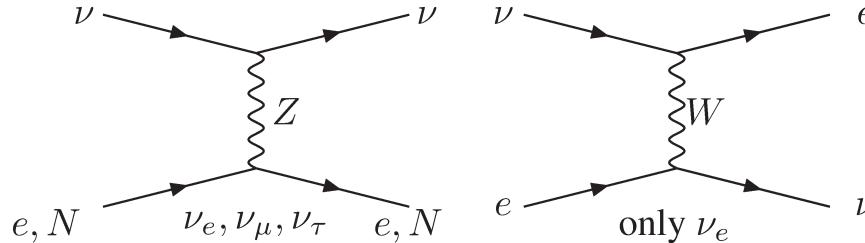
$$-i \frac{\partial}{\partial x} \begin{pmatrix} \nu_e \\ \nu_X \end{pmatrix} = \left[\begin{pmatrix} V_e - V_X - \frac{\Delta m^2}{4E} \cos 2\theta & \frac{\Delta m^2}{4E} \sin 2\theta \\ \frac{\Delta m^2}{4E} \sin 2\theta & V_X + \frac{\Delta m^2}{4E} \cos 2\theta \end{pmatrix} \right] \begin{pmatrix} \nu_e \\ \nu_X \end{pmatrix}$$

\Rightarrow Modification of mixing angle and oscillation wavelength (MSW)

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\Rightarrow Modification of mixing angle and oscillation wavelength (MSW)

- Mass difference and mixing in matter:

$$\Delta m_m^2 = \sqrt{(\Delta m^2 \cos 2\theta - 2E\Delta V)^2 + (\Delta m^2 \sin 2\theta)^2}$$

$$\sin(2\theta_m) = \frac{\Delta m^2 \sin(2\theta)}{\Delta m_{mat}^2}$$

\Rightarrow For solar ν' s in adiabatic regime

$$P_{ee} = \frac{1}{2} [1 + \cos(2\theta_m) \cos(2\theta)]$$

Dependence on θ octant

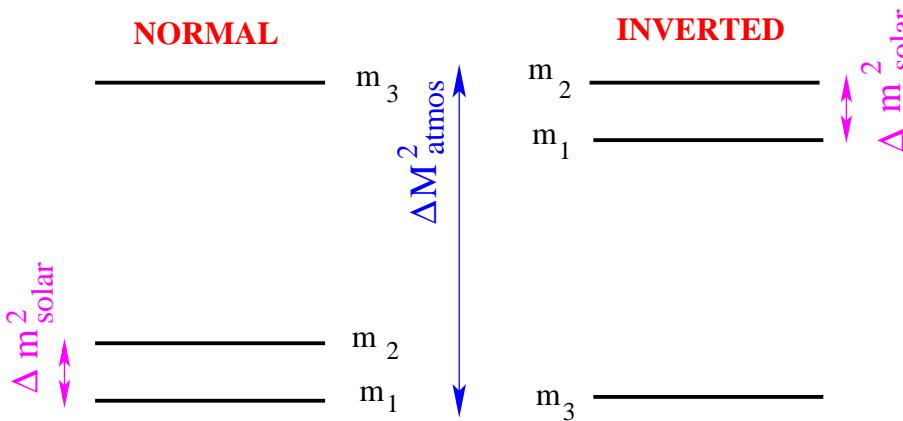
\Rightarrow In LBL terrestrial experiments

Dependence on sign of Δm^2
and θ octant

3 ν Flavour Parameters

- For 3 ν 's : 3 Mixing angles + 1 Dirac Phase + 2 Majorana Phases

$$U_{\text{LEP}} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix} \begin{pmatrix} c_{13} & 0 & s_{13}e^{i\delta_{\text{CP}}} \\ 0 & 1 & 0 \\ -s_{13}e^{-i\delta_{\text{CP}}} & 0 & c_{13} \end{pmatrix} \begin{pmatrix} c_{21} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} e^{i\eta_1} & 0 & 0 \\ 0 & e^{i\eta_2} & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

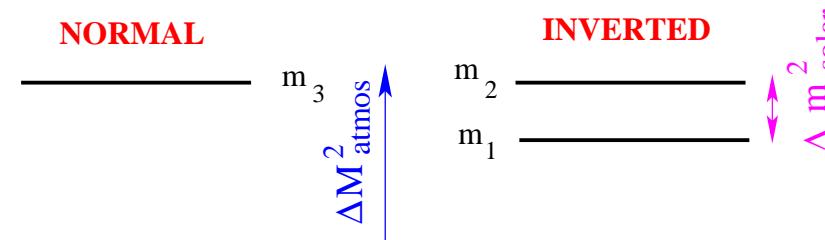


- Two Possible Orderings

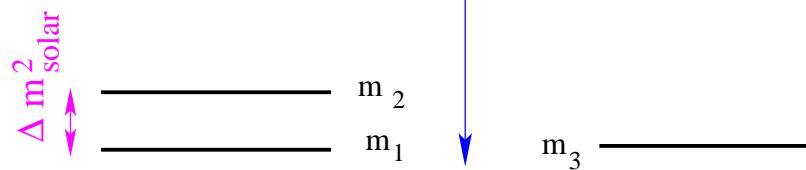
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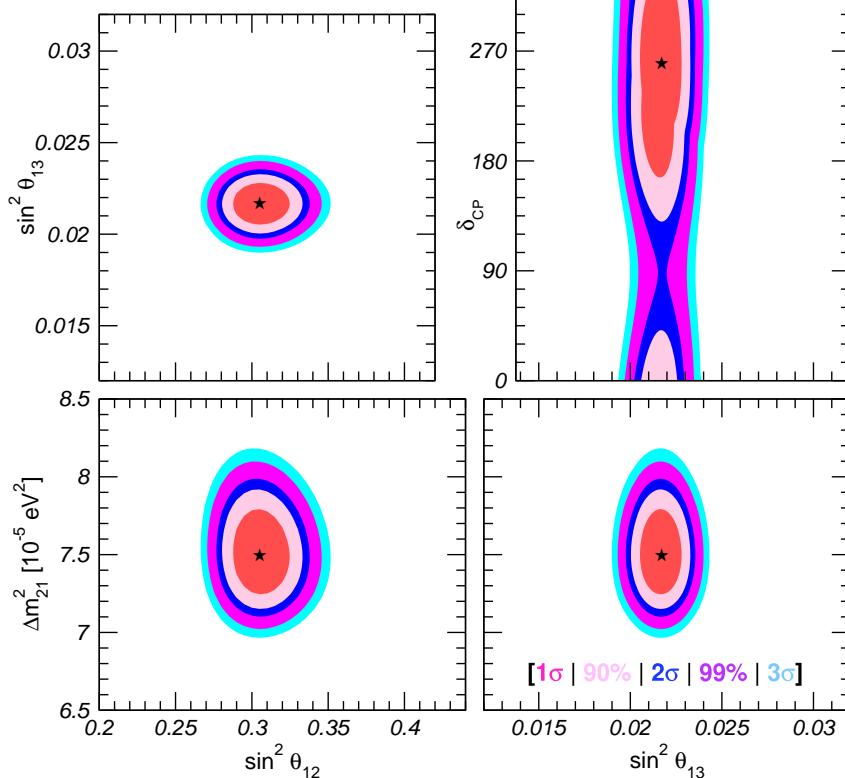
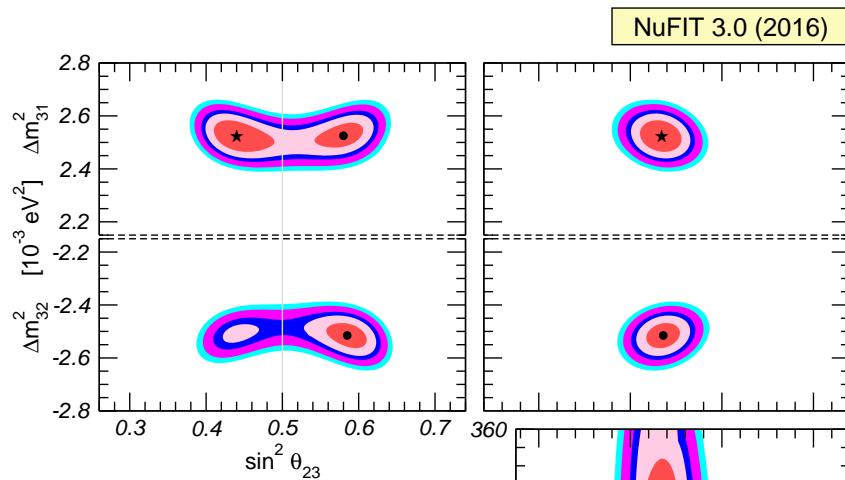
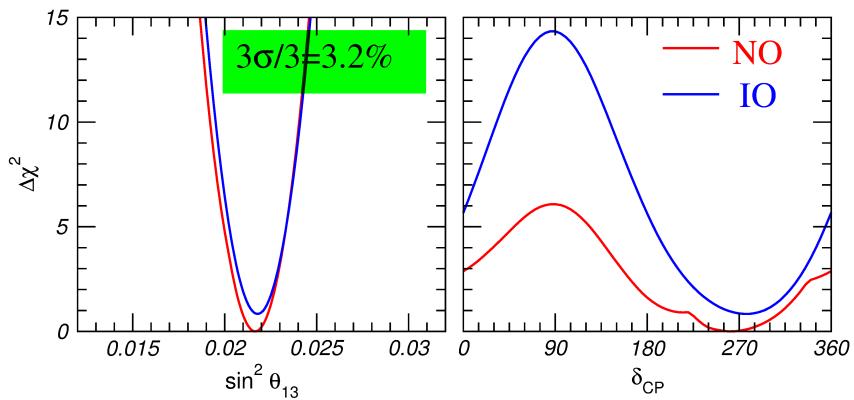
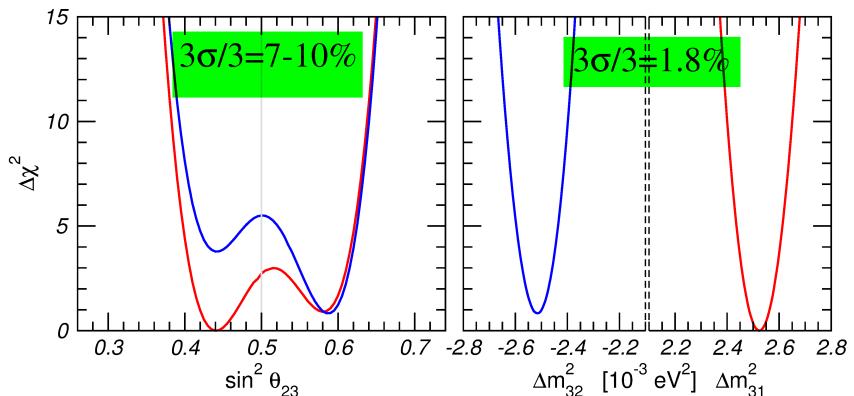
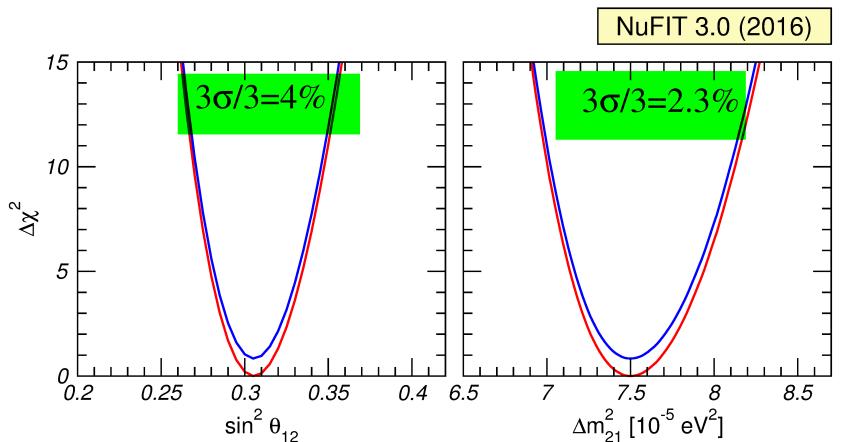
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Experiment	Dominant Dependence	Important Dependence
Solar Experiments	$\rightarrow \theta_{12}$	$\Delta m_{21}^2, \theta_{13}$
Reactor LBL (KamLAND)	$\rightarrow \Delta m_{21}^2$	θ_{12}, θ_{13}
Reactor MBL (Daya Bay, Reno, D-Chooz)	$\rightarrow \theta_{13}$	Δm_{atm}^2
Atmospheric Experiments	$\rightarrow \theta_{23}$	$\Delta m_{\text{atm}}^2, \theta_{13}, \delta_{\text{CP}}$
Acc LBL ν_μ Disapp (Minos, T2K, NOvA)	$\rightarrow \Delta m_{\text{atm}}^2$	θ_{23}
Acc LBL ν_e App (Minos, T2K, NOvA)	$\rightarrow \theta_{13}$	$\delta_{\text{CP}}, \theta_{23}$

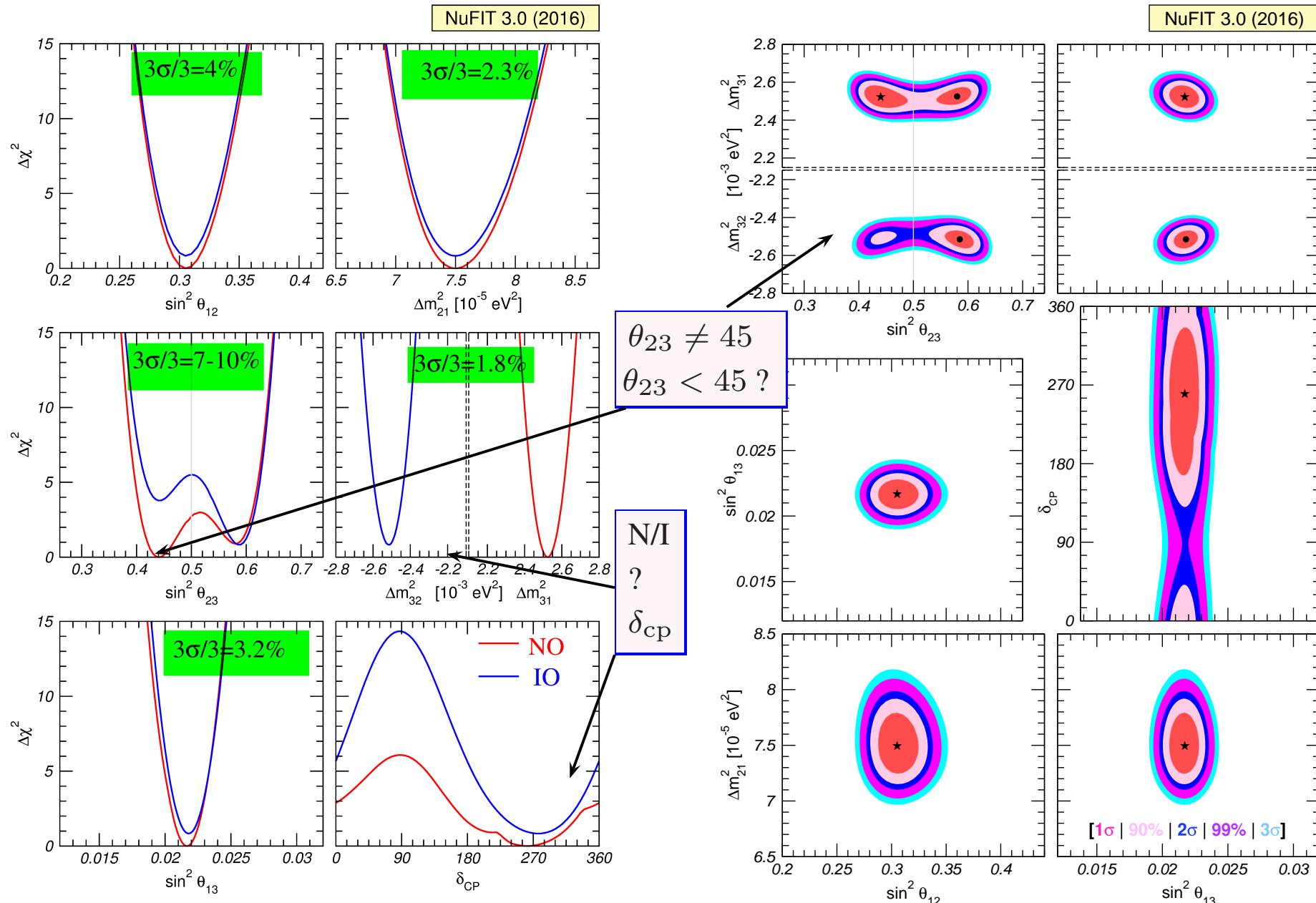
Global 6-parameter fit <http://www.nu-fit.org>

