

HIRSCHEGG 2013: ASTROPHYSICS AND NUCLEAR STRUCTURE
JANUARY 26 - FEBRUARY 1, 2013

$2\text{H}(d,p)3\text{H}$ and $2\text{H}(d,n)3\text{He}$ reaction rates
at astrophysical energies

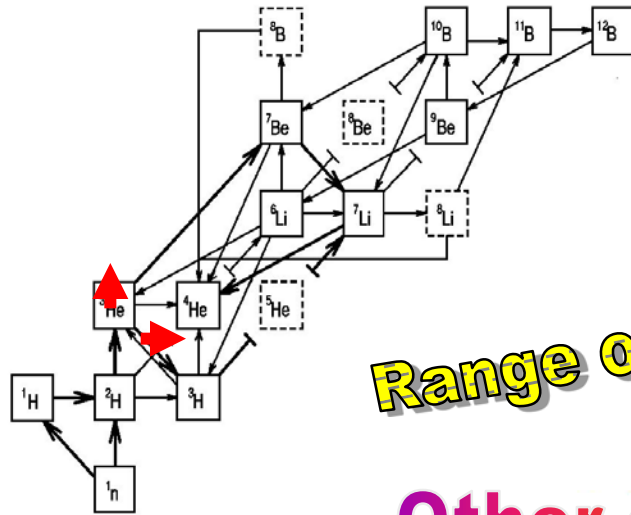
Aurora Tumino



2H+2H reactions in the primordial nucleosynthesis



$T \approx 10^9 \div 10^{11} \text{ K} - 0.1 \div 10 \text{ MeV} \quad t \approx 10^2 \div 10^3 \text{ s}$

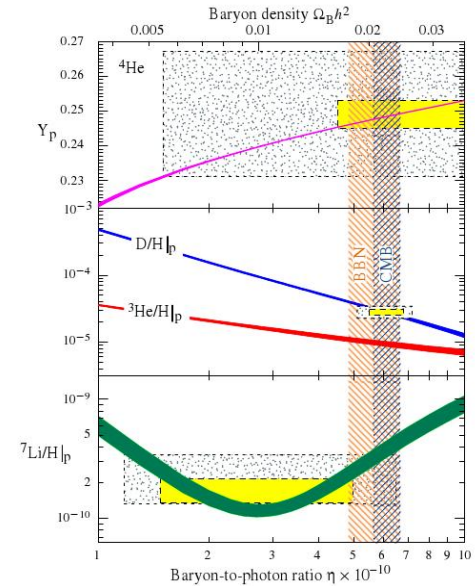


Range of interest: 50-350 keV

Other contexts of interest

- In the *Pre Main Sequence* phase (PMS) of the stellar
- In the future fusion power plants: nuclear energy production with inertial confinement

Range of interest : 0-30 keV



Status of art of the 2H+2H reactions

Prominent data sets for both ${}^2\text{H}(d,p){}^3\text{H}$ and ${}^2\text{H}(d,n){}^3\text{He}$

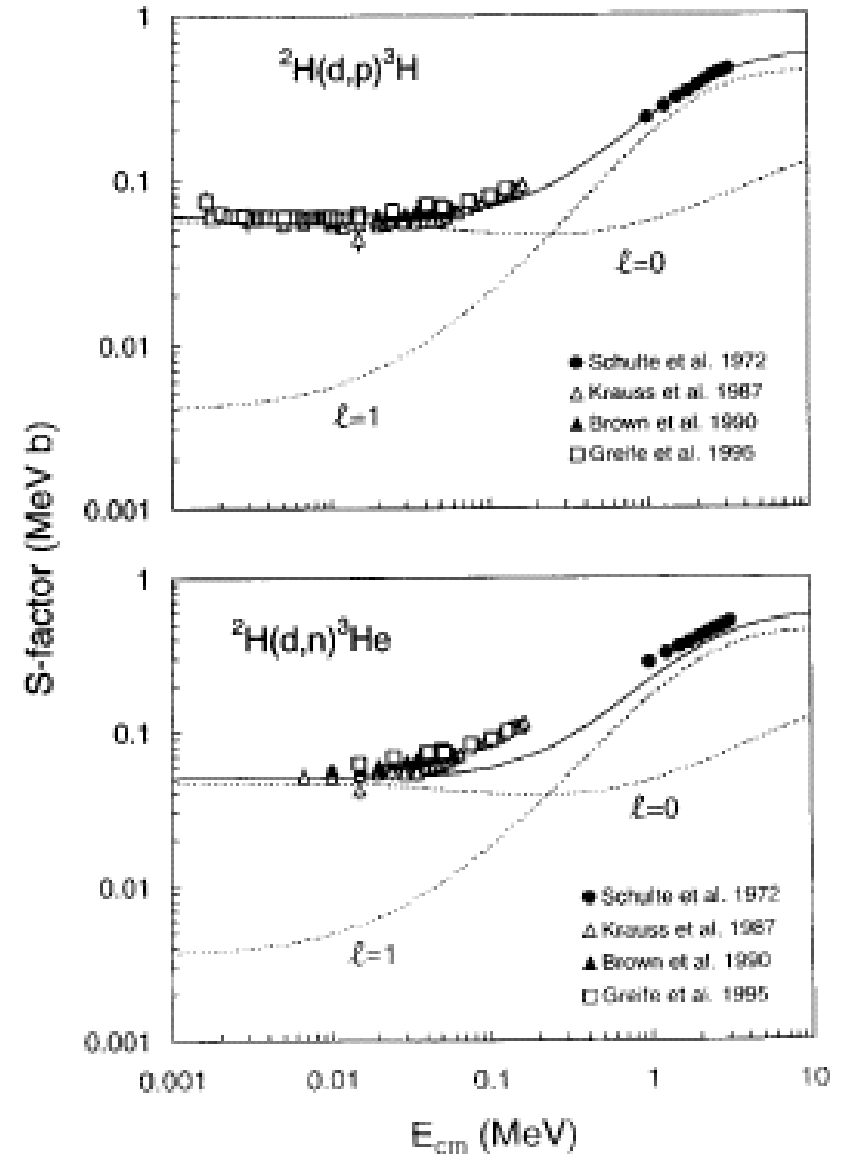
Open problems:

Missing data in the higher energy relevant BBN region: $E_{\text{cm}} = 50 - 350 \text{ keV}$

Electron screening in the ultra-low energy region below 10 keV: almost twice the adiabatic limit (14 eV)

Laboratory electron screening different from that of stellar plasma
→ Screening should be removed to assess the reaction rate correctly

→ Need to get the bare nucleus $S(E)$ factor



Trojan Horse Method

Basic principle: astrophysically relevant two-body σ from quasi-free contribution of an appropriate three-body reaction



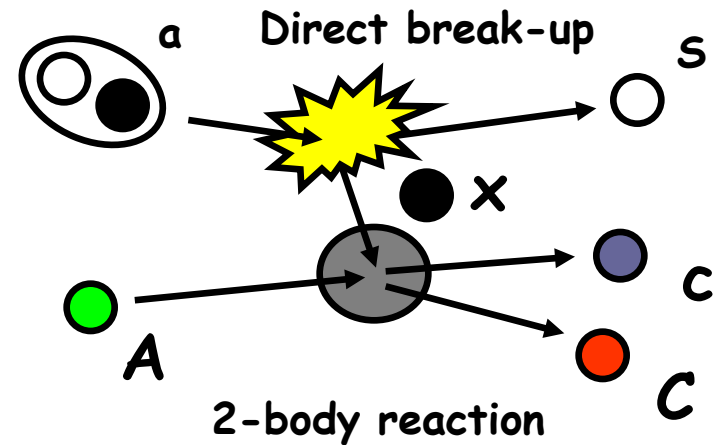
a: $x \oplus s$ clusters

Quasi-free mechanism

- ✓ only $x - A$ interaction
- ✓ $s =$ spectator ($E_s \sim 0$)

$E_A > E_{\text{Coul}} \Rightarrow$ NO Coulomb suppression

NO electron screening



In PWIA

$$\sigma_3 \propto \text{KF} |\Phi(p_s)|^2 \sigma_2$$

C. Spitaleri *et al.*, *Phys. Rev. C* 63, 005801 (2001)
 A. Tumino *et al.*, *Phys. Rev. Lett.* 98, 252502 (2007)

$$E_{\text{q.f.}} = E_{Ax} - B_{x-s} \quad \longrightarrow \quad E_{\text{q.f.}} \approx 0 \quad !!!$$

↓
 plays a key role in compensating
 for the beam energy

THM experiment

${}^2\text{H}(d,p){}^3\text{H}$ ${}^2\text{H}(d,n){}^3\text{He}$ using ${}^3\text{He}$ as TH nucleus

d-d relative energy range: from 2 keV up to 1.5 MeV

Aim:

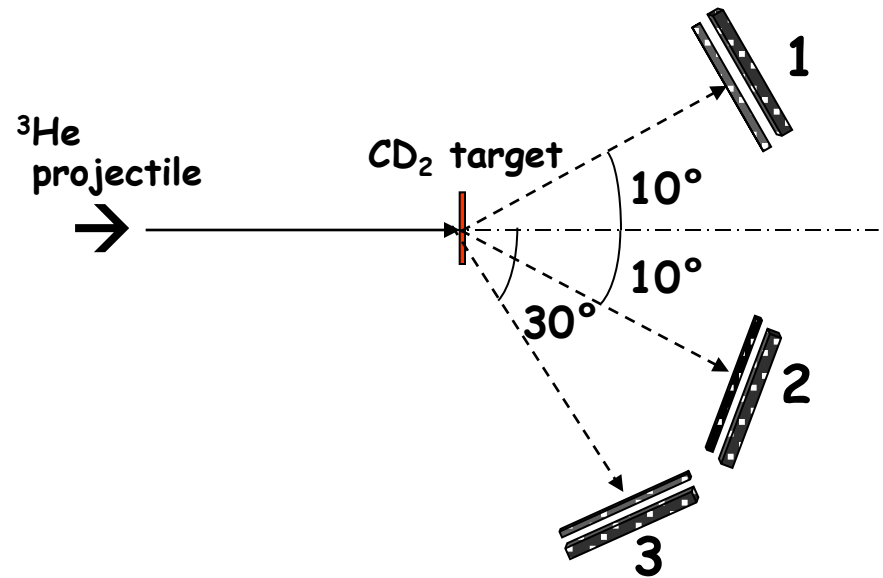
* Astrophysical factor throughout the relevant region and up, in order to have a wide energy range to be joint with available higher energy data (for the integral to converge at the relevant BBN temperature). This ensures an accurate calculation of the **reaction rate**

* Available **unscreened** data below 10 keV, needed for studying **fusion dynamics** in plasmas

Experimental set up



Nuclear Physics Institute of Academy of Science in Rez near Prague, Czech Republic

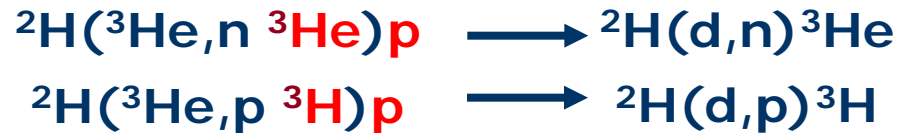


${}^3\text{H}/{}^3\text{He}$ - p coincidences (1-2 and 1-3)

For the first time detection of the proton spectator!

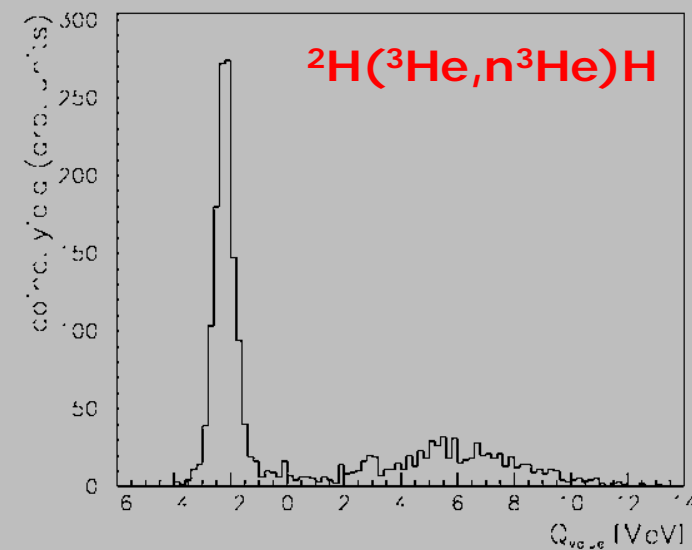
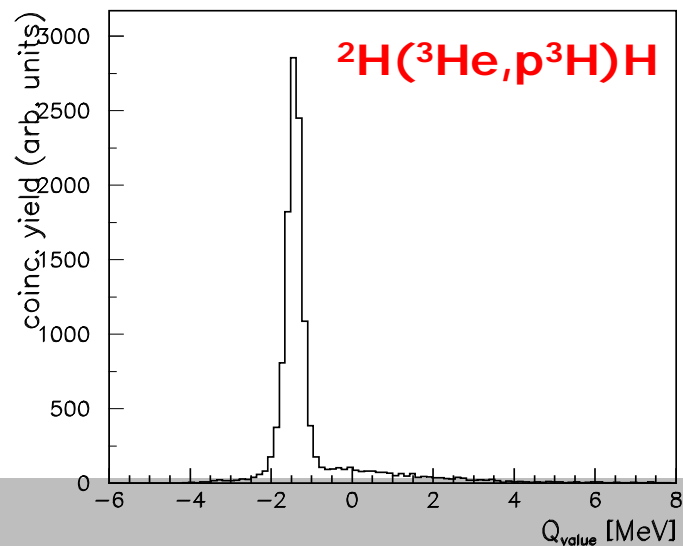
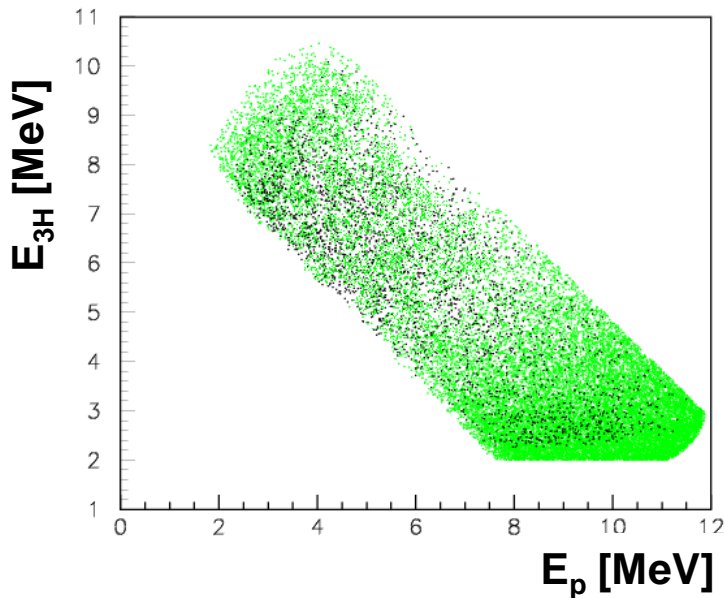
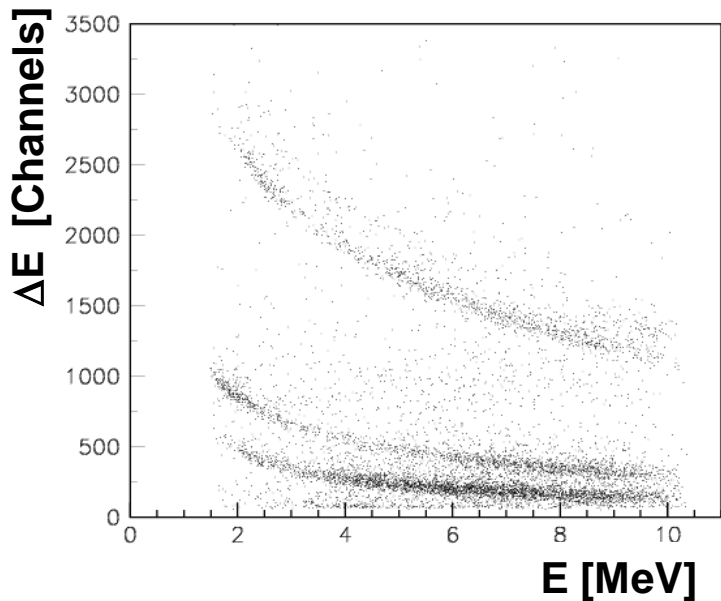
Advantages: no contribution from target break-up;
detector granularity ensured \rightarrow angular resolution of the order of 0.1° ;
100% detection efficiency

