

Hadron Structure at BESIII

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on behalf of the BESIII Collaboration

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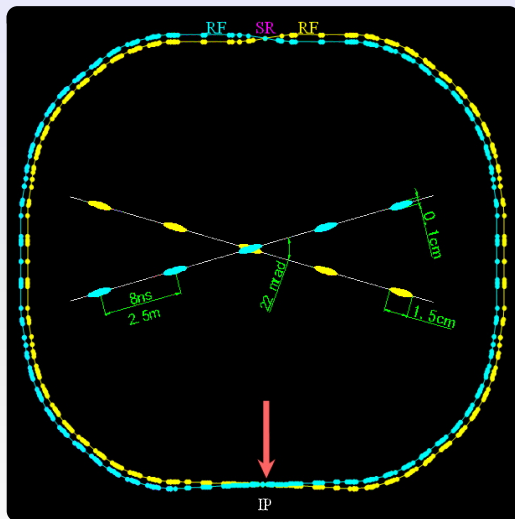
The Structure and Dynamics of Hadrons

International Workshop
XXXIX on Gross Properties of Nuclei and Nuclear Excitations



Hirschegg, January 16th - 22nd, 2011

BEPCII: e^+e^- double ring collider

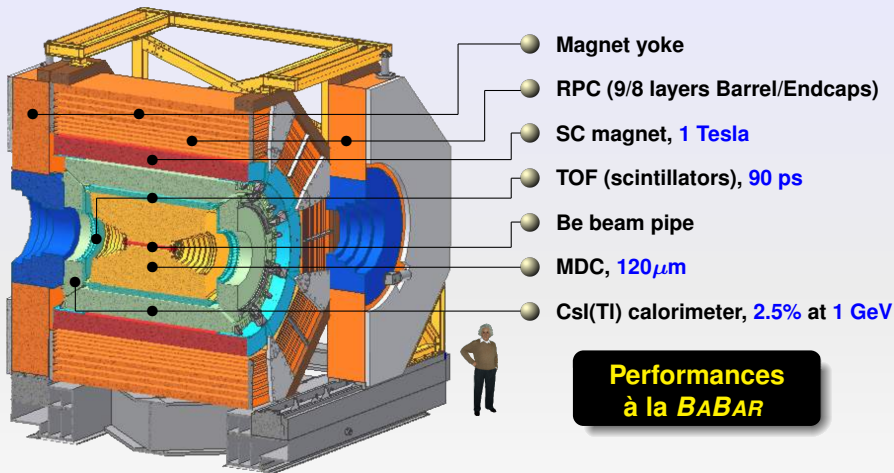


Design Features

- Beam energy: 1.0 - 2.3 GeV
- Crossing angle: 22 mrad
(DAΦNE 50 mrad)
- **Luminosity: $10^{33} \text{ cm}^{-2}\text{s}^{-1}$**
- **Optimum energy: 1.89 GeV**
- Energy spread: 5.16×10^{-4}
- Number of bunches: 93
- Bunch length: 1.5 cm
- Total current: 0.91 A



The BESIII detector

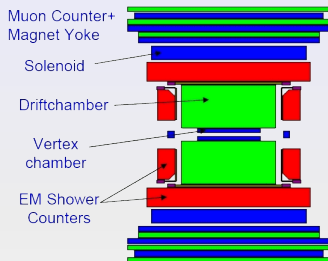


**Performances
à la *BABAR***

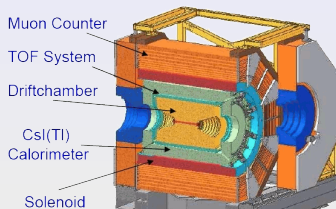
A significant improvement with respect to BESII

The BESII and BESIII detectors

BESII @ BEPC



BESIII @ BEPCII



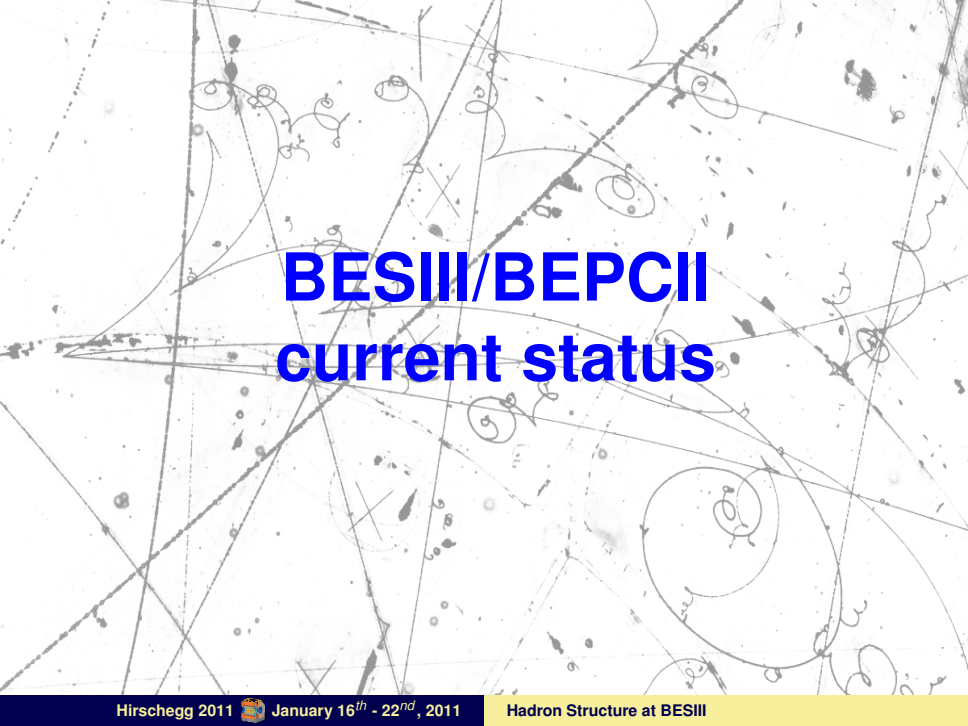
Device	Performance
MDC	$\sigma_p/p = 1.7\% \sqrt{1 + p^2}$, $dE/dx = 8\%$
TOF	180 ps (bhabha)
EMC	$\sigma_E/E < 22\%/\sqrt{E}$
MUC	3 layers
Magnet	0.4 T Solenoidal

