

Coupled Channels Approach to Meson Production on the Nucleon

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Agenda:

- Coupled Channels Description of (γ, N) and (π, N) scattering
- Photo-Production of Strangeness
- eta-Production on the nucleon
- Summary and Outlook

1. The Giessen Coupled Channels Model (GiM)



The K-Matrix Approach

$$\langle f|M(p',p)|i\rangle = \langle f|V(p',p)|i\rangle + \int \frac{d^4q}{(2\pi)^4} \langle f|M(p',q)G_{BS}(q)V(q,p)|i\rangle ,$$

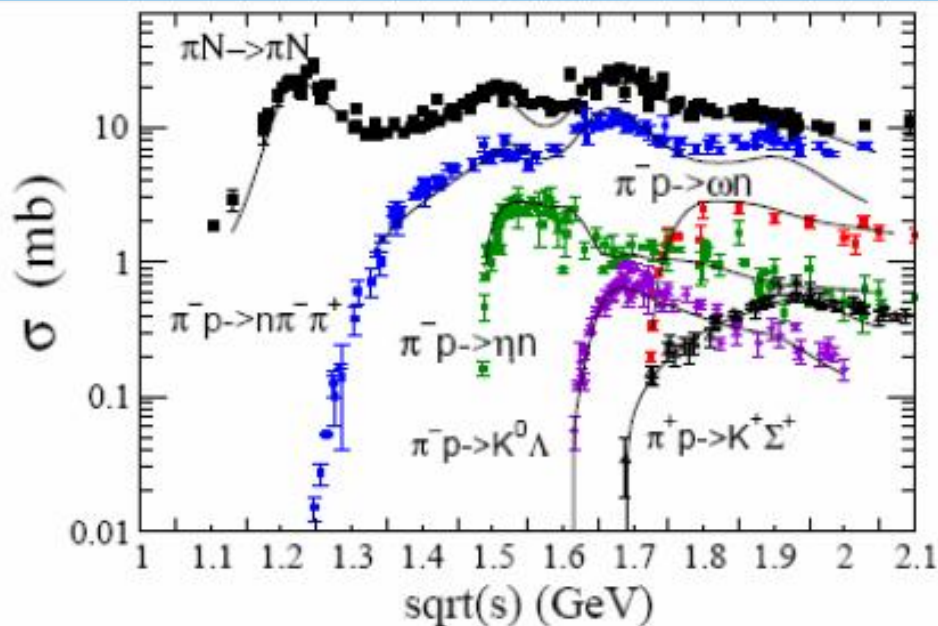
$$\langle f|\tilde{K}(p',p)|i\rangle = \langle f|V(p',p)|i\rangle + \int \frac{d^4q}{(2\pi)^4} \langle f|\tilde{K}(p',q)\text{Re}(G_{BS}(q))V(q,p)|i\rangle .$$

$$\langle f|M(p',p)|i\rangle = \langle f|\tilde{K}(p',p)|i\rangle + \int \frac{d^4q}{(2\pi)^4} \langle f|M(p',q)i\text{Im}(G_{BS}(q))\tilde{K}(q,p)|i\rangle ,$$

...or in short:

$$\mathcal{T}_{fi}^{IJ\pm} = \left[\frac{\mathcal{K}^{IJ\pm}}{1 - i\mathcal{K}^{IJ\pm}} \right]_{fi} .$$

Meson Production on the Nucleon



$l = \frac{1}{2}$ resonances

$S_{11}(1535), S_{11}(1650)$

$P_{11}(1440), P_{11}(1710)$

$P_{13}(1720), P_{13}(1900)$

$D_{13}(1520), D_{13}(2050)$

$D_{15}(1675)$

$F_{15}(1680), F_{15}(2000)$

Giessen model: Good description of the $\pi N \rightarrow \pi N, 2\pi N, \eta N, \omega N, K\Lambda, K\Sigma$ reactions in the resonance region

Data are connected \rightarrow unitarity \rightarrow Optical theorem

$$\text{Im}T_{\pi N \rightarrow \pi N}(0) = \frac{k^2}{4\pi} (\sigma_{\pi N \rightarrow \pi N} + \sigma_{\pi N \rightarrow 2\pi N} + \sigma_{\pi N \rightarrow \eta N} + \sigma_{\pi N \rightarrow \omega N} + \sigma_{\pi N \rightarrow K\Lambda} + \sigma_{\pi N \rightarrow K\Sigma})$$

Effective Lagrangians: PRC72 015210 (2005)

Born and t -channel terms:

$$L_{Born} + L_t = -\bar{u}_{B'}(p') \left[\frac{g_{\tilde{\varphi}}}{m_B + m_{B'}} \gamma_5 \gamma_\mu (\partial^\mu \tilde{\varphi}) + g_\eta i \gamma_5 \eta + g_S S \right. \\ \left. + g_V \left(\gamma_\mu V^\mu + \frac{\kappa_V}{2m_N} \sigma_{\mu\nu} V^{\mu\nu} \right) \right] u_B(p) \\ - \frac{g_S}{2m_\pi} (\partial_\mu \varphi') (\partial^\mu \varphi) S - g_V \varphi' (\partial_\mu \varphi) V^\mu - \frac{g}{4m_\varphi} \epsilon_{\mu\nu\rho\sigma} V^{\mu\nu} V'^{\rho\sigma} \varphi.$$

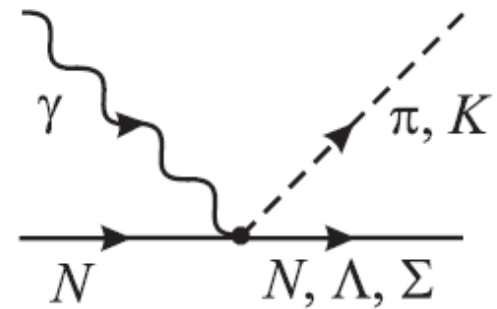
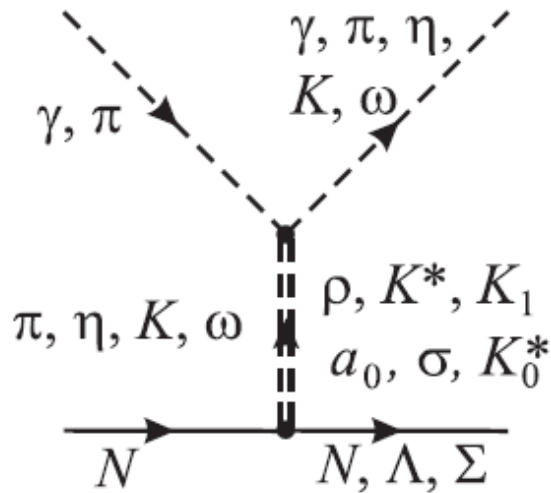
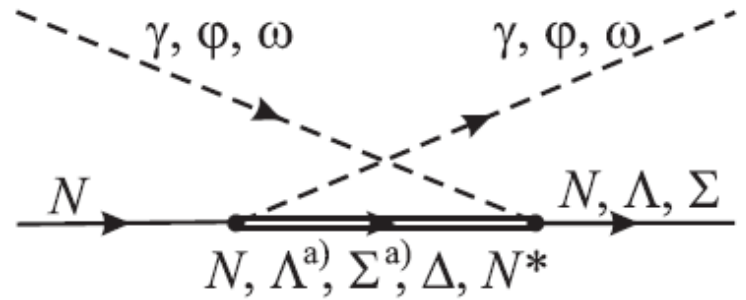
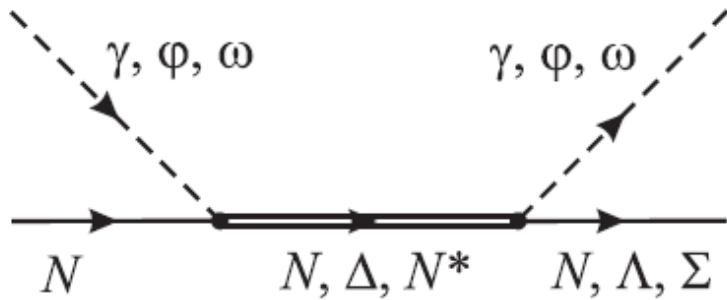
positive-parity **spin- $\frac{1}{2}$** resonances, PV coupling is used:

