

Hirscheegg, 18/01/2011

# Deep Virtual Compton Scattering: From data to GPDs

M. Guidal, IPN Orsay

 *A few basic definitions/features of GPDs*

 *A DVCS fitter code*

Review of the data (JLab, HERMES)

First extractions of the  $H_{\text{Re}}$ ,  $H_{\text{Im}}$  and  $\tilde{H}_{\text{Im}}$  CFFs

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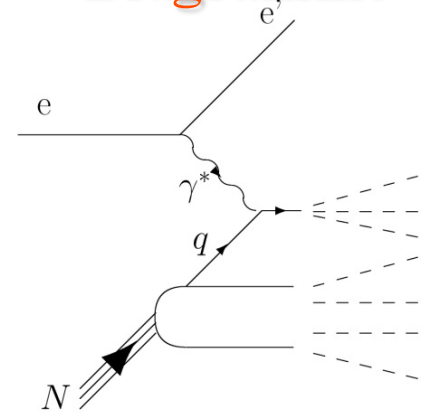
Process

Diagramme

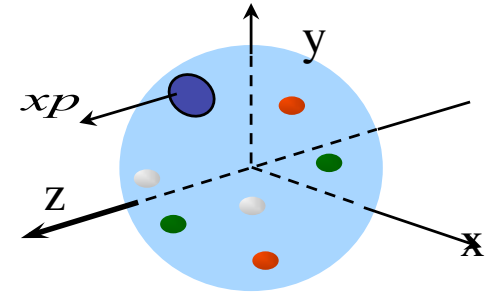
Structure function

Interpretation

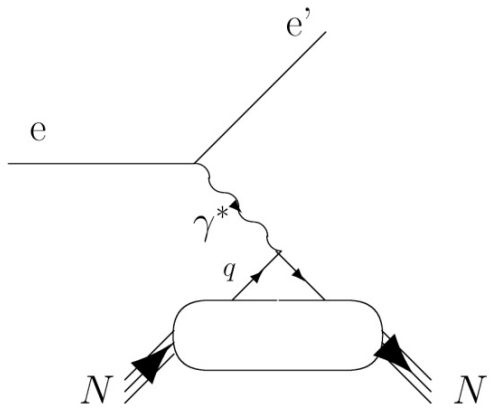
ep → eX



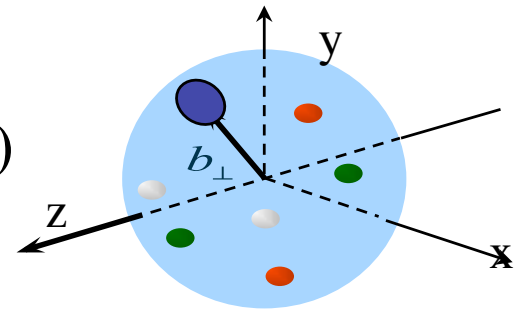
$$f_1(x), g_1(x)$$



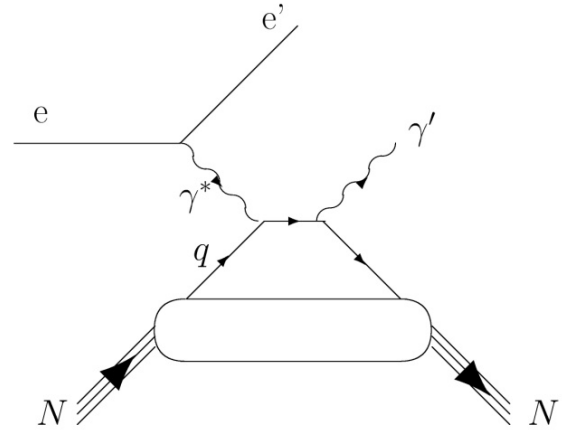
ep → ep



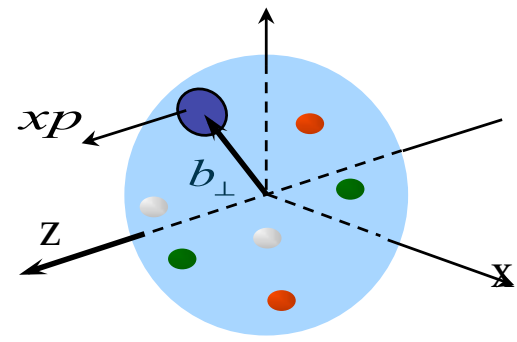
$$F_1(t), F_2(t), G_A(t), G_P(t)$$



ep → epγ

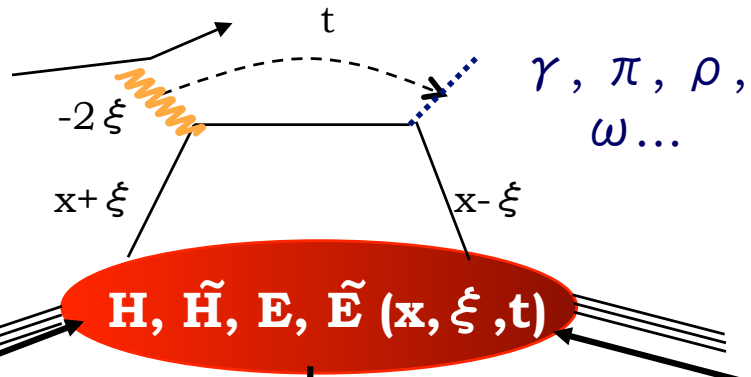


$$H(x, \xi, t), E(x, \xi, t), \tilde{H}(x, \xi, t), \tilde{E}(x, \xi, t)$$



**(restricting myself to LT-LO, chiral even, quark sector)**





**Elastic Form Factors**

$\int H(x, \xi, t) dx = F(t)$  (A)

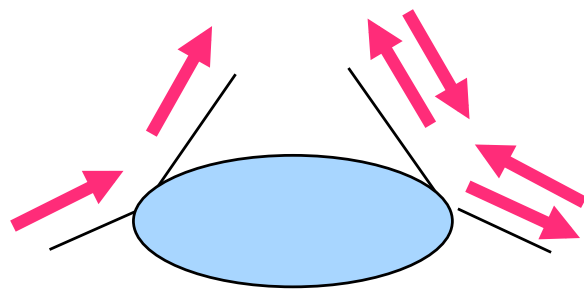
**Ji's sum rule**

$2J_q = \int x(H+E)(x, \xi, 0) dx$

$\frac{1}{2} = \left( \frac{1}{2} \Delta\Sigma + L_q \right) + (\Delta G + L_g)$

**Standard Parton Distributions**

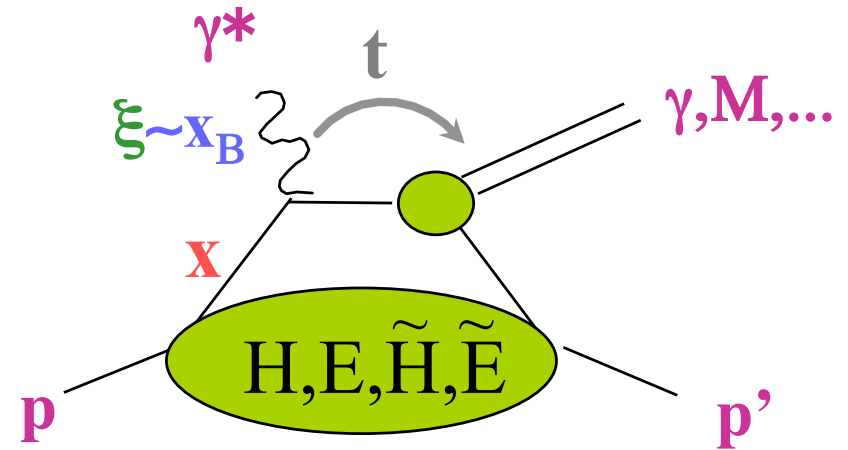
$H^q(x, 0, 0) = q(x),$   
 $\tilde{H}^q(x, 0, 0) = \Delta q(x)$



|                            |                         |                  |
|----------------------------|-------------------------|------------------|
| $H$                        | $E$                     | $q$ spin average |
| $\tilde{H}$                | $\tilde{E}$             | $q$ spin diff.   |
| $N$ spin<br><i>no flip</i> | $N$ spin<br><i>flip</i> |                  |

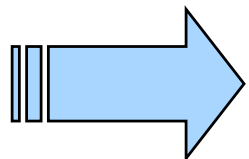
$H^q(\mathbf{x}, \xi, t)$  but only  $\xi$  and  $t$  accessible experimentally

$$\xi = \frac{x_B/2}{1 - x_B/2} \quad t = (p - p')^2$$



$$\mathbf{x} \neq x_B !$$

$$\frac{d\sigma}{d\xi dt} \sim \left| A \int_{-1}^1 \frac{H^q(\mathbf{x}, \xi, t)}{x - \xi + i\epsilon} d\mathbf{x} + B \int_{-1}^1 \frac{E^q(\mathbf{x}, \xi, t)}{x - \xi + i\epsilon} d\mathbf{x} + \dots \right|^2$$



