

Charm Production & Life in Nuclear Matter

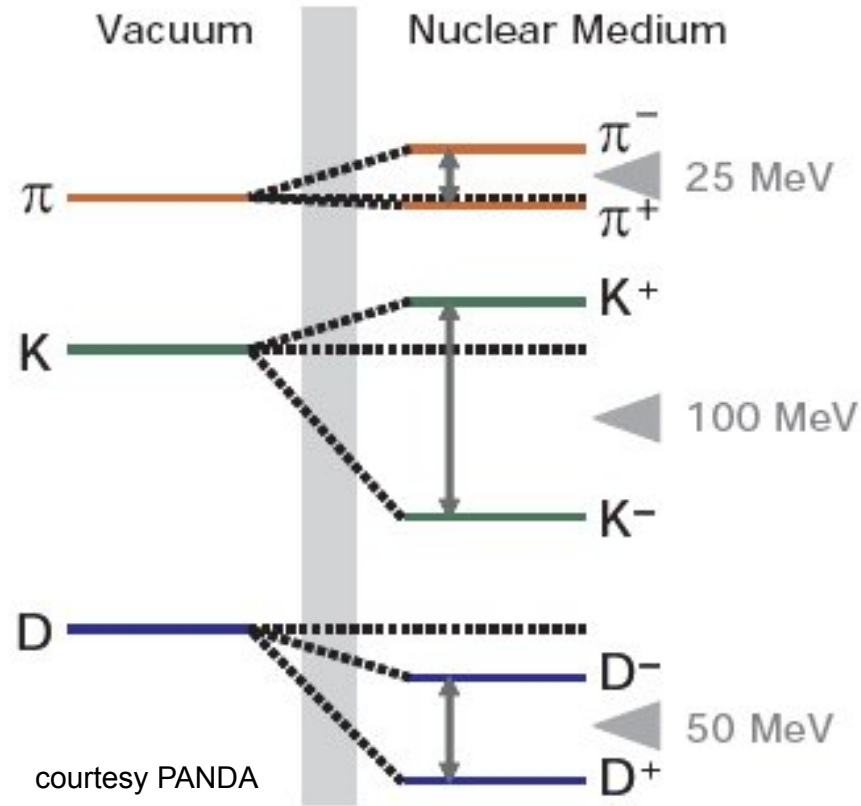
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Technische Universität Dresden

Mesons with Charm in Vakuum: Dyson-Schwinger—Bethe-Salpeter
Mesons with Charm in Medium: QCD Sum Rules
Hadrons with Charm: Production in $p \bar{p}$

dedicated research for PANDA & CBM (FAIR)

*) with T. Hilger, S. Leupold, S. Dorkin, L. Kaptari, H. Schade, A. Titov



pA:
 Scheinast et al.
 (KaoS), PRL 2006

pA: CBM, 2019
 p_bar A: PANDA, 2019

like Stark & Zeeman effects in QM:
 understanding hadronic part of QCD

Charming Mesons in Vacuum

Dyson-Schwinger – Bethe-Salpeter approach

Alkofer
Fischer
Krassnigg
Roberts
Tandy
...

guess for gluon propagator D

→ DS eq. for quark propagator (Euclidean, rainbow approx.):

$$S_q^{-1}(p) = i\gamma \cdot p + \tilde{m} + \frac{4}{3} \int \frac{d^4 l}{(2\pi)^4} [g^2 D(p-l)]_{\mu\nu} \gamma_\mu S_q(l) \gamma_\nu$$

BS eq. in rainbow-ladder approx. (Euclidean): $k_+ = k + \xi P, k_- = k + (\xi - 1)P$

$$\Gamma(P, p) = \left(-\frac{4}{3}\right) \int \frac{d^4 k}{(2\pi)^4} \gamma_\mu S(k_+) \Gamma(P, k) S(k_-) \gamma_\nu (g^2 D(p-k))_{\mu\nu}$$

↑ 4 x 4 matrix: tricky expansion → ang. integration:

$$g_i^k(p) = \int_0^\infty \frac{dk k^3}{4\pi^2} \sum A_{ij}^{km}(p, k) g_j^m(k) \rightarrow g = K g \rightarrow \det(K - 1) = 0: \text{bound states}$$

gluon propagator: ansatz

Roberts et al., Eur. Phys. J. ST 140 (2007) 53 (4.44)

$$g^2(k^2)D_{\mu\nu}(k^2) = \left(\underbrace{\frac{4\pi^2 D k^2}{\omega^2} e^{-k^2/\omega^2}}_{\text{IR}} + \underbrace{\frac{8\pi^2 \gamma_m F(k^2)}{\ln[\tau + (1 + \frac{k^2}{\Lambda_{QCD}^2})]}}_{\text{neglect}} \right) \left(\delta_{\mu\nu} - \frac{k_\mu k_\nu}{k^2} \right)$$

$$\omega = 0.5 \text{ GeV}$$

$$D = 16 \text{ GeV}^{-2}$$

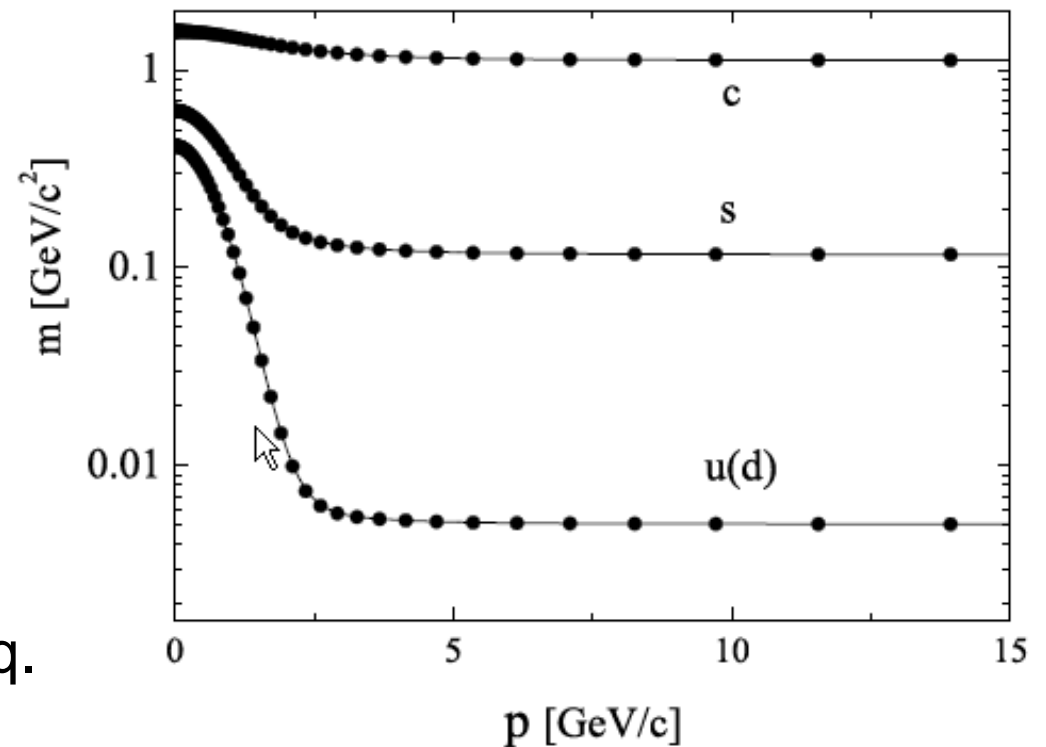
quark propagator:

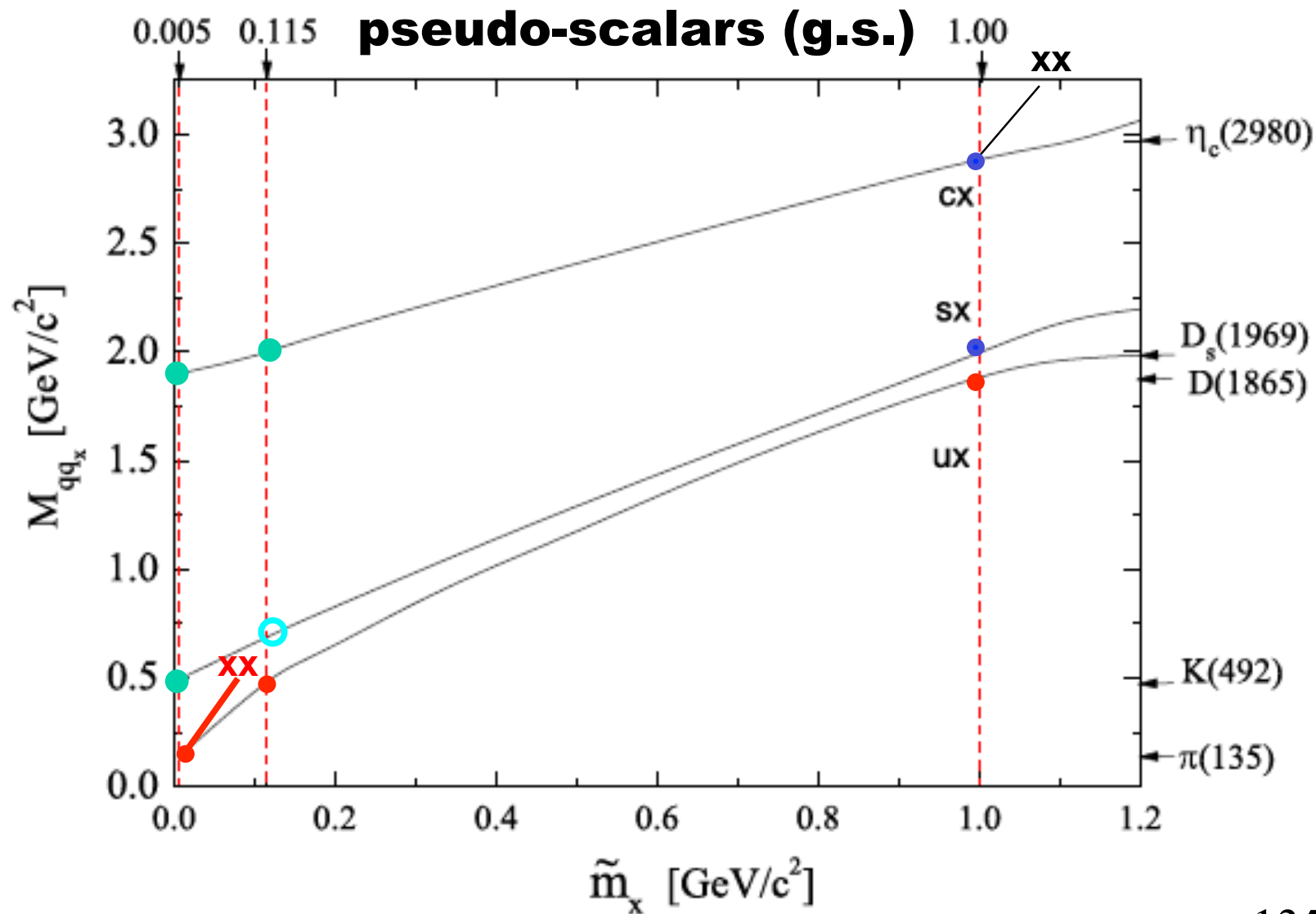
$$S_q^{-1}(p) = i\gamma \cdot p A(p) + B(p)$$

$$m(p) = B(p) / A(p)$$

$$\tilde{m} = m(p \rightarrow \infty)$$

→ input for Bethe-Salpeter eq.





pi: $m_u = 0.005$ GeV
 K: $m_s = 0.115$ GeV
 D: $m_c = 1.0$ GeV

135 MeV: pi
 497 MeV: K
 1870 MeV: D^\pm

 1970 MeV: $D^\pm s$
 2980 MeV: eta_c

under construction: scalar, vector, axial-vector channels

excited states: $\pi(1300) \sim 1080$ MeV,

non-zero T , μ : method = ?

