

# Nucleon interaction potentials in core-collapse supernovae and impact on neutrino-driven winds

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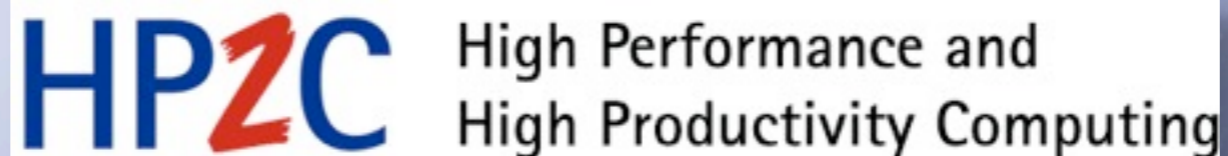
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Matthias Liebendörfer (U Basel)

Friedel Thielemann (U Basel)



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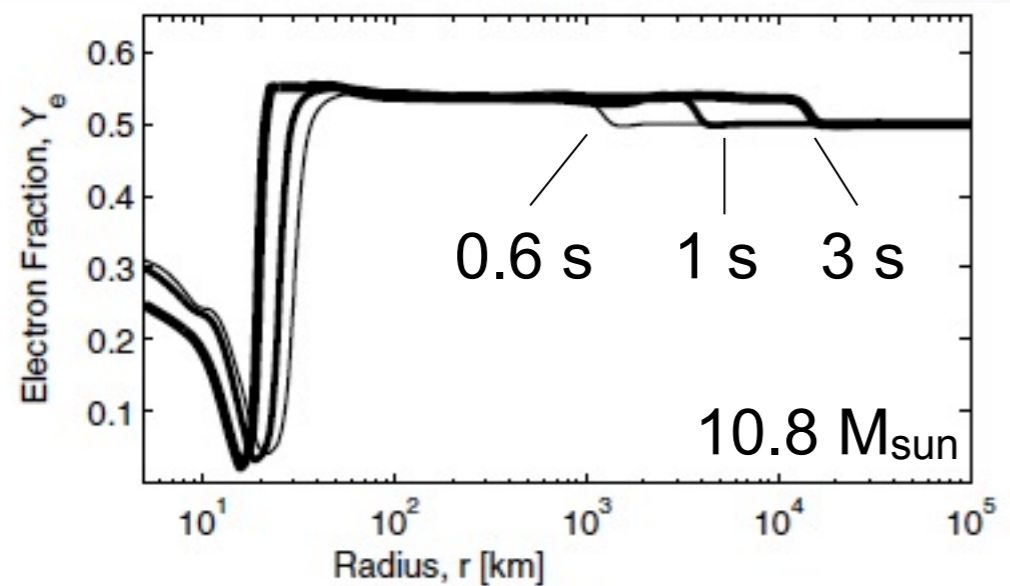
## Outline:

- 1.) introduction
- 2.) potentials
- 3.) supernova-simulations

# Nucleosynthesis conditions in neutrino-driven winds

- neutrino-driven wind: emission of low-density, high-entropy matter from proto-neutron star surface due to energy deposition by neutrinos
- candidate site for r-process nucleosynthesis
- previous long-term core-collapse supernova simulations by Fischer et al (2010), Hudepohl et al. (2010): the neutrino-driven wind is generally proton rich

[Fischer et al. A&A 517 (2010)]



- allows only vp-process (C. Fröhlich et al. 2006, Pruet et al. 2006, Wanajo et al. 2006, Arcones et al. 2011, Arcones & Thielemann 2012, ...)

# Estimate for $Y_e$

- Qian & Woosley, ApJ 471 (1996):

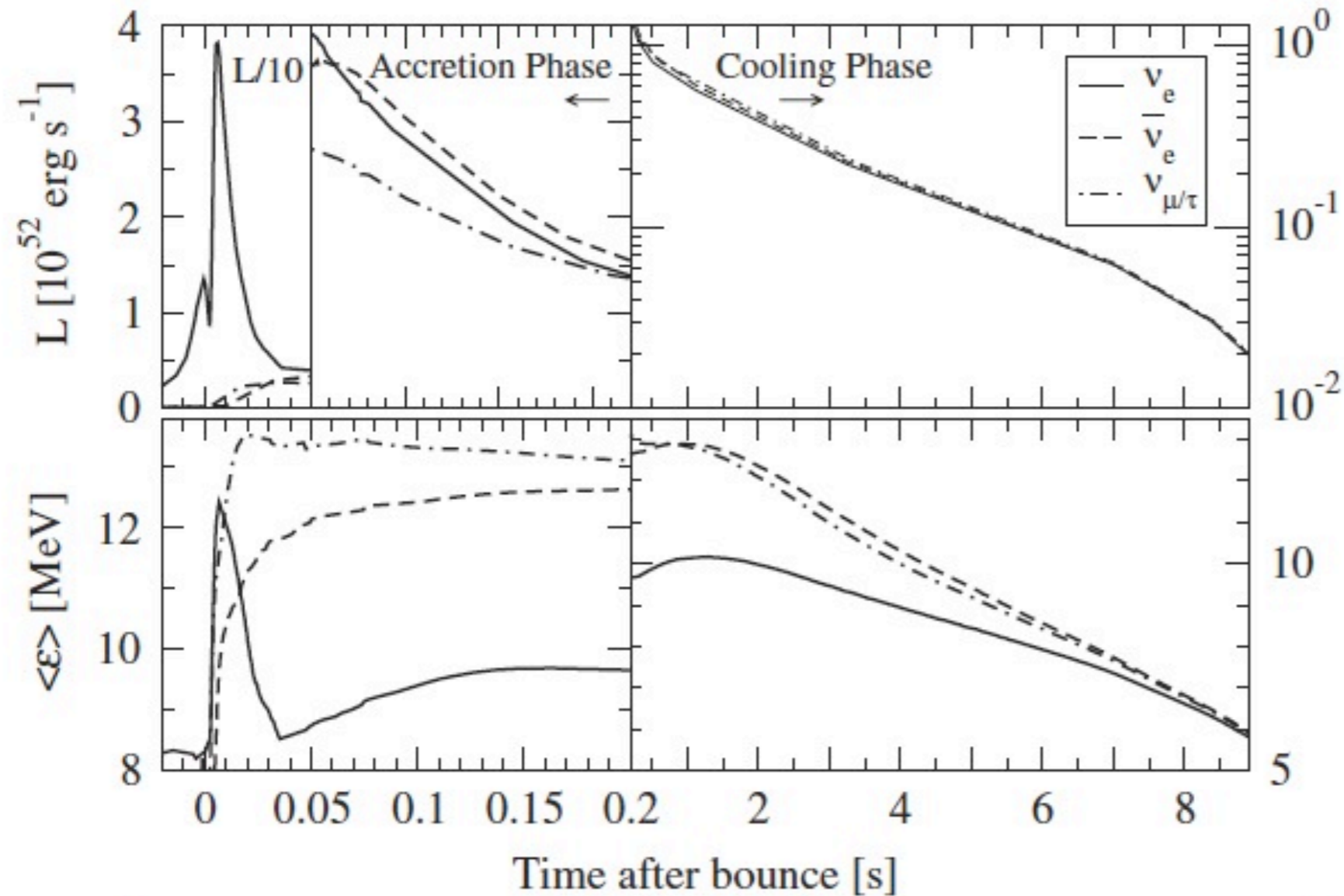
$$Y_e \simeq \left( 1 + \frac{L_{\bar{\nu}_e} \langle \epsilon_{\bar{\nu}_e} \rangle - 2Q + \frac{1.2 Q^2}{\langle \epsilon_{\bar{\nu}_e} \rangle}}{L_{\nu_e} \langle \epsilon_{\nu_e} \rangle + 2Q + \frac{1.2 Q^2}{\langle \epsilon_{\nu_e} \rangle}} \right)^{-1}$$

- $Q = m_n - m_p = 1.3 \text{ MeV}$
- neglects neutrino emission, i.e. electron and positron captures
- for similar luminosities:

$$Y_e < 0.5 \Leftrightarrow E_{\bar{\nu}_e} - E_{\nu_e} > 4Q$$

# Neutrino properties in the “standard” wind

[Hüdepohl et al. PRL 104 (2010)]



- similar luminosities
- $E_{\nu_{\mu/\tau}} \sim E_{\bar{\nu}_e} > E_{\nu_e}$
- $E_{\bar{\nu}_e} - E_{\nu_e} < 4Q \rightarrow Y_e > 0.5$

# Mean-field potentials in charged-current rates

- Bruenn `85: charged-current rates based on non-interacting nucleons
- improved charged-current rates (with mean-field effects):
  - Reddy, Prakash & Lattimer, PRD58 (1998)
  - Reddy, Prakash, Lattimer & Pons, PRC59 (1999)
- G. Martínez-Pinedo et al., PRL109 (2012), Roberts & Reddy, PRC86 (2012): crucial for late neutrino spectra

• e.g.:  $e + p \rightarrow n + \nu_e$

- energy conservation for a generic mean-field model:

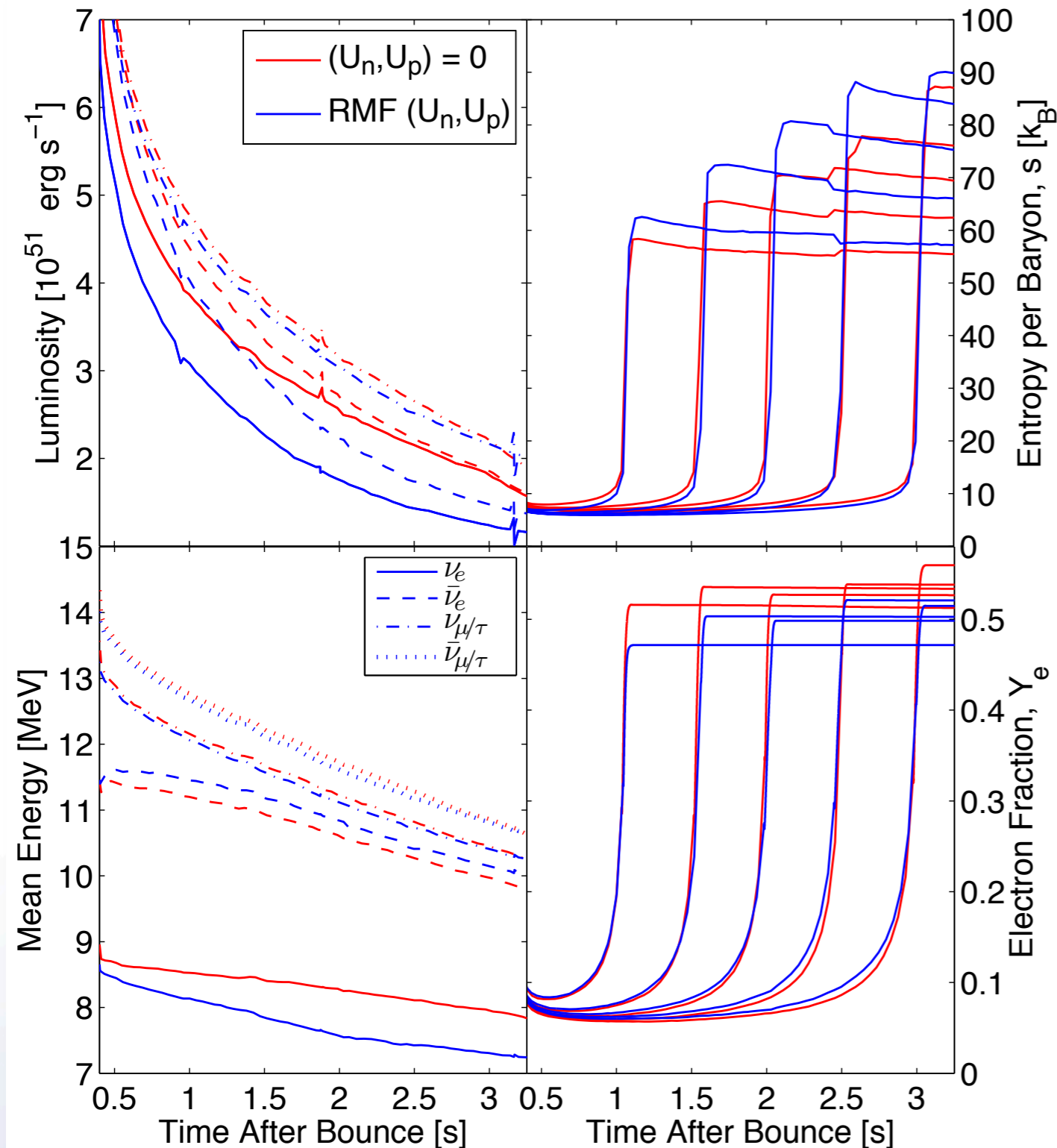
$$E_p + E_e = E_n + E_{\nu_e}$$

$$\sqrt{p_p^2 + m_p^{*2}} + U_p + \sqrt{p_e^2 + m_e^2} = \sqrt{p_n^2 + m_n^{*2}} + U_n + E_{\nu_e}$$

- neutron-rich conditions:  $\Delta U = U_n - U_p > 0 \rightarrow$  reduces neutrino energies

# Effects of mean-field potentials on the neutrino-driven wind

[Martínez-Pinedo et al., PRL 109 (2012)]



- $E_{\nu_e}$  decrease,  $E_{\bar{\nu}_e}$  increased, difference increased
- luminosities decreased
- mean-field effects can lead to neutron-richness of the wind
- same conclusions by Roberts et al. 2012

# Definition of mean-field potentials

- defined by the application! here: charged-current rates
- general expression for cross section per unit volume of neutrino absorption, e.g. Reddy et al., PRD58 (1998):

$$\begin{aligned} \frac{\sigma(E_1)}{V} &= 2 \int \frac{d^3 p_2}{(2\pi)^3} \int \frac{d^3 p_3}{(2\pi)^3} \int \frac{d^3 p_4}{(2\pi)^3} \\ &\times (2\pi)^4 \delta^4(P_1 + P_2 - P_3 - P_4) W_{fi} \\ &\times f_2(E_2)(1 - f_3(E_3))(1 - f_4(E_4)) \end{aligned}$$

- note: uniform system!
  - aim: reconstruct the nucleon distribution functions and single particle energies of the interacting system
- consistency of the potentials and the used weak interaction rates



# Definition of mean-field potentials - uniform nucleon gas

- any momentum-independent relativistic mean-field model can be formulated as

$$P(T, \mu) = P^{\text{kin}} + P^{\text{int}} \qquad n(T, \mu) = 2 \int \frac{d^3k}{(2\pi)^3} f(k)$$
$$= \frac{2}{3} \int \frac{d^3k}{(2\pi)^3} \frac{k^2}{(m^{*2} + k^2)^{1/2}} f(k) + P^{\text{int}}$$

$$f = \left[ \exp \left( \frac{\sqrt{m^{*2} + k^2} + U - \mu}{T} \right) + 1 \right]^{-1}$$

$U = \Sigma_V$ , vector self-energy  $\Sigma_V$   
 $m^* = m + \Sigma_S$ , scalar self-energy  $\Sigma_S$

- thermodynamic consistency relation:

$$n \frac{\partial U}{\partial n} = \frac{\partial P^{\text{int}}}{\partial n}$$

→  $U(n, T)$  and  $m^*(n, T)$  contain all information of the system

- note:

$$\mu - U = \nu = \mu^{\text{free}}(T, n, m^*)$$

$$\Rightarrow U = \mu - \mu^{\text{free}}(T, n, m^*)$$

# Potentials from the virial EOS

[C.J. Horowitz et al., PRC86 (2012)]

- second order nucleonic virial expansion

$$P = \frac{2T}{\lambda^3} \left\{ z_n + z_p + (z_n^2 + z_p^2) b_n + 2z_p z_n b_{pn} \right\}$$

- without explicit deuteron degree of freedom, but contribution of deuteron bound state to the second virial coefficient:

$$b_{pn}(T) \approx -0.9885 + 2.502 \exp\left(\frac{2.099}{T}\right) - 0.0179T$$

- “increased  $\Delta U$  in virial EOS compared to mean-field models”

→ used definition of  $\Delta U$  is not suitable for nucleon charged-current rates

TABLE I. Energy shift  $\Delta U$  predicted by different approaches at a density  $n = 0.001 \text{ fm}^{-3}$  and a temperature  $T = 5 \text{ MeV}$ .