Device	Performance
MDC	$\sigma_p/p = 0.5\%$, $dE/dx < 6\%$
TOF	80 ps barrel (bhabha), 100 ps endcap
EMC	$\sigma_E/E < 2.5\%/\sqrt{E}$
MUC	9 barrel + 8 endcap layers
Magnet	1 T Solenoidal

- R_{had} and precision test of Standard Model
- Light hadron spectroscopy ($\phi f_0(980)$, $\phi\pi^0$, ...)
- Charm and charmonium physics
- τ physics
- Precision measurements of CKM matrix elements
- Search for new physics / new particles

Physics Channels	Energy (GeV)	Luminosity ($10^{33} \text{ cm}^{-2} \text{ s}^{-1}$)	Events/year
J/ψ	3.10	0.6	1.0×10^{10}
τ	3.67	1.0	1.2×10^7
$\psi(2S)$	3.69	1.0	3.0×10^9
D^*	3.77	1.0	2.5×10^7
D_s	4.03	0.6	1.0×10^6
D_s	4.14	0.6	2.0×10^6





BESIII/BEPCII current status

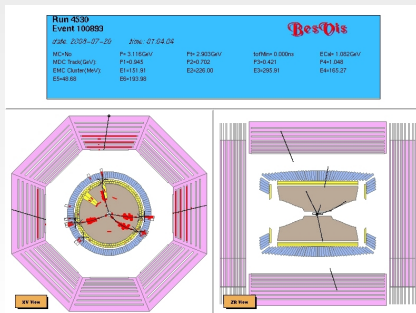
BEPCII: e^+e^- double ring collider

2010 STATUS

Parameter	Design	Achieved	
		BER	BPR
Energy (GEV)	1.89	1.89	1.89
Beam curr. (mA)	910	660	700
Bunch curr. (mA)	9.8	> 10	> 10
Bunch number	93	93	93
RF voltage	1.5	1.5	1.5
$*\nu_s$ @ 1.5 MV	0.033	0.032	0.032
β_x^*/β_y^* (m)	1.0/0.015	$\sim 1.0/0.016$	$\sim 1.0/0.016$
Inj. Rate (mA/min)	200 e^- / 50 e^+	> 200	> 50
Lum. ($10^{33} \text{ cm}^{-2} \text{ s}^{-1}$)	1	0.57	

BEPCII / BESIII milestones

- **Mar. 2008:** Collisions at $500 \text{ mA} \times 500 \text{ mA}$,
Luminosity: $1 \times 10^{32} \text{ cm}^{-2} \text{ s}^{-1}$
- **Apr. 30, 2008:** Move BESIII to IP
- **July 18, 2008:** First e^+e^- collision event in BESIII
- **Apr. 14, 2009:** $\sim 106 \text{ M } \Psi(2S) \text{ events } (150 \text{ pb}^{-1})$
($\sim 42 \text{ pb}^{-1}$ at 3.65 GeV)
- **July 28, 2009:** $\sim 226 \text{ M } J/\Psi \text{ events } (65 \text{ pb}^{-1})$
- **June 1, 2010:** $\sim 930 \text{ pb}^{-1}$ at $\Psi(3770)$
($\sim 70 \text{ pb}^{-1}$ scanning in the $\Psi(3770)$ energy region)



**Record Luminosity
on Jan 12, 2011**

$$5.7 \times 10^{32} \text{ cm}^{-2} \text{ s}^{-1}$$

or

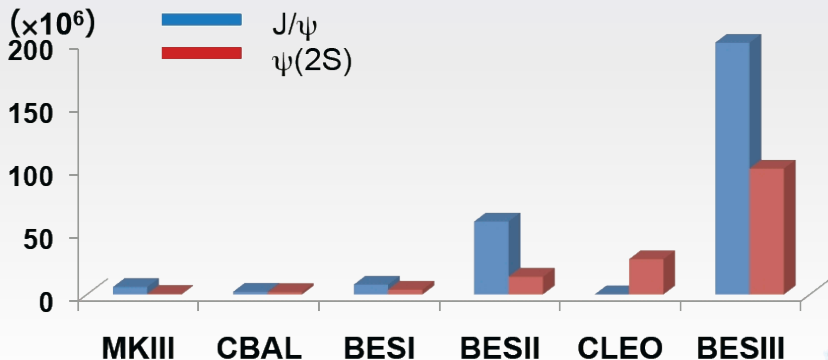
$$8 \times \text{CESRc}$$

$$45 \times \text{BEPC}$$



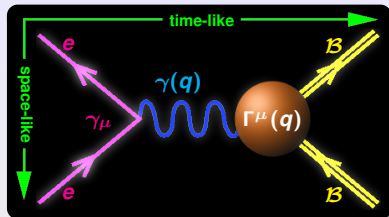
World J/ψ and $\psi(2S)$ Samples ($\times 10^6$)