$\mathbf{x}$  : mute variable

*Deconvolution needed!*

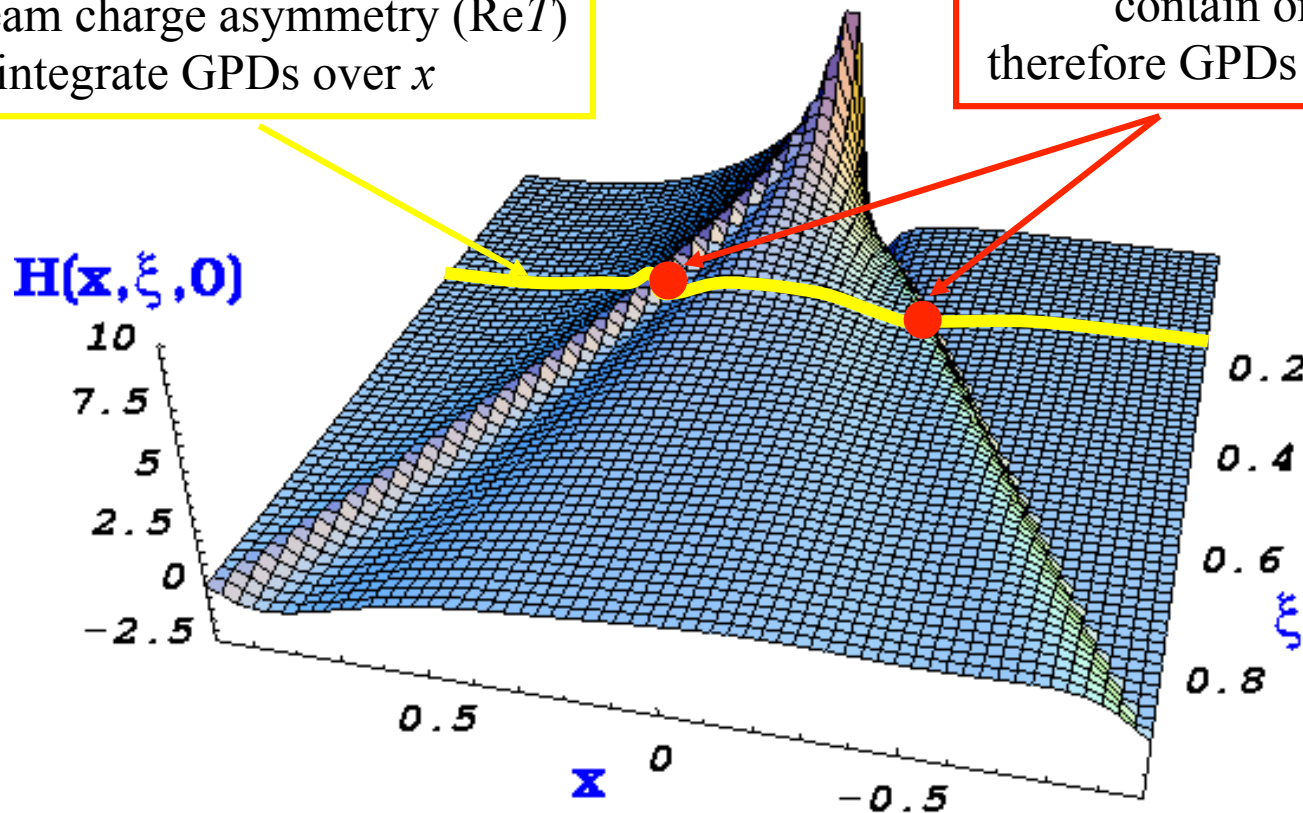
## GPD and DVCS

(at leading order:)

$$T^{DVCS} \sim \int_{-1}^{+1} \frac{H(x, \xi, t)}{x \pm \xi + i\varepsilon} dx + \dots \sim P \int_{-1}^{+1} \frac{H(x, \xi, t)}{x \pm \xi} dx - i\pi H(\pm\xi, \xi, t) + \dots$$

Cross-section measurement  
and beam charge asymmetry ( $\text{Re}T$ )  
integrate GPDs over  $x$

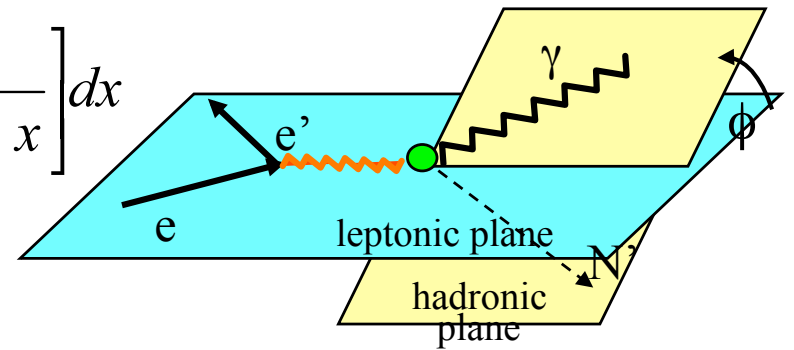
Beam or target spin asymmetry  
contain only  $\text{Im}T$ ,  
therefore GPDs at  $x = \xi$  and  $-\xi$



# Extracting GPDs from DVCS observables

$$\text{Re}\mathcal{H}_q = e_q^2 P \int_0^{+1} \left( H^q(x, \xi, t) - H^q(-x, \xi, t) \right) \left[ \frac{1}{\xi - x} + \frac{1}{\xi + x} \right] dx$$

$$\text{Im}\mathcal{H}_q = \pi e_q^2 \left[ H^q(\xi, \xi, t) - H^q(-\xi, \xi, t) \right]$$

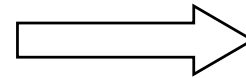


$$\xi = x_B / (2 - x_B) \quad k = -t / 4M^2$$

Proton Neutron

Polarized beam, unpolarized target (BSA) :

$$\Delta\sigma_{LU} \sim \sin\phi \text{Im} \{ F_1 \mathcal{H} + \xi(F_1 + F_2) \tilde{\mathcal{H}} - k F_2 \mathcal{E} \} d\phi$$

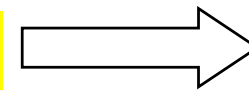


$$\text{Im} \{ \mathcal{H}_p, \tilde{\mathcal{H}}_p, \mathcal{E}_p \}$$

$$\text{Im} \{ \mathcal{H}_n, \tilde{\mathcal{H}}_n, \mathcal{E}_n \}$$

Unpolarized beam, longitudinal target (ITSA) :

$$\Delta\sigma_{UL} \sim \sin\phi \text{Im} \{ F_1 \tilde{\mathcal{H}} + \xi(F_1 + F_2) (\mathcal{H} + x_B/2 \mathcal{E}) - \xi k F_2 \tilde{\mathcal{E}} + \dots \} d\phi$$

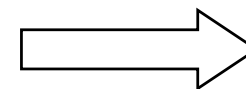


$$\text{Im} \{ \mathcal{H}_p, \tilde{\mathcal{H}}_p \}$$

$$\text{Im} \{ \mathcal{H}_n, \mathcal{E}_n, \tilde{\mathcal{E}}_n \}$$

Polarized beam, longitudinal target (BITSA) :

$$\Delta\sigma_{LL} \sim (A + B \cos\phi) \text{Re} \{ F_1 \tilde{\mathcal{H}} + \xi(F_1 + F_2) (\mathcal{H} + x_B/2 \mathcal{E}) \dots \} d\phi$$

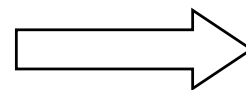


$$\text{Re} \{ \mathcal{H}_p, \tilde{\mathcal{H}}_p \}$$

$$\text{Re} \{ \mathcal{H}_n, \mathcal{E}_n, \tilde{\mathcal{E}}_n \}$$

Unpolarized beam, transverse target (tTSA) :

$$\Delta\sigma_{UT} \sim \sin\phi \text{Im} \{ k(F_2 \mathcal{H} - F_1 \mathcal{E}) + \dots \} d\phi$$



$$\text{Im} \{ \mathcal{H}_p, \mathcal{E}_p \}$$

$$\text{Im} \{ \mathcal{H}_n \}$$

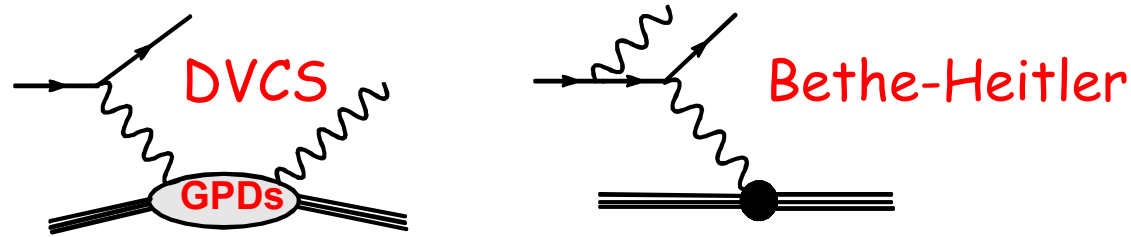
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Given the well-established **LT-LO** DVCS+BH amplitude



Can one recover the **CFFs** from data ?

$$\text{Obs} = \text{Amp}(\text{DVCS+BH}) \otimes \text{CFFs}$$

Model-independent fit, at fixed  $x_B$ ,  $t$  and  $Q^2$ ,  
of DVCS observables with  
**MINUIT + MINOS**

**8** unknowns (the CFFs), non-linear problem, strong correlations

Only **3** CFFs come out from the fit with finite error bars:

$$H_{\text{Im}}, \tilde{H}_{\text{Im}} \text{ and } H_{\text{Re}}$$

## Compton Form Factors

$$H_{Re} = P \int_0^1 dx [H(x, \xi, t) - H(-x, \xi, t)] C^+(x, \xi) \quad (1)$$

$$E_{Re} = P \int_0^1 dx [E(x, \xi, t) - E(-x, \xi, t)] C^+(x, \xi) \quad (2)$$

$$\tilde{H}_{Re} = P \int_0^1 dx [\tilde{H}(x, \xi, t) + \tilde{H}(-x, \xi, t)] C^-(x, \xi) \quad (3)$$

$$\tilde{E}_{Re} = P \int_0^1 dx [\tilde{E}(x, \xi, t) + \tilde{E}(-x, \xi, t)] C^-(x, \xi) \quad (4)$$

$$H_{Im} = H(\xi, \xi, t) - H(-\xi, \xi, t), \quad (5)$$

$$E_{Im} = E(\xi, \xi, t) - E(-\xi, \xi, t), \quad (6)$$

$$\tilde{H}_{Im} = \tilde{H}(\xi, \xi, t) + \tilde{H}(-\xi, \xi, t) \quad \text{and} \quad (7)$$

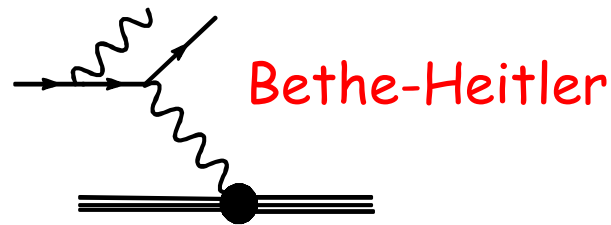
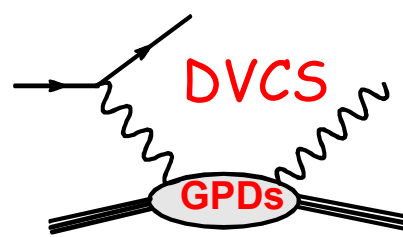
$$\tilde{E}_{Im} = \tilde{E}(\xi, \xi, t) + \tilde{E}(-\xi, \xi, t) \quad (8)$$

with

$$C^\pm(x, \xi) = \frac{1}{x - \xi} \pm \frac{1}{x + \xi}. \quad (9)$$

(in practice,  $\tilde{\mathbf{E}}_{Im}$  set to  $\mathbf{0}$ )

