

Nonthermal cosmic neutrino background



Michael Ratz



based on Phys.Rev. D92 (2015) no.12, 123006 (arXiv:1509.00481)
with: Mu-Chun Chen (UCI) and Andreas Trautner (Bonn)

(some slides stolen from Andreas' talks)

&

Kevork Abazajian, Mu-Chun Chen & M.R. (in preparation)

Erice
Italy

September 19 2017

Neutrinos vs. photons

☞ there is plenty of evidence for photons coming from the sun



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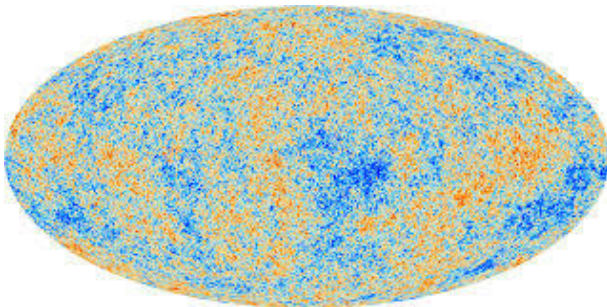
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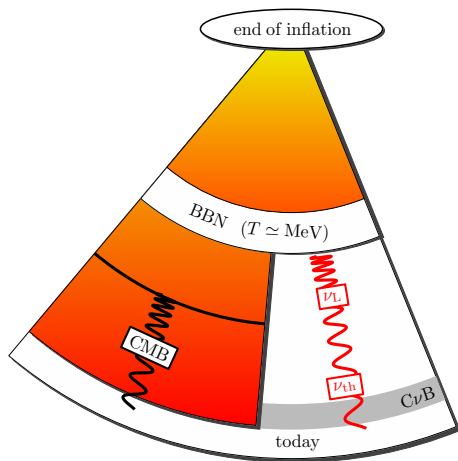
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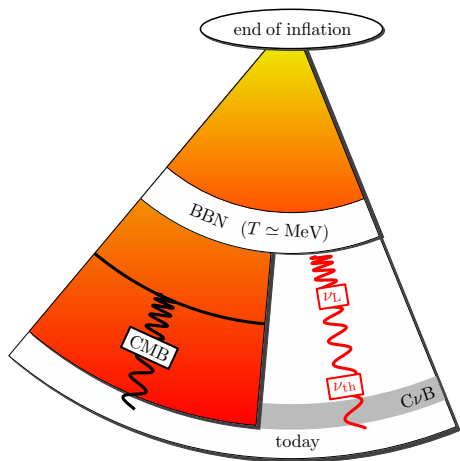
main message of this talk:

there might be more neutrinos than photons!

Standard picture

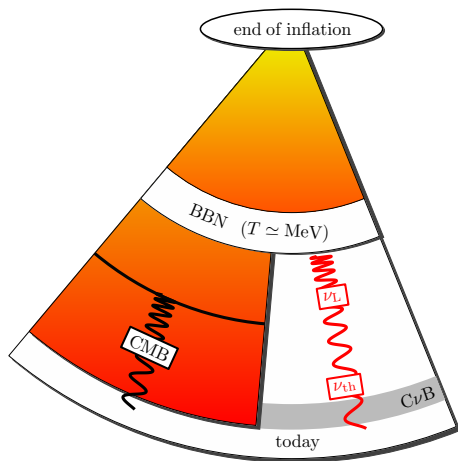


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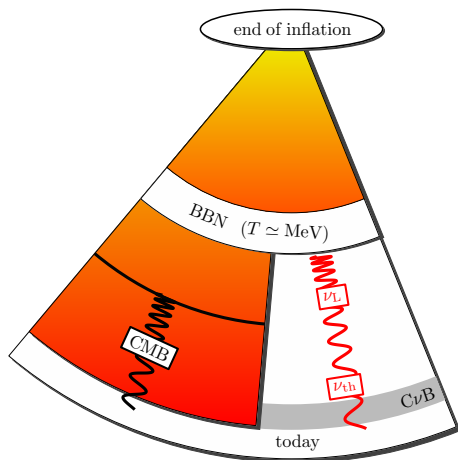
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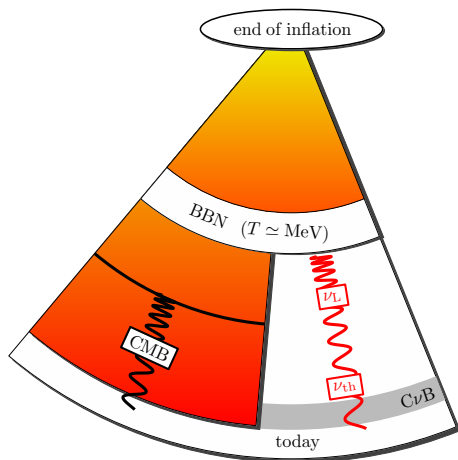
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 - $n_{\nu_{\text{th}}} \sim 336 \text{ cm}^{-3}$ Ade et al. (2016)
- $N_{\text{eff}} = 3.2 \pm 0.5$ cf. talk by M. Archidiacono