Charming Mesons in Nuclear Matter

$$\Pi(q) = i \int d^4x e^{iqx} \langle\langle T [j(x)j^\dagger(0)] \rangle\rangle \quad \rightarrow \text{OPE: QCD condensates (T,n)}$$

$$\Pi(q) = \frac{1}{\pi} \int_{-\infty}^{+\infty} ds \frac{\Delta\Pi(s, |\vec{q}|)}{s - q_0} \quad \rightarrow \text{hadron spectral funct.}$$

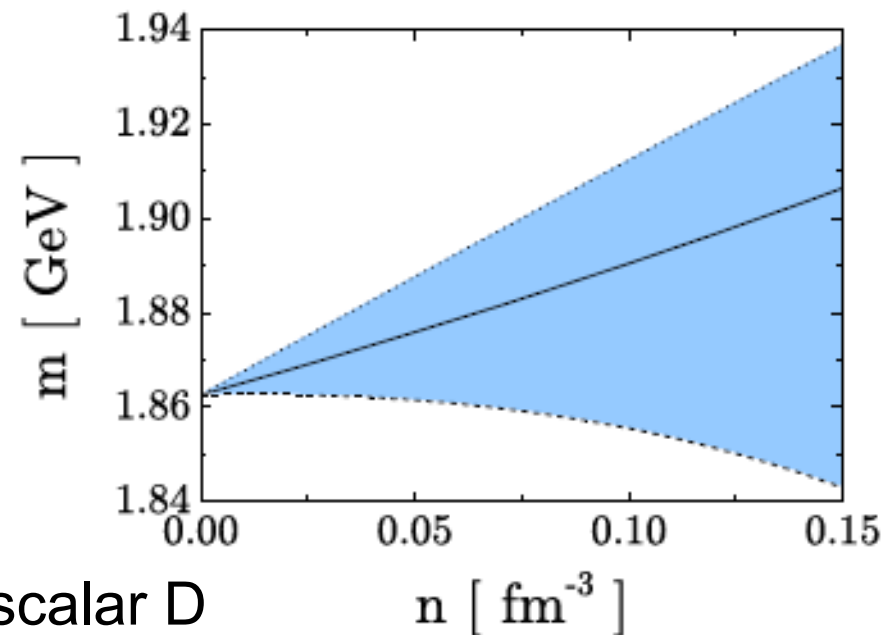
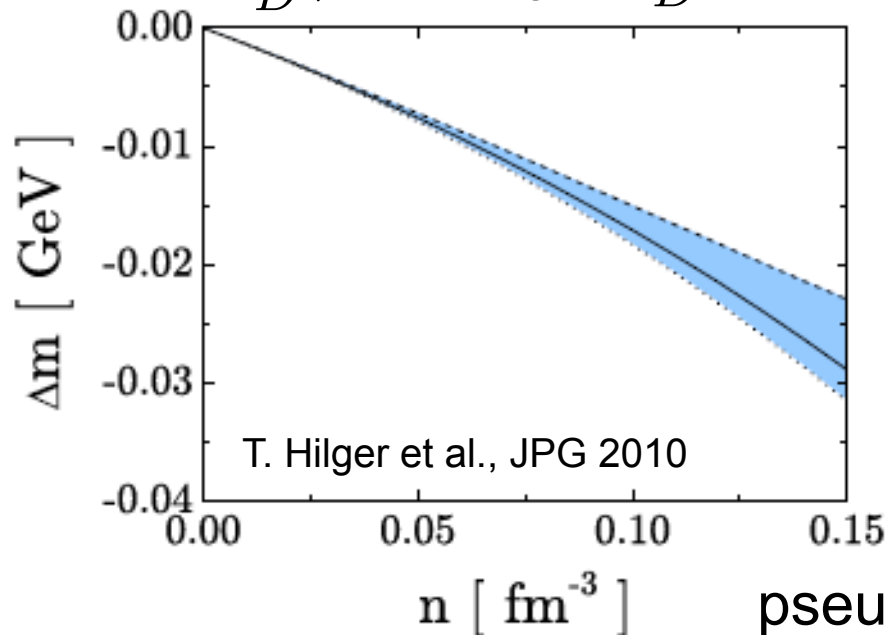
$$S_n(M) \equiv \int_{s_0^-}^{s_0^+} ds s^n \Delta\Pi(s) e^{-s^2/M^2}$$

$$\Delta m \equiv \frac{1}{2} \frac{S_1 S_2 - S_0 S_3}{S_1^2 - S_0 S_2},$$

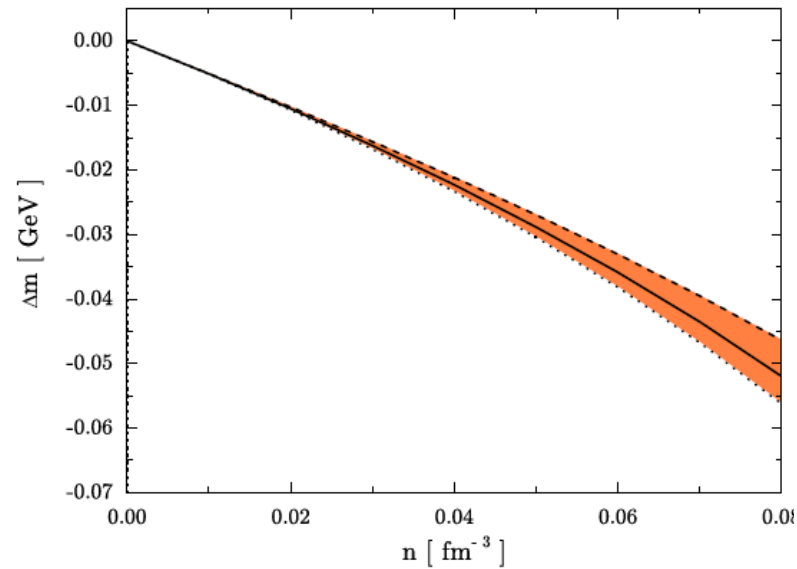
$$m_+ m_- \equiv -\frac{S_2^2 - S_1 S_3}{S_1^2 - S_0 S_2},$$

$$m^2 \equiv \Delta m^2 + m_+ m_-,$$

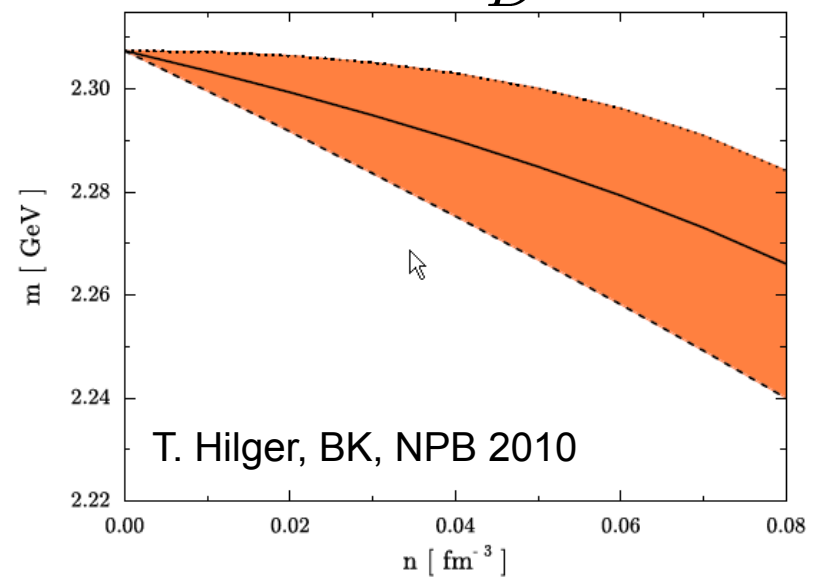
$$j_{D^+} = i\bar{d}\gamma_5 c, \quad j_{D^-} = i\bar{c}\gamma_5 d$$



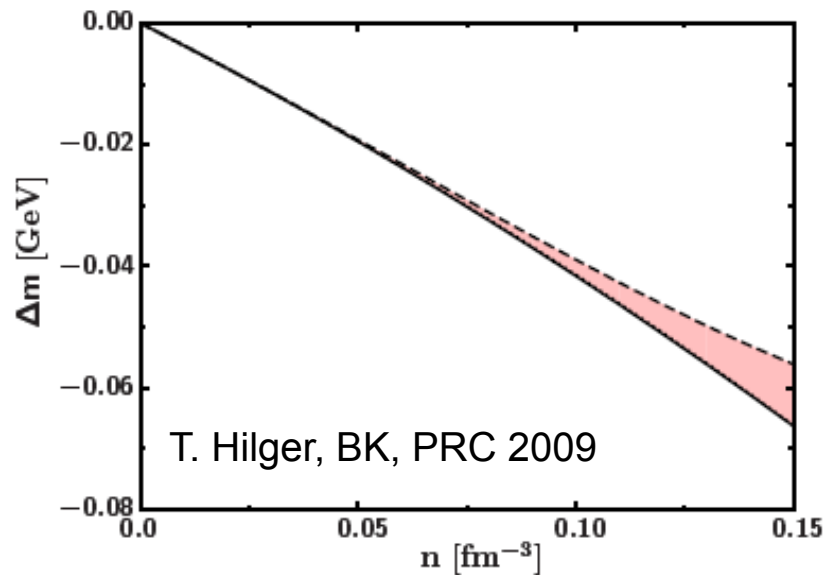
scalar $D^* - \bar{D}^*$



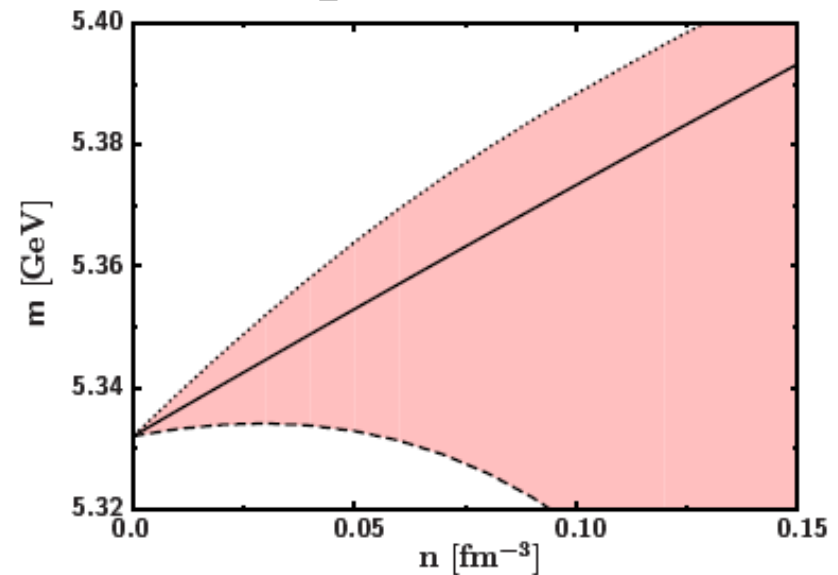
$j_{D^*} = \bar{d}c, j_{\bar{D}^*} = \bar{c}d$



pseudo-scalar $B - \bar{B}$



$j_{B^+} = i\bar{b}\gamma_5u, j_{B^0} = i\bar{b}\gamma_5d$



condensate	vacuum value $\langle \dots \rangle_{vac}$	density dependent part $\langle \dots \rangle_{med}$
$\langle \bar{q}q \rangle$	$(-0.245 \text{ GeV})^3$	$45/11 n$
$\langle \frac{\alpha_s}{\pi} G^2 \rangle$	$(0.33 \text{ GeV})^4$	$-0.65 \text{ GeV } n$
$\langle \bar{q}g\sigma\mathcal{G}q \rangle$	$0.8 \text{ GeV}^2 \times (-0.245 \text{ GeV})^3$	$3 n \text{ GeV}^2$
$\langle q^\dagger q \rangle$	0	$1.5 n$
$\langle \frac{\alpha_s}{\pi} \left(\frac{(vG)^2}{v^2} - \frac{G^2}{4} \right) \rangle$	0	$-0.05 \text{ GeV } n$
$\langle q^\dagger iD_0 q \rangle$	0	$0.18 \text{ GeV } n$
$\langle \bar{q} [D_0^2 - \frac{1}{8}g\sigma\mathcal{G}] q \rangle$	0	$-0.3 \text{ GeV}^2 n$
$\langle q^\dagger D_0^2 q \rangle$	0	$-0.0035 \text{ GeV}^2 n$
$\langle q^\dagger g\sigma\mathcal{G}q \rangle$	0	$0.33 \text{ GeV}^2 n$