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M.G. EPJA 37 (2008) 319

M.G. & H. Moutarde, EPJA 42 (2009) 71

M.G. PLB 689 (2010) 156

M.G. PLB 693 (2010) 17



# The experimental actors

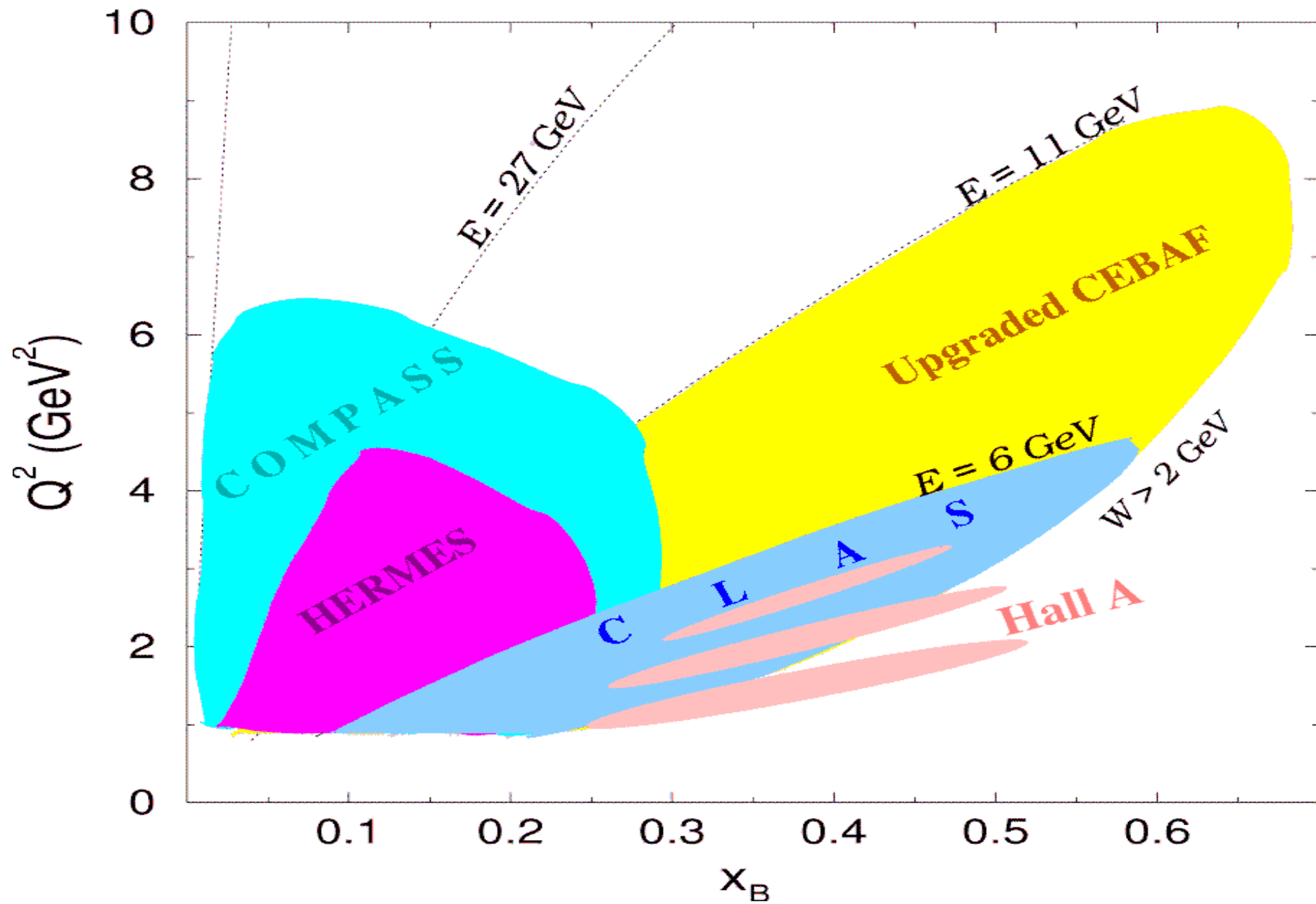


| JLab                    |                      |
|-------------------------|----------------------|
| Hall A                  | Hall B               |
| p-DVCS<br>(Bpol.) X-sec | p-DVCS<br>BSAs,ITSAs |



| DESY                                  |                     |
|---------------------------------------|---------------------|
| HERMES                                | H1/ZEUS             |
| p-DVCS<br>BSA,BCA,<br>tTSA,ITSA,BITSA | p-DVCS<br>X-sec,BCA |

| CERN  |
|---|
| COMPASS                                     |
| p-DVCS<br>X-sec,BSA,BCA,<br>tTSA,ITSA,BITSA |



HALL A

*DVCS@JLab*

$ep \rightarrow e\gamma$



Polarized Electron Beam

LH<sub>2</sub> / LD<sub>2</sub> target

Scattered Electron

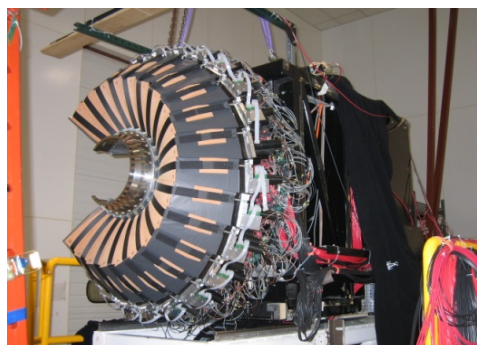
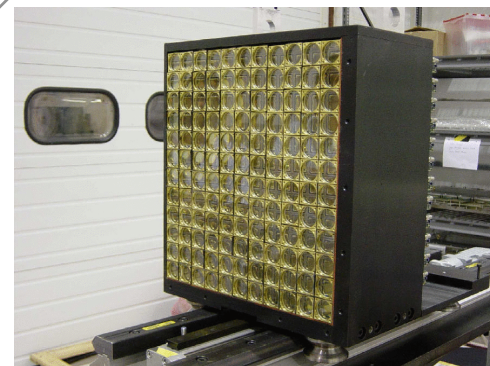
Left HRS

$$M_X^2 = (k + p - k' - q')^2$$

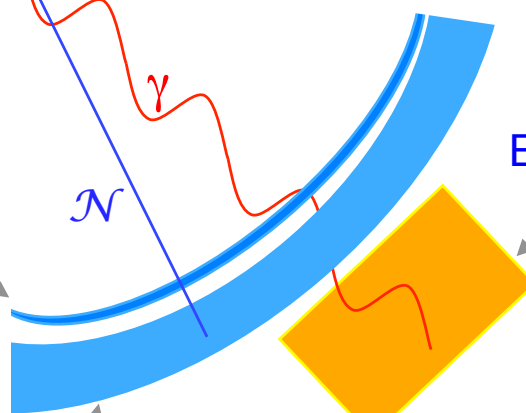


Charged Particle Tagger

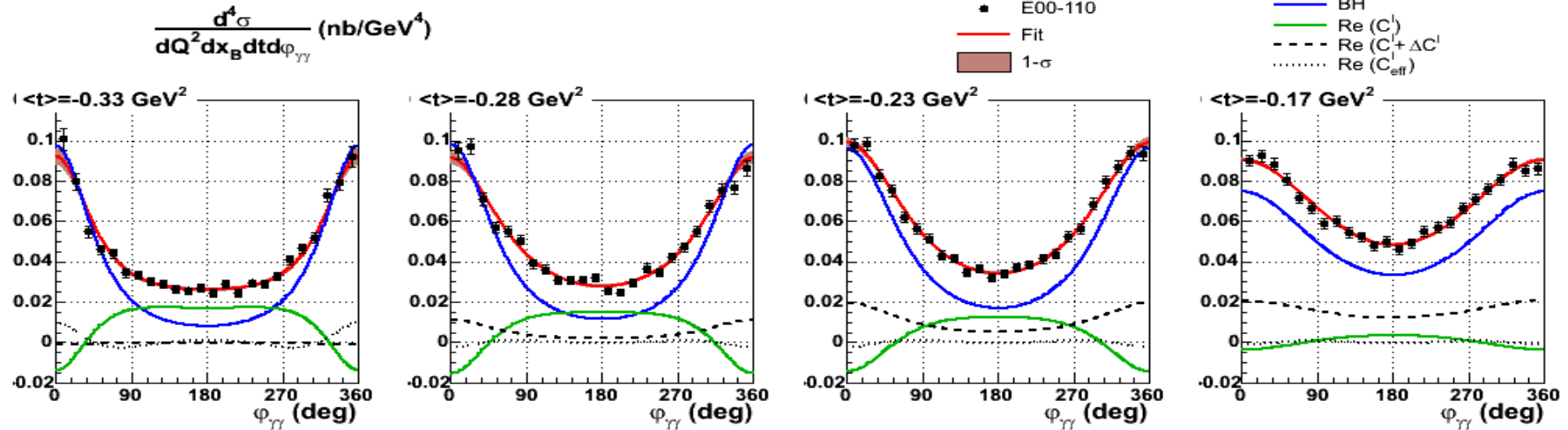
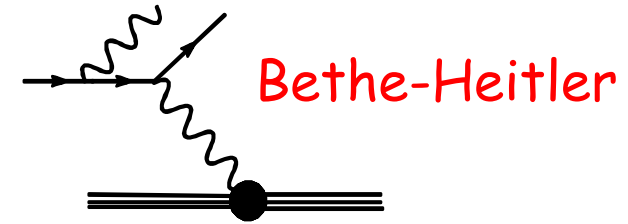
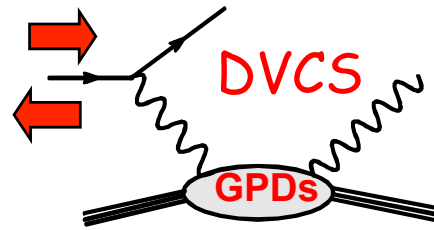
Electromagnetic Calorimeter