- **BESIII:** ~ 106 M $\psi(2S)$ events (150pb^{-1})
● **BESII:** ~ 14 M $\psi(2S)$ events
- **BESIII:** ~ 226 M J/ψ events (65pb^{-1})
● **BESII:** ~ 58 M J/ψ events





Nucleon form factors and cross sections



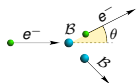
Nucleon current operator (Dirac & Pauli)

$$\Gamma^\mu(q) = \gamma^\mu F_1(q^2) + \frac{i}{2M_B} \sigma^{\mu\nu} q_\nu F_2(q^2)$$

Electric and Magnetic Form Factors

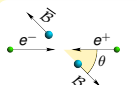
$$G_E(q^2) = F_1(q^2) + \tau F_2(q^2) \quad \tau = \frac{q^2}{4M_B^2}$$

$$G_M(q^2) = F_1(q^2) + F_2(q^2)$$



Elastic scattering (Rosenbluth)

$$\frac{d\sigma}{d\Omega} = \frac{\alpha^2 E_e' \cos^2 \frac{\theta}{2}}{4E_e^3 \sin^4 \frac{\theta}{2}} \left[G_E^2 - \tau \left(1 + 2(1 - \tau) \tan^2 \frac{\theta}{2} \right) G_M^2 \right] \frac{1}{1 - \tau}$$



Annihilation

Coulomb correction

$$\frac{d\sigma}{d\Omega} = \frac{\alpha^2 \beta C}{4q^2} \left[(1 + \cos^2 \theta) |G_M|^2 + \frac{1}{\tau} \sin^2 \theta |G_E|^2 \right]$$

$$\beta = \sqrt{1 - \frac{1}{\tau}}$$

Pointlike fermions
e.g. $e^+e^- \rightarrow \mu^+\mu^-$

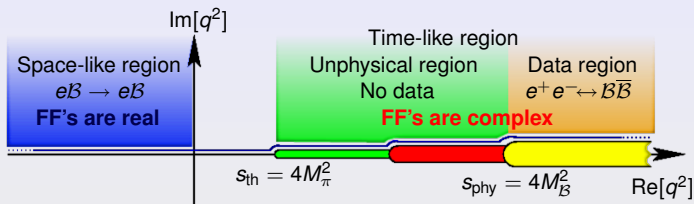
$$\frac{d\sigma}{d\Omega} = \frac{\alpha^2 \beta_\mu C}{4q^2} (2 - \beta_\mu^2 \sin^2 \theta)$$



$$|G_E| = |G_M| \equiv 1$$

Analyticity of baryon form factors

q^2 -complex plane



Crossing: tot. helicity = $\begin{cases} 1 \Rightarrow G_E \\ 0 \Rightarrow G_M \end{cases}$

$$G_E(4M_B^2) = G_M(4M_B^2)$$

QCD counting rule constrains the asymptotic behaviour

Matveev, Muradyan, Tevkheldize, Brodsky, Farrar

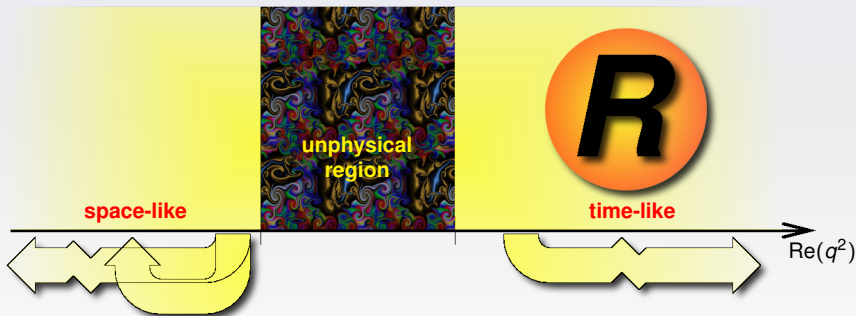
Counting rule: $q^2 \rightarrow -\infty$
 $i = 1$ Dirac, $i = 2$ Pauli FF

$$F_i(q^2) \propto (-q^2)^{-(i+1)} \Rightarrow G_{E,M} \propto (-q^2)^{-2}$$

Analyticity: $q^2 \rightarrow \pm\infty$
 (Phragmén Lindelöf)