Esteban, Maltoni, Martinez-Soler, Schwetz, MCG-G ArXiv:1611:01514



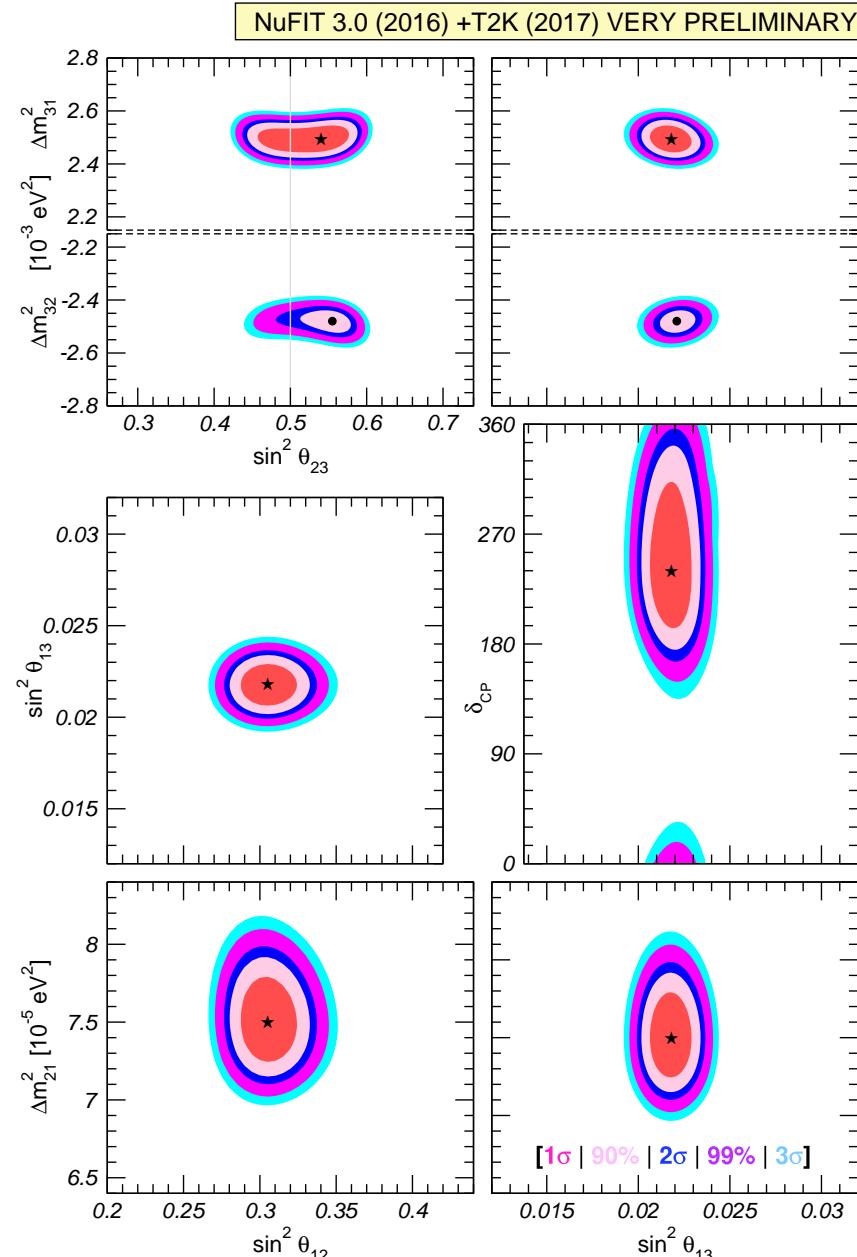
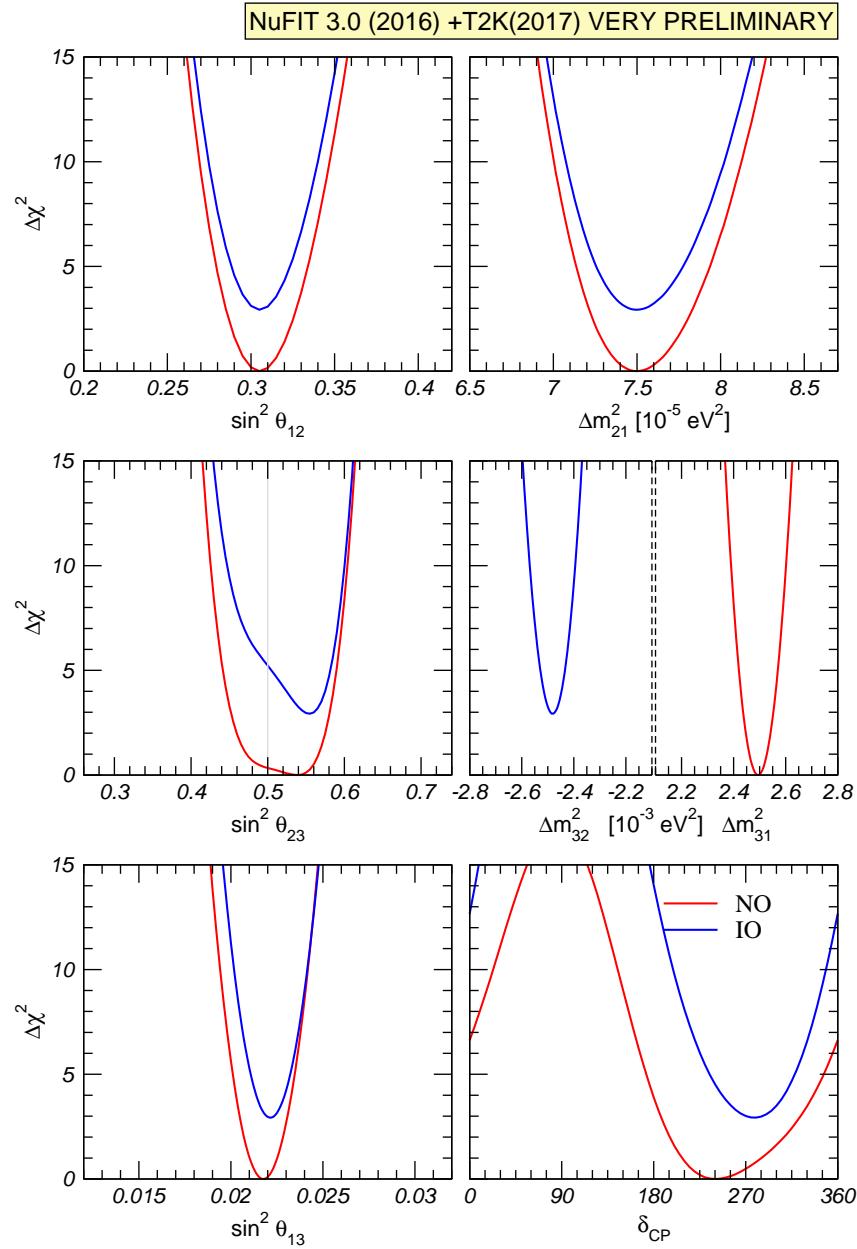
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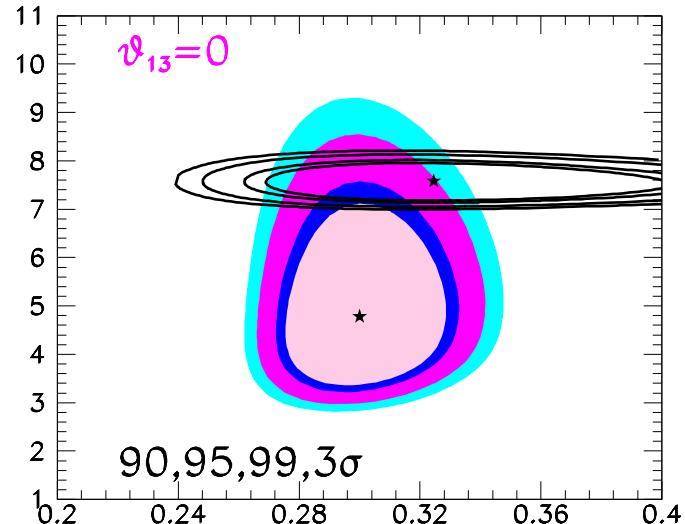
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Esteban, Maltoni, Martinez-Soler, Schwetz, MCG-G effect OF T2K (2017) VERY PRELIMINARY



3 ν Analysis: “12” Sector and θ_{13}

- For $\theta_{13} = 0$



- When θ_{13} increases

$$P_{ee} \simeq \begin{cases} \text{Solar High E : } c_{13}^4 \sin^2 2\theta_{12} \\ \text{Solar Low E : } c_{13}^4 \left(1 - \sin^2 2\theta_{12}/2\right) \\ \text{Kam : } c_{13}^4 \left(1 - \sin^2 2\theta_{12} \sin^2 \frac{\Delta m_{21}^2 L}{4E}\right) \end{cases}$$

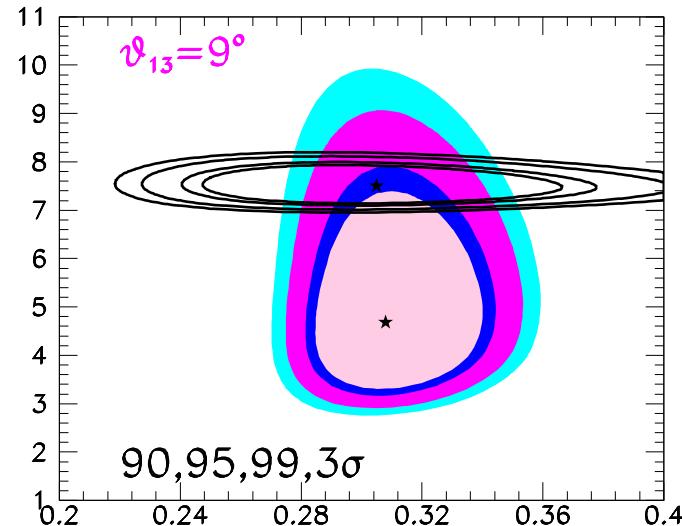
⇒ KamLAND region shifts left

⇒ Solar slight shifts right (due to High E)

$$\sin^2 \theta_{12} = \begin{cases} 0.3 \text{ From Solar} \\ 0.325 \text{ From KLAND} \end{cases}$$

3 ν Analysis: “12” Sector and θ_{13}

- For $\theta_{13} \simeq 9^\circ$

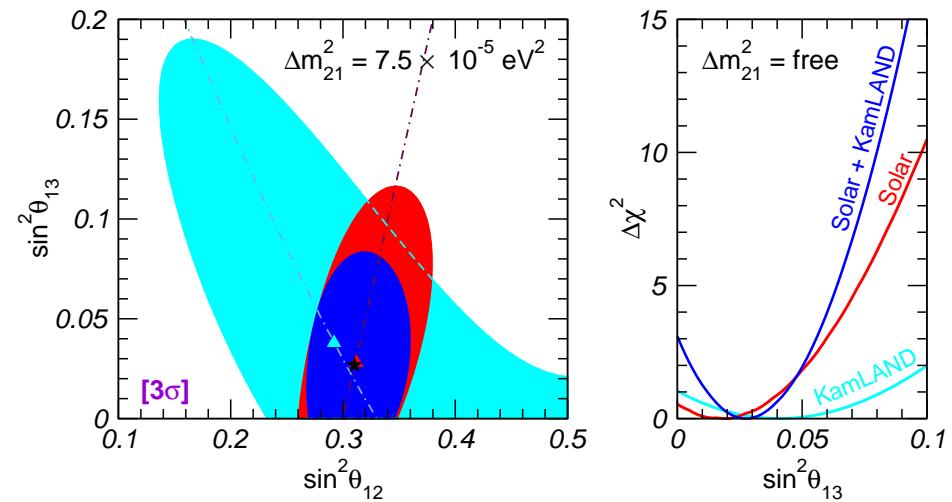


- ⇒ Good match of best fit θ_{12}
 ⇒ Residual tension on Δm_{21}^2

- When θ_{13} increases

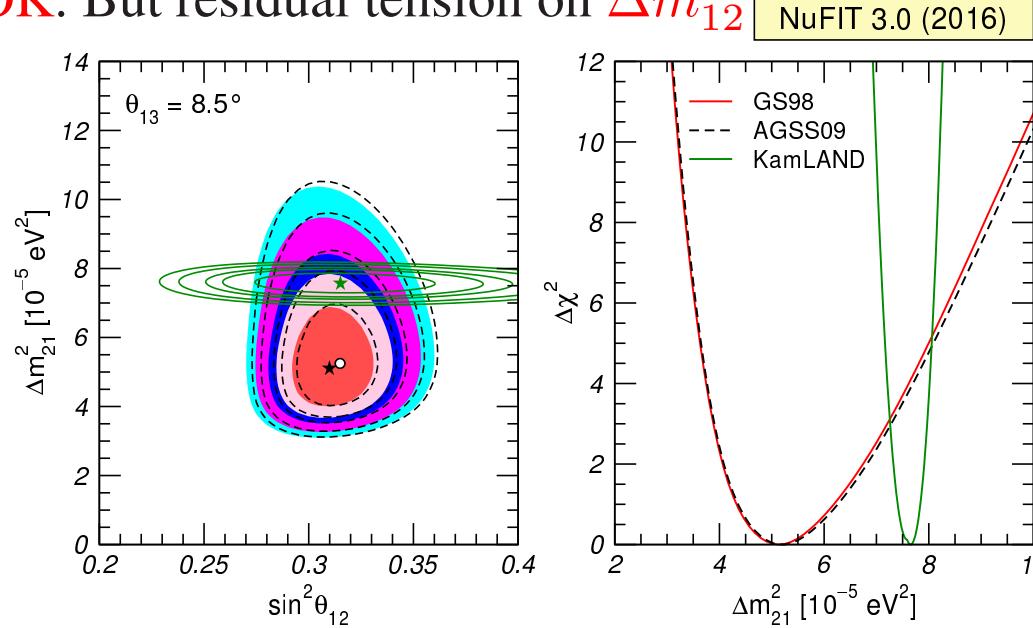
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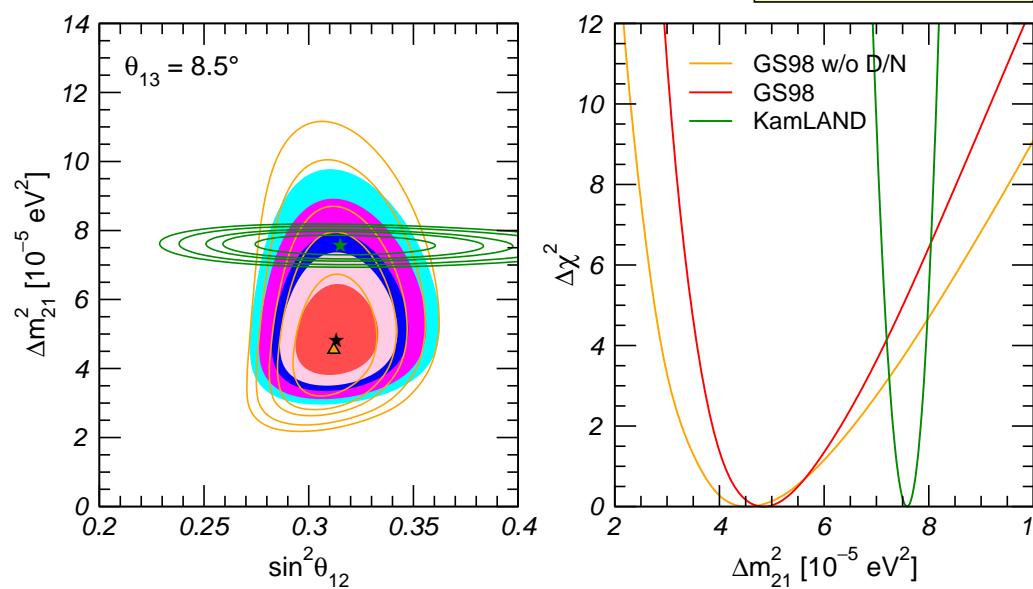
3 ν Analysis: Δm_{21}^2 KamLAND vs SOLAR

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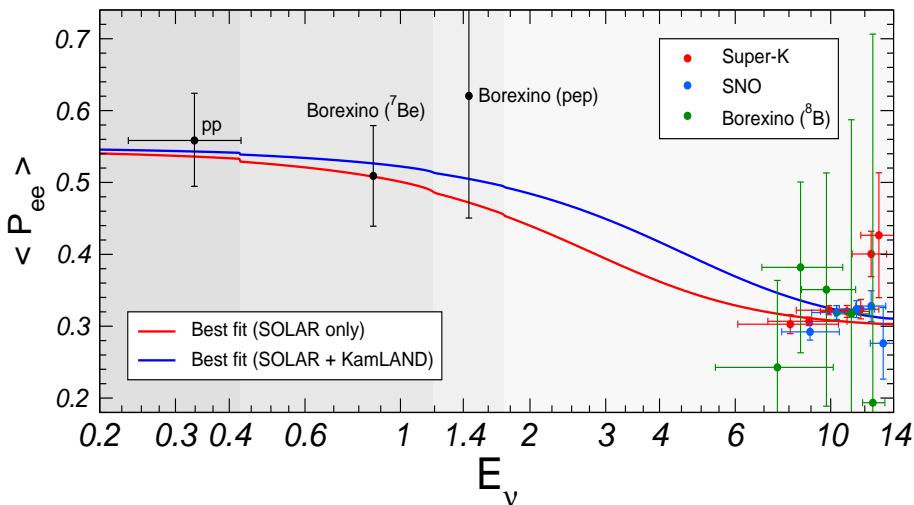


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Tension related to: a) “too large” of Day/Night at SK



b) smaller-than-expected low-E turn up from MSW at best global fit

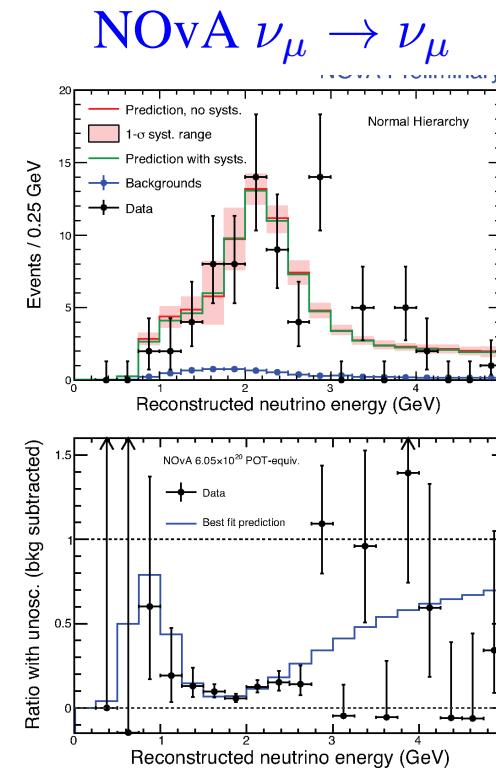
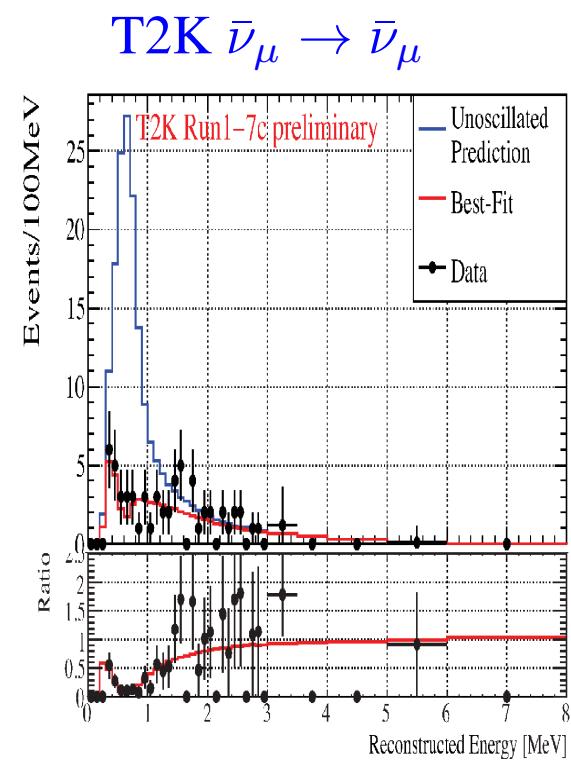
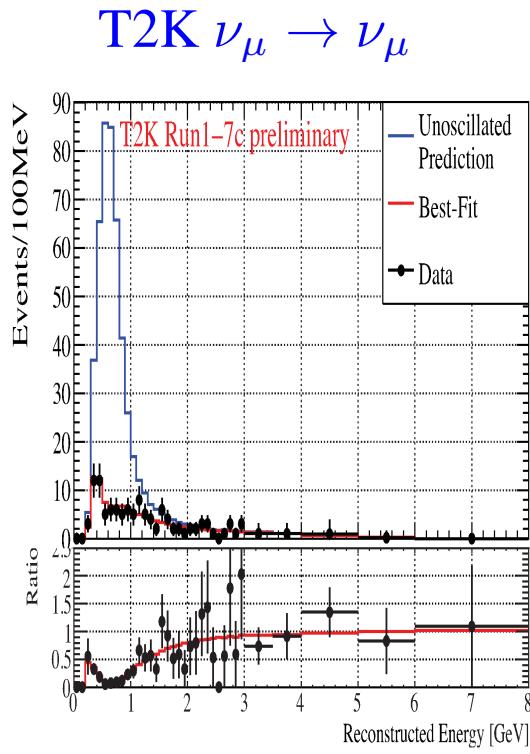
Modified matter potential? More latter ...