Weinberg type sum rules for chiral partners of heavy-light mesons

$$m_c \quad m_q \rightarrow 0$$

$$\frac{1}{\pi} \int_{-\infty}^{+\infty} d\omega \omega \Delta\Pi_{P-S}(\omega) = -2m_c \langle \bar{q}q \rangle ,$$

$$\frac{1}{\pi} \int_{-\infty}^{+\infty} d\omega \omega^3 \Delta\Pi_{P-S}(\omega) = -2m_c^3 \langle \bar{q}q \rangle + m_c \langle \bar{q}g\sigma\mathcal{G}q \rangle - m_c \langle \Delta \rangle$$

$$\frac{1}{\pi} \int_{-\infty}^{+\infty} d\omega \omega^5 \Delta\Pi_{P-S}(\omega) = -2m_c^5 \langle \bar{q}q \rangle + 3m_c^3 \langle \bar{q}g\sigma\mathcal{G}q \rangle - 3m_c^3 \langle \Delta \rangle + \dots$$

$$\frac{1}{\pi} \int_{-\infty}^{+\infty} d\omega \omega \Delta\Pi_{V-A}(\omega) = 8m_c \langle \bar{q}q \rangle , \quad \langle \bar{q}g\sigma\mathcal{G}q \rangle - 8\langle \bar{q}D_0^2q \rangle \equiv \langle \Delta \rangle$$

$$\frac{1}{\pi} \int_{-\infty}^{+\infty} d\omega \omega^3 \Delta\Pi_{V-A}(\omega) = 8m_c^3 \langle \bar{q}q \rangle + 4m_c \langle \Delta \rangle$$

↑
zero in vacuum

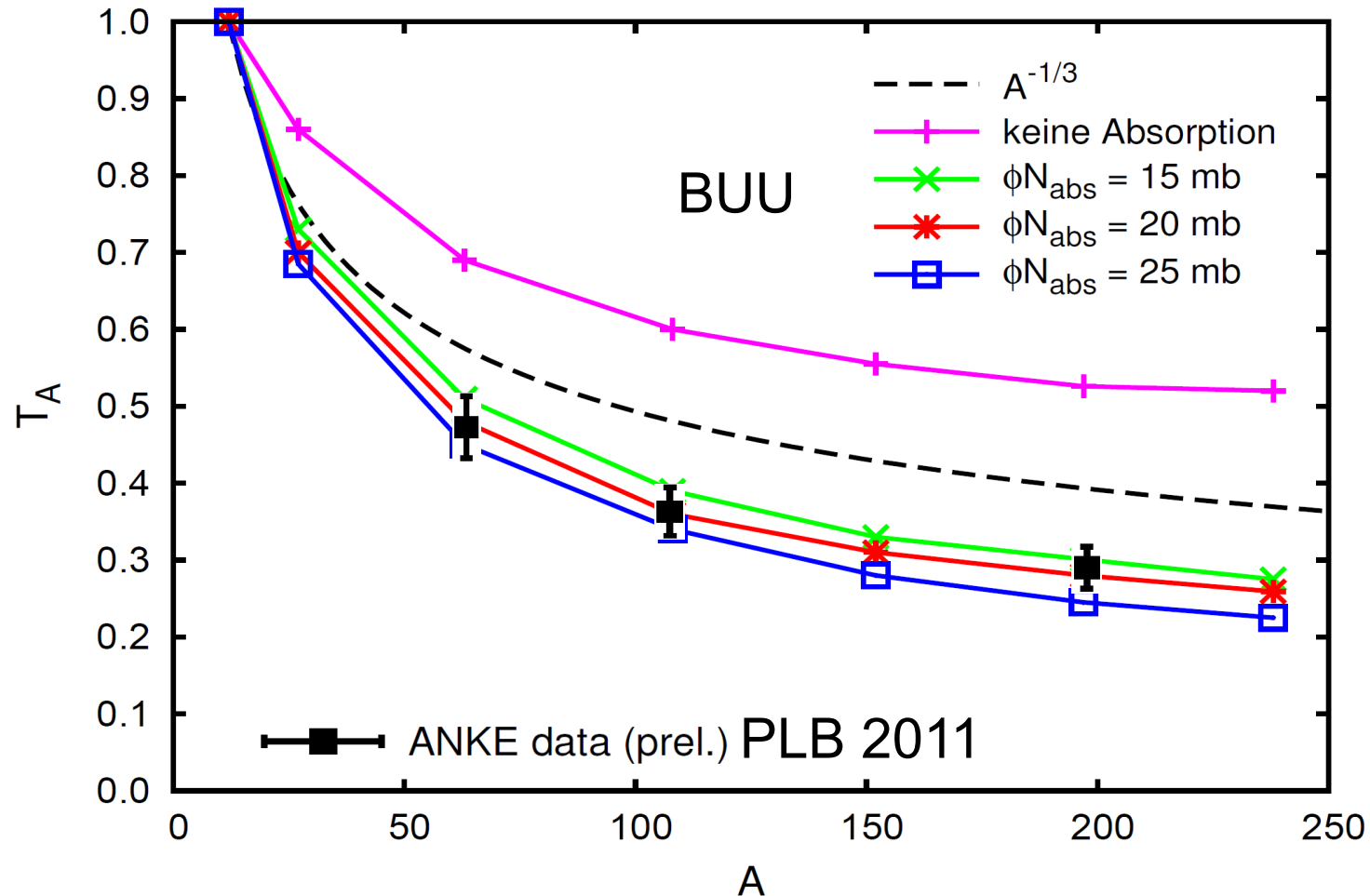
$$\frac{1}{\pi} \int_{-\infty}^{+\infty} d\omega \omega^5 \Delta\Pi_{V-A}(\omega) = 8m_c^5 \langle \bar{q}q \rangle - 4m_c^3 \langle \bar{q}g\sigma\mathcal{G}q \rangle - 12m_c^3 \langle \Delta \rangle + \dots$$

heavy-quark symmetry: $\Pi_{(1)} = \frac{1}{3} \left(\frac{q^\mu q^\nu}{q^2} - g^{\mu\nu} \right) \Pi_{\mu\nu}$

l.o. in $|q^2|/m_c \ll 1$: $\Pi_{(1)}^{V-A} = \Pi^{P-S} = \frac{-2}{m_c} \langle \bar{q}q \rangle$

Aside: Width of Strangeonium

$pA \rightarrow X\phi$: Transparency Ratio $T_A = \frac{\sigma_{pA \rightarrow \phi X}}{A} \frac{C}{\sigma_{pC \rightarrow \phi X}}$
 \searrow
 $K^+ K^-$



$\Gamma_\phi = 45 - 73 \text{ MeV}$ in Valencia – Paryev models

Glauber eikonal type approach

p = projectile

$$\sigma_{pA \rightarrow \phi X} = \sigma_{pN \rightarrow \phi X} \int d^2b \int_{-\sqrt{R^2-b^2}}^{\sqrt{R^2-b^2}} dz n(\vec{b}, z)$$

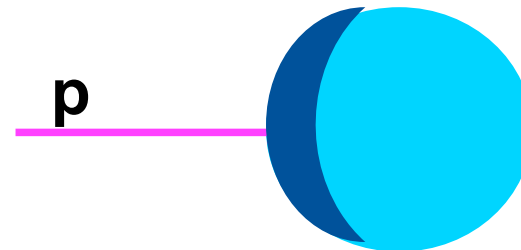
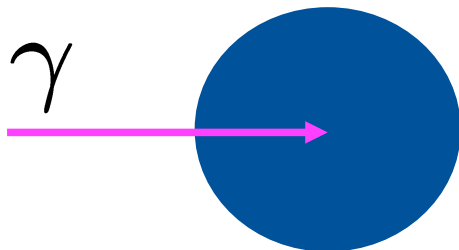
$c\bar{c}$

$$\times \exp \left\{ -\sigma_{pN}^{\text{tot}} \int_{-\sqrt{R^2-b^2}}^z dz' n(\vec{b}, z') - \sigma_{\phi N}^{\text{tot}} \int_z^{\sqrt{R^2-b^2}} dz' n(\vec{b}, z') \right\}$$

abs

attenuation of projectile **absorption of ejectile**

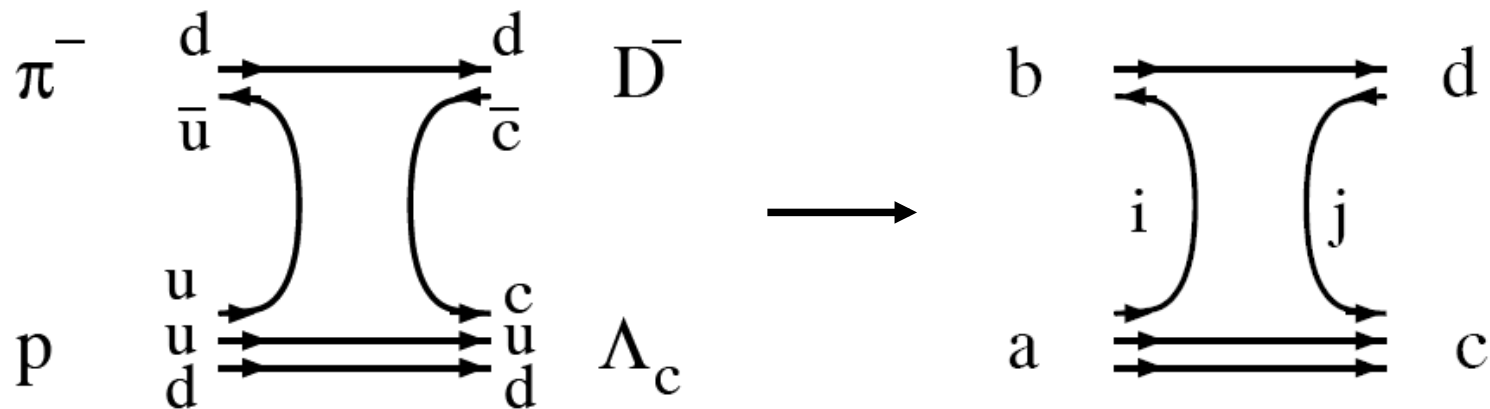
photo (electro) production: „illumination“ of whole nucleus
 proton (p_bar) induced production: „illumination“ of front side



Exclusive Associate Charm Production in $p \bar{p}$ *

Regge approach à la Kaidalov et al.

peripheral collisions: small momentum transfer/forward angles



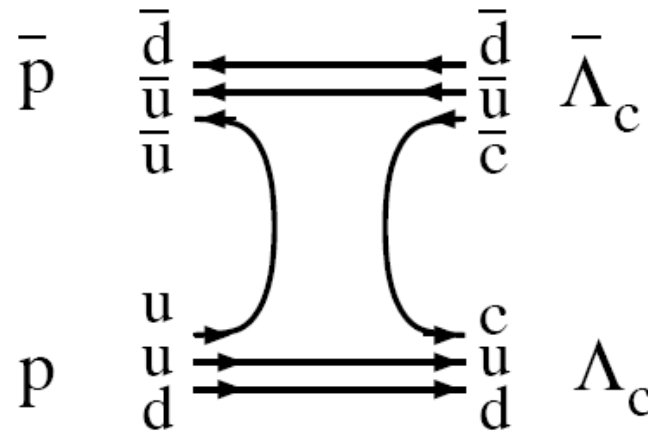
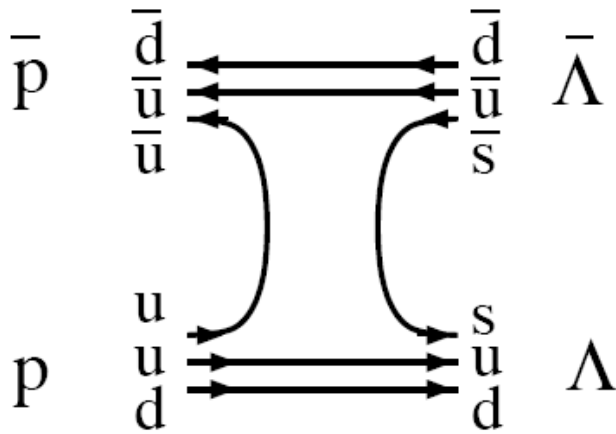
consistency of $a b \rightarrow a b, c d \rightarrow c d$

$$\left| \begin{array}{ccc} b & \rightarrow & d \\ \text{ } & \text{ } & \text{ } \\ a & \rightarrow & c \end{array} \right|^2 \rightarrow \begin{array}{ccc} b & \rightarrow & b \\ \text{ } & \text{ } & \text{ } \\ a & \rightarrow & a \end{array} \otimes \begin{array}{ccc} d & \rightarrow & d \\ \text{ } & \text{ } & \text{ } \\ c & \rightarrow & c \end{array}$$