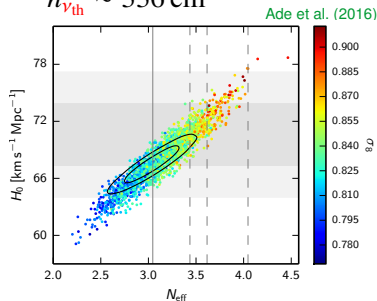
indirect evidence: $N_{\text{eff}}^{(3\nu, \text{theory})} = 3.046$

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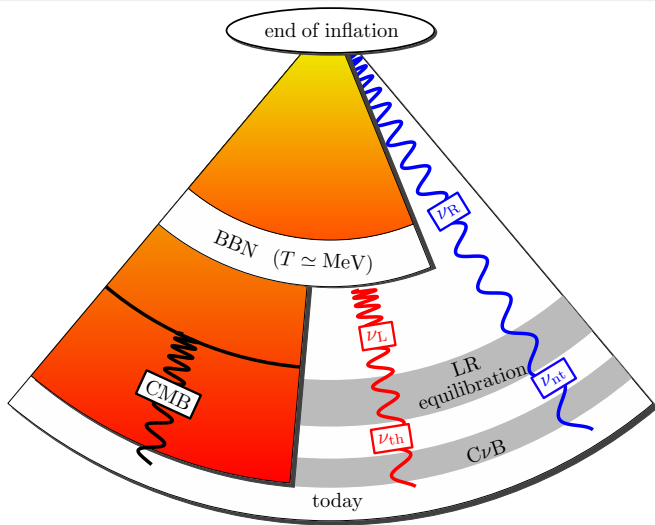


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Standard picture + nonthermal Dirac neutrinos



Dirac neutrinos in the early universe

☞ **Dirac** neutrinos get their mass from the Yukawa coupling

$$\mathcal{L}_\nu = Y_\nu^{ij} \begin{pmatrix} \bar{e}_L^i \\ \bar{\nu}_L^i \end{pmatrix} \cdot \tilde{H} \nu_R^j + \text{h.c.}$$

☞ $m_\nu \lesssim 0.1 \text{ eV} \curvearrowright$ singular values of $Y_\nu \lesssim 10^{-12}$

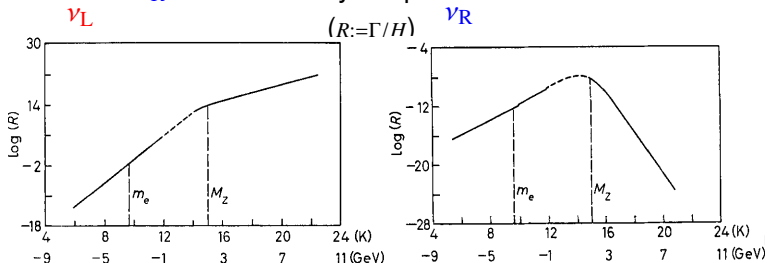
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☞ standard C ν B initially consists *only* of **left-chiral neutrinos ν_L** while ν_R are too weakly coupled

Antonelli, Fargion, and Konoplich (1981)



Nonthermal neutrino background

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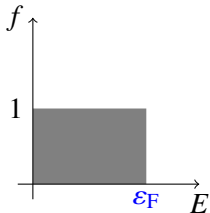
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☞ most extreme possibility: degenerate Fermi gas
fill ν_R states from the bottom up



ultrarelativistic approximation

$$n_{\nu_R} = \frac{g}{6\pi^2} \epsilon_F^3$$

$$\rho_{\nu_R} = \frac{g}{8\pi^2} \epsilon_F^4$$

$g = 2$ for spin-1/2 fermion

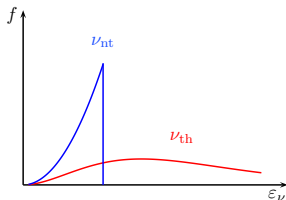
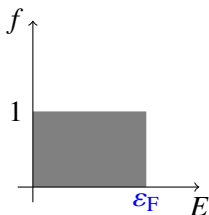
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Evolution of the nonthermal background

$$n_{\nu_R}(T) = n_{\nu_R}(T_{RH}) \cdot \left(\frac{a(T_{RH})}{a(T)} \right)^3$$

scale factor



Evolution of the nonthermal background

$$n_{\nu_R}(T) = \frac{g \xi^3}{6\pi^2} \frac{g_{*S}(T)}{g_{*S}(T_{RH})} T^3$$

$$\xi := \varepsilon_F / T_{RH}$$



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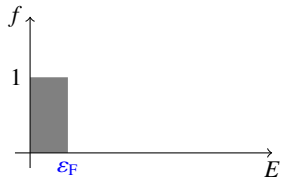


