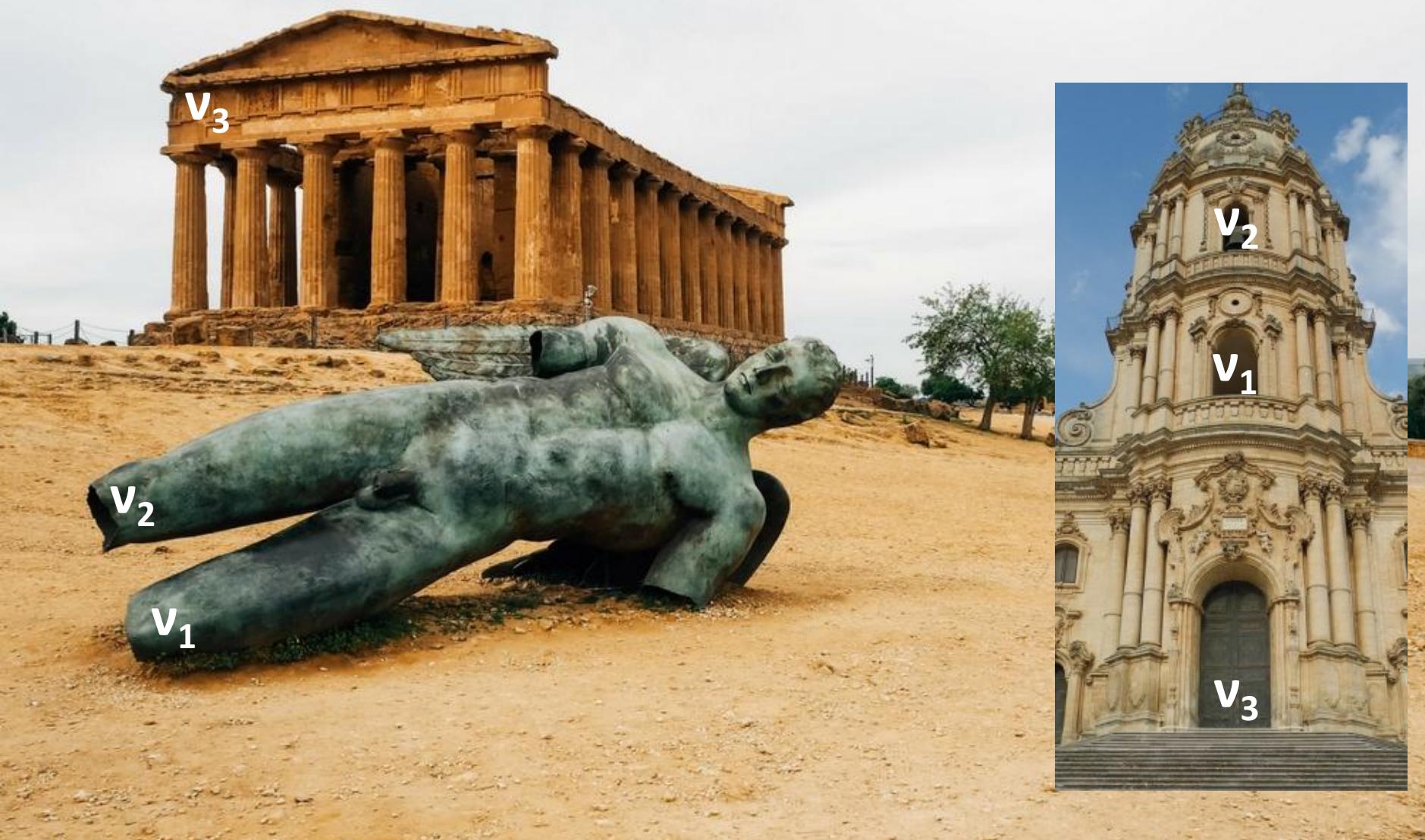


Measuring the Neutrino Mass Ordering in JUNO



International School
of Nuclear Physics
Erice, 16 Sep 2017

Michael Wurm
Uni Mainz

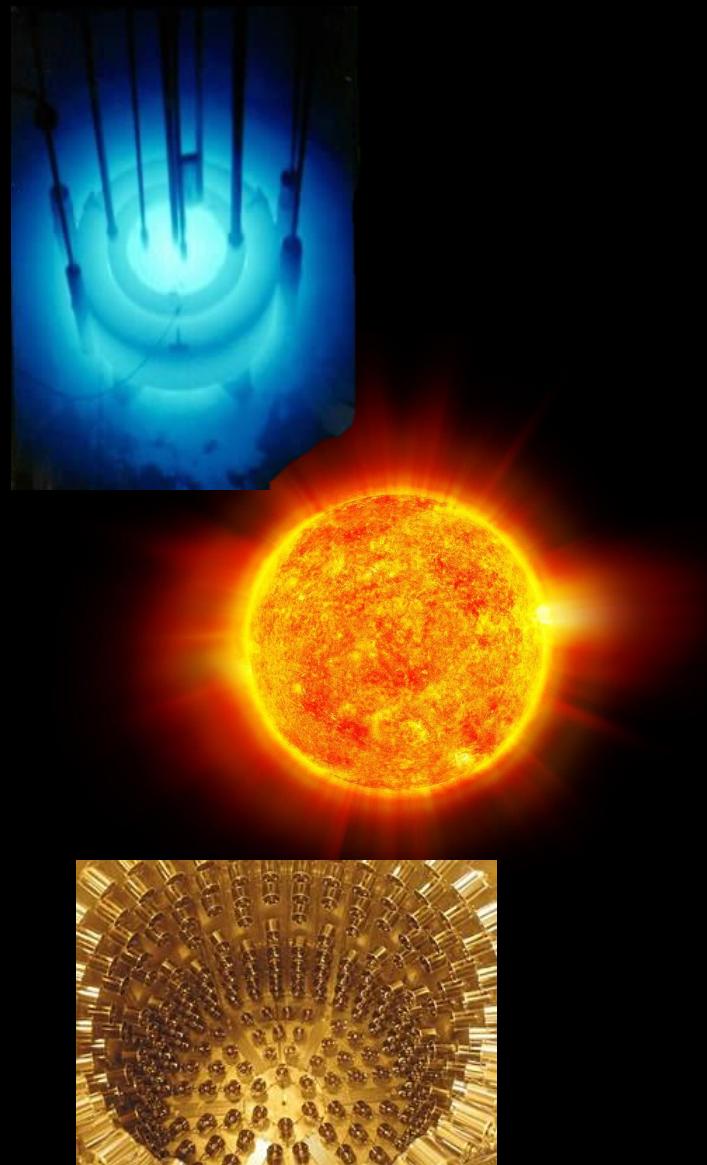
 PRISMA

The PRISMA logo consists of a stylized red and blue circular emblem followed by the word 'PRISMA' in a bold, sans-serif font.

Outline

- **Neutrino mass ordering**
 - motivation
 - experimental methods

- **JUNO experiment**
 - signature of mass ordering
 - detector layout
 - systematic effects
 - other experimental inputs



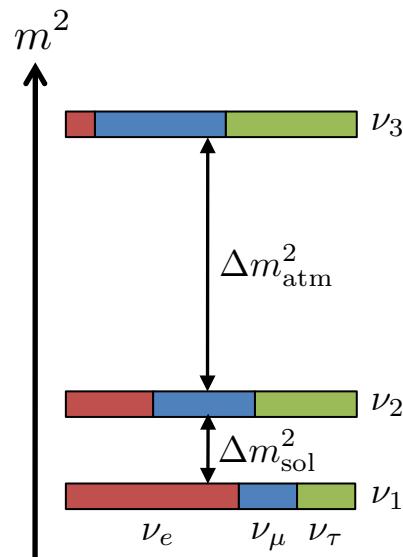
Status of 3-flavor oscillations

$$\mathbf{U}_{3 \times 3} = \mathbf{U}_{\text{PMNS}}$$

$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix} \begin{pmatrix} c_{13} & 0 & s_{13}e^{-i\delta} \\ 0 & 1 & 0 \\ -s_{13}e^{i\delta} & 0 & c_{13} \end{pmatrix} \begin{pmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix}$$

atmospheric mixing
 (maximal 45°?) reactor mixing & CP violation
 (small $\theta_{13} \approx 9^\circ$, $\delta \approx -\pi$?)

solar mixing
 (large 33°)



- $\Delta m_{\text{sol}}^2 = \Delta m_{21}^2$ → small splitting: $+8 \times 10^{-5} \text{ eV}^2$
- $\Delta m_{\text{atm}}^2 = \Delta m_{32}^2 \approx \Delta m_{31}^2$ → large splitting: $\pm 2.5 \times 10^{-3} \text{ eV}^2$

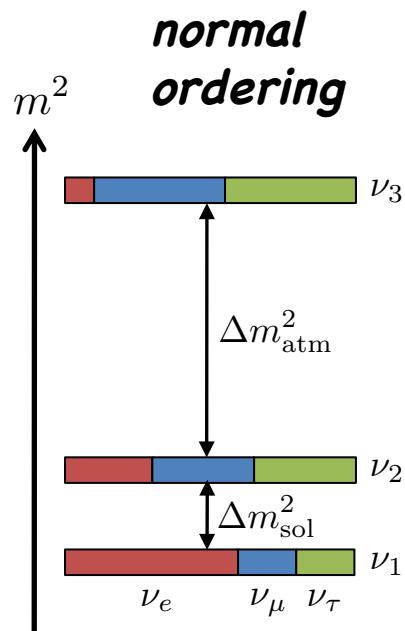


Open issues in 3-flavor mixing?

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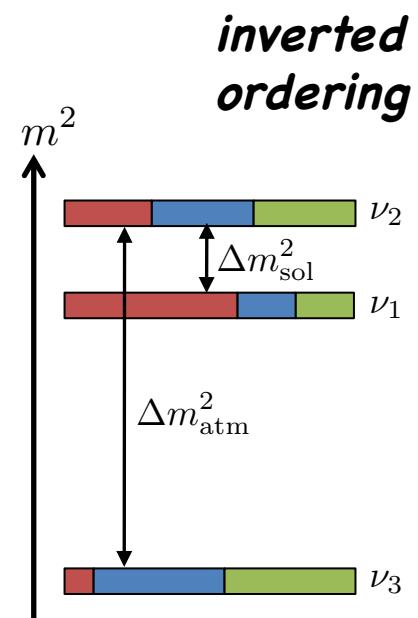
$$U_{3 \times 3} = U_{\text{PMNS}}$$

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What is the

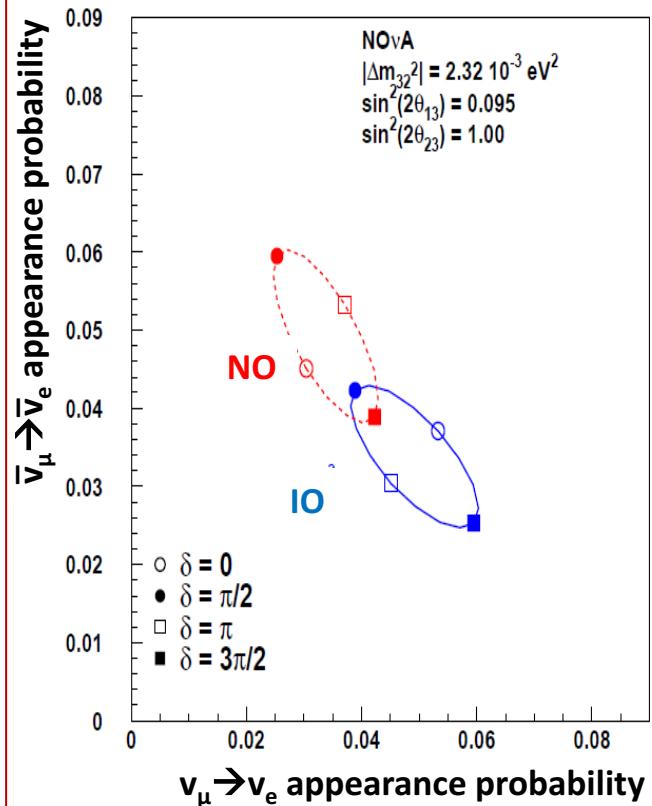
- **octant of θ_{23} ($\gtrless 45^\circ$)?**
- **value of CP-phase?**
- **mass ordering (MO)?**
(sign of Δm_{atm}^2)
- **unitarity of PMNS matrix (sterile ν 's)?**



Implications of neutrino mass ordering

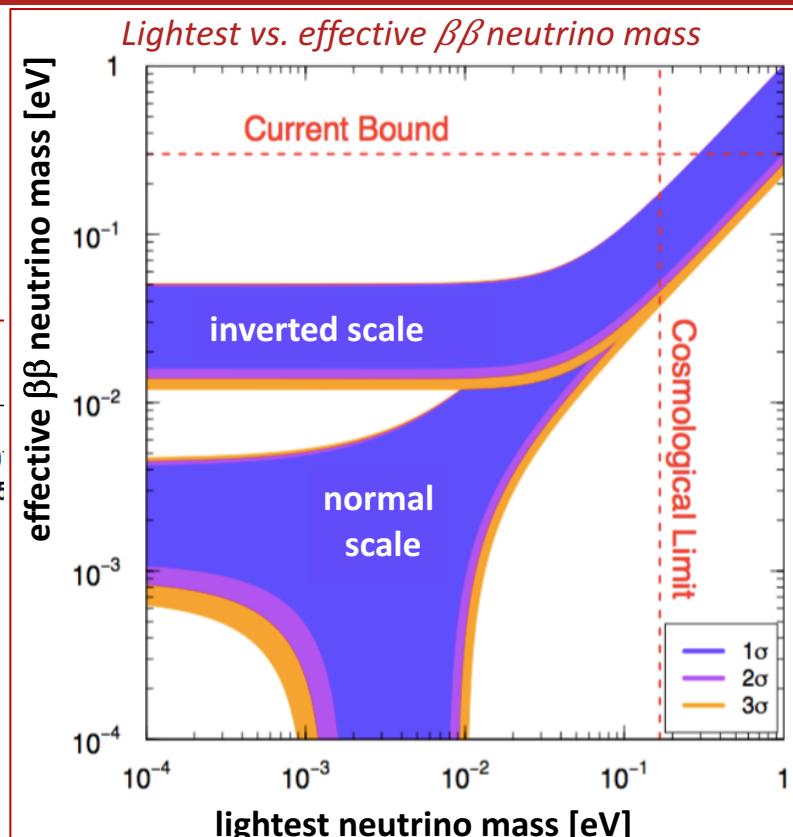
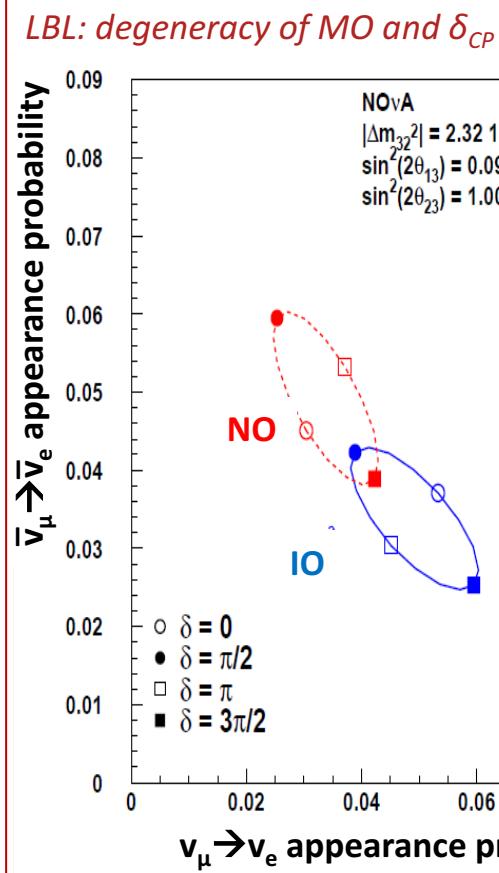
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LBL: degeneracy of MO and δ_{CP}



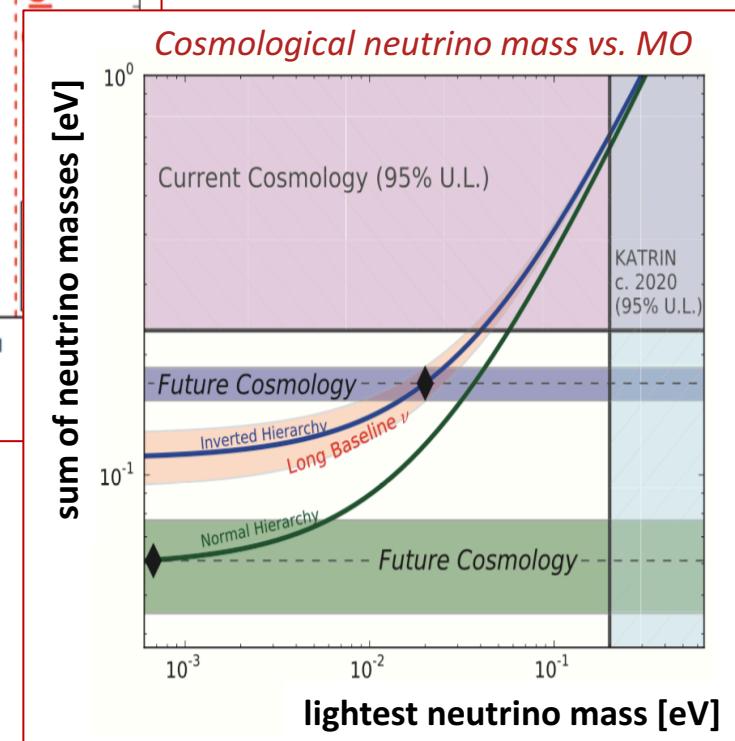
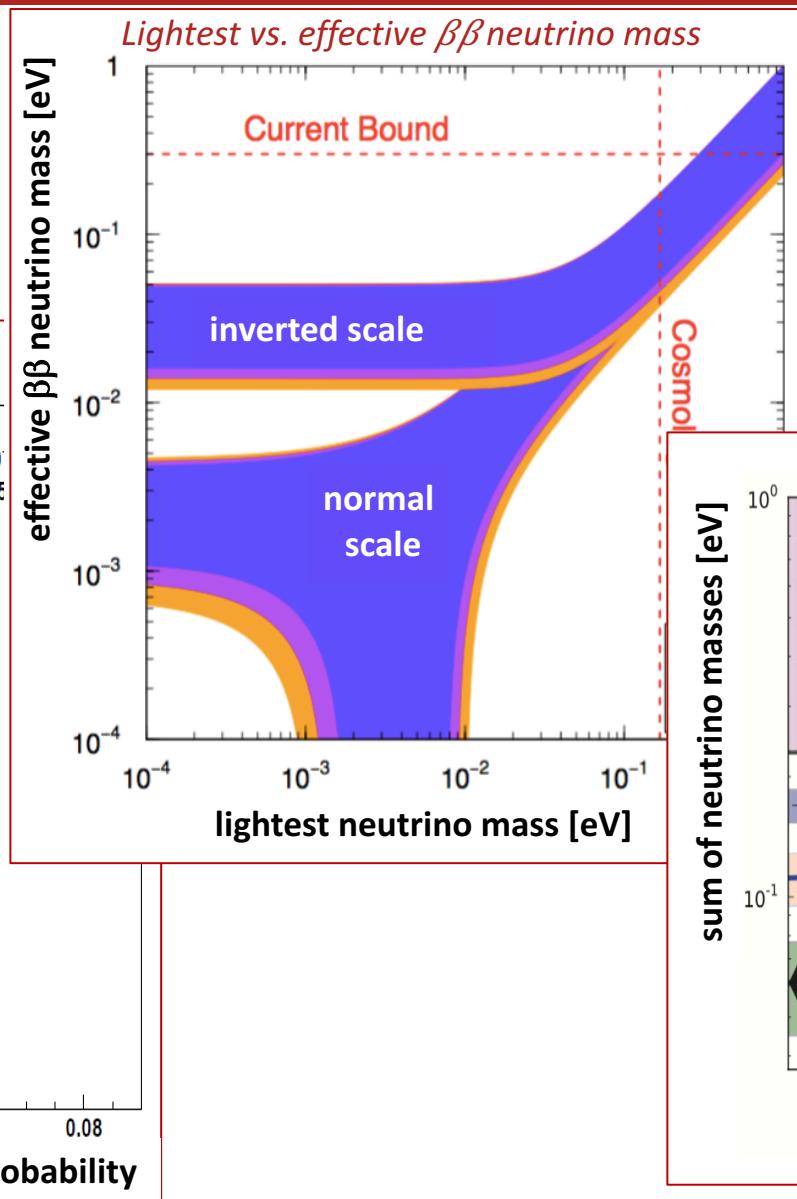
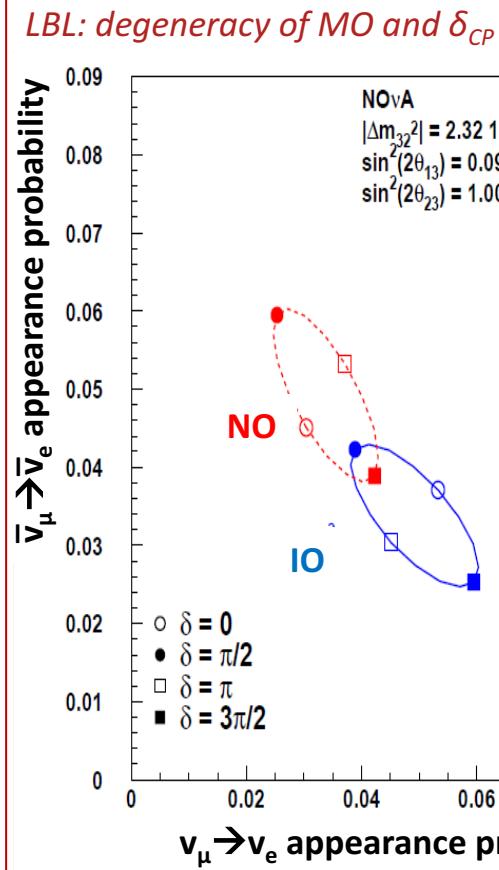
Implications of neutrino mass ordering

