

# Nuclear Physics at the $N = Z$ Line

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ウィマー カトリン

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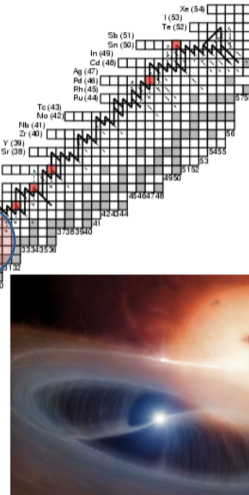
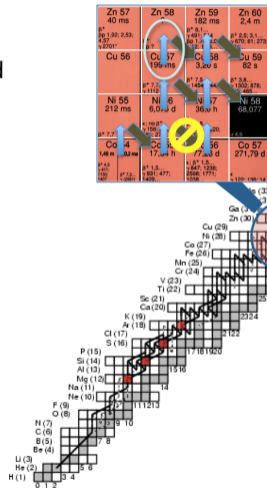
# Outline

- 1 Nucleosynthesis along the  $N = Z$  line
- 2 Isospin symmetry
- 3 Shape coexistence

# Nucleosynthesis along the $N = Z$ line

Analysis of X-ray burst light curves needs nuclear physics input

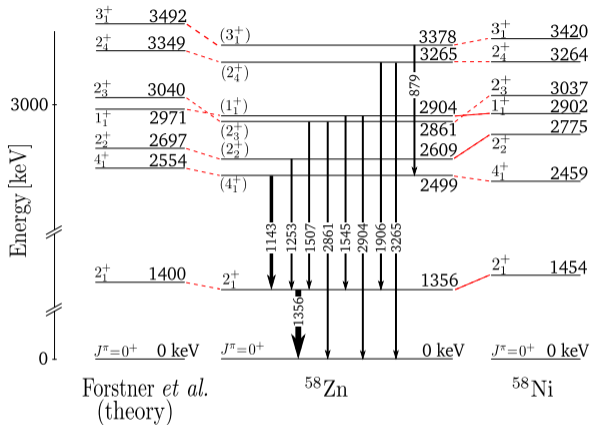
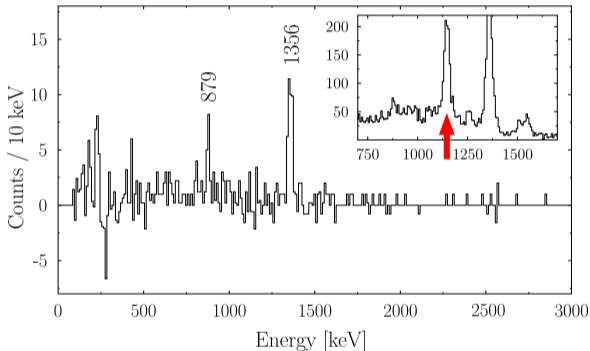
- *rp*-process nucleosynthesis slows down at waiting points
- Proton capture energetically disfavored
- Slow  $\beta^+$  decay rate dictates flow
- Examples:  $^{56}\text{Ni}$ ,  $^{64}\text{Ge}$ ,  $^{66}\text{Se}$ ,  $^{72}\text{Kr}$
- Sensitivity studies show  $(p, \gamma)$  reaction rates very important
- Spectroscopy of excited states (often through surrogate reactions)
- Spectroscopic factors from mirrored reactions
- $Q$ -values and masses are needed



J. Fisker et al. (2008)



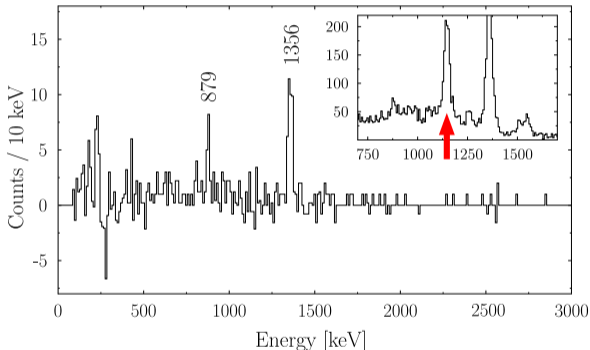
- $^{57}\text{Cu}(p, \gamma)$  reaction rate dominated by  $2^+$  resonances in  $^{58}\text{Zn}$
- First spectroscopy of  $^{58}\text{Zn}$



- Remaining uncertainty in the reaction rate dominated by  $Q$ -value

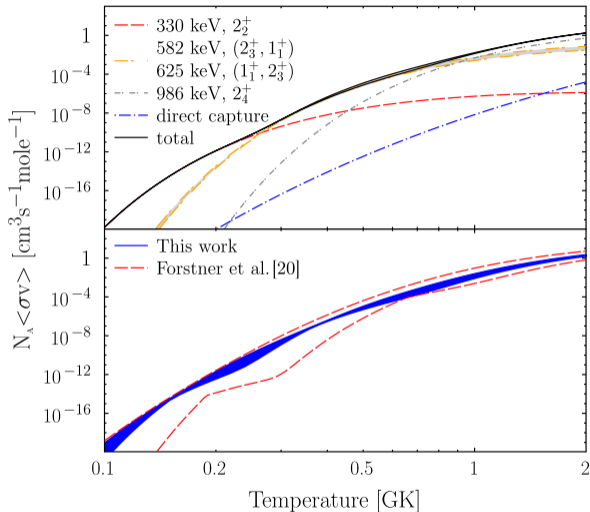
C. Langer *et al.*, Phys. Rev. Lett. **113** (2014) 032502.

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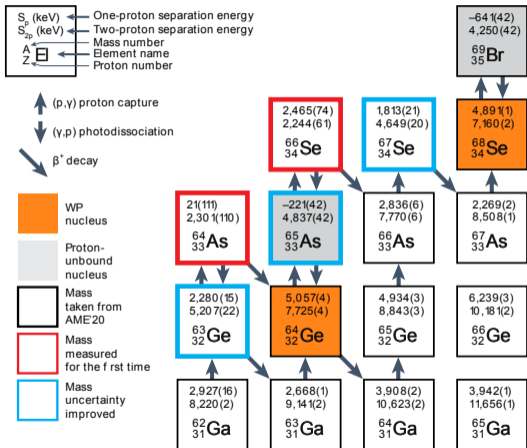
**Uncertainty of reaction rate reduced  
by 3 orders of magnitude**

C. Langer et al., Phys. Rev. Lett. **113** (2014) 032502.



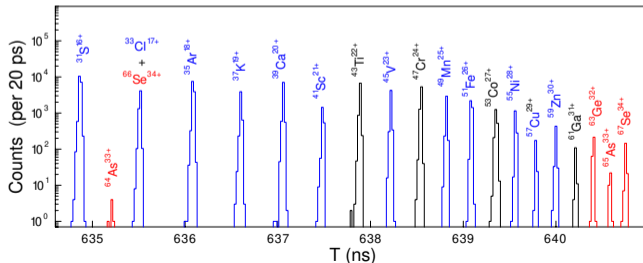
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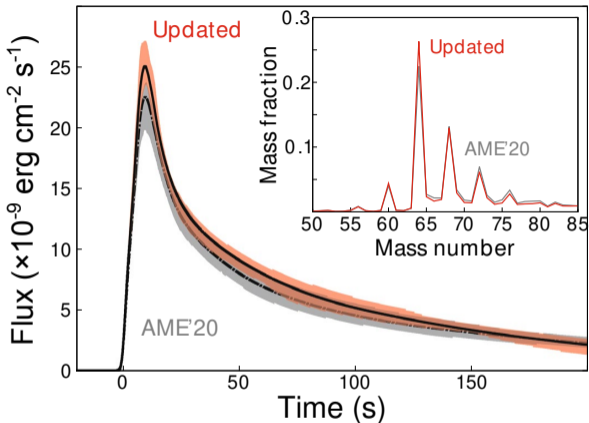
■ Proton capture on  $^{64}\text{Ge}$  leads to proton unbound  $^{65}\text{As}$



X. Zhou et al., Nature Physics **19** (2023) 1091.

- Waiting points at  $^{64}\text{Ge}$  ( $T_{1/2} = 64$  s) and  $^{66}\text{Se}$  ( $T_{1/2} = 36$  s)
- Mass uncertainties limiting reliability for reaction rate calculation and X-ray burst light curves
- New measurements at cooler-storage ring CSR, Lanzhou
- Improved uncertainties and new values

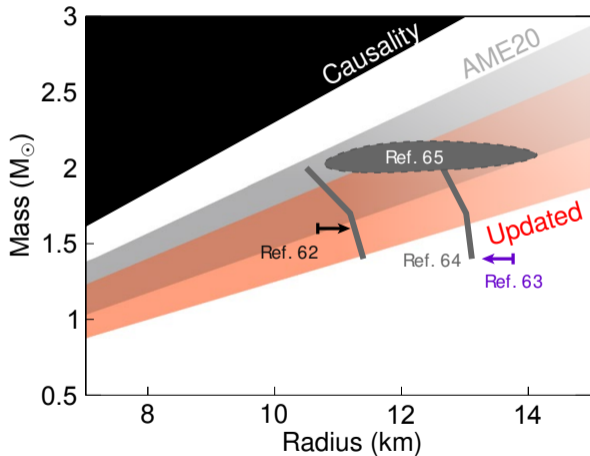




- X-ray burst luminosity allows to constrain distance and gravitational redshift ( $1 + z$ ) of the burster

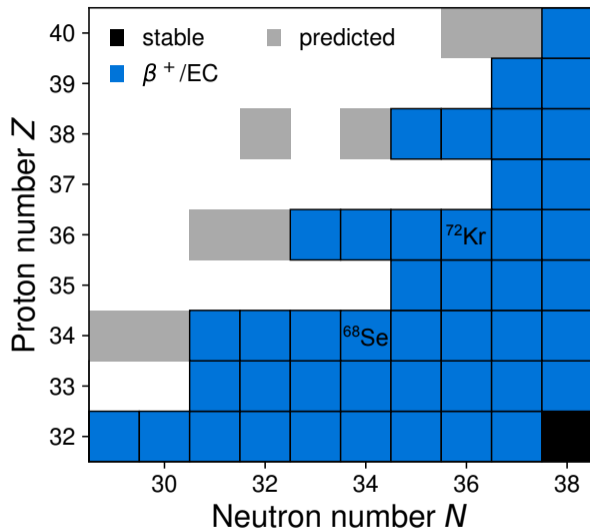
## Limits on neutron-star compactness

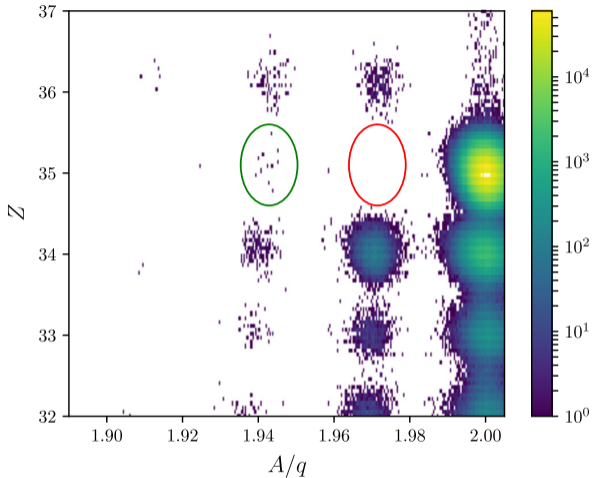
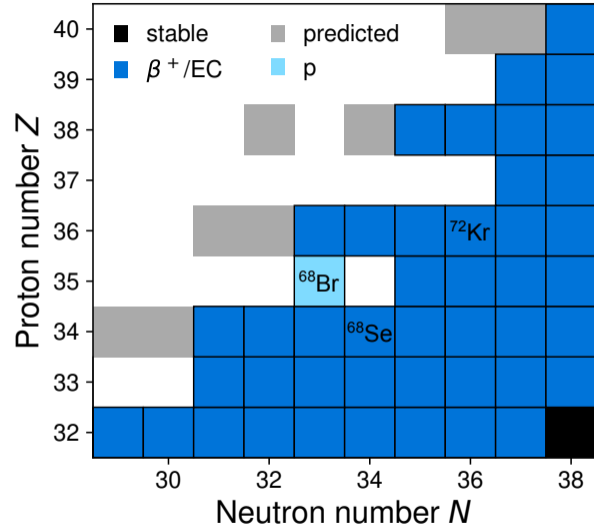
- Less bound  $^{65}\text{As}$ , stronger bound  $^{66}\text{Se}$  stalled  $rp$ -process at the  $^{64}\text{Ge}$  waiting point