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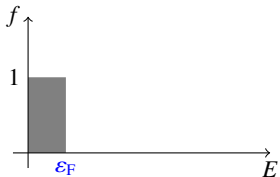
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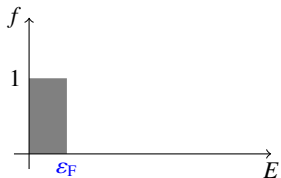
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$$\frac{n_{\nu_R}(T_\gamma)}{n_\gamma} = \frac{g \xi^3}{12 \zeta(3)} \frac{g_{*S}(T_\gamma)}{g_{*S}(T_{RH})} \quad \& \quad \Delta N_{\text{eff}}^{(\nu_R)} = \frac{8}{7} \frac{30}{8 \pi^4} \frac{g \xi^4}{2} \left(\frac{g_{*S}(T_{\text{BBN}})}{g_{*S}(T_{RH})} \right)^{4/3}$$

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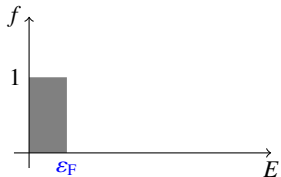
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maximal number of nonthermal neutrinos:

$$n_{\nu_R}(T_\gamma) = 0.53 n_\gamma \left(\frac{\Delta N_{\text{eff}}^{(\nu_R)}}{0.7} \right)^{3/4} \lesssim 217 \text{ cm}^{-3}$$

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Planck: $\Delta N_{\text{eff}} = 0.2 \pm 0.5$

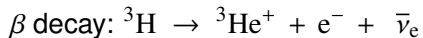
How to look for relic neutrinos



Direct detection of CνB on earth

👉 proposal: capture ν 's with tritium ${}^3\text{H}$

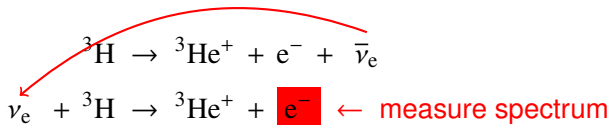
Weinberg (1962)



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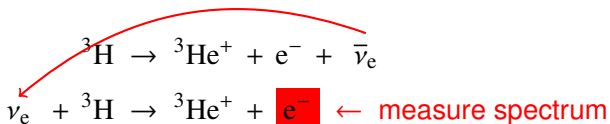
Weinberg (1962)



Direct detection of $\bar{\nu}_e$ on earth

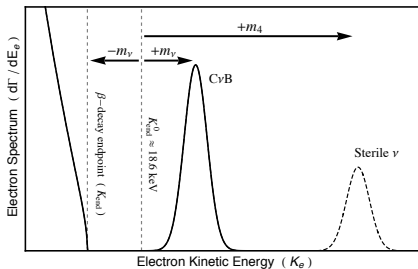
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Weinberg (1962)



- $\langle E_{\text{kin}}^{\nu_{\text{th}}} \rangle_{\text{today}} \approx 1.7 \cdot 10^{-4} \text{ eV}$
- $\Delta m_{12}^2 \approx 7.5 \cdot 10^{-5} \text{ eV}^2$
- $\Delta m_{13}^2 \approx 2.5 \cdot 10^{-3} \text{ eV}^2$

↪ at least two species are nonrelativistic!



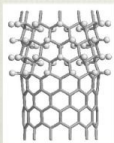
Long, Lunardini, and Sabancilar (2014)

Experimental proposal

PTOLEMY (Princeton Tritium Observatory for Light, Early-Universe, Massive-Neutrino Yield)

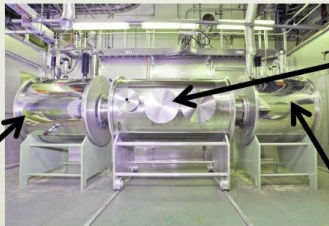
cf. talk by C. Tully

C. Tully et. al. (2013)



tritium
source

1 g prototype – next 2 yr,
100 g target – 3 yr?