3 ν Analysis: θ_{23}

- Best determined in ν_μ and $\bar{\nu}_\mu$ disappearance in LBL

$$P_{\mu\mu} \simeq 1 - (c_{13}^4 \sin^2 2\theta_{23} + s_{23}^2 \sin^2 2\theta_{13}) \sin^2 \left(\frac{\Delta m_{31}^2 L}{4E} \right) + \mathcal{O}(\Delta m_{21}^2)$$

- At osc maximum $\sin^2 \left(\frac{\Delta m_{31}^2 L}{4E} \right) = 1 \Rightarrow P_{\mu\mu} \simeq 0$ for $\theta_{23} \simeq \frac{\pi}{4}$

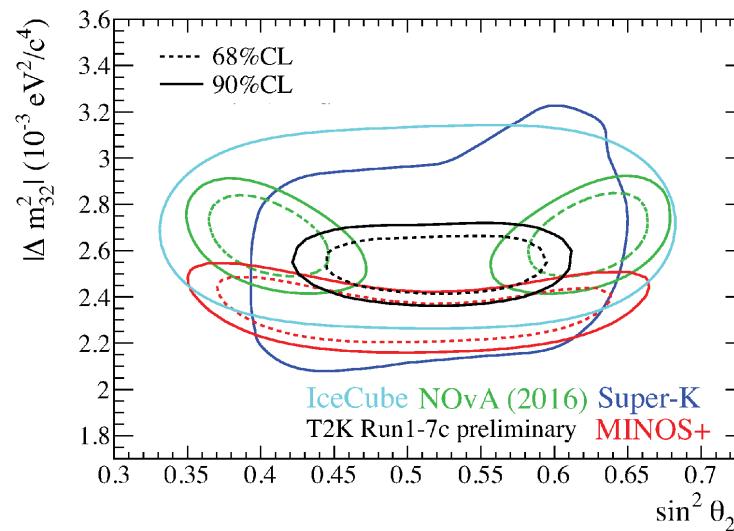


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- Allowed regions by the different experiments:



In making this figure θ_{13} is constrained by prior from reactor data

Caution: Not the same using θ_{13} reactor prior than combining with reactor results
(because of Δm_{32}^2 in reactors)

Δm_{23}^2 in LBL vs Reactors

- At LBL determined in ν_μ and $\bar{\nu}_\mu$ disappearance spectrum

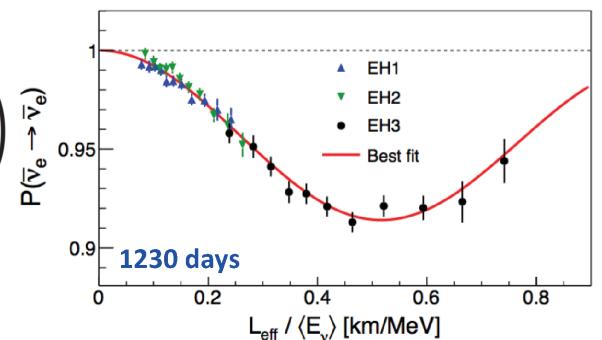
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- At MBL Reactors (Daya-Bay, Reno, D-Chooz) determined in $\bar{\nu}_e$ disapp spectrum

$$P_{ee} \simeq 1 - \sin^2 2\theta_{13} \sin^2 \left(\frac{\Delta m_{ee}^2 L}{4E} \right) - c_{13}^4 \sin^2 2\theta_{12} \sin^2 \left(\frac{\Delta m_{21}^2 L}{4E} \right)$$

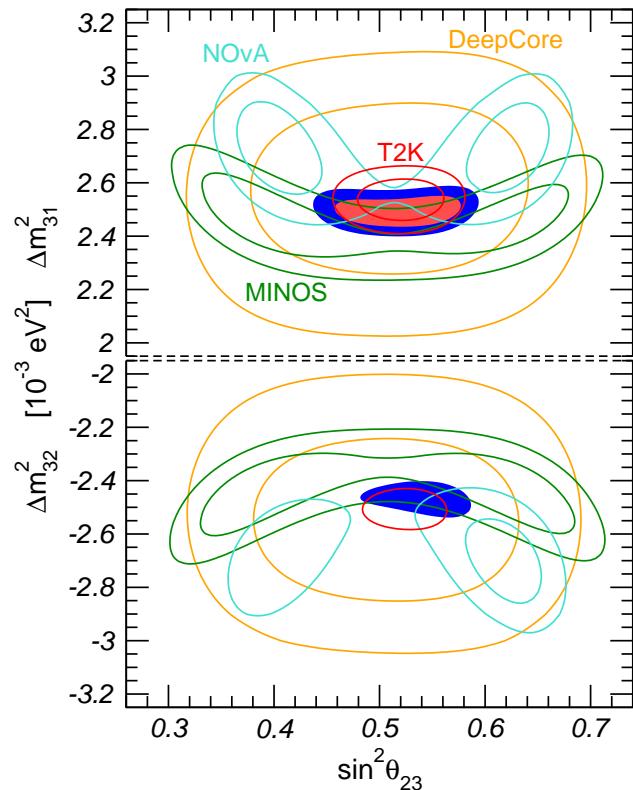
$$\Delta m_{ee}^2 \simeq |\Delta m_{32}^2| \pm c_{12}^2 \Delta m_{21}^2 \simeq |\Delta m_{32}^2| \pm 0.05 \times 10^{-3} \text{ eV}^2$$

Nunokawa,Parke,Zukanovich (2005)

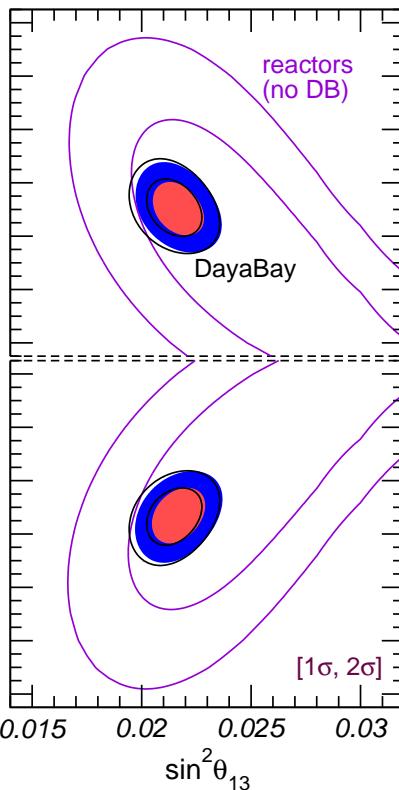


Δm_{23}^2 in LBL vs Reactors: Consistency

- At LBL determined in ν_μ and $\bar{\nu}_\mu$ disappearance spectrum
- At MBL Reactors (Daya-Bay, Reno, D-Chooz) determined in $\bar{\nu}_e$ disapp spectrum

LBL ν_μ disappearanceREAC $\bar{\nu}_e$ disappearance

Sept (2017) PRELIM



- Consistent values of $|\Delta m_{32}^2|$
- Hint for non-maximal θ_{23} driven by NO ν A and MINOS
- T2K (2017) slight fav $\theta_{23} > 45$

Leptonic CP Violation

- Leptonic CP $\Rightarrow P_{\nu_\alpha \rightarrow \nu_\beta} \neq P_{\bar{\nu}_\alpha \rightarrow \bar{\nu}_\beta}$:

$$P_{\nu_\alpha \rightarrow \nu_\beta} - P_{\bar{\nu}_\alpha \rightarrow \bar{\nu}_\beta} \propto J \quad \text{with} \quad J = \text{Im}(U_{\alpha 1} U_{\alpha 2}^* U_{\beta 2} U_{\beta 1}^*) = J_{\text{LEP,CP}}^{\max} \sin \delta_{\text{CP}}$$

$$J_{\text{LEP,CP}}^{\max} = \frac{1}{8} c_{13} \sin^2 2\theta_{13} \sin^2 2\theta_{23} \sin^2 2\theta_{12}$$

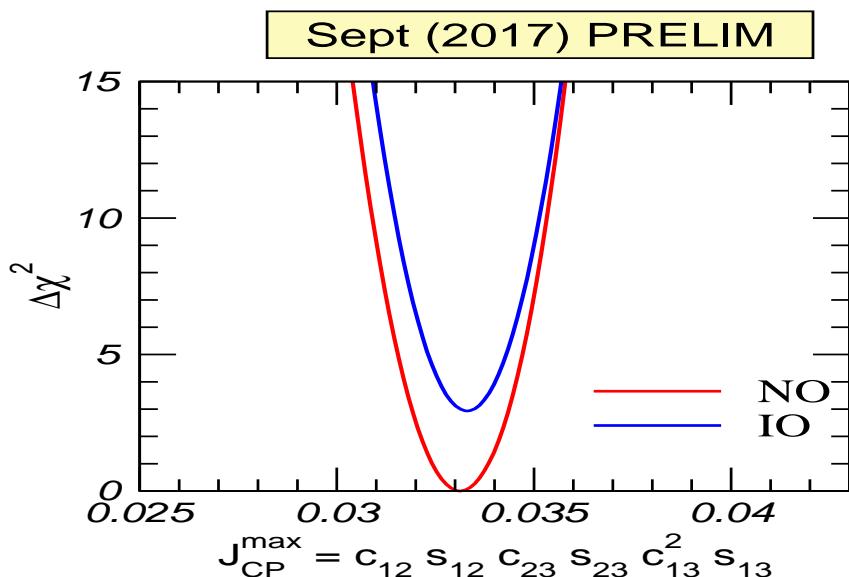
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- Maximum Allowed Leptonic CPV:



$$J_{\text{LEP,CP}}^{\max} = (3.29 \pm 0.07) \times 10^{-2}$$

to compare with

$$J_{\text{CKM,CP}} = (3.04 \pm 0.21) \times 10^{-5}$$

\Rightarrow Leptonic CPV may be largest CPV
in New Minimal SM

if $\sin \delta_{\text{CP}}$ not too small

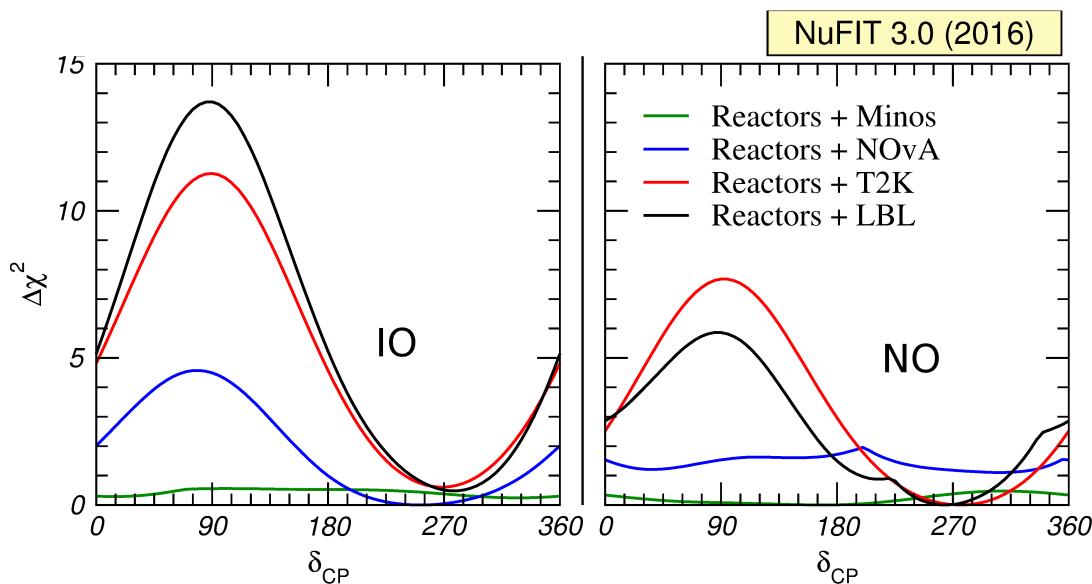
Leptonic CP Phase

- Leptonic CPV Phase: Mainly from $\nu_\mu \rightarrow \nu_e$ in LBL (complicated by matter effects)

$$P_{\mu e} \simeq s_{23}^2 \sin^2 2\theta_{13} \left(\frac{\Delta_{31}}{B_\mp} \right)^2 \sin^2 \left(\frac{B_\mp L}{2} \right) + 8 J_{\text{LEP,CP}}^{\max} \frac{\Delta_{12}}{V_E} \frac{\Delta_{31}}{B_\mp} \sin \left(\frac{V_E L}{2} \right) \sin \left(\frac{B_\mp L}{2} \right) \cos \left(\frac{\Delta_{31} L}{2} \pm \delta_{\text{CP}} \right)$$

$$\Delta_{ij} = \frac{\Delta m_{ij}^2}{2E} \quad B_\pm = \Delta_{31} \pm V_E \quad J_{\text{LEP,CP}}^{\max} = \frac{1}{8} c_{13} \sin^2 2\theta_{13} \sin^2 2\theta_{23} \sin^2 2\theta_{12}$$

Before T2K (2017)



- Best fit $\delta_{\text{CP}} \sim 270^\circ$
- CP conserv at 70% (NO), 97% (IO)
- Driven by “fluctuation” in T2K

Mass hierarchy	ν_e		$\bar{\nu}_e$	
	Normal	Inverted	Normal	Inverted
$\delta_{\text{CP}} = -\pi/2$	28.8	25.5	6.0	6.5
$\delta_{\text{CP}} = 0$	24.2	21.2	6.9	7.4
$\delta_{\text{CP}} = \pi/2$	19.7	17.2	7.7	8.4
$\delta_{\text{CP}} = \pm\pi$	24.2	21.6	6.8	7.4
Data	32		4	

⇒ One concluded :
Significance may not grow soon

Leptonic CP Phase:T2K 2017

Accumulated 14.7×10^{20} protons-on-target (POT) in neutrino mode and 7.6×10^{20} POT in antineutrino mode - full data set presented here

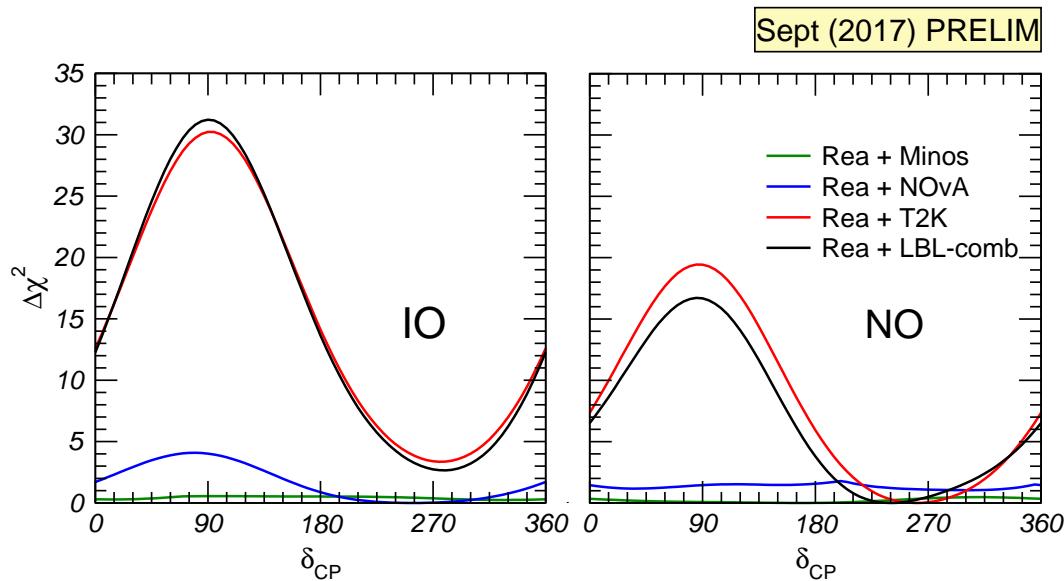
- 29% of the approved T2K POT

	Sample	Predicted Rates				Observed Rates
		$\delta_{cp} = -\pi/2$	$\delta_{cp} = 0$	$\delta_{cp} = \pi/2$	$\delta_{cp} = \pi$	
ν_e	CCQE 1-Ring e-like FHC	73.5	61.5	49.9	62.0	74
	CC1 π 1-Ring e-like FHC	6.92	6.01	4.87	5.78	15
$\overline{\nu}_e$	CCQE 1-Ring e-like RHC	7.93	9.04	10.04	8.93	7
	CCQE 1-Ring μ -like FHC	267.8	267.4	267.7	268.2	240
ν_μ	CCQE 1-Ring μ -like RHC	63.1	62.9	63.1	63.1	68