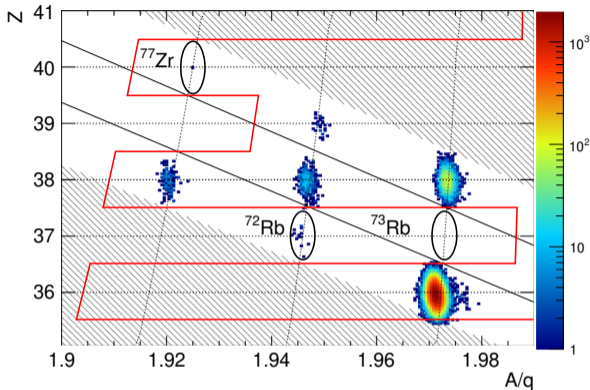
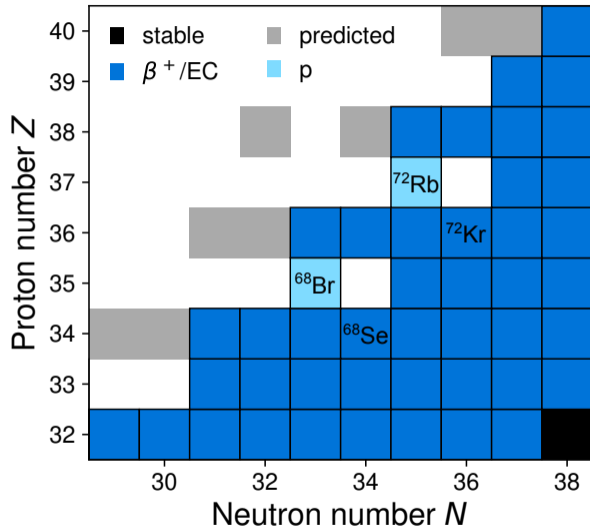
X. Zhou et al., Nature Physics **19** (2023) 1091.







K. Wimmer et al., Phys. Lett. B **795** (2019) 266.



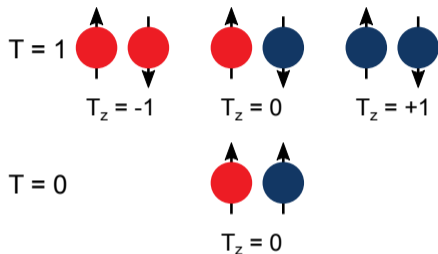
K. Wimmer et al., Phys. Lett. B **795** (2019) 266,  
 H. Suzuki et al., Phys. Rev. Lett **119** (2017) 192503.

- Odd-odd  $^{68}\text{Br}$  and  $^{72}\text{Rb}$  longer lived than less proton-rich neighbors ( $T_{1/2} \sim 100$  ns)

Influence on *rp*-process nucleosynthesis needs to be explored

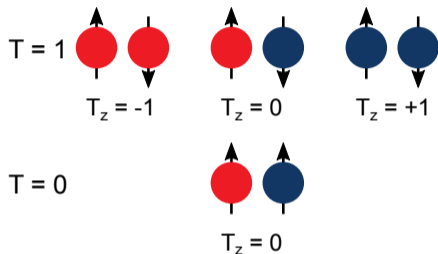
# Isospin symmetry

- Neutron and proton: two representations of the nucleon with isospin  $t_z = \pm 1/2$
- Led to the concept of quarks as constituents



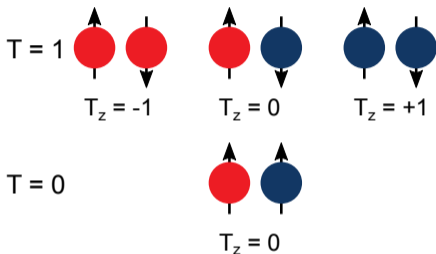
- Two nucleon system in  $T = 0$  and 1 channel: explains deuteron  $J^\pi = 1^+$
- Strong interaction **independent** of isospin or charge  
 $V_{np} = (V_{pp} + V_{nn})/2$
- **Symmetric** under exchange of protons and neutrons  
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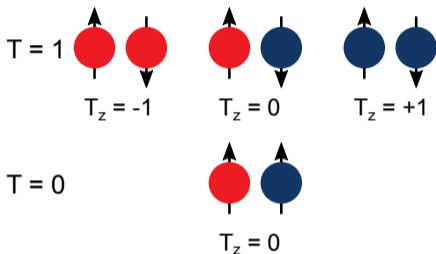
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- Violated by electromagnetic effects
- Light quark mass difference  $m_u \neq m_d$   
 $\rightarrow$  free neutron is unstable
- Relative proton-neutron mass difference 0.0013  
 $\rightarrow$  symmetry breaking is small
- $nn$ ,  $pp$ , and  $np$  scattering length are different

In nuclei:

- Exactly degenerate energies of isobaric multiplets
- Pure isospin quantum numbers
- No isospin mixing in nuclear states
- Identical wave functions for the members of an isobaric multiplet

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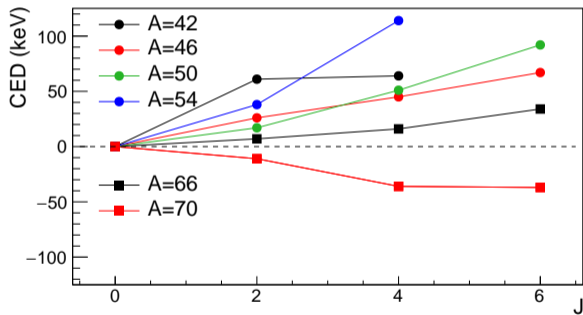
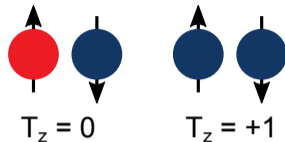
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- Coulomb energy differences between  $T = 1$  states:

$$\text{CED}(J^\pi) = E(J^\pi, T_z = 0) - E(J^\pi, T_z = 1)$$

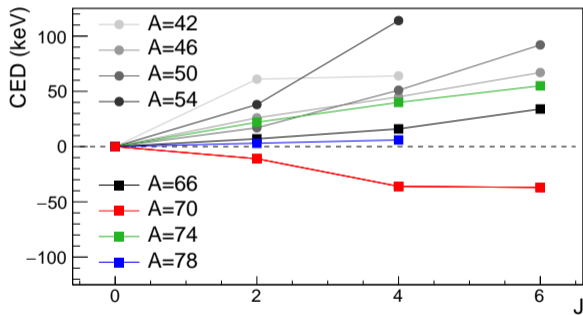
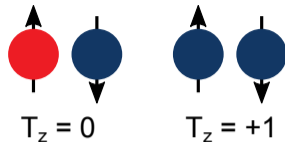


G. de Angelis et al., Eur. Phys. J. A **12** (2001) 51,  
 B. S. Nara Singh et al., Phys. Rev. C **75** (2007) 061301.

- CED rise as a function of spin in the *sd* and *fp* shell
- $A = 70$  isobars show anomalous Coulomb energy differences
- Weakly bound: reduction of Coulomb repulsion due to spatial extension of proton wave functions
- However, negative CED only occur in  $A = 70$  isotones
- May be explained by a shape change between  $^{70}\text{Se}$  and  $^{70}\text{Br}$

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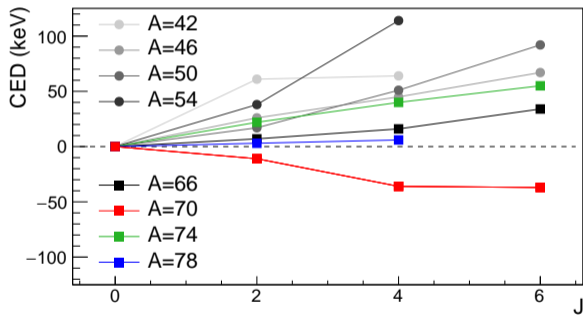
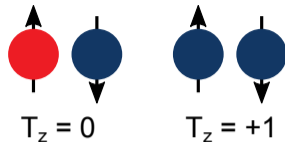
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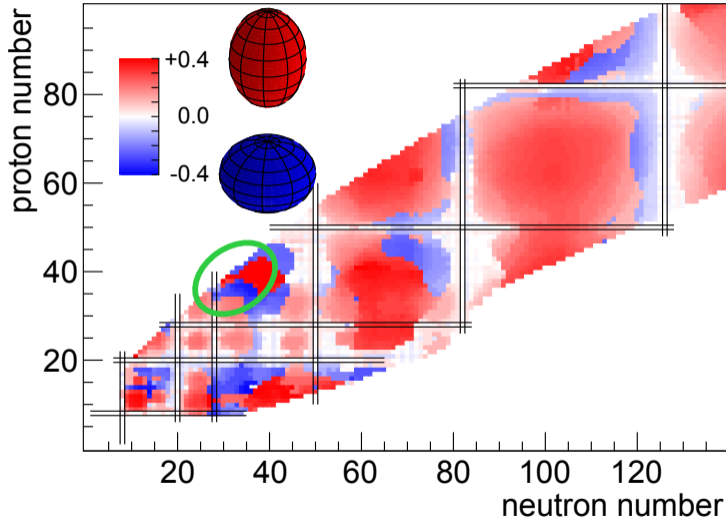