$$L_{\frac{1}{2}B\varphi}^{PV} = -\frac{g_{RB\varphi}}{m_R \pm m_B} \bar{u}_R \begin{pmatrix} \gamma_5 \\ i \end{pmatrix} \gamma_\mu u_B \partial^\mu \varphi.$$

negative-parity **spin- $\frac{1}{2}$** resonances, PS coupling is used:

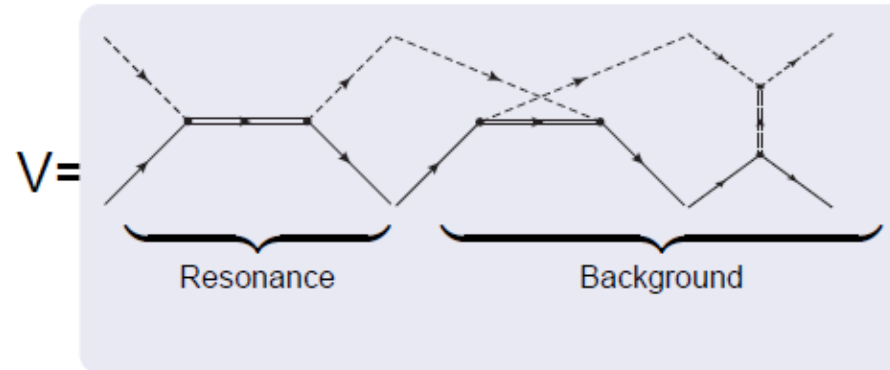
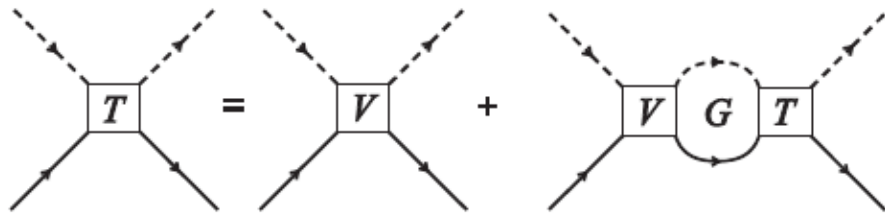
$$L_{\frac{1}{2}B\varphi}^{PS} = -g_{RB\varphi} \bar{u}_R \begin{pmatrix} 1 \\ -i\gamma_5 \end{pmatrix} u_B \varphi.$$

Tree-Level Diagrams:



The CC-Problem:

Bethe-Salpeter in K -matrix: Γ_{N^*} is dynamically generated

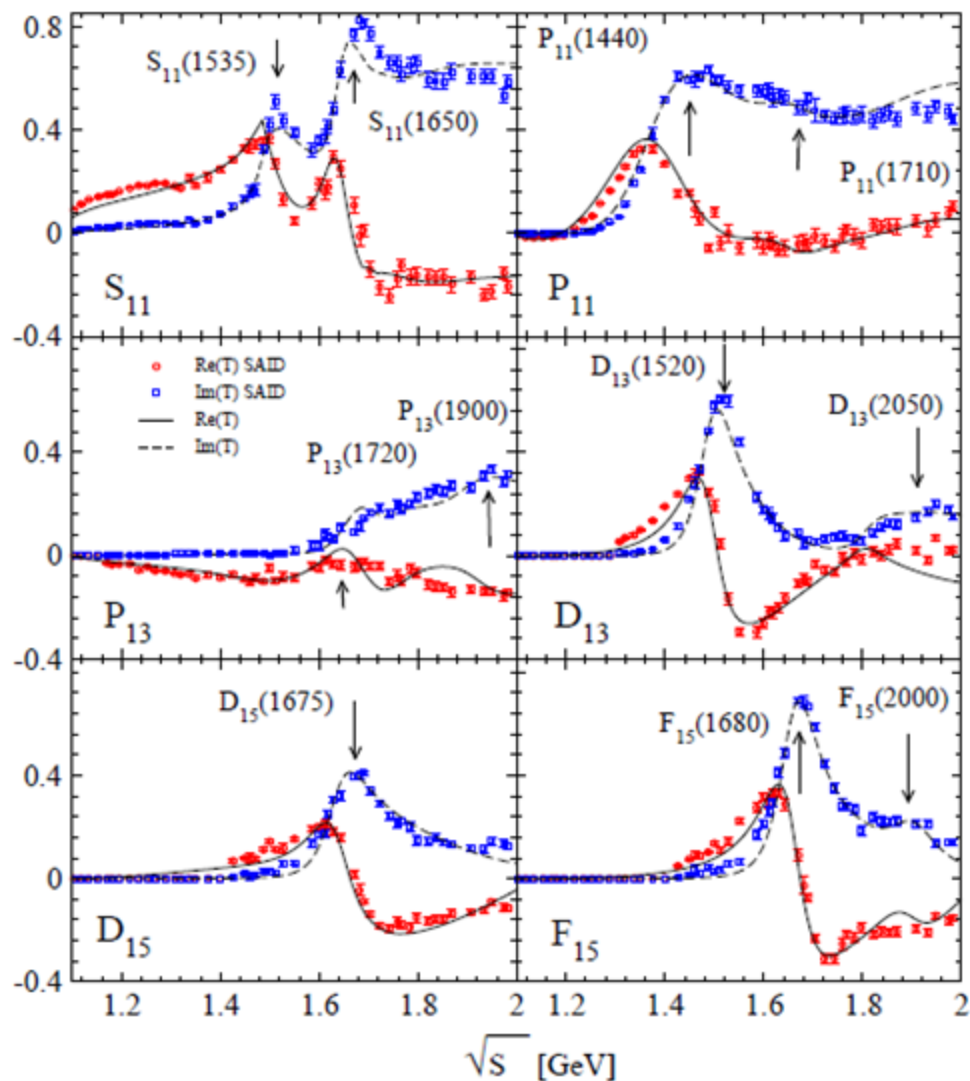


How many reaction channels?