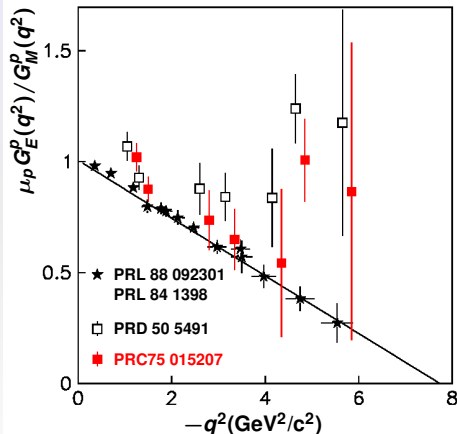
$$G_{E,M}(-\infty) = G_{E,M}(+\infty)$$

The ratio $R = \mu_p \frac{G_E^p}{G_M^p}$



Space-like G_E^p/G_M^p measurements

Space-like data



$$G_E^p = F_1^p + \frac{q^2}{4M_p^2} F_2^p$$

$$G_M^p = F_1^p + F_2^p$$

Space-like

F_1 and $\frac{q^2}{4M_p^2} F_2$ cancellation

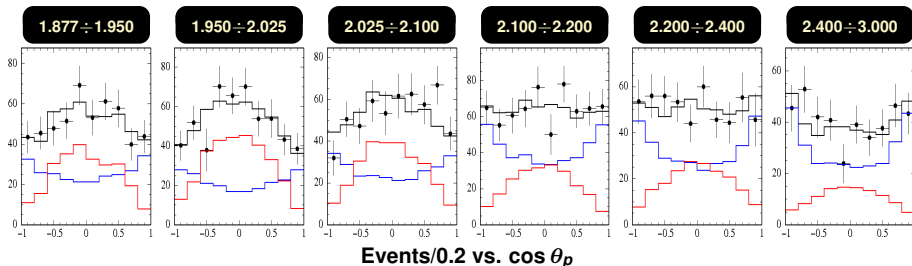
$$\frac{G_E^p(q^2)}{G_M^p(q^2)} < 1$$

Time-like

F_1 and $\frac{q^2}{4M_p^2} F_2$ enhancement

$$\left| \frac{G_E^p(q^2)}{G_M^p(q^2)} \right| > 1$$

$\cos \theta_p$ distributions from threshold up to 3 GeV [intervals in $E_{CM} \equiv q$ (GeV)]



$$\frac{d\sigma}{d\cos\theta_p} = A \left[H_E(\cos\theta_p, q^2) \left| \frac{G_E^p(q^2)}{G_M^p(q^2)} \right|^2 + H_M(\cos\theta_p, q^2) \right]$$

H_E and H_M from MC

Histograms show contributions from



At low q

$$\sin^2 \theta_p > 1 + \cos^2 \theta_p$$

First observation!

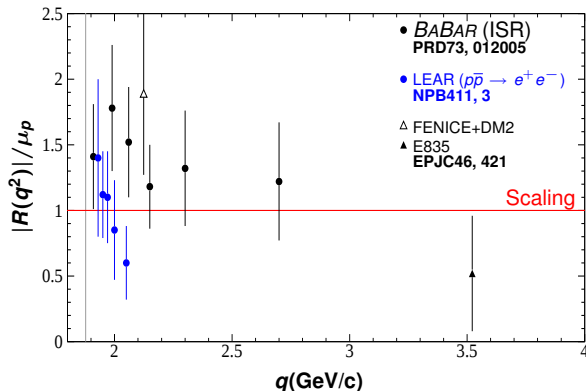
$$|G_E^p| > |G_M^p|$$

At higher q , $|G_E^p| \rightarrow |G_M^p|$

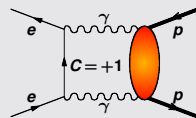
Time-like $|G_E^p/G_M^p|$ measurements

$$\frac{d\sigma}{d\cos\theta} = \frac{\pi\alpha^2\beta_p C}{2q^2} |G_M^p|^2 \left[(1 + \cos^2\theta) + \frac{4M_p^2}{q^2\mu_p^2} \sin^2\theta |R|^2 \right]$$

$$R(q^2) = \mu_p \frac{G_E^p(q^2)}{G_M^p(q^2)}$$



$\gamma\gamma$ exchange

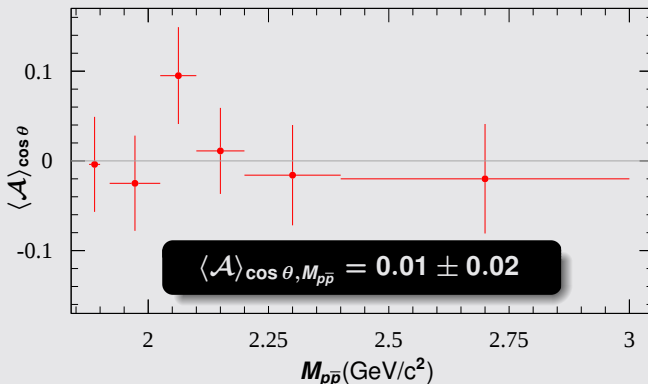


$\gamma\gamma$ exchange interferes with the Born term

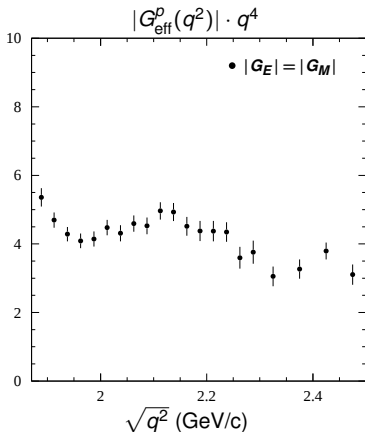


Asymmetry in angular distributions
[PLB659, 197]

$$\mathcal{A}(\cos \theta, M_{p\bar{p}}) = \frac{\frac{d\sigma}{d\Omega}(\cos \theta, M_{p\bar{p}}) - \frac{d\sigma}{d\Omega}(-\cos \theta, M_{p\bar{p}})}{\frac{d\sigma}{d\Omega}(\cos \theta, M_{p\bar{p}}) + \frac{d\sigma}{d\Omega}(-\cos \theta, M_{p\bar{p}})}$$