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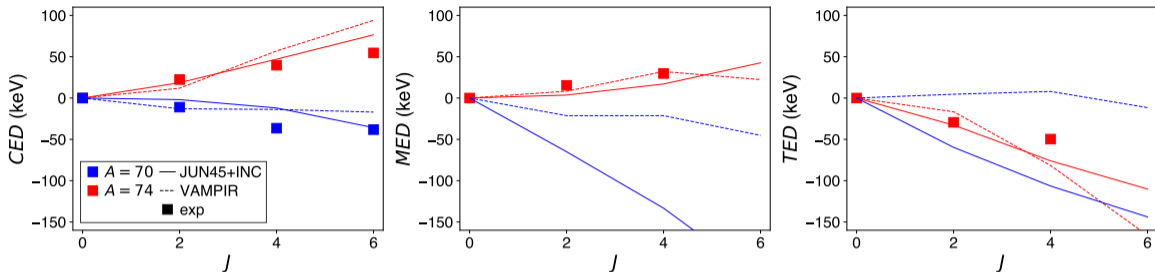
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→ Further lowering of states for  $T_z = -1$  nucleus  $^{70}\text{Kr}$  expected

- Predicted deformation parameters using finite-range droplet macroscopic model

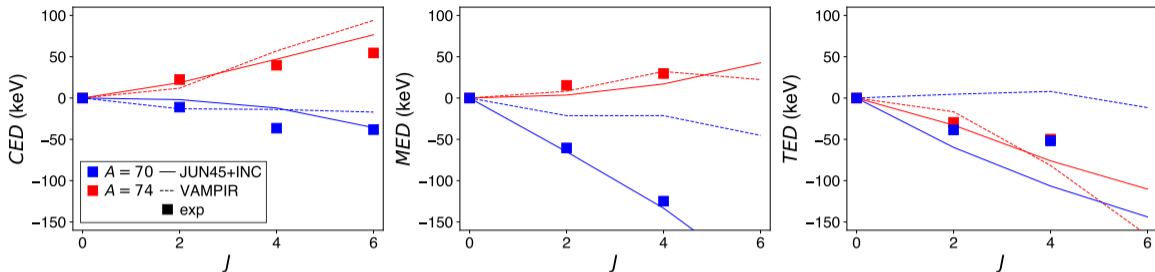


P. Möller et al., At. Data Nucl. Data Tables **109** (2016) 1.



A. Petrovici, Phys. Rev. C **91** (2015) 014302, K. Kaneko et al., Phys. Rev. Lett. **109** (2012) 092504, J. Henderson et al., Phys. Rev. C **90** (2014) 051303(R), D. M. Debenham et al., Phys. Rev. C **94** (2016) 054311, K. Wimmer et al., Phys. Lett. B **785** (2018) 441, G. L. Zimba et al. Phys. Rev. C **110** (2024) 024314.

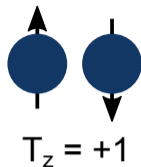
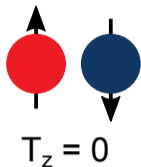
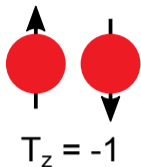
- Large positive contribution from monopole components leads to positive MED for  $A = 74$ , large negative spin-orbit component to negative MED for  $A = 70$
- Negative TED due to the fact that the excitation energy of the odd-odd  $T_z = 0$  nucleus is larger than either of the even-even isobars, proton-neutron pairing
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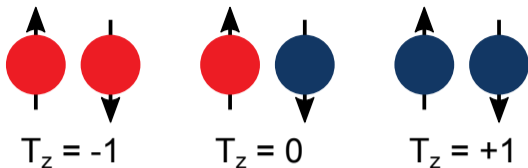
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**Energies alone do not probe the wave function,  
we need another observable to test the symmetry**



Charge independence of the nuclear interaction implies

- Exactly degenerate energies of isobaric multiplets
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- Determine multipole matrix elements from measured  $B(E2)$  values

$$M_{p/n} = \langle J_f || \sum_{p/n} r^\lambda Y_\lambda(\Omega) || J_i \rangle$$

$$B(E2; J_i \rightarrow J_f) = \frac{|\langle J_f || E2 || J_i \rangle|^2}{2J_i + 1} = \frac{M_p^2(E2)}{2J_i + 1}$$

- In isospin representation:

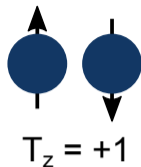
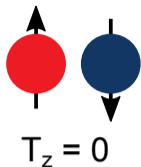
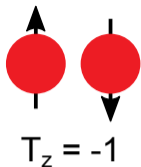
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- Assuming isospin symmetry:

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A. M. Bernstein, V. R. Brown, and V. A. Madsen, Phys. Rev. Lett. 42 (1979) 425.





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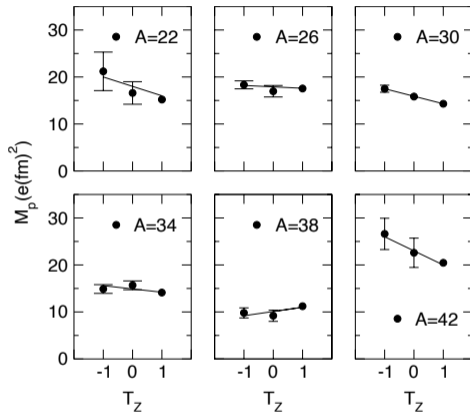
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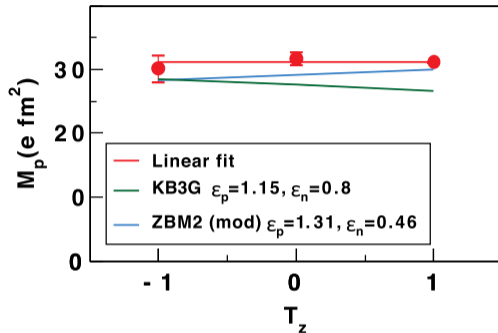
A. M. Bernstein, V. R. Brown, and V. A. Madsen, Phys. Rev. Lett. **42** (1979) 425.

- $M_p(T_z)$  should be linear if isospin is conserved



F. M. Prados Estévez et al., Phys. Rev. C **75** (2007) 014309.

- Well tested for nuclei up to  $A = 46$



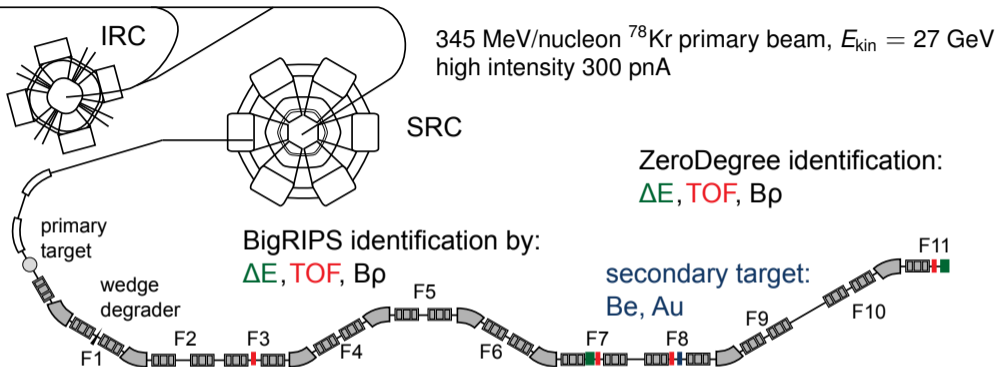
A. Boso et al., Phys. Lett. B **797** (2019) 134835.

- No  $B(E2)$  data on  $T_z = -1$  nuclei beyond  $A = 54$

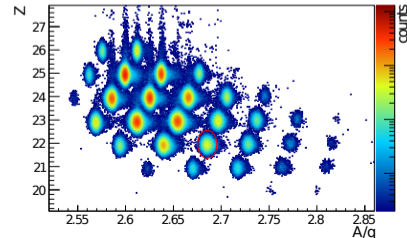
K. L. Yurkewicz et al., Phys. Rev. C **70** (2004) 054319.

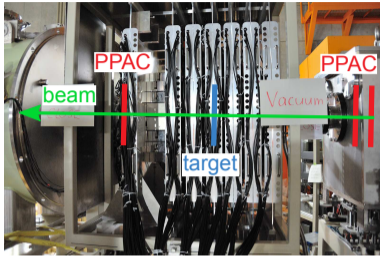
Different experiments and techniques used for different isobars

→ need for a consistent approach

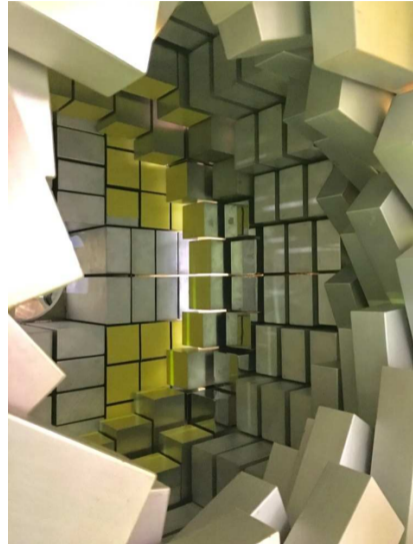
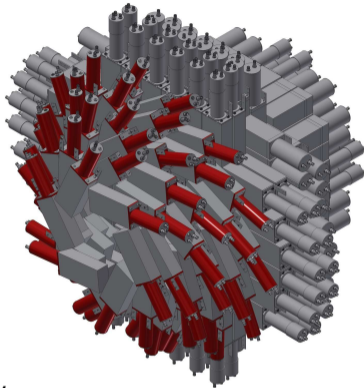


- Fragmentation or fission of intense primary beam
- Particle identification by  $B\rho - \Delta E - \text{TOF}$ :  
intensity  $^{70}\text{Kr}$  only 15 pps
- Secondary reaction target at F8 surrounded by  $\gamma$ -ray detectors
- Identification after target:  
ZeroDegree spectrometer in large acceptance mode





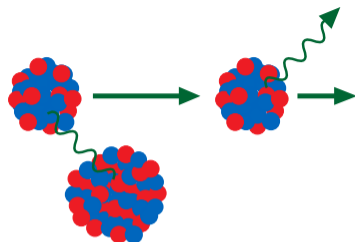
S. Takeuchi et al.,  
Nucl. Instr. Meth. **A 763** (2014) 596.