$$T = \begin{pmatrix} T_{\gamma\gamma} & T_{\gamma\pi} & T_{\gamma\eta} & T_{\gamma\omega} & \dots \\ T_{\pi\gamma} & T_{\pi\pi} & T_{\pi\eta} & T_{\pi\omega} & \dots \\ T_{\eta\gamma} & T_{\eta\pi} & T_{\eta\eta} & T_{\eta\omega} & \dots \\ \dots & \dots & \dots & \dots & \dots \end{pmatrix}$$

- | | |
|---------------------------------|------------------------------|
| $\gamma N \rightarrow \gamma N$ | $\pi N \rightarrow \pi N$ |
| $\gamma N \rightarrow \pi N$ | $\pi N \rightarrow 2\pi N$ |
| $\gamma N \rightarrow \eta N$ | $\pi N \rightarrow \eta N$ |
| $\gamma N \rightarrow \omega N$ | $\pi N \rightarrow \omega N$ |
| $\gamma N \rightarrow K\Lambda$ | $\pi N \rightarrow K\Lambda$ |
| $\gamma N \rightarrow K\Sigma$ | $\pi N \rightarrow K\Sigma$ |

Results for pion-induced reactions



$l = \frac{1}{2}$ resonances important:

$S_{11}(1535)$, $S_{11}(1650)$
 $P_{11}(1440)$, $P_{11}(1710)$
 $P_{13}(1720)$, $P_{13}(1900)$
 $D_{13}(1520)$, $D_{13}(2050)$
 $D_{15}(1675)$
 $F_{15}(1680)$, $F_{15}(2000)$

2. Strangeness Production on the Nucleon

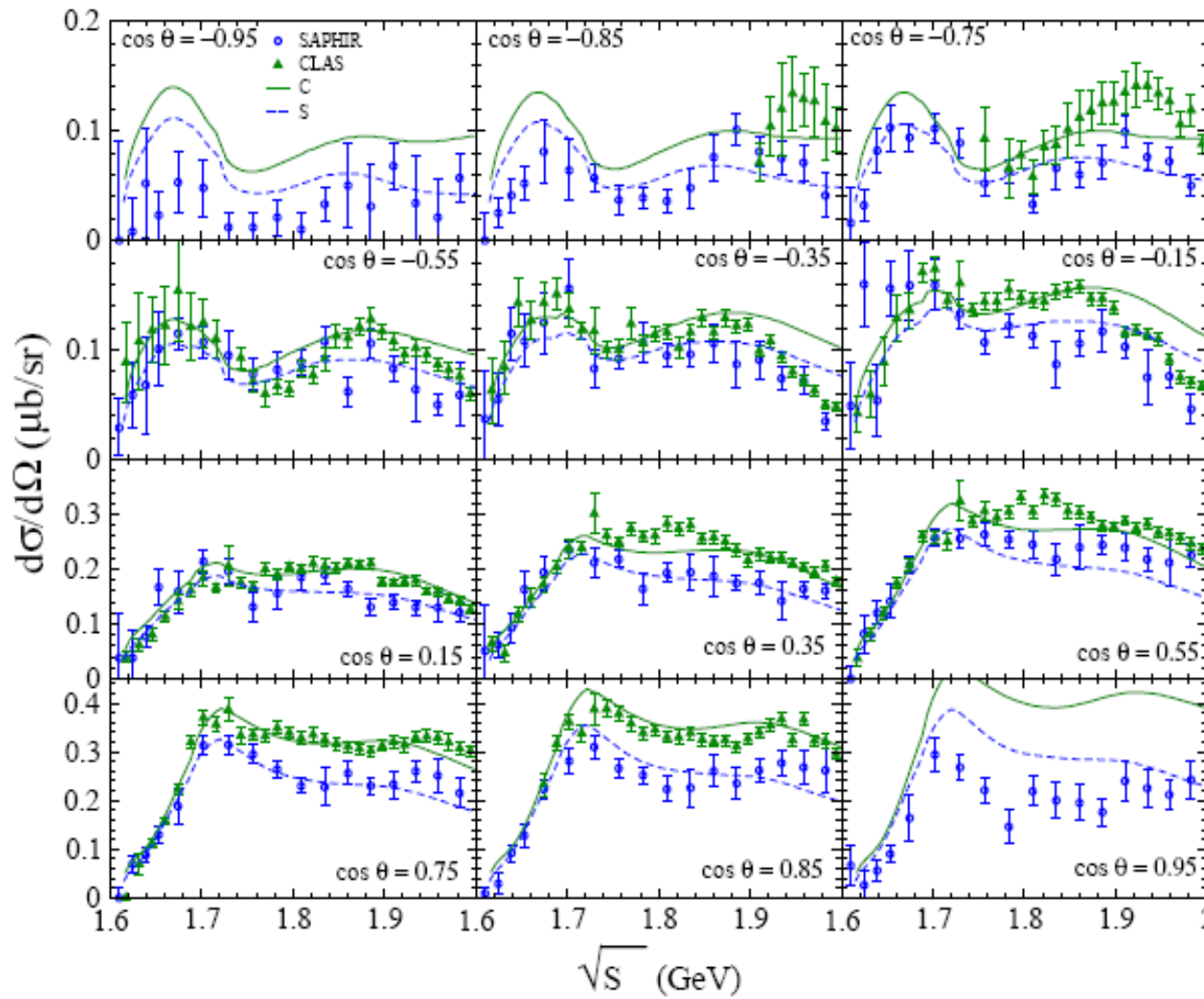


Strange decays of non-strange resonances. PDG:

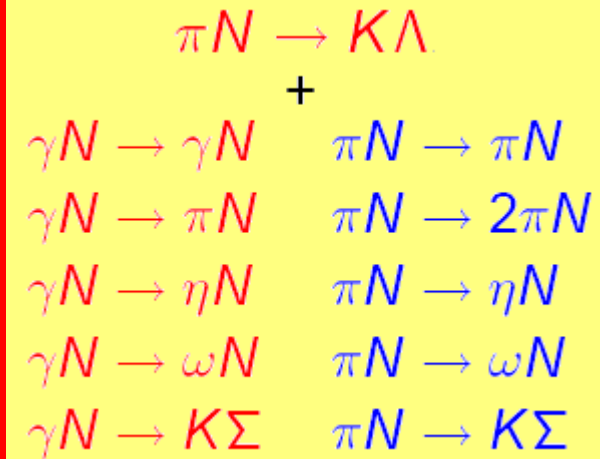
Resonance	$L_2 I_2 J$	Overall	ΛK	ΣK
$N(939)$	P_{11}	★★★★		
$N(1440)$	P_{11}	★★★★		
$N(1520)$	D_{13}	★★★★		
$N(1535)$	S_{11}	★★★★		
$N(1650)$	S_{11}	★★★★	★★★	★★
$N(1675)$	D_{15}	★★★★	*	
$N(1680)$	F_{15}	★★★★		
$N(1700)$	D_{13}	★★★	★★	*
$N(1710)$	P_{11}	★★★	★★	*
$N(1720)$	P_{13}	★★★★	★★	*
$N(1900)$	P_{13}	★★		
$N(1990)$	F_{17}	★★	*	
$N(2000)$	F_{15}	★★	*	*
$\Delta(1232)$	P_{33}	★★★★	—	
$\Delta(1600)$	P_{33}	★★★	—	
$\Delta(1620)$	S_{31}	★★★★	—	
$\Delta(1700)$	D_{33}	★★★★	—	*
$\Delta(1750)$	P_{31}	*	—	
$\Delta(1900)$	S_{31}	★★	—	*
$\Delta(1905)$	F_{35}	★★★★	—	*
$\Delta(1910)$	P_{31}	★★★★	—	*
$\Delta(1920)$	P_{33}	★★★	—	*
$\Delta(1930)$	D_{35}	★★★	—	*
$\Delta(1940)$	D_{33}	*	—	
$\Delta(1950)$	F_{37}	★★★★	—	*
$\Delta(2000)$	F_{35}	★★	—	