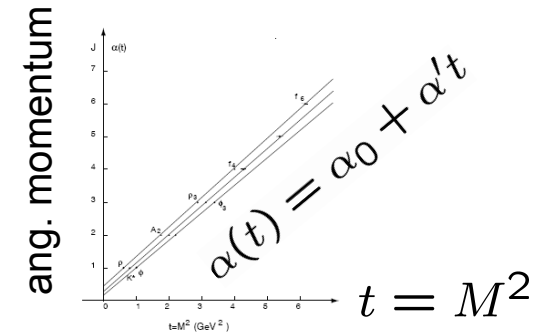
shopping list: $\bar{p}p \rightarrow \bar{\Lambda}\Lambda, \bar{\Lambda}_c\Lambda_c, \bar{K}K, \bar{D}D, \bar{D}D^* \dots$

*) work by A.I. Titov: Open Charm Physics at PANDA, Mainz, Oct. 19-20, 2009

Baryon Pairs in Exit Channel



cross section:
$$\frac{d\sigma}{dt} = \frac{1}{16\pi(s - 4M_N^2)^2} |T_{fi}|^2$$



Regge pole amplitude with K^* dominance:

$$T_{m_f n_f; m_i, n_i}^{\bar{p}p \rightarrow \bar{\Lambda}\Lambda} = \underbrace{C(t)}_{\text{fit (universal)}} \underbrace{\mathcal{M}_{m_f n_f; m_i, n_i}^{\bar{p}p \rightarrow \bar{\Lambda}\Lambda}(s, t)}_{\text{spin}} \frac{g_{K^* N \Lambda}^2}{s_0} \Gamma(1 - \alpha_{\bar{s}q}(t)) \left(-\frac{s}{s_{\bar{p}p: \bar{\Lambda}\Lambda}} \right)^{\alpha_{\bar{s}q}(t) - 1}$$

\uparrow
 s_0
 1 GeV

K^* trajectory
 $\alpha_{\bar{s}q}(t) - 1$

$$\alpha(t) = \alpha(0) + \gamma(\sqrt{T} - \sqrt{T-t})$$

additivity:

$$-t \ll T: \quad \alpha(t) = \alpha(0) + \alpha' t, \quad \alpha' = \gamma/2\sqrt{T}. \quad 2\alpha_{\bar{s}q}(0) = \alpha_{\bar{q}q}(0) + \alpha_{\bar{s}s}(0) \quad (1)$$

$$2/\alpha'_{\bar{s}q} = 1/\alpha'_{\bar{q}q} + 1/\alpha'_{\bar{s}s} \quad (2)$$

$$\sqrt{T_\rho} = 2.46 \text{ GeV}, \quad \alpha'_\rho \simeq 0.742 \text{ GeV}^{-2},$$

ρ ϕ

$$\sqrt{T_{K^*}} = 2.58 \text{ GeV}, \quad \alpha'_{K^*} \simeq 0.71 \text{ GeV}^{-2}$$

$$w_{ab \rightarrow cd}^2 \simeq w_{ab \rightarrow ab} \times w_{cd \rightarrow cd}$$

$$\sqrt{T_\phi} \simeq 2.70 \text{ GeV}, \quad \alpha'_\phi \simeq 0.676 \text{ GeV}^{-2},$$

diagonal transitions $\bar{p}p \rightarrow \bar{p}p$, ($s_{\bar{p}p}$) and $\bar{\Lambda}\Lambda \rightarrow \bar{\Lambda}\Lambda$, ($s_{\bar{\Lambda}\Lambda}$):

$$(s_{\bar{p}p:\bar{\Lambda}\Lambda})^{2(\alpha_{K^*}(0)-1)} = (s_{\bar{p}p})^{\alpha_\rho(0)-1} \times (s_{\bar{\Lambda}\Lambda})^{\alpha_\phi(0)-1} \quad (3)$$

$$s_{ab} = \left(\sum_i^{n_a} M_{i\perp} \right) \left(\sum_j^{n_b} M_{j\perp} \right)$$

$$M_{q\perp} \simeq 0.5 \text{ GeV}, \quad M_{s\perp} \simeq 0.6 \text{ GeV}, \quad \text{and} \quad M_{c\perp} \simeq 1.6 \text{ GeV}$$

spin amplitude: $\mathcal{M}_{m_f n_f; m_i n_i}^{\bar{p}p \rightarrow \bar{\Lambda} \Lambda}(s, t) = \mathcal{N}(s, t) \Gamma_{m_f m_i}^{(p)\mu} \Gamma_{n_f n_i}^{(\bar{p})\nu} \left(-g_{\mu\nu} + \frac{q_\mu q_\nu}{q^2} \right)$

from $\mathcal{L}_{K^*NY} = -\bar{Y} \left(\gamma_\mu - \frac{\kappa_{K^*NY}}{M_N + M_Y} \sigma_{\mu\nu} \right) N \partial^\nu K^{*\mu} + \text{h.c.}$

$$\Gamma_\mu^{(p)} \equiv \bar{u}_\Lambda \left((1 + \kappa_{K^*N\Lambda}) \gamma_\mu - \kappa_{K^*N\Lambda} \frac{(p_p + p_\Lambda)_\mu}{M_N + M_\Lambda} \right) u_p$$

$$\Gamma_\mu^{(\bar{p})} = \bar{v}_{\bar{p}} \left((1 + \kappa_{K^*N\Lambda}) \gamma_\mu + \kappa_{K^*N\Lambda} \frac{(p_{\bar{p}} + p_{\bar{\Lambda}})_\mu}{M_N + M_\Lambda} \right) v_{\bar{\Lambda}}$$

$$\mathcal{N}(s, t) = \frac{F_\infty(s)}{F(s, t)}, \quad F_\infty(s) = 2s,$$

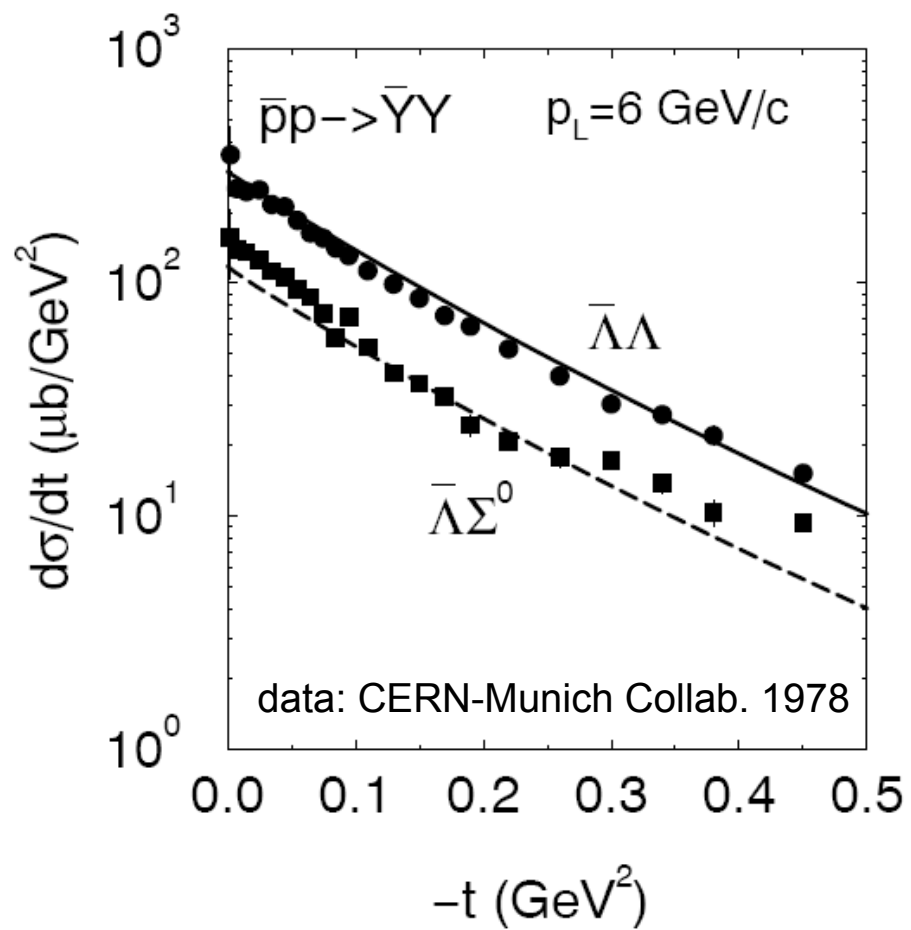
$$F^2(s, t) = \text{Tr} \left(\Gamma^{(p)\mu} \Gamma^{(p)\mu'\dagger} \right) \text{Tr} \left(\Gamma^{(\bar{p})\nu} \Gamma^{(\bar{p})\nu'\dagger} \right) \left(g_{\mu\nu} - \frac{q_\mu q_\nu}{q^2} \right) \left(g_{\mu'\nu'} - \frac{q_{\mu'} q_{\nu'}}{q^2} \right)$$