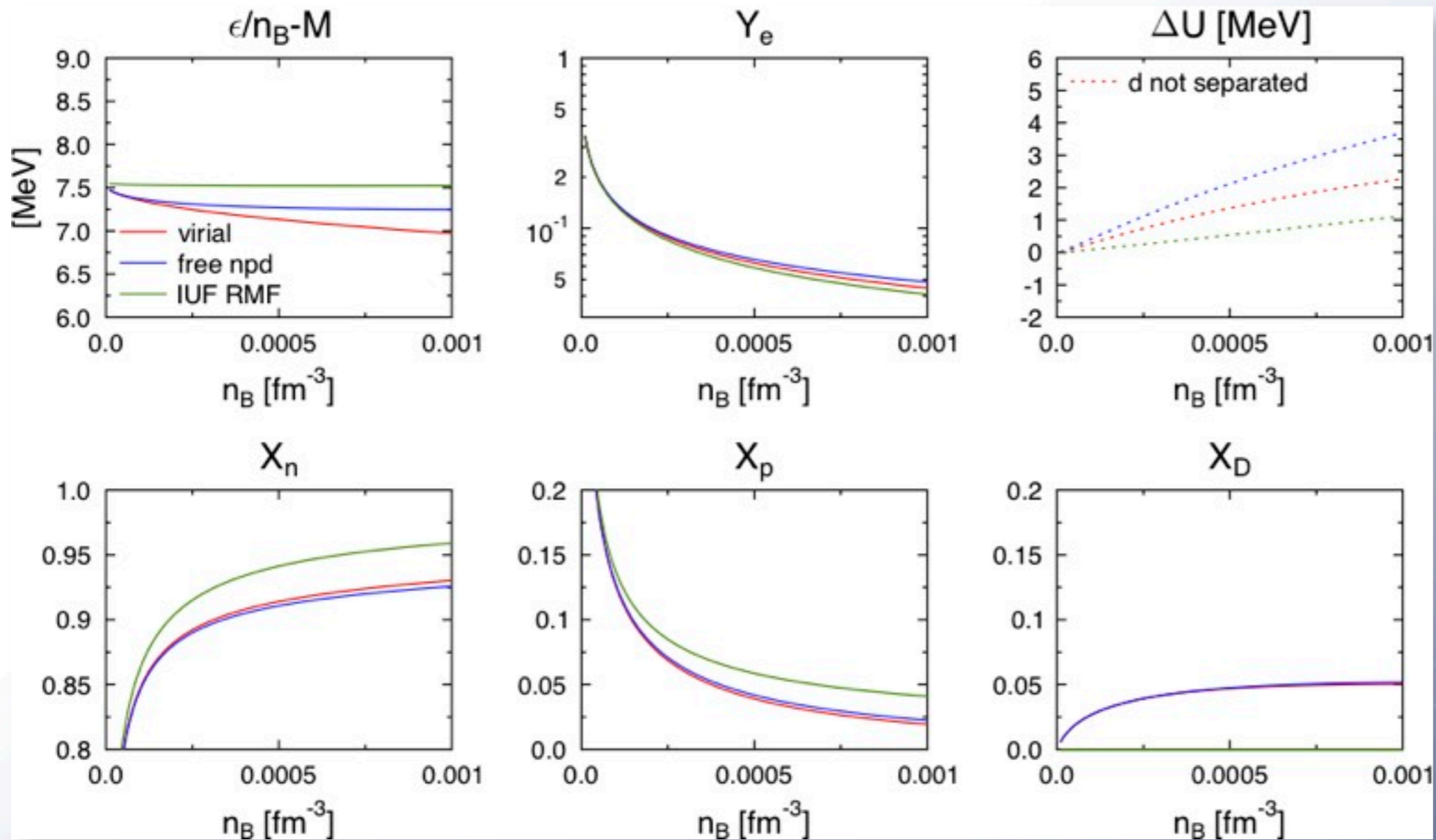
Model	$\Delta U$ (MeV)
Lowest order virial, Eq. (21)	3.85
Virial $\mu_i - \mu_i^f$ , Eq. (31)	2.27
Mean-field model GM3, Eq. (36)	0.23
Mean-field model IUFSU [15]	1.11

# Potentials from the virial EOS

- definition used:

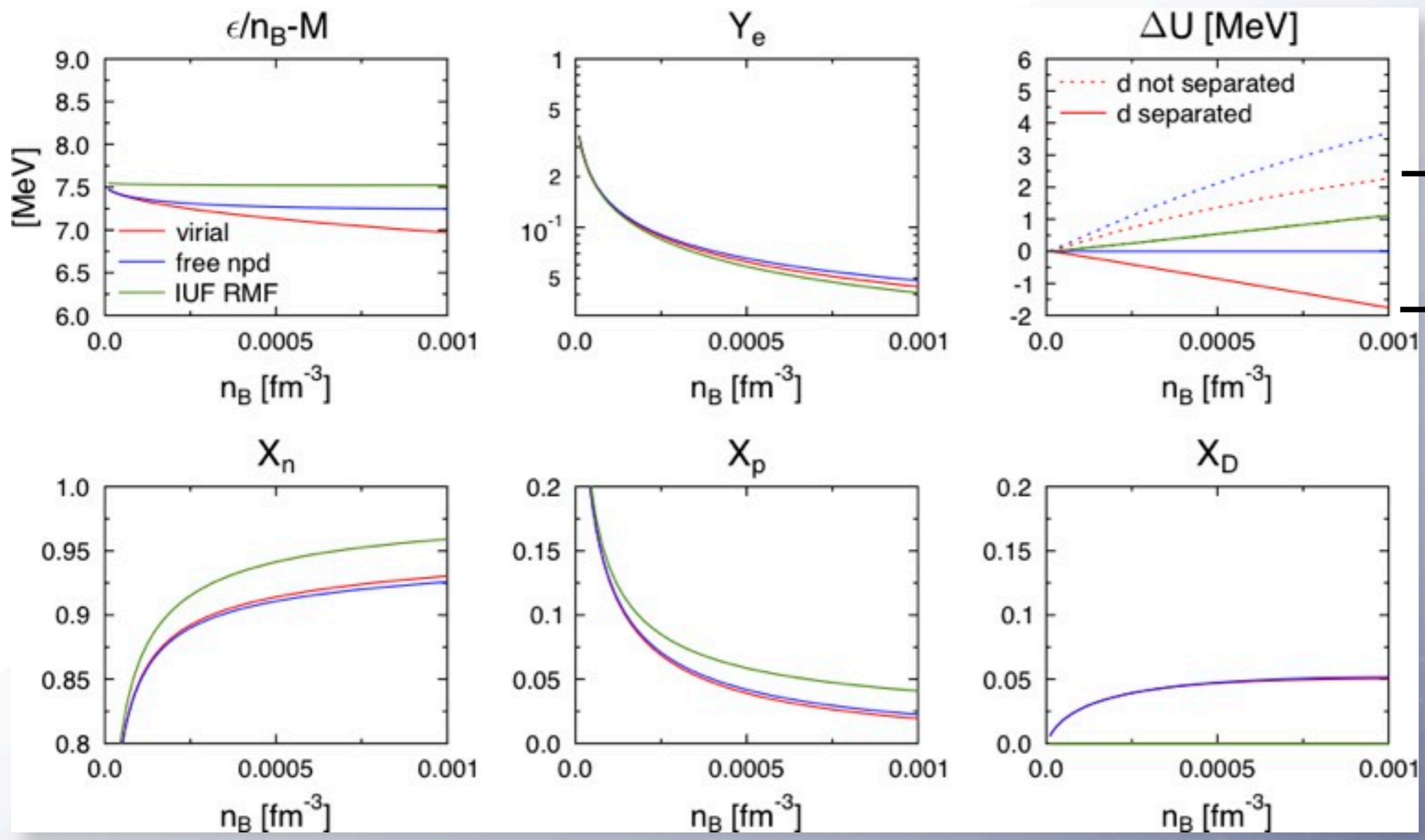
$$U_p = \mu_p - \mu^{\text{free}}(T, n_p^{\text{tot}})$$

- beta-equilibrium,  $T=5$  MeV



# Potentials from the virial EOS

- separating deuteron contribution:  $U_p = \mu_p - \mu^{\text{free}}(T, n_p)$
- beta-equilibrium,  $T=5$  MeV  $n_p = n_p^{\text{tot}} - n_D = X_p n_B$



} deuteron contribution

→ each bound state has its own effective potential and these have to be separated from nucleons

# Potentials from SN EOS

- mixture of heavy and light nuclei, unbound nucleons → non-uniform system
- what one should do: calculate the full neutrino response (with mean-field, correlations, nuclear structure, light clusters, etc) of the system as a whole
- done in practice:
  - separate rates for nucleons, light nuclei, heavy nuclei
  - unbound nucleon component treated as uniform

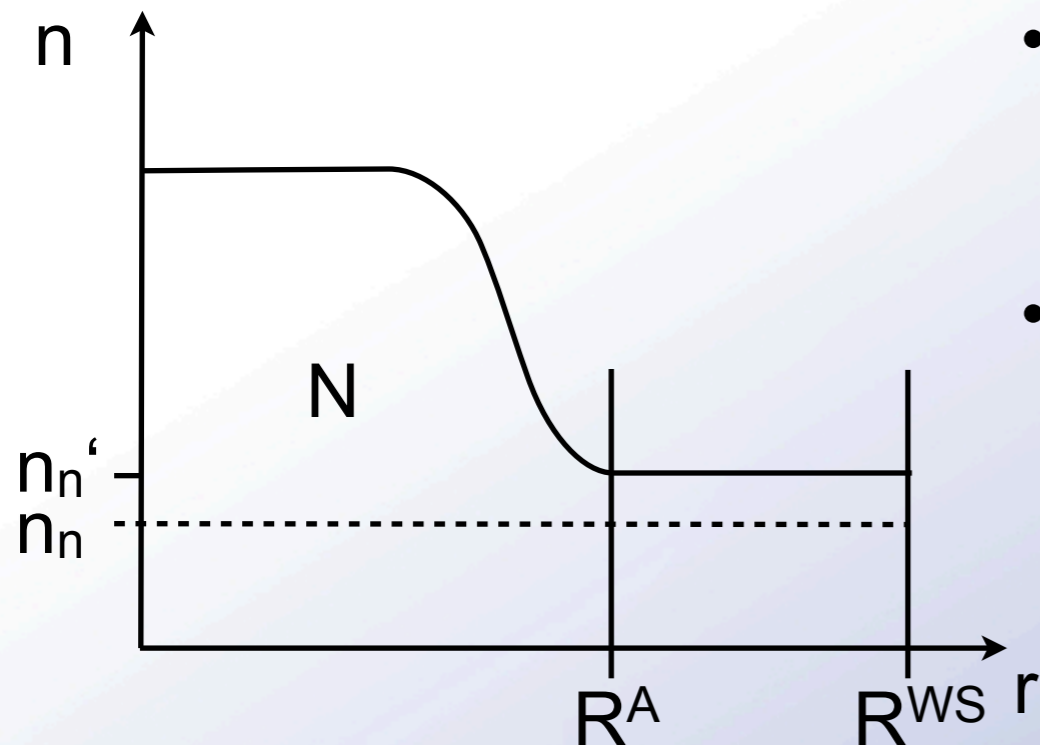
# Potentials from (tabulated) SN EOS

- typical tabulated quantities:

- mass fractions:  $X_n, X_p, (X_d), (X_h), X_\alpha, X_{\text{heavies}}, \dots$
- thermodynamic quantities:  $\mu_n, \mu_p, S, \dots$
- possibly some microscopic properties:  $m^*$

- naive guess:

$$U_i = \mu_i - \mu_i^{\text{free}}(T, n_i, m_i^*), \quad n_i = X_i n_B / A_i$$



- but:  $X_i$  is an average quantity of the WS cell, the heavy nucleus is defined as a coordinate space cluster ( $\rightarrow$  F. Gulminelli)

- one should use

$$U_i = \mu_i - \mu_i^{\text{free}}(T, n'_i, m_i^*), \quad n'_i = ?$$

$\rightarrow$  available EOS tables allow only an approximated calculation of  $\Delta U$

# HS EOS: excluded volume NSE with interactions

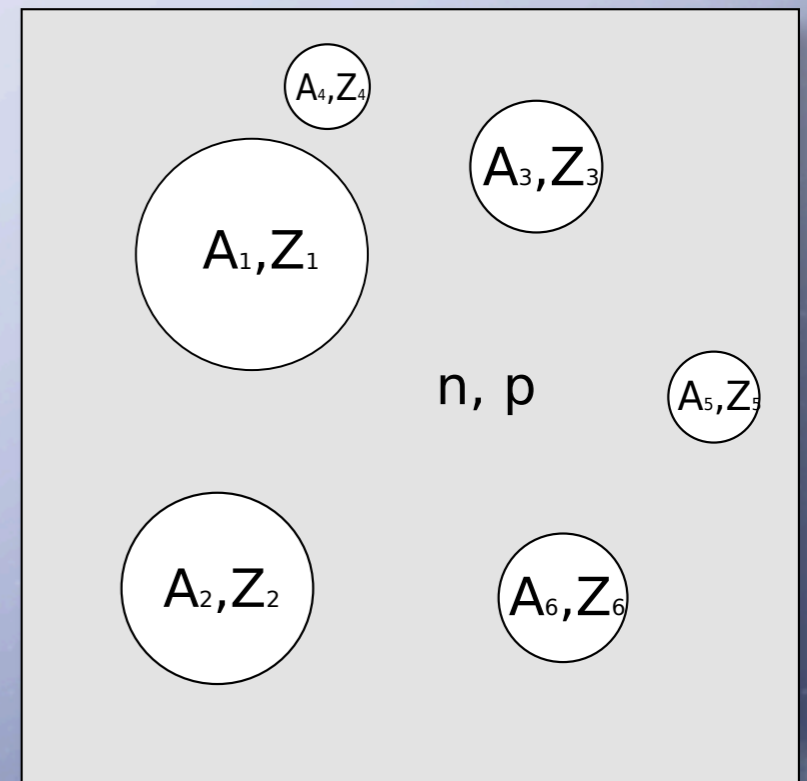
[MH, J. Schaffner-Bieleich; NPA837(2010)] [A. Steiner, MH, T. Fischer; arXiv1207.2184]

- eight EOS tables for different interactions available:  
NL3, TM1, TMA, FSUgold, DD2, SHFo, SHFx, IUFSU

<http://phys-merger.physik.unibas.ch/~hempel/eos.html>

- relativistic mean-field interactions and excluded volume effects
- uniform distribution of nucleons outside nuclei

→ allows consistent description of the EOS  
and neutrino interactions



# Potentials from the HS EOS

- excluded volume effects can be recast as effective mean-field interactions

simple nucleon gas

$$P = \frac{2}{3} \int \frac{d^3k}{(2\pi)^3} \frac{k^2}{(m^{*2} + k^2)^{1/2}} f(k) + P^{\text{int}}$$

$$f = \left[ \exp \left( \frac{\sqrt{m^{*2} + k^2} + U - \mu}{T} \right) + 1 \right]^{-1}$$

- total pressure

$$P = \sum_{i=n,p} \frac{2}{3} \int \frac{d^3k}{(2\pi)^3} \frac{k^2}{(m_i^{*2} + k^2)^{1/2}} f_i + \sum_{A,Z} \frac{g_{A,Z}}{3} \int \frac{d^3k}{(2\pi)^3} \frac{k^2}{m_{A,Z}} f_{A,Z} + P^{\text{fields}} + P^{\text{Coul}}$$

- nucleons:

$$f_i = \frac{1}{1 + \exp[(E_i - \mu_i)/T]} \quad E_i = \sqrt{k^2 + m_i^{*2}} + U_i$$

$$U_{n/p} = g_\omega \omega(T, n'_n, n'_p) + (2Z - 1) g_\rho \rho(T, n'_n, n'_p) + \frac{1}{\kappa} \sum_{A,Z} p_{A,Z}^0 / n_B^0 + Z p^{\text{Coul}} / n_e$$

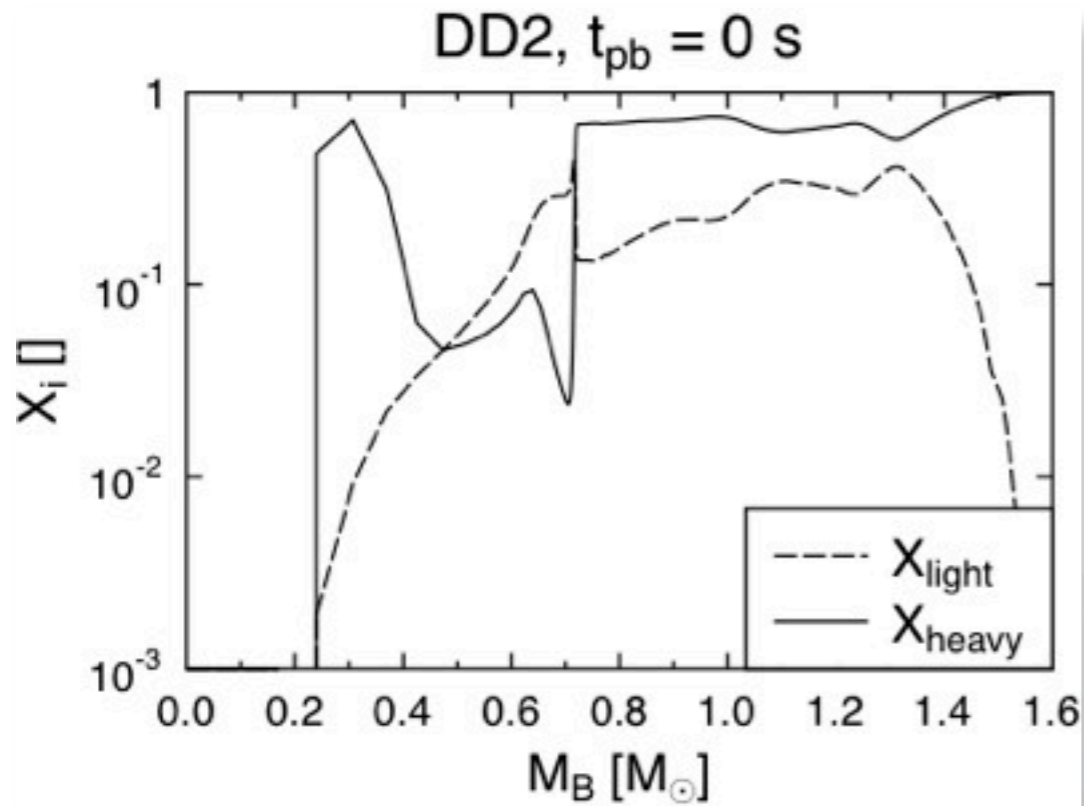
- nuclei:

$$f_{A,Z} = \frac{1}{\exp[(E_{A,Z} - \mu_{A,Z})/T]} \quad E_{A,Z} = M_{A,Z} + \frac{k^2}{2M_{A,Z}} + U_{A,Z}$$