No firm information !

$\gamma p \rightarrow K\Lambda$ Results from the Giessen Model



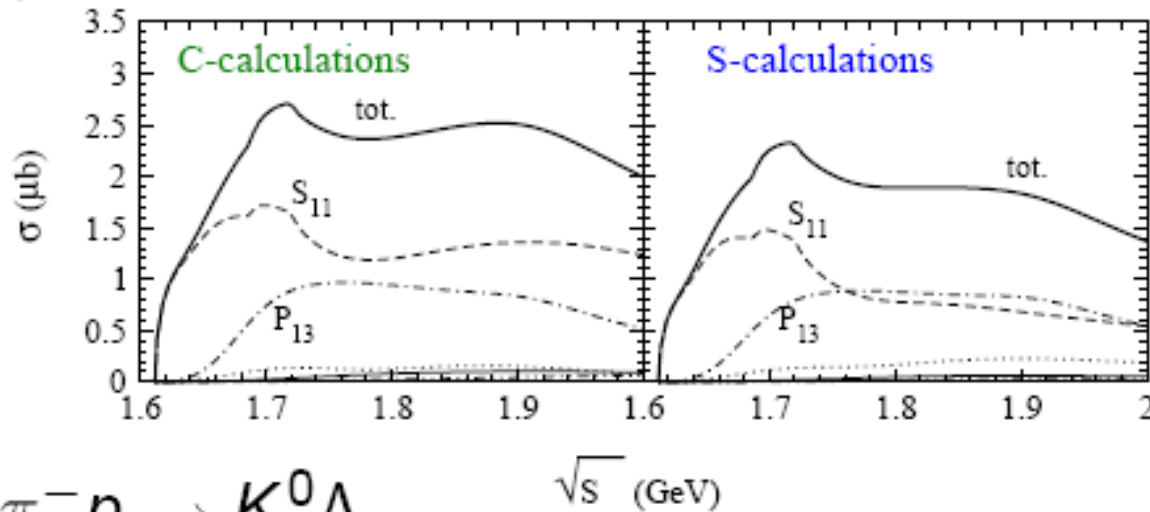
- separate fits to SAPHIR and CLAS data
- constraints from other hadronic and γ channels



Resonance contributions:

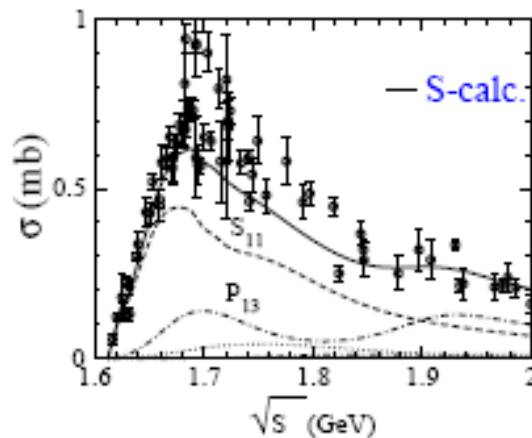
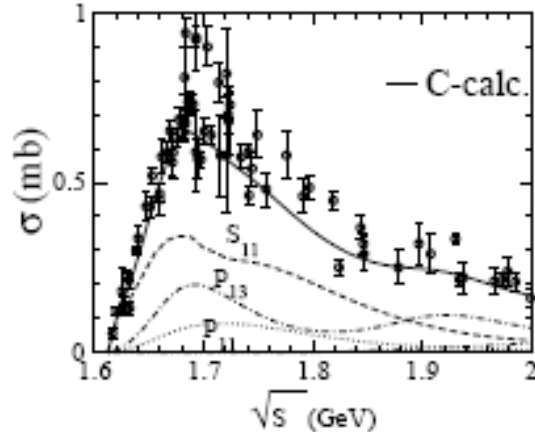
$S_{11}(1650)$ $P_{13}(1720)$ and $P_{13}(1900)$

$\gamma p \rightarrow K^+ \Lambda$



$\pi^- p \rightarrow K^0 \Lambda$

\sqrt{s} (GeV)



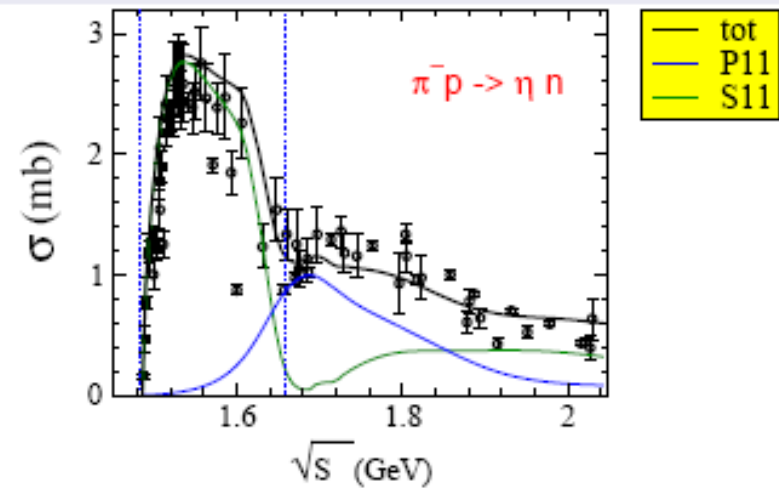
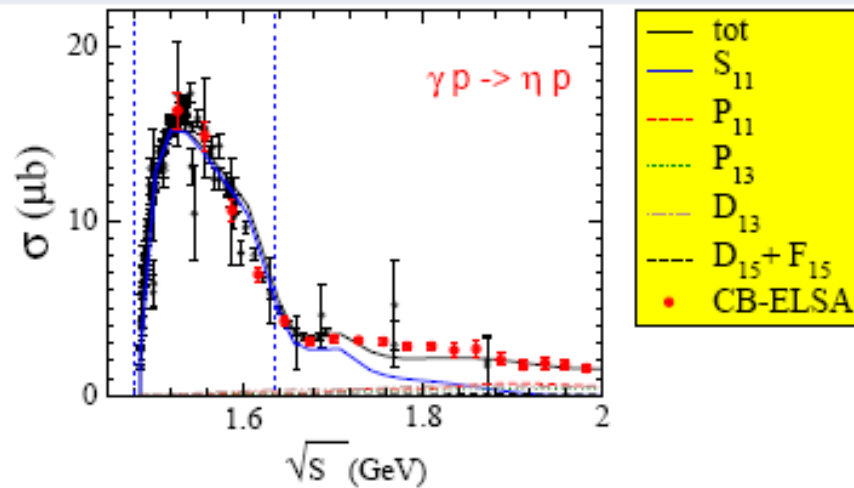
Consequences on
Reaction Dynamics
of $K\Lambda$ Channels
from CLAS/SAPHIR
Solutions