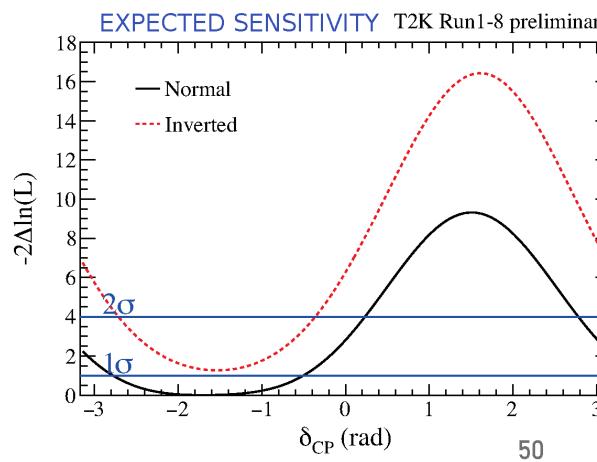
M. Hartz, KeK colloquim, August 2017

Leptonic CP Phase

Including T2K (2017) PRELIMINARY



- Best fit at $\delta_{\text{CP}} \sim 240^\circ$
 - CP conserv at 95% (NO)
 - 15° – 160° disfavoured at $\Delta\chi^2 > 9$
 - Still more than expected sensitiv in T2K
 - $\chi^2_{\text{min,IO}} - \chi^2_{\text{min,NO}} \simeq 3$



Leptonic CP Violation

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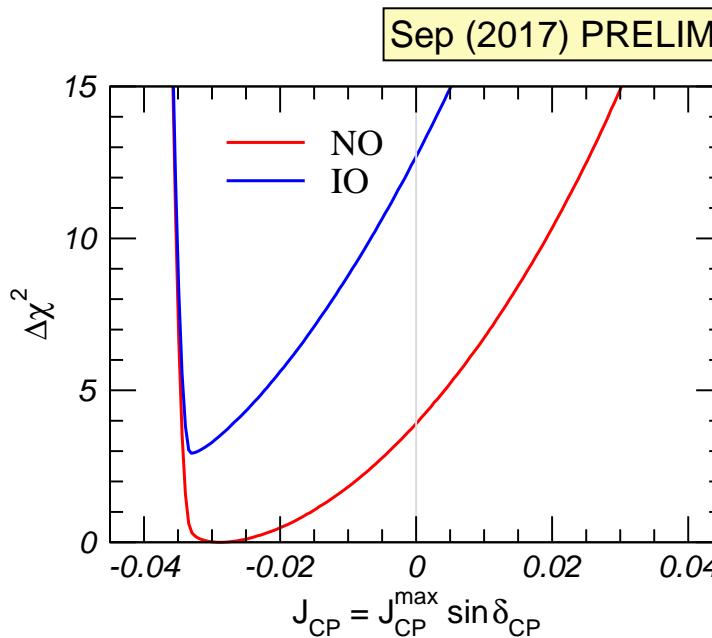
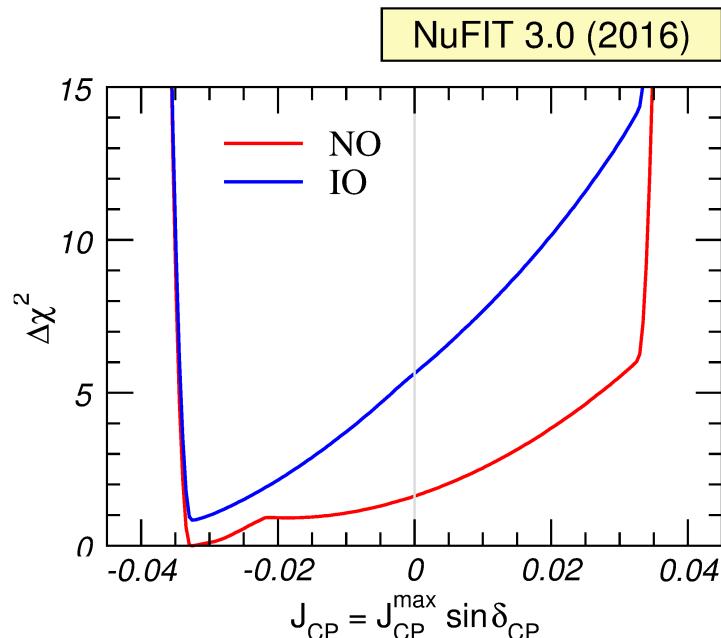
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- Leptonic Jarlskog Invariant : Best fit $J_{\text{LEP,CP}} = -0.030$



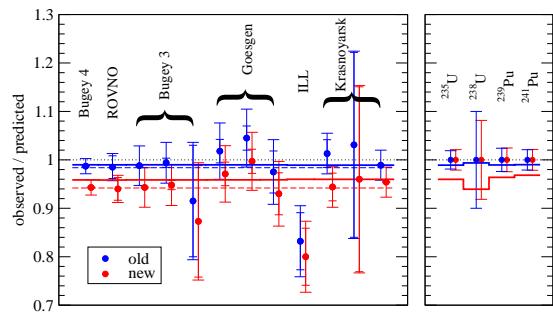
Confirmed Low Energy Picture and MY List of Q&A

- At least two neutrinos are massive \Rightarrow There is NP
- Three mixing angles are non-zero (and relatively large) \Rightarrow very different from CKM
- Leptonic CP: Best fit $J_{\text{Lep,CP}} = -0.033$. CP conservation at 95% CL
- Ordering: No significant preference yet
 - Requires new oscillation experiments
- Oscillations DO NOT determine the lightest mass
 - Only model independent probe of m_ν β decay: $\sum m_i^2 |U_{ei}|^2 \leq (2.2 \text{ eV})^2$
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- Dirac or Majorana?: We do not know, anxiously waiting for ν -less $\beta\beta$ decay
- Only three light states?

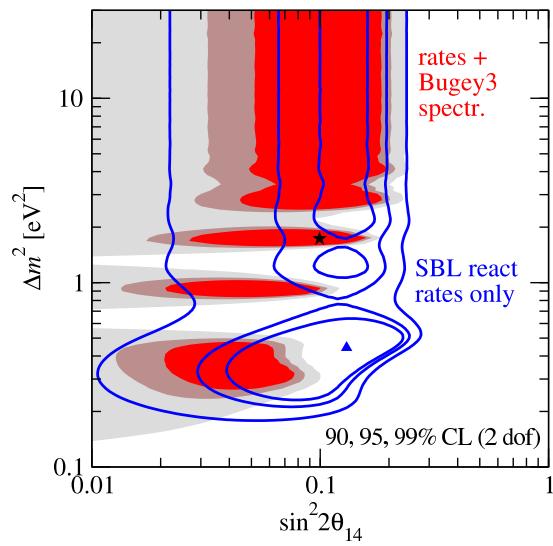
- Several **Observations** which can be Interpreted as **Oscillations** with $\Delta m^2 \sim \text{eV}^2$

Reactor Anomaly

New reactor flux calculation
 \Rightarrow Deficit in data at $L \lesssim 100$ m



Explained as ν_e disappearance

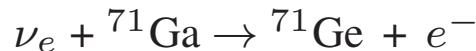


Kopp et al, ArXiv 1303.3011

Gallium Anomaly

Acero, Giunti, Laveder, 0711.4222
 Giunti, Laveder, 1006.3244

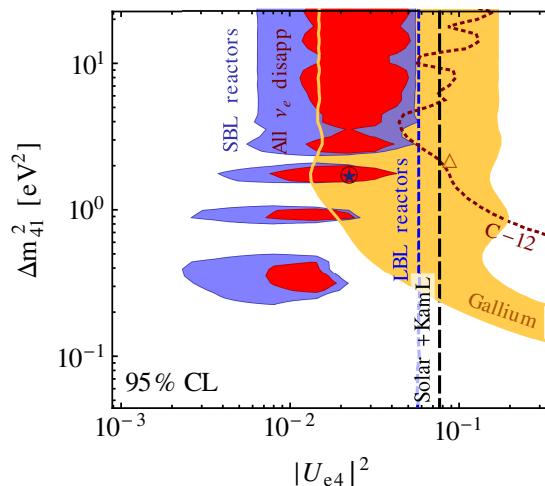
Radioactive Sources (^{51}Cr , ^{37}Ar)
 in calibration of Ga Solar Exp;



Give a rate lower than expected

$$R = \frac{N_{\text{obs}}}{N_{\text{Bahc}}^{\text{th}}} = 0.86 \pm 0.05 \quad (2.8\sigma)$$

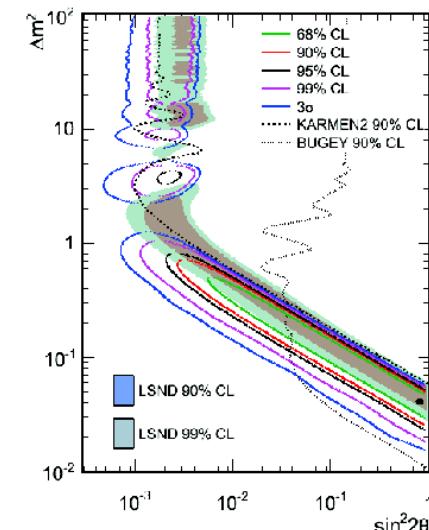
Explained as ν_e disappearance



Kopp et al, ArXiv 1303.3011

LSND, MiniBoone

$\nu_\mu \rightarrow \nu_e$ and $\bar{\nu}_\mu \rightarrow \bar{\nu}_e$



Light Sterile Neutrinos

- These explanations require $3+N_s$ mass eigenstates $\rightarrow N_s$ sterile neutrinos

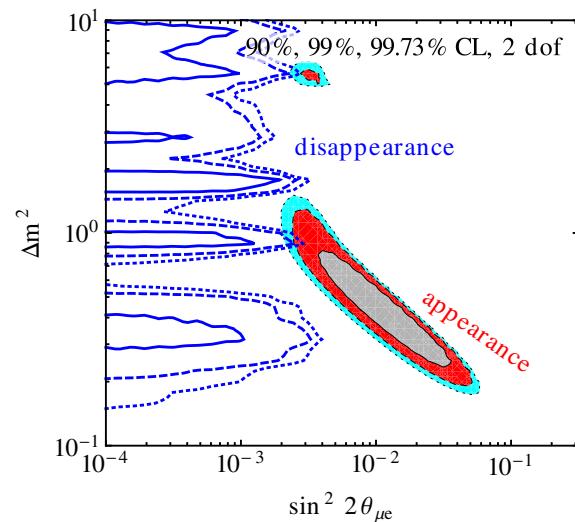
$\nu_e \rightarrow \nu_e$ **disapp** (REACT,Gallium,Solar, LSND/KARMEN)

- Problem: fit together $\nu_\mu \rightarrow \nu_e$ **app** (LSND,KARMEN,NOMAD,MiniBooNE,E776,ICARUS)
 $\nu_\mu \rightarrow \nu_\mu$ **disapp** (CDHS,ATM,MINOS,ICECUBE)

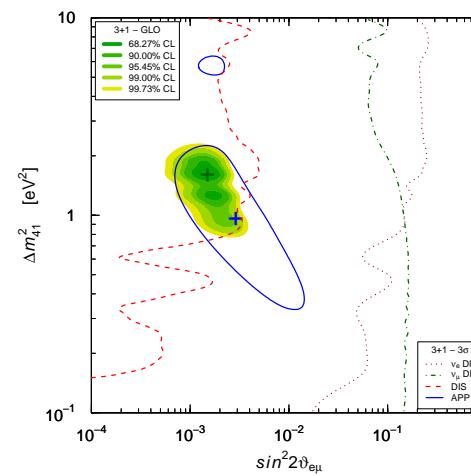
- Generically: $P(\nu_e \rightarrow \nu_\mu) \sim |U_{ei}^* U_{\mu i}|$ [i =heavier state(s)]

But $|U_{ei}|$ constrained by $P(\nu_e \rightarrow \nu_e)$ disappearance data
And $|U_{\mu i}|$ constrained by $P(\nu_\mu \rightarrow \nu_\mu)$ disappearance data } \Rightarrow **Severe tension**

Kopp et al, ArXiv 1303.3011

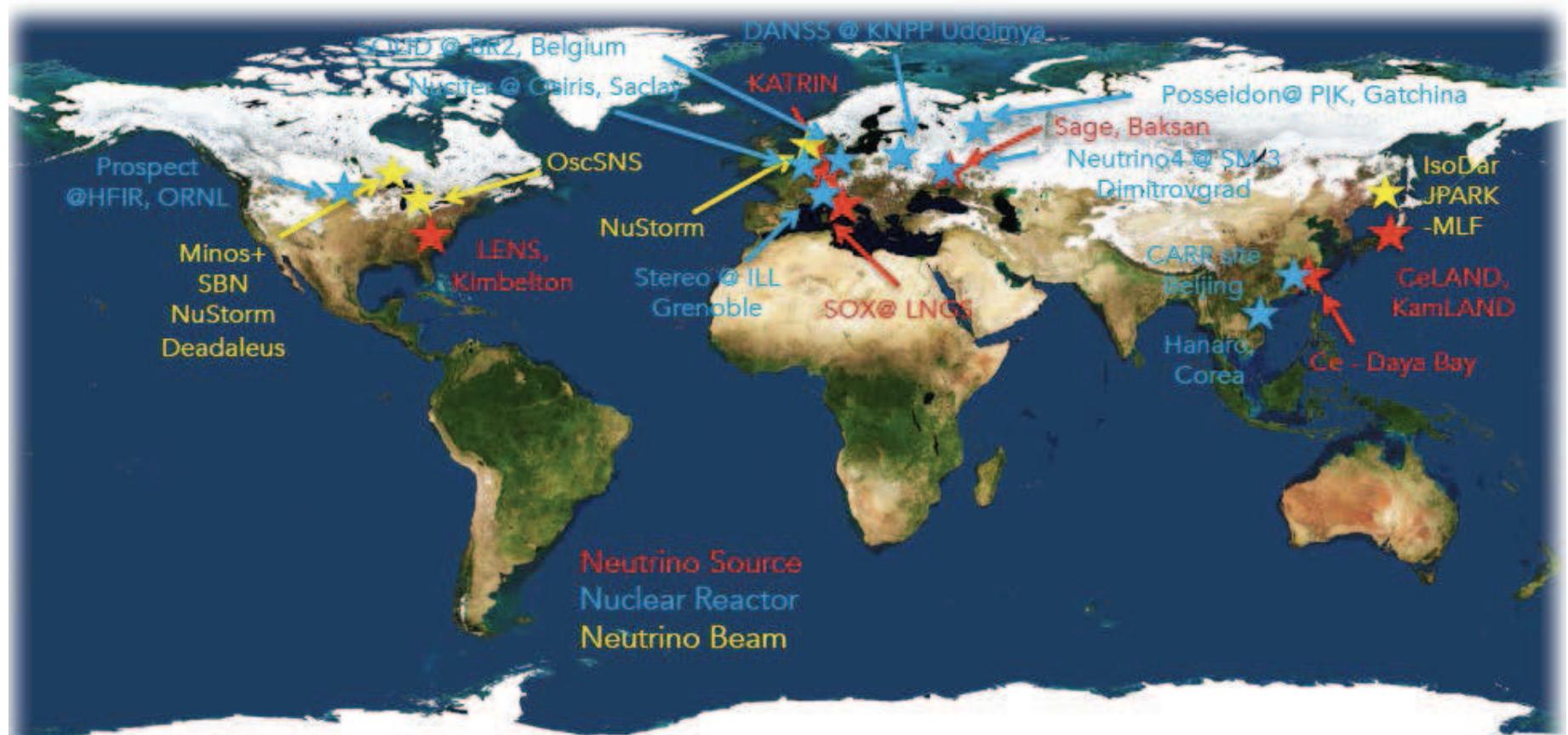


Giunti et al, ArXiv 1308.5288



- New generation of ν_e disappearance experiments \Rightarrow adding to the tension

Searches for eV sterile neutrinos



This talk: (anti-) ν_e disappearance only

$$P_{ee} = 1 - \sin^2 2\theta_{ee} \sin^2 \frac{\Delta m_{41}^2}{4E} \quad \& \quad \sin^2 2\theta_{ee} = |U_{e4}|^2 \left(1 - |U_{e4}|^2\right)$$