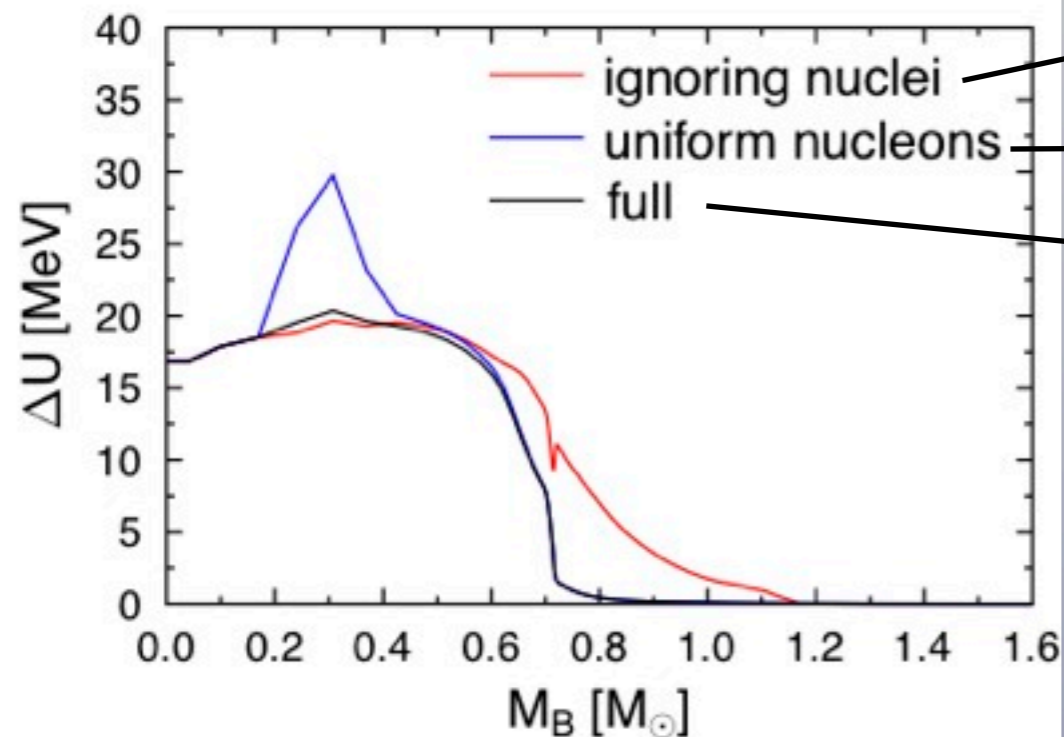
$$U_{A,Z} = \left( p_{nuc}^0 + \frac{1}{\kappa} \sum_{A,Z} p_{A,Z}^0 \right) A / n_B^0 + E_{A,Z}^{\text{Coul}} + Z p^{\text{Coul}} / n_e$$



# $\Delta U$ in a core-collapse supernova



- core-collapse supernova simulation (details later)
- DD2 EOS



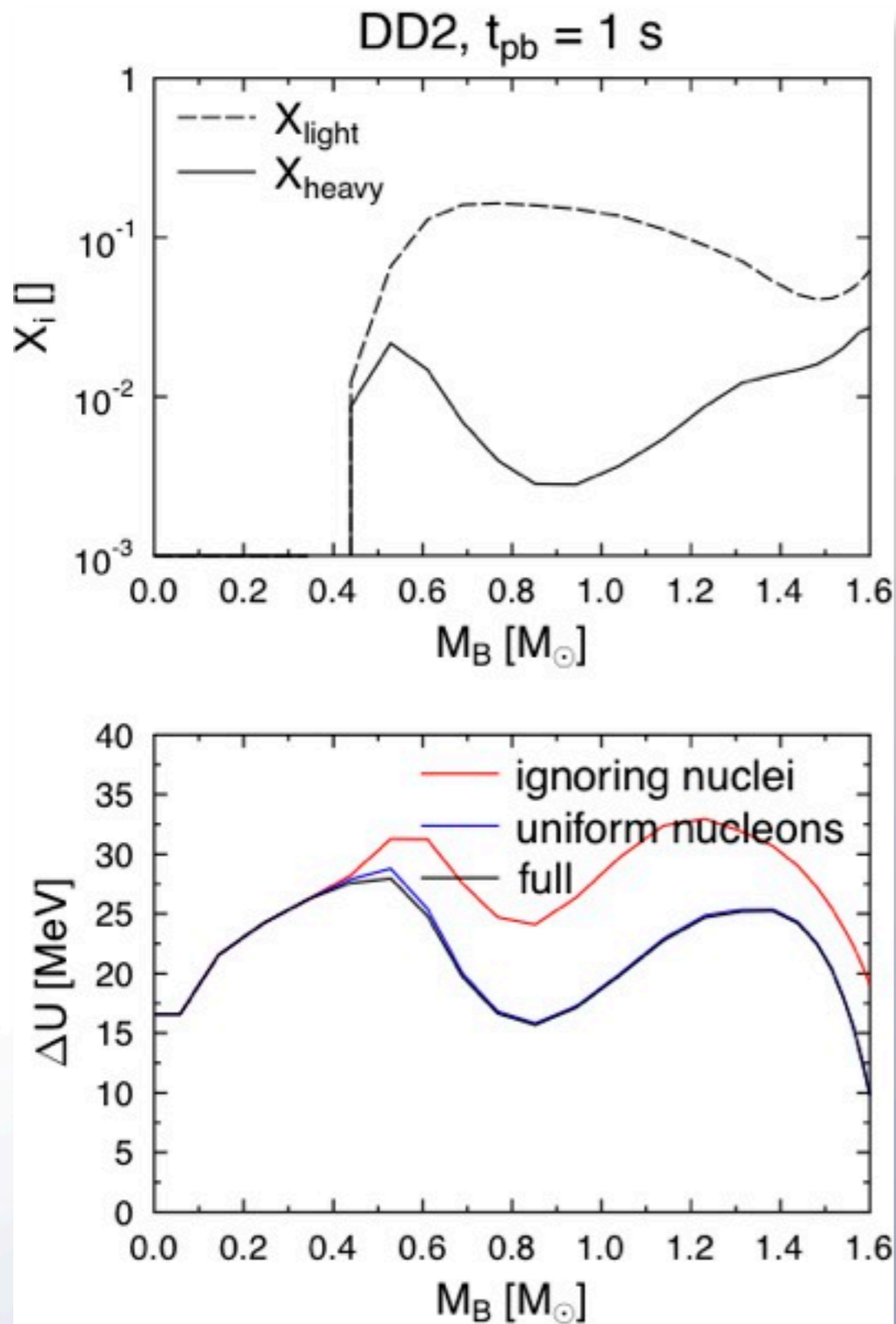
$$U_p = \mu_p - \mu_p^{\text{free}}(T, n_p^{\text{tot}}, m^*), \quad n_p^{\text{tot}} = Y_e n_B$$

$$U_p = \mu_p - \mu_p^{\text{free}}(T, n_p, m^*), \quad n_p = X_p n_B$$

$$U_p = \mu_p - \mu_p^{\text{free}}(T, n'_p, m^*), \quad n'_p \text{ local density}$$