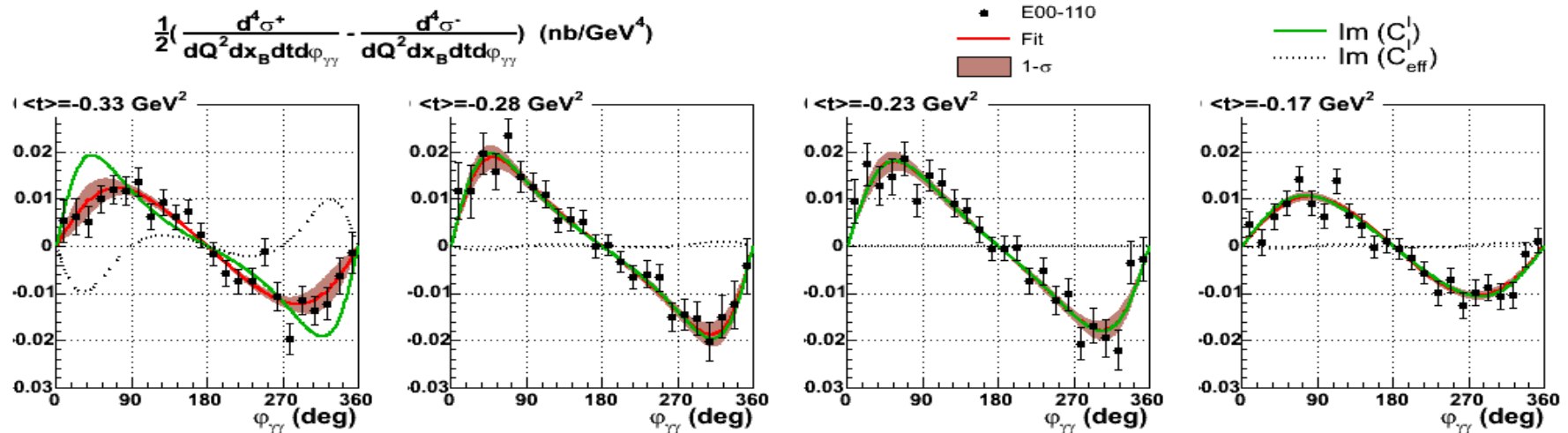
Nucleon Detector



## Unpolarized cross sections

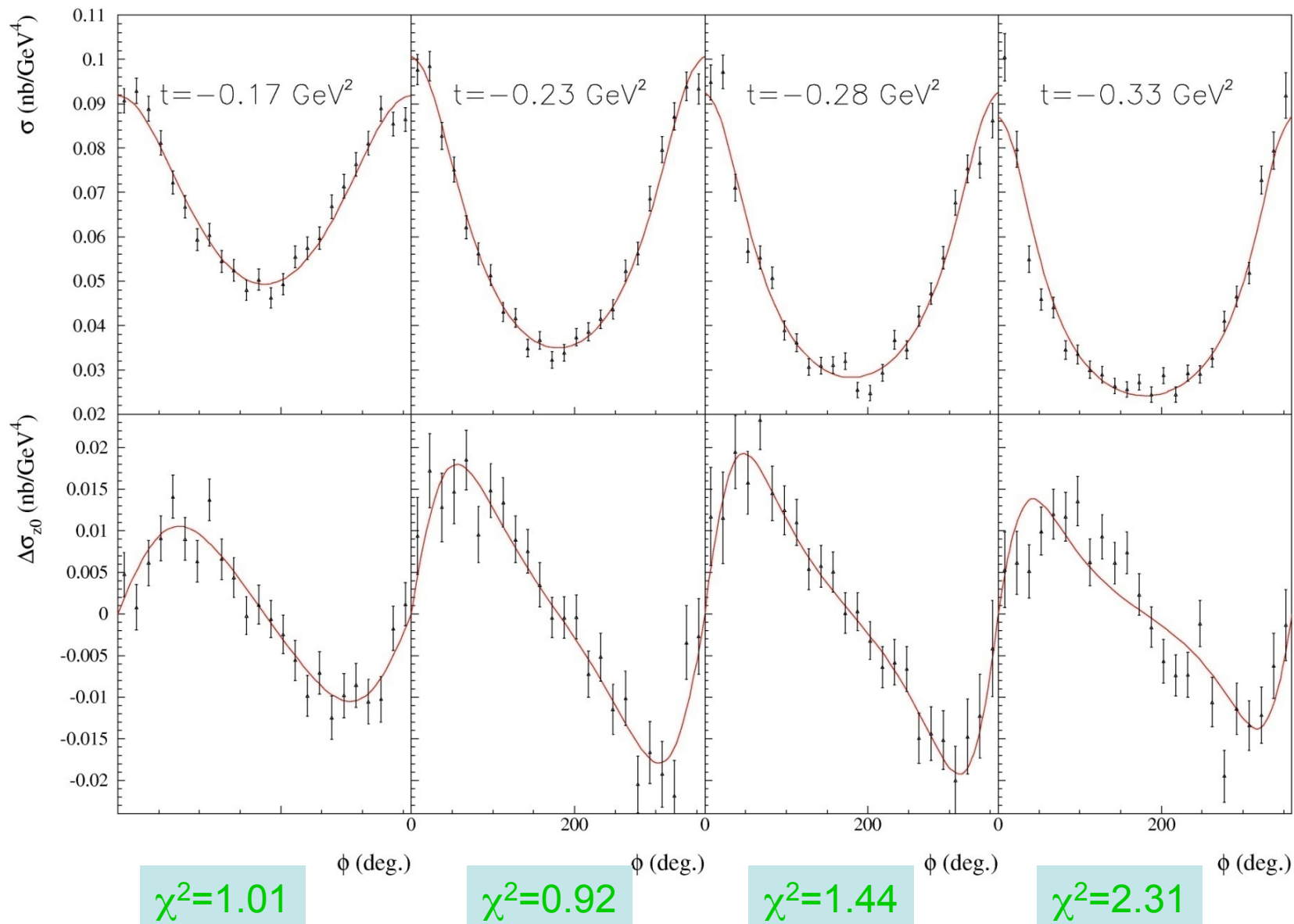


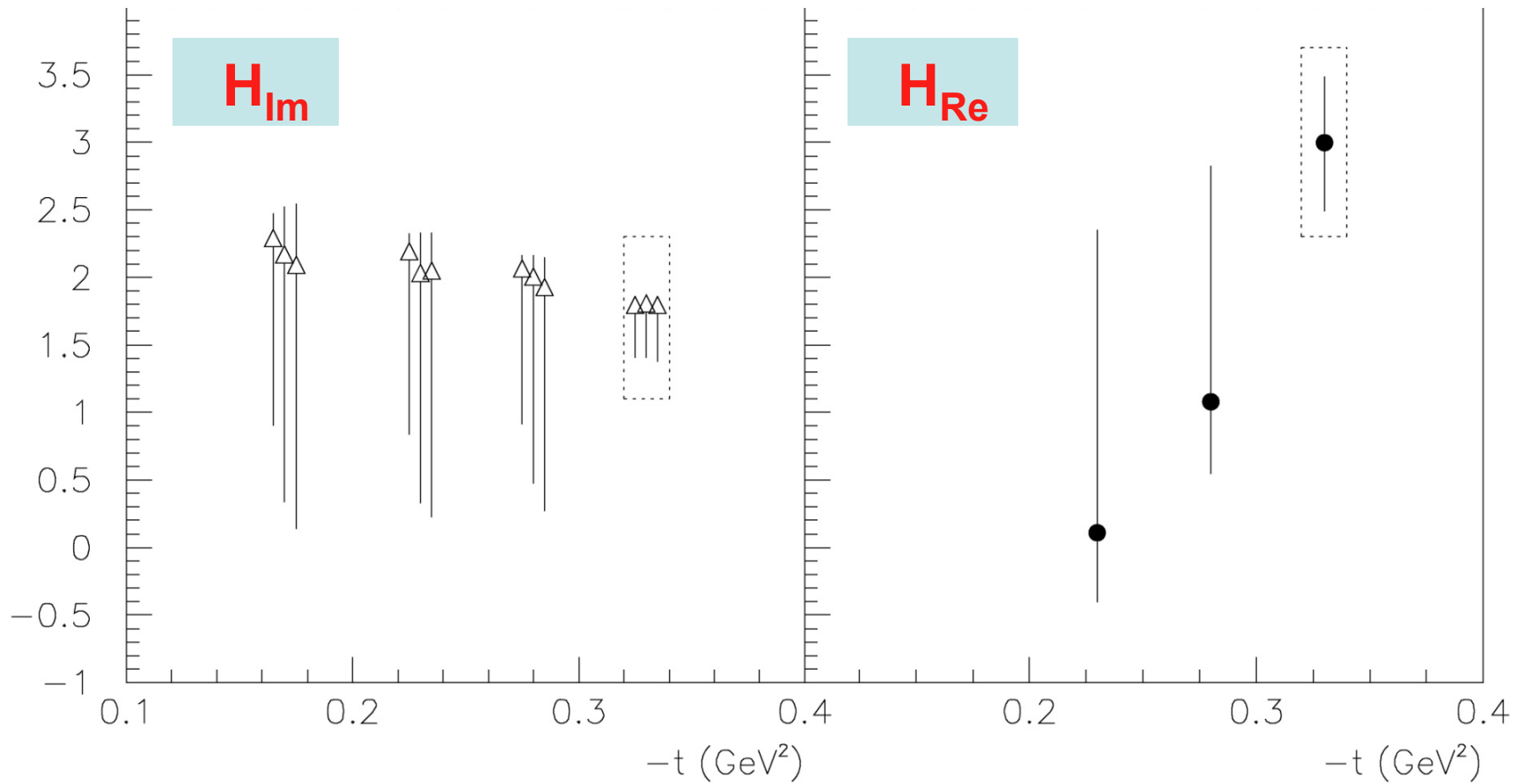
## Difference of (beam-)polarized cross sections



# Hall A : $\sigma$ & $\sigma_{z0}$ , $x_B=0.36, Q^2=2.3, t=.17,.23,.28,.33$

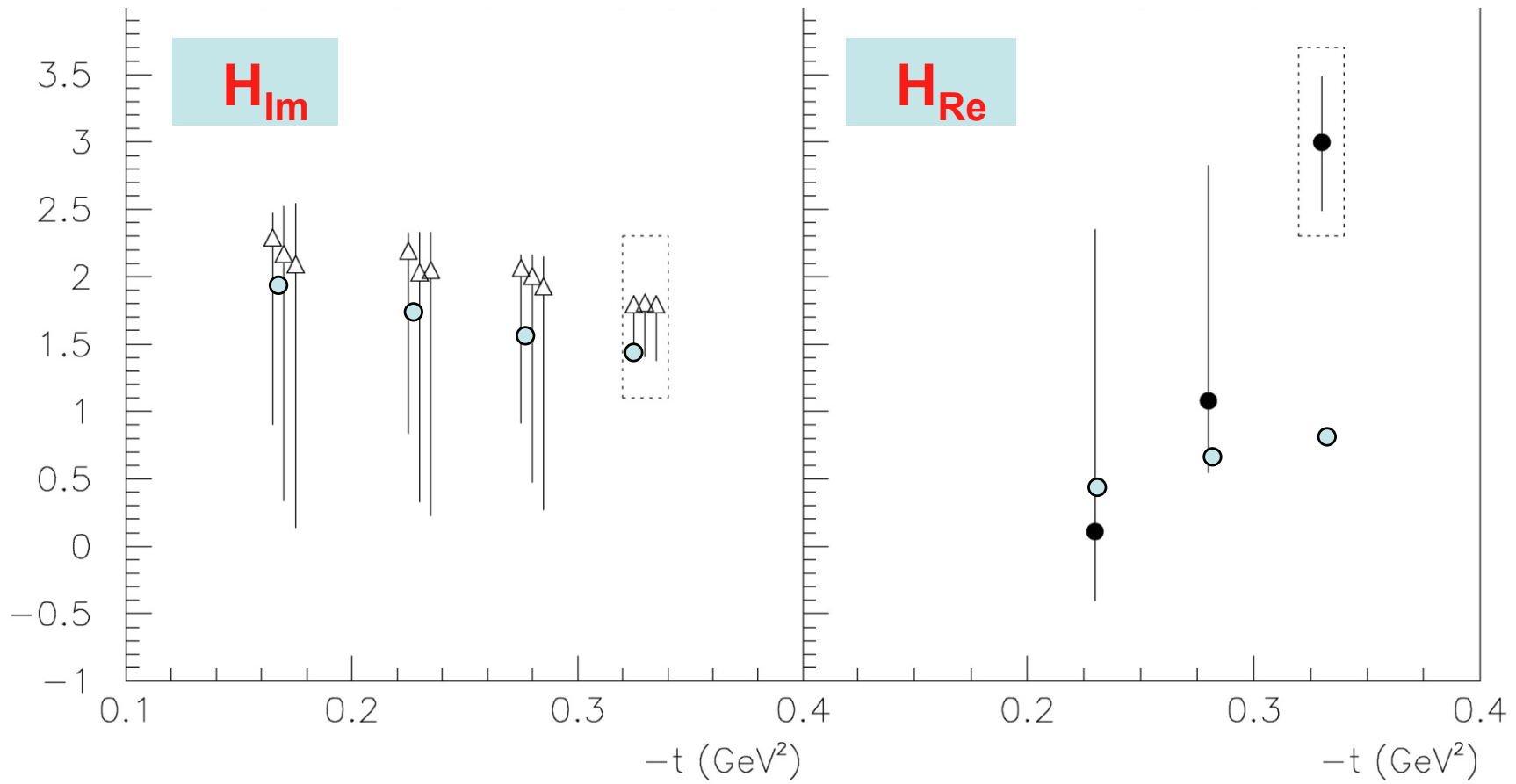
$E_e=5.75$  GeV,  $x_B=0.36, Q^2=2.3$  GeV<sup>2</sup>