JG|U



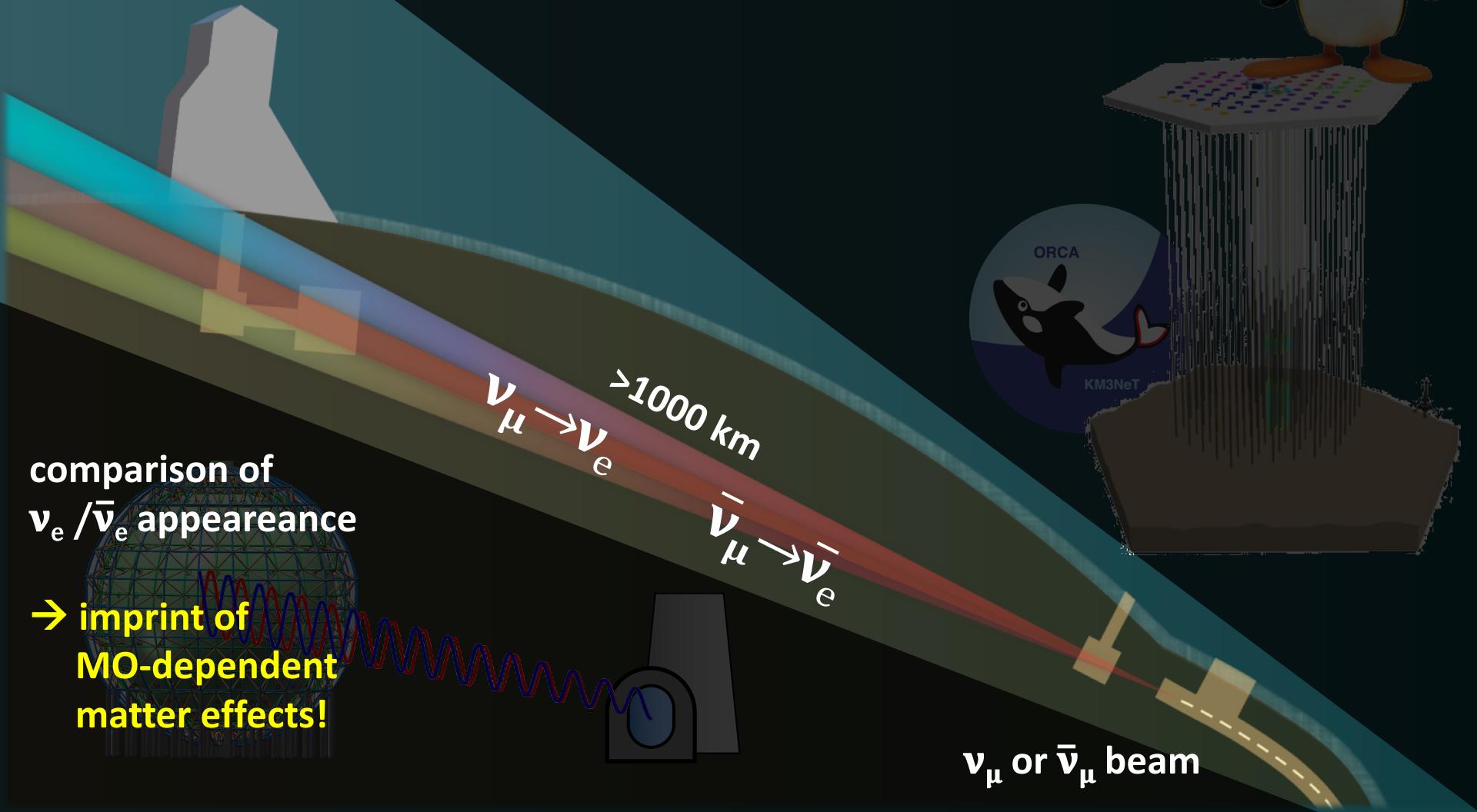
Implications of neutrino mass ordering

JG|U



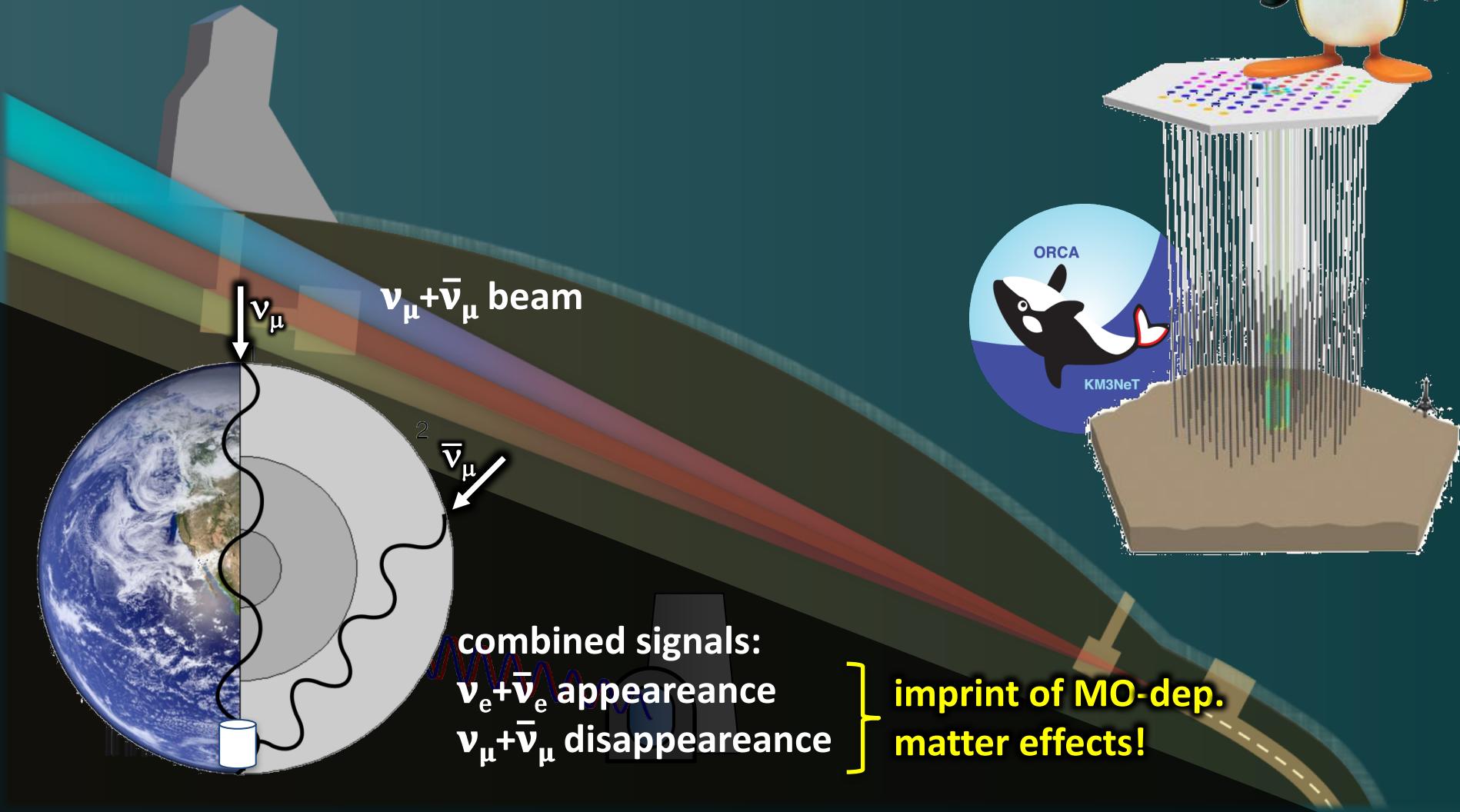
Concepts for MO measurement

1 Very-Long Baseline Neutrino Beams



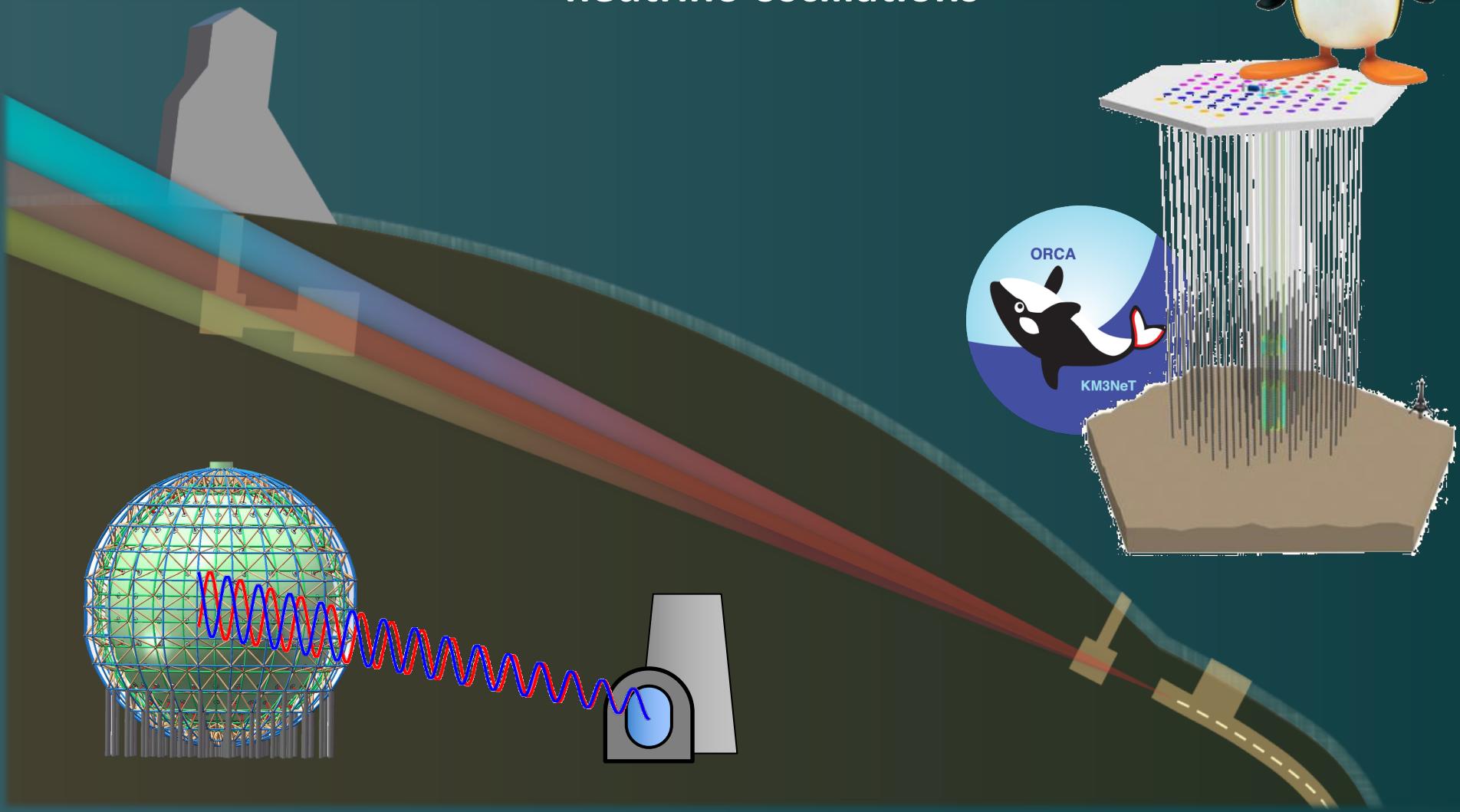
Concepts for MO measurement

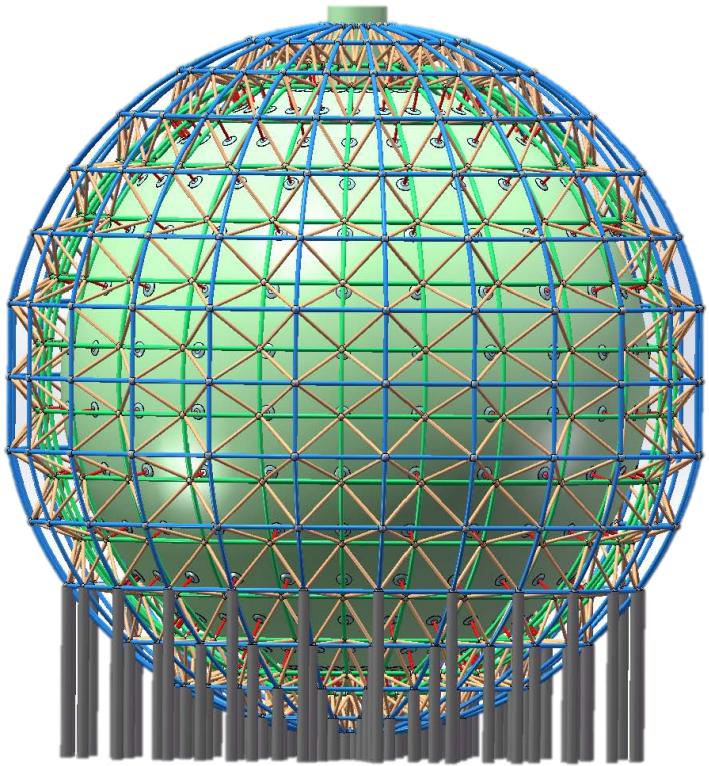
2 Low-energy atmospheric neutrino oscillations



Concepts for MO measurement

3 Mid-baseline reactor neutrino oscillations





JUNO characteristics

- liquid scintillator detector: 20ktons
- number of PMTs: 17,000 (20'')
- energy resolution: 3% at 1MeV
- rock overburden: 700m
- distance to reactors: 53km

Physics objectives

- neutrino mass hierarchy
- sub-% measurement of solar oscillation parameters
- astrophysical neutrinos
- nucleon decay
- eV-scale sterile neutrinos

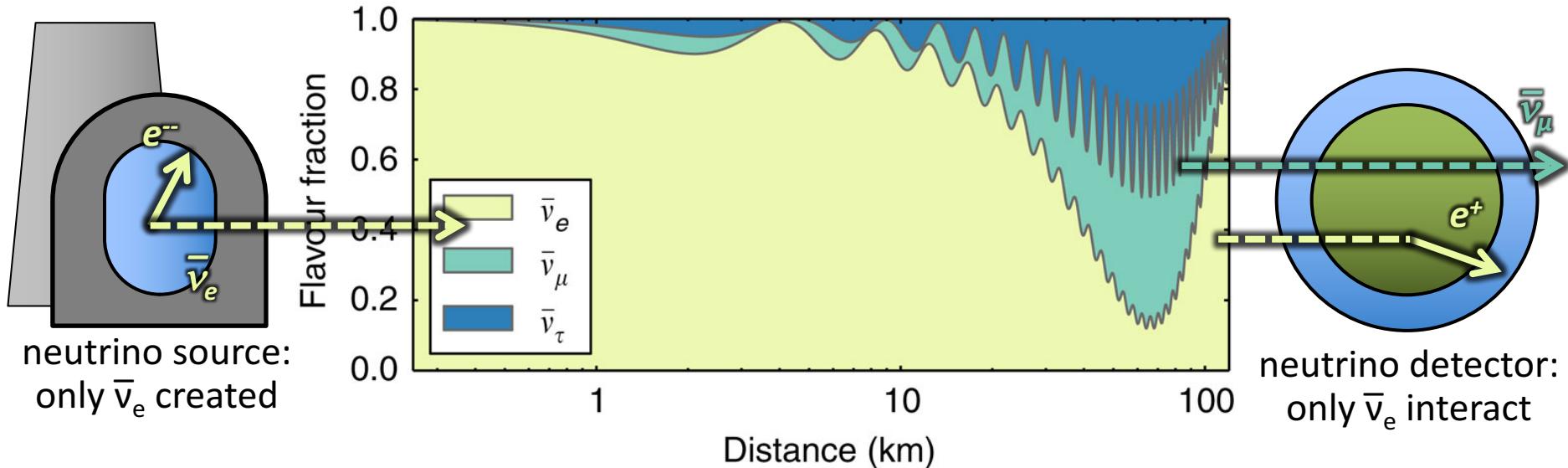


Reactor antineutrino oscillations

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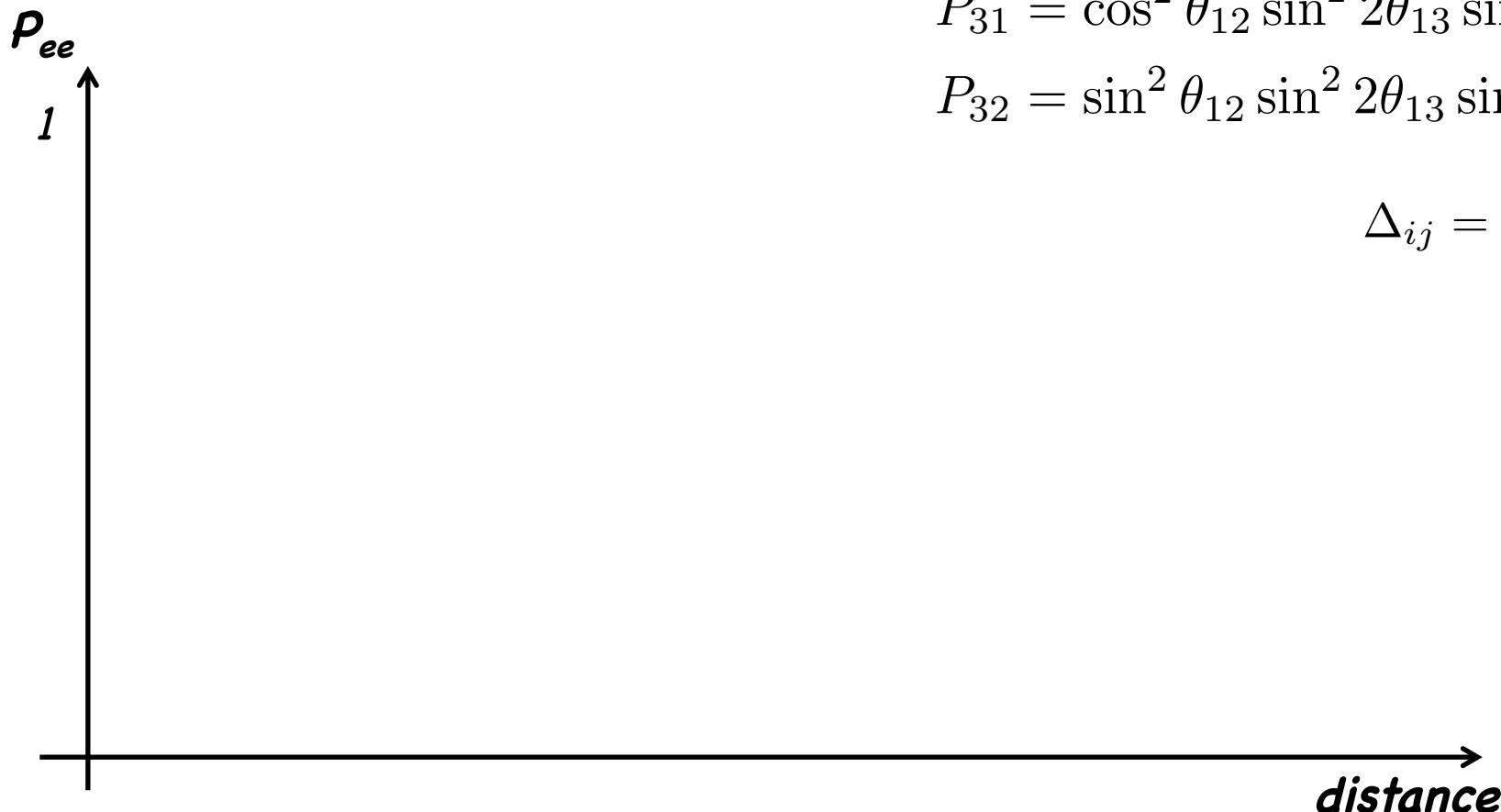
Common three-flavor reactor electron-antineutrino survival probability:

$$P_{ee} = 1 - \sin^2(2\theta_{13}) \sin^2\left(\frac{\Delta m_{31}^2}{4E}\right) - \sin^2(2\theta_{12}) \sin^2\left(\frac{\Delta m_{21}^2}{4E}\right)$$



- oscillation parameters are extracted from $\bar{\nu}_e$ disappearance pattern
- however, the formula above implicitly assumes $\Delta m_{31}^2 = \Delta m_{32}^2$

Reactor $\bar{\nu}$ oscillations: full 3-flavor picture JG|U



Survival probability

$$P_{\bar{e}\bar{e}} = 1 - P_{21} - P_{31} - P_{32}$$

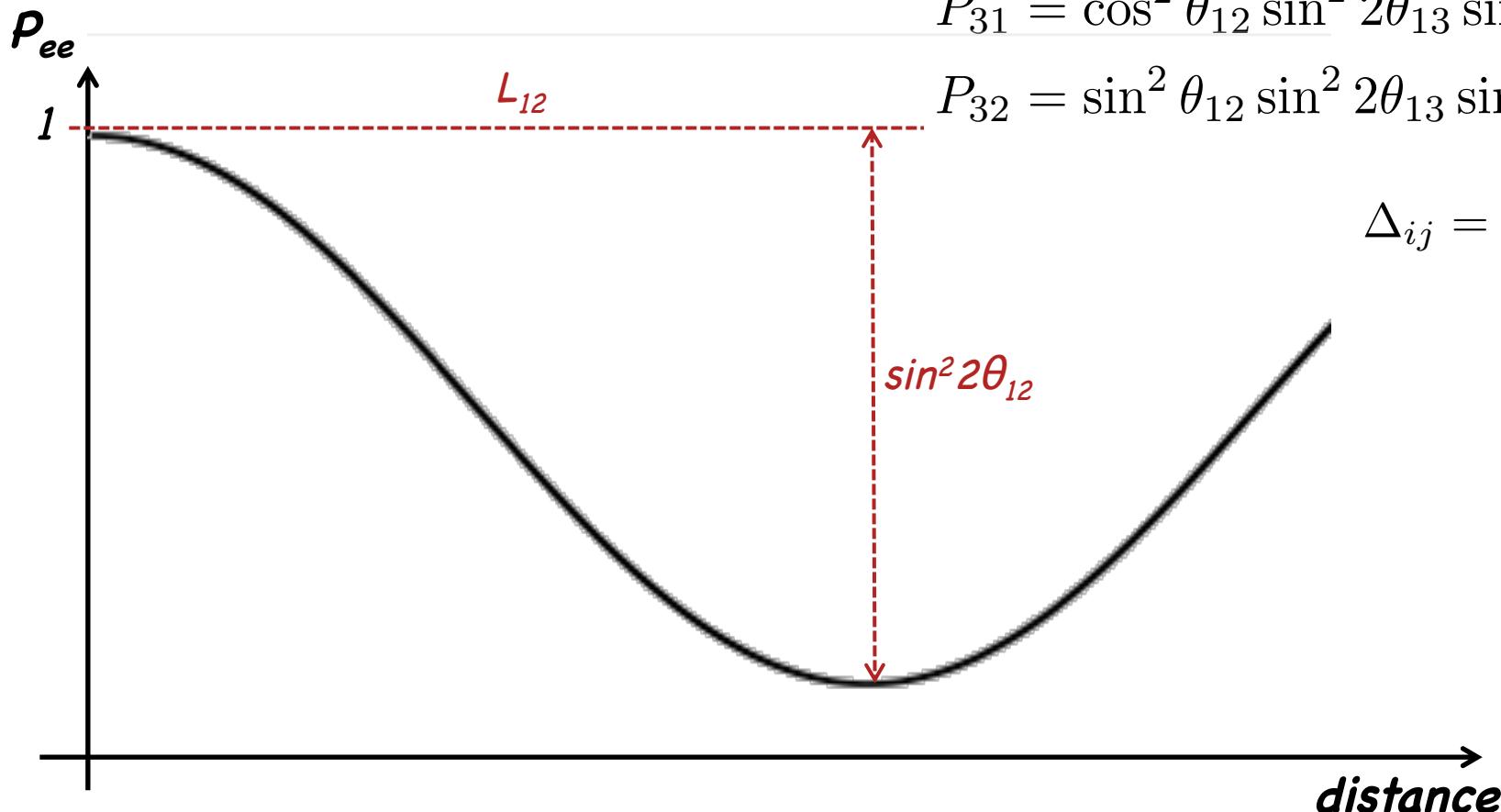
$$P_{21} = \cos^4 \theta_{13} \sin^2 2\theta_{12} \sin^2 \Delta_{21}$$

$$P_{31} = \cos^2 \theta_{12} \sin^2 2\theta_{13} \sin^2 \Delta_{31}$$

$$P_{32} = \sin^2 \theta_{12} \sin^2 2\theta_{13} \sin^2 \Delta_{32}$$

$$\Delta_{ij} = \frac{\Delta m_{ij}^2 L}{4E}$$

Reactor $\bar{\nu}$ oscillations: full 3-flavor picture JG|U



Survival probability

$$P_{\bar{e}\bar{e}} = 1 - P_{21} - P_{31} - P_{32}$$

$$P_{21} = \cos^4 \theta_{13} \sin^2 2\theta_{12} \sin^2 \Delta_{21}$$

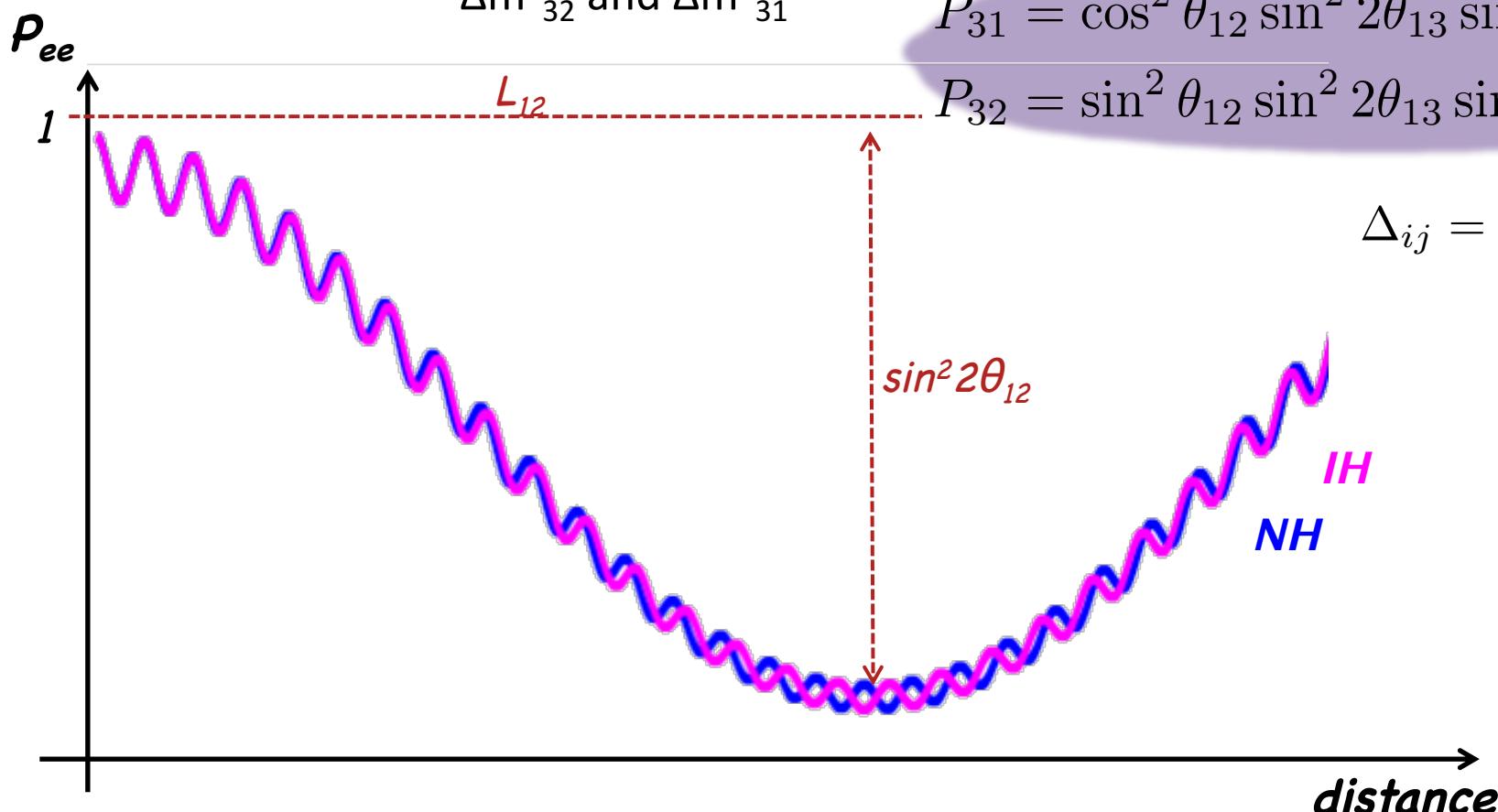
$$P_{31} = \cos^2 \theta_{12} \sin^2 2\theta_{13} \sin^2 \Delta_{31}$$

$$P_{32} = \sin^2 \theta_{12} \sin^2 2\theta_{13} \sin^2 \Delta_{32}$$

$$\Delta_{ij} = \frac{\Delta m_{ij}^2 L}{4E}$$

Reactor $\bar{\nu}$ oscillations: full 3-flavor picture JG|U

- subdominant oscillation pattern depends on phase terms of P_{31}/P_{32}
- depends on **relative sizes** of Δm^2_{32} and Δm^2_{31}