$|G_E^p(q^2)|$ and $|G_M^p(q^2)|$ from $\sigma_{p\bar{p}}$ and DR

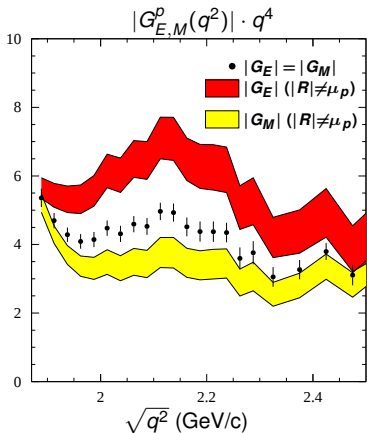


$$|G_{\text{eff}}(q^2)|^2 = \frac{\sigma_{p\bar{p}}(q^2)}{\frac{4\pi\alpha^2\beta C}{3s}} \left(1 + \frac{1}{2\tau}\right)^{-1}$$

- Usually what is extracted from the cross section $\sigma(e^+e^- \rightarrow p\bar{p})$ is the effective time-like form factor $|G_{\text{eff}}^p|$ obtained assuming $|G_E^p| = |G_M^p|$ i.e. $|R| = \mu_p$
- Using DR's to parameterize R and the *BABAR* data on $\sigma(e^+e^- \leftrightarrow p\bar{p})$, $|G_E^p|$ and $|G_M^p|$ may be disentangled
- BESIII can measure separately $|G_E^p|$ and $|G_M^p|$

Cfr. talk by Simone Pacetti:
Dispersion Relations and Nucleon Form Factors

$|G_E^p(q^2)|$ and $|G_M^p(q^2)|$ from $\sigma_{p\bar{p}}$ and DR

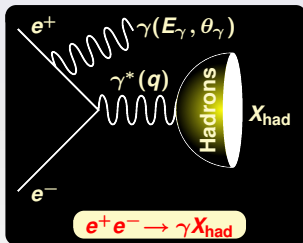


$$|G_M(q^2)|^2 = \frac{\sigma_{p\bar{p}}(q^2)}{\frac{4\pi\alpha^2\beta C}{3s}} \left(1 + \frac{|R(q^2)|}{2\mu_{pT}}\right)^{-1}$$

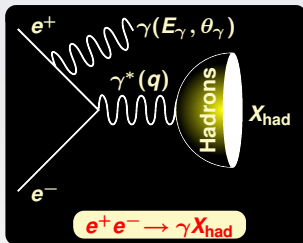
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**Cfr. talk by Simone Pacetti:
Dispersion Relations and Nucleon Form Factors**

ISR



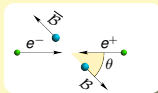
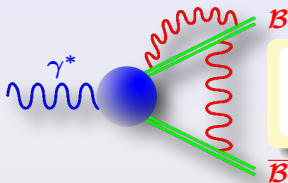
ISR



The Coulomb Factor

$p\bar{p}$ Coulomb interaction as FSI

[Sommerfeld, Sakharov, Schwinger, Fadin, Khoze]



Annihilation

Coulomb correction

$$\frac{d\sigma}{d\Omega} = \frac{\alpha^2 \beta C}{4q^2} \left[(1 + \cos^2 \theta) |G_M|^2 + \frac{1}{\tau} \sin^2 \theta |G_E|^2 \right]$$

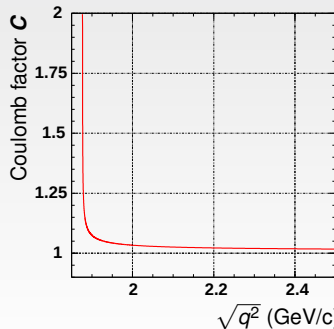
Distorted wave approximation

$$C = |\Psi_{\text{Coul}}(0)|^2$$

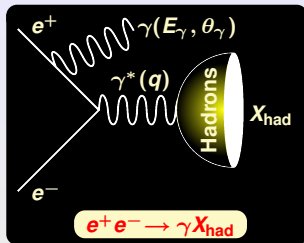
S-wave: $C = \frac{\frac{\pi\alpha}{\beta}}{1 - \exp\left(-\frac{\pi\alpha}{\beta}\right)} \xrightarrow{\beta \rightarrow 0} \frac{\pi\alpha}{\beta}$

D-wave: $C = 1$

No Coulomb factor for boson pairs (P-wave)



Initial State Radiation



- $\frac{d^2\sigma}{dE_\gamma d\theta_\gamma} = W(E_\gamma, \theta_\gamma) \cdot \sigma_{e^+e^- \rightarrow X_{\text{had}}}(s)$

- $W(E_\gamma, \theta_\gamma) = \frac{\alpha}{\pi x} \left(\frac{2 - 2x + x^2}{\sin^2 \theta_\gamma} \right)$

- $s = q^2$, q X_{had} momentum
- E_γ, θ_γ ... CM γ energy, scatt. ang.
- E_{CM} CM e^+e^- energy
- $x = E_\gamma / 2E_{\text{CM}}$

Advantages

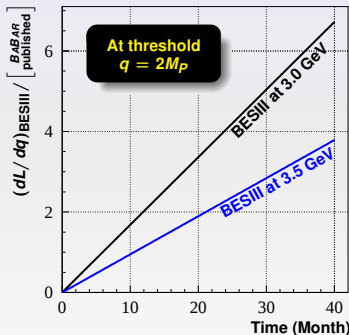
- All energies (q^2) at the same time
 $\Downarrow$
 Better control on systematics
 (e.g. greatly reduced point to point)
- Detected ISR $\Rightarrow$ full X_{had} angular coverage
- CM boost $\Rightarrow$ $\begin{cases} \text{at threshold } \epsilon \neq 0 \\ \text{energy resolution } \sim 1 \text{ MeV} \end{cases}$

ISR: BESIII vs BABAR

ISR Luminosity

$$\frac{dL}{dq} = \frac{2q}{E_{\text{cm}}^2} L_{ee} \int_{\cos \theta_{\gamma}^{\min}}^{\cos \theta_{\gamma}^{\max}} W(E_{\gamma}, \theta_{\gamma}) d \cos \theta_{\gamma}$$

L_{ee} total luminosity
 $\theta_{\gamma}^{\min, \max}$ geom. accept.