Not possible with neutron detectors



Data analysis follows standard procedure

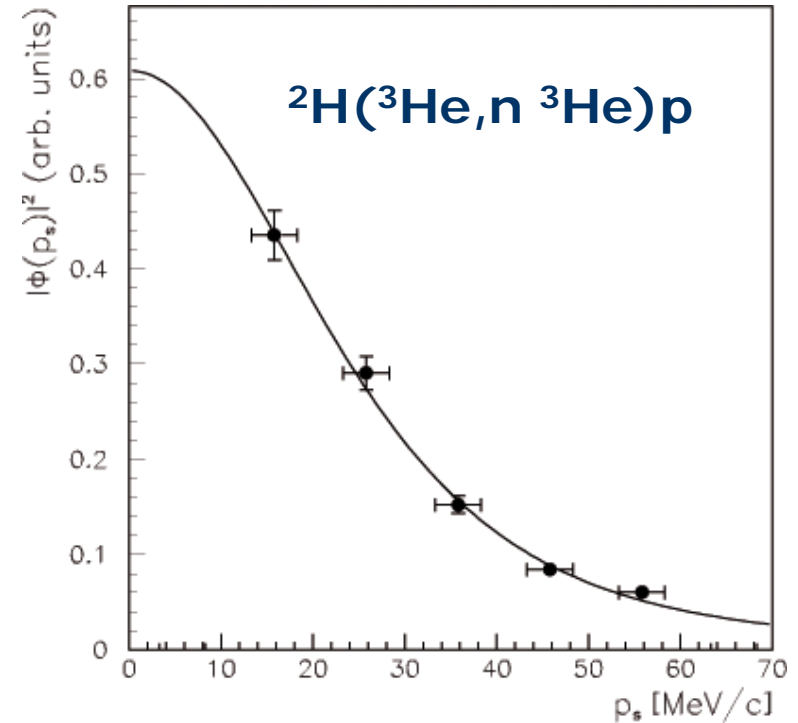
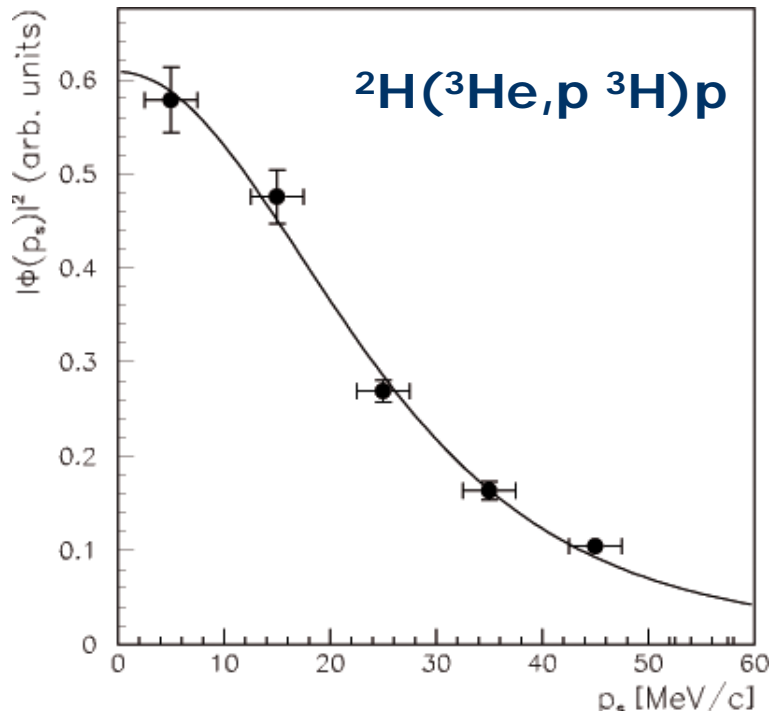
Selection of the 3-body channels



Selection of the quasi-free mechanism

Comparison between the experimental momentum distribution and the theoretical one (for ${}^3\text{He}$ given by the Eckart function) \rightarrow QF mechanism

$$|\Phi(\vec{p}_s)|^2 \propto \frac{d^3\sigma}{d\Omega_t d\Omega_p dE_p} \frac{1}{(KF) \left(\frac{d\sigma_{dd}}{d\Omega} \right)^N}$$



Extraction of the two-body cross section (1)

R-matrix by C. Angulo and P. Descouvemont (NPA 639 (1998) 733)

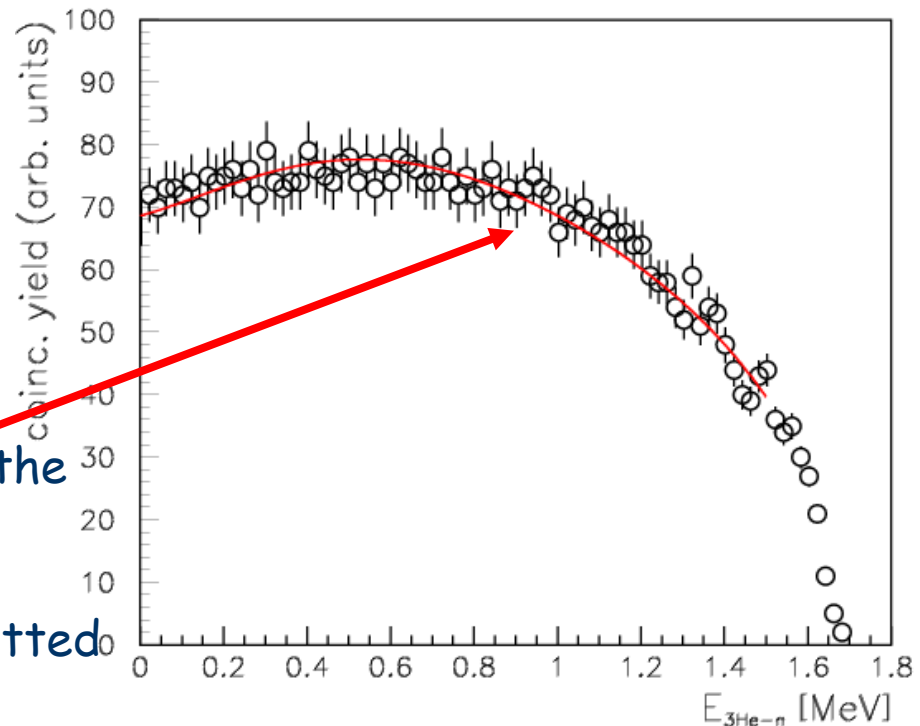
Inclusion of both $l=0$ and $l=1$ components in the cross section, whose energy dependence is very well represented by their penetrabilities

$$\frac{d\sigma}{dE d\Omega}(d + d \rightarrow C + c) = \frac{1}{E_{cm}} \sum_{l=0,1} C_l P_l^2 T_l(k_{dd} R)$$

$$\frac{d\sigma_3}{dE} = \text{KF} |\varphi(p_s)|^2 \frac{d\sigma}{dE}$$

Free parameters are scaling factors C_l and channel radius R : determined from the fit of the theoretical distributions to the measured coincidence yields