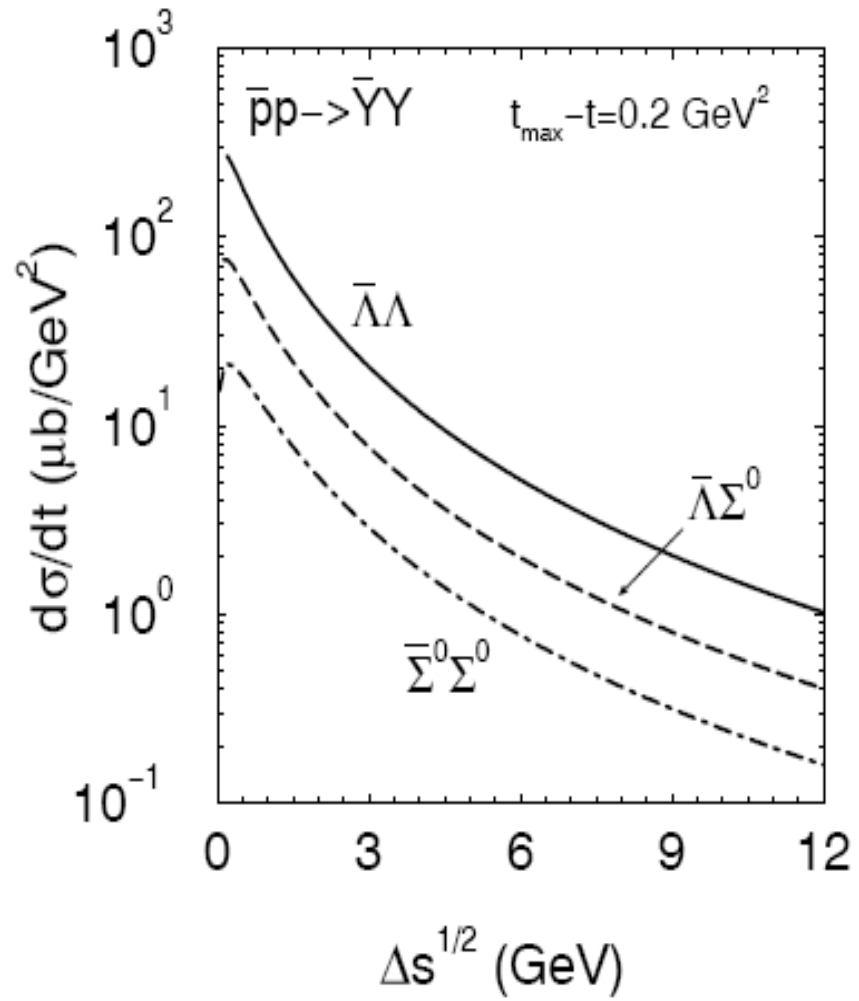
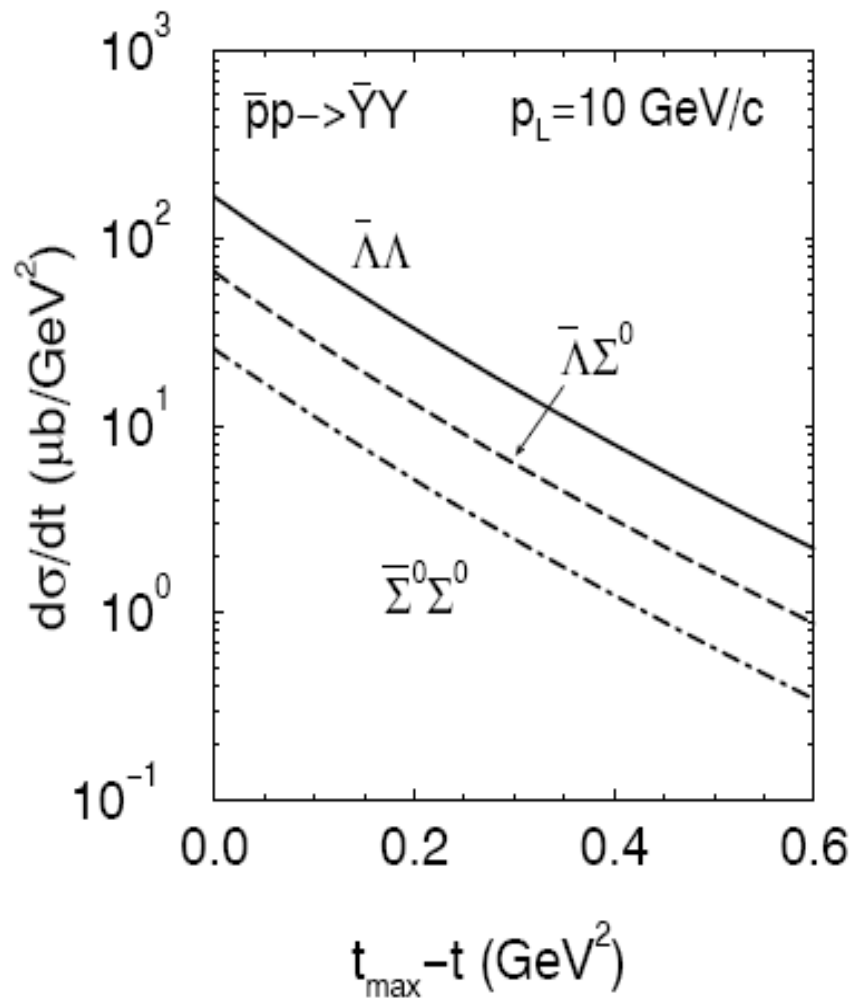
Nijmegen pot.:

$$g_{K^*NY} = -5.18, \kappa_{K^*NY} = 2.79 : Y = \Lambda$$

$$g_{K^*NY} = -3.29, \kappa_{K^*NY} = -0.91 : Y = \Sigma$$

fit:
$$C(t) = \frac{0.37}{(1 - t/1.15)^2}$$





$$\Lambda \rightarrow \Lambda_c^+ \equiv \Lambda_c$$

$$\Sigma^0 \rightarrow \Sigma_c^+ \equiv \Sigma_c$$

$$K^* \rightarrow \bar{D}^*$$

$$\alpha_\phi \rightarrow \alpha_{J/\psi}$$

$$\alpha_{D^*}^I(0) = -1.02, \quad \sqrt{T_{D^*}} = 3.91 \text{ GeV}, \quad \alpha'_{D^*} \simeq 0.467 \text{ GeV}^{-2}$$

$$\alpha_{J/\psi}(0) = -2.60, \quad \sqrt{T_{J/\psi}} \simeq 5.36 \text{ GeV}, \quad \alpha'_{J/\psi} \simeq 0.34 \text{ GeV}^{-2}$$

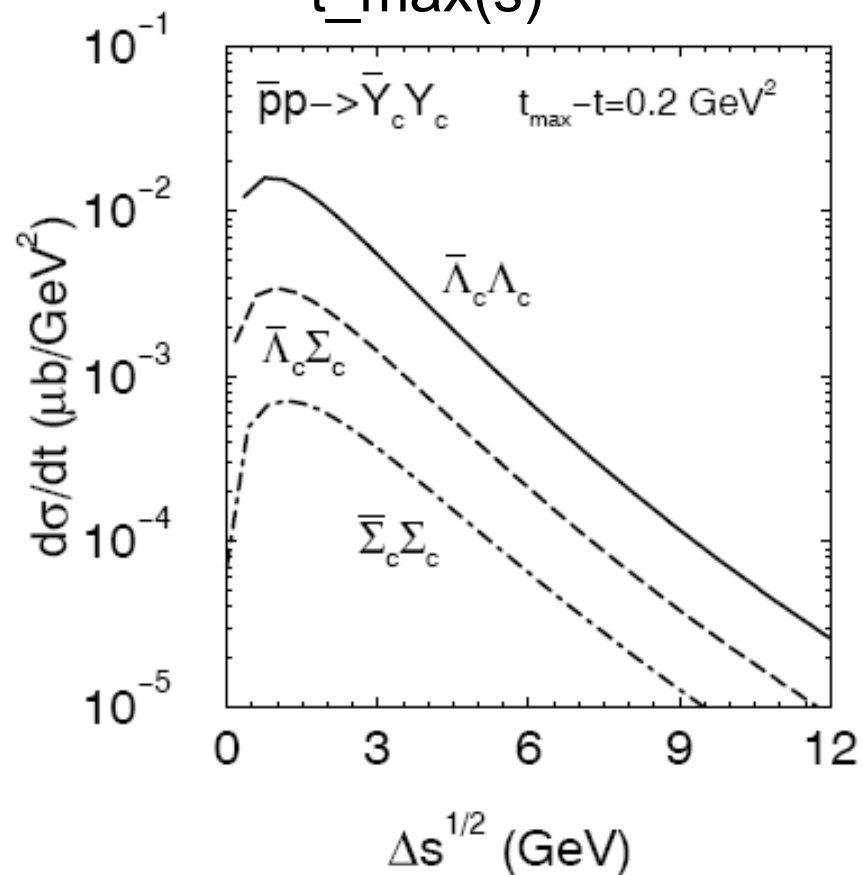
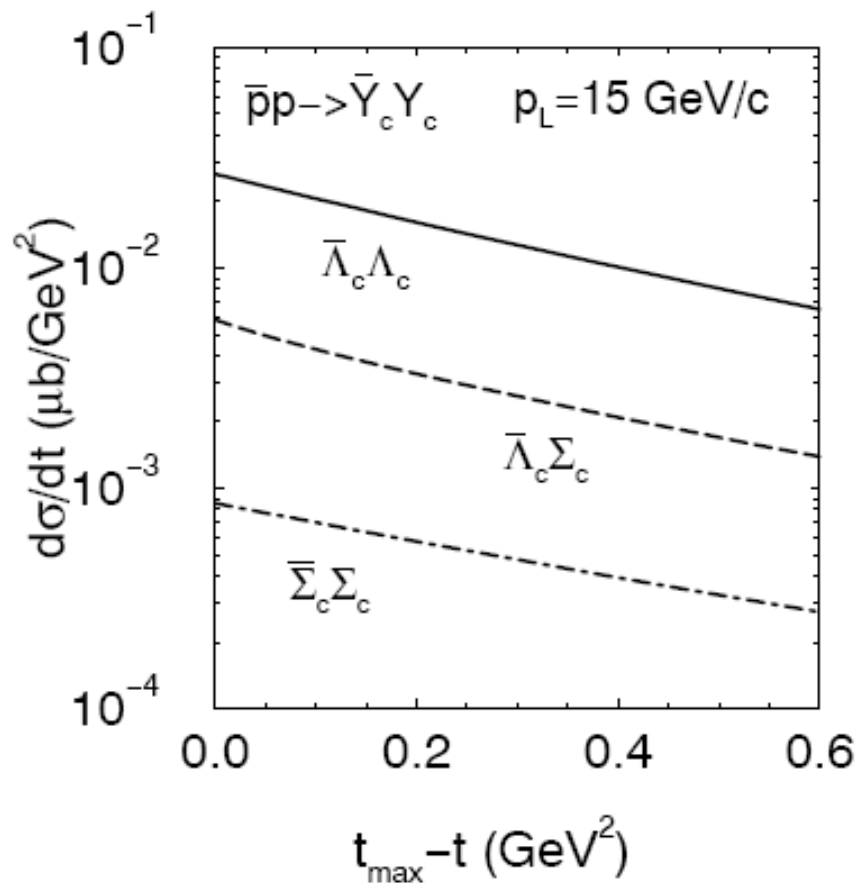
$$s_{\bar{p}p:\bar{\Lambda}_c\Lambda_c} \simeq 5.98 \text{ GeV}^2.$$

SU(4) symmetry: $g_{DNY_c} = g_{KNY}$

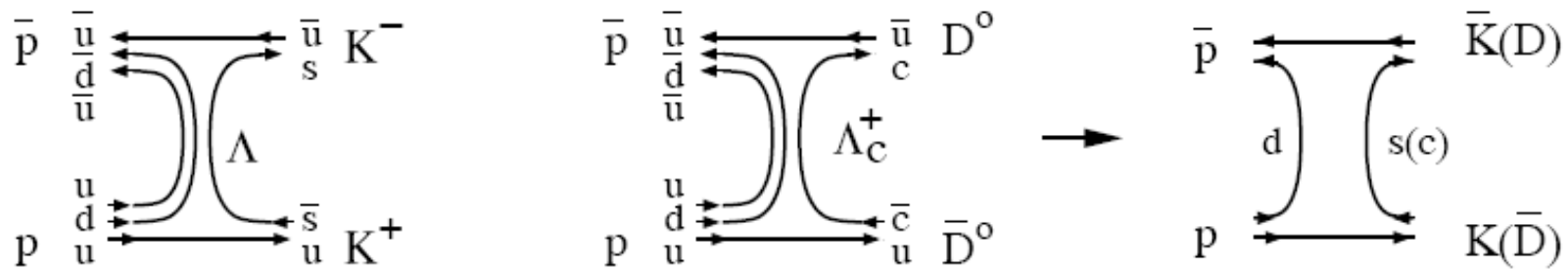
$$g_{D^*NY_c} = g_{K^*NY}$$

bumpy structure:

$t_{\text{max}}(\text{s})$



Meson Pairs in Exit Channel



Λ exchange:

$$T_{m_i, n_i}^{\bar{p}p \rightarrow K^- K^+} = C'(t) \mathcal{M}_{m_i, n_i}^{\bar{p}p \rightarrow K^- K^+}(s, t) \frac{g_{KN\Lambda}^2}{s_0} \Gamma\left(\frac{1}{2} - \alpha_{ds}(t)\right) \left(-\frac{s}{s_{\bar{p}p:KK}}\right)^{\alpha_{ds}(t) - \frac{1}{2}}$$

$$(1) \quad 2\alpha_{ds}(0) = \alpha_{\bar{d}d}(0) + \alpha_{\bar{s}s}(0)$$

$$(2) \quad 2/\alpha'_{ds} = 1/\alpha'_{\bar{d}d} + 1/\alpha'_{\bar{s}s} .$$

$$\alpha_{ds} = \alpha_{\Lambda} = -0.65 + 0.94t$$

$$\alpha_{\bar{d}d}(t) = -1.58 + \alpha'_{\bar{d}d} t \quad \text{with } \alpha'_{\bar{d}d} = 1.542 \text{ GeV}^{-2}$$

$$(3) \quad (s_{\bar{p}p:KK})^{2(\alpha_{ds}(0) - \frac{1}{2})} = (s_{\bar{p}p})^{\alpha_{\bar{d}d}(0)} \times (s_{KK})^{\alpha_{\bar{s}s}(0) - 1} \quad s_{KK} = 1.21 \text{ GeV}^2 \text{ and } s_{\bar{p}p} = 2.25 \text{ GeV}^2$$