BESIII

lower CM
energy



lower
background



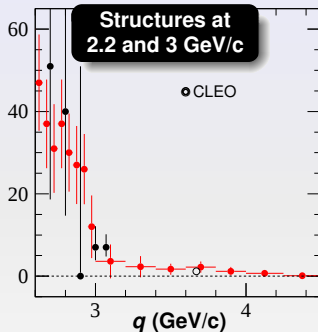
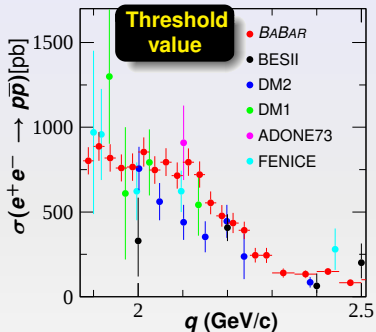
ISR γ detection + 0°
and
No ISR γ detection



×2.5 and ×5
in statistics

$$\sigma(e^+e^- \rightarrow p\bar{p}) = \frac{4\pi\alpha^2\beta_p \mathcal{C}}{3q^2} \left[|G_M|^2 + \frac{2M_p^2}{q^2} |G_E|^2 \right]$$

$$\mathcal{C} \underset{\beta \rightarrow 0}{\sim} \frac{\pi\alpha}{\beta}$$

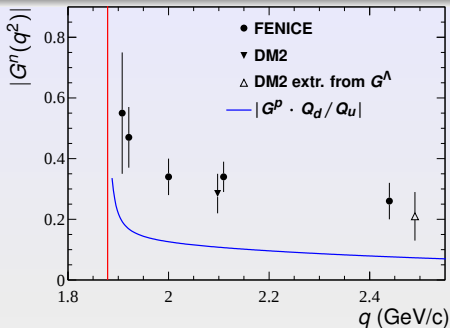


$$\sigma(e^+e^- \rightarrow p\bar{p})(4M_p^2) = \frac{\pi^2\alpha^3}{2M_p^2} \frac{\beta_p}{\beta_p} |G^p(4M_p^2)|^2 = 0.85 |G^p(4M_p^2)|^2 \text{ nb}$$

$$|G^p(4M_p^2)| \equiv 1 \quad \text{as pointlike fermion pairs!}$$

Using the ISR technique with only few fb^{-1} of integrated luminosity BESIII can easily achieve the **BABAR** statistics

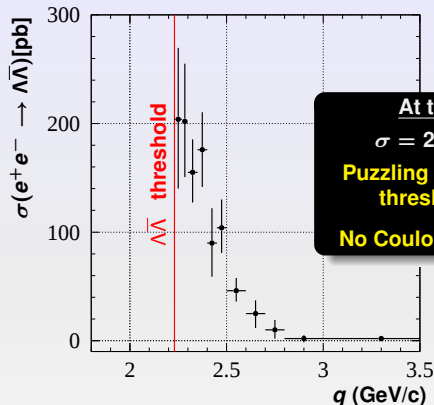
$$e^+e^- \rightarrow n\bar{n}$$



- Measured only once by FENICE at ADONE
- $\int \mathcal{L} = 500 \text{ nb}^{-1}$ (15' at BESIII)
- ~ 100 candidates $n\bar{n}$ events!
- $\sigma(n\bar{n}) > \sigma(p\bar{p})$?
- Not zero at threshold?

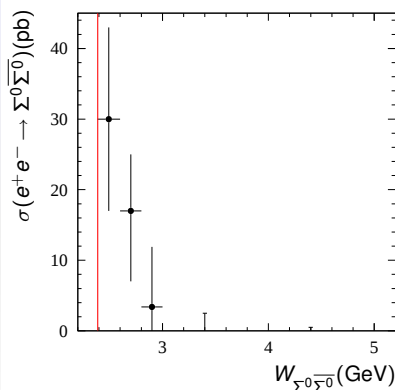
BESIII has the unique possibility to measure this cross section

- $J/\psi \rightarrow n\bar{n}$ (BR $\simeq 2 \cdot 10^{-3}$) $\geq 10^4$ events
- $\psi(2S) \rightarrow n\bar{n}$ (BR $\simeq 3 \cdot 10^{-4}$) $\geq 10^3$ events
- At threshold by means of ISR (boost)
- $n, \bar{n}$ detection efficiency and pattern by means of:
 $J/\psi \rightarrow n(\bar{p}\pi^+)$ and $J/\psi \rightarrow \bar{n}(p\pi^-)$ ($\geq 10^5$ events)

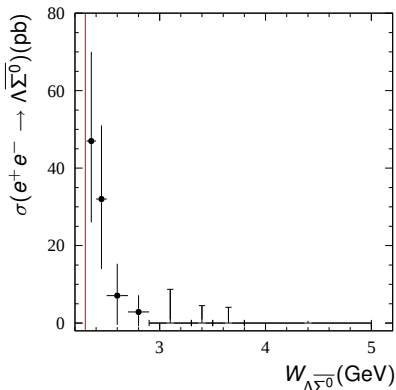


Only at the J/ψ mass BESIII can increase the BABAR statistics at least by a factor of two because of a better Λ reconstruction resolution (only one Λ reconstructed)