△ **Result of the (model independent) fit**

**Bounds (for ALL CFFs):**  
**{-3,3}, {-5,5}, {-7,7} x VGG**



△ Result of the (model independent) fit

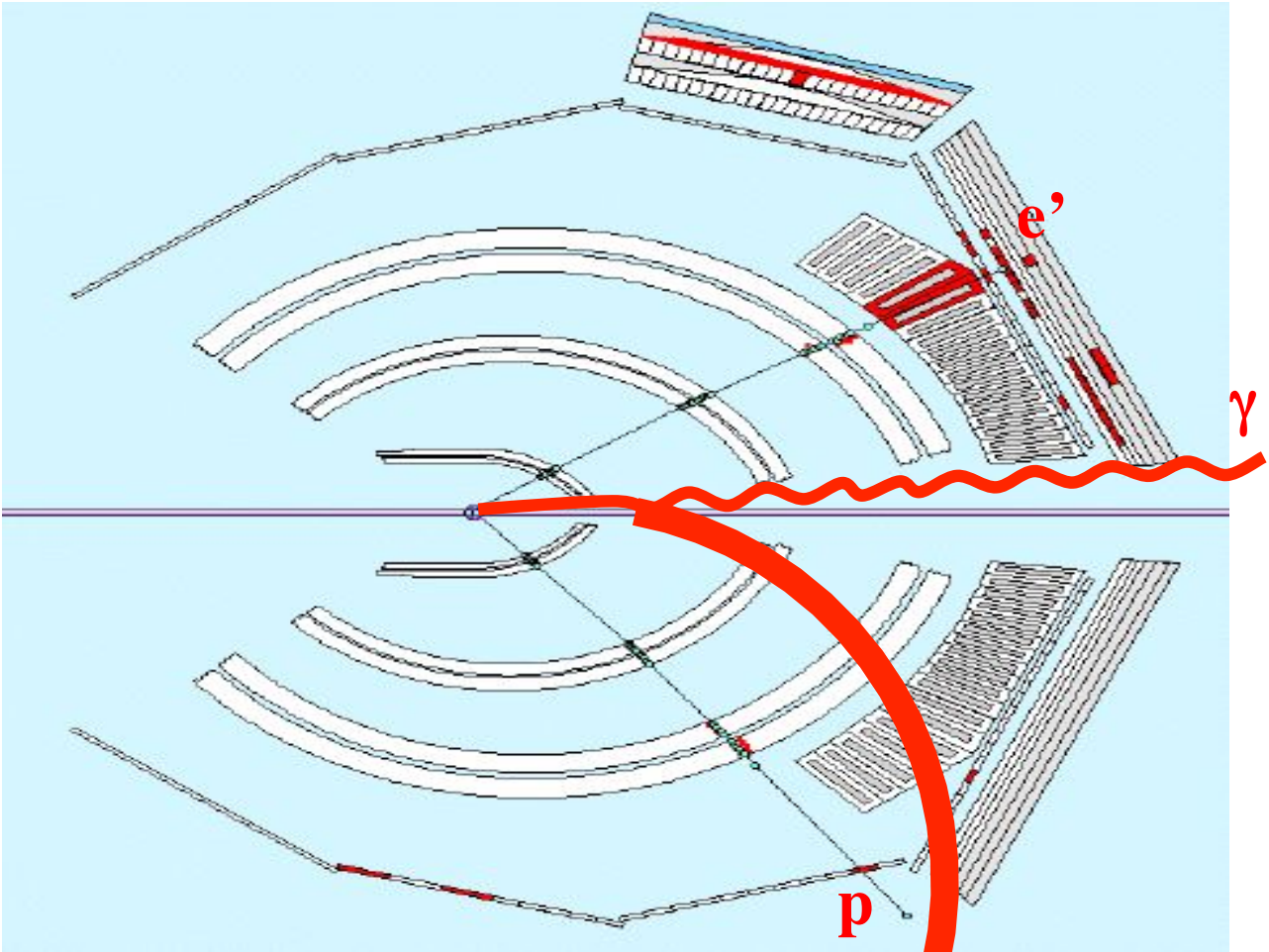
○ VGG prediction



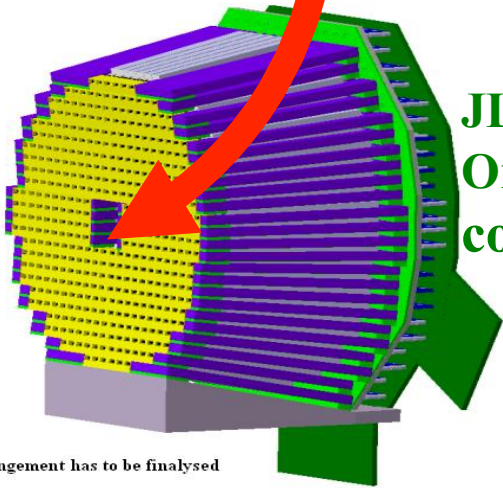
# DVCS@JLab

HALL B

$$ep \Rightarrow e\gamma$$



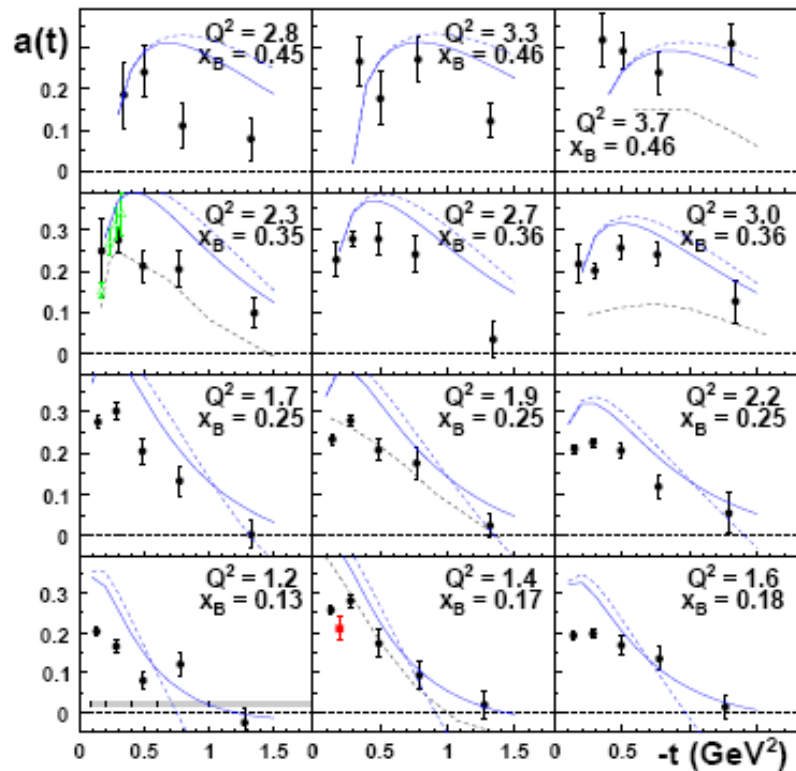
420  $\text{PbWO}_4$  crystals :  $\sim 10 \times 10 \text{ mm}^2$ ,  $l=160 \text{ mm}$   
Read-out : APDs + preamps