Two coincidence yields per channel to be fitted at the same time

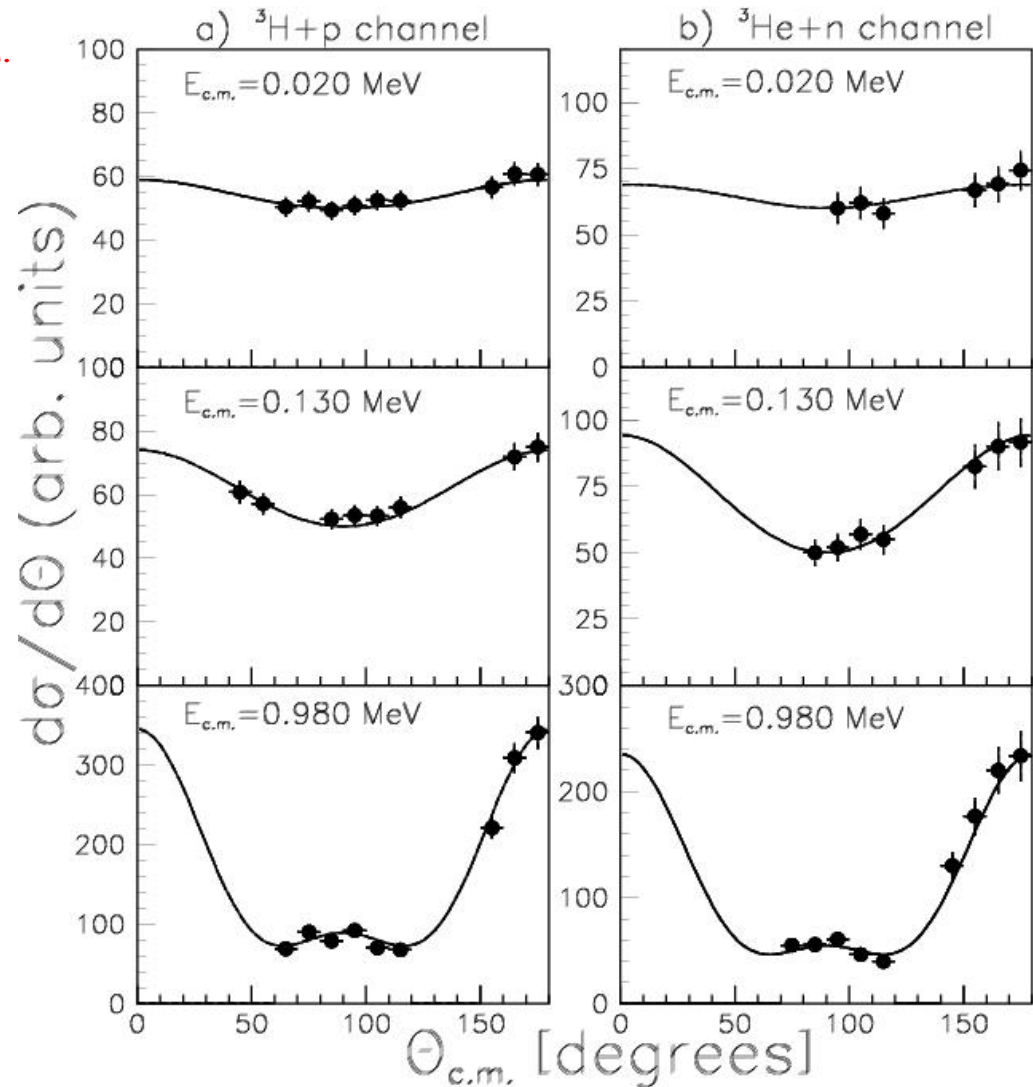


Extraction of the two-body cross section (2)

$$d\sigma/d\theta_{c.m.} = \frac{\text{Coinc. yield at fixed } \Delta E_{c.m.}}{KF |\phi(p_s)|^2}$$

Solid lines: fit of direct data by

A. Krauss *et al.*, Nucl. Phys. A465, 150 (1987)
 R.L. Schulte *et al.*, Nucl. Phys. A192, 609 (1972)

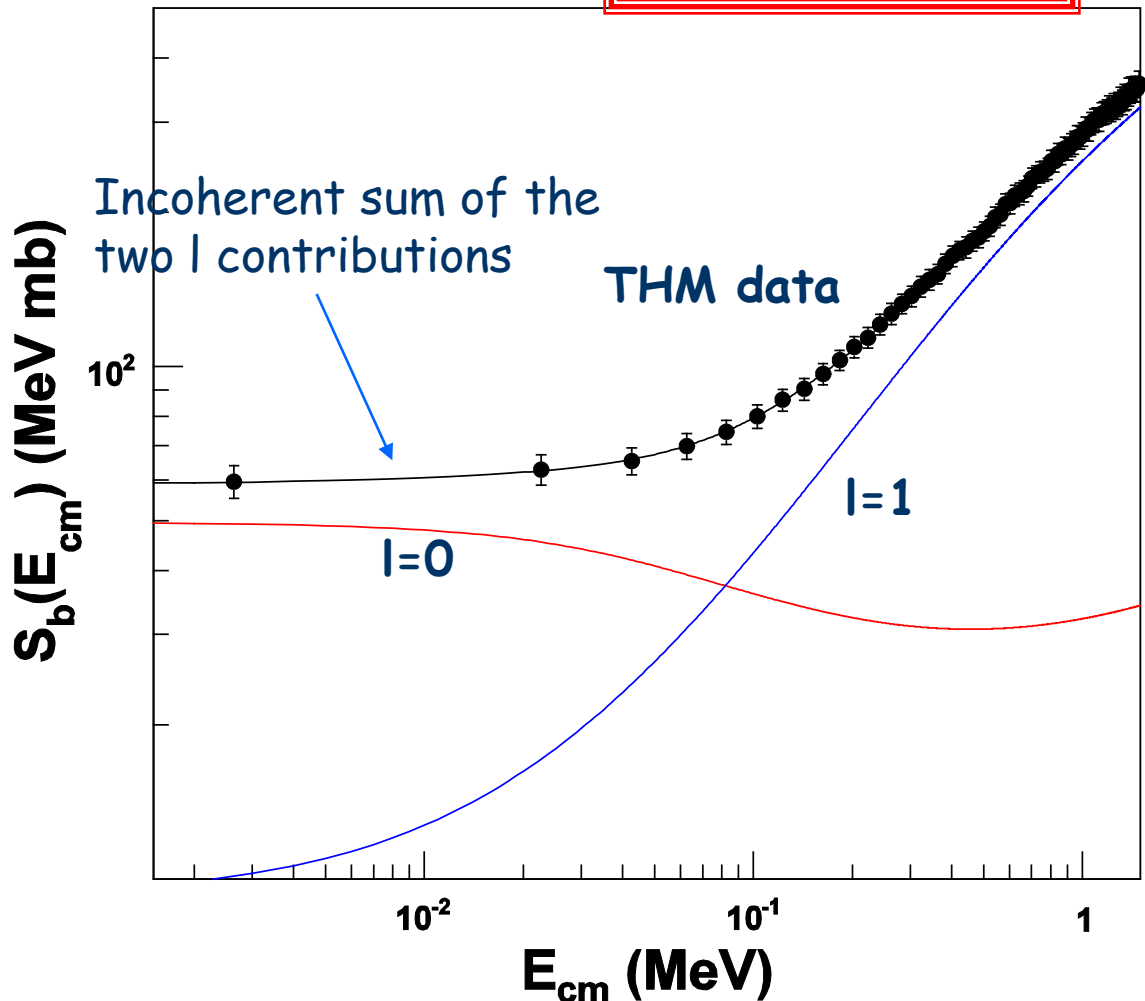


Extraction of the two-body cross section (3)

$$S(E) = \sigma(E) E e^{2\pi\eta}$$

With the deduced scaling ratio of the s and p waves, $\rightarrow S(E)$ factor after normalization to direct data

Direct data have different accuracies \rightarrow weighted normalization to available direct data from 15 keV to 1.5 MeV



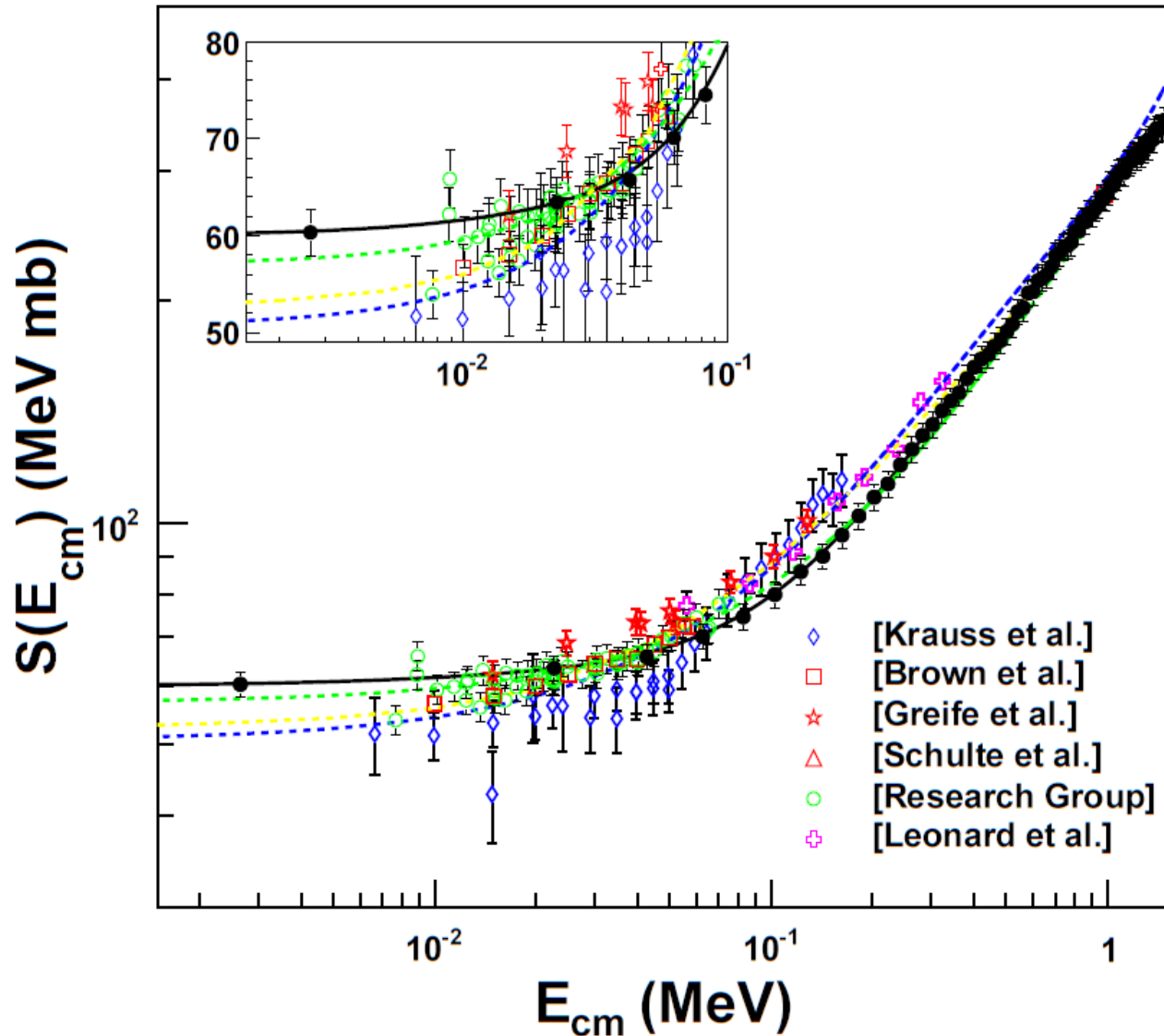
Extraction of the two-body cross section (4)