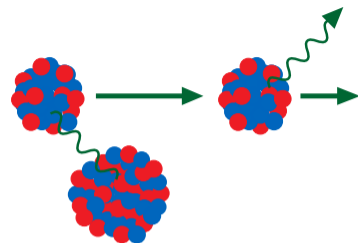
- 226 NaI(Tl) detectors
- Intrinsic resolution 7 % at 1 MeV
- In-beam resolution  $\sim 10$  % at 150 A MeV
- Efficiency  $\sim 20$  % at 1 MeV (before add-back)
- Beam tracking by PPACs

- Excitation of the projectile in the electromagnetic field of a high-Z target
- Absorption of virtual photon
- At relativistic energies one-step excitation is limited to (first)  $2^+$  states
- Measure cross section from de-excitation yield
- Nuclear excitation also contributes and interferes
- Developed consistent analysis approach for relativistic Coulomb excitation

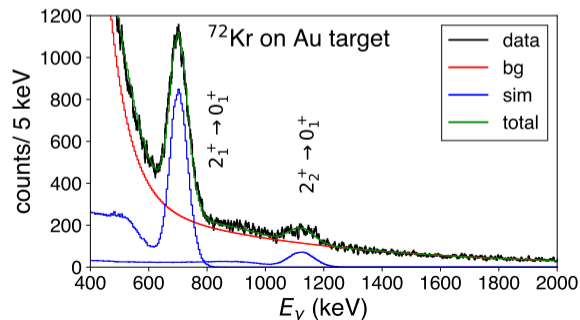
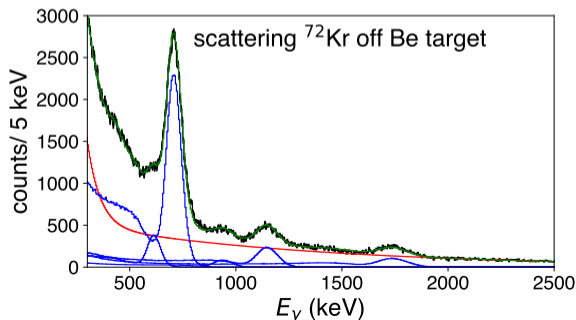
K. Wimmer et al., Eur. Phys. J. A 56 (2020) 159.

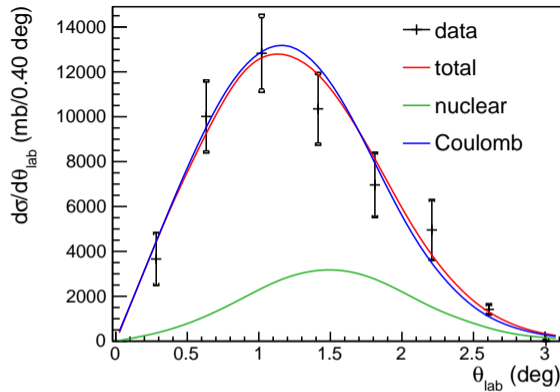
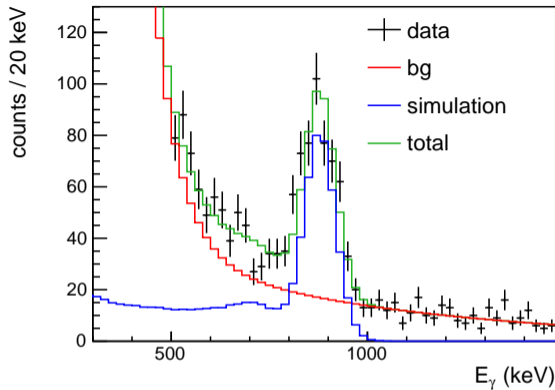


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- Measure cross section from de-excitation yield
- Nuclear excitation also contributes and interferes
- Developed consistent analysis approach for relativistic Coulomb excitation



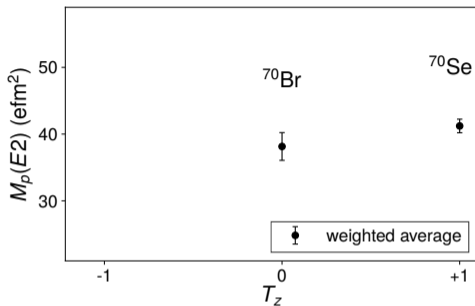
K. Wimmer et al., Eur. Phys. J. A **56** (2020) 159.





- Excitation energy of  $^{70}\text{Kr}$ :  $E(2^+) = 884$  keV
- Nuclear deformation length from Be target data:  $\beta_N = 0.22(4)$
- Feeding corrections estimated from  $^{72}\text{Kr}$  and  $^{68}\text{Se}$ , and theoretical calculations
- $B(E2 \uparrow) = 2726(294)_{\text{stat.}}(224)_{\text{syst.}}(258)_{\text{theo.}} \text{ e}^2\text{fm}^4$   
or  $\beta_C = 0.25(2)$

K. Wimmer et al., Phys. Lett. B **785** (2018) 441.



- Previous measurements of Se/Br suggest negative trend

J. Ljungvall et al., Phys. Rev. Lett. **100** (2008) 102502,  
A. J. Nichols et al., Phys. Lett. B **733** (2014) 52.

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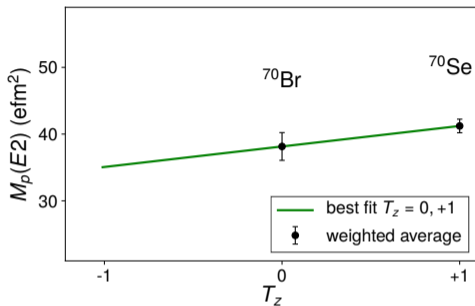
$$M_0 = 76(4) \text{ efm}^2, M_1 = -6(5) \text{ efm}^2$$

- Larger matrix element for proton-rich?
- Negative trend in other  $A > 50$  cases

C. Morse et al., Phys. Lett. B. **787** (2018) 198.

- Extrapolation  $M(E2, T_z = -1) = 35.0(43) \text{ efm}^2$
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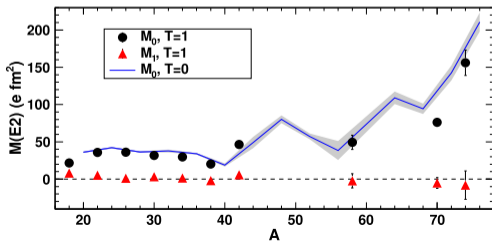
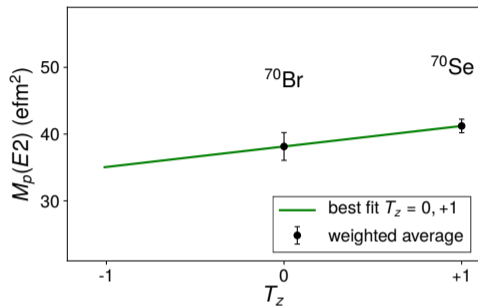
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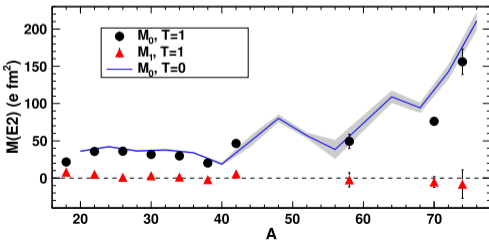
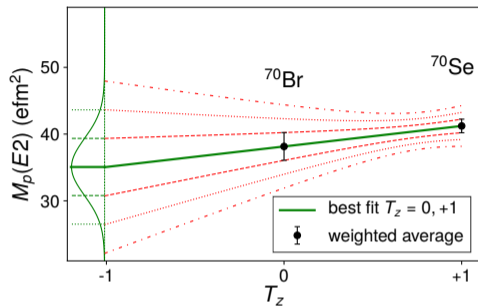
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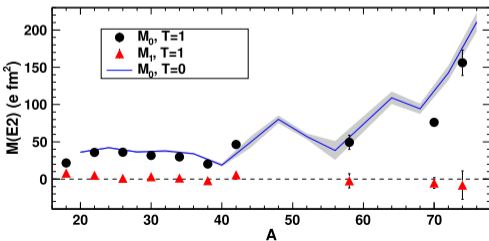
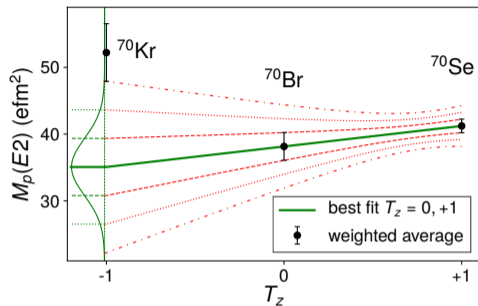
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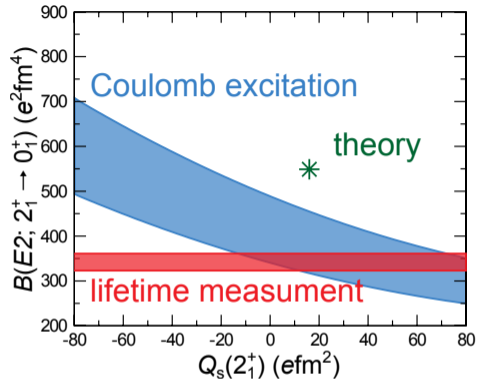
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**Sign of deviation from isospin symmetry in  $A = 70$  triplet**

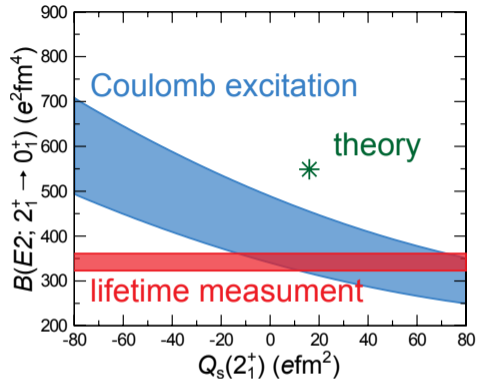
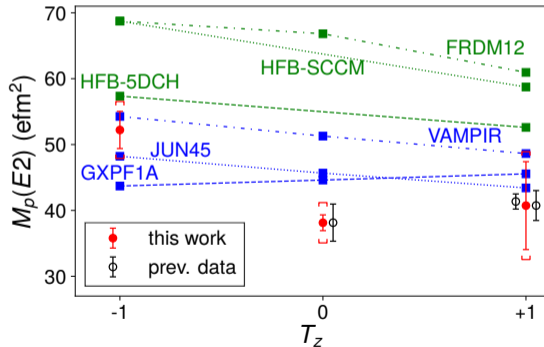
K. Wimmer et al., Phys. Rev. Lett. **126** (2021) 072501.