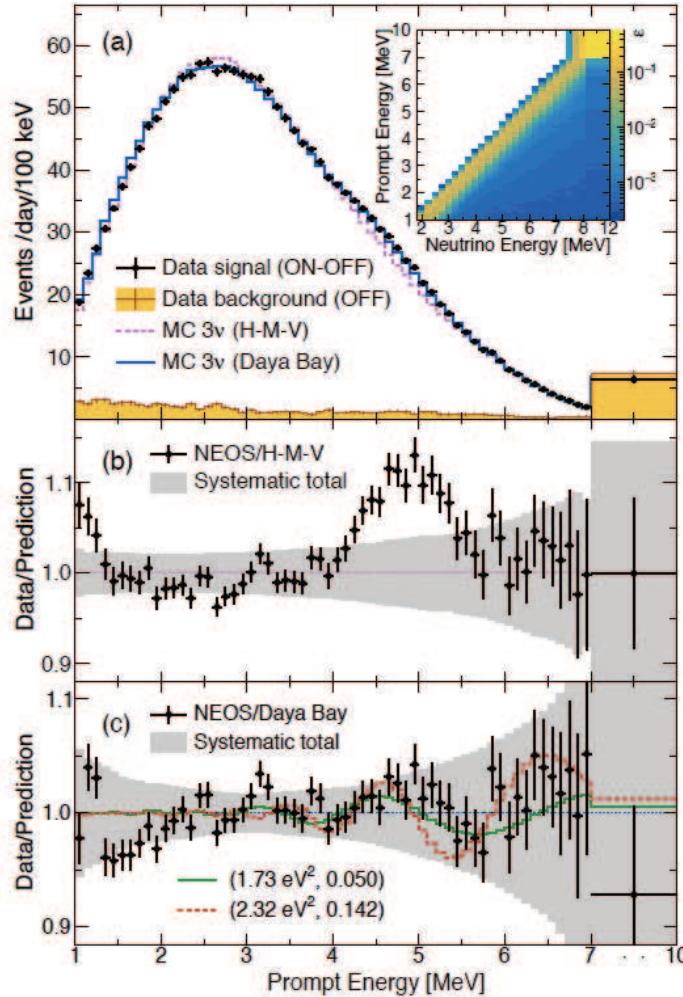
NEOS @ Hanbit (Korea)

arXiv:1610.05134v4 [hep-ex] 21 Mar 2017

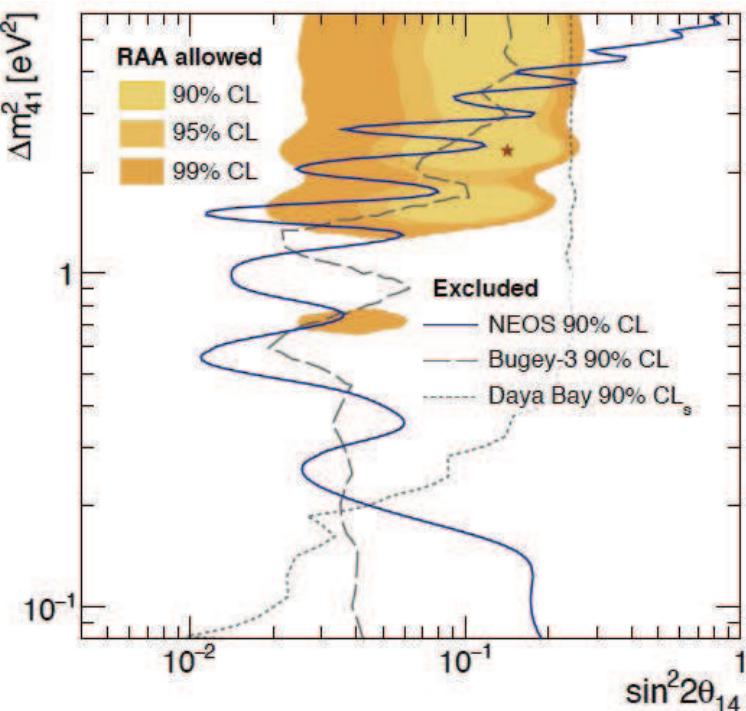
Single detector / single distance

Analysis done with Daya Bay spectrum as reference

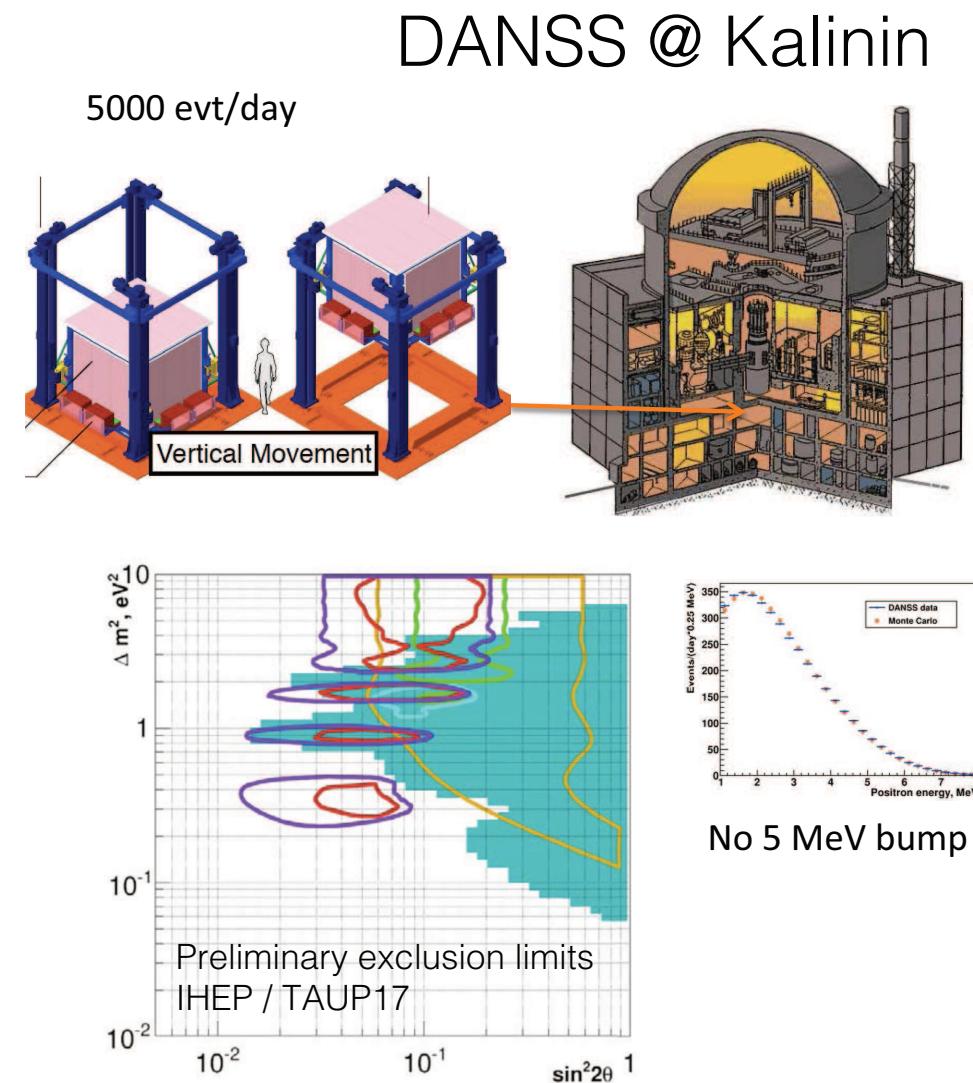
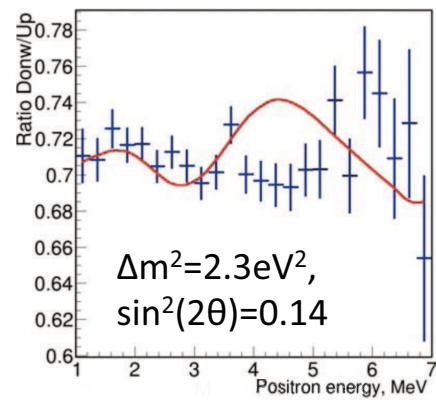
Relies on 5 MeV bumb!



S. Schönert | TUM | Sterile neutrinos



- 3 GW extended core (5000 ev/day)
- Plastic strips with Gd-loaded interlayer, WLS fibers
- Vertical motion of the detector (9.7-12.2 m)
- Independent of burn-up or spectral feature



⇒ Decrease of the significance of the reactor anomaly

Dentler et al 1709.04294

⇒ Global fit with 3+N steriles severely disfavoured unless some data is dropped

Giunti et al 1703.00860

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Anxiously waiting for Katrin
- Dirac or Majorana?: We do not know, anxiously waiting for ν -less $\beta\beta$ decay
- Only three light states? Tension between hints and bounds
New results from $\bar{\nu}_e$ disappearance further disfavour $\mathcal{O}(\text{eV})$ ν_s interpretation
- Other NP at play?

Alternative Oscillation Mechanisms

- Oscillations are due to:
 - Misalignment between CC-int and propagation states: Mixing \Rightarrow Amplitude
 - Difference phases of propagation states \Rightarrow Wavelength. For Δm^2 -OSC $\lambda = \frac{4\pi E}{\Delta m^2}$

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- ν masses are not the only mechanism for oscillations

Violation of Equivalence Principle (VEP): Gasperini 88, Halprin,Leung 01

Non universal coupling of neutrinos $\gamma_1 \neq \gamma_2$ to gravitational potential ϕ

Violation of Lorentz Invariance (VLI): Coleman, Glashow 97

Non universal asymptotic velocity of neutrinos $c_1 \neq c_2 \Rightarrow E_i = \frac{m_i^2}{2p} + c_i p$

Interactions with space-time torsion: Sabbata, Gasperini 81

Non universal couplings of neutrinos $k_1 \neq k_2$ to torsion strength Q

Violation of Lorentz Invariance (VLI) Colladay, Kostelecky 97; Coleman, Glashow 99

due to CPT violating terms: $\bar{\nu}_L^\alpha b_\mu^{\alpha\beta} \gamma_\mu \nu_L^\beta \Rightarrow E_i = \frac{m_i^2}{2p} \pm b_i$

$$\lambda = \frac{\pi}{E|\phi|\delta\gamma}$$

$$\lambda = \frac{2\pi}{E\Delta c}$$

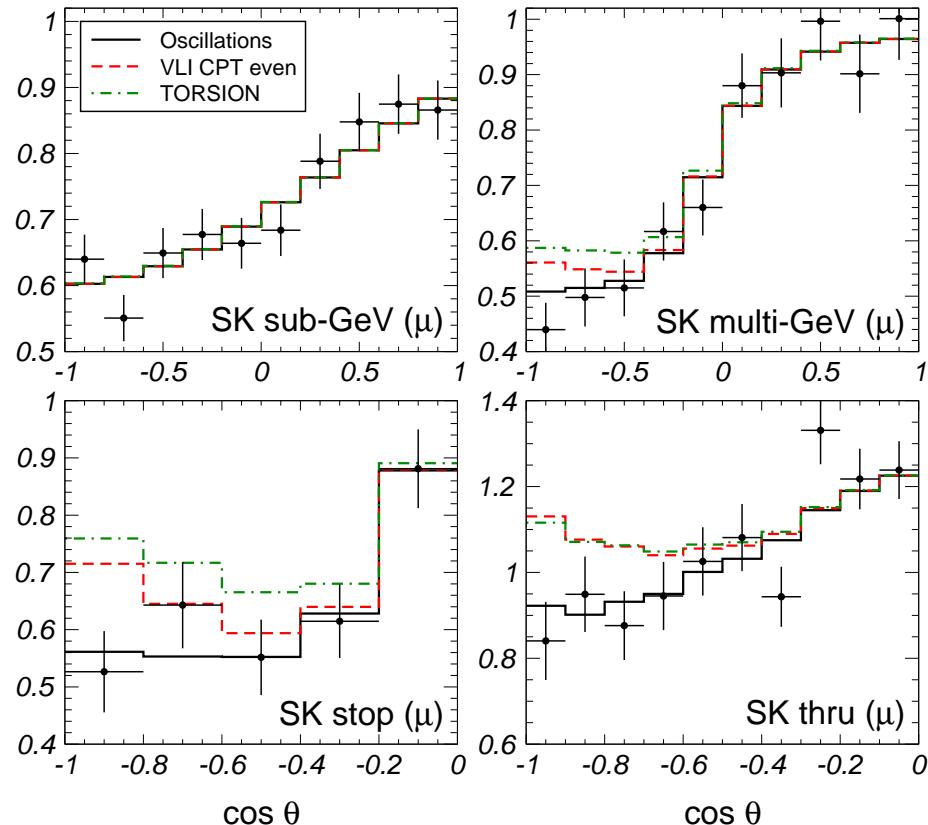
$$\lambda = \frac{2\pi}{Q\Delta k}$$

$$\lambda = \pm \frac{2\pi}{\Delta b}$$

ATM ν 's: Subdominant NP Effects

- Using atmospheric neutrino data these effects can be constrained

MCG-G, M. Maltoni hep-ph,0404085,0704.1800



At 90% CL:

$$\frac{|\Delta c|}{c} \leq 1.2 \times 10^{-24}$$

$$|\phi \Delta \gamma| \leq 5.9 \times 10^{-25}$$

$$|Q \Delta k| \leq 4.8 \times 10^{-23} \text{ GeV}$$

$$|\Delta b| \leq 3.0 \times 10^{-23} \text{ GeV}$$

- Including non-standard neutrino NC interactions with fermion f

$$\mathcal{L}_{\text{NSI}} = -2\sqrt{2}G_F \varepsilon_{\alpha\beta}^{fP} (\bar{\nu}_\alpha \gamma^\mu L \nu_\beta) (\bar{f} \gamma_\mu P f), \quad P = L, R$$

- In flavour basis $\vec{\nu} = (\nu_e, \nu_\mu, \nu_\tau)^T$ the neutrino evolution eq.:

$$i \frac{d}{dx} \vec{\nu} = H^\nu \vec{\nu} \quad \text{with} \quad H^\nu = H_{\text{vac}} + H_{\text{mat}} \quad \text{and} \quad H^{\bar{\nu}} = (H_{\text{vac}} - H_{\text{mat}})^*$$

$$H_{\text{mat}} = \sqrt{2}G_F N_e(r) \begin{pmatrix} 1 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix} + \sqrt{2}G_F N_e(r) \begin{pmatrix} \varepsilon_{ee} & \varepsilon_{e\mu} & \varepsilon_{e\tau} \\ \varepsilon_{e\mu}^* & \varepsilon_{\mu\mu} & \varepsilon_{\mu\tau} \\ \varepsilon_{e\tau}^* & \varepsilon_{\mu\tau}^* & \varepsilon_{\tau\tau} \end{pmatrix}$$

$$\varepsilon_{\alpha\beta}(r) \equiv \sum_{f=ued} \frac{N_f(r)}{N_e(r)} \varepsilon_{\alpha\beta}^{fV} \Rightarrow 3\nu \text{ evolution depends on 6 (vac) + 8 per } f \text{ (mat)}$$

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\Rightarrow Parameters degeneracies (some well-known but being rediscovered lately ...)

In particular CPT \Rightarrow invariance under simultaneously:

$$\theta_{12} \leftrightarrow \frac{\pi}{2} - \theta_{12}, \quad (\varepsilon_{ee} - \varepsilon_{\mu\mu}) \rightarrow -(\varepsilon_{ee} - \varepsilon_{\mu\mu}) - 2,$$

$$\Delta m_{31}^2 \rightarrow -\Delta m_{32}^2, \quad (\varepsilon_{\tau\tau} - \varepsilon_{\mu\mu}) \rightarrow -(\varepsilon_{\tau\tau} - \varepsilon_{\mu\mu}),$$

$$\delta \rightarrow \pi - \delta, \quad \varepsilon_{\alpha\beta} \rightarrow -\varepsilon_{\alpha\beta}^* \quad (\alpha \neq \beta),$$

NSI: Bounds/Degeneracies from/in Oscillation data

M.C G-G, M.Maltoni 1307.3092

		90% CL	
Param.	best-fit	LMA	LMA-D
$\varepsilon_{ee}^u - \varepsilon_{\mu\mu}^u$	+0.298	[+0.00, +0.51]	$\oplus [-1.19, -0.81]$
$\varepsilon_{\tau\tau}^u - \varepsilon_{\mu\mu}^u$	+0.001	[-0.01, +0.03]	[-0.03, +0.03]
$\varepsilon_{e\mu}^u$	-0.021	[-0.09, +0.04]	[-0.09, +0.10]
$\varepsilon_{e\tau}^u$	+0.021	[-0.14, +0.14]	[-0.15, +0.14]
$\varepsilon_{\mu\tau}^u$	-0.001	[-0.01, +0.01]	[-0.01, +0.01]

- Bounds $\mathcal{O}(1 - 10\%)$
- Except $\varepsilon_{ee}^{q,V} - \varepsilon_{\mu\mu}^{q,V}$

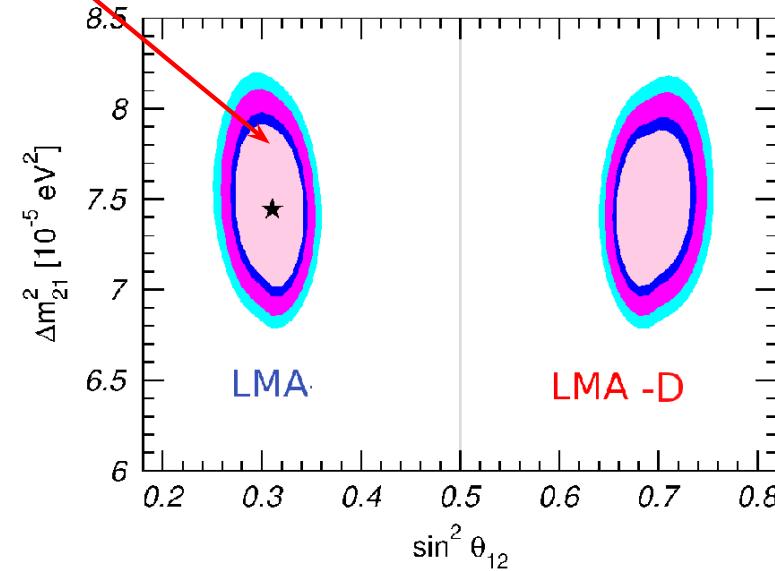
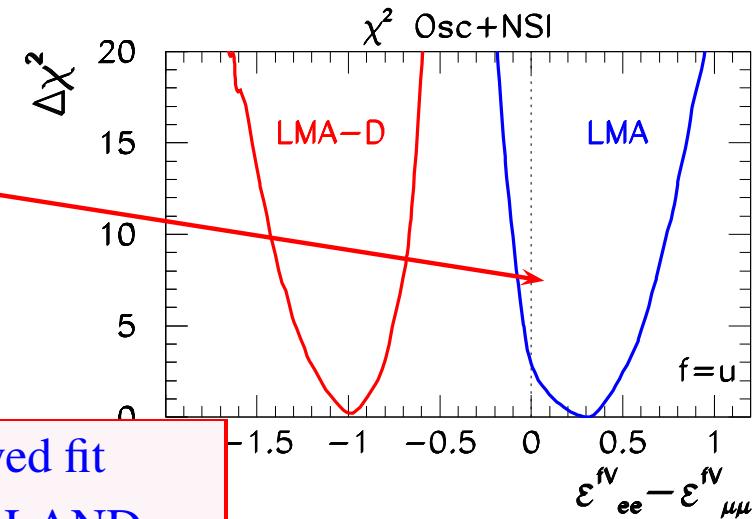
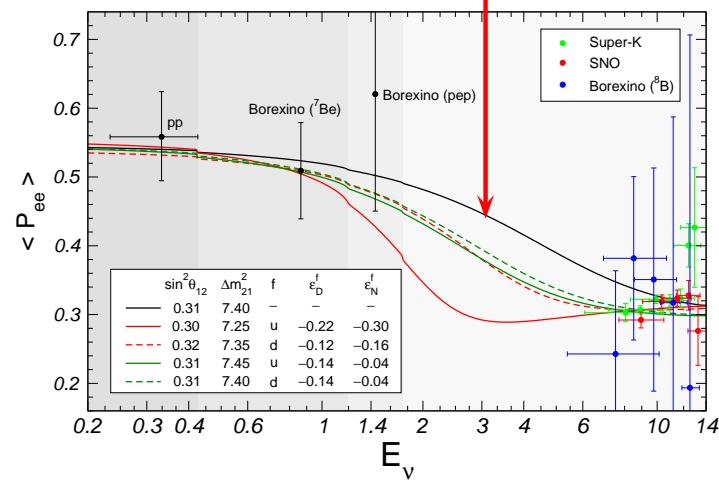
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LMA: Improved fit
to Solar+KamLAND