3. η -Production on the Nucleon



Photo- & Hadro-Production of η on the Proton

$S_{11}(1535)$ dominates
both $\gamma p \rightarrow \eta p$ and $\pi^- p \rightarrow \eta n$ reactions



- dominated by $S_{11}(1535)$
- 5/2-Partial waves account for high energy tail

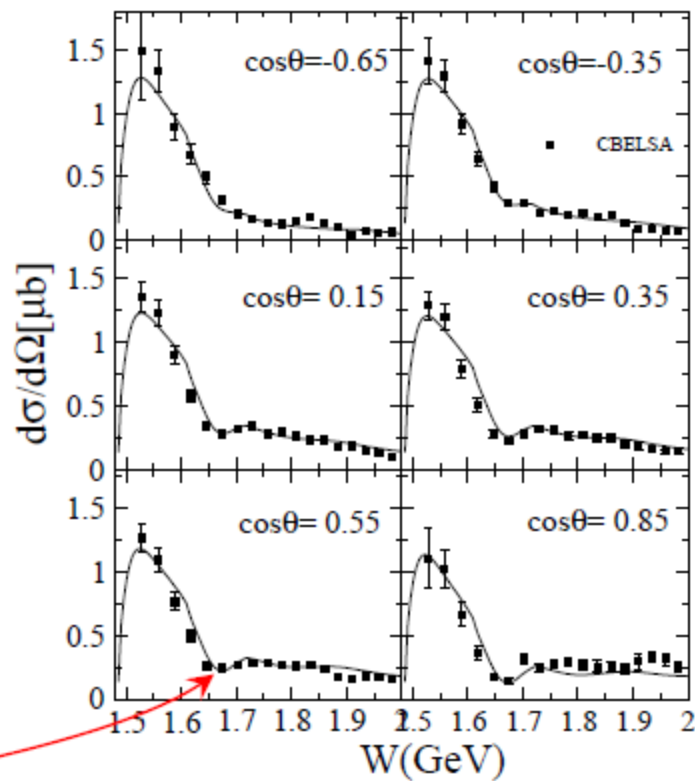
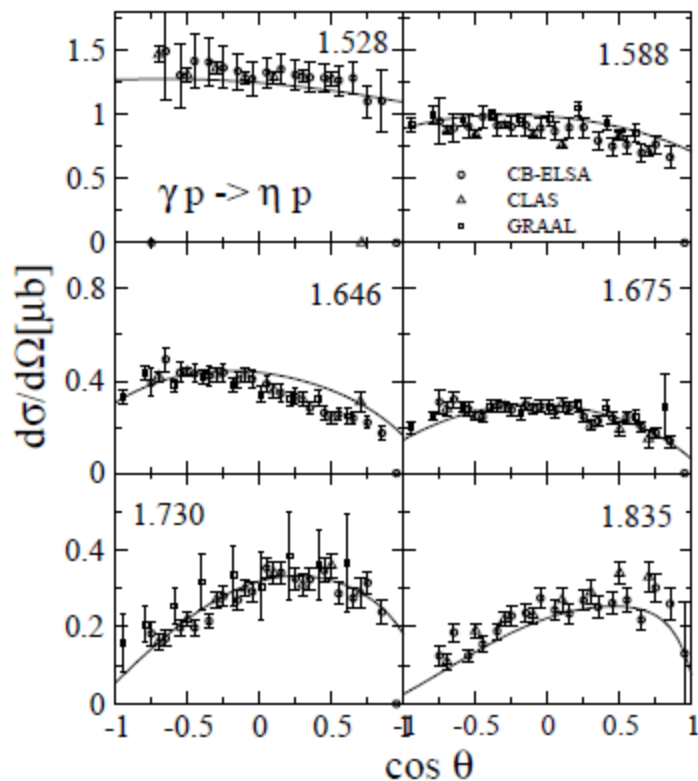
- destructive interference by $S_{11}(1650)$
- importance of $P_{11}(1710)$ above $\sim 1600\text{MeV}$

Results for the $\gamma p \rightarrow \eta p$

First peak - well known $S_{11}(1535)$

$\frac{d\sigma}{d\Omega}$ as a function of $\cos(\theta)$

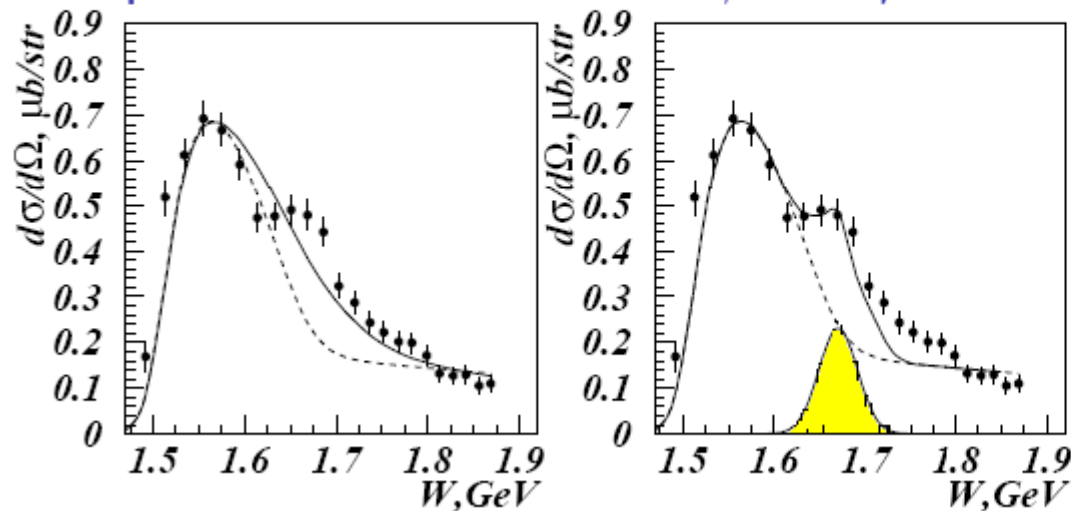
$\frac{d\sigma}{d\Omega}$ as a function of W



The structure at 1.67 GeV in $\gamma p \rightarrow \eta p$ is due to $S_{11}(1650)$
no need for any exotic state!