- $^{70}\text{Se}$  is oblate deformed
- Isospin symmetry: same expected for  $^{70}\text{Kr}$
- Theoretical calculations predict
  - Oblate deformation for  $^{70}\text{Se}$  and  $^{70}\text{Kr}$
  - Only a small increase in  $M_p$  in  $^{70}\text{Kr}$



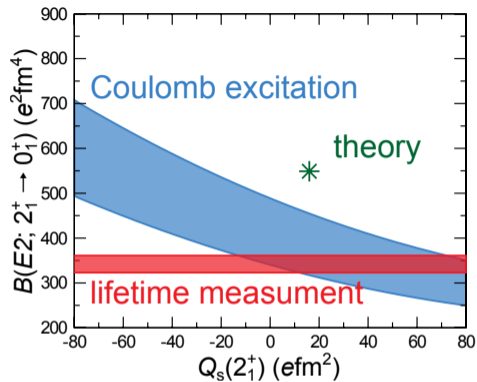
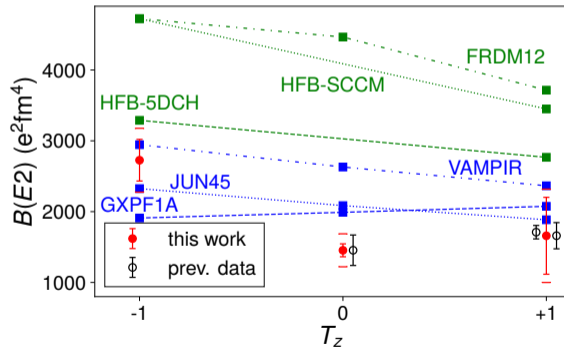
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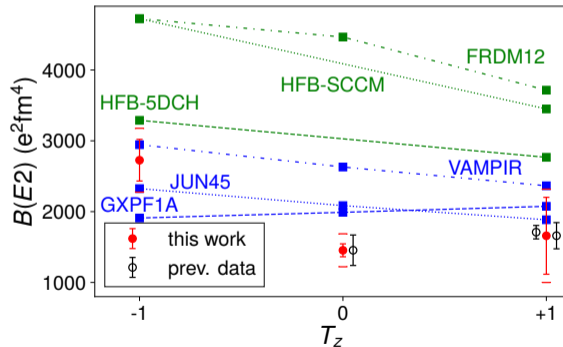
A. M. Hurst et al., Phys. Rev. Lett. **98** (2007) 072501,  
 J. Ljungvall et al., Phys. Rev. Lett. **100** (2008) 102502.

- (Axial) rotational model

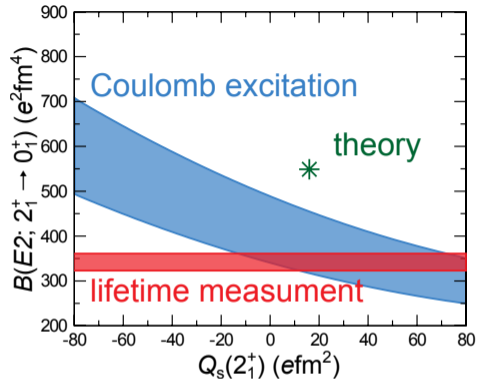
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## Shape change in the mirror nuclei $^{70}\text{Se}$ and $^{70}\text{Kr}$



A. M. Hurst et al., Phys. Rev. Lett. **98** (2007) 072501,  
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- Heaviest isospin triplet where all three matrix elements are experimentally known
- $M_p(E2; 0_1^+ \rightarrow 2_1^+)$  value of  $^{70}\text{Kr}$  significantly larger than in  $^{70}\text{Se}$
- $3\sigma$  deviation from the extrapolation of a linear relationship  $M_p(T_z)$

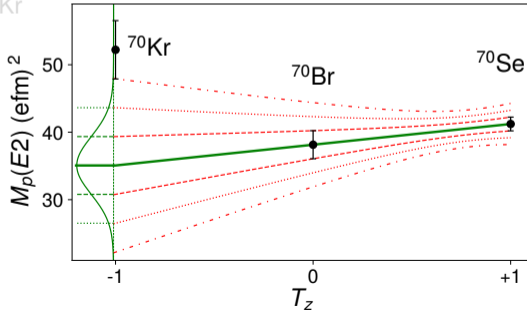
- Isospin mixing of  $T = 0, 1$  states in  $^{70}\text{Br}$ ?
  - No close-lying  $2^+$  states known
  - Isospin mixing cannot explain the increase in collectivity in  $^{70}\text{Kr}$

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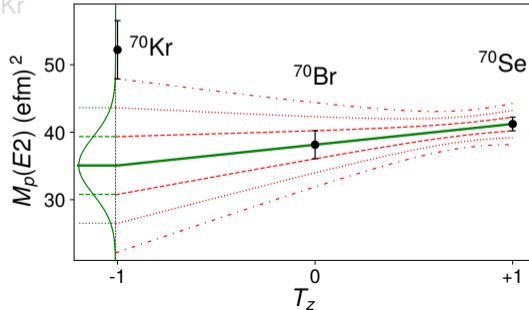
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Low-energy Coulomb excitation could help, but experiment presently out of reach  
cf.  $^{70}\text{Kr}$  intensity 15 pps

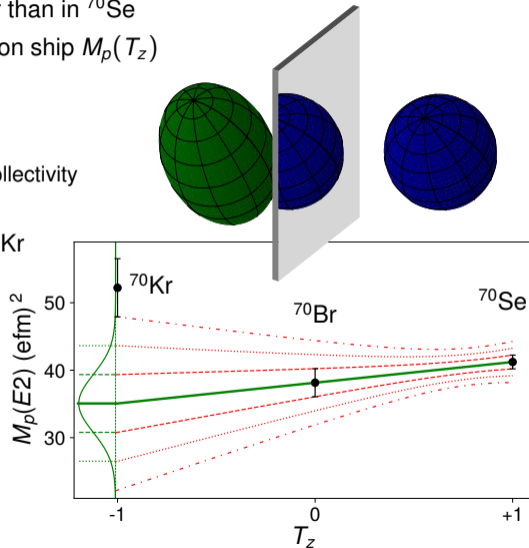
- What about other medium-mass  $T = 1$  triplets?



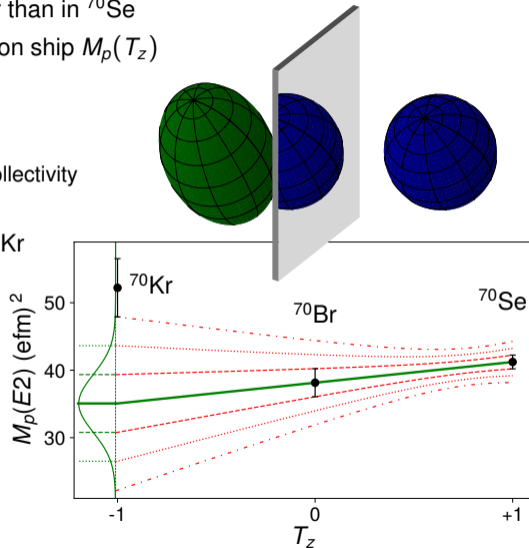
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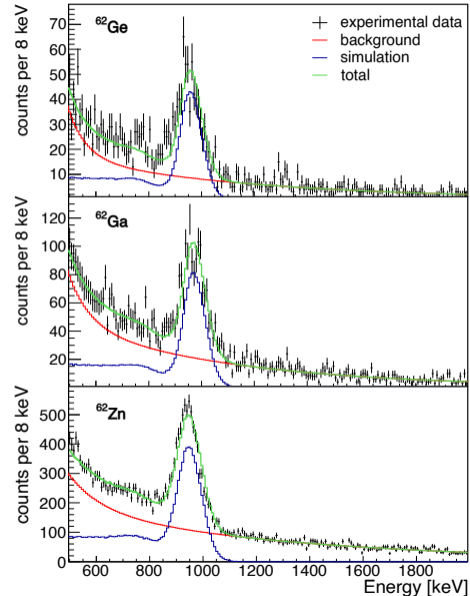
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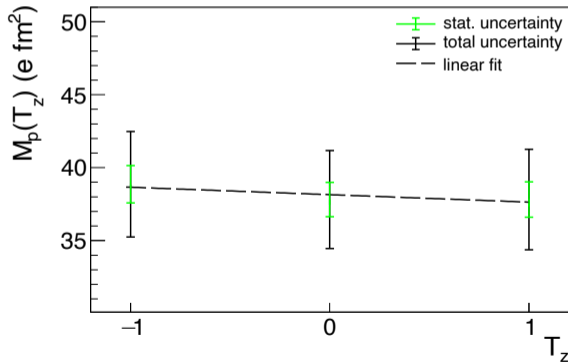


- Systematic uncertainties from different measurements
  - use same technique for all three members of a triplet
- New experiment: Coulomb excitation of  $A = 62$ ,  $T = 1$  triplet using identical target, beam energy, and detector
- Cancellation of systematic uncertainties

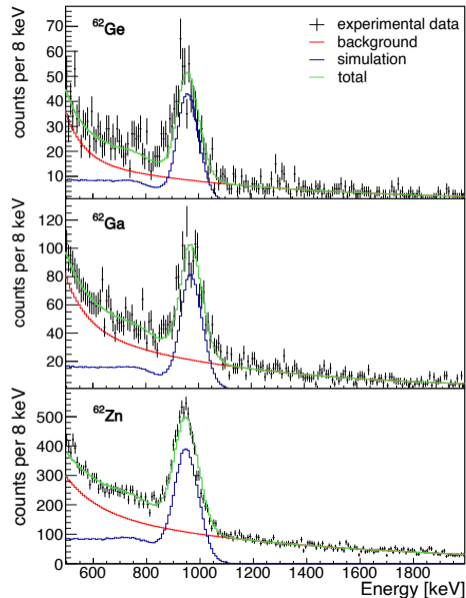


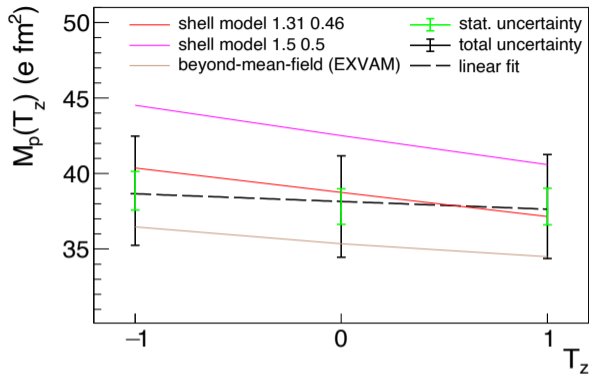
T. Hüyük et al., in prep.

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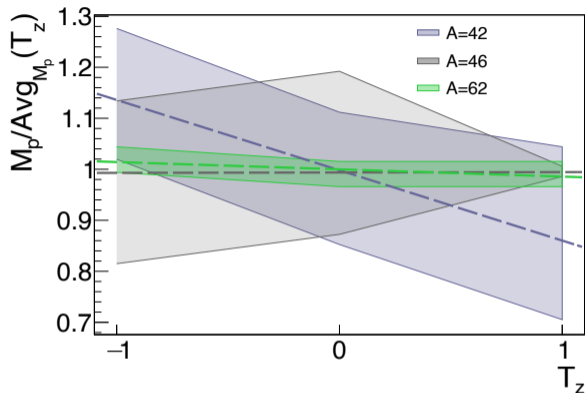
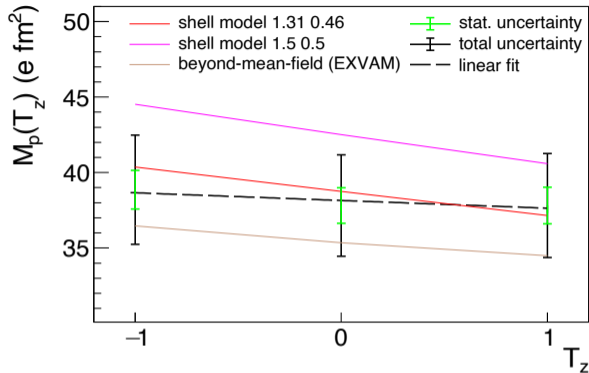
T. Hüyük et al., in prep.