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M.C G-G, M.Maltoni 1307.3092

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Degenerate solution LMA-D ($\theta_{12} > 45^\circ$)

Miranda, Tortola, Valle, hep-ph/0406280

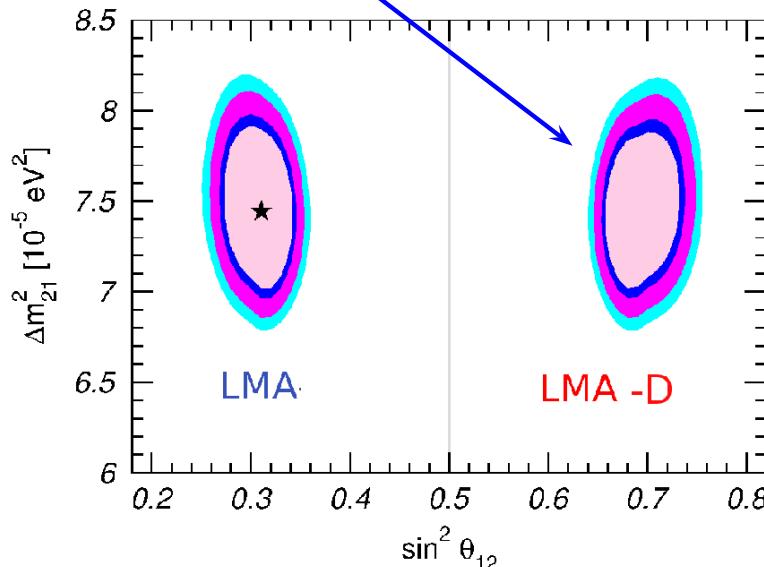
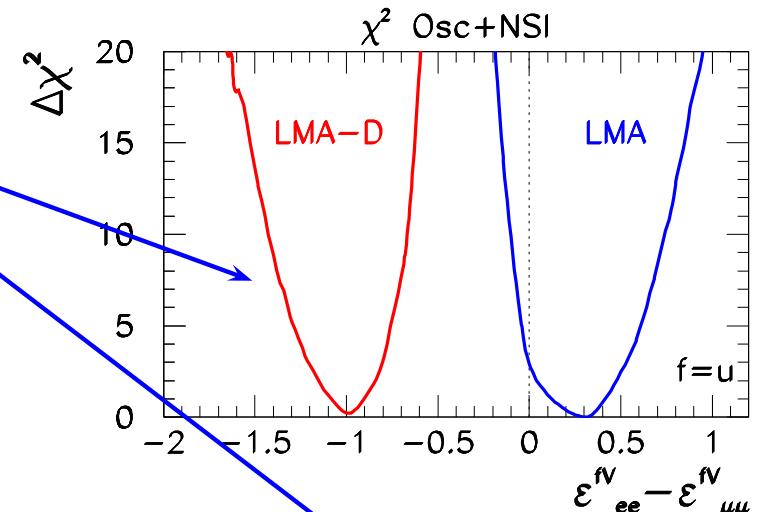
Cannot be resolved with osc-experiments

Requires NC scattering experiments

Coloma et al 1701.04828

Requires NSI $\sim G_F$ (light mediators?)

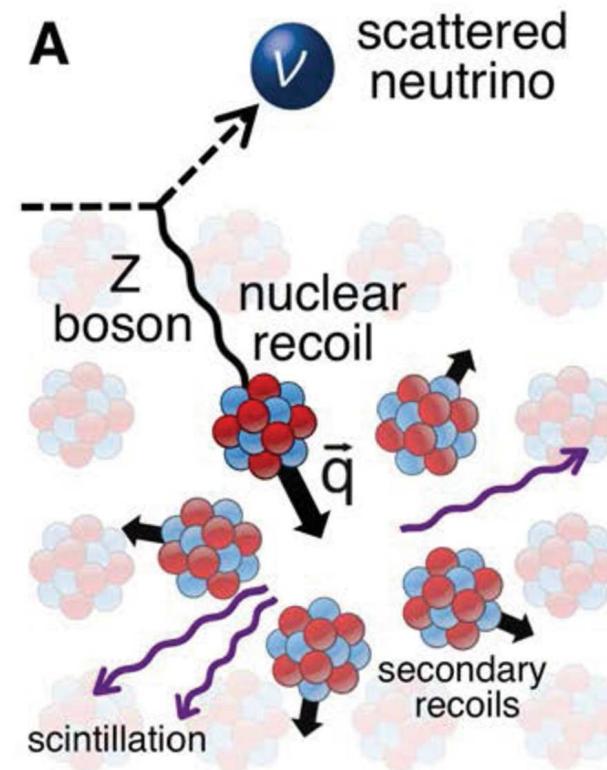
Farzan 1505.06906, and Shoemaker 1512.09147



COHERENT EXPERIMENT

Science 2017 [ArXiv:1708.01294]

- observation of coherent neutrino-nucleus scattering at 6.7σ at CsI[Na] detector
- neutrinos from stopped pion source at Oak Ridge NL
- 142 events observed, in agreement with Standard Model



NSI: Combination with COHERENT data

Coloma, MCGG, Maltoni,Schwetz ArXiv:1708.02899

- COHERENT has detected for first time Coherent νN scattering [1708.01294](#):
142($1 \pm 0.28(\text{sys})$) observed events over a steady bck of 405
136(SM) + 6($1 \pm 0.25(\text{sys})$) beam-on bck) expected
- In presence of NSI: $N_{\text{NSI}}(\varepsilon) = \gamma [f_{\nu_e} Q_{we}^2(\varepsilon) + (f_{\nu_\mu} + f_{\bar{\nu}_\mu}) Q_{w\mu}^2(\varepsilon)]$

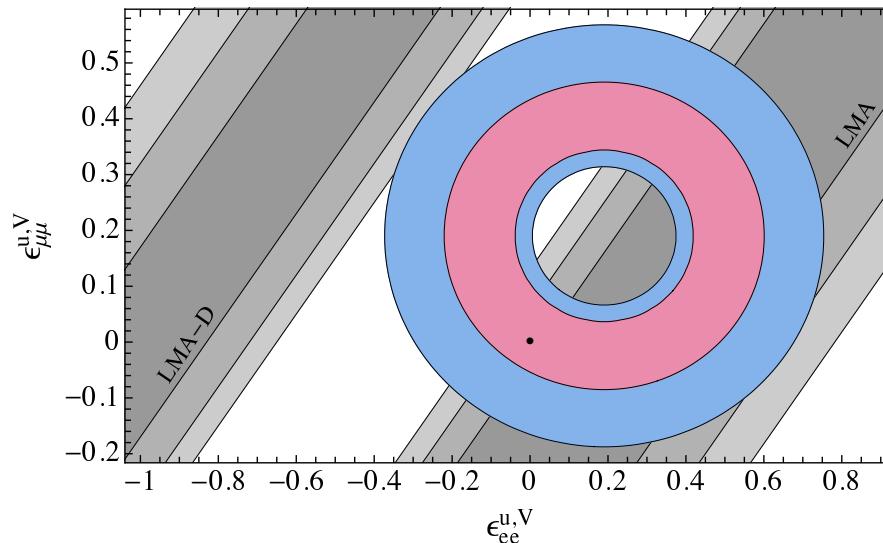
$$Q_{w\alpha}^2 \propto [Z(g_p^V + 2\varepsilon_{\alpha\alpha}^{u,V} + \varepsilon_{\alpha\alpha}^{d,V}) + N(g_n^V + \varepsilon_{\alpha\alpha}^{u,V} + 2\varepsilon_{\alpha\alpha}^{d,V})]^2 + \sum_{\beta \neq \alpha} [Z(2\varepsilon_{\alpha\beta}^{u,V} + \varepsilon_{\alpha\beta}^{d,V}) + N(\varepsilon_{\alpha\beta}^{u,V} + 2\varepsilon_{\alpha\beta}^{d,V})]^2$$

NSI: Combination with COHERENT data

Coloma, MCGG, Maltoni, Schwetz ArXiv:1708.02899

- COHERENT has detected for first time Coherent νN scattering [1708.01294](#):
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- Impact on LMA-D: Allowed COHERENT region vs LMA-D required range



NSI: Combination with COHERENT data

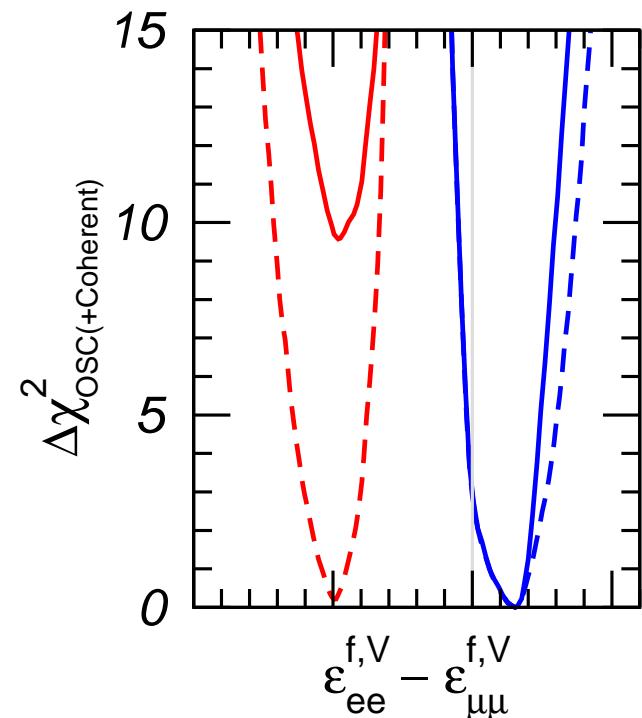
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- OSCILLATION + COHERENT \Rightarrow LMA-D excluded at more than 3.1σ

All NSI's constrained

	$f = u$	$f = d$
$\epsilon_{ee}^{f,V}$	[0.028, 0.60]	[0.030, 0.55]
$\epsilon_{\mu\mu}^{f,V}$	[-0.088, 0.37]	[-0.075, 0.33]
$\epsilon_{\tau\tau}^{f,V}$	[-0.090, 0.38]	[-0.075, 0.33]
$\epsilon_{e\mu}^{f,V}$	[-0.073, 0.044]	[-0.07, 0.04]
$\epsilon_{e\tau}^{f,V}$	[-0.15, 0.13]	[-0.13, 0.12]
$\epsilon_{\mu\tau}^{f,V}$	[-0.01, 0.009]	[-0.009, 0.008]



Confirmed Low Energy Picture and MY List of Q&A

- At least two neutrinos are massive \Rightarrow There is NP
- Three mixing angles are non-zero (and relatively large) \Rightarrow very different from CKM
- Leptonic CP: Best fit $J_{\text{Lep,CP}} = -0.033$. CP conservation at 95% CL
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A Detour in the Sun

- Sun=Main sequence star
- Solar Models describes the Sun based on:

Mass: $M_{\odot} = 2 \times 10^{33}$ gr

Radius: $R_{\odot} = 7 \times 10^5$ km

Surf Lum: $L_{\odot} = 3.842 \times 10^{33} (1 \pm 0.004)$ erg/sec

Age: $\tau_{\odot} = 4.57 \times 10^9 (1 \pm 0.0044)$ yr

- Basic assumptions:

- The Sun is spherically symmetric
- Some Equation of State

- Incorporate:

- Transport of Energy: Radiative and Convective
 \Rightarrow Model of opacities
- Chemical Evolution by Nuclear Reactions
 \Rightarrow pp-chain and CNO cycles
- Microscopic Diffusion

- Using inputs from:

- Lab Measurements of Nuclear Rates
- Element Abundance Determination By
 - \Rightarrow Spectroscopy of Photosphere: C, N, O
 - \Rightarrow Meteorites: Mg,Si,S,Fe
 - \Rightarrow Other methods: Ne, Ar

- They Predict Observables:

- Neutrino Flux Spectrum
- Relevant to Helioseismology :
 - \Rightarrow Surface He Abundance
 - \Rightarrow Inner Radius of Convective Zone
 - \Rightarrow Sound Speed Profile

The Solar Composition Problem

- Newer determination of abundances in solar surface give lower values
- Solar Models with lower metallicities fail in reproducing helioseismology data

$$\log \epsilon_i \equiv \log N_i/N_H + 12$$

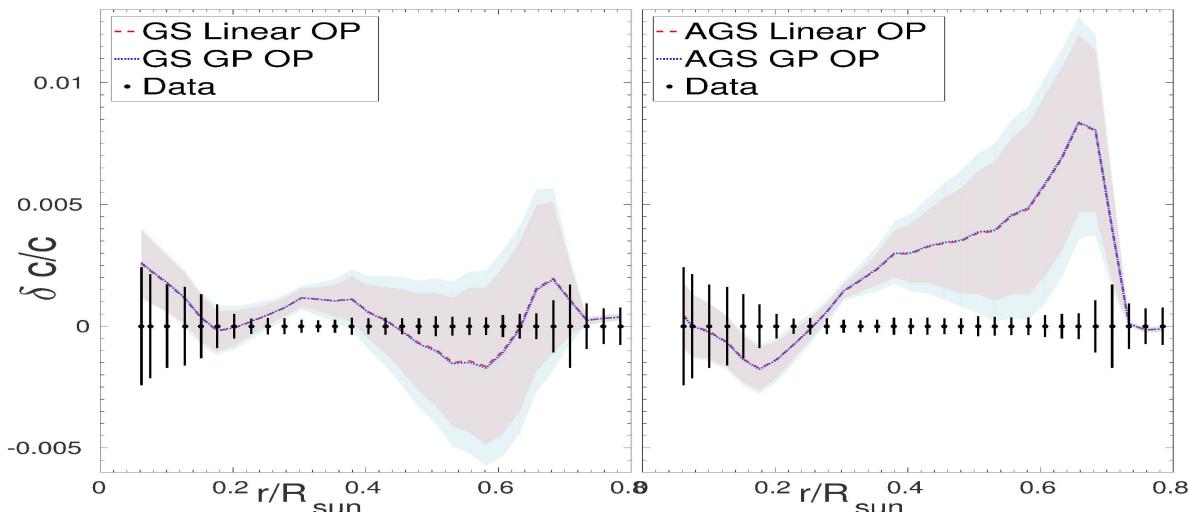
Element	GS98	AGSS09met
C	8.52 ± 0.06	8.43 ± 0.05
N	7.92 ± 0.06	7.83 ± 0.05
O	8.83 ± 0.06	8.69 ± 0.05
Mg	7.58 ± 0.01	7.53 ± 0.01
Si	7.56 ± 0.01	7.51 ± 0.01
S	7.20 ± 0.06	7.15 ± 0.02
Fe	7.50 ± 0.01	7.45 ± 0.01
Ar	6.40 ± 0.06	6.40 ± 0.13
Ne	8.08 ± 0.06	7.93 ± 0.10

⇒ Two sets of SSM:

Starting from Bahcall *et al* 05, Serenelli *et al* 2016

B16-GS98 with old abund

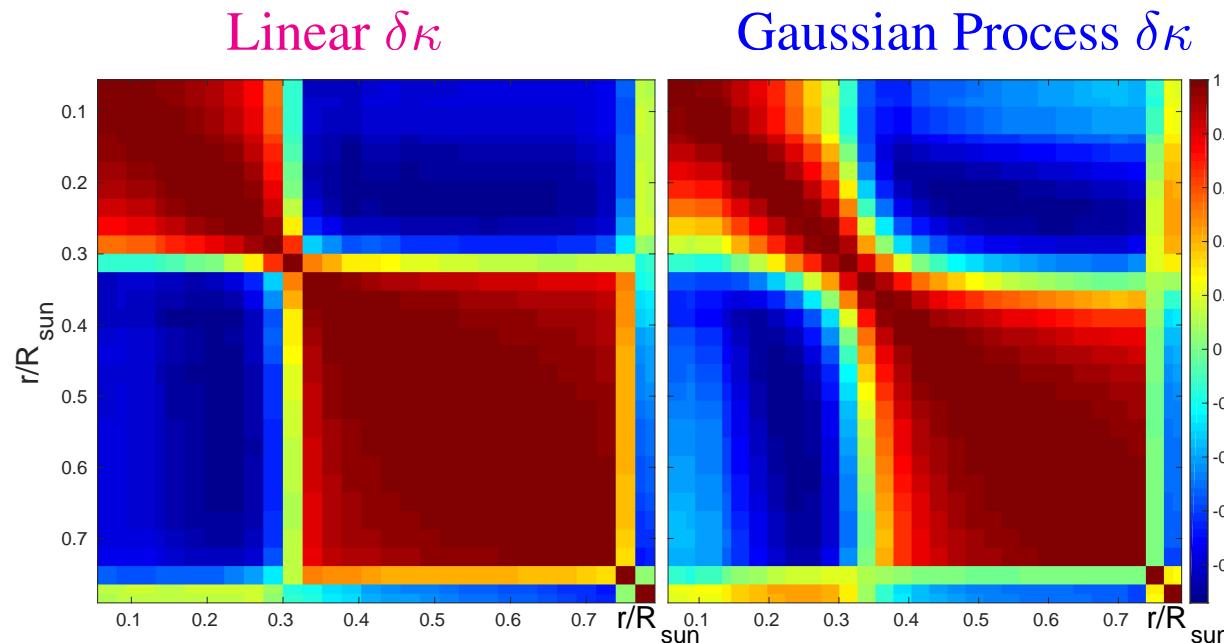
B16-AGSS09met with new abund



- Predictions very strongly correlated
- B16-GS98 (dis)agreement at 2.5σ
 - B16-AGSS09 disagreement 4.7σ
 - Bayes factor B16-AGSS09/B16-GS98 < -13
(very strong disfavouring)