- nuclei lead to differences
- “full” gives smoother  $\Delta U$

# $\Delta U$ in a core-collapse supernova

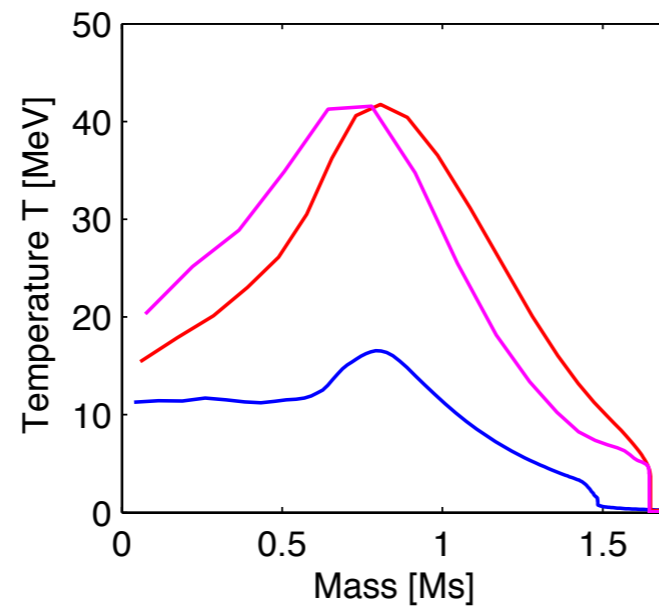
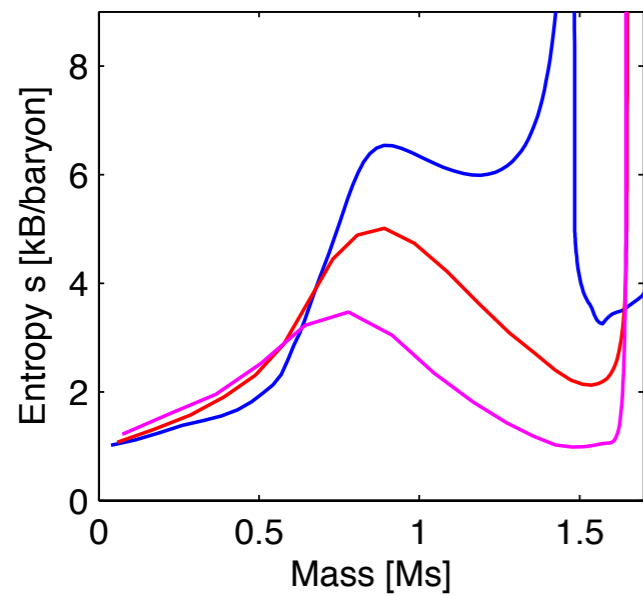
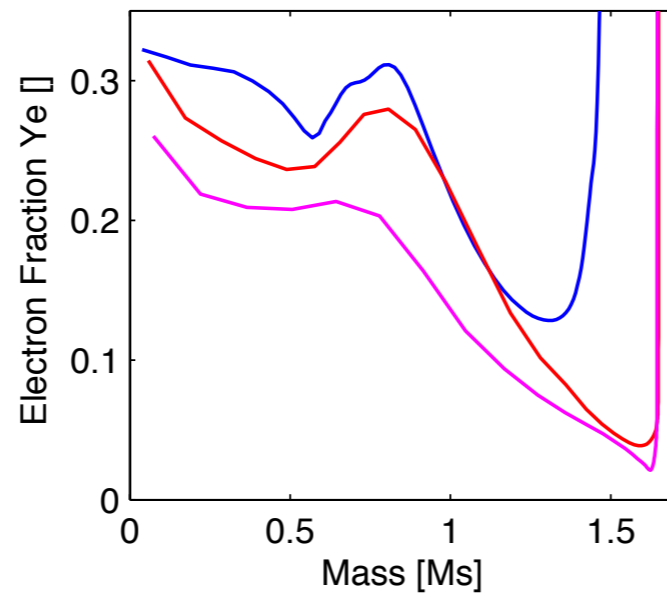
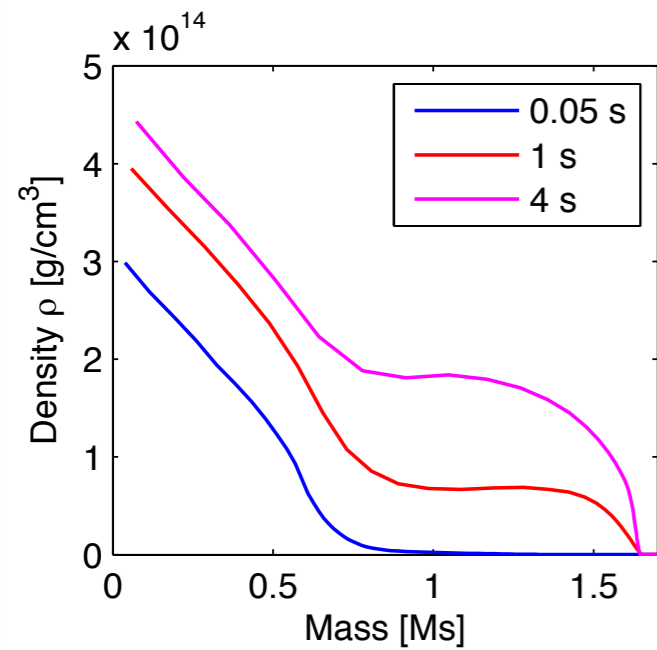


- light nuclei remain abundant in the PNS envelope
- they should be treated separately from unbound nucleons

# Simulation setup

- hydrodynamics: AGILE
- e-flavor neutrinos: IDSA (M. Liebendörfer)
- $\mu/\tau$  neutrinos: Advanced Spectral Leakage (ASL) (A. Perego)
- new PUSH to trigger explosions (A. Perego)
  - total energy emitted in  $\mu/\tau$  neutrinos  $\sim 5 \times 10^{52}$  erg, only little reabsorption
  - PUSH: artificially induced explosion via enhanced  $\mu/\tau$  absorption
  - energy deposition parameterized by  $k_{\text{push}}=1.3$
- simplified alpha-network (K. Ebinger, MH)
  - 25 symmetric and asymmetric nuclei
  - nuclear reactions estimated by burning timescales (Fowler et al. (1975))
  - advection based on Plewa & Müller (1999)
- detailed non-NSE EOS (MH)
- $15 M_{\text{sun}}$  solar metallicity progenitor, Woosley, Heger & Weaver (2002)
- HS(TM1) EOS (similar to Shen)

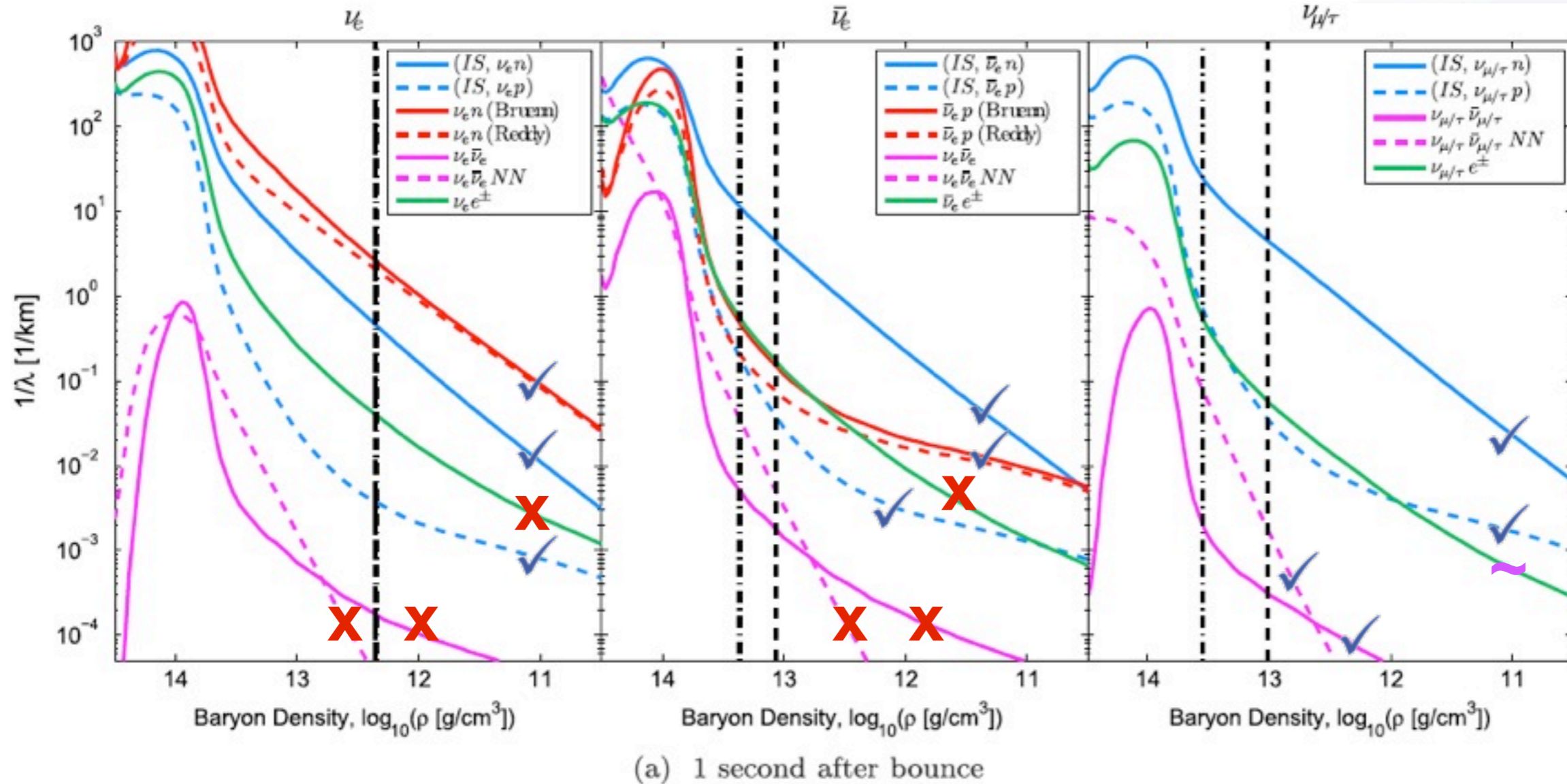
# PNS cooling



- results without  $\Delta U$
- $M_B = 1.642 M_{\text{sun}}$
- $M_G(T=0) = 1.495 M_{\text{sun}}$
- very satisfactory overall cooling behavior