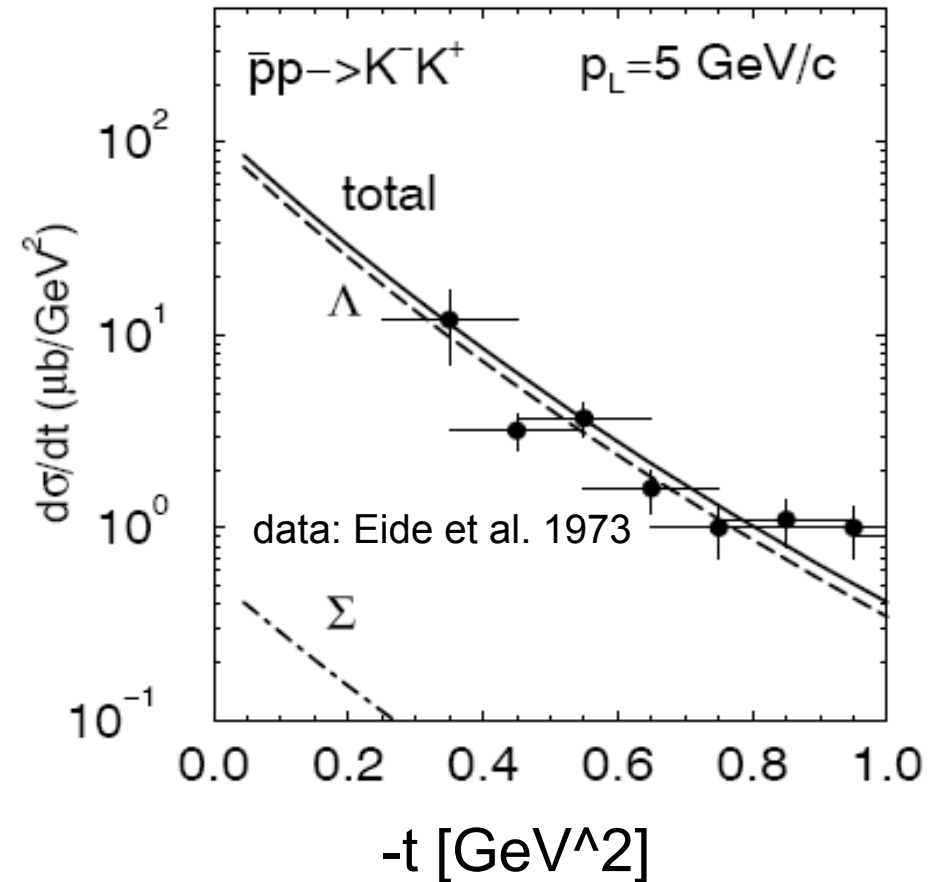
$$\mathcal{M}_{m_i n_i}^{\bar{p}p \rightarrow \bar{K}K}(s, t) = \mathcal{N}(s, t) [\bar{v}_{n_i} (\not{p}_Y - M_Y) u_{m_i}] ,$$

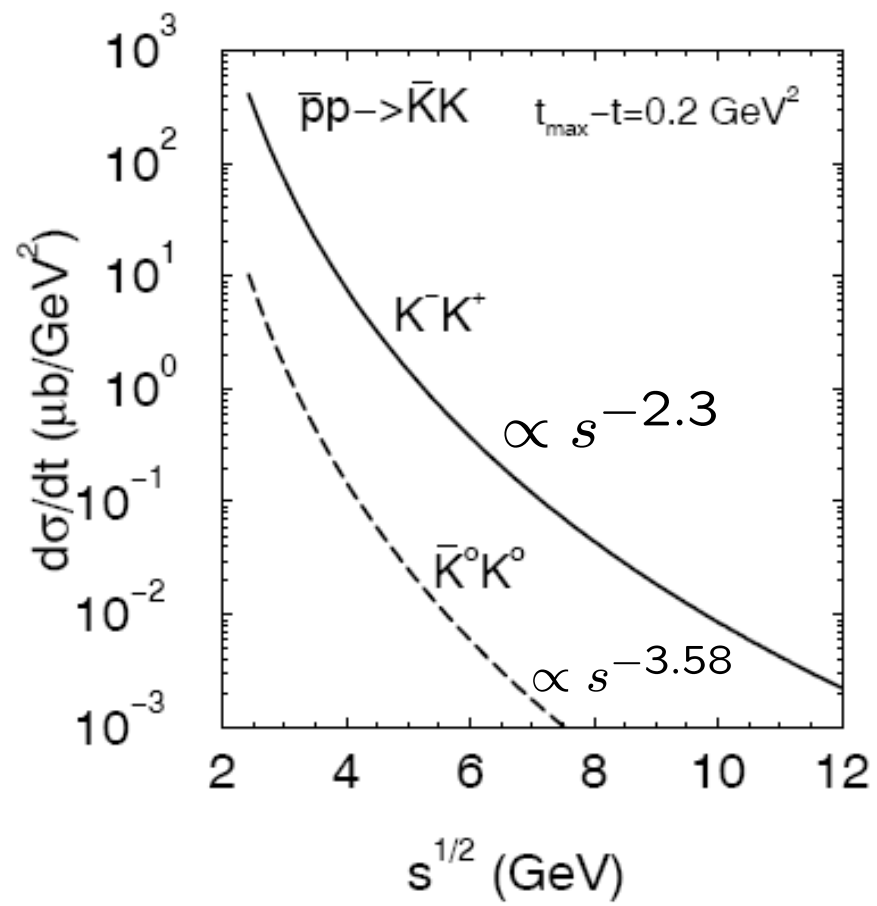
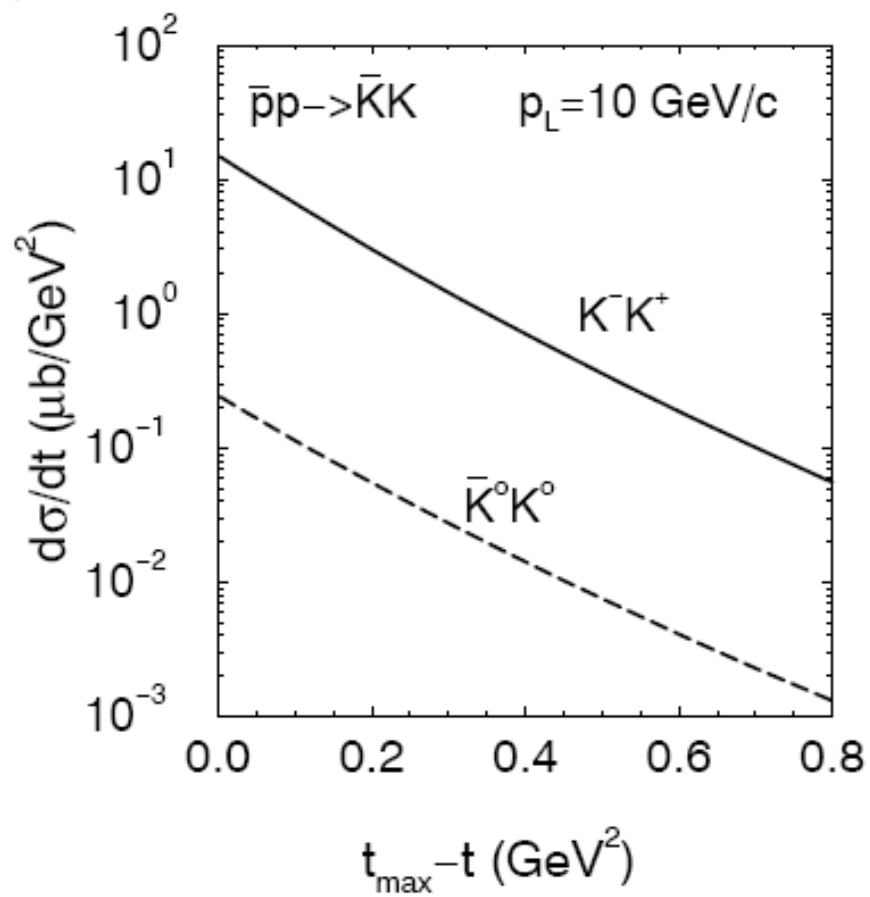
$$\mathcal{N}(s, t) = \frac{F_\infty(s)}{F(s, t)}, \quad F_\infty^2(s) = s M_Y^2 / 2 ,$$

$$F^2(s, t) = \frac{1}{2} ((s - 2M_N^2)(M_Y^2 - t) + 4M_N M_Y (M_N^2 + M_K^2 + t) - (M_N^2 - M_K^2 + t)^2 - M_N^2 (M_Y^2 + t)) ,$$

from $\mathcal{L}_{NYK} = -i\bar{N} \gamma_5 Y K + \text{h.c.}$

$$\text{fit: } C'(t) = \frac{0.51}{(1 - t/1.15)^2}$$





$$\Lambda \rightarrow \Lambda_c^+ \equiv \Lambda_c$$

$$\Sigma^0 \rightarrow \Sigma_c^+$$

$$\Sigma^+ \rightarrow \Sigma_c^{++}$$

$$K^+ \rightarrow \bar{D}^0$$

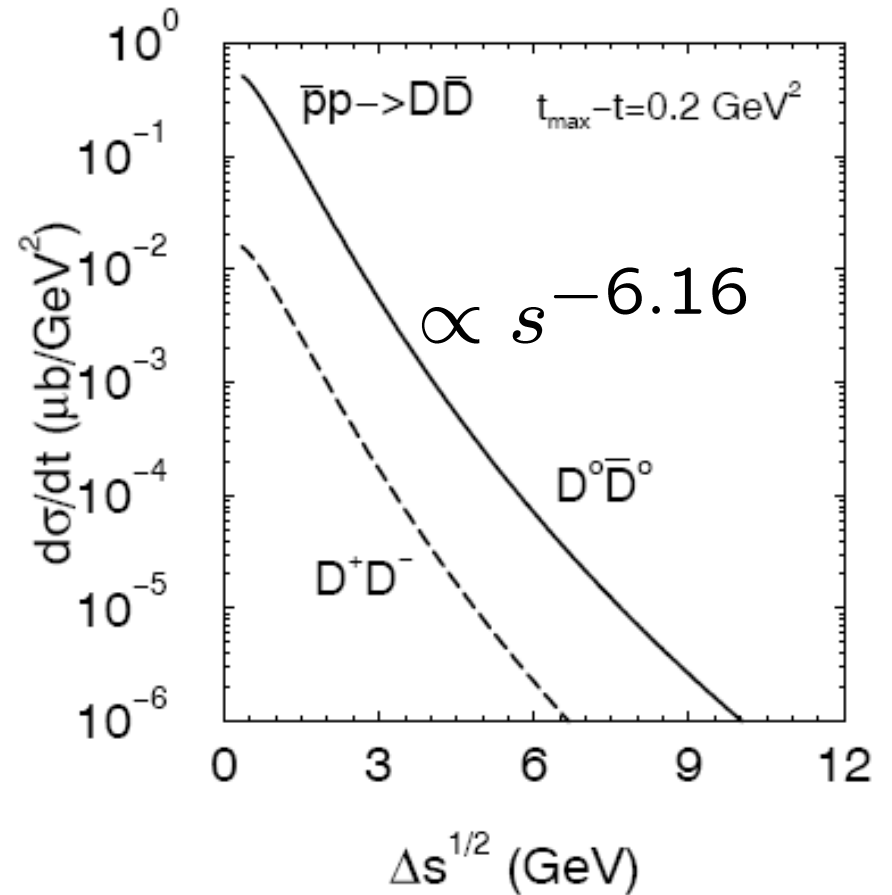
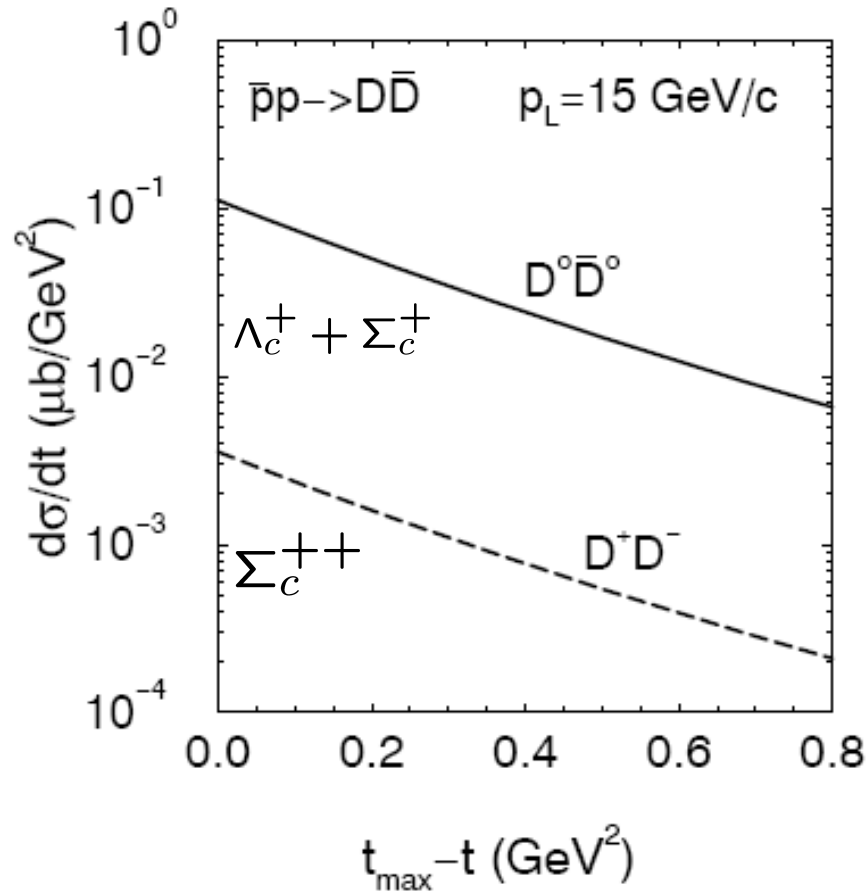
$$\bar{K}^0 \rightarrow D^+$$