Modeling the uncertainty in the opacity profile

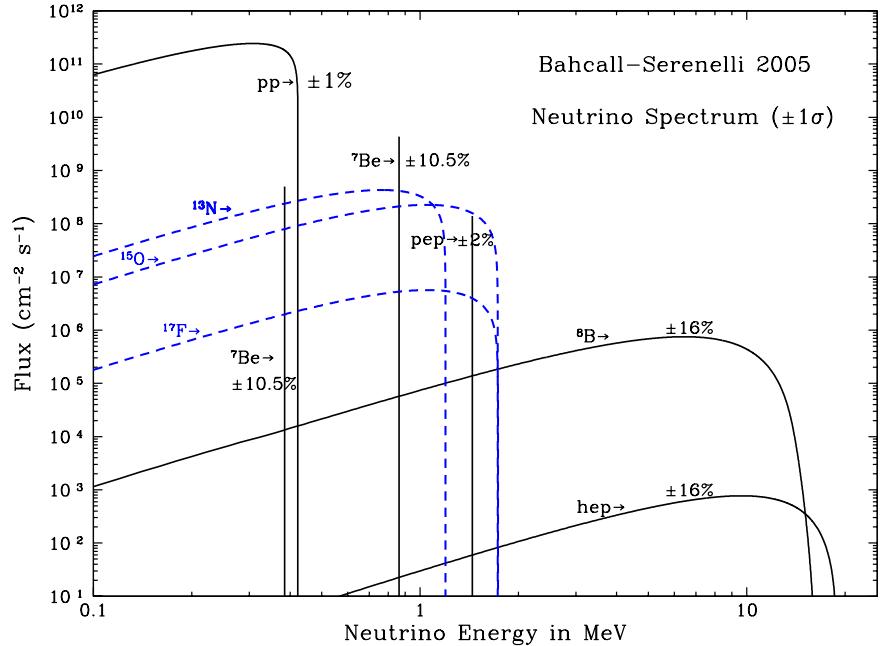
- Opacity is a function $\kappa(T, \rho, X_i = N_i/N_H)$. How to parametrize its uncertainty?
- Generically $(1 + \delta\kappa(T))\langle\kappa(T, \rho, X_i)\rangle$
 \Rightarrow Most studies $\delta\kappa(T) = C$ or $\delta\kappa(T) = a + b \log T$ with prior for σ_C (or σ_a, σ_b)
 \Rightarrow only very rigid variations allowed
- Alternative: Gaussian Process ansatz with same $\sigma(T)$ but correlation length $L < 1$



Song, MCG-G,Serenelli,Villante (17)

Still, even with GP opacity uncertainty Bayes factor B16-AGSS09/B16-GS98=-4.1
(Moderate to strong disfavour)

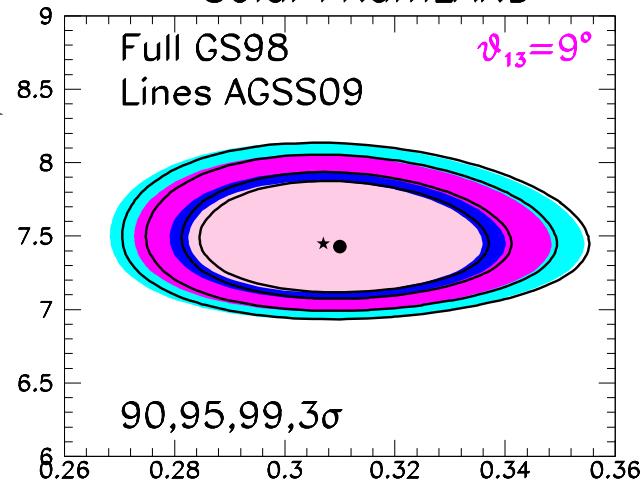
The Neutrino Fluxes



Flux $\text{cm}^{-2} \text{s}^{-1}$	B16GS98	B16-AGSS09met	Diff (%)
$\text{pp}/10^{10}$	5.98	$6.03 (1 \pm 0.005)$	0.8
$\text{pep}/10^8$	1.44	$1.46 (1 \pm 0.01)$	2.1
$\text{hep}/10^3$	7.98	$8.25 (1 \pm 0.30)$	3.4
${}^7\text{Be}/10^9$	4.93	$4.40 (1 \pm 0.06)$	8.8
${}^8\text{B}/10^6$	5.46	$4.50 (1 \pm 0.12)$	17.7
${}^{13}\text{N}/10^8$	2.78	$2.04 (1 \pm 0.14)$	26.7
${}^{15}\text{O}/10^8$	2.05	$1.44 (1 \pm 0.16)$	30.0
${}^{17}\text{F}/10^{16}$	5.29	$3.26 (1 \pm 0.18)$	38.4

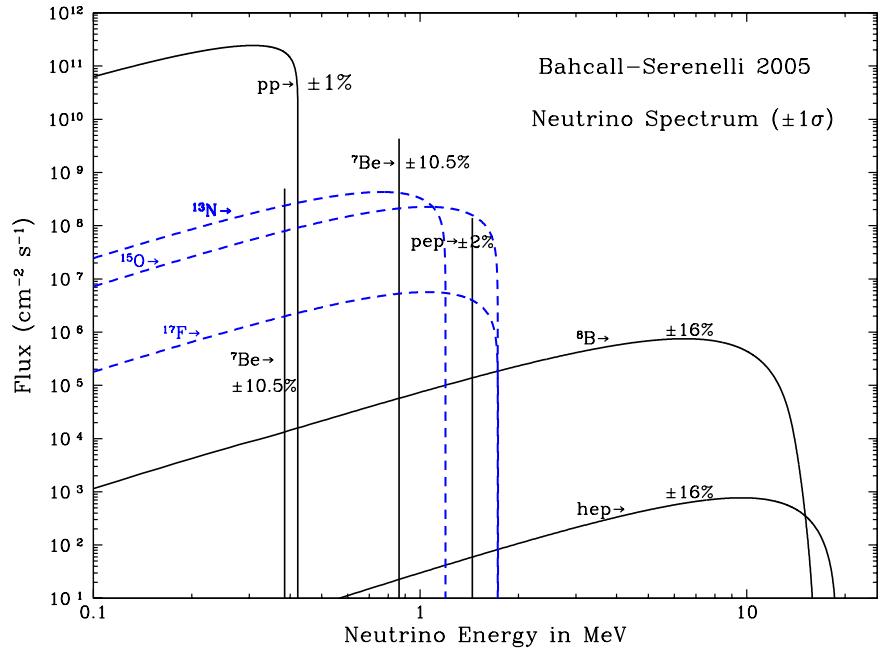
Most difference in CNO fluxes

Solar+KamLAND



- Negligible Impact in Osc Parameter Determination

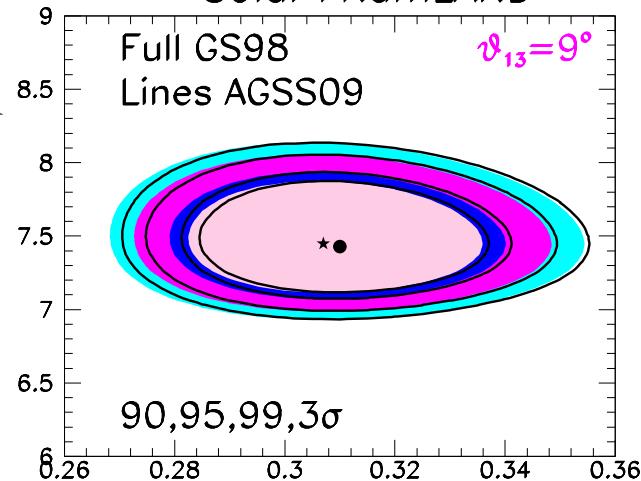
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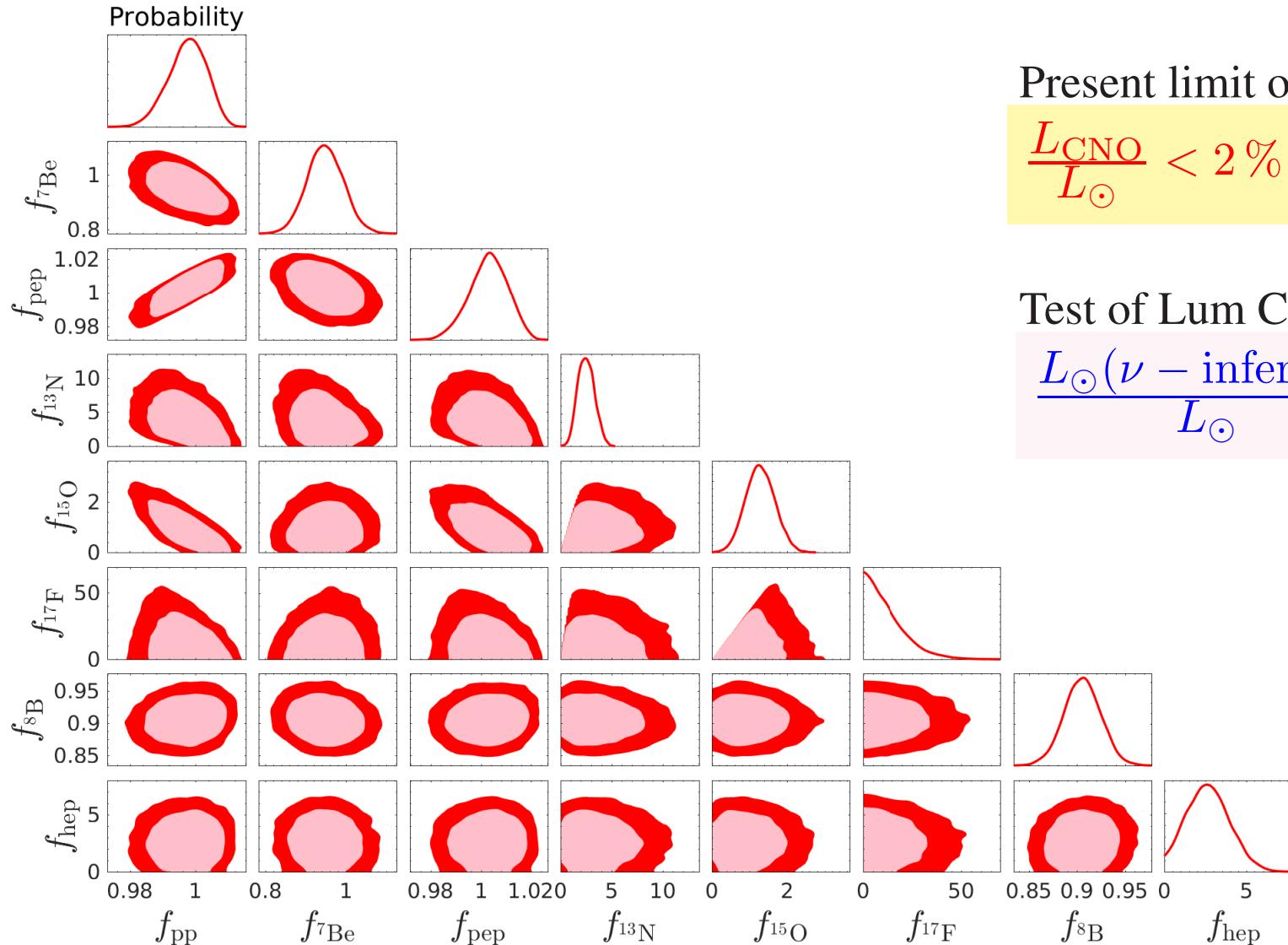
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- Negligible Impact in Osc Parameter Determination
- ⇒ Possible to extract fluxes for data

Testing How the Sun Shines with ν' s

Results of Oscillation analysis with solar flux normalizations free: $f_i = \frac{\Phi_i}{\Phi_i^{GS98}}$



Present limit on CNO:

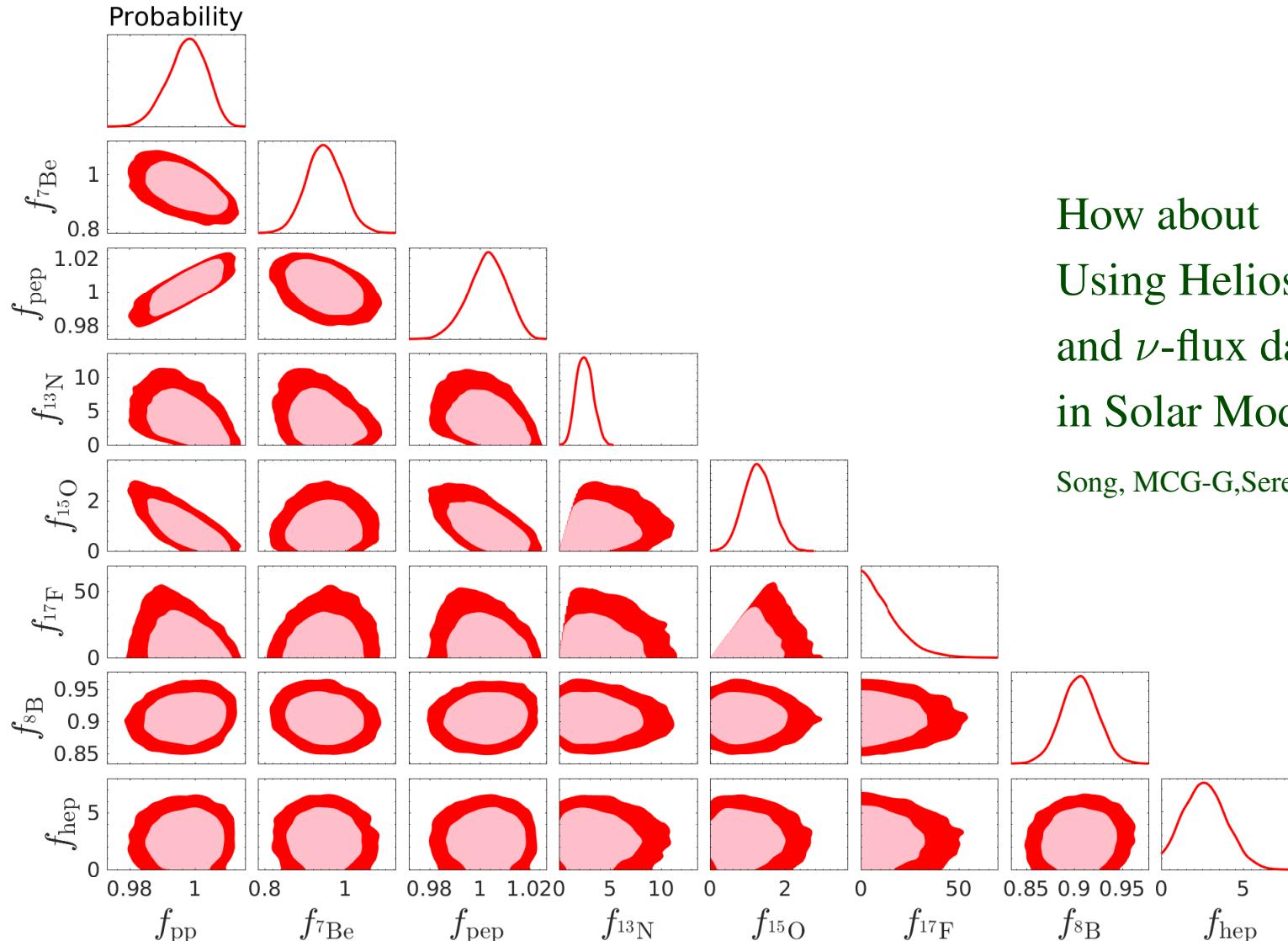
$$\frac{L_{\text{CNO}}}{L_{\odot}} < 2 \% \text{ (} 3\sigma \text{)}$$

Test of Lum Constraint:

$$\frac{L_{\odot}(\nu - \text{inferred})}{L_{\odot}} = 1.04 \pm 0.07$$

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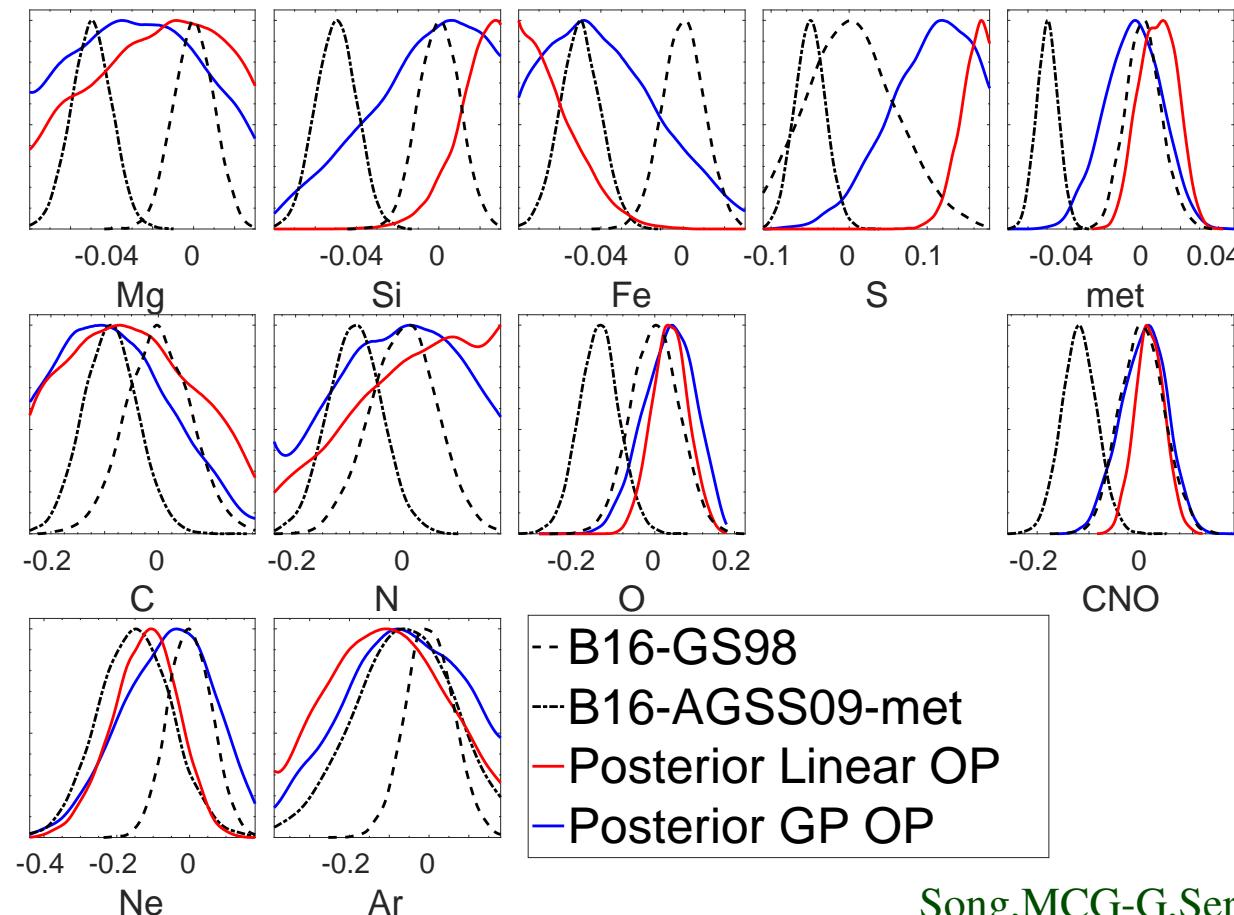
How about
Using Helioseismic
and ν -flux data
in Solar Modeling?