# Contribution of individual rates

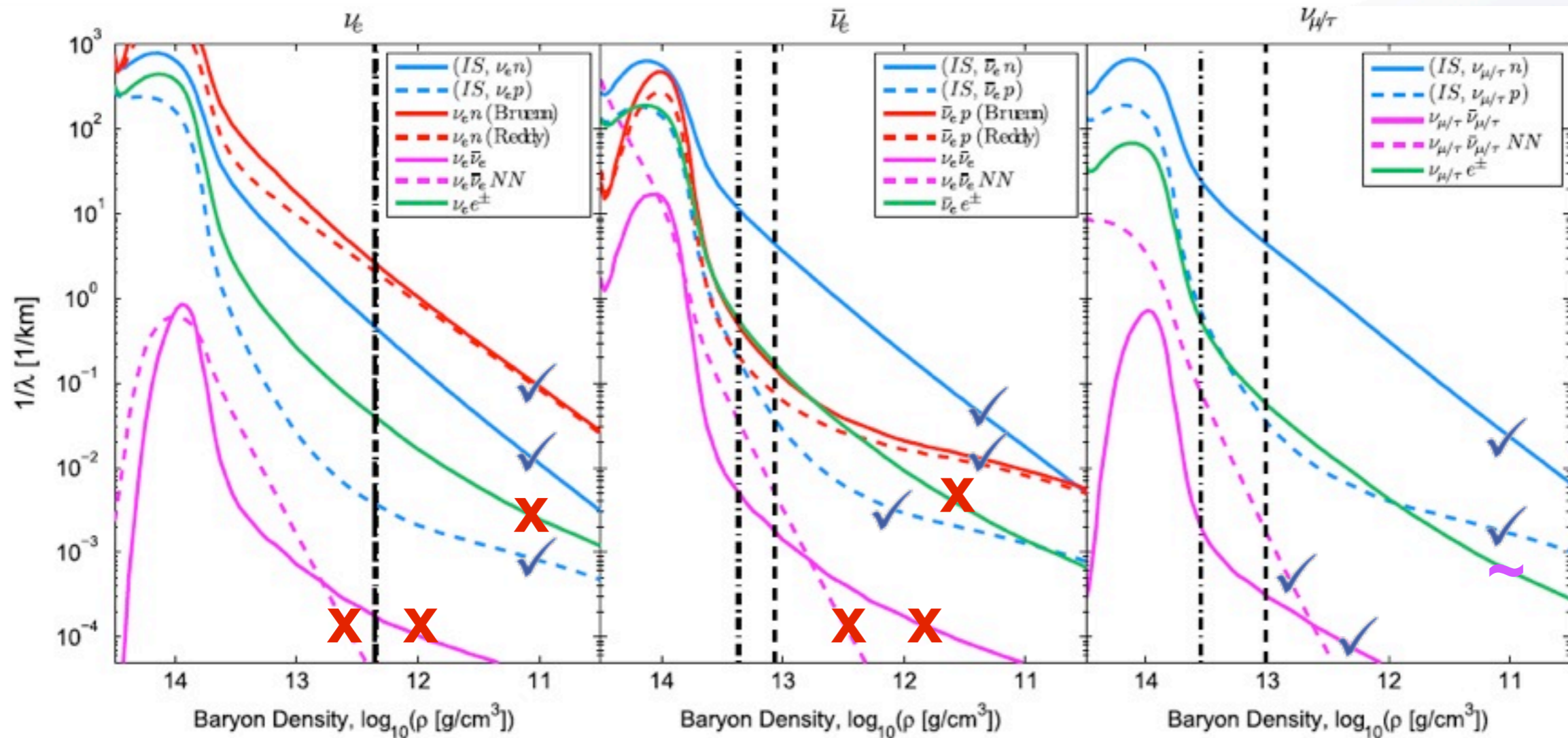
[Fischer et al. PRD85 (2012)]



- (IS,  $\nu N$ ): iso-energetic neutrino-nucleon scattering X not included here
- ( $\nu n$ ), ( $\nu p$ ): charged-current reactions
- ( $\nu \bar{\nu}$ ): pair production
- ( $\nu \bar{\nu} NN$ ): Bremsstrahlung
- ( $\nu e$ ): neutrino electron scattering (NES)

# Contribution of individual rates

[Fischer et al. PRD85 (2012)]

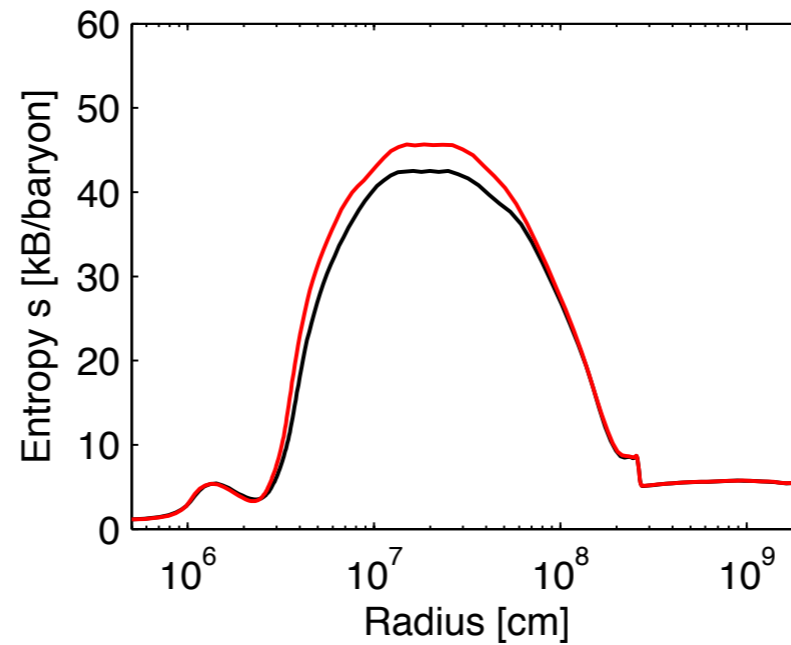
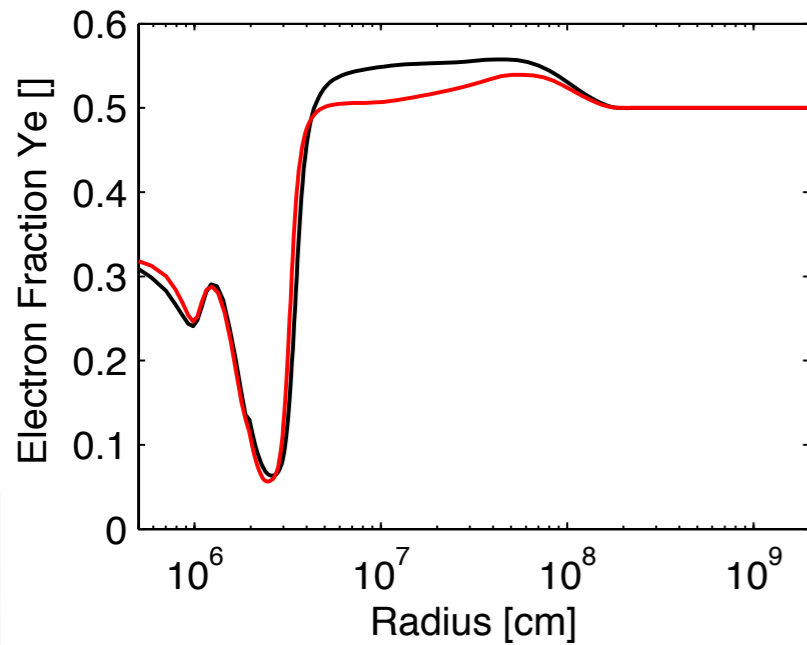
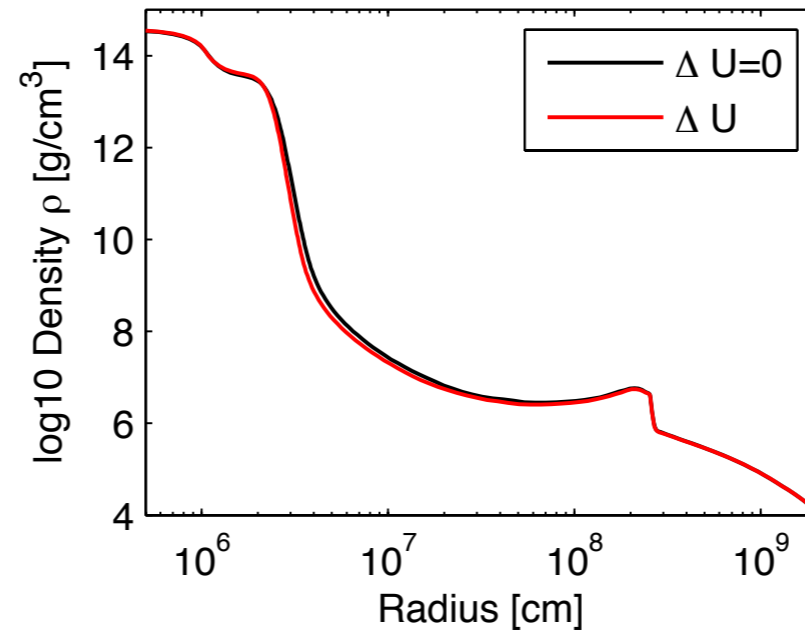
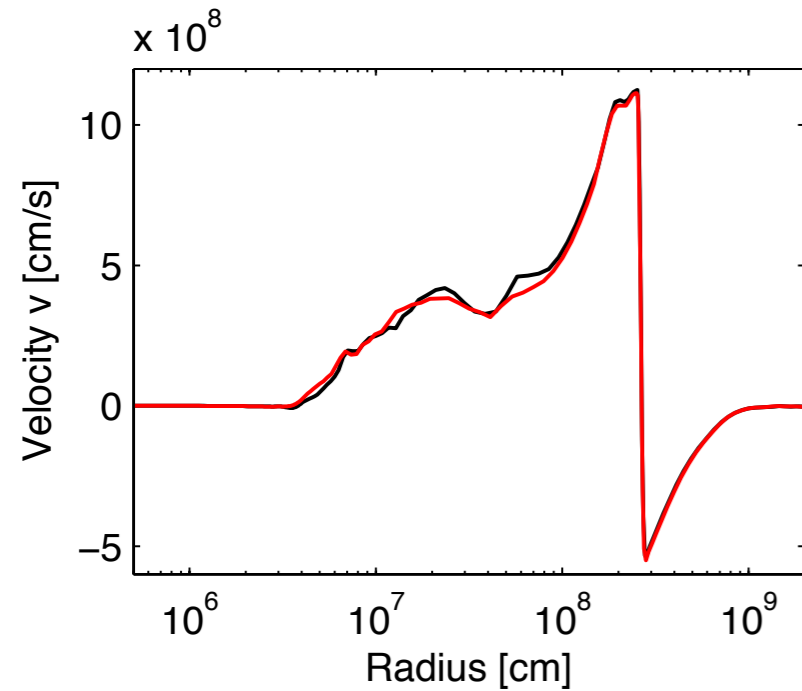