Excitement in eta-Production on the neutron: Indications for a new sharp resonance?

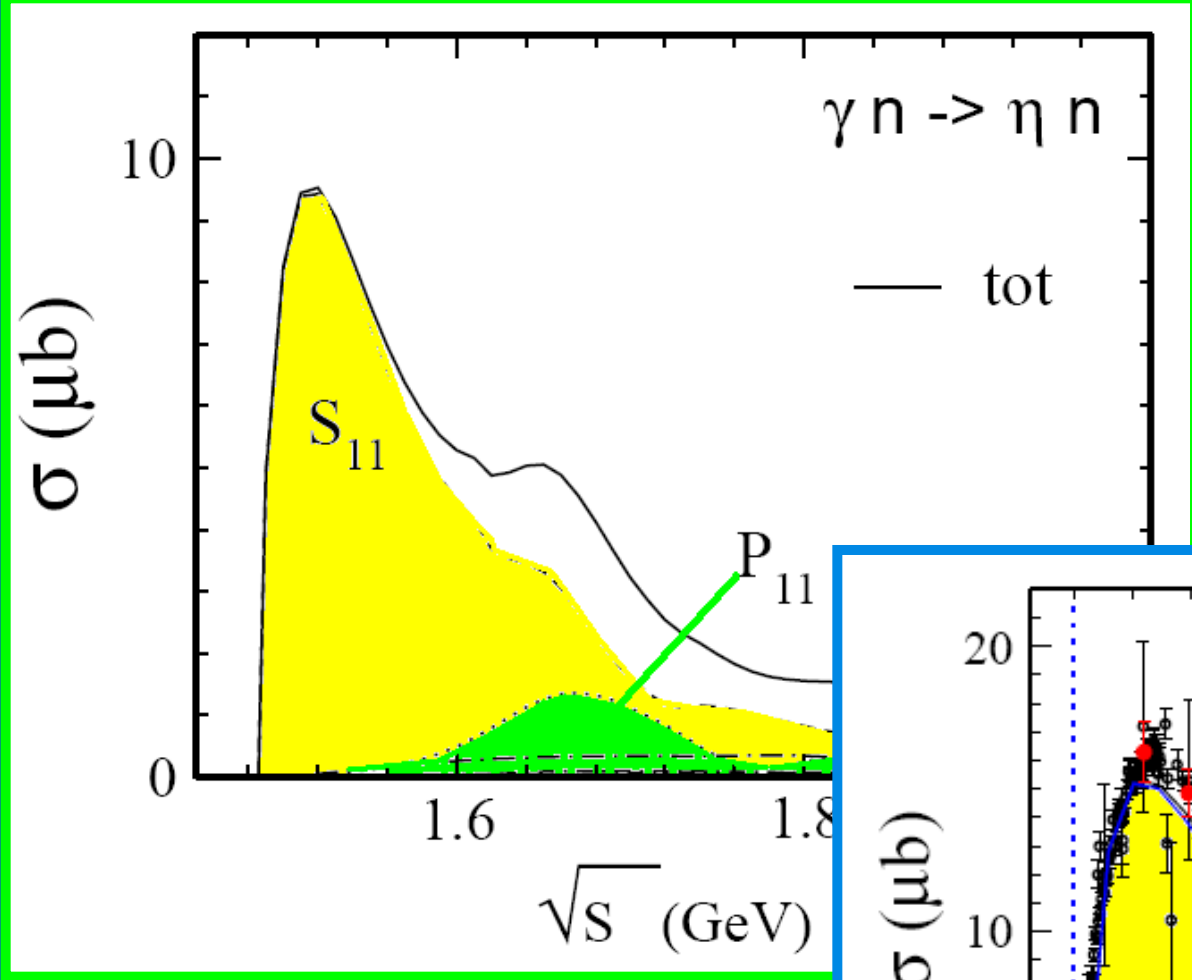
Polyakov, Azimov, Strakovsky, Arndt, Kuznetsov:
predict a narrow N^* in $\gamma n \rightarrow \eta n$ at 1.67 GeV.



First result from GRAAL:
 $\gamma n^* \rightarrow \eta n$ above 1.6 GeV
(V. Kuznetsov et al.,
hep-ex/0601002) observe a
resonance-like structure at
1.65 GeV

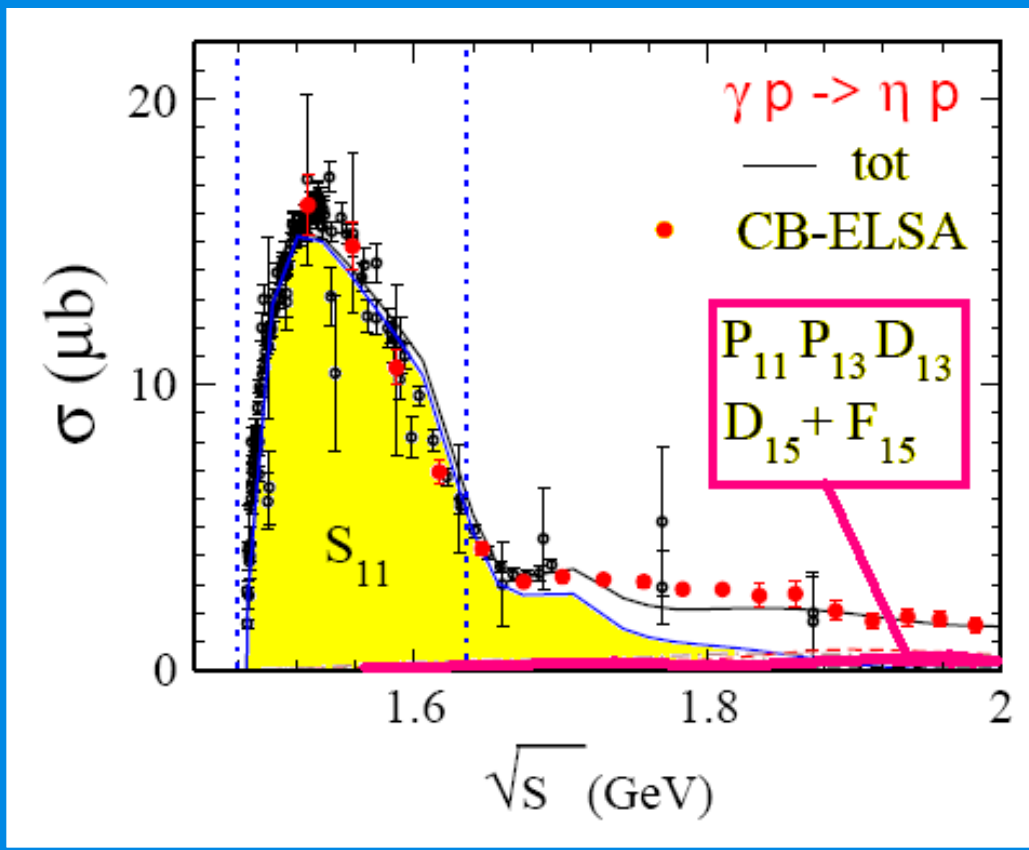
new resonance ?