Song, MCG-G,Serenelli,Villante (17)

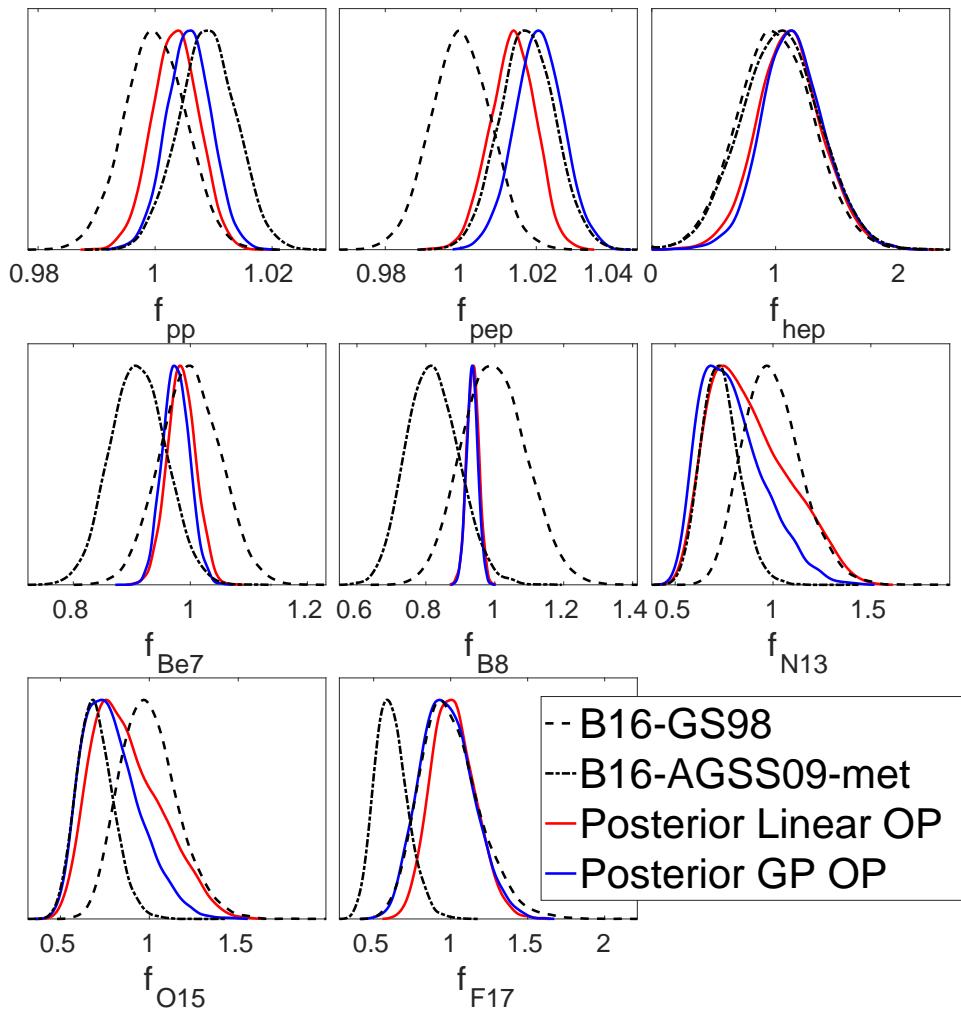
Using ν and Helioseismic Data in Sun Modeling

- Proposal: Invert approach and use the ν and helioseismic data in construction of SSM
- Method: Bayesian Inference of Abundance Posterior Distrib (from Uniform Priors)
- Test effects of effects of other modeling aspects (f.e. opacity uncertainty profiles)

$$x = \ln \frac{N_i}{N_H} - \langle \ln \frac{N_i}{N_H} \rangle_{GS98}$$



ν fluxes from ν +helioseismic data



Confirmed Low Energy Picture and MY List of Q&A

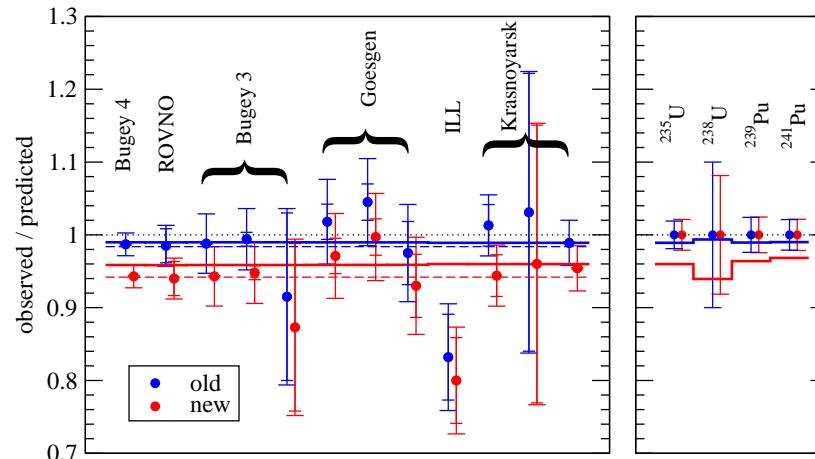
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Thank You

3 ν Analysis: Reactor Flux anomaly and θ_{13}

- The reactor $\bar{\nu}_e$ fluxes was recalculated about 6 yrs ago
T.A. Mueller et al., [arXiv:1101.2663].; P. Huber, [arXiv:1106.0687].

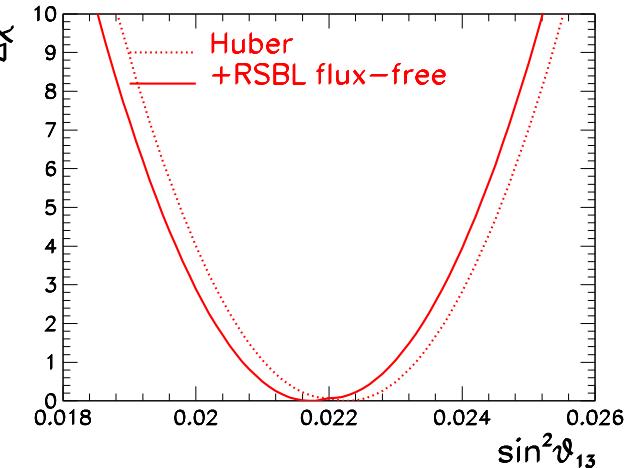
- Both found higher fluxes $\sim 3.5\%$
 \Rightarrow *negative* reactor experiments
 at short baselines (RSBL) indeed
 observed a deficit



- For 3ν analysis a consistent approach (T. Schwetz et. al. [arXiv:1103.0734]):
 – Fit oscillation parameters and reactor fluxes simultaneously
 – Use calculated fluxes (a) or RSBL data (b) as priors

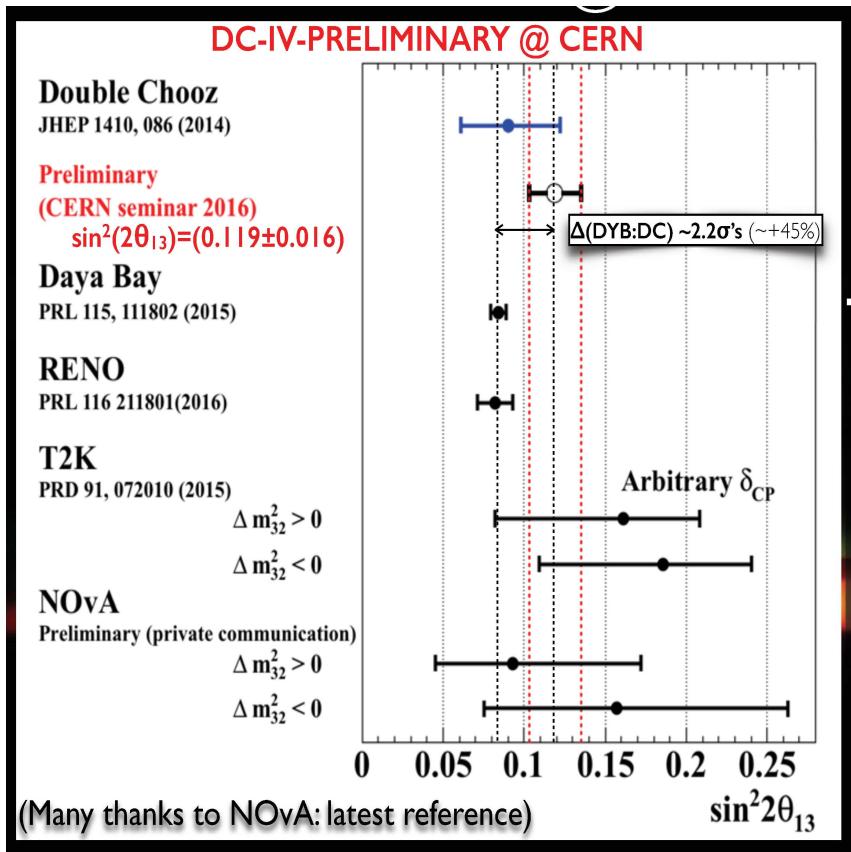
Difference at $\lesssim 0.3\sigma$ level

$$\chi^2_{min,a} - \chi^2_{min,b} \sim 7$$

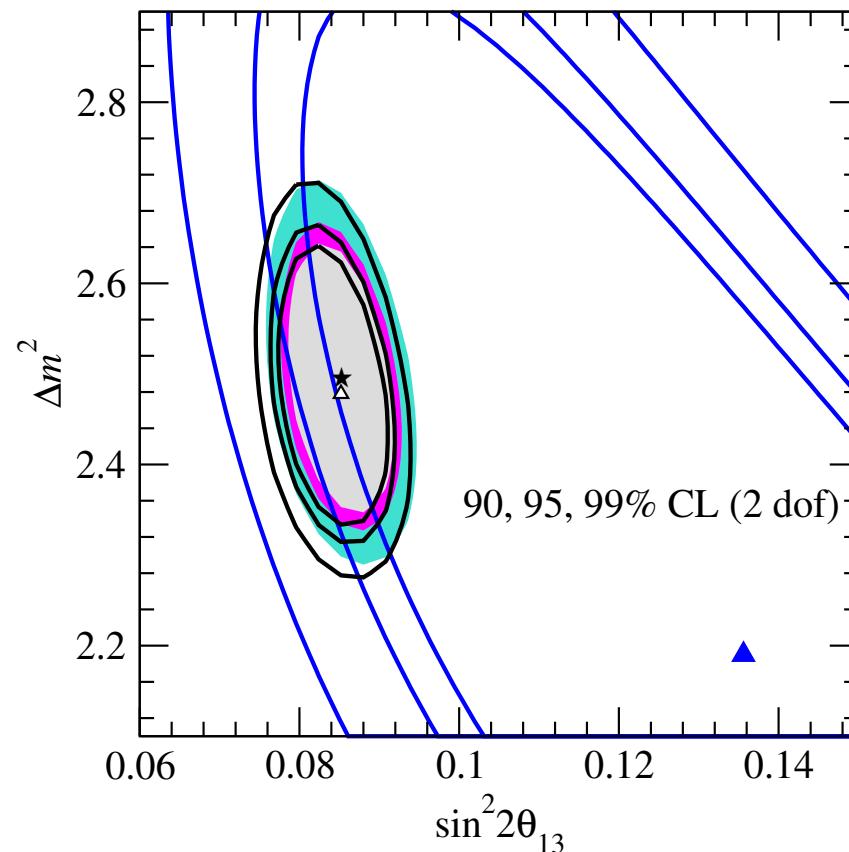


Issues in 3 ν Analysis: Consistency of θ_{13}

Daya Bay vs Double Chooz?



Allowed regions of DC vs Daya Bay



From DC (Anatael Cabrera) Talk CERN Sep 16

Fig. Courtesy of T. Schwetz

No significant discrepancy

Lepton Mixing Unitarity

- Previous results assume U_{LEP} to be unitary
- If ν_L mixed with m extra states $U_{\text{LEP}} = (K_{l,3 \times 3}, K_{h,3 \times m})$ Schechter, Valle (1980)
And $U_{\text{LEP}} U_{\text{LEP}}^\dagger = I_{3 \times 3}$ but in general $U_{\text{LEP}}^\dagger U_{\text{LEP}} \neq I_{(3+m) \times (3+m)}$
- If m states are heavy ($M \gg E_\nu$) oscillations measure $K_{L,3 \times 3}$ (not unitary)

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Flavour Changing Neutral Currents

- But this unitarity violation \Rightarrow Flavour Violation in Charged Lepton Processes
Universality Violation of Charge Current ...

- Constraints on these processes limit leptonic unitarity violation to

$$|K_l K_l^\dagger| = \begin{pmatrix} 0.9979 - 0.9998 & < 10^{-5} & < 0.0021 \\ < 10^{-5} & 0.9996 - 1.0 & < 0.0008 \\ < 0.0021 & < 0.0008 & 0.9947 - 1.0 \end{pmatrix}$$

Antusch *et al* ArXiv:1407.6607

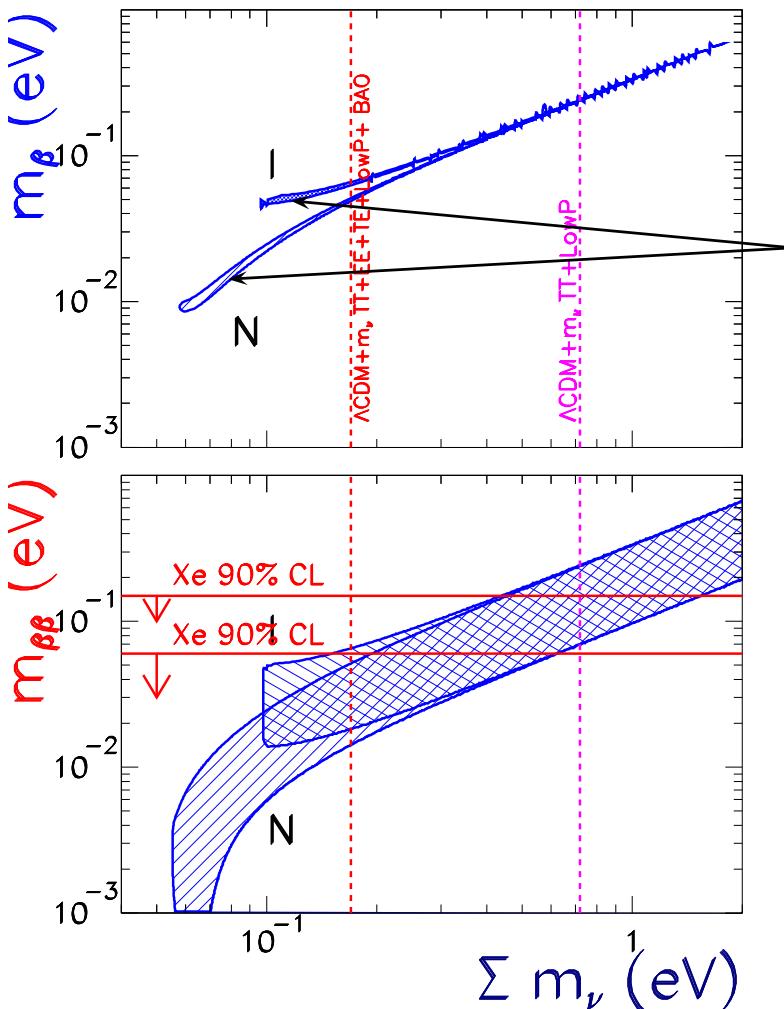
or equivalently $K_l \simeq (I + \epsilon)U(\theta_{ij}, \delta, \eta_i)$ with $|\epsilon_{\alpha j}| \leq \text{few} \times 10^{-3}$ while $K_h \sim \mathcal{O}(\epsilon)$

Neutrino Mass Scale: The Cosmo-Lab Connection

Global oscillation analysis

⇒ Correlations m_{ν_e} , m_{ee} and $\sum m_i$
(Fogli et al (04))

Nufit (95%)



Lower bound on $\sum m_i$ depends on ordering

Precision determination/bound of $\sum m_i$ can give information on ordering ?

Hannestad, Schwetz 1606.04691, Simpson et al 1703.03425, Capozzi et al 1703.04471 ...

Or much ado about nothing?

Cosmo data will only add to N/I likelihood
when accuracy on $\sum m_\nu$ better than 0.02 eV
(to see a 2σ N/I difference between 0.06 and 0.1)

Hannestad, Schwetz 1606.04691