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T. Hüyük et al., in prep.



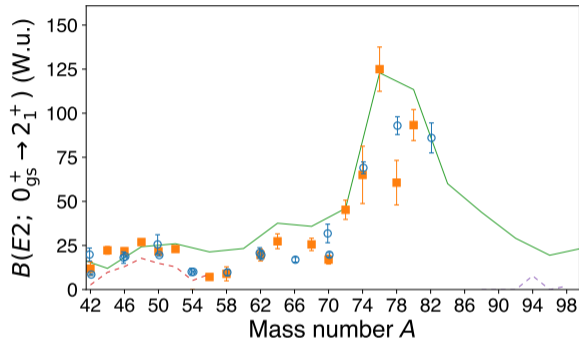
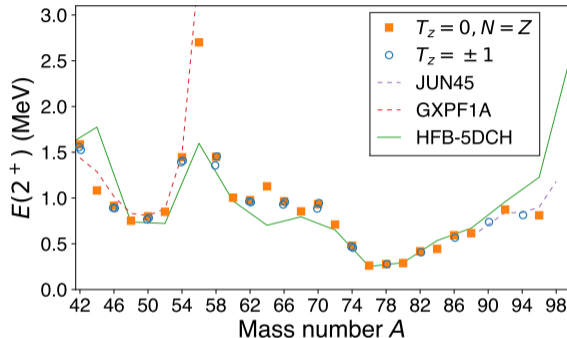
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## Precision experiment with radioactive beams

T. Hüyük et al., in prep.



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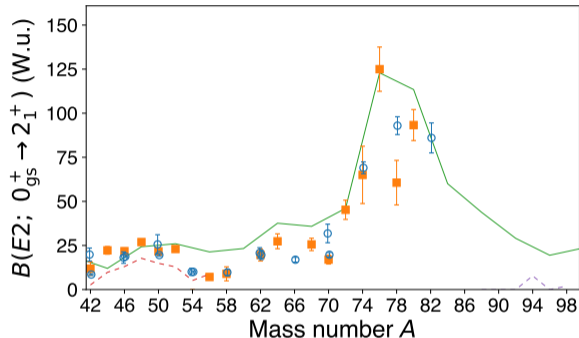
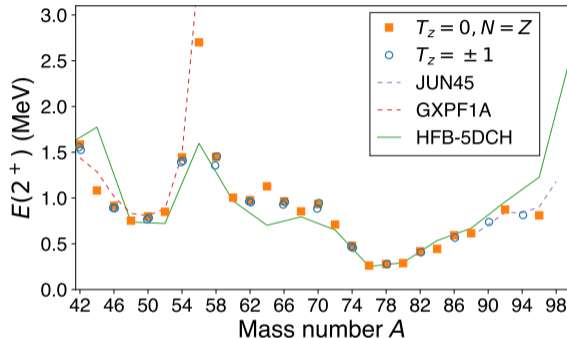


- $A = 62$  triplet well in shell-model regime
- Strong onset of collective behavior from  $^{72}\text{Kr}$
- Maximum collectivity and deformation observed for  $^{76}\text{Sr}$
- For  $N = Z$  curious odd-odd versus even-even staggering

K. Wimmer, P. Ruotsalainen, S.M. Lenzi et al., Phys. Lett. B **847** (2023) 138249.

R. D. O. Llewellyn et al., Phys. Rev. Lett. **124** (2020) 152501.

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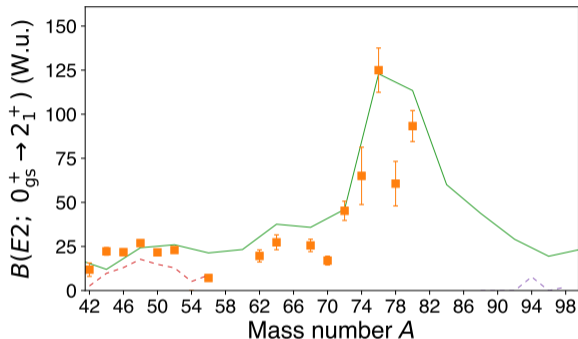
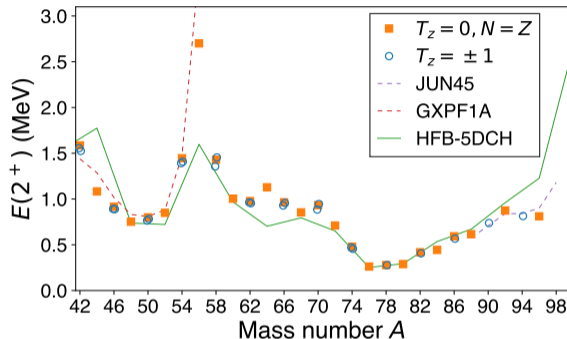


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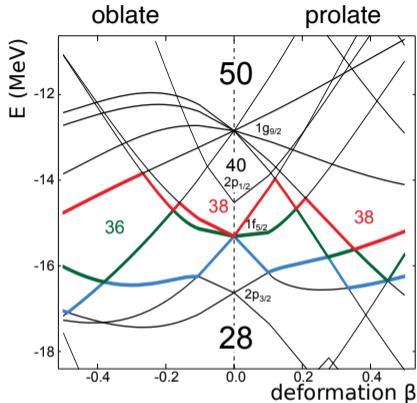
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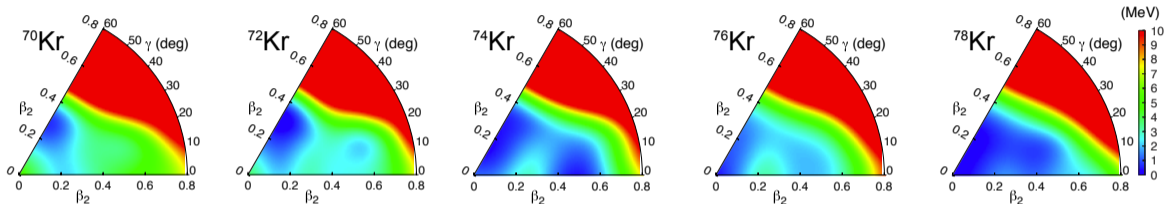
- Nuclei around  $A = 80$  are very strongly deformed
- Small changes in the single-particle structure can lead to drastic change in deformation
- Contribution of  $p$  orbitals to radial Coulomb term quenched due to decrease in radius  
A. Fernández et al., Phys. Lett. B **823** (2021) 136784.
- Coulomb interaction depends on spatial configuration of protons
- $^{70}\text{Kr}$  currently out of reach for shell model calculations  
 required model space is at least  $pf_{5/2}g_{9/2}$ , but excitations beyond 50 and below 28 are required to appropriately model the collectivity

- Fully microscopic description of the deformation in the region yet to be attained

**In a region where deformation and collectivity rise, a small change in the configuration of protons and neutrons can cause large difference in shape**

# Shape coexistence

- Proton-rich Kr ( $Z = 36$ ) isotopes show a variety of shapes
- Self-consistent beyond mean-field calculations of potential energy surface



T. R. Rodríguez, Phys. Rev. C **90** (2014) 034306.

- Spherical  $^{76,78}\text{Kr}$
- Degenerate minima in  $^{74}\text{Kr}$ : shape coexistence and mixing

E. Clement et al., Phys. Rev. C **75** (2007) 054313.

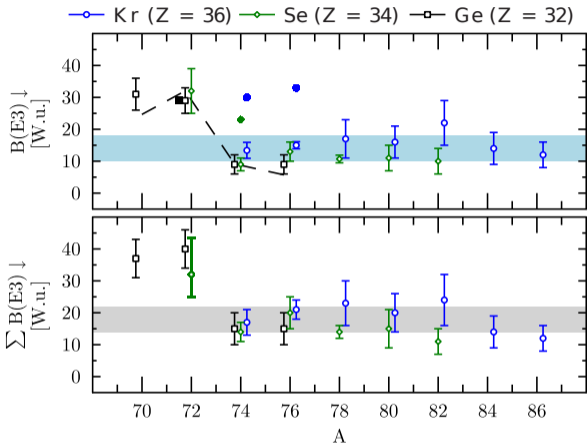
- $^{72}\text{Kr}$ : oblate ground state and rapid oblate - prolate transition with increasing spin

A. Gade et al., Phys. Rev. Lett. **95** (2005) 022502, H. Iwasaki et al., Phys. Rev. Lett. **112** (2014) 142502.

- Second minimum: excited  $0^+$  state in  $^{72}\text{Kr}$  with large difference in deformation

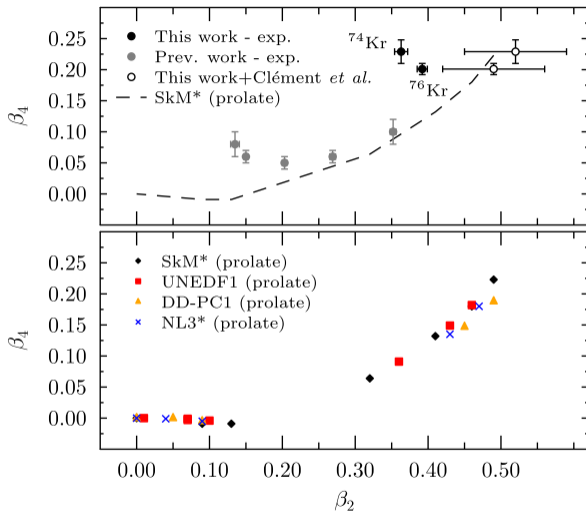
E. Bouchez et al., Phys. Rev. Lett. **90** (2003) 082502.