MAC-E filter
(reject $E < 50\text{-}150$ eV
below endpoint)

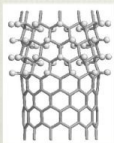
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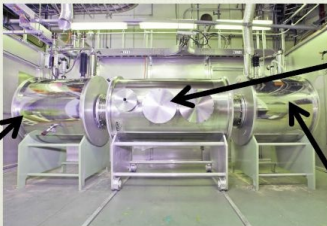
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☞ expected rate: 8–23 events per 100 g tritium and year for Majorana neutrinos

de Salas, Gariazzo, Lesgourgues, and Pastor (2017)

depends on DM halo & absolute ν mass

Dirac vs. Majorana

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Long, Lunardini, and Sabancilar (2014)
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$$\Gamma_{\text{C}\nu\text{B}}^{\text{Majorana}} = 2 \cdot \Gamma_{\text{C}\nu\text{B}}^{\text{Dirac}} \approx \frac{8 - 23}{\text{yr}^{-1} \cdot 100 \text{ g}}$$

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☞ local ν density higher than average

Ringwald and Wong (2004) ; de Salas, Gariazzo, Lesgourgues, and Pastor (2017)

$$\text{e.g. } \Gamma_{\nu B}^{\text{Majorana}} \approx 23 \text{ yr}^{-1} / 100 \text{ g} \quad \text{for } m_\nu = 150 \text{ meV}$$

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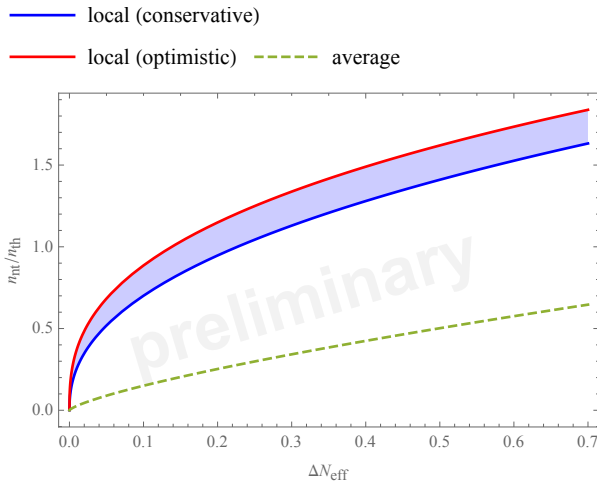
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bottom–line:

discrimination between Dirac and Majorana through measurement of relic neutrinos may be impossible

Is there an appropriate ν_R production mechanism?

👉 e.g. fermionic preheating

Greene and Kofman (1999)
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☞ large amounts of ν_R get produced during inflation and get 'cooled down' afterwards

Summary & outlook



neutrinos might be more abundant than photons!

	t_{creation}	N_{eff}	relic density
ν_{th}	$t_{\text{BBN}} \sim 1 \text{ s}$	3.046	$n_{\nu_{\text{th}}} \approx 336 \text{ cm}^{-3}$
ν_{nt}	$t_{\text{infl.}}$	$\lesssim 0.7$	$n_{\nu_{\text{nt}}} \lesssim 217 \text{ cm}^{-3}$
γ	$t \approx 3.8 \cdot 10^5 \text{ a}$	16/7	$n_{\gamma} \approx 412 \text{ cm}^{-3}$

$(n_{\nu_{\text{nt}}} \lesssim 84 \text{ cm}^{-3} \text{ for } \Delta N_{\text{eff}} = 0.2)$

Summary & outlook



neutrinos might be more abundant than photons!



nonthermal neutrinos may spoil the distinction between Dirac and Majorana

Summary & outlook



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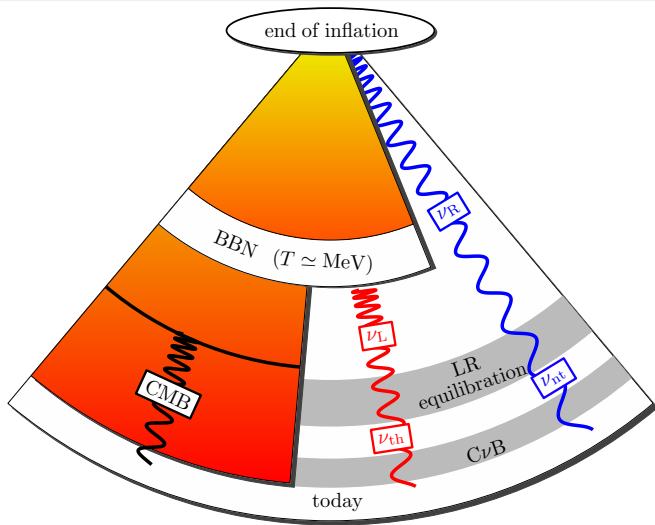


nonthermal neutrinos may spoil the distinction between Dirac and Majorana



nonthermal neutrinos directly probe the universe at the stage of inflation

Standard picture + nonthermal Dirac neutrinos



Backup slides

Fermionic preheating

👉 ingredients

Greene and Kofman (1999)
Baacke, Heitmann, and Patzold (1998)