Comparison between the incoherent sum (black line) and direct data (colored symbols)

Yellow line: polynomial expansion reported in the NACRE compilation
C. Angulo et al., NPA 656, 3 (1999)

Blue line: from
R.H. Cyburt, PRD 70, 023505 (2004)

Green line: from
P. Descouvemont et al., At. Data Nucl. Data Tables 88, 203 (2004)



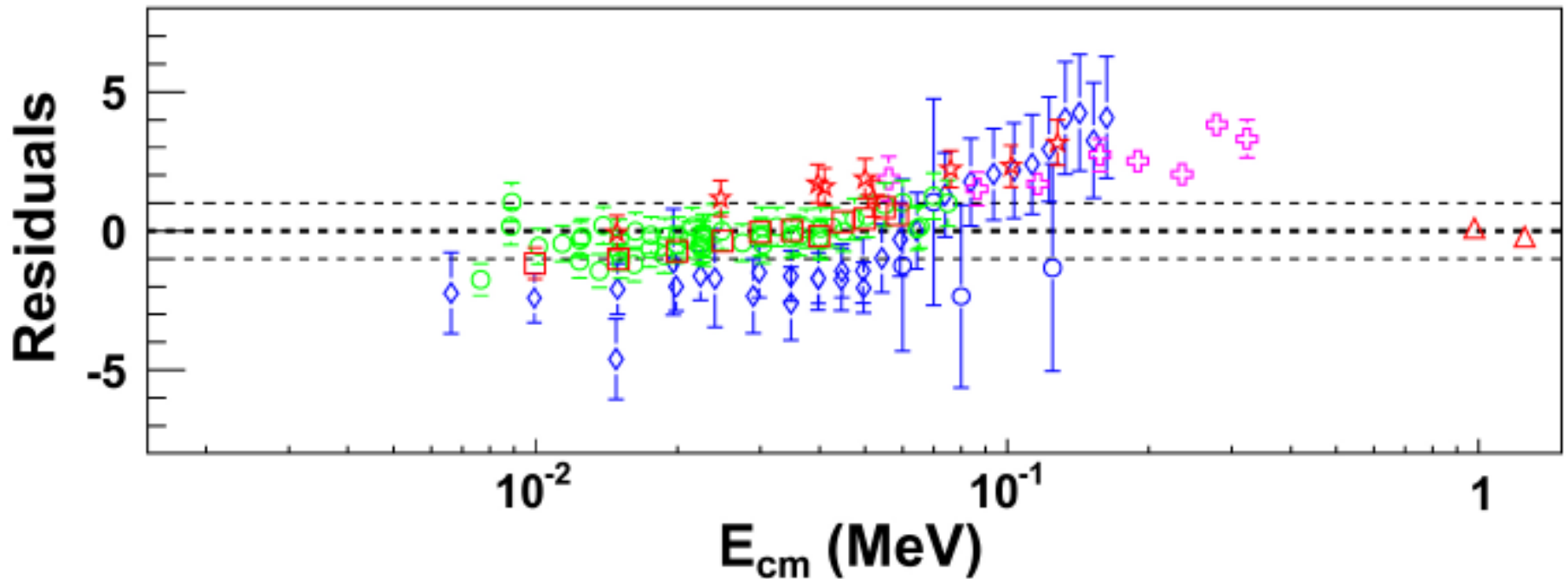
A. Tumino et al., Few Body Syst. 50 (2011) 323

A. Tumino et al., Phys. Lett. B 700 (2011) 111

Residual scattering in the direct data about the THM theoretical curve divided by the weighted dispersion σ (4.24 keVb for the $3\text{He}+n$ channel)

Dashed horizontal lines: 1-sigma error bars. These plots help to visualize the trends of the deviation from the normalized theoretical $S(E)$ factor for each of the direct data sets.

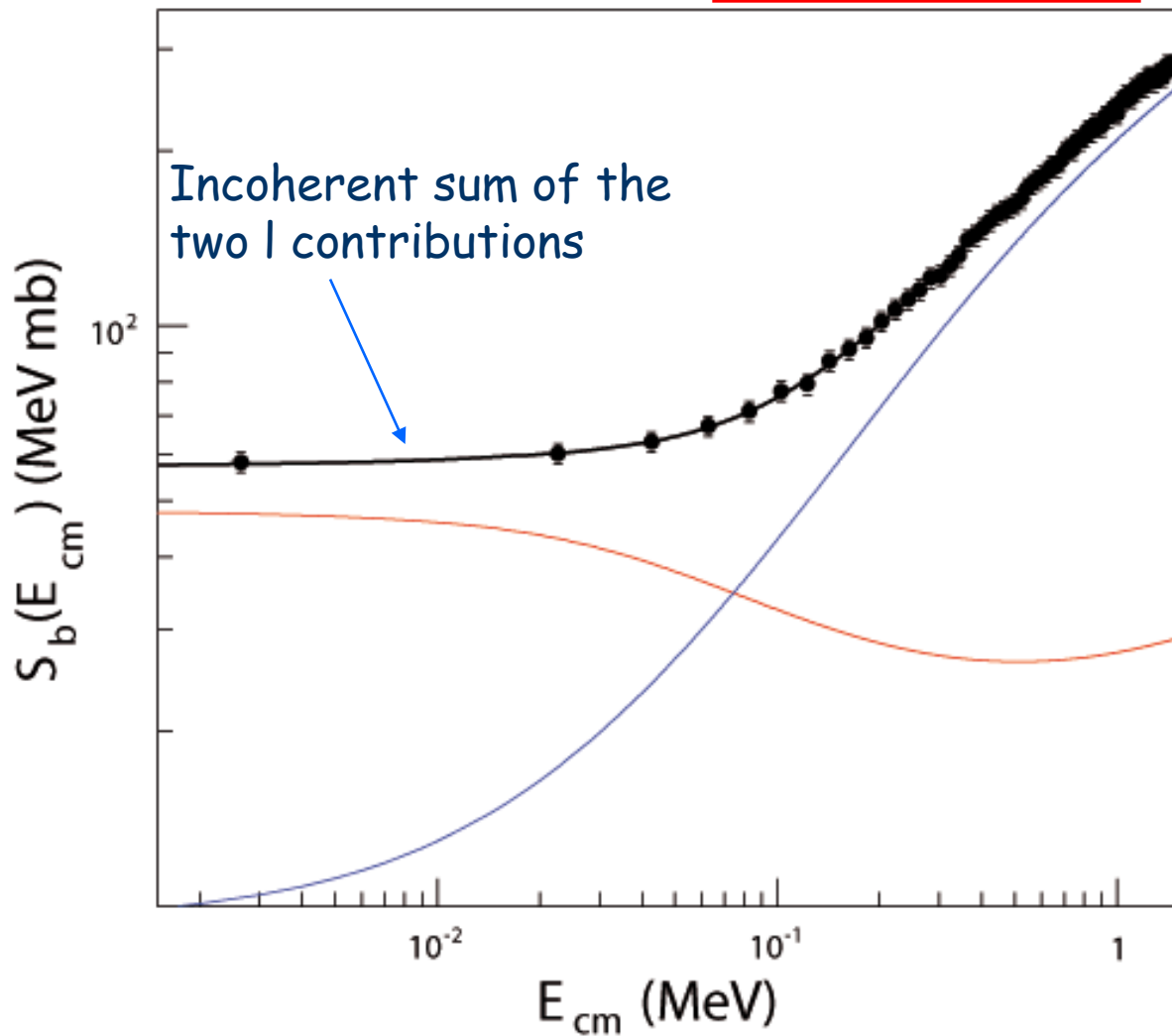
$\sigma=4.24$ keVb



Extraction of the two-body cross section (3)