Survival probability

$$P_{\bar{e}\bar{e}} = 1 - P_{21} - P_{31} - P_{32}$$

$$P_{21} = \cos^4 \theta_{13} \sin^2 2\theta_{12} \sin^2 \Delta_{21}$$

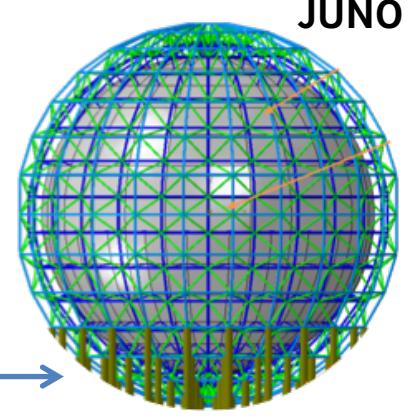
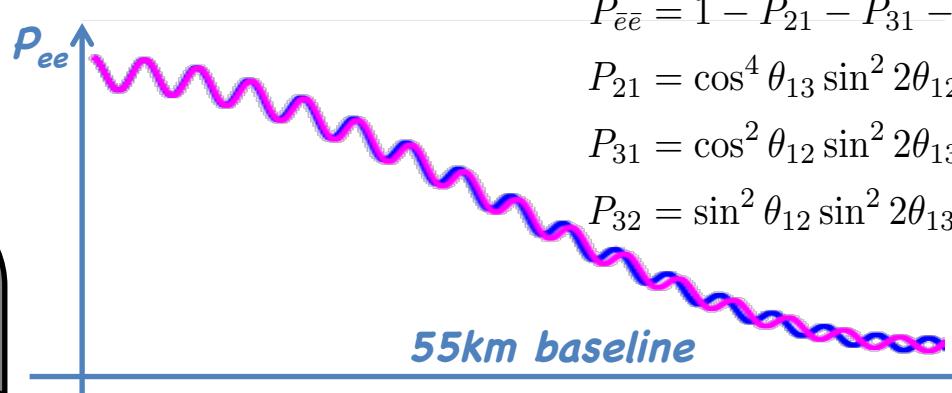
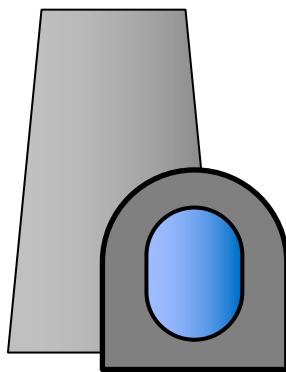
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$$\Delta_{ij} = \frac{\Delta m_{ij}^2 L}{4E}$$

Oscillation pattern at 1st solar maximum

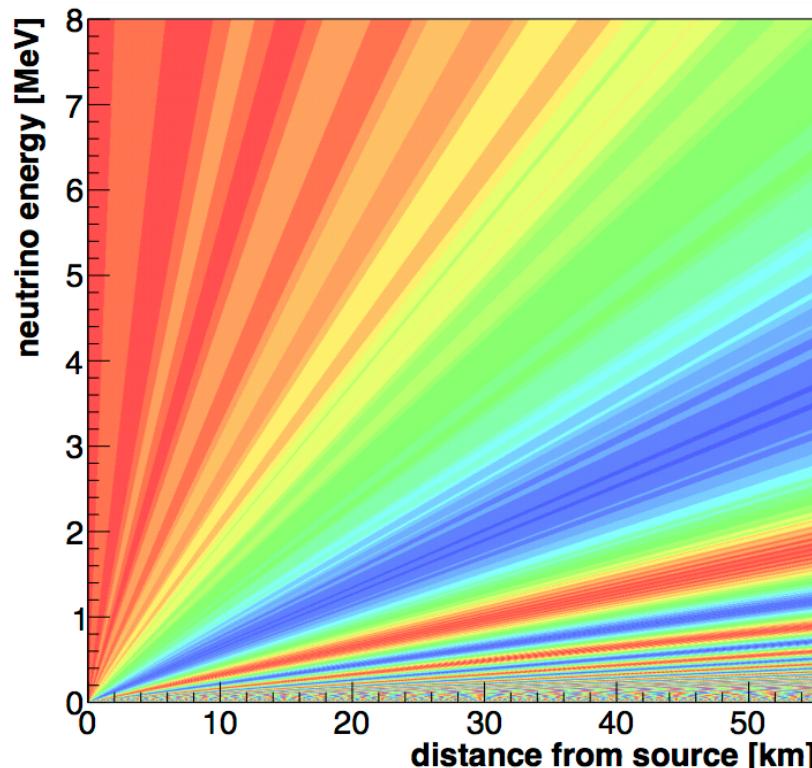
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Nuclear reactors at

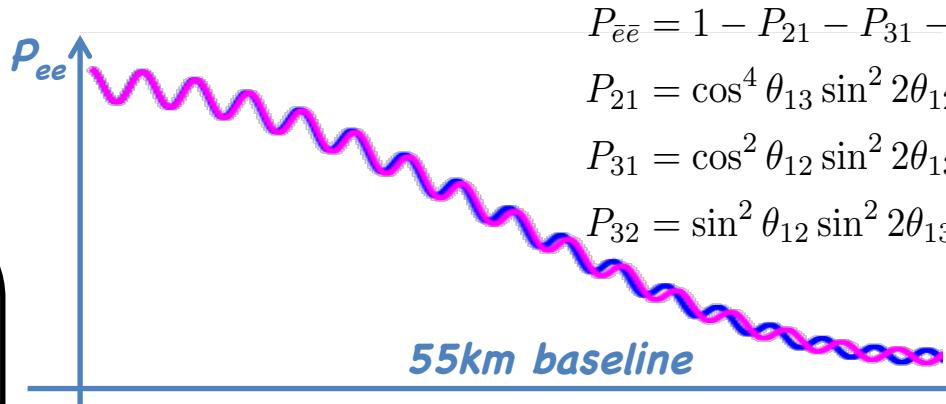
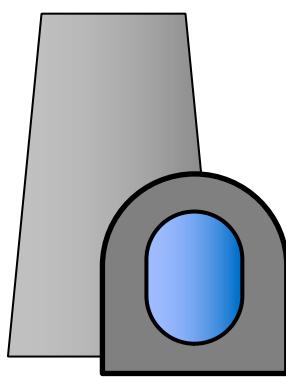
- Yangjiang
- Taishan
- (so. China)

Total power:
(eventually)
38 GW



Oscillation pattern at 1st solar maximum

JG|U

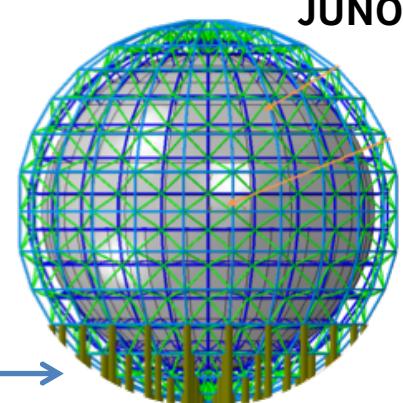


$$P_{\bar{e}\bar{e}} = 1 - P_{21} - P_{31} - P_{32}$$

$$P_{21} = \cos^4 \theta_{13} \sin^2 2\theta_{12} \sin^2 \Delta_{21}$$

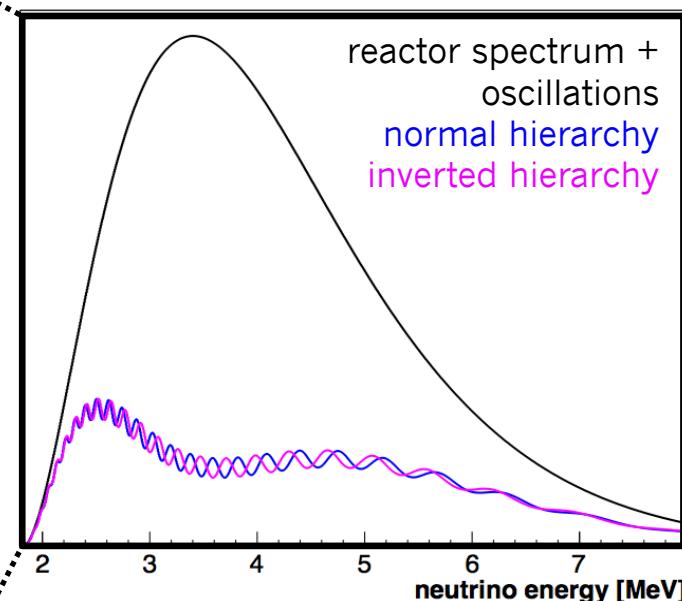
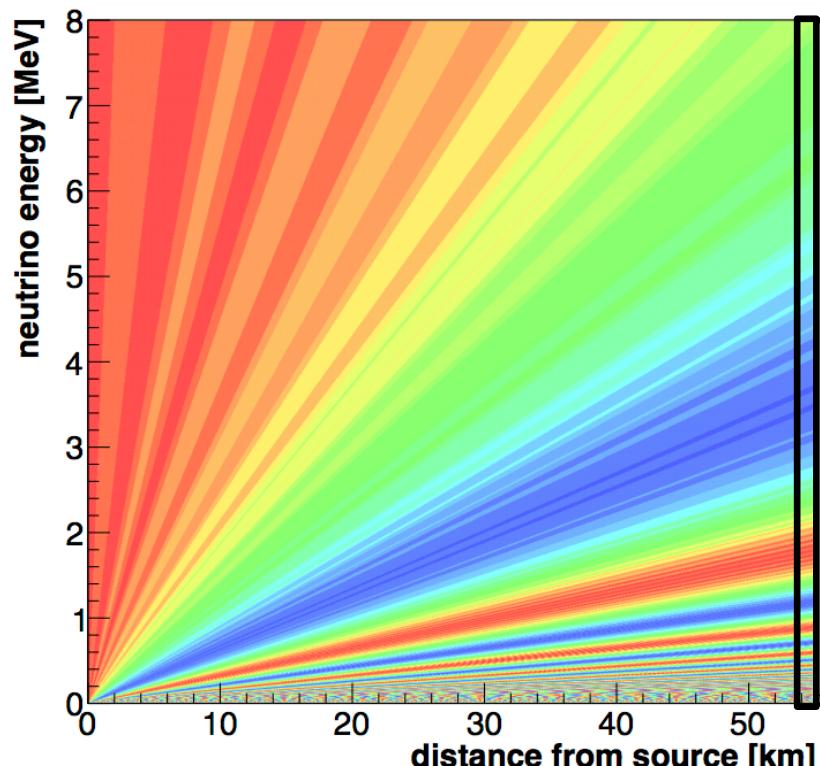
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$$P_{32} = \sin^2 \theta_{12} \sin^2 2\theta_{13} \sin^2 \Delta_{32}$$



Nuclear reactors at
▪ Yangjiang
▪ Taishan
(so. China)

Total power:
(eventually)
38 GW



→ MH from spectral wiggles

Basic detector requirements for JUNO

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- reactor antineutrinos at MeV energies
 - **Liquid-scintillator detector**
 - Detection by inverse beta decay
- signature in position of spectral wiggles
 - **~3% energy resolution** at 1 MeV
 - photoelectron yield: **~1,100 pe/MeV**
- large distance to source and high-statistics measurement
 - large target mass: **20 kilotons of LAB**
- cosmogenic background
 - rock overburden of **~700 m**



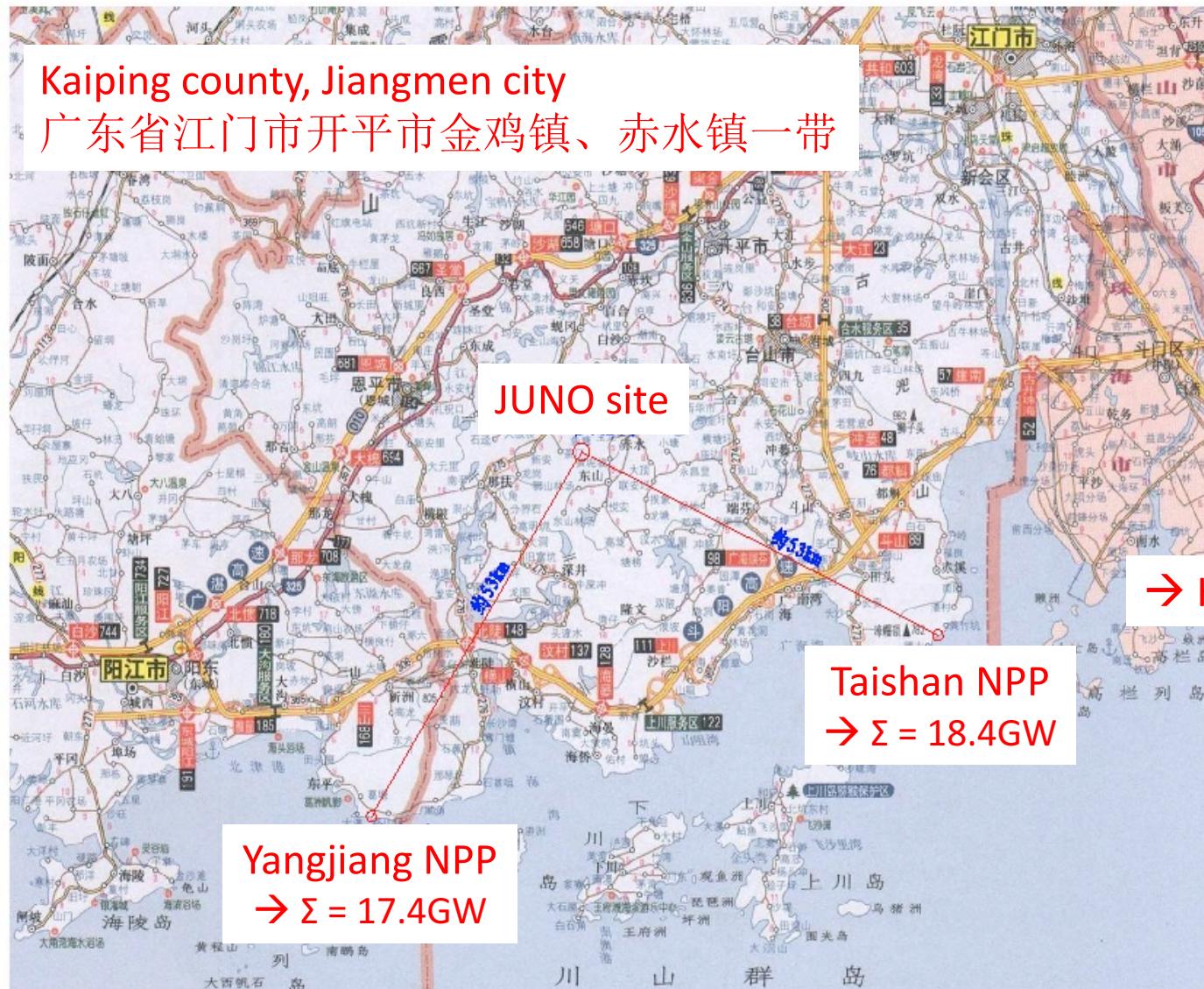
JUNO Experimental Setup

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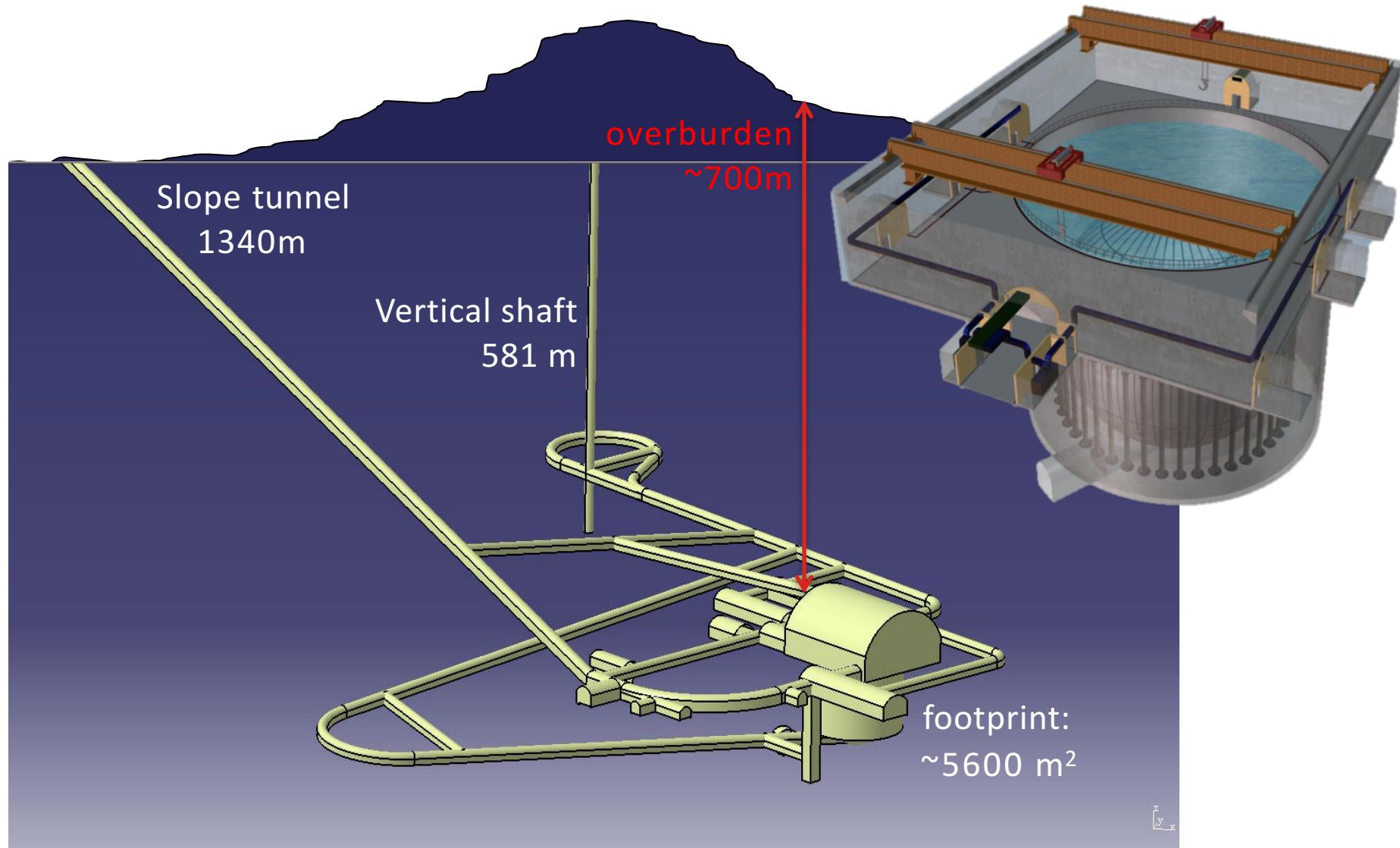
JUNO Experimental Setup