- Prediction for  $^{70}\text{Kr}$ : oblate deformed

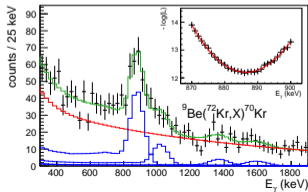
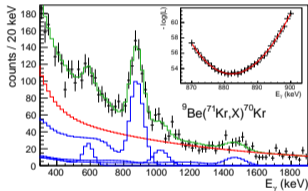
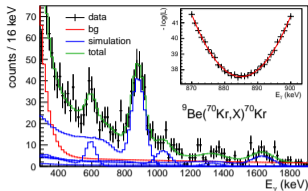


M. Spieker et al., Phys. Rev. C **106** (2022) 054305.

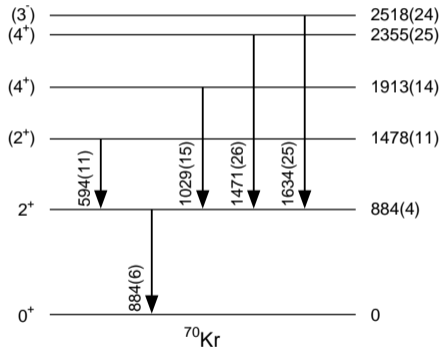
- Large octupole and hexadecupole deformation inferred from inelastic scattering



M. Spieker et al., Phys. Lett. B **841** (2023) 137932.



- Inelastic scattering of  ${}^{70}\text{Kr}$  on Be target
- One- and two-neutron removal reaction from  ${}^{71,72}\text{Kr}$
- Likely-hood fit to obtain  $\gamma$ -ray transitions energies



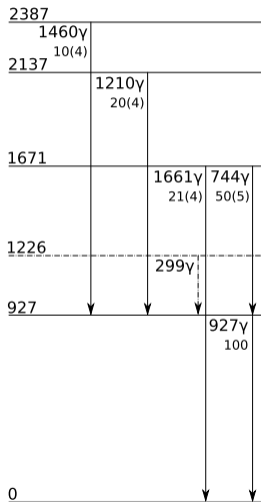
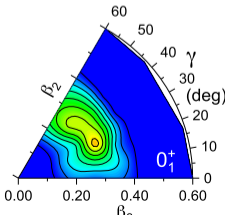
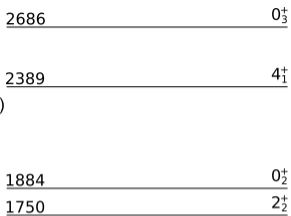
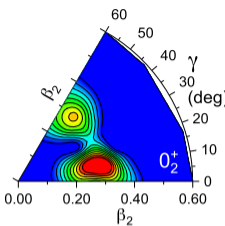
K. Wimmer et al., Phys. Lett. B **785** (2018) 441.

**Coexisting excited band in  ${}^{70}\text{Kr}$**   
 **$0^+$  states still missing in  ${}^{70}\text{Se}$  and  ${}^{70}\text{Kr}$**



- New excited states in  $^{66}\text{Se}$
- SCCM calculations show rough agreement with data
- Coexisting triaxial-deformed configurations
- Ground-state band more oblate
- Excited band more prolate

Z. Elekes et al.,  
Phys. Lett. B **844** (2023) 138072.



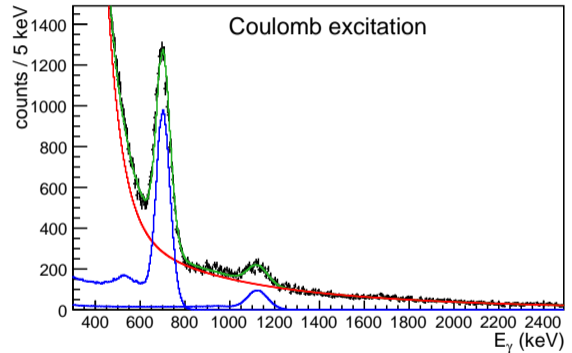
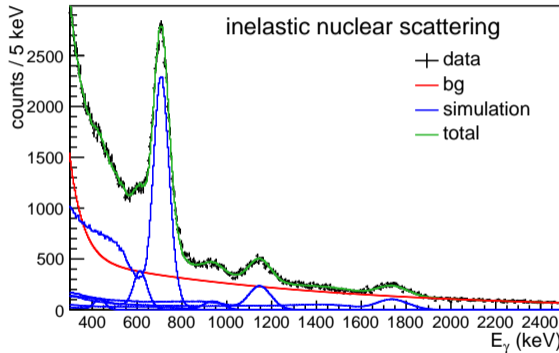
SCCM

Experiment

- High-spin  $^{72}\text{Kr}$  level scheme well known from fusion evaporation reactions

N. S. Kelsall et al., Phys. Rev. C **64** (2001) 024309, S. M. Fisher et al., Phys. Rev. C **67** (2003) 064318.

- Excited states in  $^{72}\text{Kr}$  populated in inelastic scattering off Be and Au targets

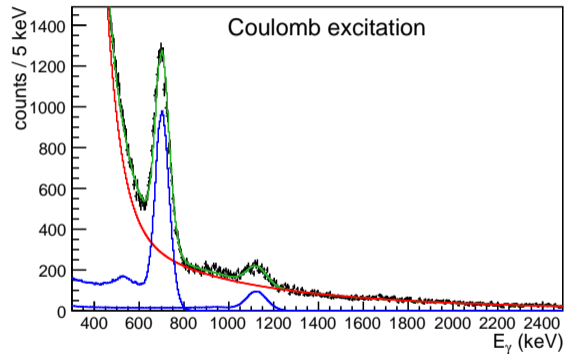
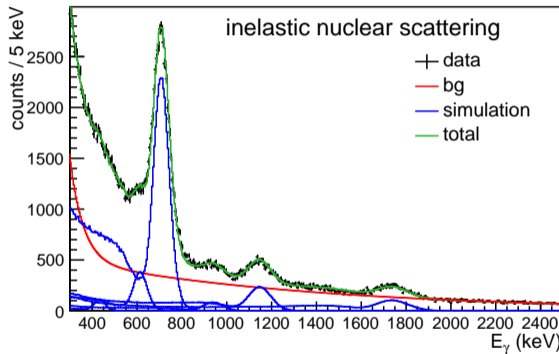


- Four new transitions observed
- 1148(5) keV transition also in Coulomb excitation  $\rightarrow$  new  $2^+$  state
- 947(7) keV transition in coincidence  $\rightarrow$  new  $4^+$  state

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- Physical  $J^\pi = 0^+, 2^+, \text{ and } 4^+$  states are mixture of pure prolate and oblate configurations:

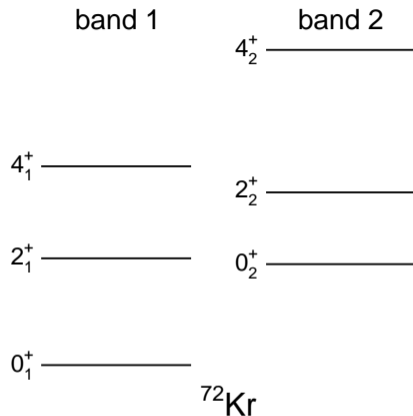
$$|J_1^+\rangle = +a_J|J_p^+\rangle + b_J|J_o^+\rangle$$

$$|J_2^+\rangle = -b_J|J_p^+\rangle + a_J|J_o^+\rangle$$

- Yrast band prolate deformed at high spin

R. B. Piercey et al., Phys. Rev. Lett. **47** (1981) 1514.

- Extrapolation using variable moment of inertia  $I = I_0 + \omega^2 I_1$   
 $\rightarrow$  unperturbed energies



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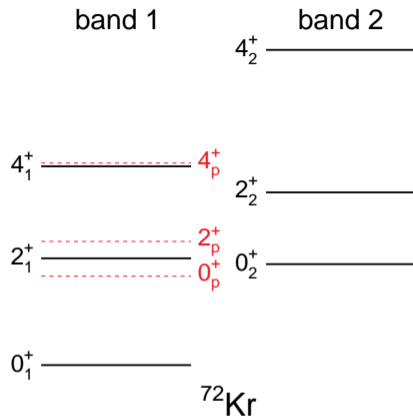
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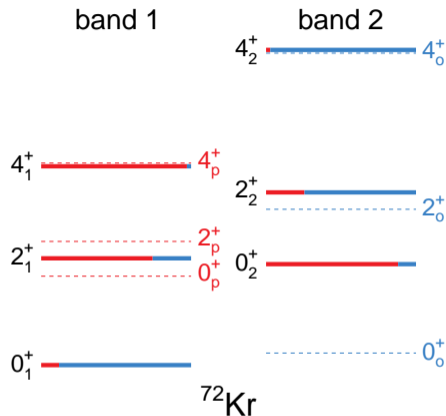
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- ground state oblate dominated

- New  $2_2^+$  and  $4_2^+$  states allow to extend the mixing analysis

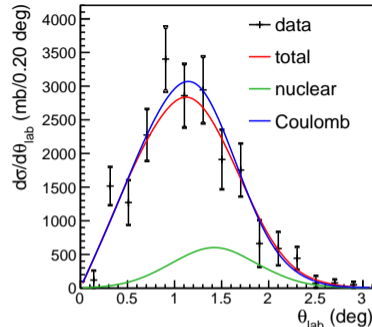
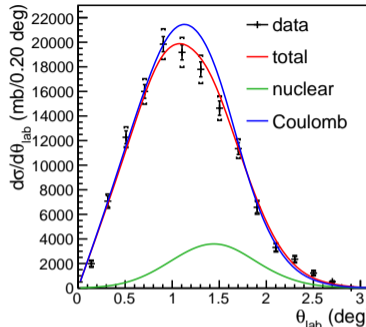
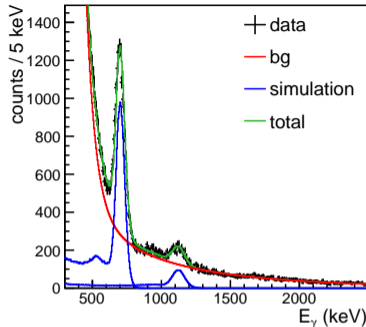
- Inversion with oblate ground state, rapid transition towards prolate yrast states

- In agreement with interpretation of  $B(E2; 4_1^+ \rightarrow 2_1^+)$



E. Bouchez et al., Phys. Rev. Lett. **90** (2003) 082502.

H. Iwasaki et al., Phys. Rev. Lett. **112** (2014) 142502.



- Nuclear deformation length and  $E2$  matrix elements obtained from comparison with FRESKO (DWCC) calculations

state	$\beta_N$	$\beta_C$	$B(E2 \uparrow)$ ( $e^2\text{fm}^4$ ) this	prev.
$2_1^+$	0.309(2)(9)(8)	0.296(3)(11)(13)	4023(81) <sub>stat.</sub> (290) <sub>syst.</sub> (380) <sub>theo.</sub>	4997(647) 4050(750)
$2_2^+$	0.123(4)(5)(3)	0.112(3)(4)(5)	665(39) <sub>stat.</sub> (58) <sub>syst.</sub> (63) <sub>theo.</sub>	-

A. Gade et al., Phys. Rev. Lett. **95** (2005) 022502, H. Iwasaki et al., Phys. Rev. Lett. **112** (2014) 142502.

**Different deformation  $\rightarrow$  shape coexistence**

- So far, only energies are considered to obtain  $a, b_J$ :

$$b_0^2 = 0.881, b_2^2 = 0.256, \text{ and } b_4^2 = 0.028$$

- Matrix elements (transitions between the pure configurations are forbidden)

$$\langle 2_1^+ || E2 || 0_1^+ \rangle = b_0 b_2 \langle 2_0^+ || E2 || 0_0^+ \rangle + a_0 a_2 \langle 2_p^+ || E2 || 0_p^+ \rangle$$

$$\langle 2_2^+ || E2 || 0_1^+ \rangle = b_0 a_2 \langle 2_0^+ || E2 || 0_0^+ \rangle - a_0 b_2 \langle 2_p^+ || E2 || 0_p^+ \rangle$$

$$\langle 4_1^+ || E2 || 2_1^+ \rangle = b_2 b_4 \langle 4_0^+ || E2 || 2_0^+ \rangle + a_2 a_4 \langle 4_p^+ || E2 || 2_p^+ \rangle$$

$$\langle 0_2^+ || E0 || 0_1^+ \rangle = a_0 b_0 (\langle 0_0^+ || E0 || 0_0^+ \rangle - \langle 0_p^+ || E0 || 0_p^+ \rangle)$$