JLab/ITEP/  
Orsay/Saclay  
collaboration

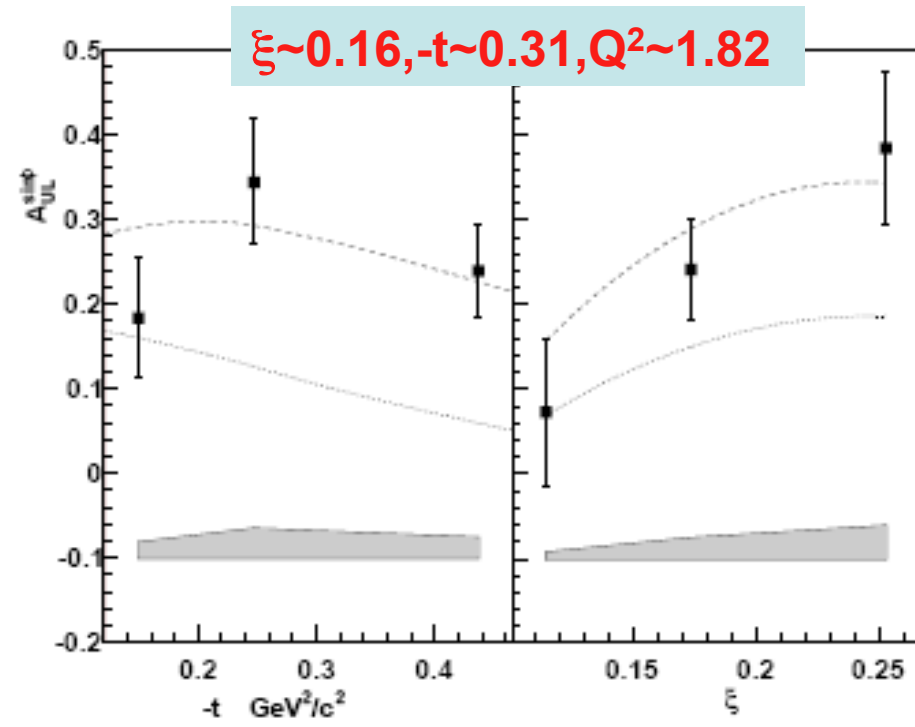
Crystal arrangement has to be finalised





**CLAS DVCS BSAs**

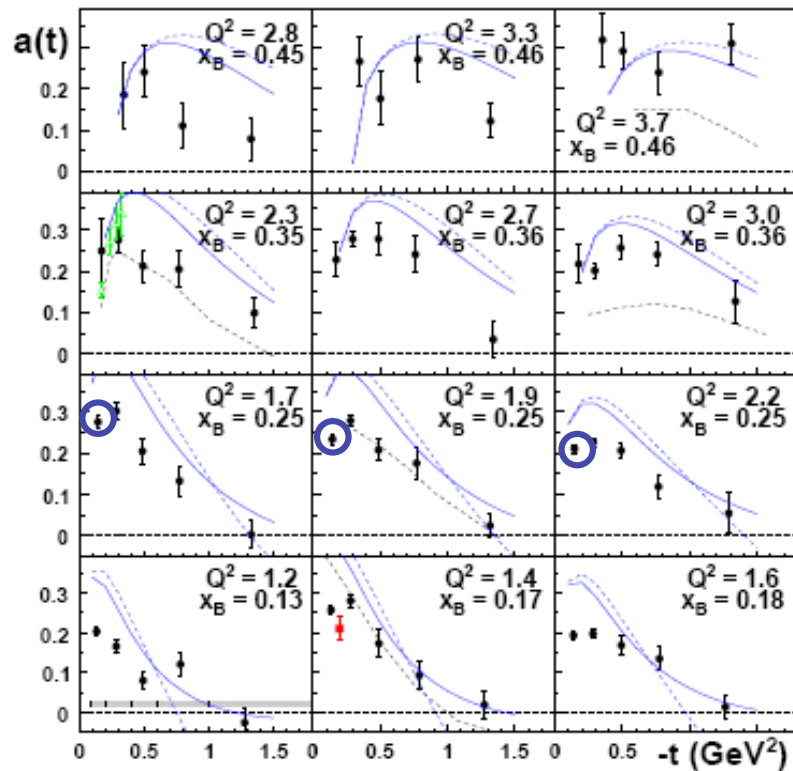
F.-X. Girod et al., Phys. Rev. Lett. 100, 162002 (2008).



**CLAS DVCS TSAs**

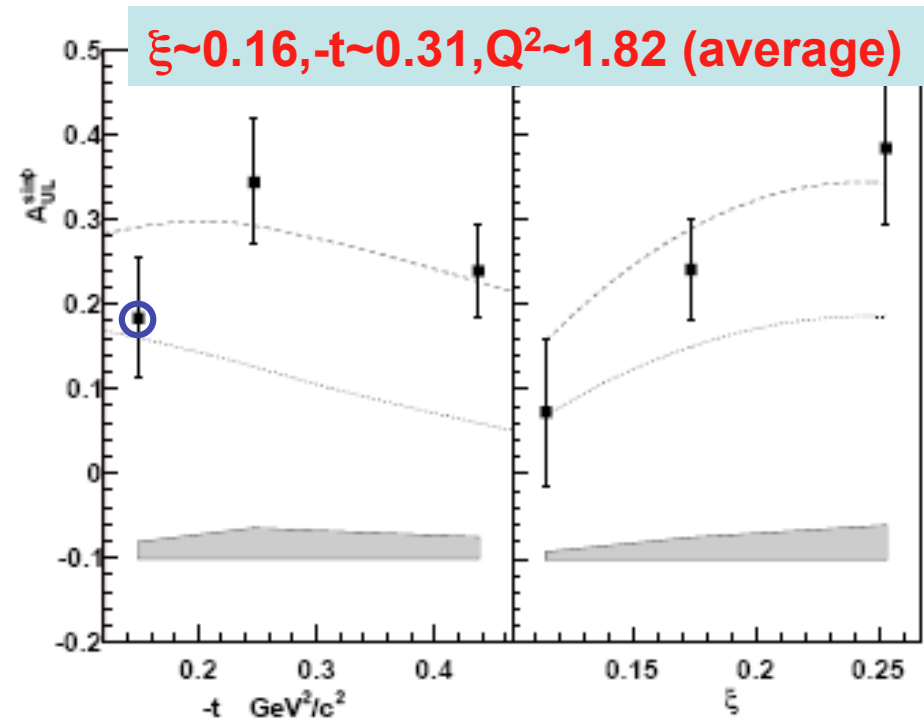
S. Chen et al., Phys. Rev. Lett. 97, 072002 (2006).

**Can we extract (in a model-independent way) some CFFs from fitting (simultaneously) the CLAS DVCS BSAs and TSAs ? (at approximately the same kinematics)**



**CLAS DVCS BSAs**

F.-X. Girod et al., Phys. Rev. Lett. 100, 162002 (2008).

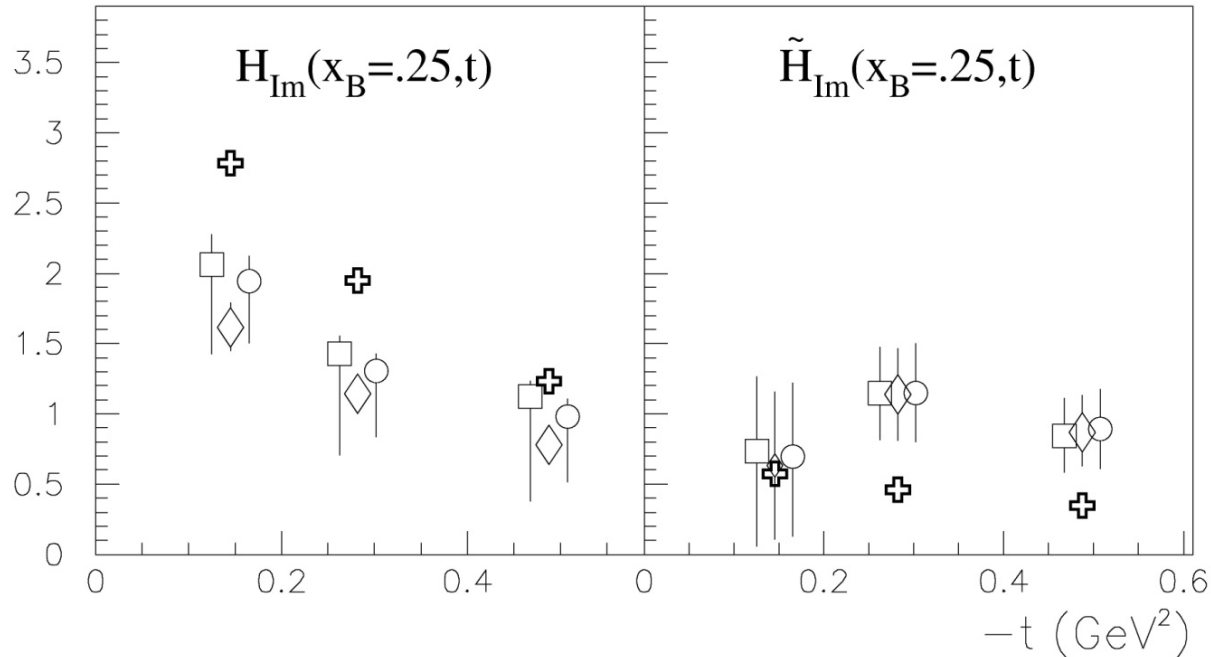


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S. Chen et al., Phys. Rev. Lett. 97, 072002 (2006).

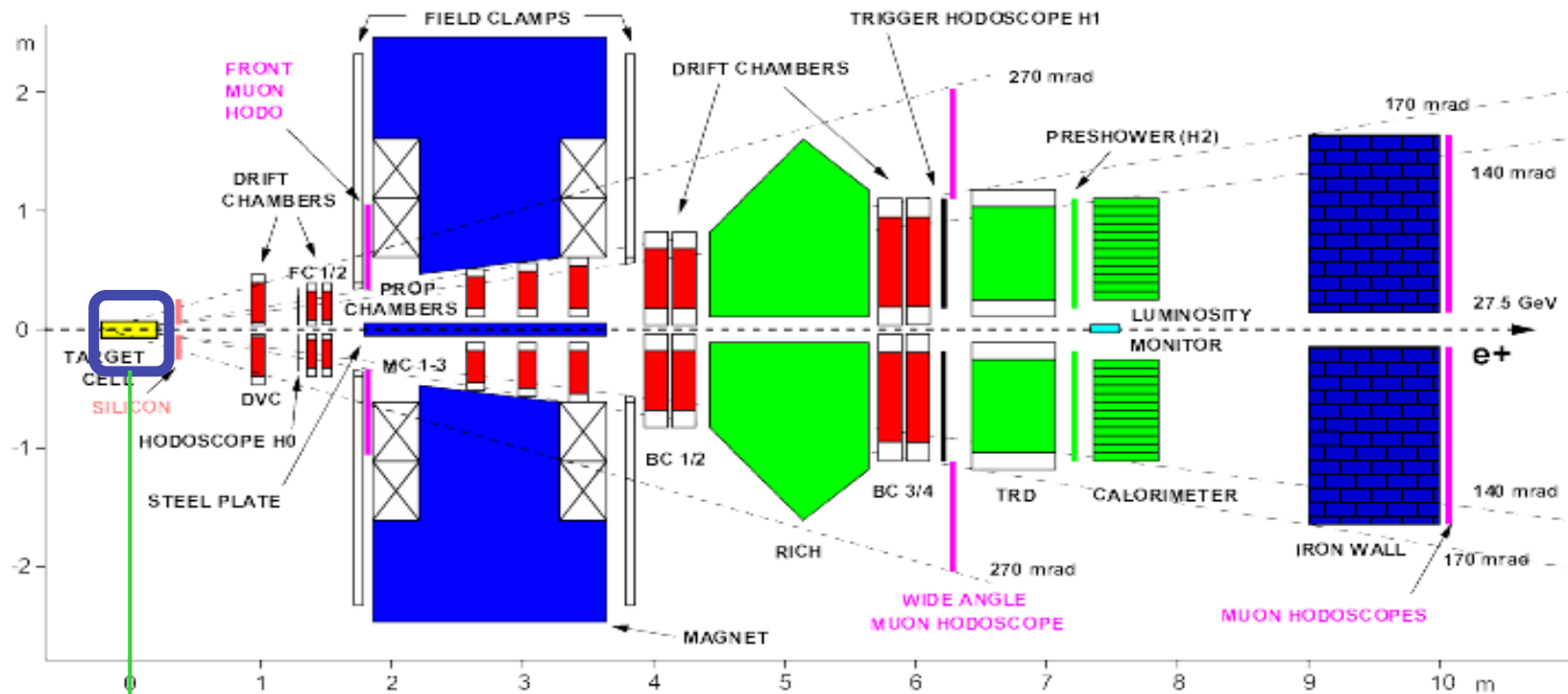
**Can we extract (in a model-independent way) some CFFs from fitting (simultaneously) the CLAS DVCS BSAs and TSAs ? (at approximately the same kinematics)**