JG|U



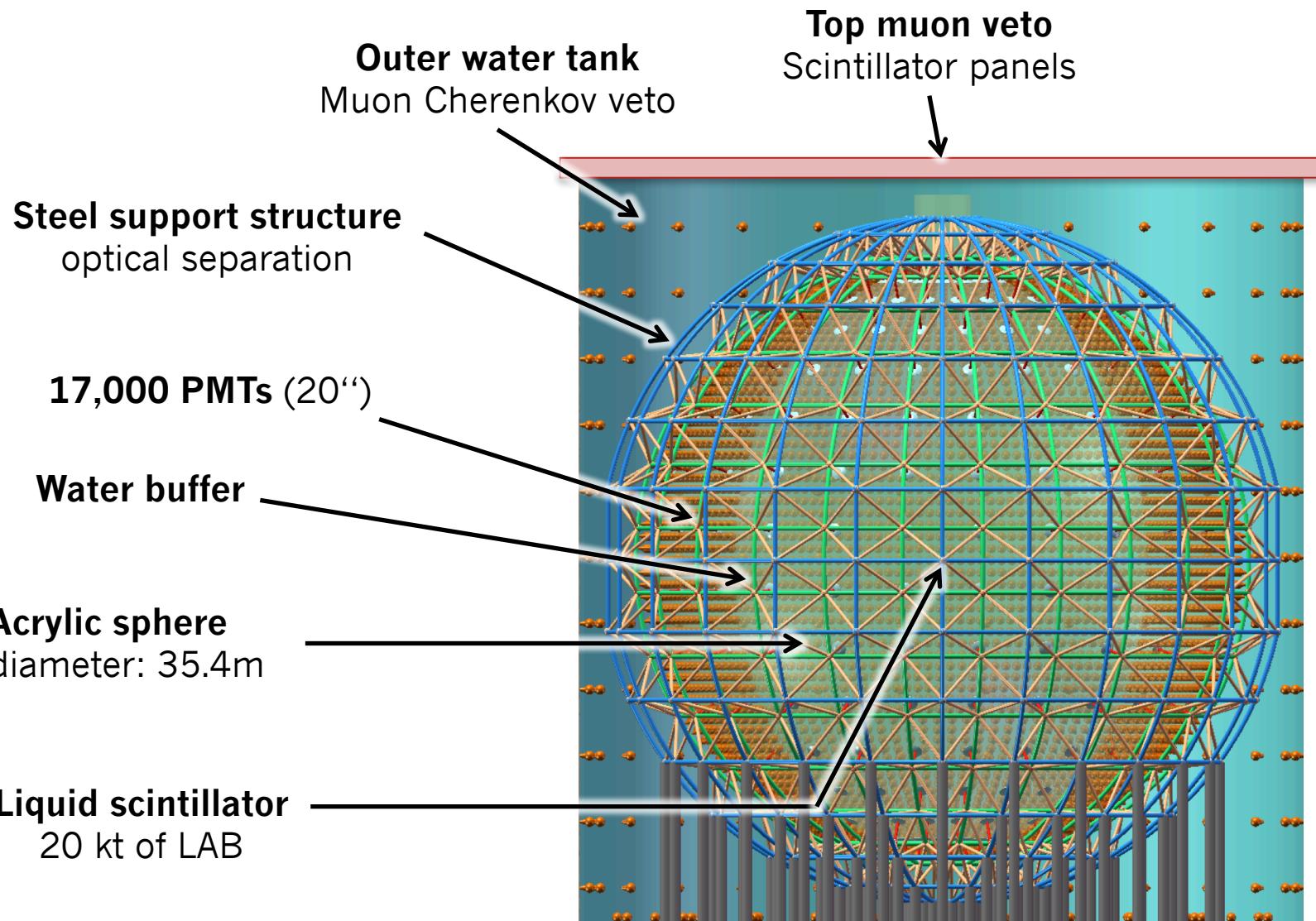
New underground laboratory

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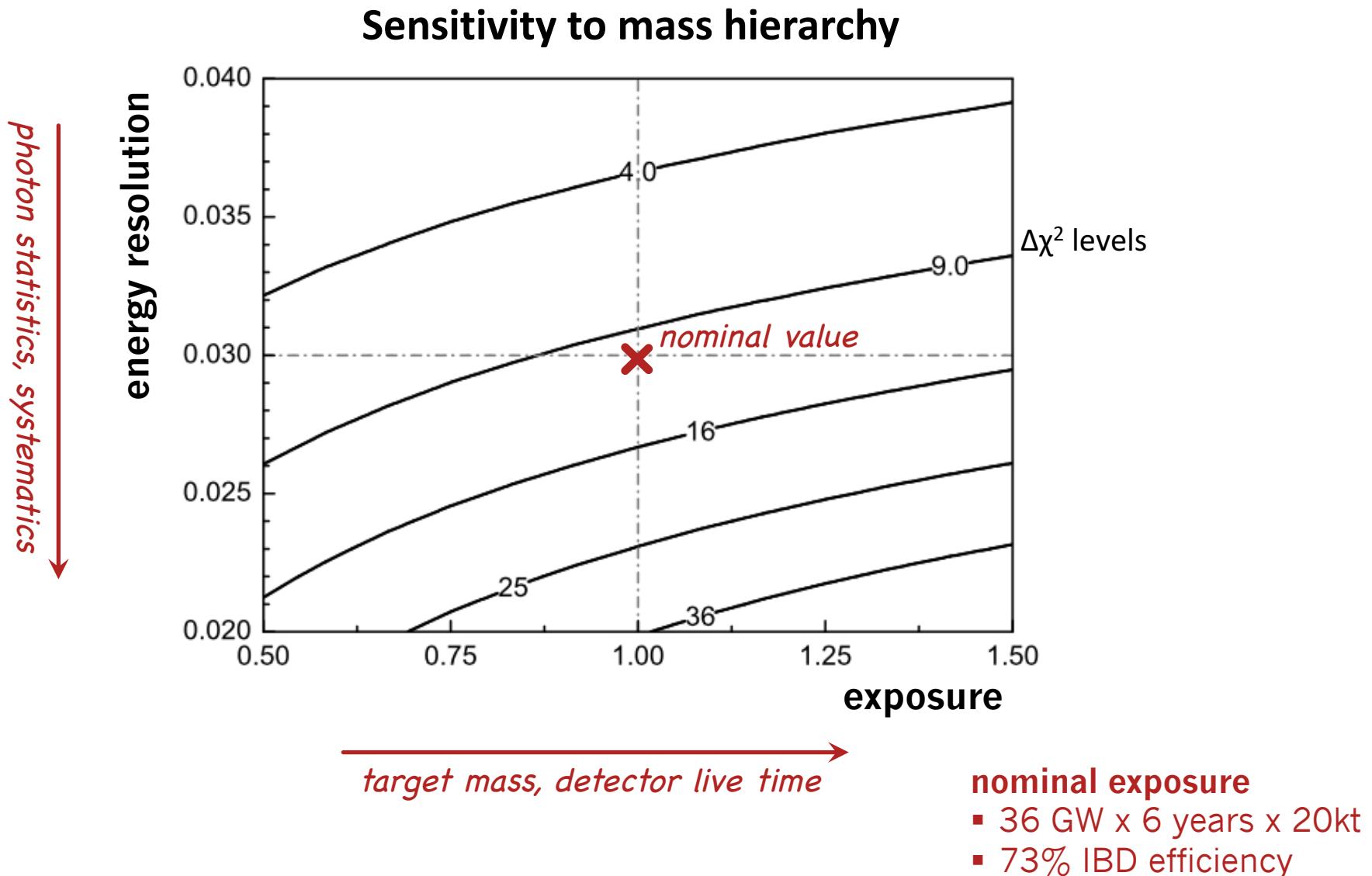
JUNO Detector layout

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Sensitivity to mass ordering ¹

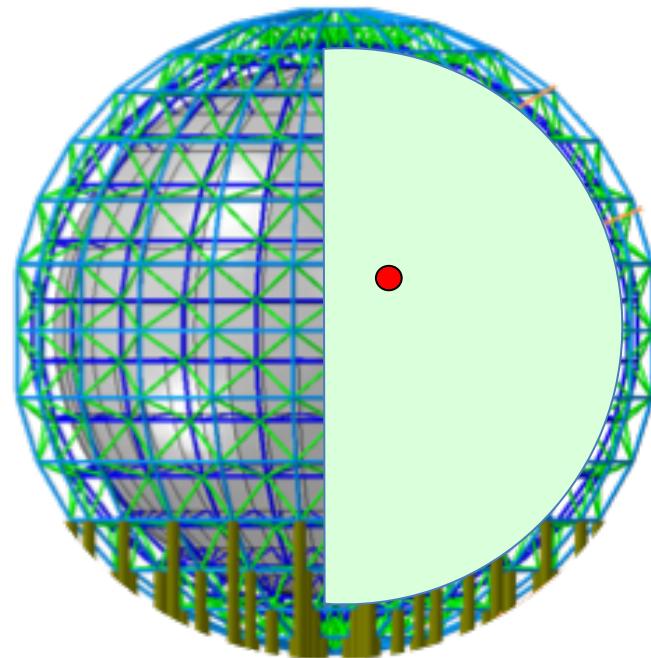
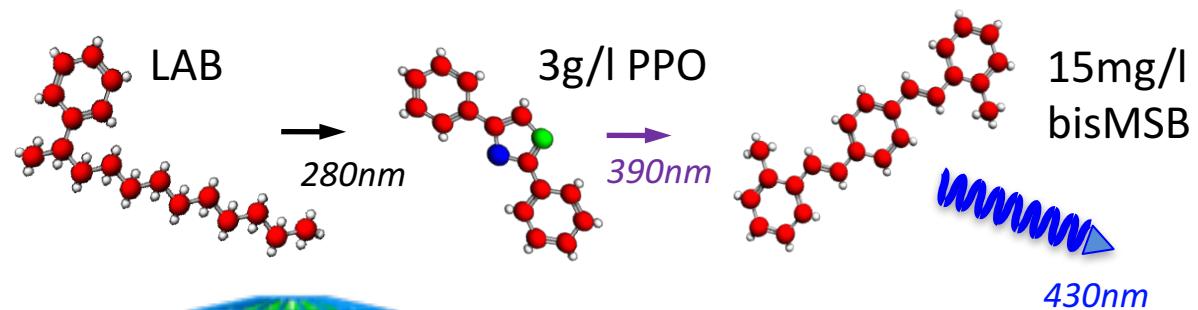
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Energy resolution: Photon statistics

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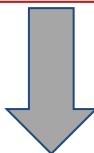
Scintillator light yield:
>10⁴ photons per MeV



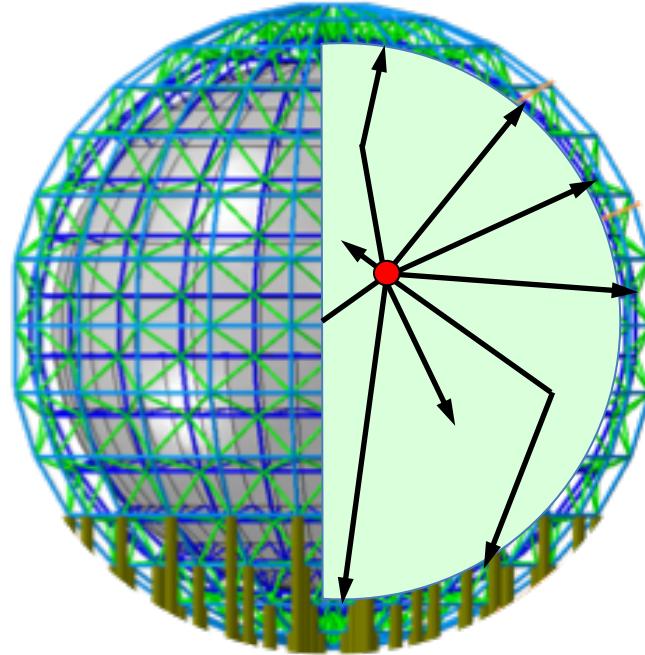
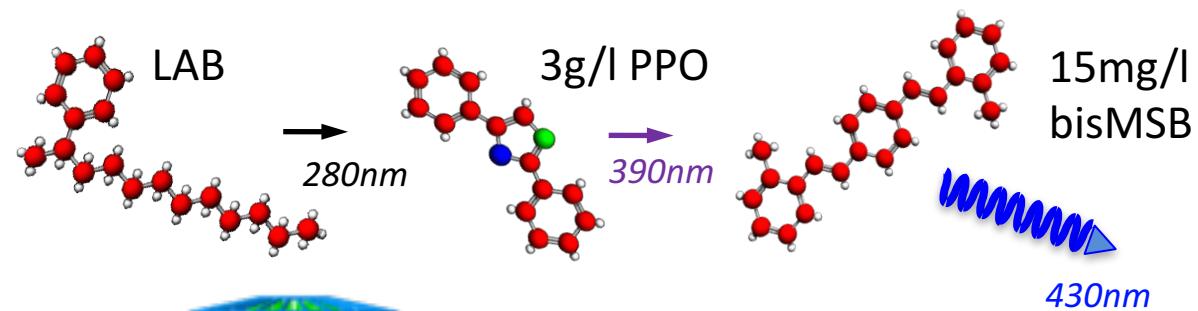
Energy resolution: Photon statistics

JG|U

Scintillator light yield:
>10⁴ photons per MeV



Light absorption in the
liquid scintillator



Energy resolution: Photon statistics

JG|U

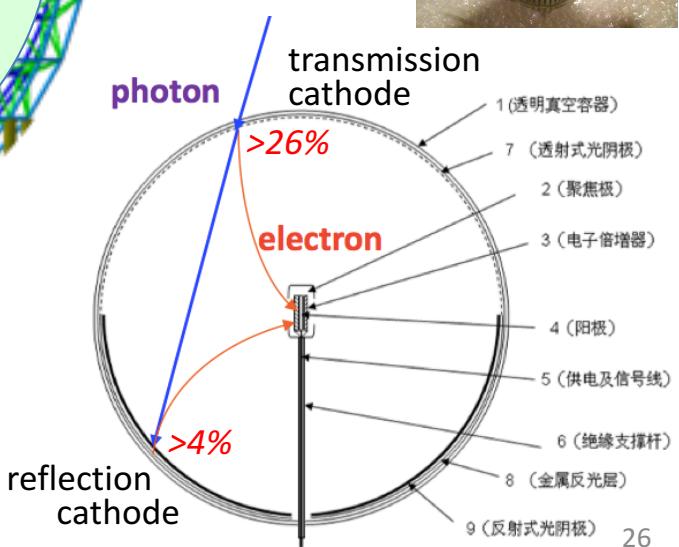
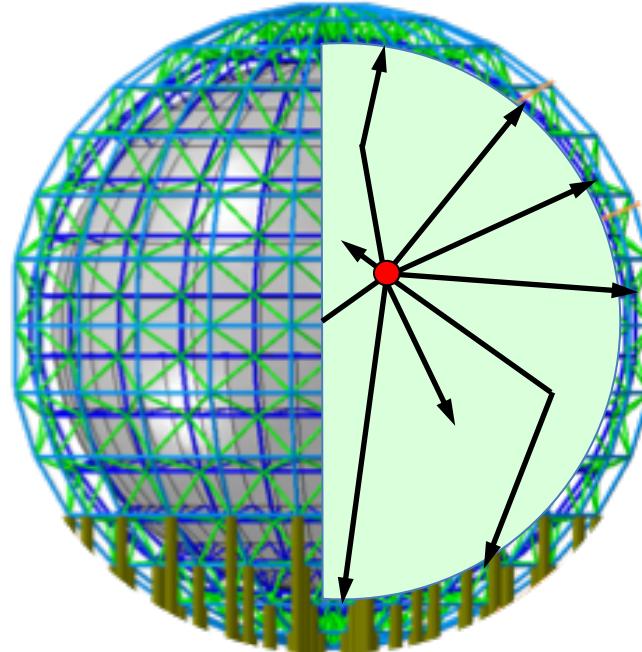
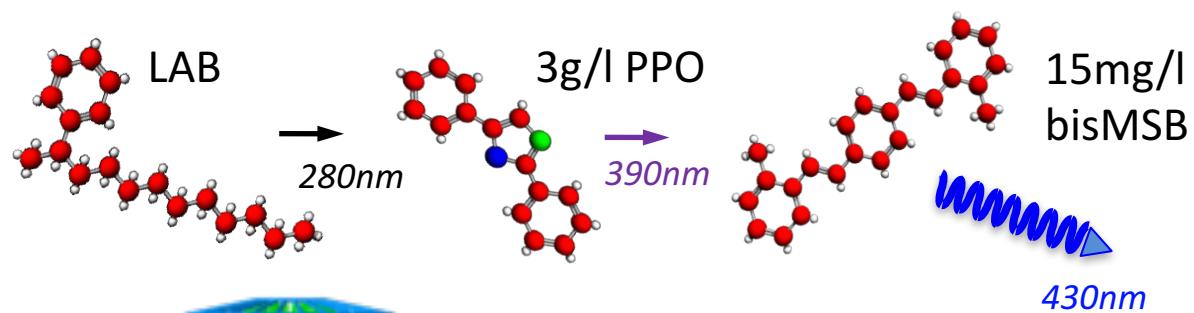
Scintillator light yield:
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Light absorption in the
liquid scintillator



PMT coverage (75%)
detection efficiency (>30%)



Energy resolution: Photon statistics

JG|U

Scintillator light yield:
>10⁴ photons per MeV



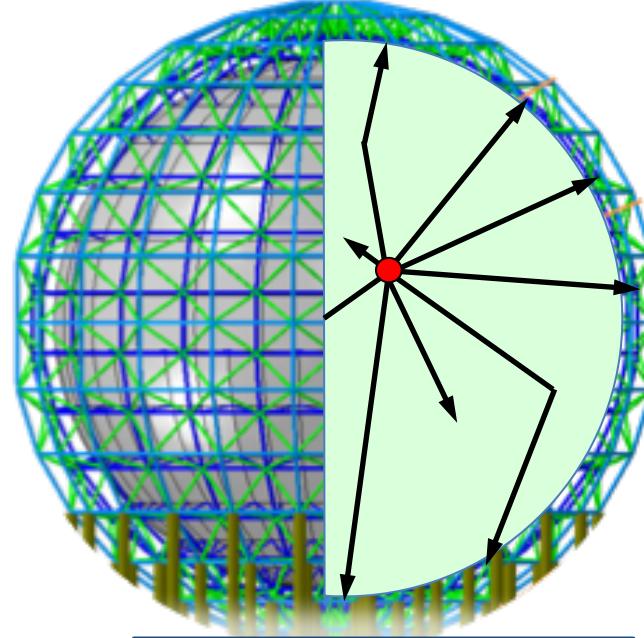
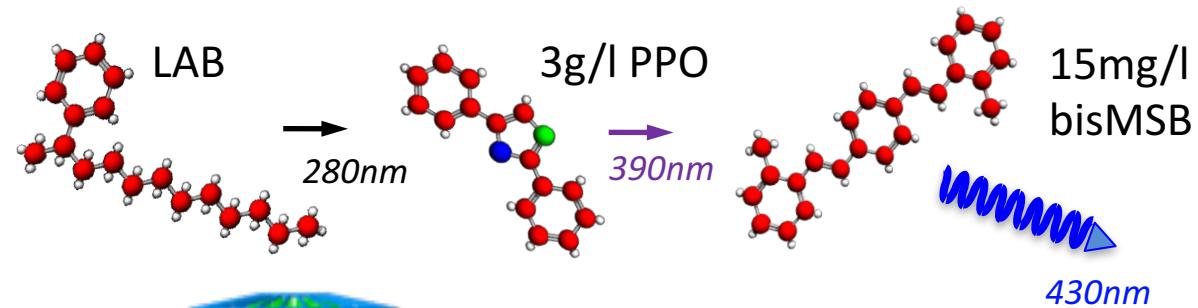
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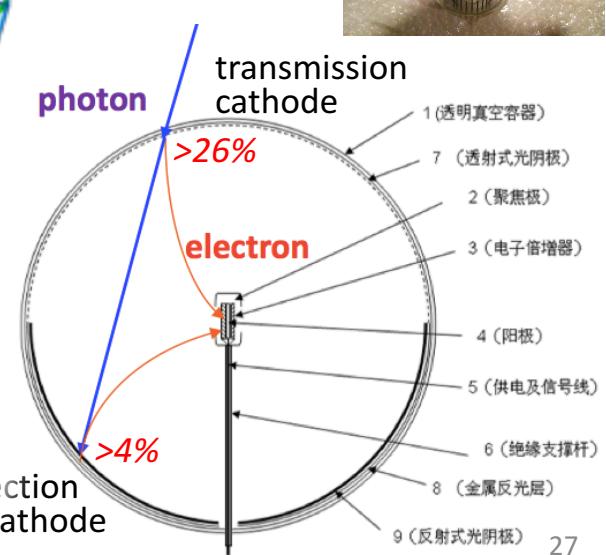


Photoelectron yield:
>1100 pe/MeV



Energy resolution:

$$\frac{\Delta E}{E} \sim \frac{1}{\sqrt{N_{pe}}} \leq \frac{3\%}{\sqrt{E [MeV]}}$$



Energy resolution: Systematic effects

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Energy resolution function

$$\frac{\Delta E}{E} = \sqrt{\frac{a^2}{E} + b^2 + \frac{c^2}{E^2}}$$

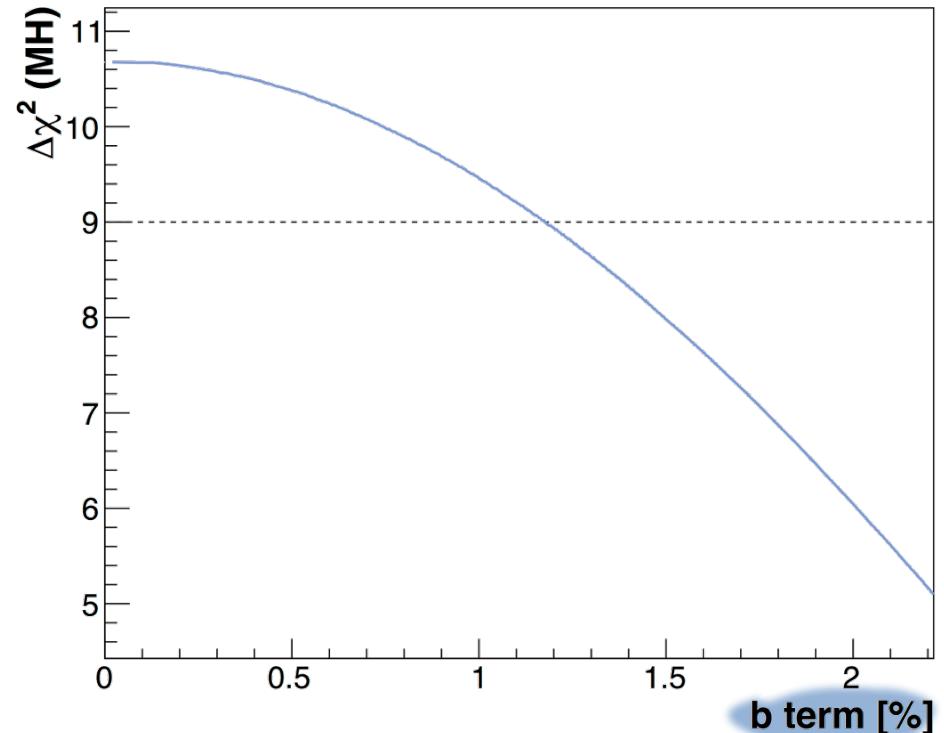
a term:

stochastic term (*photon statistics*)

b & c terms:

systematic contributions (*detector effects*)

- PMT dark noise
- linearity of electronics
- position reconstruction uncertainty
- ...



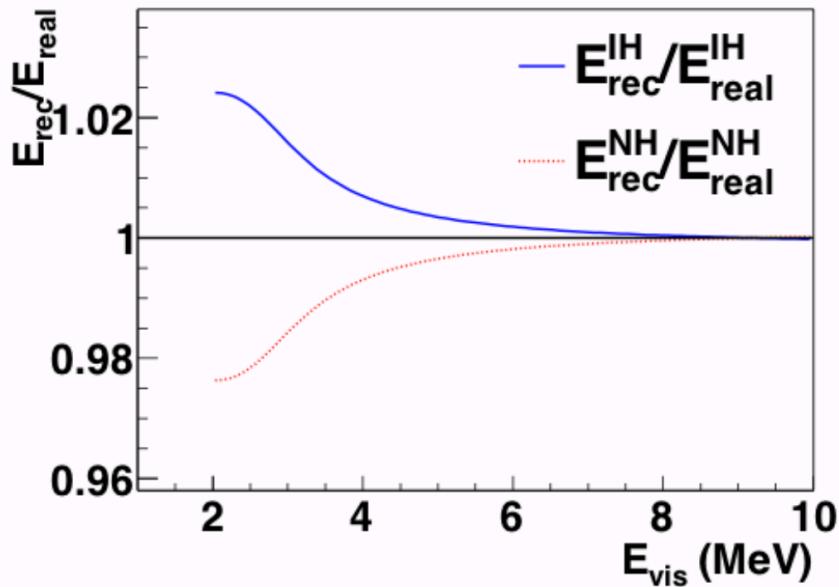
- calibrations w/ radioactive sources deployed in LS (γ 's, e^+ , AmBe for n's etc.)
- multi-calorimetry with small PMTs ...