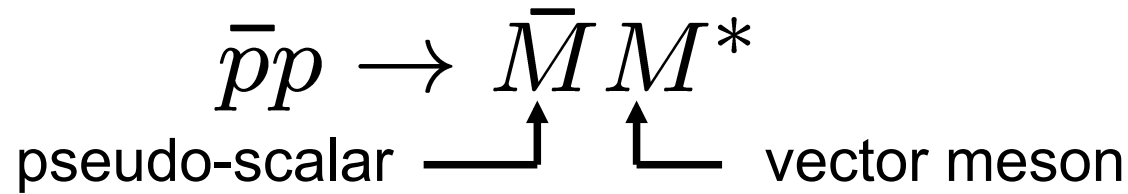
$$2\alpha_{dc}(0) = \alpha_{\bar{d}d}(0) + \alpha_{\bar{c}c}(0)$$

$$2/\alpha'_{dc} = 1/\alpha'_{\bar{d}d} + 1/\alpha'_{\bar{c}c},$$

$$\alpha'_{dc}(0) \simeq -2.09, \quad \alpha'_{dc} \simeq 0.557 \text{ GeV}^{-2}$$

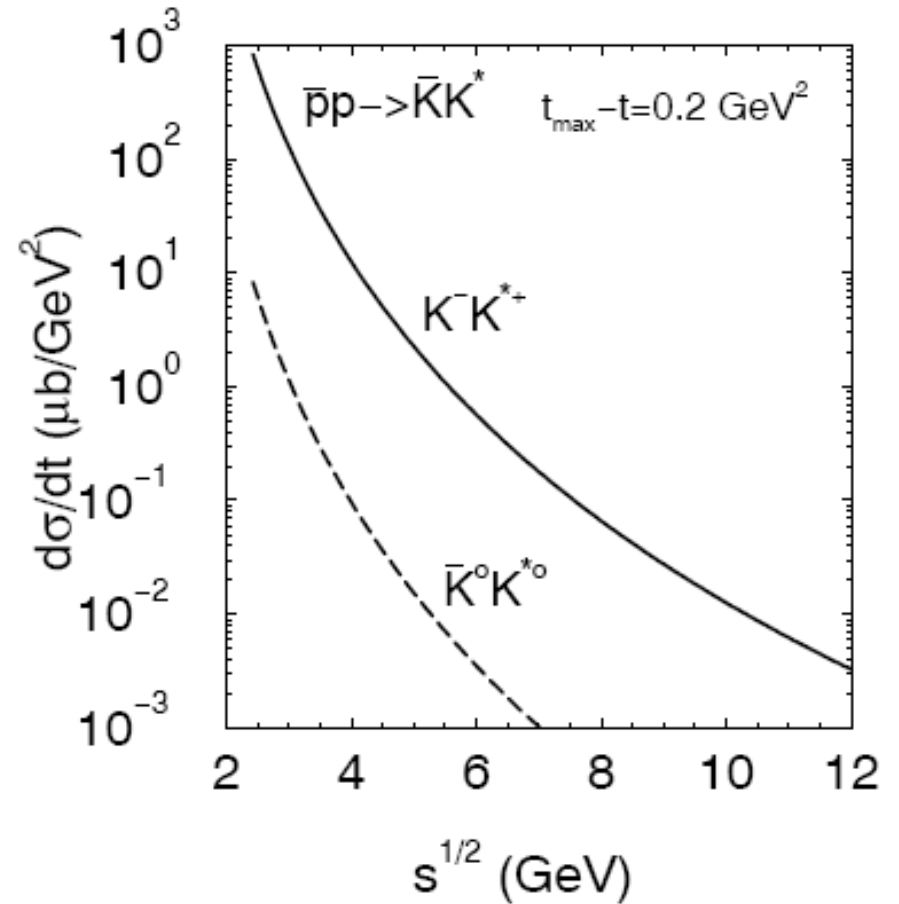
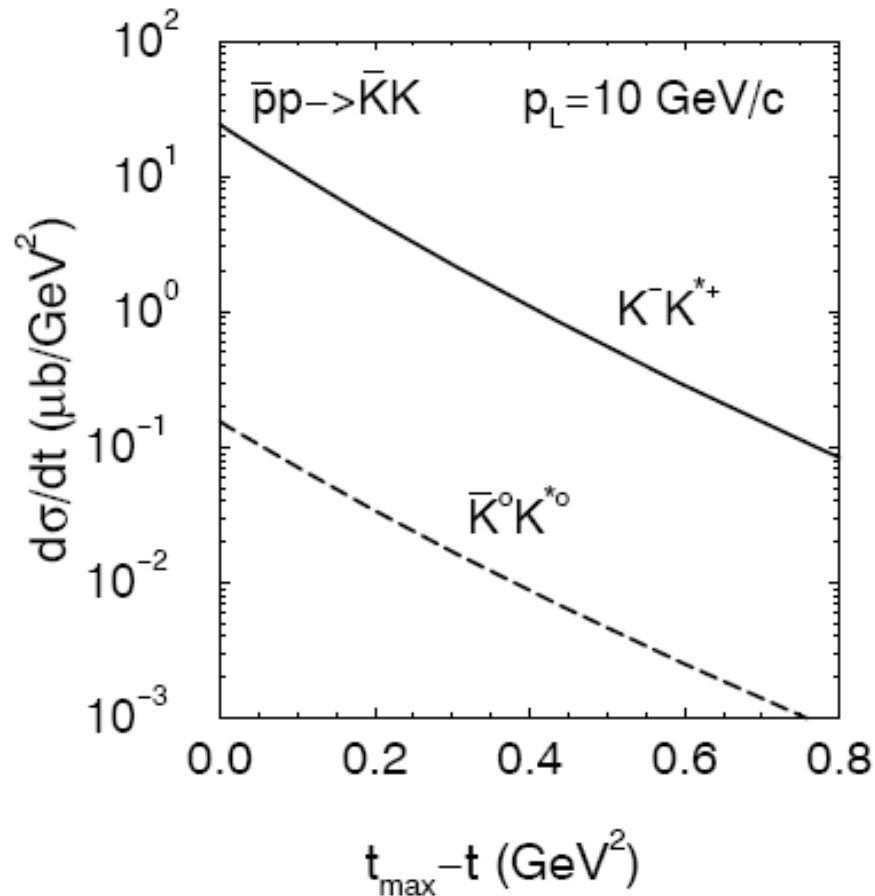
$$s_{\bar{p}p:D\bar{D}} \simeq 3.59 \text{ GeV}^2.$$

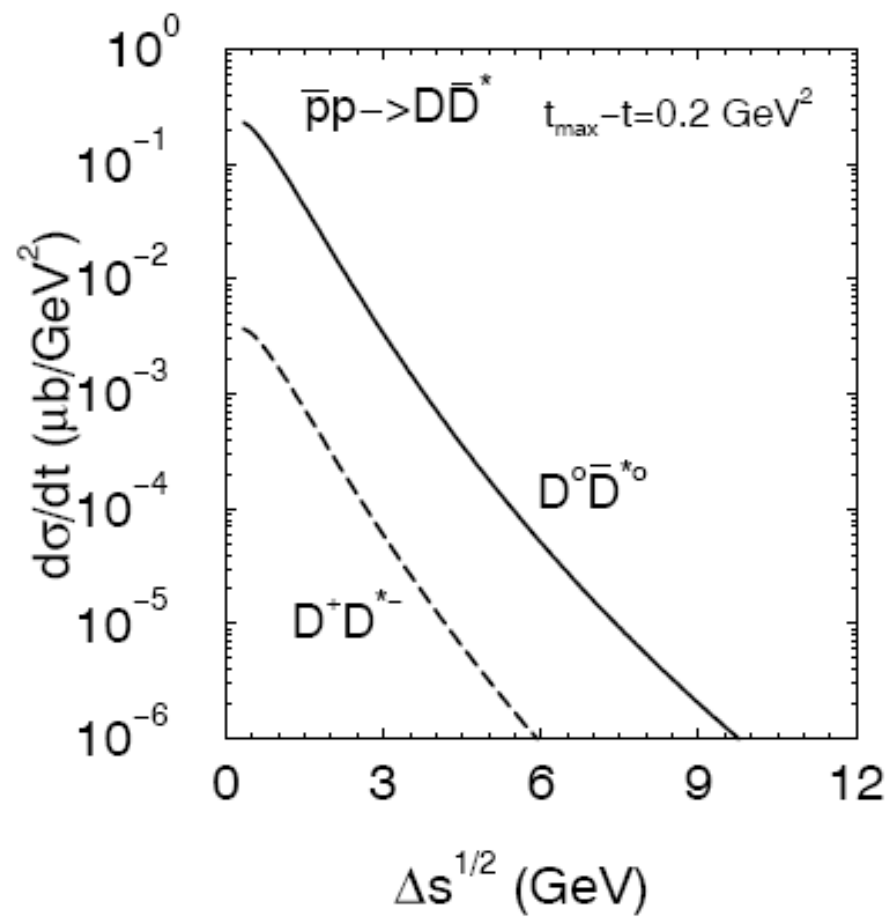
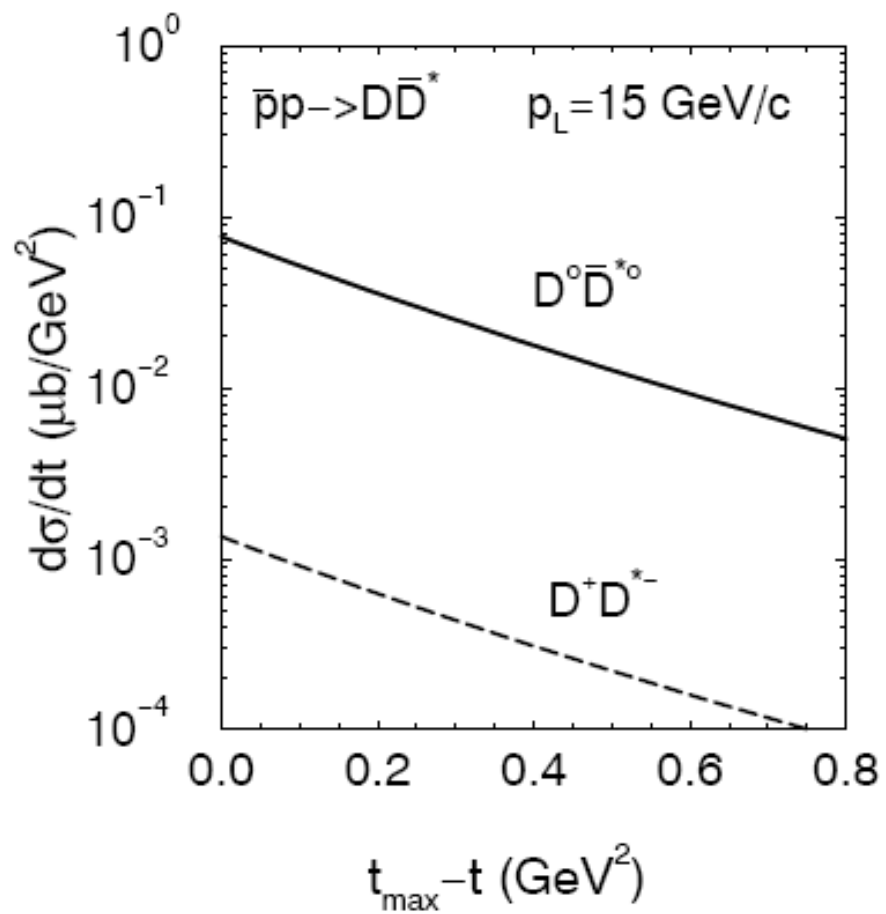