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 $b_0^2 = 0.881$ ,  $b_2^2 = 0.256$ , and  $b_4^2 = 0.028$
- Matrix elements (transitions between the pure configurations are forbidden)
- $4^+$  states pure  $a_4 = 1$ , deformation  $\beta$  from reduced transition probability

$$B(E2; J_i \rightarrow J_f) = \frac{5}{16\pi} (eQ_0)^2 |\langle J_i K_i 20 | J_f K_f \rangle|^2$$

$$Q_0^{o/p} = ZR^2 \frac{3}{\sqrt{5\pi}} (\beta_{o/p} + 0.36\beta_{o/p}^2)$$

$$B(E2; 2_1^+ \rightarrow 0_1^+) = \left( \frac{3e}{4\pi} R^2 Z \right)^2 |\langle 2020 | 00 \rangle|^2 [b_0 b_2 (1 + 0.36\beta_o) \beta_o + a_0 a_2 (1 + 0.36\beta_p) \beta_p]^2$$

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$$\rho^2(E0; 0_2^+ \rightarrow 0_1^+) = \left( \frac{3e}{4\pi} Z \right)^2 a_0^2 b_0^2 (\beta_o - \beta_p)^2$$

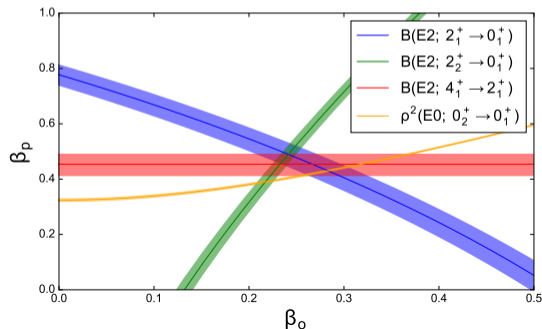
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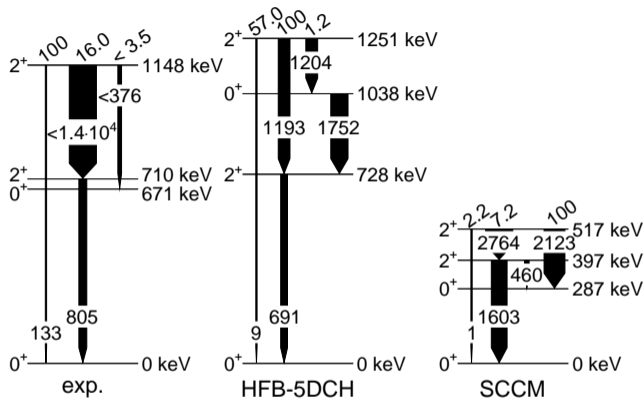
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$$Q_0^{o/p} = ZR^2 \frac{3}{\sqrt{5\pi}} (\beta_{o/p} + 0.36\beta_{o/p}^2)$$

- Equation system with many possible signs
- Using  $a_0^2 = 0.256, a_2^2 = 0.744$  from the energies
- Overlap in the region  $\beta_o = 0.24$  and  $\beta_p = 0.45$
- Shape coexistence and mixing

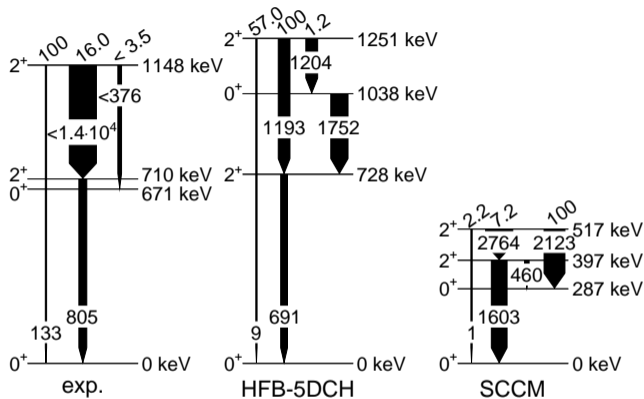
K. Wimmer et al., Eur. Phys. J. A **56** (2020) 159.





- Beyond mean field calculations using Gogny D1S interaction
- HFB-5DCH calculations  
J. P. Delaroche et al., Phys. Rev. C **81** (2010) 014303.
- SCCM method  
T. R. Rodríguez, Phys. Rev. C **90** (2014) 034306.
- Both in expanded spaces

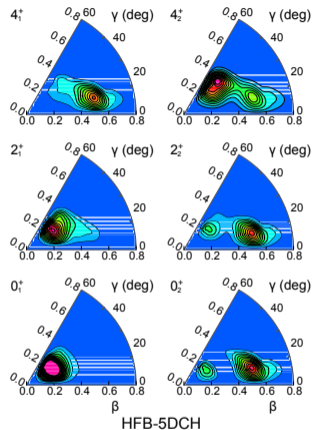
- Reproduce  $B(E2; 2_1^+ \rightarrow 0_1^+)$  rather well
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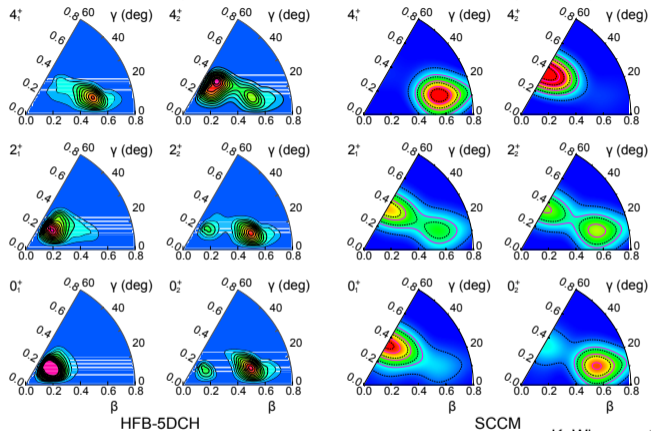
Probability densities (HFB-5DCH method) and collective wave functions (SCCM)



K. Wimmer et al., Eur. Phys. J. A **56** (2020) 159.

- 5DCH:  $0_1^+$  and  $2_1^+$  oblate, transition to prolate for  $4_1^+$
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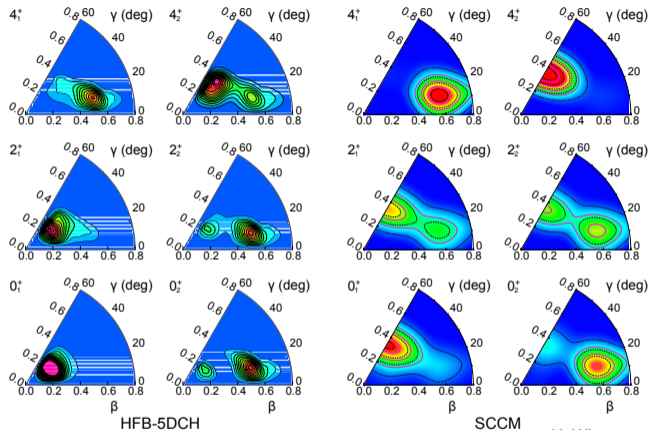
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K. Wimmer et al., Eur. Phys. J. A 56 (2020) 159.

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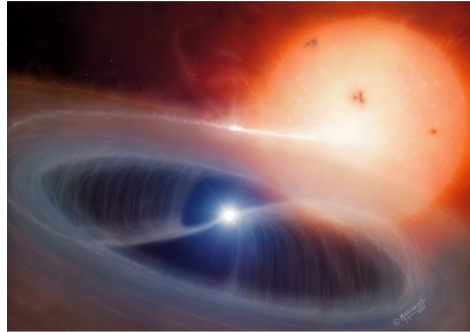


K. Wimmer et al., Eur. Phys. J. A **56** (2020) 159.

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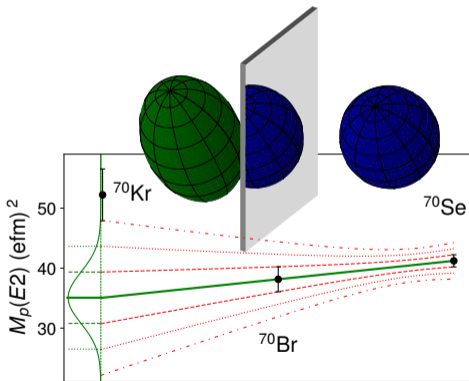
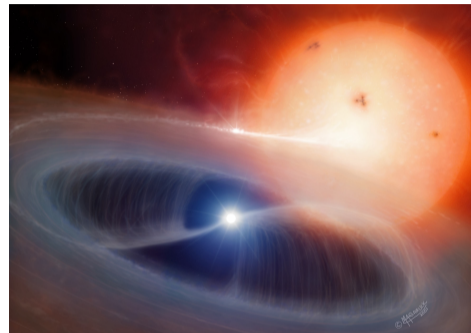
## Coexistence and shape change along yrast band

- Their properties influence nucleosynthesis
- Mass measurements and proton-capture reactions
- Lifetimes of proton-unbound nuclei





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- Isospin symmetry of multipole matrix elements violated at  $A = 70$
- Shape change in the mirror nuclei  $^{70}\text{Se}$  and  $^{70}\text{Kr}$
- Symmetry preserved in  $A = 62$  system
- Interesting region of large ground state deformation

## RIBF94

W. Korten, T. Arici, P. Doornenbal, P. Aguilera, A. Algora, T. Ando, H. Baba, B. Blank, A. Boso, S. Chen, A. Corsi, P. Davies, G. de Angelis, G. de France, D. Doherty, J. Gerl, R. Gernhäuser, D. Jenkins, A. Jungclaus, S. Koyama, T. Motobayashi, S. Nagamine, M. Niikura, A. Obertelli, D. Lubos, B. Rubio, E. Sahin, H. Sakurai, T. Saito, L. Sinclair, D. Steppenbeck, R. Taniuchi, V. Vaquero, R. Wadsworth, and M. Zielinska

U Tokyo, RIKEN, CEA Saclay, GSI, U Giessen, CCEN, U Valencia, U Bordeaux, INFN Padova, U York, INFN Legnaro, GANIL, TU München, CSIC Madrid, U Oslo, U Padova, UA Madrid, CNS Tokyo, NSCL, CSNSM, U Jyväskylä

## RIBF151

S.M. Lenzi, A. Poves, T. Hüyük, F. Browne, P. Doornenbal, T. Koiwai, T. Arici, M. Bentley, M. L. Cortés, N. Imai, A. Jungclaus, N. Kitamura, B. Longfellow, R. Lozeva, B. Mauss, D. Napoli, M. Niikura, X. Pereira-Lopez, F. Recchia, P. Ruotsalainen, R. Taniuchi, S. Uthayakumaar, V. Vaquero, R. Wadsworth, and R. Yajzey

Thank you for your attention