# t-dependence at fixed $x_B$ of $H_{Im}$ & $\tilde{H}_{Im}$

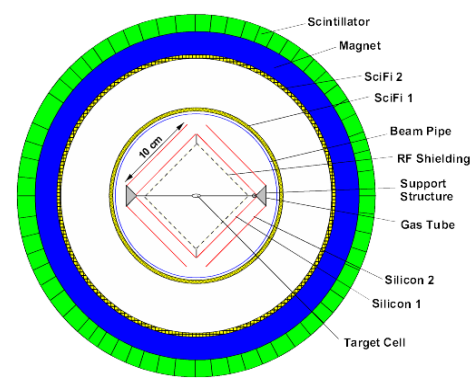


**Axial charge more concentrated than  
electromagnetic charge ?**

- |  |   |
|--|---|
| <p>□ Fit with <b>7 CFFs</b><br/>(boundaries <b>5xVGG CFFs</b>)</p> <p>◇ Fit with <b>ONLY H</b> and <b><math>\tilde{H}</math></b></p> | <p>○ Fit with <b>7 CFFs</b><br/>(boundaries <b>3xVGG CFFs</b>)</p> <p>⊕ <b>VGG prediction</b></p> |
|--|---|



**p-DVCS BSA, BCA, ITSA, tTSA, BITSA**



A. Airapetian et al., JHEP 0806, 066 (2008)

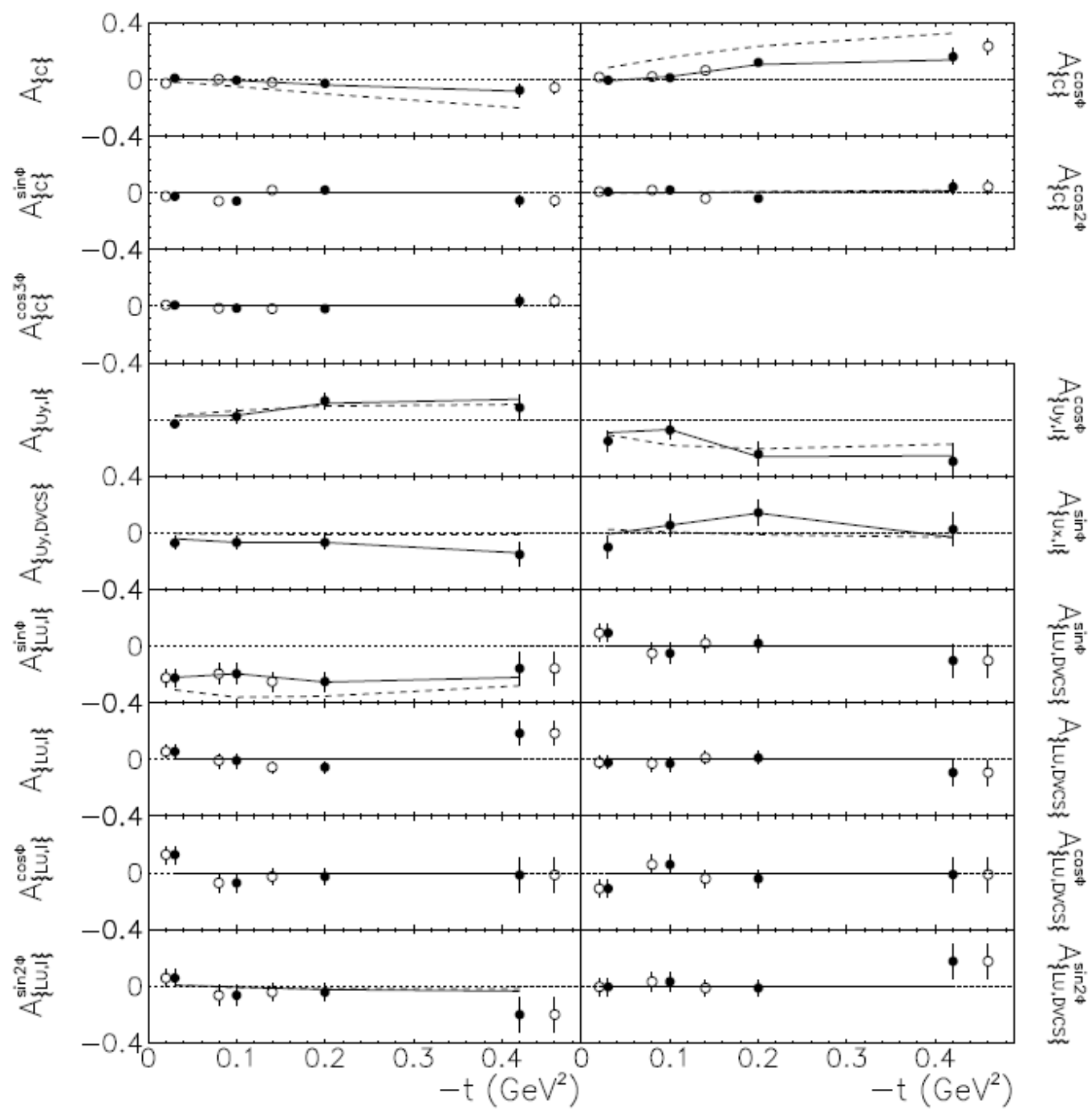
A. Airapetian et al., JHEP 0911, 083 (2009)

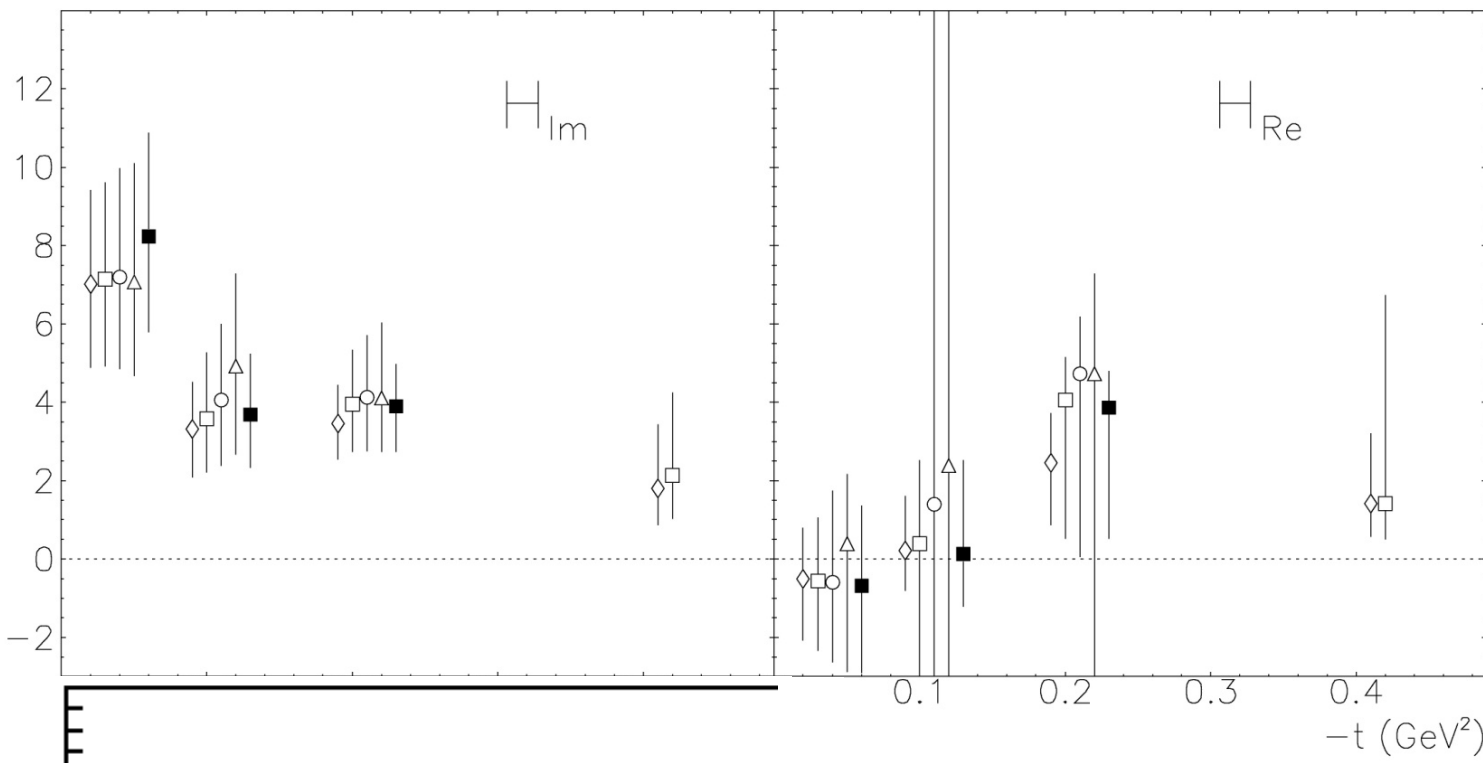
A. Airapetian et al., JHEP 1006, 019 (2010)