$$T_{\lambda_f; m_i, n_i}^{\bar{p}p \rightarrow \bar{K}^- K^{*+}} = C'(t) \mathcal{M}_{\lambda_f; m_i, n_i}^{\bar{p}p \rightarrow \bar{K} K} (s, t) \frac{g_{K^* N \Lambda} g_{K N \Lambda}}{s_0} \Gamma\left(\frac{1}{2} - \alpha_{ds}(t)\right) \left(-\frac{s}{s_{\bar{n}n, \bar{K} K^*}}\right)^{\alpha_{ds}(t) - \frac{1}{2}}$$

$$\mathcal{M}_{\lambda_f; m_i, n_i}^{\bar{p}p \rightarrow \bar{K} K} (s, t) = \mathcal{N}(s, t) \Gamma_{\lambda_f; m_i, n_i}^\mu \quad \Gamma_{\lambda_f; m_i, n_i}^\mu = \bar{v}_{n_i} \left[\gamma_5 (\not{p}_Y - M_Y) (\gamma^\mu + \frac{\kappa_{NYK^*}}{2(M_N + M_Y)} (\gamma^\mu \not{p}_{K^*} - \not{p}_{K^*} \gamma^\mu)) \right] u_{m_i} \epsilon_{\lambda_i}^{\mu*}$$

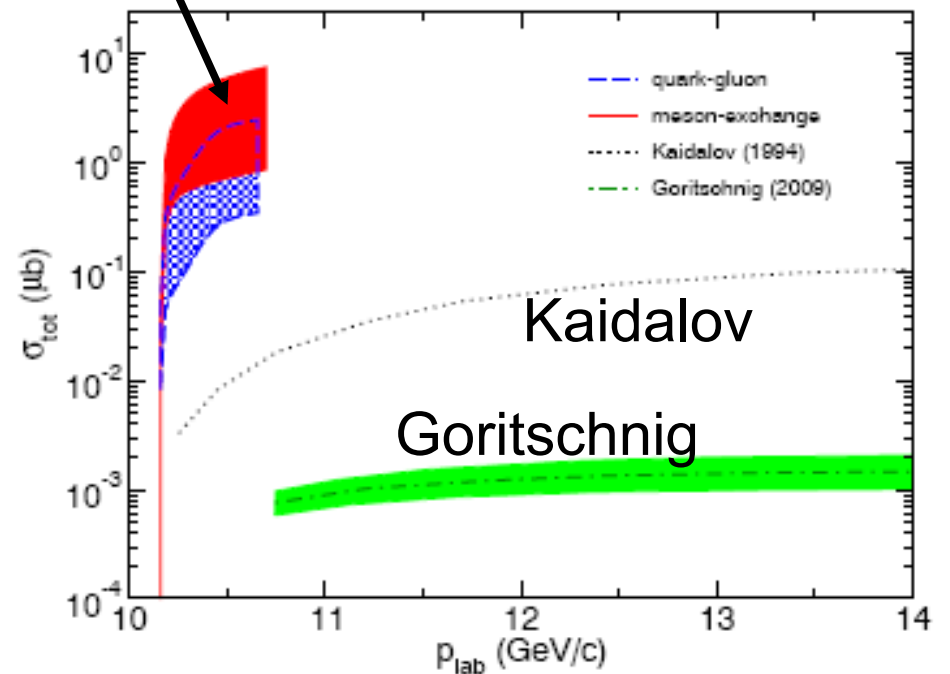
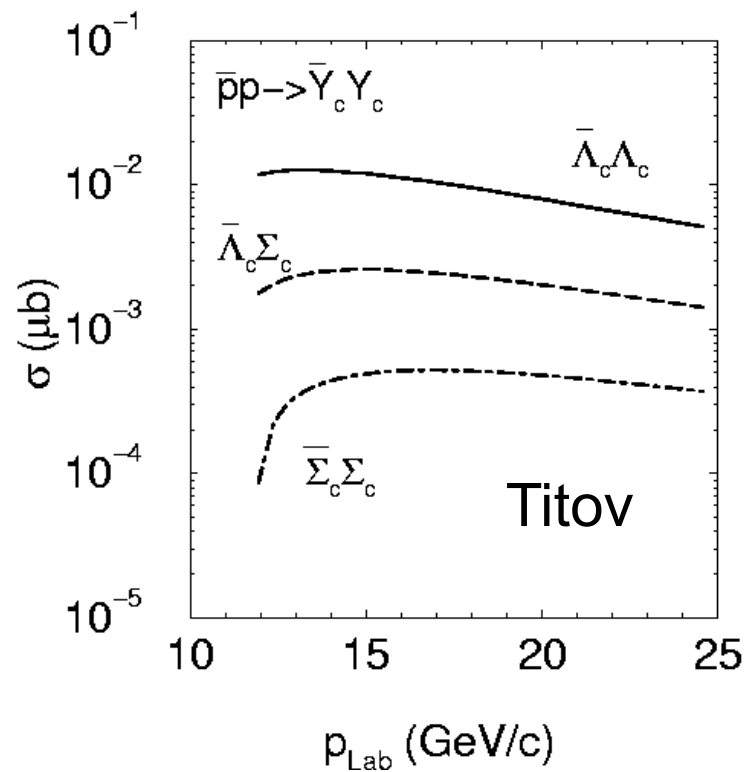
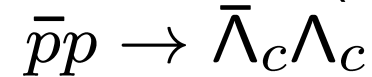




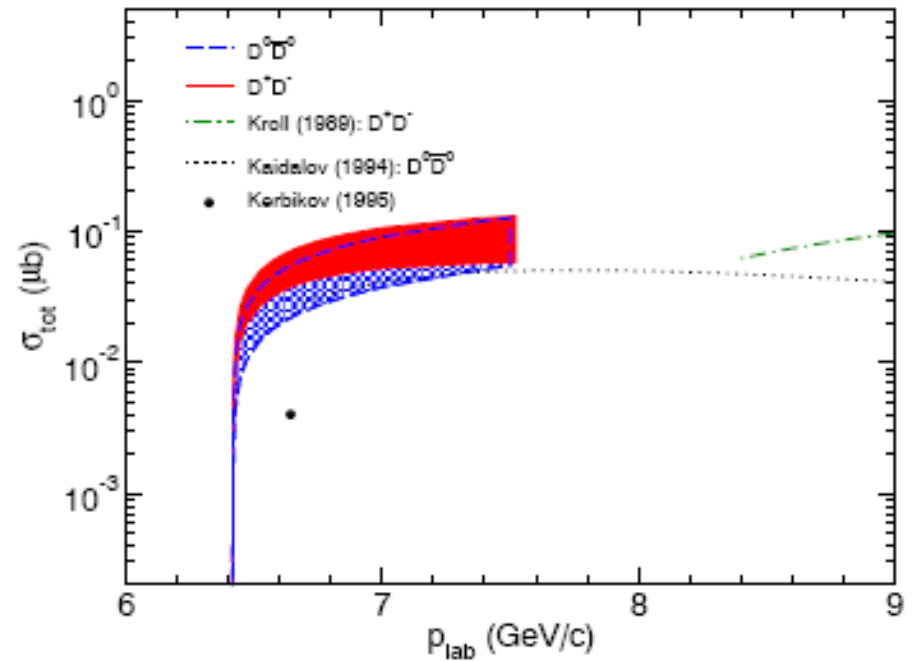
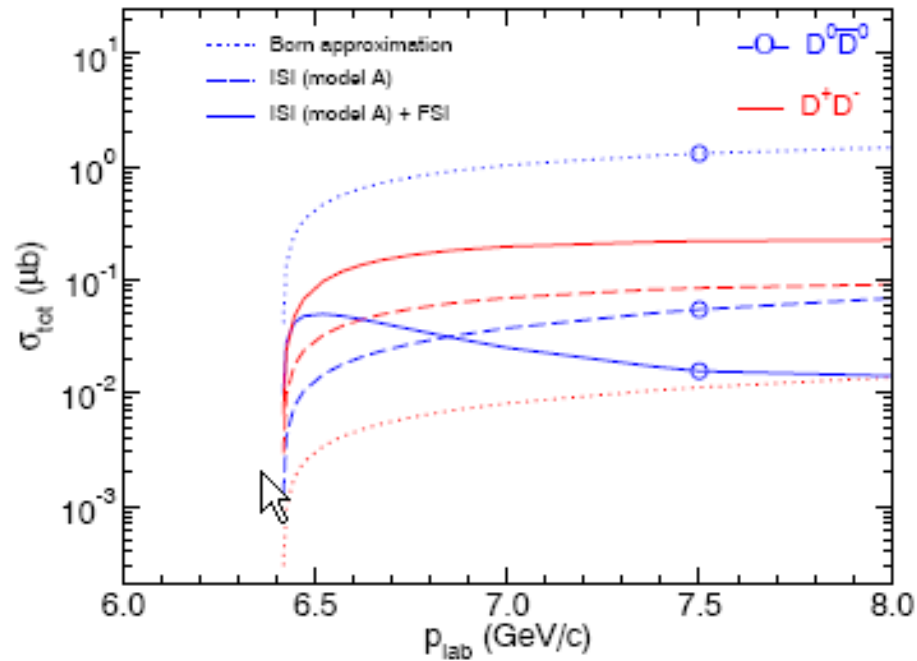
Longitudinal Asymmetries: cf. Titov, BK, PRC 78 (2008) 025201

$$A = \frac{d\sigma^{\leftarrow} - d\sigma^{\rightarrow}}{d\sigma^{\leftarrow} + d\sigma^{\rightarrow}} \quad \rightarrow \text{PAX}$$

Very different predictions by Haidenbauer, Krein, PLB 687 (2010) 314



„an impressive qualitative difference“



Artoisenet, Braaten, PRD 2009: inclusive charm production within parton model \rightarrow factor 10 uncertainty due to variations of

$$m_c, \mu_r, \mu_f$$

Linnyk, Bratkovskaya, Cassing, IJMP 2008: elementary charm Xsections from PYTHIA fits to high-energy data \rightarrow Au + Au at 25 AGeV

much remains to be done!

Summary

- DS-BS: our first results are encouraging
next: other channels, excited states
goal: in medium
- QCD sum rules: fairly robust „mass splitting“ of $D - \bar{D}$
Weinberg type differences of heavy-light mesons
→ amplified chiral condensate
- Transparency ratio: width of charmonia (like phi)
- Regge type phenomenology for associate charm production
in $p \bar{p}$: predictions for peripheral collisions