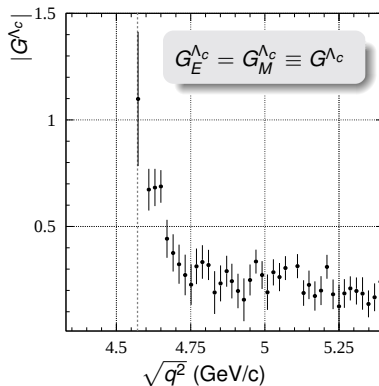
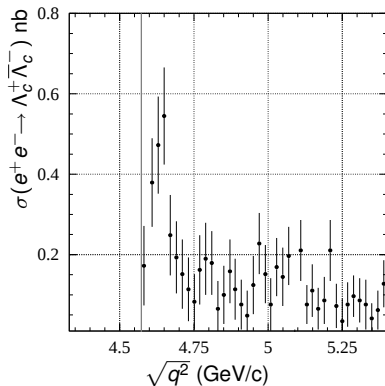
Λ polarization for free $\Rightarrow G_E^\Lambda - G_M^\Lambda$ relative phase

Cross sections of $e^+e^- \rightarrow \Sigma^0\bar{\Sigma}^0, \Lambda\bar{\Sigma}^0$ via ISR (*BABAR*)

$$\sigma(e^+e^- \rightarrow \Sigma^0\bar{\Sigma}^0)_{\text{th}} = 30 \pm 13 \text{ pb}$$



$$\sigma(e^+e^- \rightarrow \Lambda\bar{\Sigma}^0)_{\text{th}} = 47 \pm 22 \text{ pb}$$

Belle $\sigma(e^+e^- \rightarrow \Lambda_c^+ \bar{\Lambda}_c^-)$ 

$$|G^{\Lambda_c}(4M_{\Lambda_c}^2)| = 1.1 \pm 0.3(\text{stat}) \pm 0.4(\text{syst})$$

Accessible to BESIII

- Existing results, obtained by **BABAR** (ISR), show interesting and unexpected behaviors, mainly at thresholds, for

$$e^+e^- \rightarrow p\bar{p}$$

and

$$e^+e^- \rightarrow \Lambda\bar{\Lambda}$$

- Only one measurement (**FENICE** with energy scan) for

$$e^+e^- \rightarrow n\bar{n}$$

There are physical limits in reaching the threshold of many of these channels via energy scan (stable hadrons produced at rest can not be detected)

The Initial State Radiation technique provides a unique tool to access threshold regions working at higher resonances

BESIII Zero-Degree Detector

- J/ψ , $\psi(2S)$, $\psi(3770)$ resonances decay with high BR's to final states with π^0 and γ_{FS} (final state)
- At BESIII these decay channels represent severe backgrounds for typical ISR final states with γ_{IS} detected at wide angle

 π^0 and final γ angular distributions are isotropic
 ISR angular distribution is peaked at small angles



A zero-degree radiative photon tagger will suppress most of these backgrounds

The BESIII Collaboration has accepted an upgrade (July 2011?) of the present luminosity monitor with a new zero-degree detector (ZDD), with a better energy resolution, to tag ISR photons as well as to measure the luminosity

Summary

An exciting scenario allow for the investigation of Form Factors at BESIII:

- $e^+e^- \rightarrow p\bar{p}$
- $e^+e^- \rightarrow n\bar{n}$
- $e^+e^- \rightarrow \Lambda\bar{\Lambda}$
- Time-Like $|G_E^p/G_M^p|$, $|G_E^p|$ and $|G_M^p|$
- $e^+e^- \rightarrow \Sigma^0\bar{\Sigma}^0$
- $e^+e^- \rightarrow \Lambda\bar{\Sigma}^0$
- $e^+e^- \rightarrow \Lambda_c^+\bar{\Lambda}_c^-$
- $|G_E^\Lambda|$ - $|G_M^\Lambda|$ relative phase

Achieved luminosities:

● $\mathcal{L}_{\Psi(2S)} : 5.7 \times 10^{32} \text{cm}^{-2} \text{s}^{-1}$

● $\mathcal{L}_{J/\psi} : 0.7 \times 10^{32} \text{cm}^{-2} \text{s}^{-1}$



**Investigation at
unprecedented
luminosities!**

● wide energy range $\sqrt{s} : 2 \div 4, 6 \text{ GeV}$

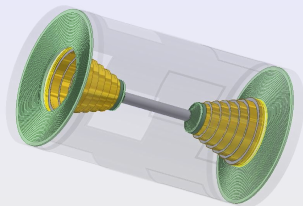
● investigation at threshold and for different q^2 (ISR)

BACK-UP SLIDES

BESIII main features

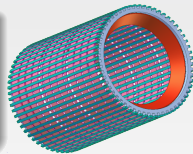
Drift Chamber

- Low gas mixture (60% He, 40% Propane)
- Carbon filter cylindres: $R_{in} = 6.3 \text{ cm}$, $T_{in} = 1 \text{ mm}$,
 $R_{out} = 81 \text{ cm}$ $T_{out} = 1 \text{ cm}$
- 6 Al stepped flanges: $T = 1.8 \text{ cm}$
- 43 layers: 7000 $25 \mu\text{m}$ gold-plated sense wires, 22000 Al field-shaping wires
- $\sigma_{x,y} \sim 130 \mu\text{m}$, $\sigma(De/dx) \sim 6\%$