${}^2\text{H}({}^3\text{He}, p){}^3\text{H}$

$$S(E) = \sigma(E) E e^{2\pi\eta}$$



Extraction of the two-body cross section (4)



Direct data at 15 keV
normalized to the THM bare
 $S(E)$ and fitted with

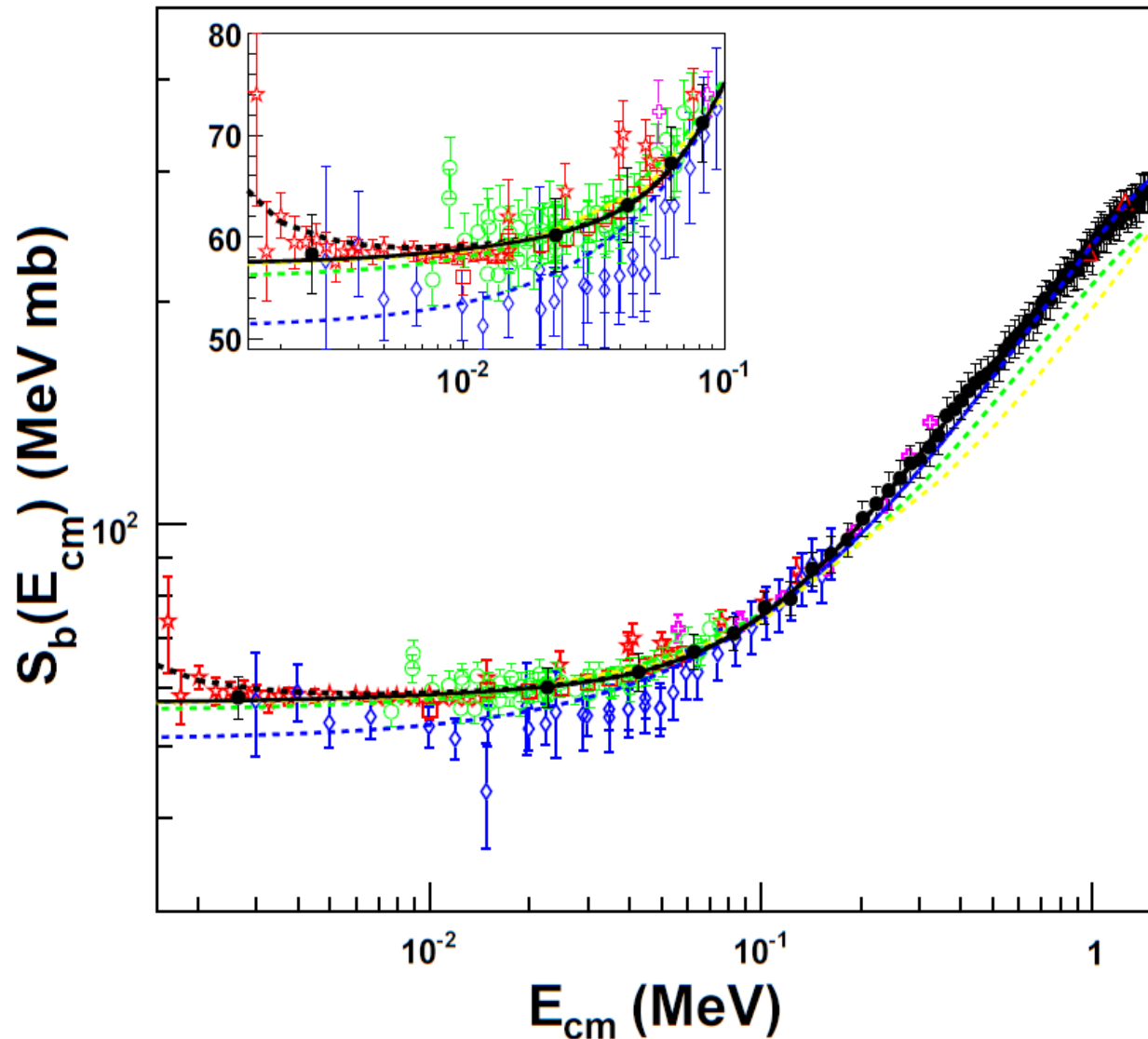
$$f_{\text{lab}}(E) = \exp(U_e/E)$$

(Assenbaum, H.J. et al., 1987, Z. Phys. A,
327, 461)

with the screening potential
 U_e as free parameter:

$$\rightarrow U_e = 13.2 \pm 1.8 \text{ eV}$$

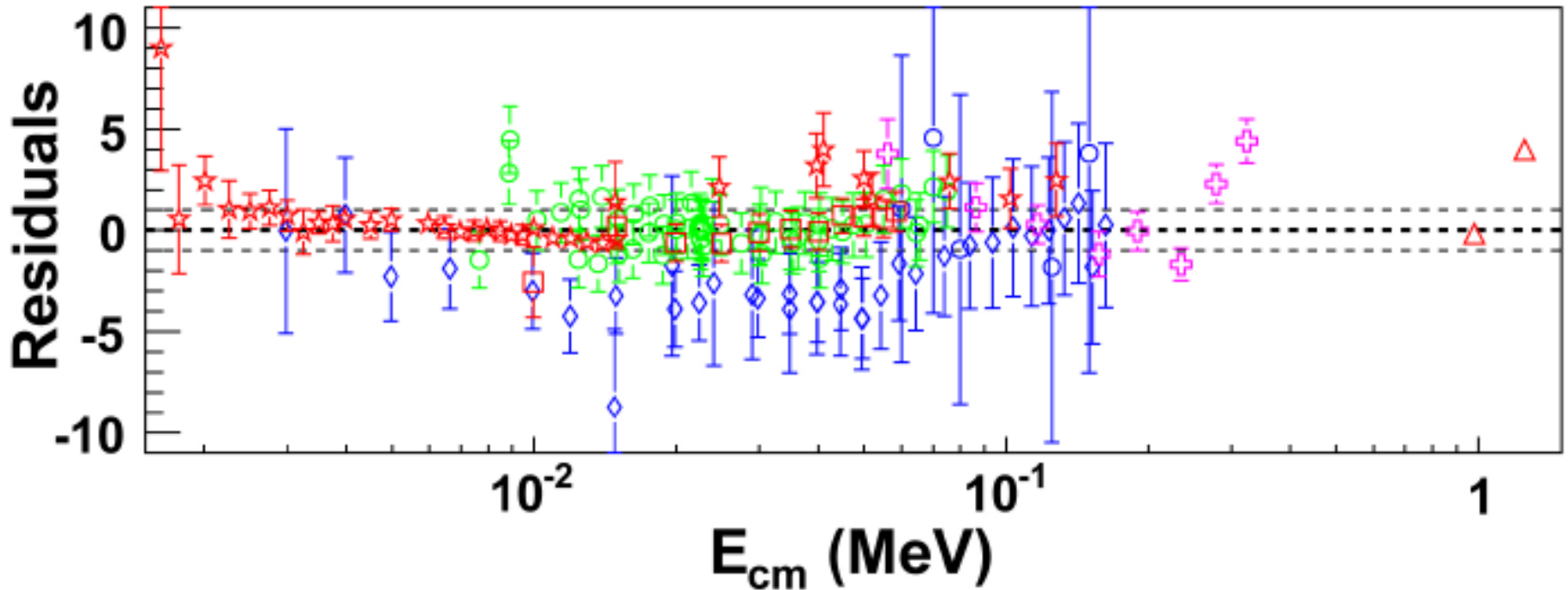
In agreement with the
adiabatic limit



Residual scattering in the direct data about the THM theoretical curve divided by the weighted dispersion σ (1.82 keVb for the $^3\text{H}+p$ channel)

Dashed horizontal lines: 1-sigma error bars

$\sigma = 1.82 \text{ keVb}$



Tentative estimate of the screening potential from $d+d \rightarrow n+{}^3\text{He}$

Ingredients:

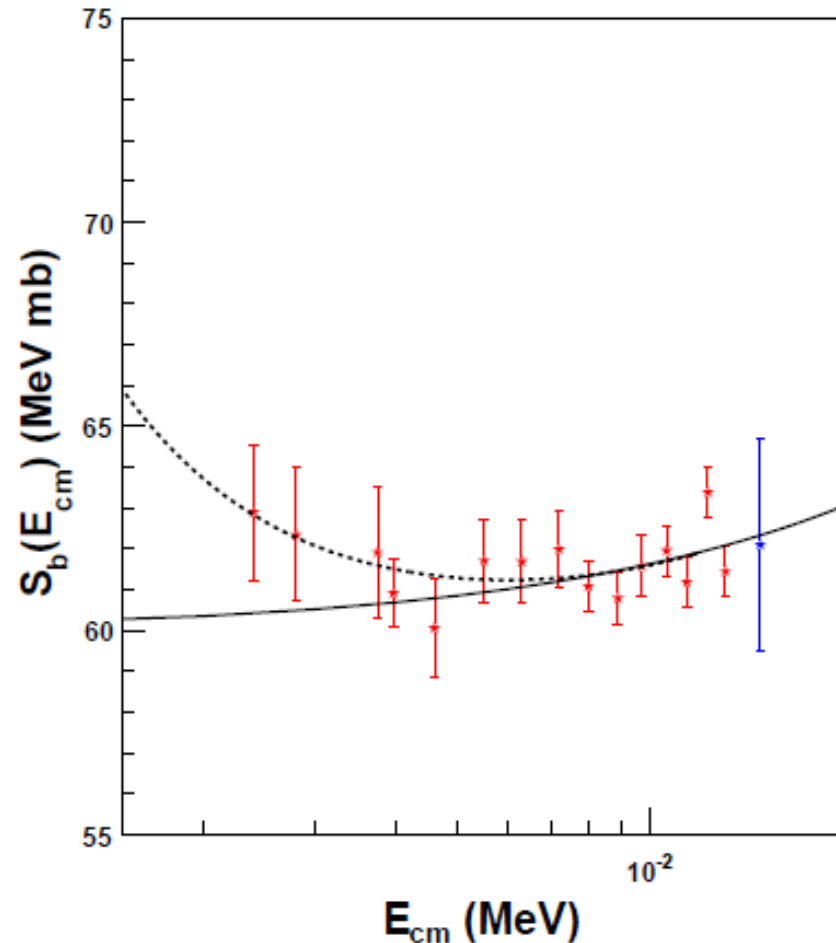
- $\sigma_{\text{pt}} / \sigma_{n3\text{He}}$ from Greife et al. 1995, with $\sigma_{n3\text{He}}$ further corrected by a factor 1.02 to be consistent with their data in far geometry

- THM bare $S(E)$ factor

- screening function with U_e as free parameter

$$\rightarrow U_e = 11.7 \pm 1.6 \text{ eV}$$

in agreement within experimental errors with the previous estimate from $d+d \rightarrow t+p$



Some numbers

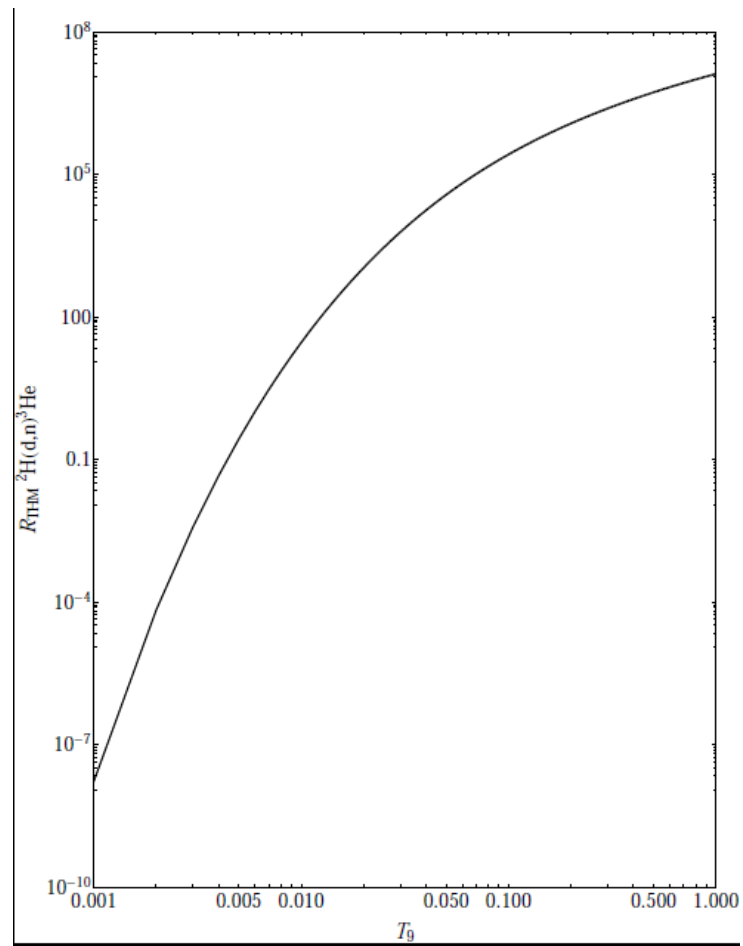
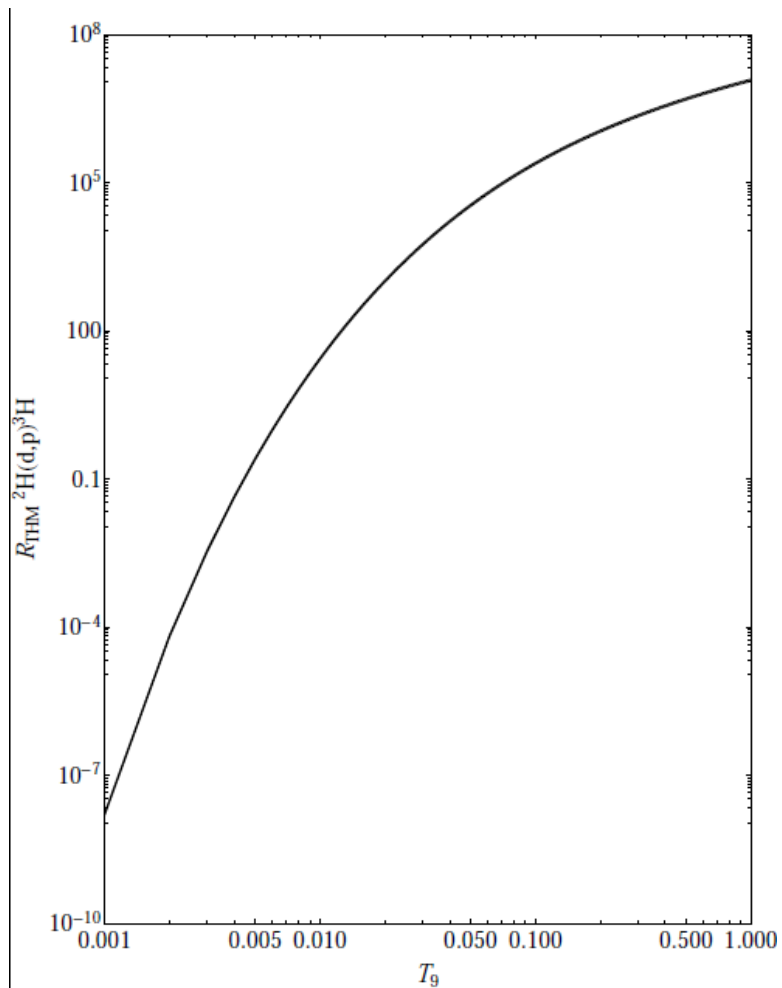
S(0) for $^3\text{He}+n$ [keV b]	$\Delta S(0)$ [keV b]	Ref.
60.1	1.9	Present results from THM
53 keV		C. Angulo et al. (NACRE)
50.67 keV		R.H. Cyburt
57.2 keV	3.5	P. Descouvemont et al.

S(0) for $^3\text{H}+p$ [keV b]	$\Delta S(0)$ [keV b]	Ref.
57.4	1.8	Present results from THM
56 keV		C. Angulo et al. (NACRE)
51.15 keV		R.H. Cyburt
57.1 keV	1.8	P. Descouvemont et al.