(a) 1 second after bounce

- 1s pb: NES gives an important contribution to inelastic processes of  $\bar{\nu}_e$ , i.e. thermalization
- significance increases in the later evolution

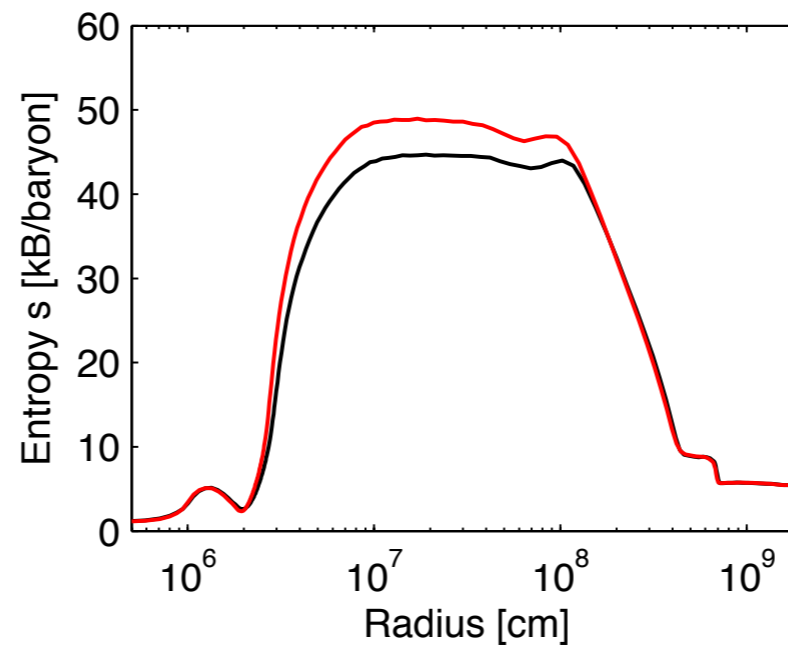
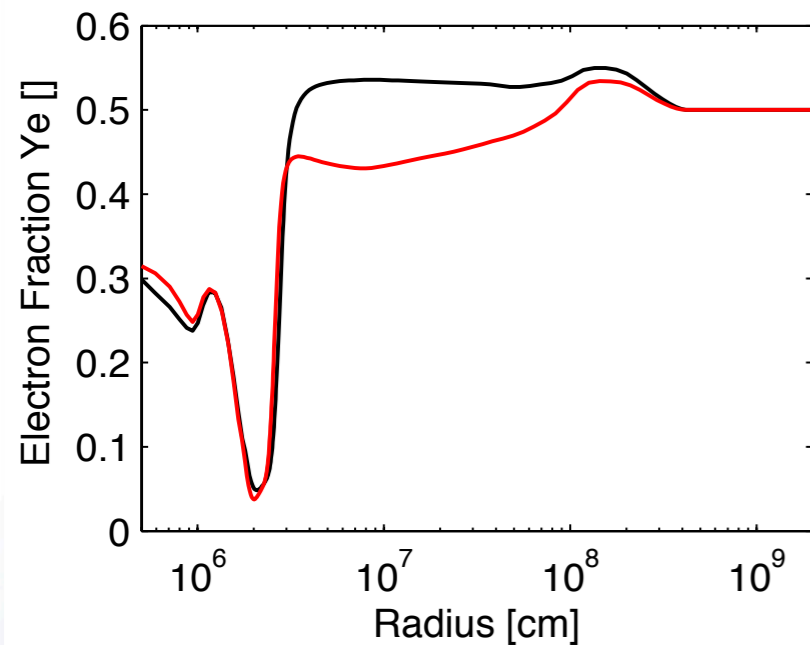
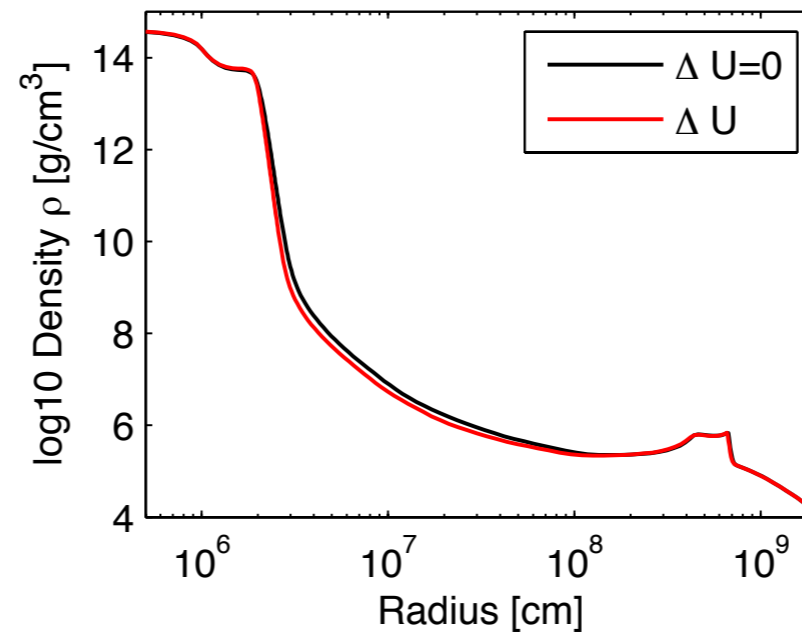
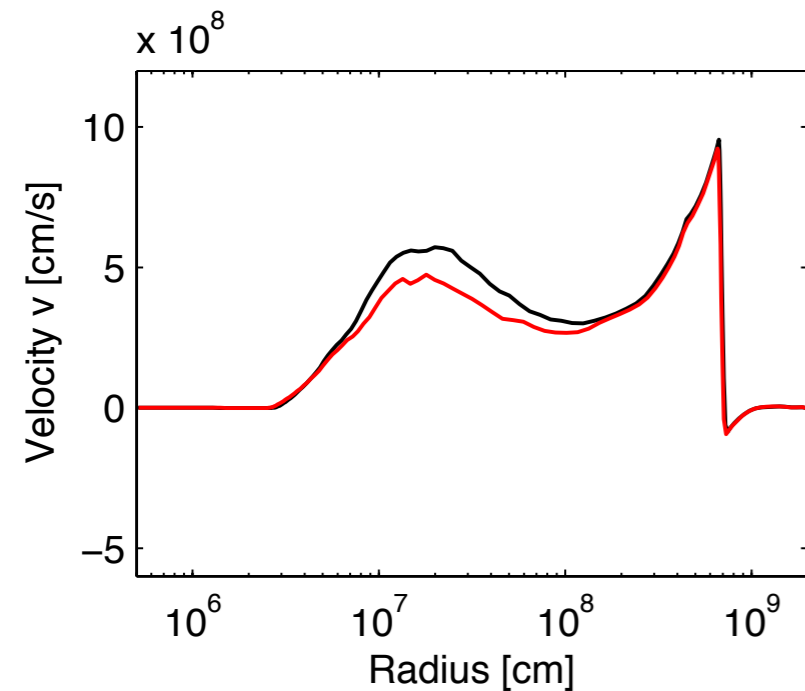
**X** not included here

# Wind formation and effect of $\Delta U$ at 0.2 s after explosion



- $t^{\text{expl}} \sim 300$  ms pb
- $E^{\text{expl}} \sim 6 \times 10^{50}$  erg
- $\Delta U$  delays explosion by 27 ms

# Wind formation and effect of $\Delta U$ at 0.5 s after explosion



- $t^{\text{expl}} \sim 300$  ms pb
- $E^{\text{expl}} \sim 6 \times 10^{50}$  erg
- $\Delta U$  delays explosion by 27 ms
- wind formation
- decrease of  $Y_e$  due to  $\Delta U$

strong effects of  $\Delta U$ : missing neutrino-reactions,  $\mu\tau$  cooling, calculation of  $\Delta U$  (?)  
→ Boltzmann neutrino-transport



# Conclusions & Outlook

- nucleosynthesis conditions in neutrino driven winds are influenced by the details of the nuclear interactions - the nucleon interaction potentials
- interesting probe of the symmetry energy
- definition of these potentials depends on the charged-current rates used
- general aim: reproduce the (local) nucleon distribution
- bound-states have to be treated explicitly
- work in progress: online publication of  $U_i$  for eight different supernova EOS tables
- identify origin of differences in first exploratory supernova simulations, compare with Boltzmann neutrino transport