**17 out of 23**  
 **$\Phi$  moments**

—  
**Result of fit**

- - -  
**VGG prediction**





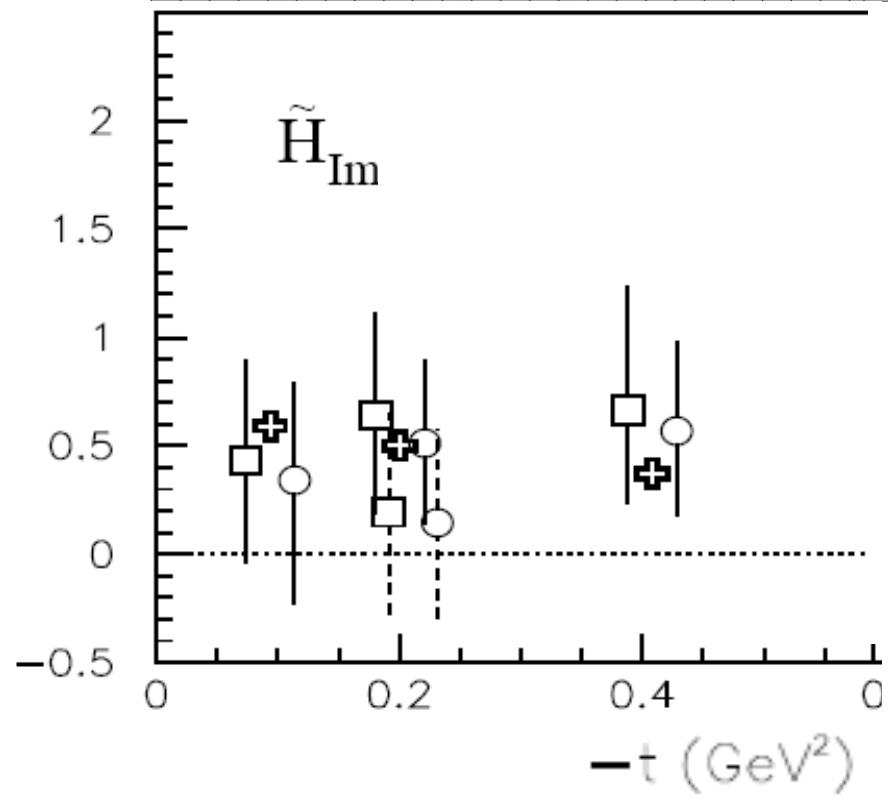
Average kinematics

■  $x_B=0.09, Q^2=2.5$

Bounds:

- ◇  $\{-3,3\} \times \text{VGG}$
- $\{-5,5\} \times \text{VGG}$
- $\{-7,7\} \times \text{VGG}$
- △  $\{-10,10\} \times \text{VGG}$

M.G. & H. Moutarde  
EPJA 37 (2008) 319

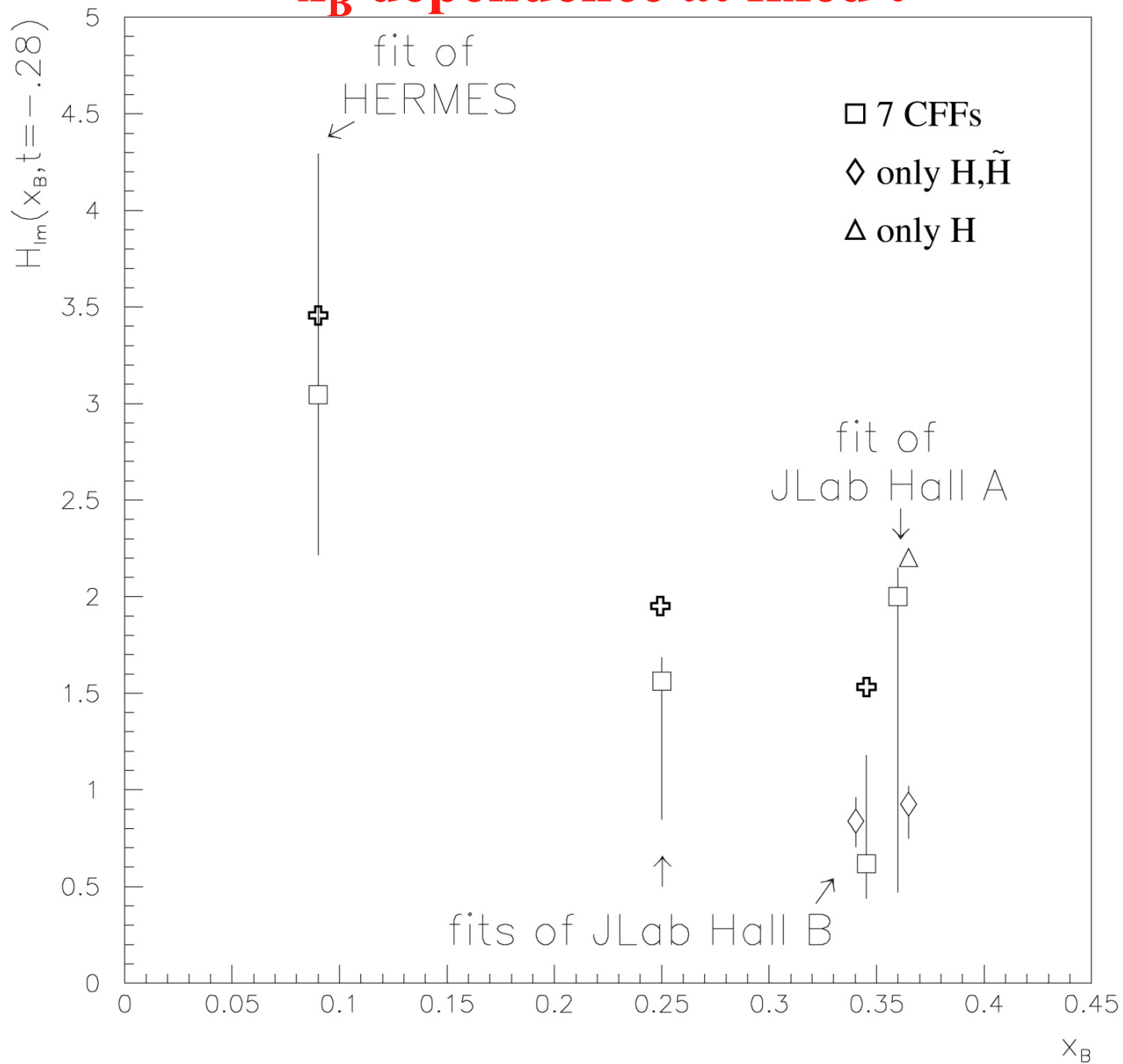


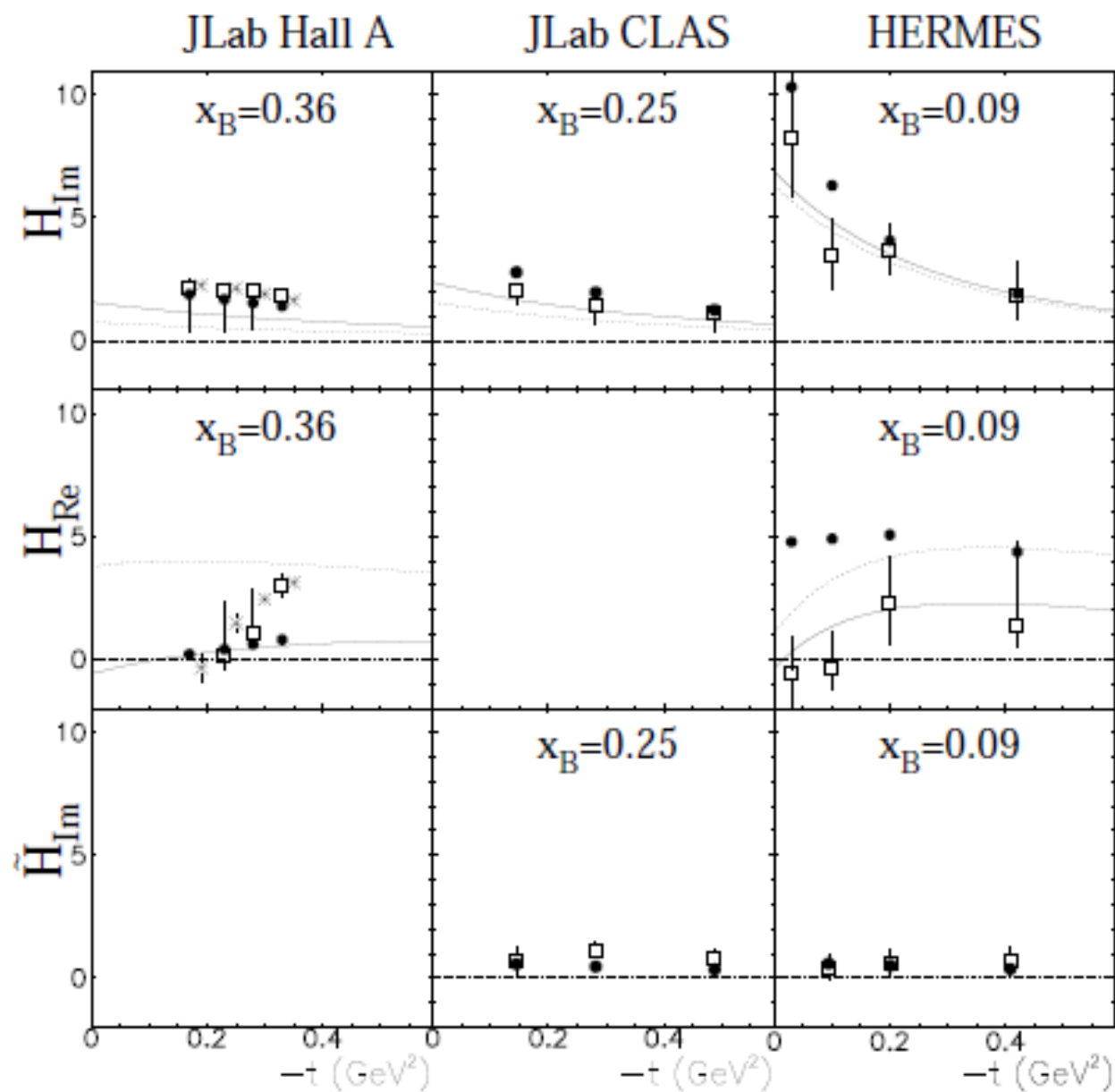
Bounds:

- $\{-5,5\} \times \text{VGG}$
- $\{-3,3\} \times \text{VGG}$
- ⊕ **VGG prediction**

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# $x_B$ dependence at fixed $t$





**Figure 1:** The  $H_{Im}$ ,  $H_{Re}$  and  $H_{Im}^4$  CFFs, as defined in Eqs.1, 5 and 7, as a function of  $-t$ . The empty squares show the results of our works, the stars the result of the CFF fit of Ref. [22], the curves the results of the model-based fit of Ref. [23] and the solid points show the predictions of the VGG model [13, 4, 21].



- ✦ *First CFFs model independent fits (leading-twist/leading order approximation); “Minimal theoretical input”*
- ✦ *Procedure tested by Monte-Carlo*
- ✦ *Procedure is working on real data; extraction of  $H_{im}$ ,  $H_{Re}$  and  $\tilde{H}_{Im}$  at JLab (cross sections) and HERMES (asymmetries) energies*
- ✦ *Relatively large uncertainties on extracted CFFs (due to lack of observables -and precision on data-)*
- ✦ *Introducing more theoretical input will reduce uncertainties (but model dependency)*
- ✦ *Large flow of new observables and data expected soon; will bring much more experimental constraints to extract CFFs with minimum theoretical input*