Energy scale non-linearities

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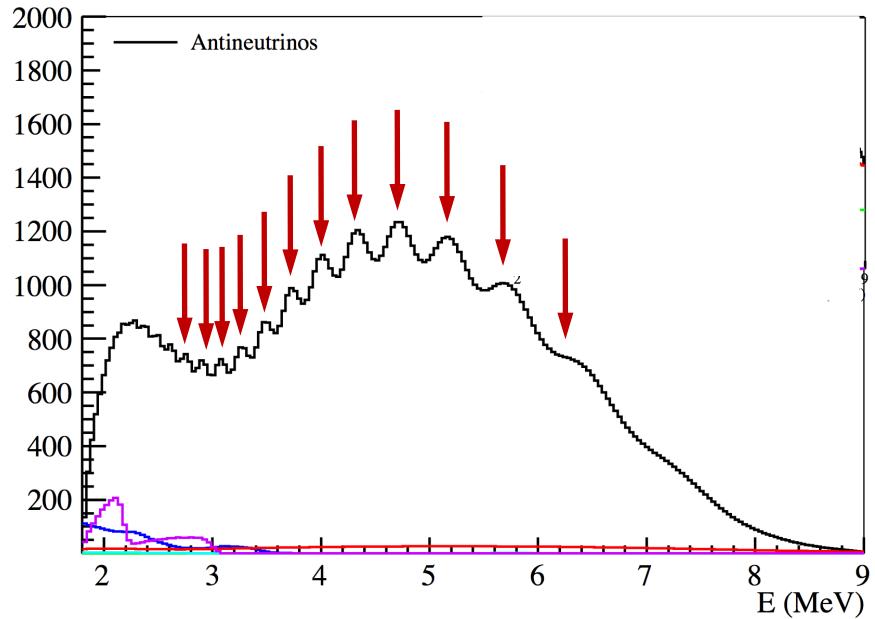
→ potentially very dangerous

example of non-linearity curves
canceling the signature of MO



E_{rec} : reconstructed energy
 E_{real} : true energy

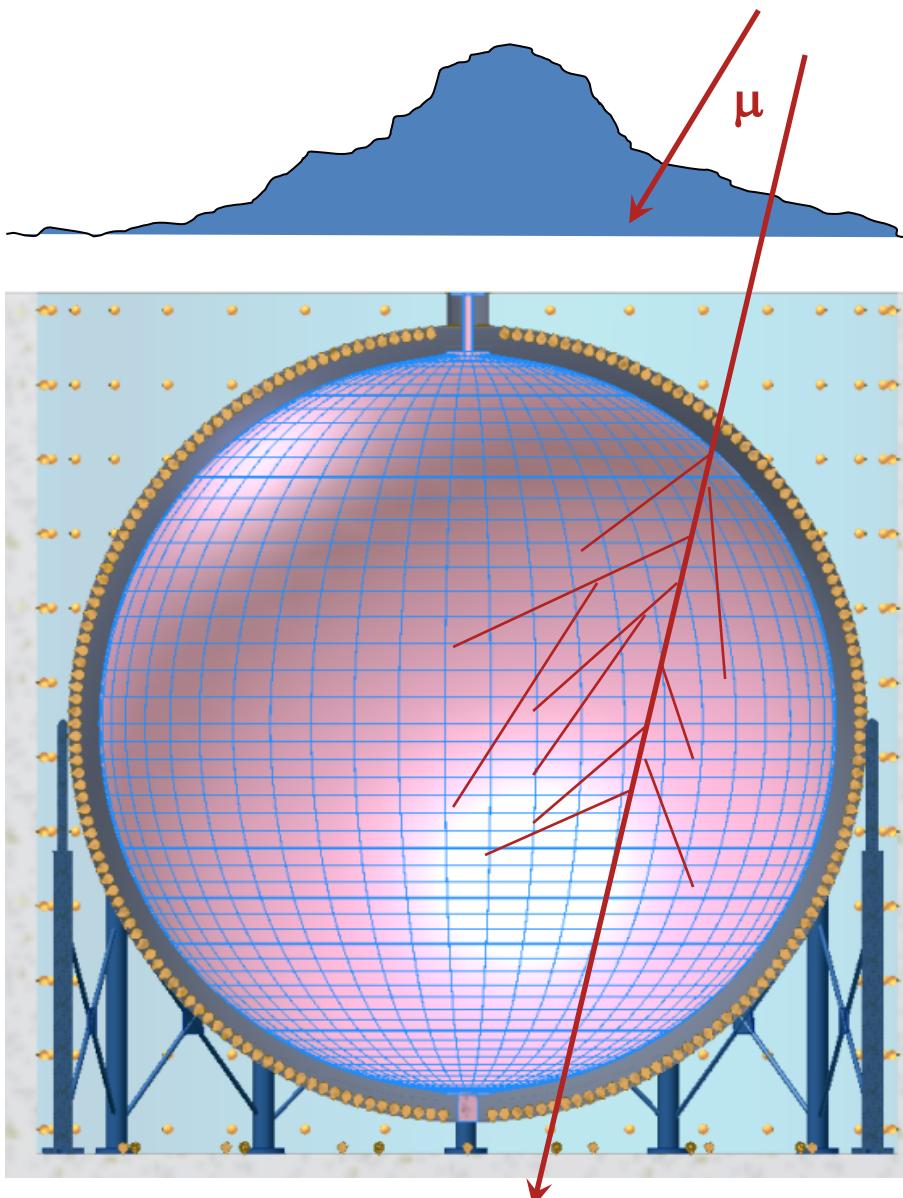
however, relative position of peaks
constrained by oscillation physics
→ active test for energy non-linearities



→ systematic studies show that effect can be largely avoided by **self-calibration**

Cosmogenic backgrounds¹

JG|U



Cosmic background levels

- rock shielding: 700 m
 - μ rate in Central Detector: $\sim 3 \text{ s}^{-1}$
 - showering μ rate: $\sim 0.5 \text{ s}^{-1}$
- *radioisotopes from ^{12}C spallation*

Most dangerous: βn -emitters

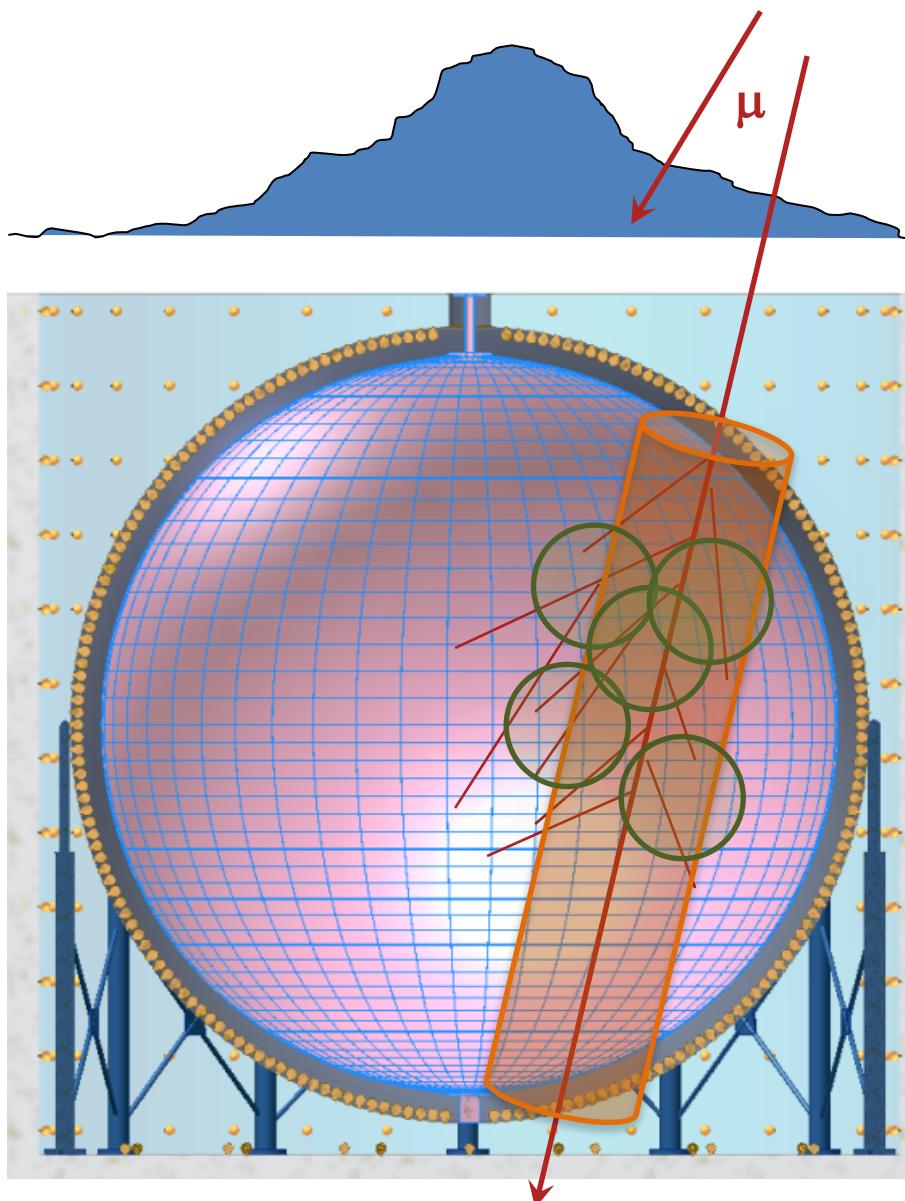
- $^{9}\text{Li} \rightarrow ^{9}\text{Be} + e^- + \nu_e$ $[\tau(^{9}\text{Li}) \sim 257\text{ms}]$
 └─ $2\alpha + n$
- prompt electron signal
+ delayed neutron capture
- mimics neutrino (IBD) signature!

Expected ^{9}Li rate: $\sim 80 \text{ d}^{-1}$

- signal to background $< 1:1$
- veto based on parent μ mandatory!

Cosmogenic backgrounds²

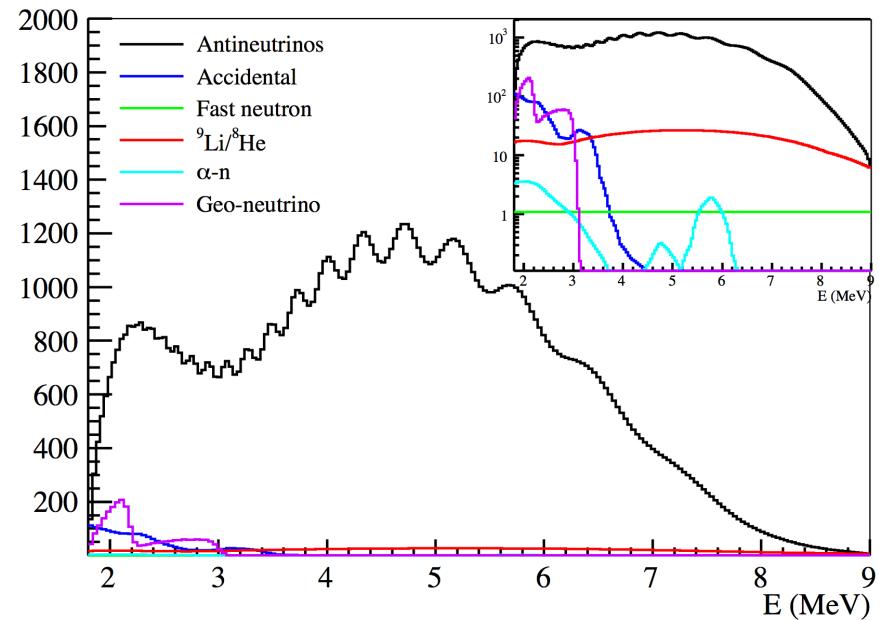
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Possibilities for vetoing ${}^9\text{Li}$

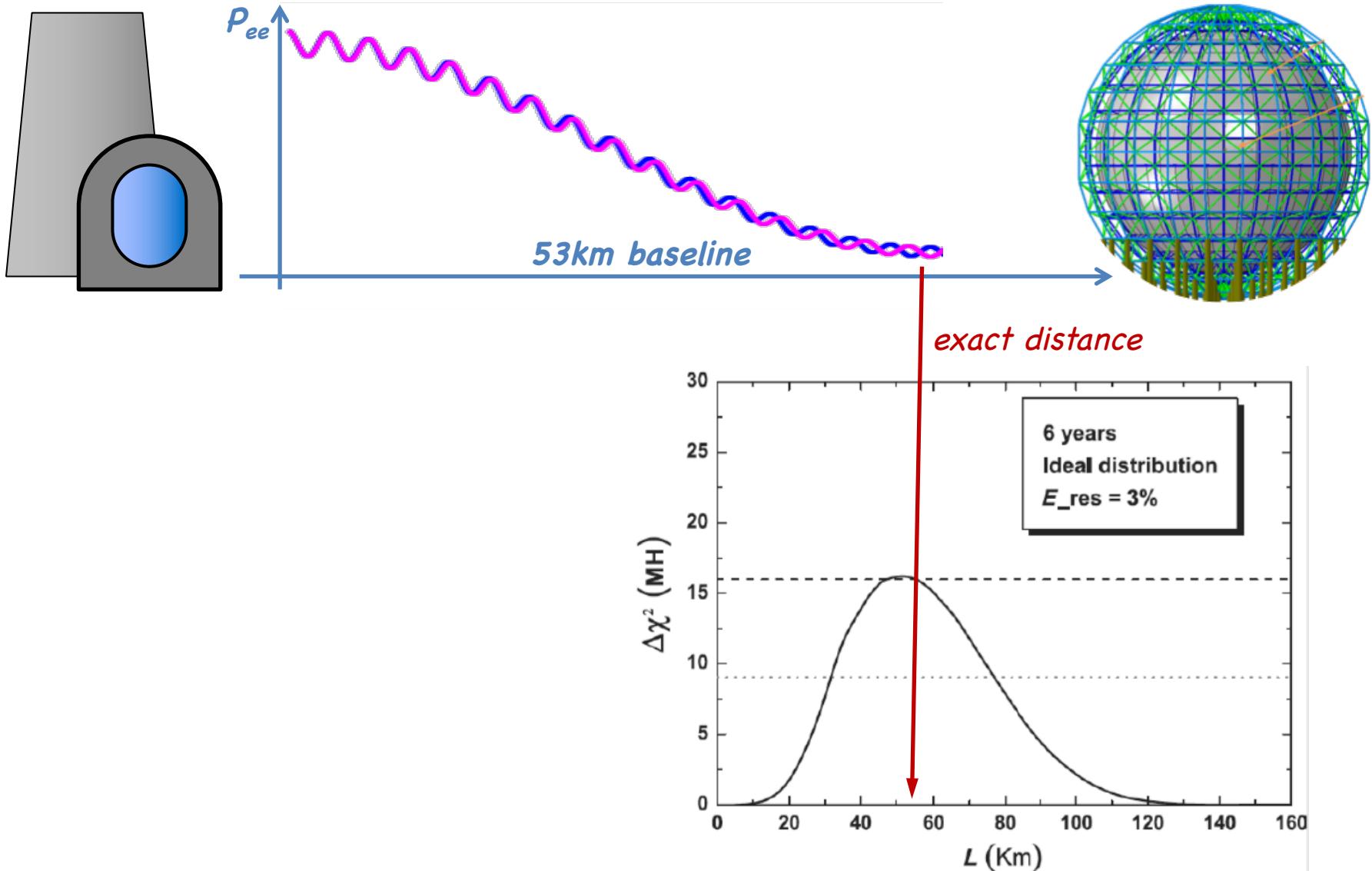
- radial cut around muon track
- identification of showering muons
 - cuts relative to neutron vertices
 - local (?) dE/dx of muons
 - ...

current veto: ${}^9\text{Li}/{}^8\text{He}: 77\text{d}^{-1} \rightarrow 1.6 \text{ d}^{-1}$
17% loss of exposure



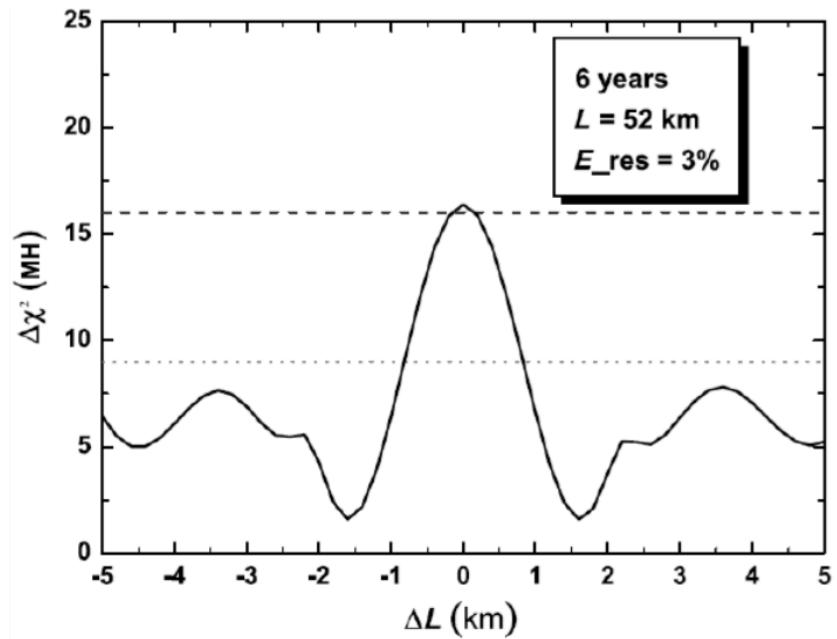
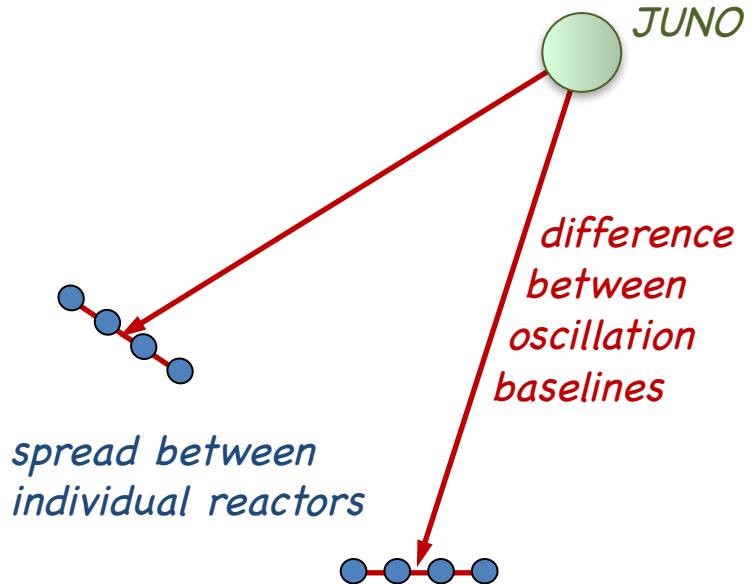
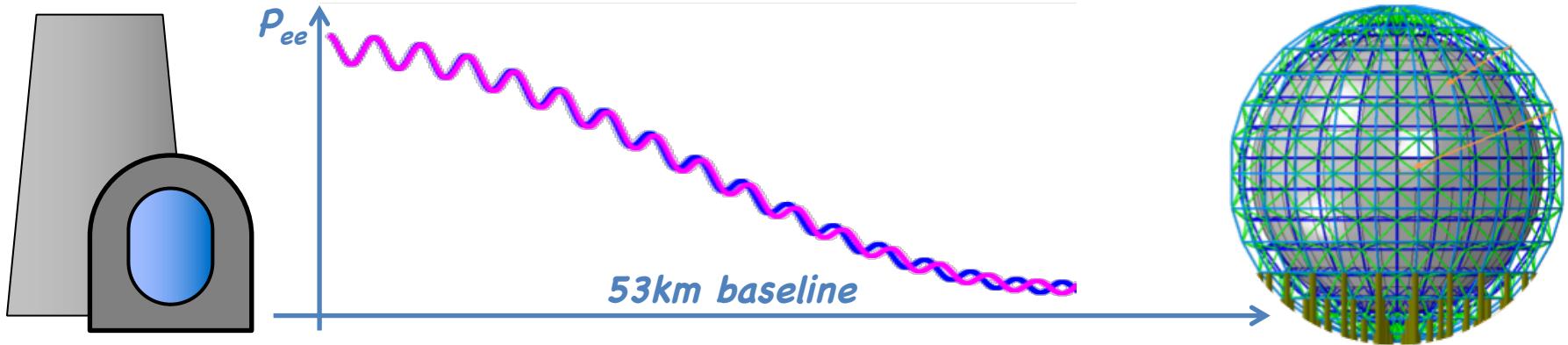
Systematics from oscillation baselines¹

JG|U



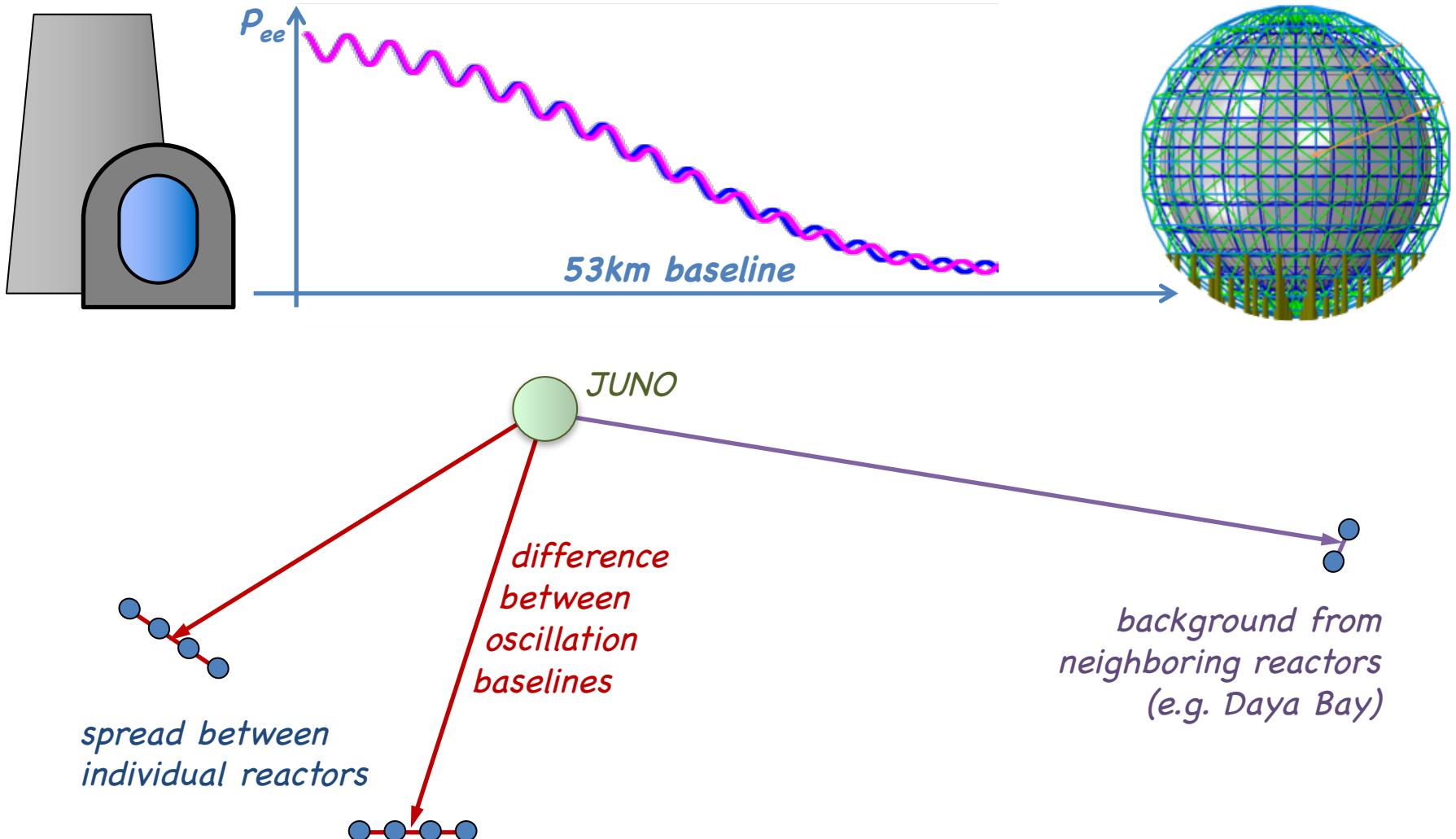
Systematics from oscillation baselines²

JG|U



Systematics from oscillation baselines ³

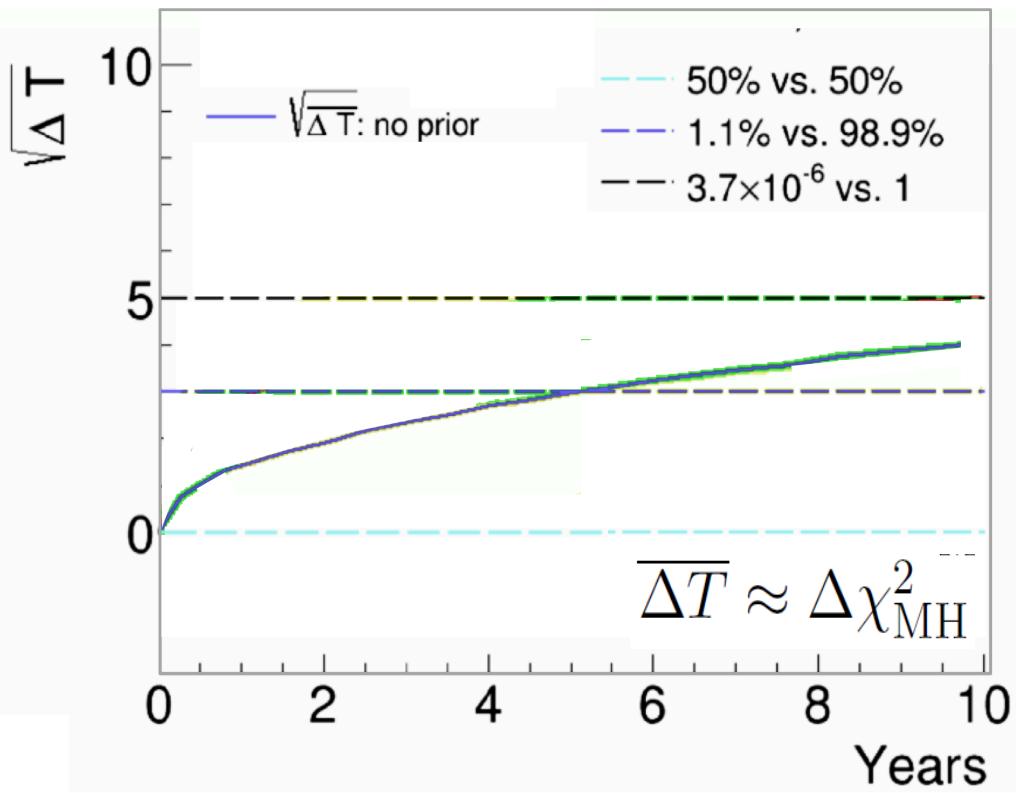
JG|U



Sensitivity to mass ordering ²

JG|U

JUNO, arXiv:1507.05613



JUNO's expected sensitivity level

(assuming 3% energy resolution)