CsI Calorimeter

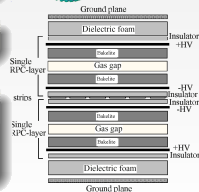
- 6240 CsI(Tl): 5280 Barrel, 960 Endcaps, 13000 photodiodes
- $28 \times 5.2^2 \text{ cm}^3$
- $\Delta E/E \sim 2.5\%$ at 1 GeV, noise $\sim 220 \text{ keV}$



Superconducting Magnet: 1 T

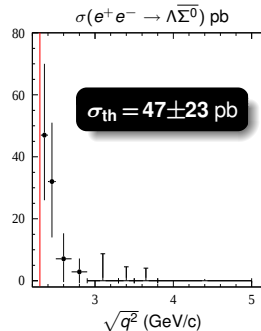
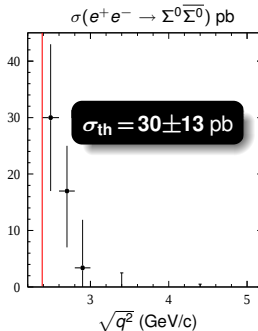
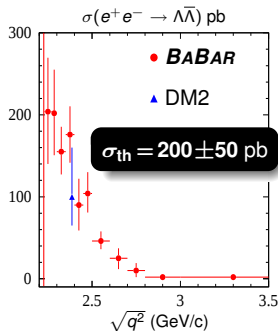
RPC μ Chambers

9/8 layers Barrel/Endcaps, Strip x, y 4cm
Plastic foil instead linseed oil: noise $\sim 0.1 \text{ Hz/cm}^2$, $\epsilon \sim 95\%$



$$\sigma(e^+e^- \rightarrow B^0 \bar{B}^0) = \frac{4\pi\alpha^2\beta C_0}{3q^2} \left[|G_M^{B^0}|^2 + \frac{2M_{B^0}^2}{q^2} |G_E^{B^0}|^2 \right] \xrightarrow{q \rightarrow 2M_{B^0}} \frac{\pi\alpha^2\beta}{2M_{B^0}^2} |G^{B^0}|^2 \rightarrow 0$$

No Coulomb correction at hadron level: $C_0 = 1$



Remnant of
Coulomb interactions
at quark level?



$C_0 \propto \beta^{-1}$
as $q \rightarrow 2M_{B^0}$



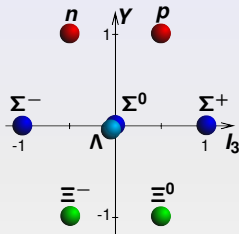
For any neutral baryon

$$\sqrt{\sigma_{B^0 \bar{B}^0}} \propto \frac{|G^{B^0}|}{M_{B^0}}$$

Coulomb correction
at quark level

$$\sqrt{\sigma_{B^0 \bar{B}^0} (4M_{B^0}^2)} = K \cdot \frac{|G_{B^0}|}{M_{B^0}}$$

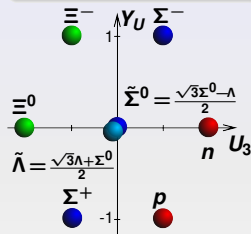
K is unknown but equal
for all neutral baryons
with equal quark content



$$(Y, I_3) \rightarrow (Y_U, U_3)$$

$$U_3 = -\frac{1}{2} I_3 + \frac{3}{4} Y$$

$$Y_U = -Q$$



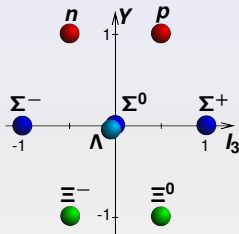
Indirect relation: $G^{\Sigma^0} - G^{\Lambda} + \frac{2}{\sqrt{3}} G^{\Lambda \Sigma^0} = 0$

$$M_{\Sigma^0} \sqrt{\sigma_{\Sigma^0 \bar{\Sigma}^0}} - M_{\Lambda} \sqrt{\sigma_{\Lambda \bar{\Lambda}}} + \frac{2}{\sqrt{3}} M_{\Lambda \Sigma^0} \sqrt{\sigma_{\Lambda \Sigma^0}} = (-0.06 \pm 6.0) \times 10^{-4}$$

Coulomb correction
at quark level

$$\sqrt{\sigma_{B^0 \bar{B}^0}(4M_{B^0}^2)} = K \cdot \frac{|G_{B^0}|}{M_{B^0}}$$

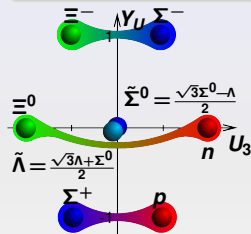
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Data and U -spin predictions at threshold

- $M_{\Sigma^0} \sqrt{\sigma_{\Sigma^0 \Sigma^0}} - M_{\Lambda} \sqrt{\sigma_{\Lambda \Lambda}} + \frac{2}{\sqrt{3}} \overline{M_{\Lambda \Sigma^0}} \sqrt{\sigma_{\Lambda \Sigma^0}} = (-0.06 \pm 6.0) \times 10^{-4}$
- $\sigma(e^+e^- \rightarrow n\bar{n}) = \frac{1}{4} (3\sqrt{\sigma_{\Lambda \Lambda}} M_{\Lambda} - \sqrt{\sigma_{\Sigma^0 \Sigma^0}} M_{\Sigma})^2 \frac{1}{M_n^2} = 0.5 \pm 0.2 \text{ nb}$