Actual experiment: quasi-free eta-Production on the deuteron



**GiM CC-Results
eta-Production on
the Neutron**

**GiM CC-Results
eta-Production on
the Proton**



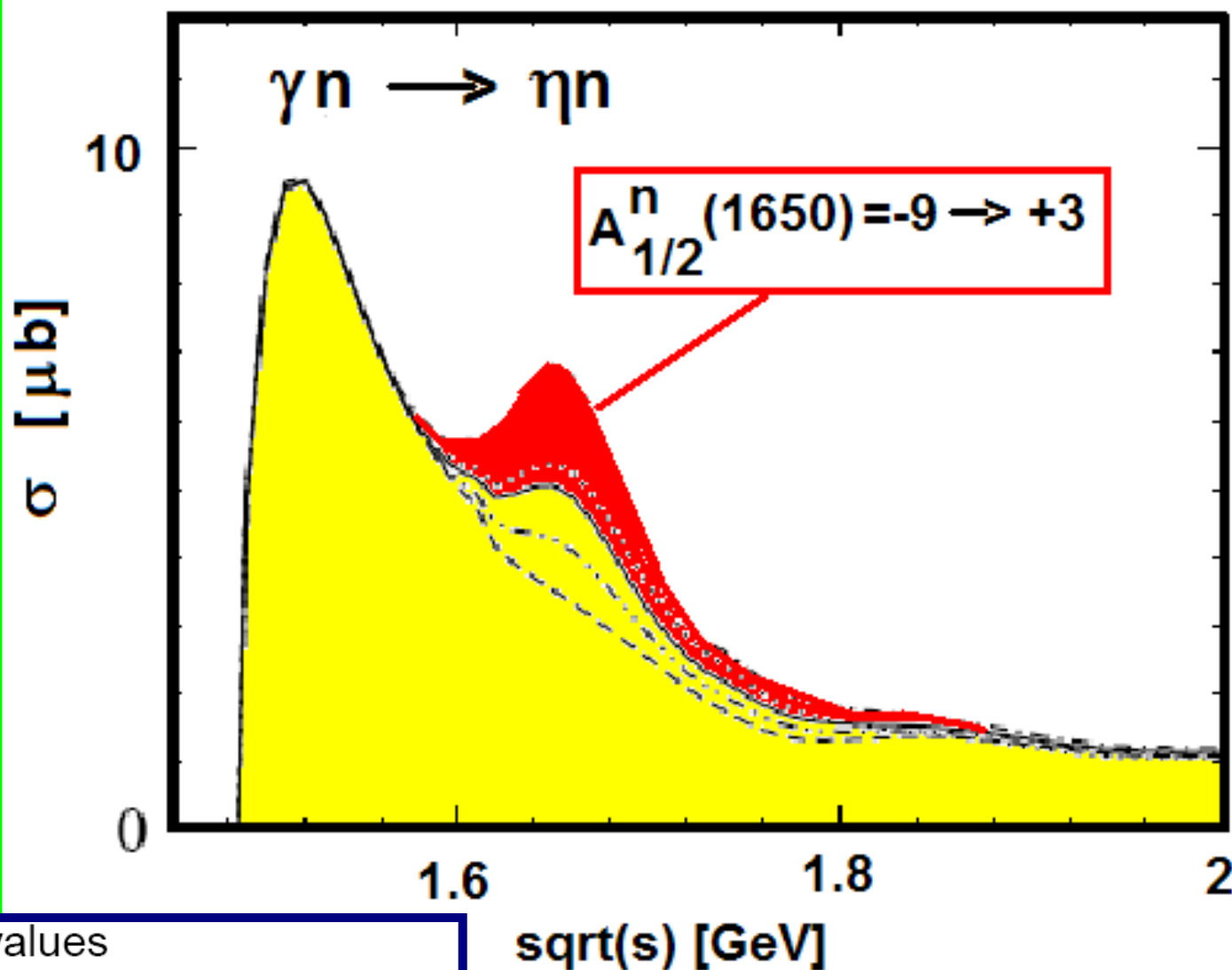
Resonance parameters

Giessen model, PLB650 172 (2007)

N^*	$\Gamma_{\eta N}$	$A_{\frac{1}{2}}^p$	$A_{\frac{1}{2}}^n$
$S_{11}(1535)$ (Giessen)	56.2	95	-74
(PDG)	53 ± 1	90 ± 30	-46 ± 27
$S_{11}(1650)$ (Giessen)	2.5	57	-9
(PDG)	2.3 ± 2	53 ± 16	-15 ± 21
$P_{11}(1710)$ (Giessen)	42	-50	+24
(PDG)	21 ± 16	$+9 \pm 22$	-2 ± 14

Table: Helicity amplitudes (in $10^{-3} \text{GeV}^{-\frac{1}{2}}$) and branching ratios to ηN . First line: parameters obtained in the present calculations. Second line: PDG values.

Results for $\gamma n \rightarrow \eta n$: Variation of Partial Wave Amplitude



Central values

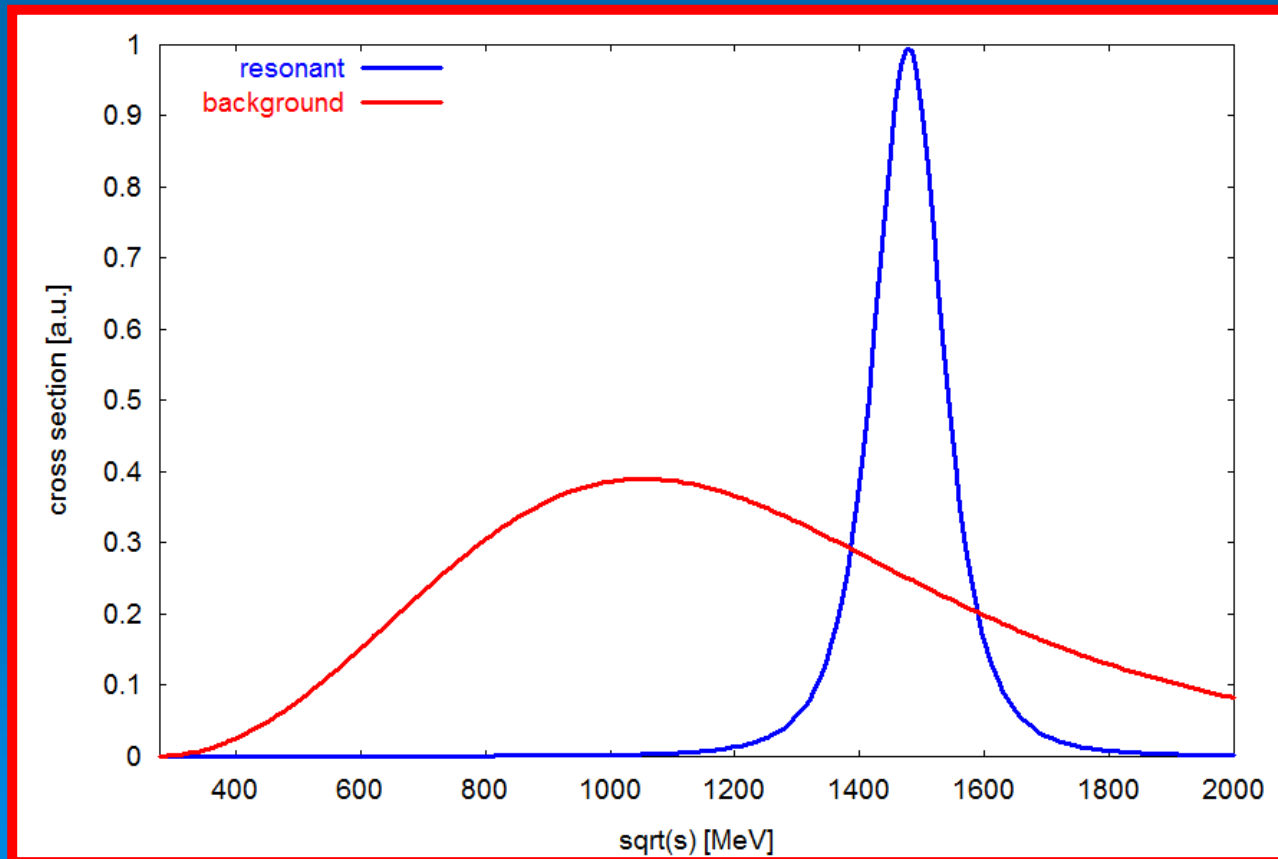
$$A_{1/2}^n(1650) = -9 \times 10^{-3} \text{GeV}^{-\frac{1}{2}}$$