- JUNO alone based on 6 years: $\sim 3\sigma$

defining factors:

- E resolution: 3% at 1MeV
- statistics: 100,000 ev

Sensitivity budget	$\Delta\chi^2$
Statistics only	+16
different core distances	-3
reactor background	-1.7
spectral shape	-1
S/B ratio (rate)	-0.6
S/B ratio (shape)	-0.1

Input from accelerator/atmospheric ν's

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- JUNO measures reactor antineutrino disappearance $\bar{\nu}_e \rightarrow \bar{\nu}_e$ via effective

$$\Delta m_{ee}^2 = \cos^2 \theta_{12} \Delta m_{31}^2 + \sin^2 \theta_{12} \Delta m_{32}^2$$

- Accelerator/atmospheric experiments measure $\nu_\mu \rightarrow \nu_\mu$ disappearance:

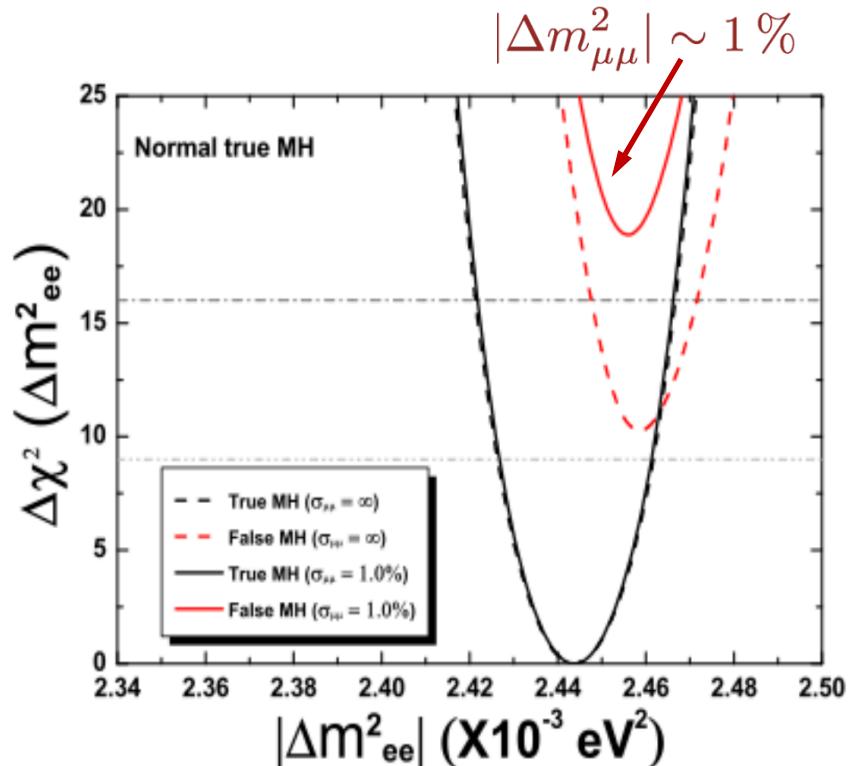
$$\begin{aligned}\Delta m_{\mu\mu}^2 \simeq & \sin^2 \theta_{12} \Delta m_{31}^2 + \cos^2 \theta_{12} \Delta m_{32}^2 \\ & + \sin 2\theta_{12} \sin \theta_{13} \tan \theta_{23} \cos \delta \Delta m_{21}^2\end{aligned}$$

□ NOvA/T2K → $|\Delta m_{\mu\mu}^2| \sim 1\%$

- **effective Δm^2 values** can be linked via

$$|\Delta m_{ee}^2| - |\Delta m_{\mu\mu}^2| = \pm \Delta m_{21}^2 (\cos 2\theta_{12} - \sin 2\theta_{12} \sin \theta_{13} \tan \theta_{23} \cos \delta)$$

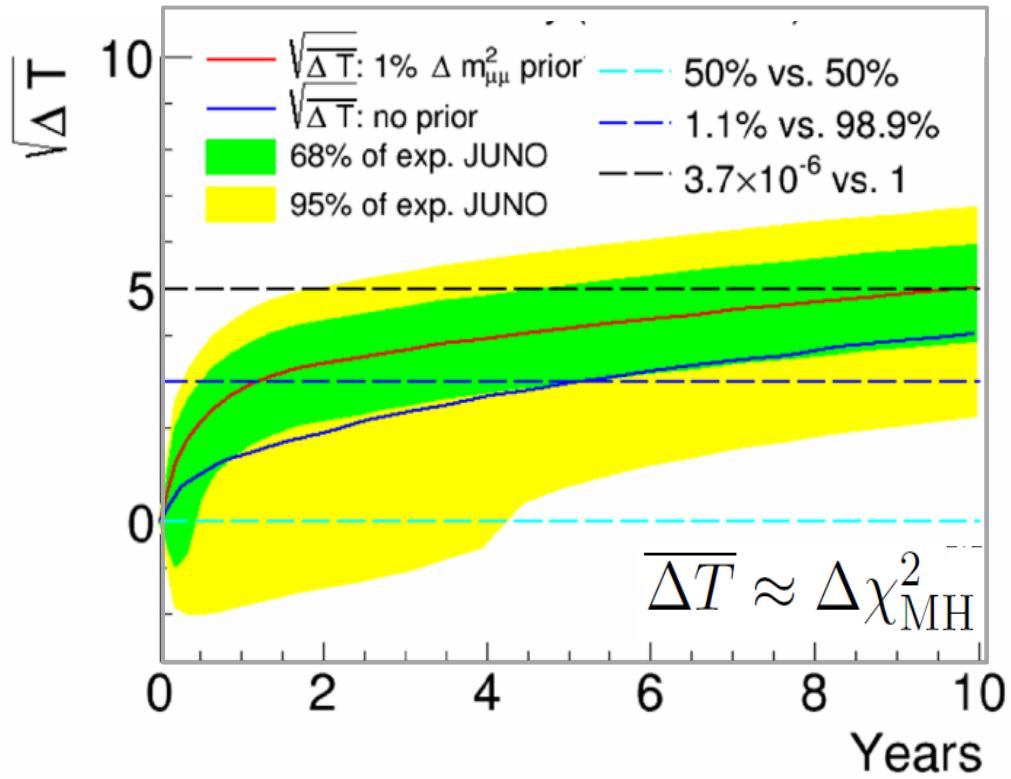
→ **inclusion of accurate measurement of $|\Delta m_{\mu\mu}^2|$ as prior in the analysis**



Sensitivity to mass ordering ³

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JUNO, arXiv:1507.05613



- JUNO's expected sensitivity level**
(assuming 3% energy resolution)
- JUNO alone based on 6 years: $\sim 3\sigma$
 - + precise data by T2K/NOvA on $\Delta m^2_{\mu\mu}$: 4σ

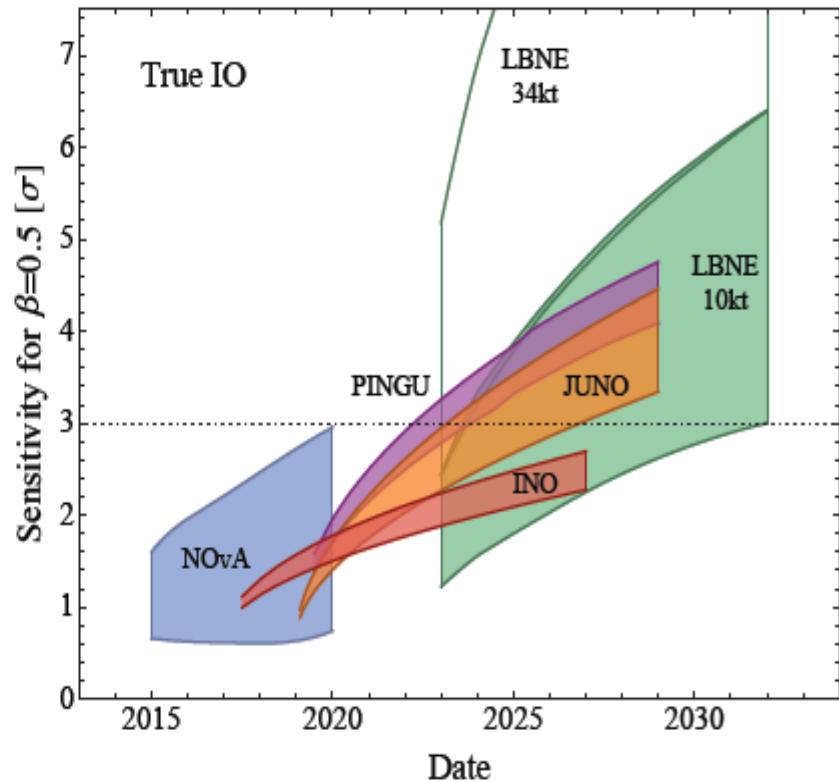
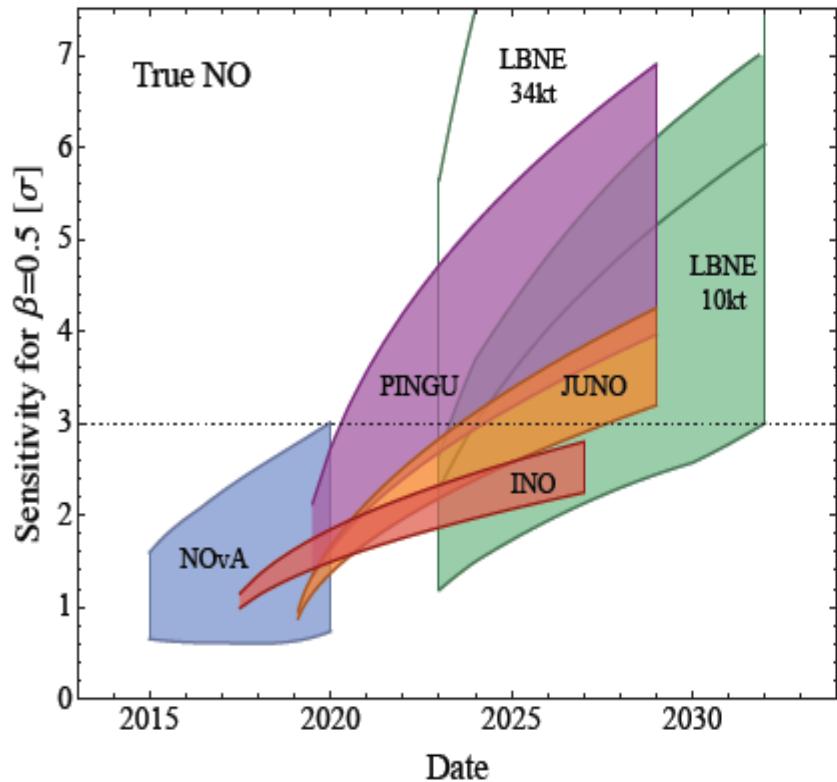
defining factors:

- E resolution: 3% at 1MeV
- statistics: 100,000 ev

Sensitivity budget	$\Delta\chi^2$
Statistics only	+16
different core distances	-3
reactor background	-1.7
spectral shape	-1
S/B ratio (rate)	-0.6
S/B ratio (shape)	-0.1
information on $\Delta m^2_{\mu\mu}$	+8

Global effort on Mass Ordering

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different techniques

- reactor neutrinos: JUNO
- atmospheric v's: INO, PINGU, ORCA
- long-baseline beam: LBNE → DUNE

mode

$$\nu_e \rightarrow \nu_e$$

$$\nu_\mu \rightarrow \nu_\mu$$

$$\nu_\mu \rightarrow \nu_e$$

main uncertainties

energy res. (3-3.5%)

value of $\theta_{23} = 40-50^\circ$

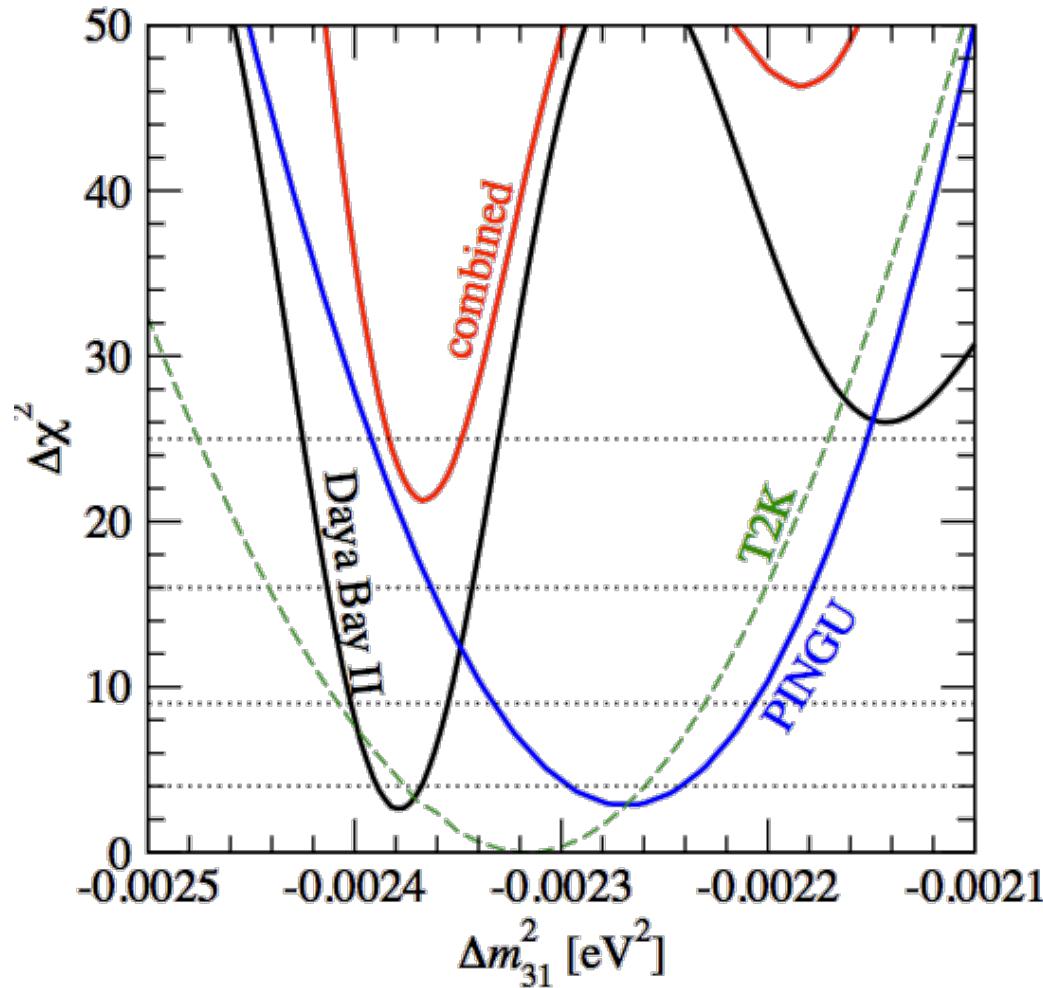
value of δ_{CP}

JUNO + future atmospheric ν results

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Blennow, Schwetz, arXiv:1306.3988

example assuming **very poor Δm^2 measurements**



Conclusions

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JUNO will offer a rich physics program!

→ *Yellow Book, arXiv:1507.05613*

■ Reactor neutrino oscillations

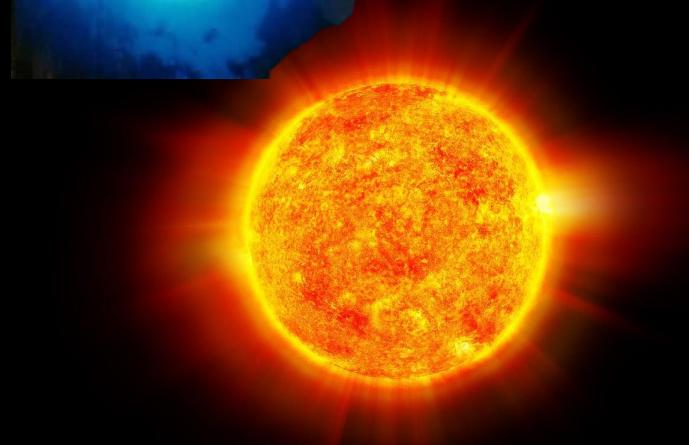
- mass ordering: $3\sigma \rightarrow 4\sigma$ (with input on $\Delta m^2_{\mu\mu}$)
- sub-% measurement of osc. parameters

■ Neutrinos from natural sources

- Galactic Supernova neutrinos
- Diffuse Supernova Neutrino Background
- Solar neutrinos
- Geoneutrinos
- Neutrinos from dark matter annihilation
- Atmospheric neutrinos

■ Short-baseline oscillations (sterile v's)

■ Proton decay into $K^+\bar{\nu}$



553 collaborators from 72 institutions



Armenia, Belgium, Brazil, Chile, China, Czech Republic, Germany, Finland, France, Italy, Latvia, Pakistan, Russia, Slovakia, Thailand, Taiwan, and the United States

German institutes

**RWTHAACHEN
UNIVERSITY**

UH
Universität Hamburg
DER FORSCHUNG | DER LEHRE | DER BILDUNG

JÜLICH
FORSCHUNGZENTRUM

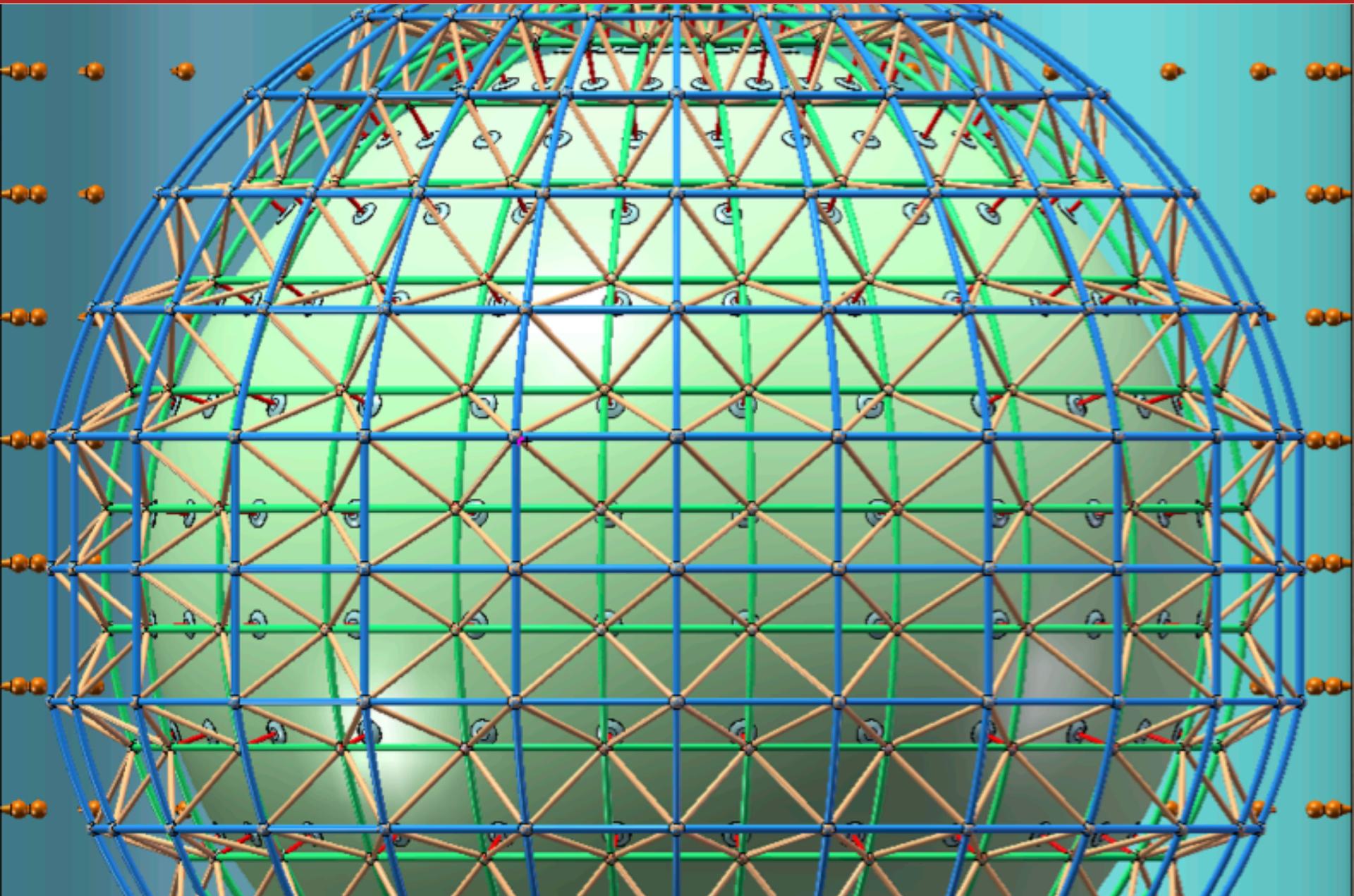
JG|U JOHANNES GUTENBERG
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TUM
Technische Universität München

EBERHARD KARLS
UNIVERSITÄT
TÜBINGEN



Backup slides



Matter effects, mass hierarchy, CP violation

Oscillation probability for ν_e appearance

in a ν_μ neutrino beam:

$$\begin{aligned}
 & \text{atmospheric oscillations} \rightarrow T2K \\
 P_{\mu e(\bar{\mu} \bar{e})} = & \sin^2 \theta_{23} \sin^2 2\theta_{13} \left(\frac{\Delta_{13}}{B_\pm} \right)^2 \sin^2 \left(\frac{B_\pm L}{2} \right) \\
 & \text{solar oscillations} \\
 + & \cos^2 \theta_{23} \sin^2 2\theta_{12} \left(\frac{\Delta_{12}}{A} \right)^2 \sin^2 \left(\frac{AL}{2} \right) \approx 0 \\
 + & J \frac{\Delta_{12}}{A} \frac{\Delta_{13}}{B_\pm} \sin \left(\frac{AL}{2} \right) \sin \left(\frac{B_\pm L}{2} \right) \cos \left(\mp \delta - \frac{\Delta_{13} L}{2} \right) \\
 & \text{neutrino-antineutrino asymmetry term}
 \end{aligned}$$

effects of weak matter potential

leptonic CP violation

$$J = \cos \theta_{13} \sin 2\theta_{12} \sin 2\theta_{13} \sin 2\theta_{23}$$

weak matter potential A

$$\Delta_{ij} = \frac{\Delta m_{ij}^2}{2E_\nu}$$

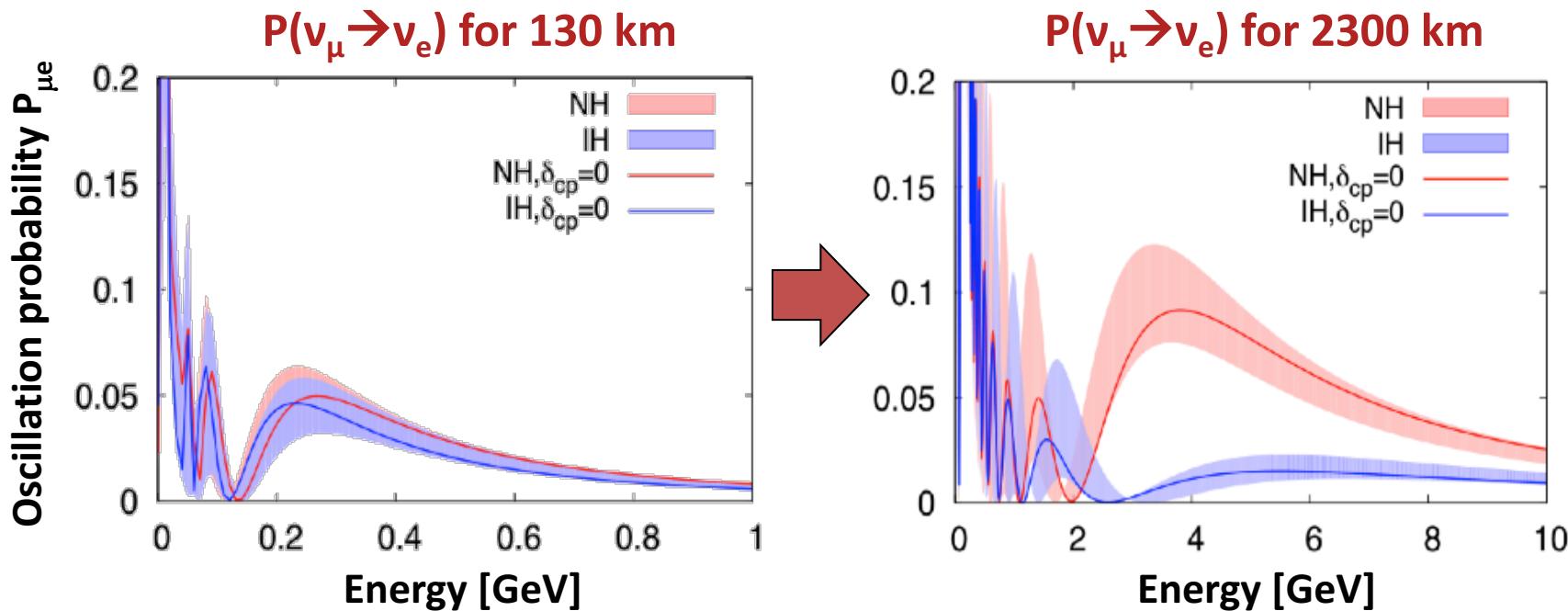
$$B_\pm = |A \pm \Delta_{13}|$$

$$A = \sqrt{2}G_F N_e$$

$\longrightarrow \nu \leftrightarrow \bar{\nu}$ asymmetry if $A \sim \Delta_{13}$!