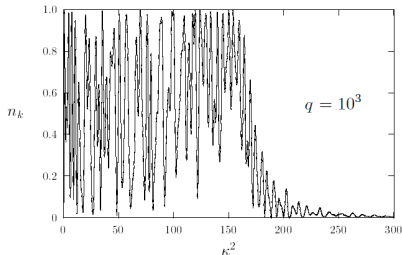
- ✓ massive scalar field ϕ such as inflaton w/ $\mathcal{V}(\phi) \sim \frac{m_\phi^2}{2}\phi^2$
- ✓ coupling to fermions $\lambda \phi \bar{\Psi}\Psi$

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- ✓ coupling to fermions $\lambda \phi \bar{\Psi}\Psi$
- ↪ (nonperturbative) “parametric resonance” effect:



occupation number of fermions in $m_\phi^2\phi^2$ -inflation
after 50 inflaton oscillations

Greene and Kofman (1999)

$$q := \lambda^2 \phi_0^2 / m_\phi^2$$

$$\varepsilon_F \sim q^{1/4} m_\phi$$

$$\frac{q^{1/4}}{2} \sim \frac{\varepsilon_F}{T_{RH}} = \xi \lesssim 3$$

▶ back

Nonthermal ν_R production mechanism

- to produce nonthermal ν_R one needs a coupling

$$\mathcal{L} \supset \lambda \phi \overline{\nu_R^c} \nu_R + \text{h.c.}$$

- Majorana mass term forbidden by e.g. \mathbb{Z}_4^L
- reheating of the SM via perturbative decay of ϕ ,
or $\phi^2 H^2$ coupling and the “scalar” parametric resonance

Witten (2001)

Kofman, Linde, and Starobinsky (1994) ; Traschen and Brandenberger (1990)

[▶ back](#)

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- 👉 annual modulation?
due to different mean velocity

Lisanti, Safdi, and Tully (2014)

$$\langle v_{\text{CvB, nt}} \rangle = 572 (1 + z) \left(\frac{0.1 \text{ eV}}{m_\nu} \right) \left(\frac{\Delta N_{\text{eff}}^{(\nu_R)}}{0.7} \right)^{1/4} \text{ km s}^{-1}$$

$$\langle v_{\text{CvB, th}} \rangle = 1580 (1 + z) \left(\frac{0.1 \text{ eV}}{m_\nu} \right) \text{ km s}^{-1}$$

redshift

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due to different mean velocity

Lisanti, Safdi, and Tully (2014)

$$\langle v_{\text{CvB, nt}} \rangle = 572 (1 + z) \left(\frac{0.1 \text{ eV}}{m_\nu} \right) \left(\frac{\Delta N_{\text{eff}}^{(\nu_R)}}{0.7} \right)^{1/4} \text{ km s}^{-1}$$

$$\langle v_{\text{CvB, th}} \rangle = 1580 (1 + z) \left(\frac{0.1 \text{ eV}}{m_\nu} \right) \text{ km s}^{-1}$$

- ➡ it would *in principle* also be possible

Huang and Zhou (2016)

Discriminate thermal from nonthermal relic neutrinos?

👉 obvious difference: spectrum?

➡ would require e^- energy resolution of $\mathcal{O}(10^{-4})$ eV

👉 annual modulation?

Lisanti, Safdi, and Tully (2014)

due to different mean velocity

$$\langle v_{\text{CMB, nt}} \rangle = 572 (1+z) \left(\frac{0.1 \text{ eV}}{m_\nu} \right) \left(\frac{\Delta N_{\text{eff}}^{(\nu_R)}}{0.7} \right)^{1/4} \text{ km s}^{-1}$$

$$\langle v_{\text{CMB, th}} \rangle = 1580 (1+z) \left(\frac{0.1 \text{ eV}}{m_\nu} \right) \text{ km s}^{-1}$$

➡ it would *in principle* also be possible

Huang and Zhou (2016)

👉 however, this would require $\mathcal{O}(10^6)$ recorded events

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