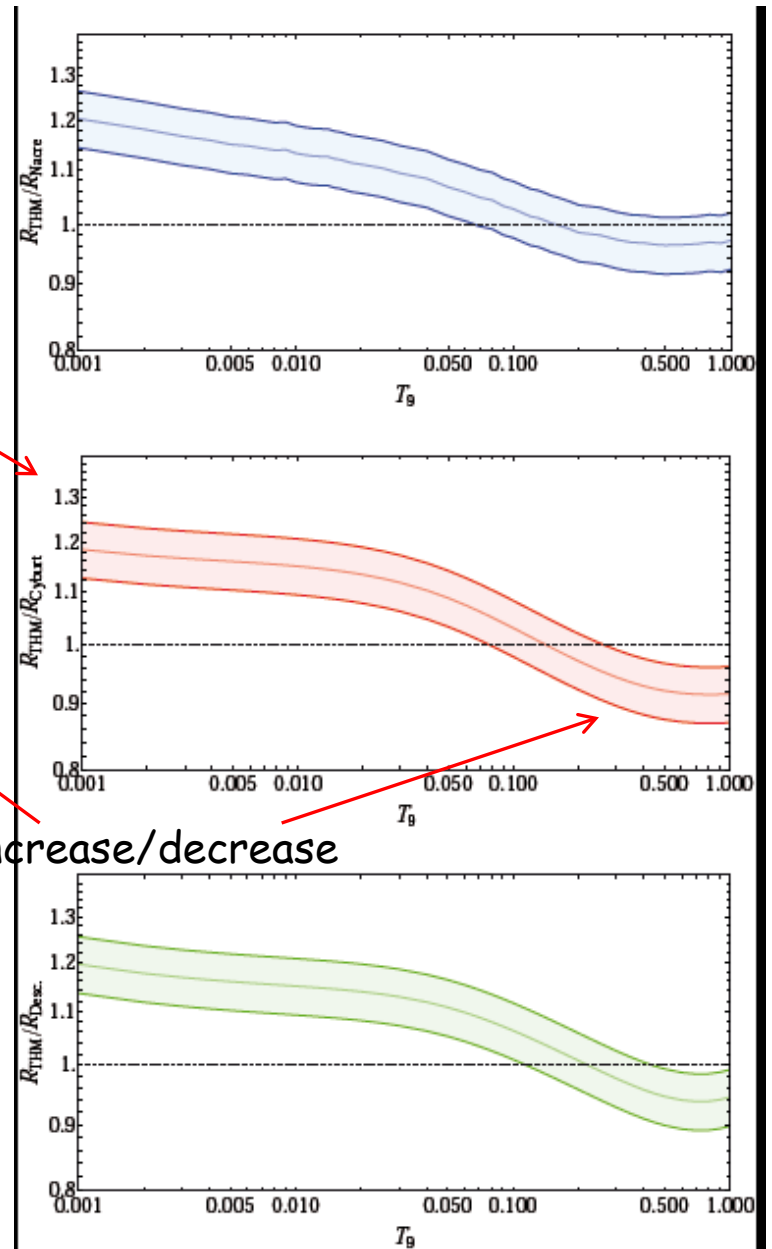
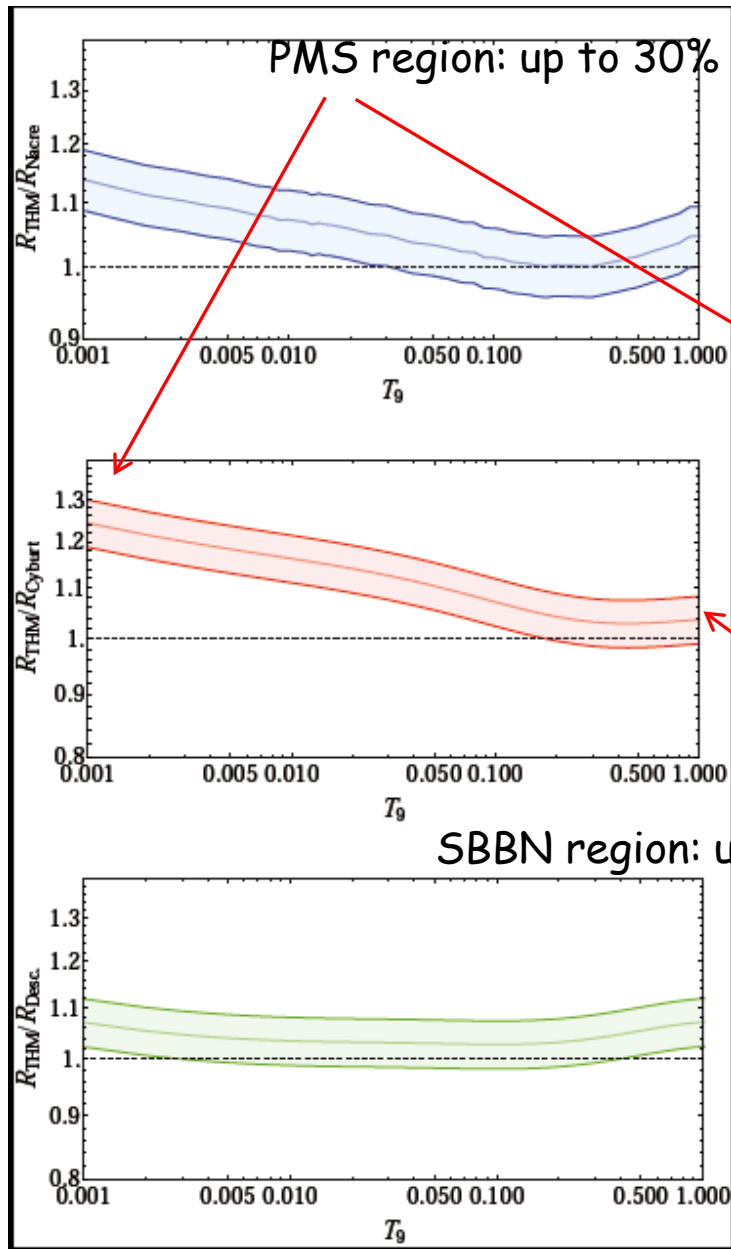
However, none of the lines provide the correct slope of the THM data throughout the investigated region, with deviations by more than 15%.

$S(0)_{^3\text{H}+p} S(0)_{^3\text{He}+n} = 0.96 \pm 0.04$ in agreement with prediction by A. Bonasera and S. Kimura: this little difference in the $S(0)$ values is attributed to the different Q -values of the two mirror $d + d$ fusion channels.

Reaction rates



THM results compared with the calculated reaction rates available in the literature



Conclusions

${}^2\text{H}(d,n){}^3\text{He}$ and ${}^2\text{H}(d,p){}^3\text{H}$ via ${}^2\text{H}({}^3\text{He},n){}^3\text{He}$ and ${}^2\text{H}({}^3\text{He},p){}^3\text{H}$: first experiments where the spectator is detected

$S(E)$ factor and reaction rates determined from 2 keV up to 1.5 MeV, throughout the energy region of interest for pure and applied physics and up

Estimate of screening potential from ${}^3\text{H}+p$: $U_e = 13.2 \pm 1.8$ eV

Tentative estimate from ${}^3\text{He}+n$: $U_e = 11.7 \pm 1.6$ eV

...both in agreement with the adiabatic limit

... next step \rightarrow astrophysical implications: applying recent abundance sensitivity studies (Coc & Vangioni 2010), the new rates imply a 8% decrease in the ${}^7\text{Li}$ abundance ... solving the Li depletion problem ?!

PMS: up to 30% variations in the rates and new investigation of fusion dynamics in plasmas

Thank you!

The collaboration

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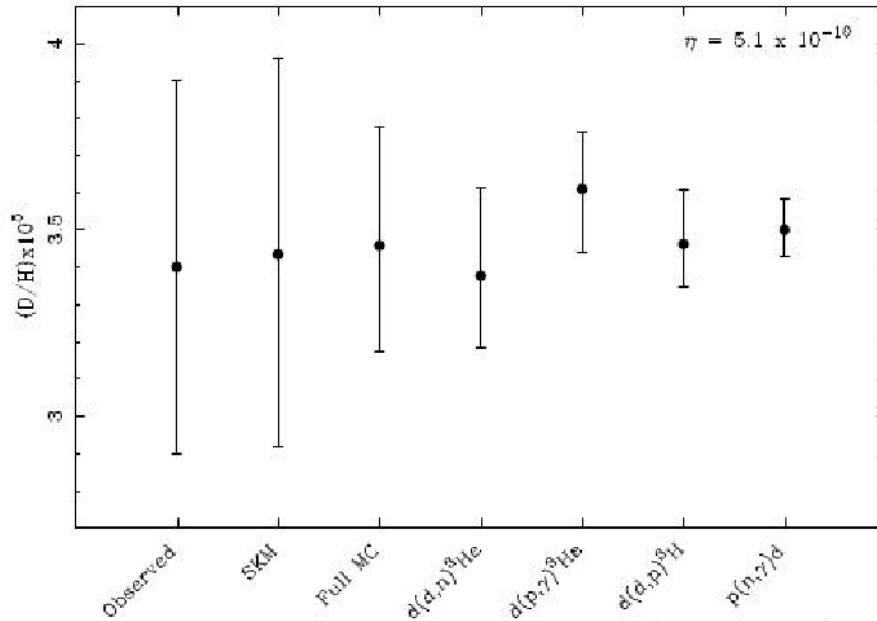
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Deuterium and uncertainty of η



Uncertainty on η from deuterium:
 50% observative
 50% cross section uncertainty
 of reactions involving deuterium.

[Smith et al., 1993]