Oscillation patterns for long-baseline beam JGU

- Oscillation probabilities differ for $\nu_\mu \rightarrow \nu_e$ vs. $\bar{\nu}_\mu \rightarrow \bar{\nu}_e$
- Enhanced electron-flavor appearance for:
neutrinos \rightarrow normal hierarchy
antineutrinos \rightarrow inverted



- Far detector at first atmospheric oscillation maximum:
longer baseline \rightarrow larger energy \rightarrow larger matter effect!

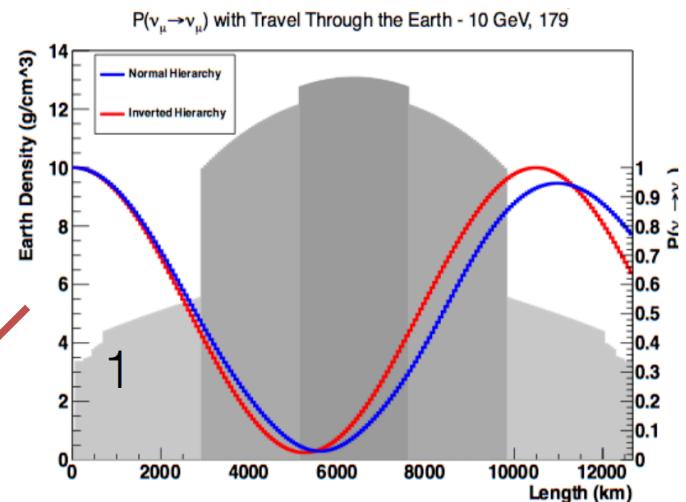
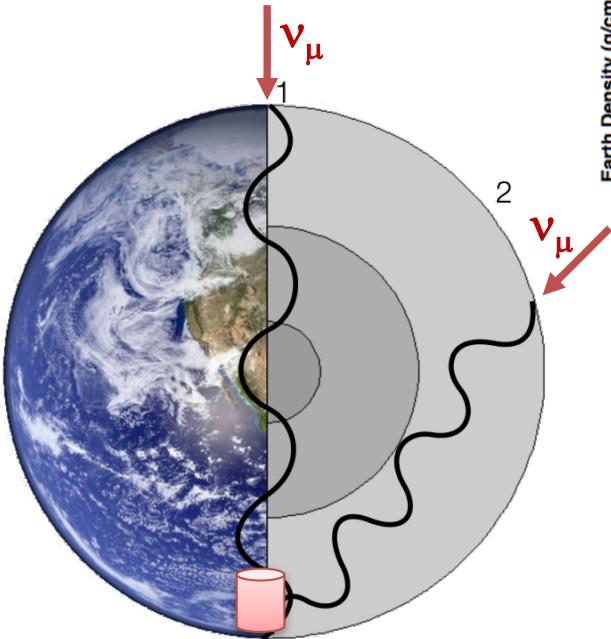
MH from atmospheric neutrinos

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D. Grant

Source: Atmospheric μ -neutrinos

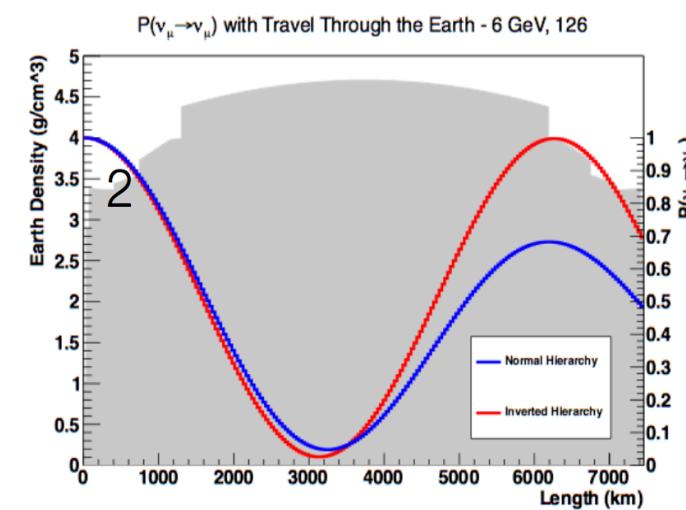
- Energies: 2-20 GeV
- Baselines: 20-13000 km
- Matter potential:
Earth core & mantle



MH signature

matter effects in

- $\nu_\mu \rightarrow \nu_\mu$ disappearance
- $\nu_\mu \rightarrow \nu_e$ appearance



Detector requirements

- relatively low energy threshold
- good angular resolution
- flavor identification
- nice to have: lepton charge ID ($\nu/\bar{\nu}$)

Atmospheric ν signal observed in PINGU

JG|U

S.Böser

Event statistics

- ν_μ : $5.0 \times 10^4 \text{ yr}^{-1}$
- ν_e : $3.8 \times 10^4 \text{ yr}^{-1}$

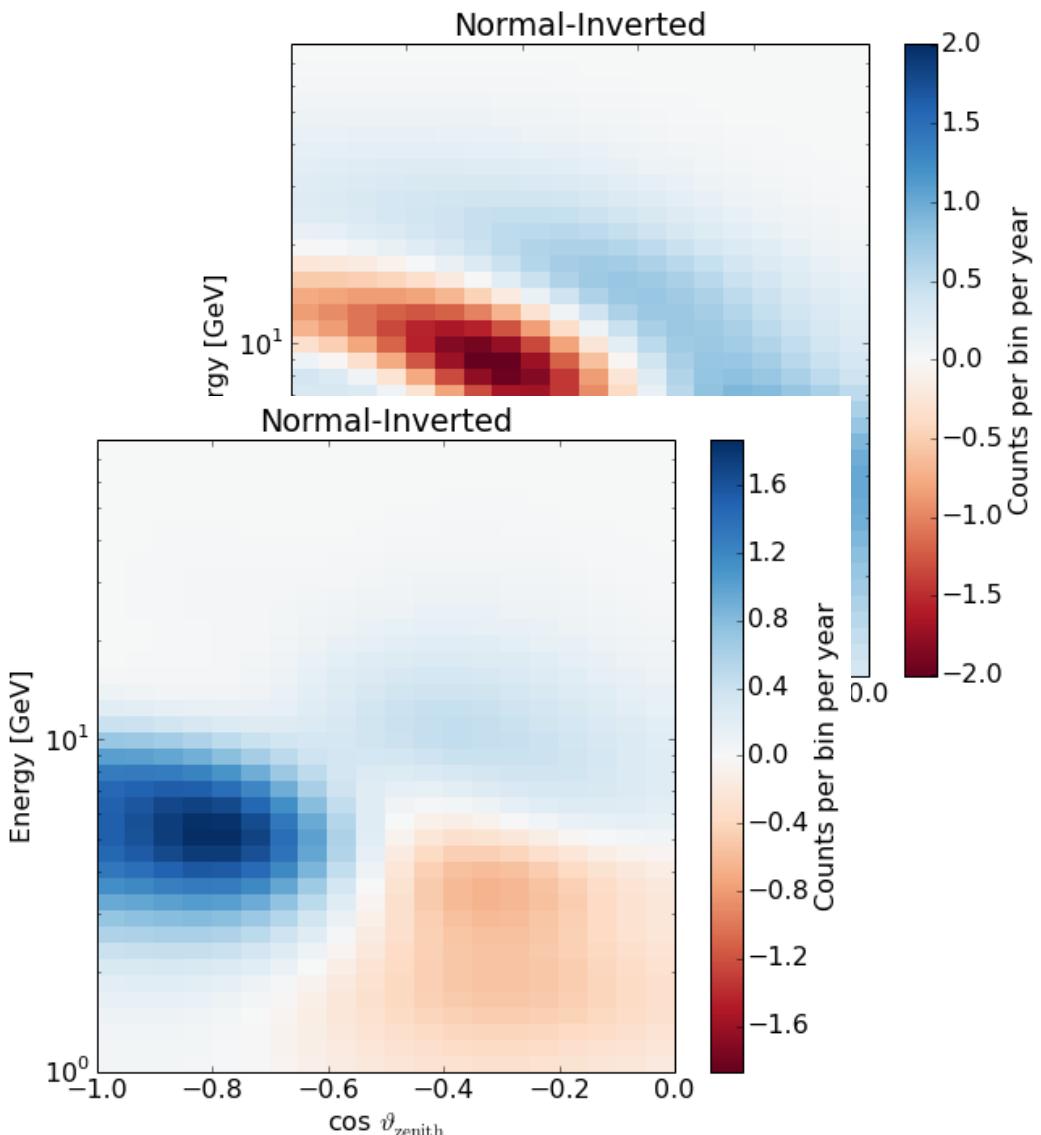
→ detectable difference

Detector resolution

- energy resolution:
~20% above 10 GeV
- directional resolution
improving with energy

Particle identification

- ν_μ (CC): tracks
 - ν_e (CC) + ν_x (NC): cascades
- distinction of event types



JUNO's liquid scintillator

JG|U

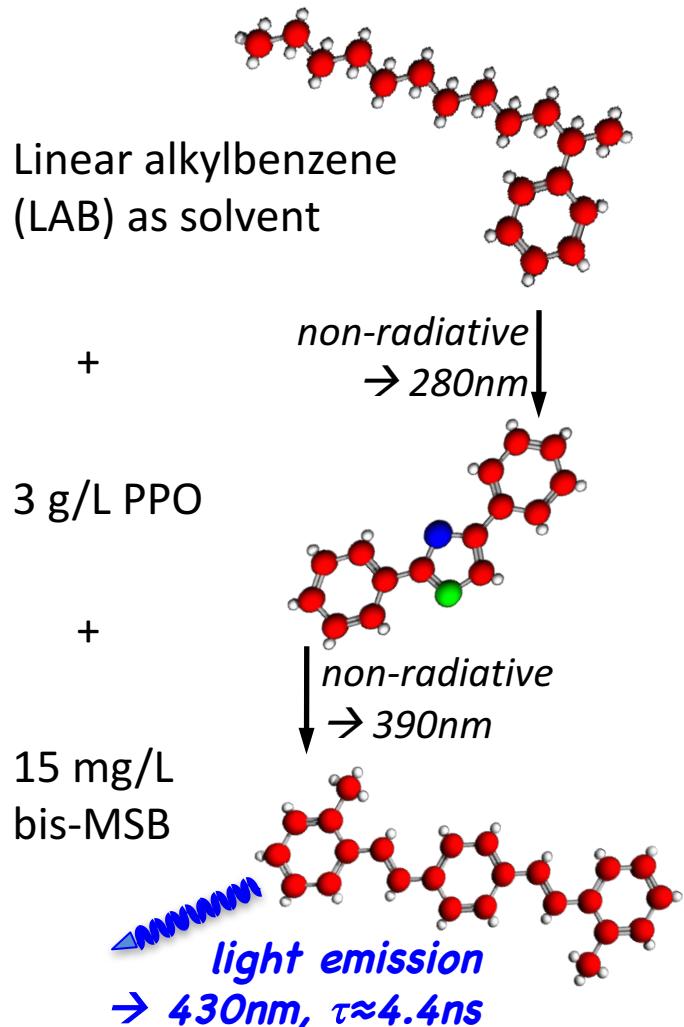
Required properties:

- Light transport over >17m
 - solvent LAB very transparent
 - no addition of gadolinium
 - Al_2O_3 column purification
- **High light yield:** >10⁴ ph/MeV
 - pure LAB, no addition of paraffins
 - large fluor (PPO) concentration
- **Radiopurity:**
 - reactor neutrinos: <10⁻¹⁵ g/g in U/Th
 - solar neutrinos: <10⁻¹⁷ g/g
 - vacuum distillation

for free:

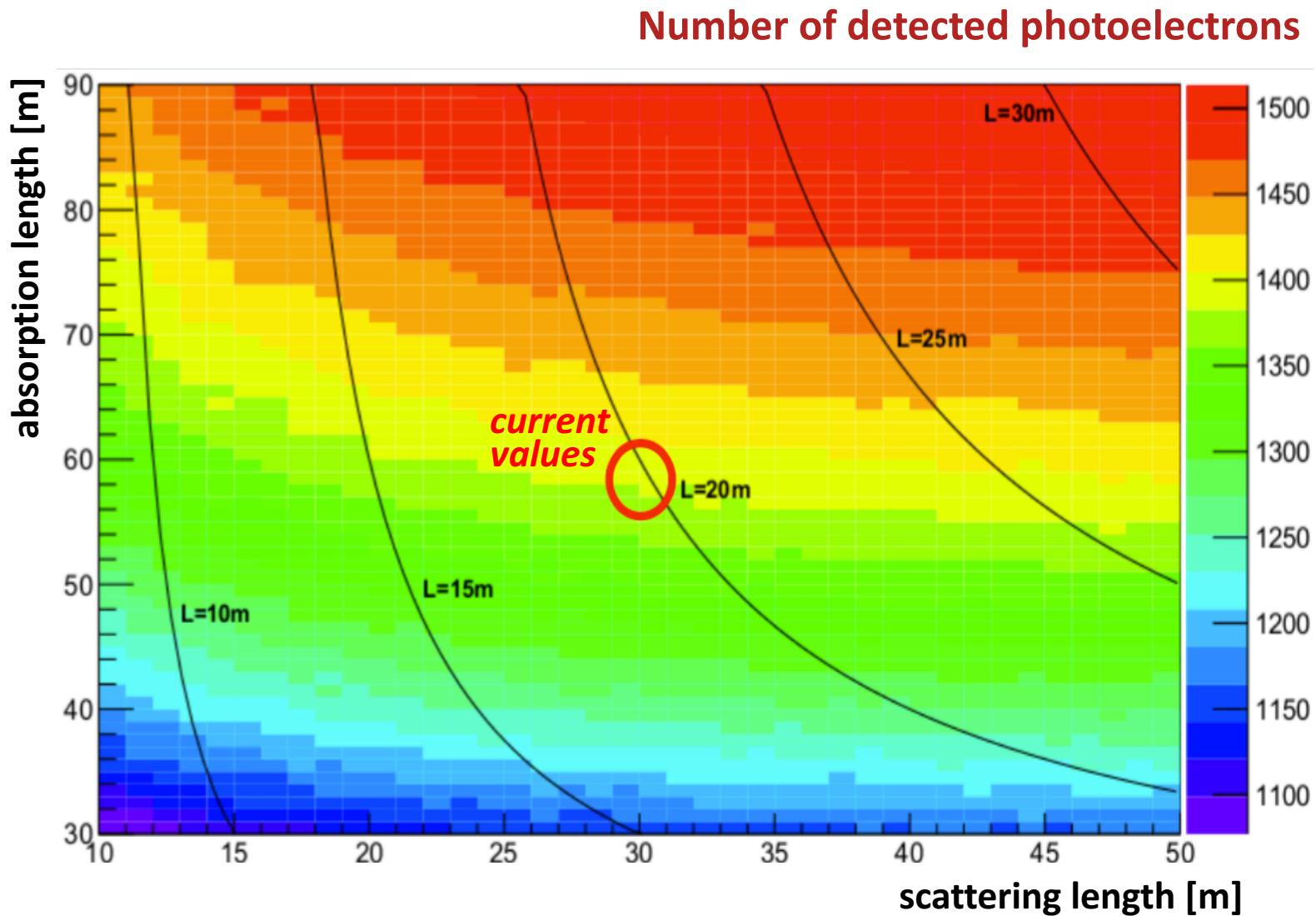
- Fast fluorescence times
 - **good spatial resolution**
- **Good pulse shaping** properties
 - background discrimination, e.g. e^+/e^-

LENA-style liquid scintillator



p.e. yield vs. scintillator transparency

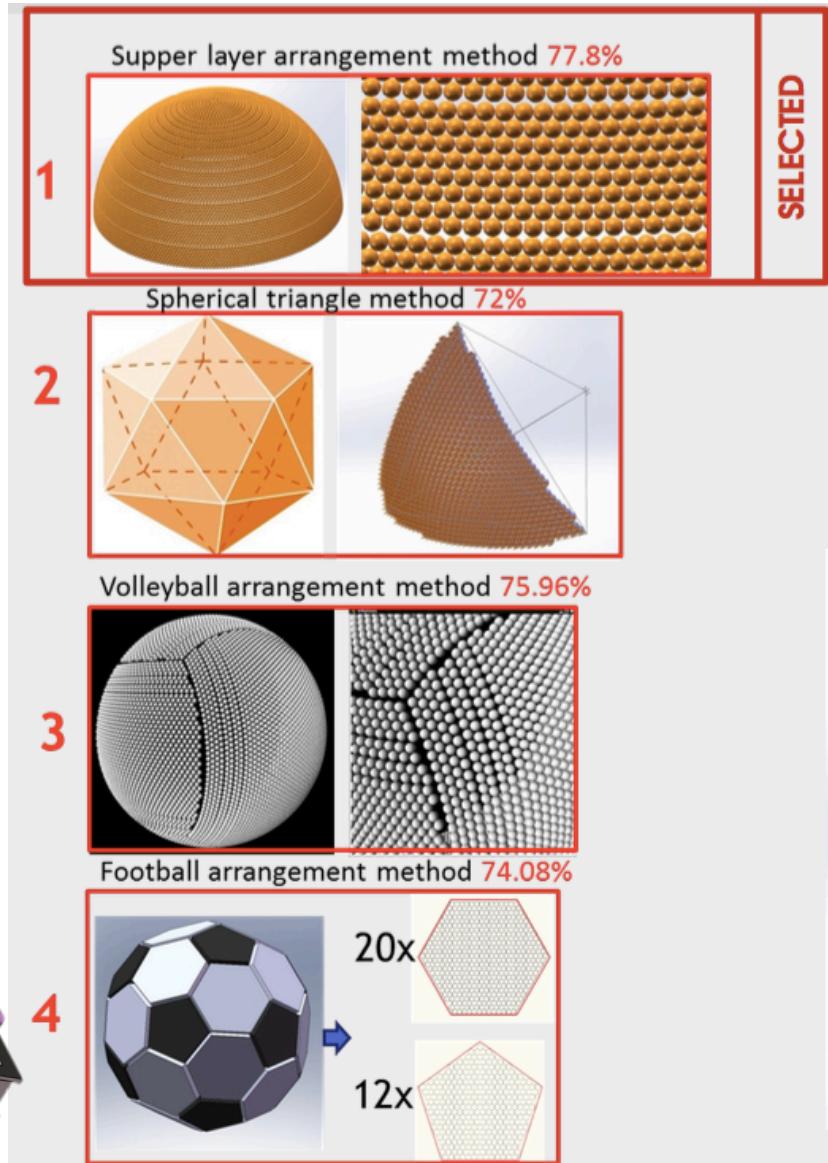
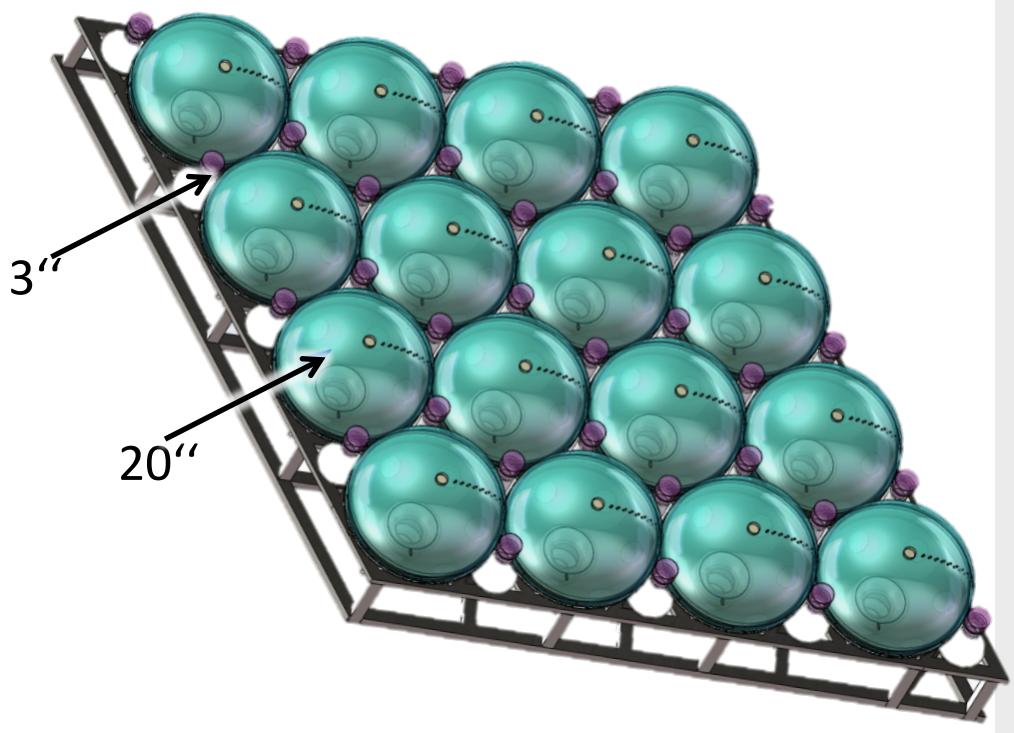
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Light detection

Light collection required:

- optical coverage: 75%
 - 17,000 large PMTs (20'')
 - additional small PMTs (3'')



Light detection

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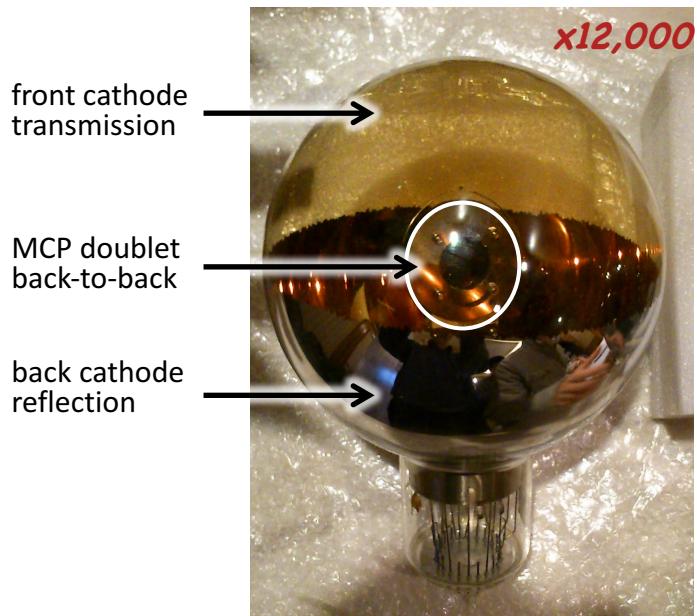
Light collection required:

- optical coverage: 75%
 - quantum efficiency QE x collection efficiency CE = 35%
- photons detected: ~26%



Hamamatsu R12860 (20" PMT)

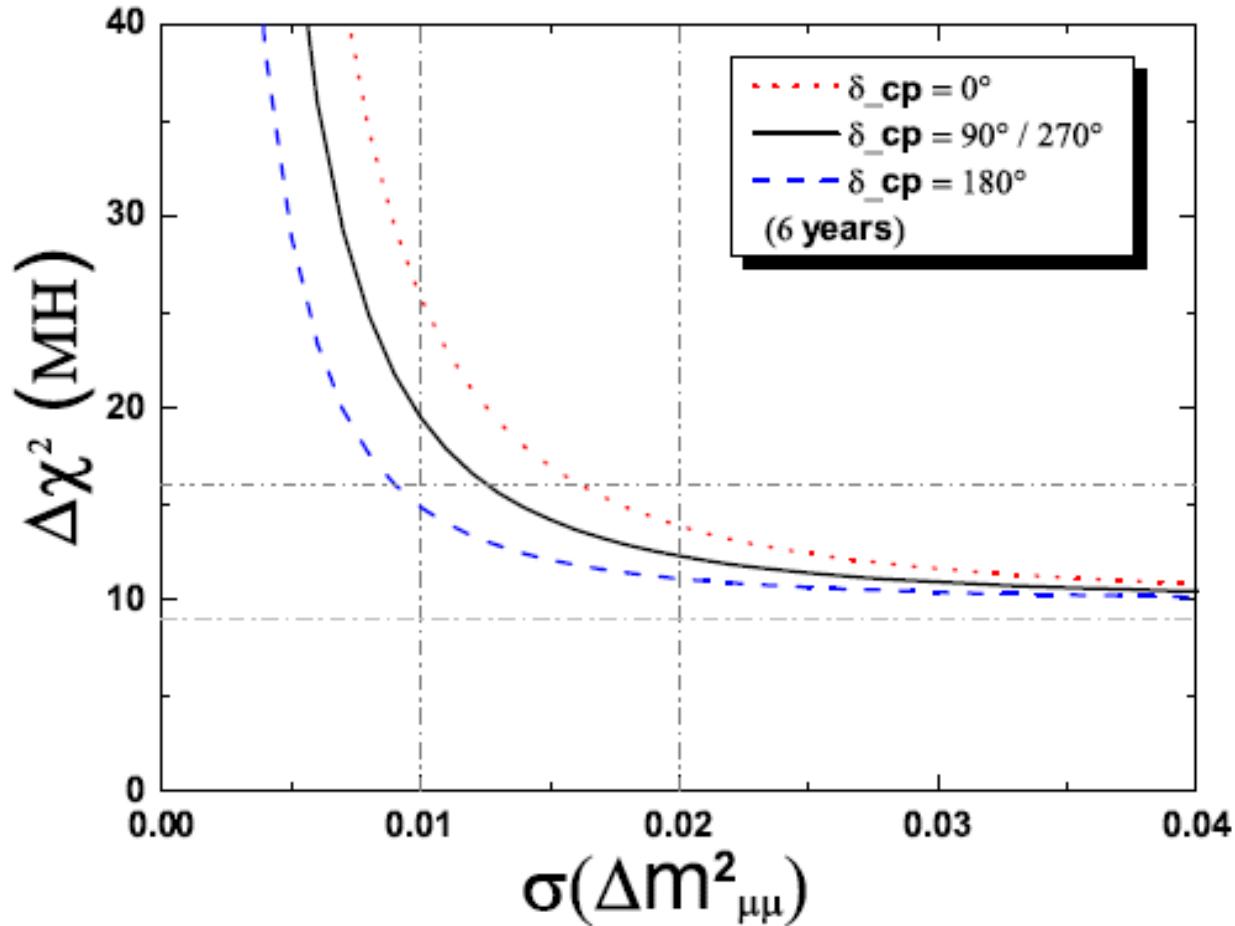
Parameter	Hamamatsu 20"	new MCP-PMT
Photocathode	transmission	transmission + reflection
QE (400nm)	30%(T)	26%(T) + 4%(R)
relative CE	100%	110%
peak-to-valley ratio	>3	>3
transit time spread	~3ns	~12ns
dark rate	~30kHz	~30kHz
afterpulsing	10%	3%



MCP-PMT 8" prototype

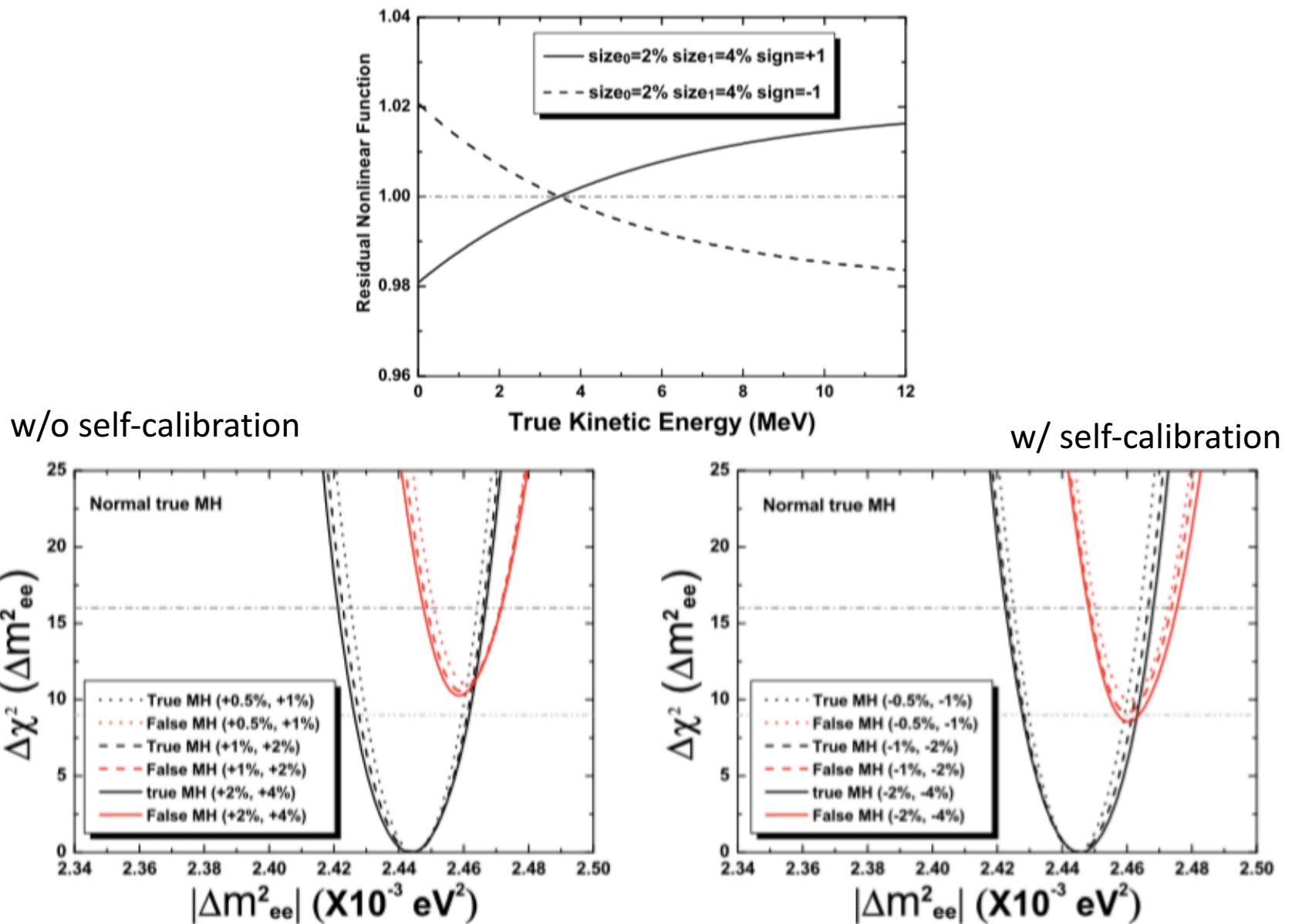
Influence of $\Delta m^2_{\mu\mu}$ accuracy

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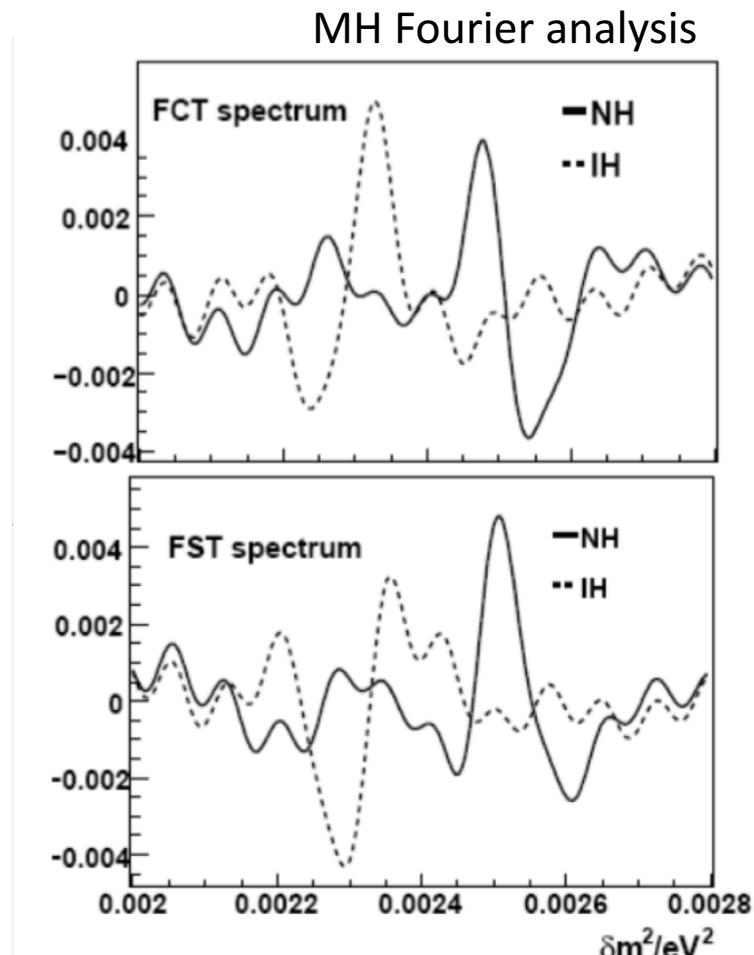
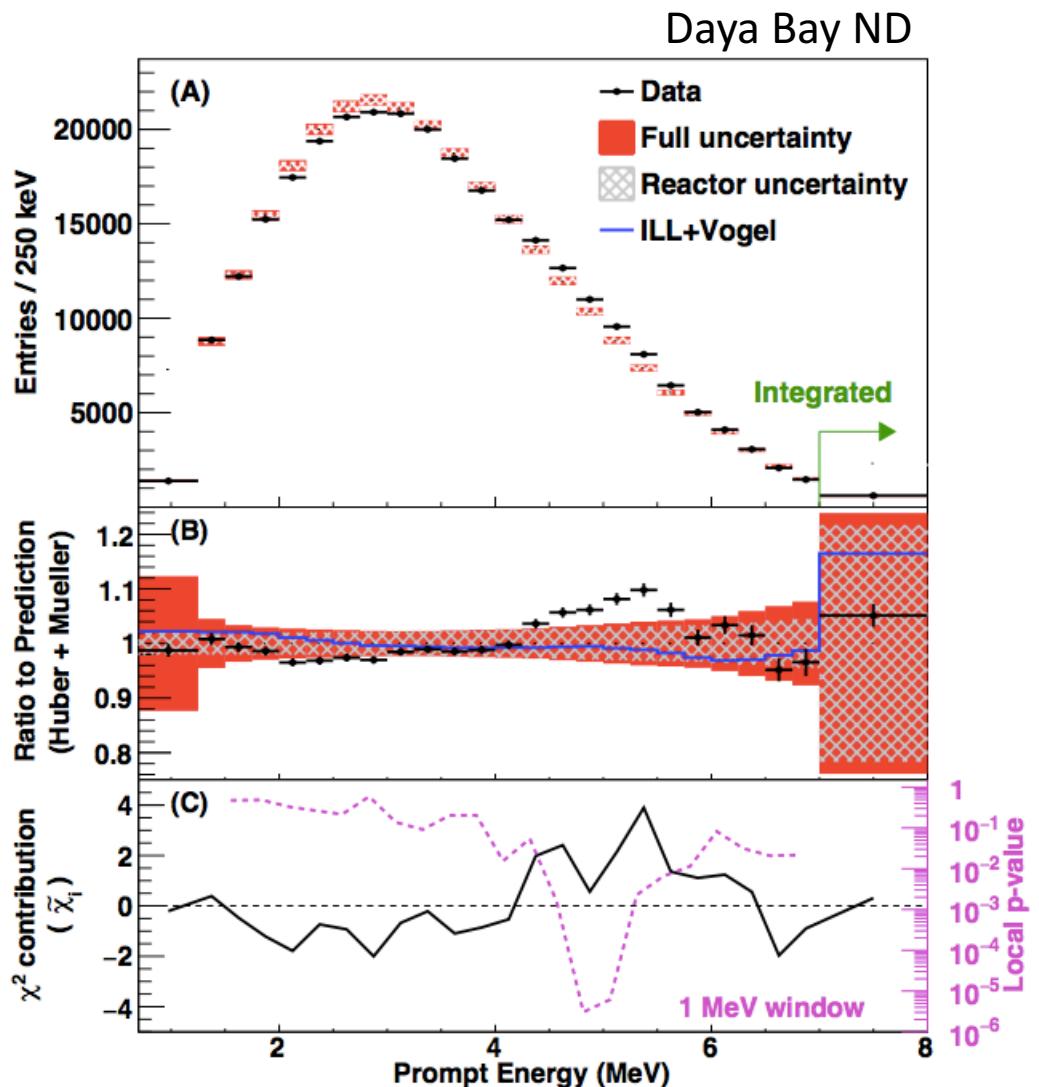
Influence of energy scale linearity

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Reactor anomaly: 5 MeV bump

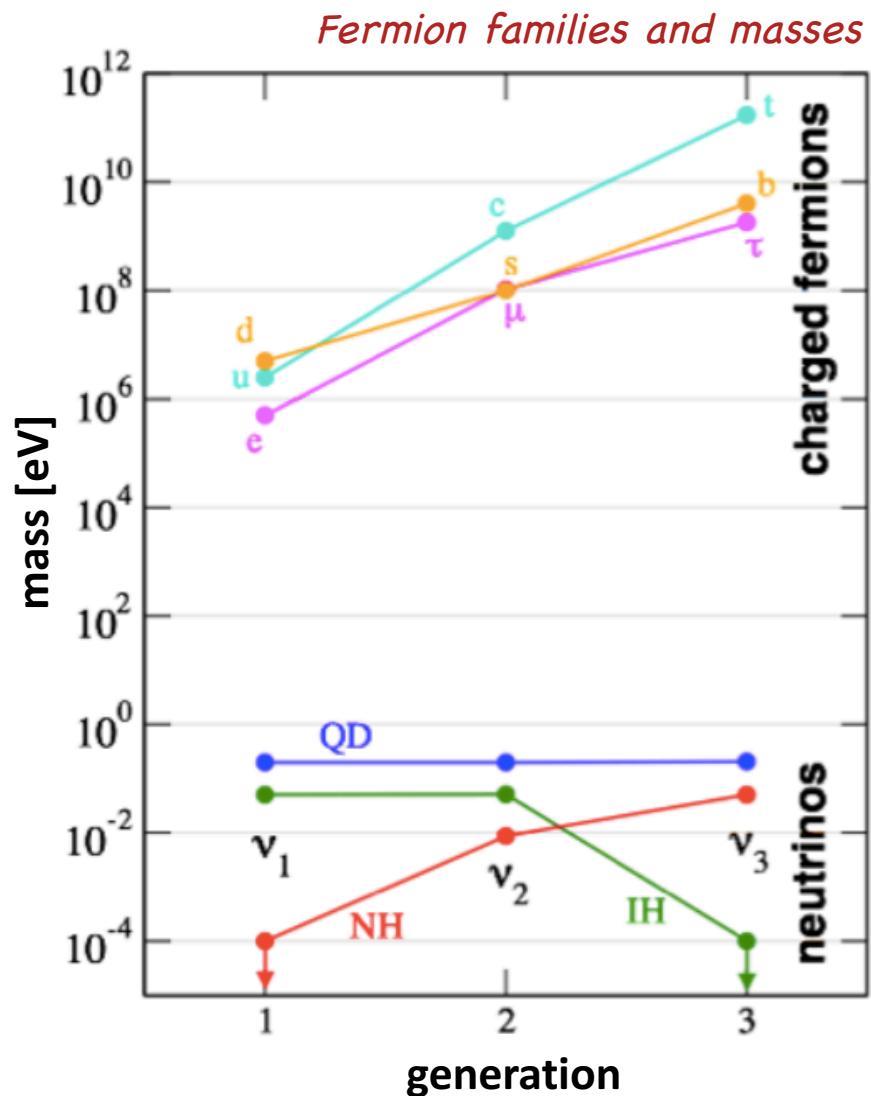
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J. Learned et. al. Hep-ex/0612022

Implications of $\text{sgn}(\Delta m^2_{32})$

- Arrangement of the neutrino masses
 - normal ordering: $m_1 < m_2 < m_3$
 - inverted ordering: $m_3 < m_1 < m_2$
 - quasi-degenerate: $m_1 \approx m_2 \approx m_3$
- resolving the **degeneracy** in the interpretation of δ_{CP} measurements
- target range for **sensitivity** of **$0\nu\beta\beta$ decay** experiments
- combination with **cosmology** to resolve **neutrino masses**

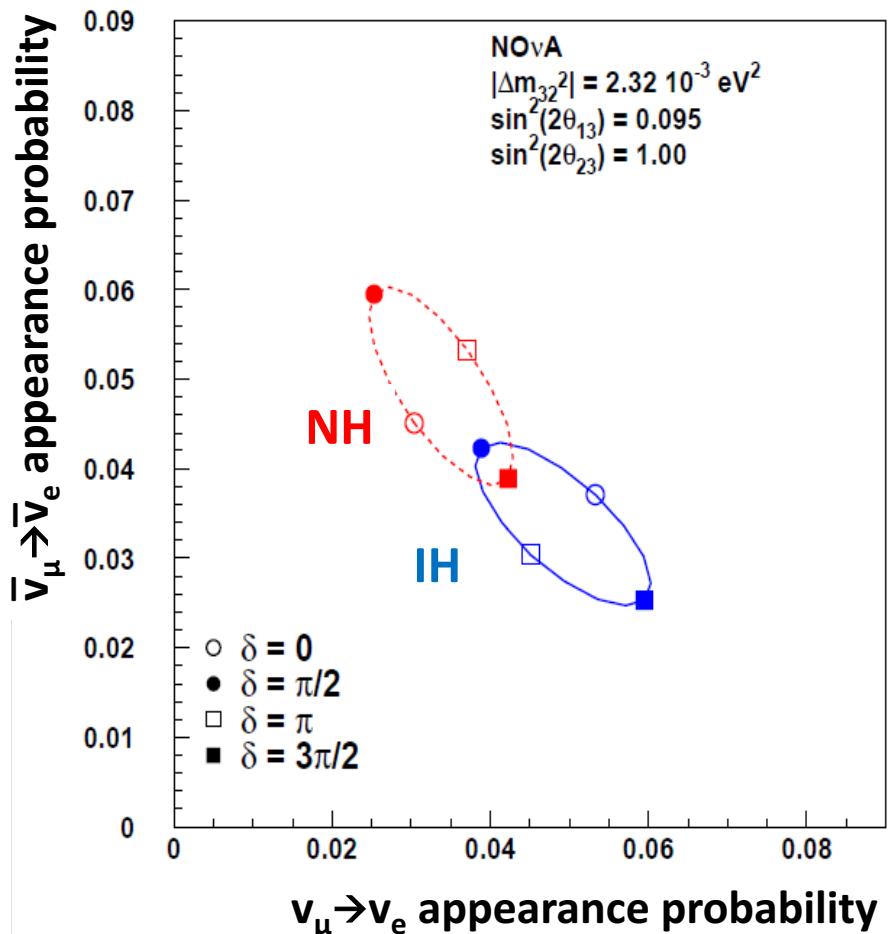


Implications of $\text{sgn}(\Delta m_{32}^2)$

JG|U

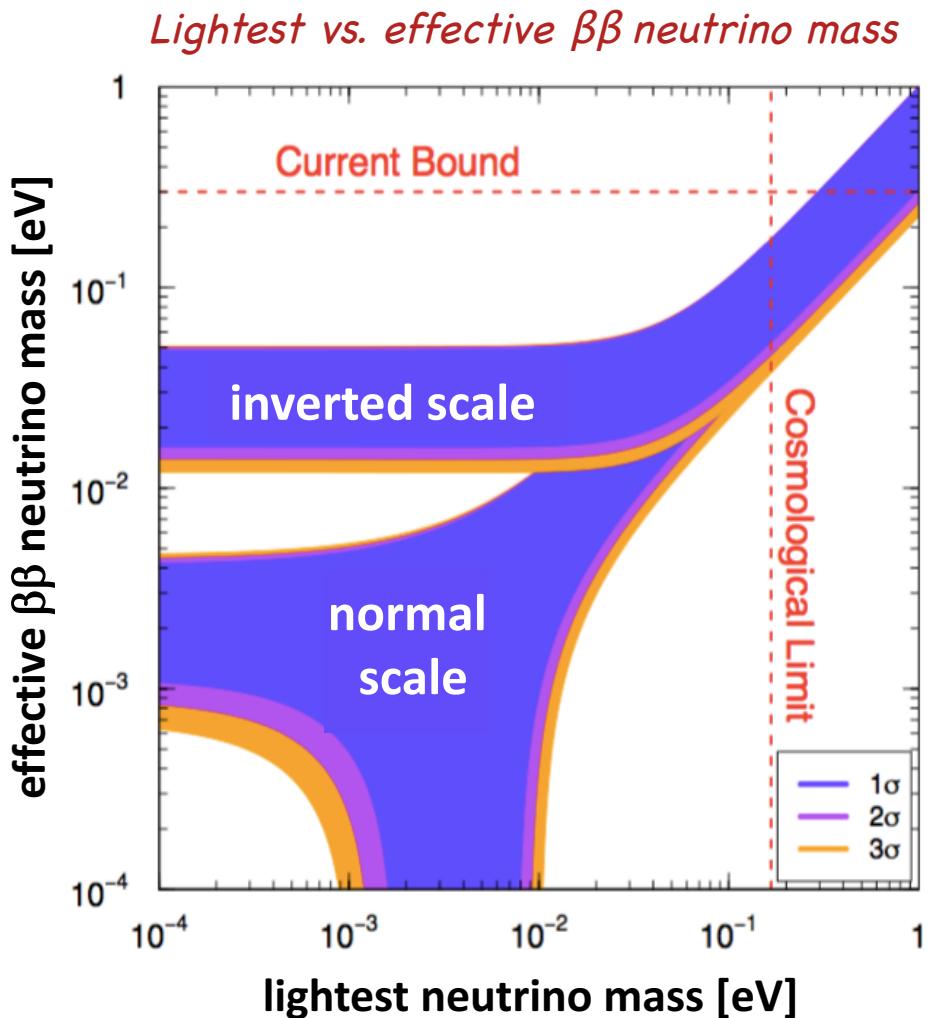
- Arrangement of the neutrino masses
 - normal ordering: $m_1 < m_2 < m_3$
 - inverted ordering: $m_3 < m_1 < m_2$
 - quasi-degenerate: $m_1 \approx m_2 \approx m_3$
- resolving the **degeneracy in the interpretation of δ_{CP} measurements**
- target range for **sensitivity of $0\nu\beta\beta$ decay experiments**
- combination with **cosmology** to resolve **neutrino masses**

NOvA: degeneracy of MH and δ_{CP}



Implications of $\text{sgn}(\Delta m^2_{32})$

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 - normal ordering: $m_1 < m_2 < m_3$
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Implications of $\text{sgn}(\Delta m^2_{32})$

JG|U

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 - normal ordering: $m_1 < m_2 < m_3$
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