$$A_{1/2}^n(1710) = 24 \times 10^{-3} \text{GeV}^{-\frac{1}{2}}$$

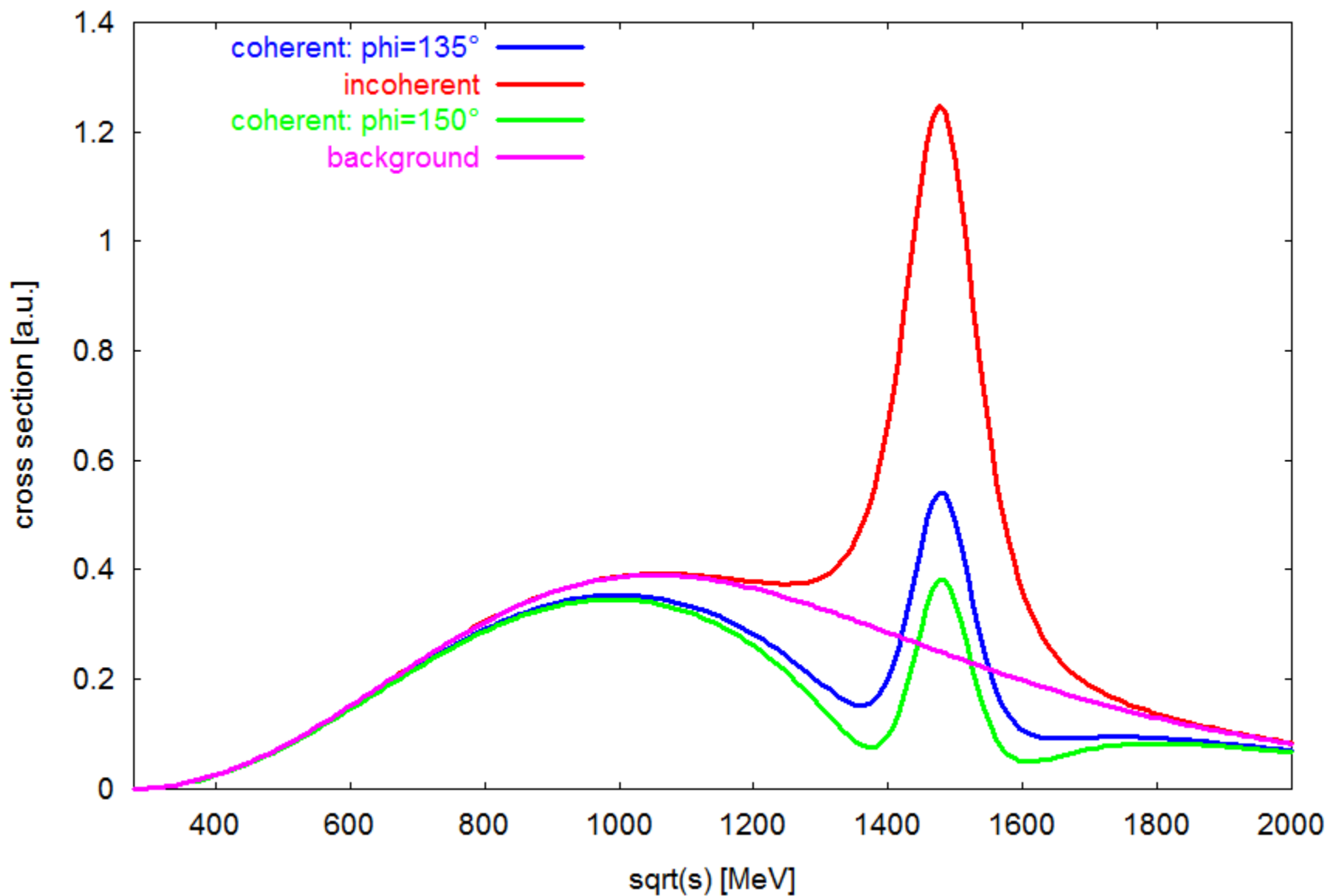
PLB650 172 (2007)

Interference: A simple model:

- Background amplitude $M_b(\sqrt{s})$
- Resonant amplitude $M_r(\sqrt{s}) \sim M_0 e^{i\phi} / (s - m_r^2 - i\sqrt{s}\Gamma(\sqrt{s}))$
- $\sigma_{\text{coh.}} \sim |M_b(\sqrt{s}) + M_r(\sqrt{s})|^2$
- $\sigma_{\text{incoh.}} \sim |M_b(\sqrt{s})|^2 + |M_r(\sqrt{s})|^2$



Interference Phenomenon



Summary and Outlook

- The Giessen K-Matrix Model
- Kaon (Strangeness) Production on the Proton
- η -Production on the Nucleon
- Caveats in Spectra: *It's a bump but not a resonance...*
- ongoing: 2-Pion dynamics
- also: Pion, Photon, Proton induced Production of Hypernuclei,
- and: Hypernuclei by Fragmentation in HIC (HypHI)
- in progress: $S=-1, -2$ Hypernuclei by Antiproton Annihilation on Nuclei \rightarrow PANDA@FAIR, and
- CC-effects and the X,Y,Z states

Main Contributors: V. Shklyar, S. Bender, Th. Gaitanos, R. Shyam