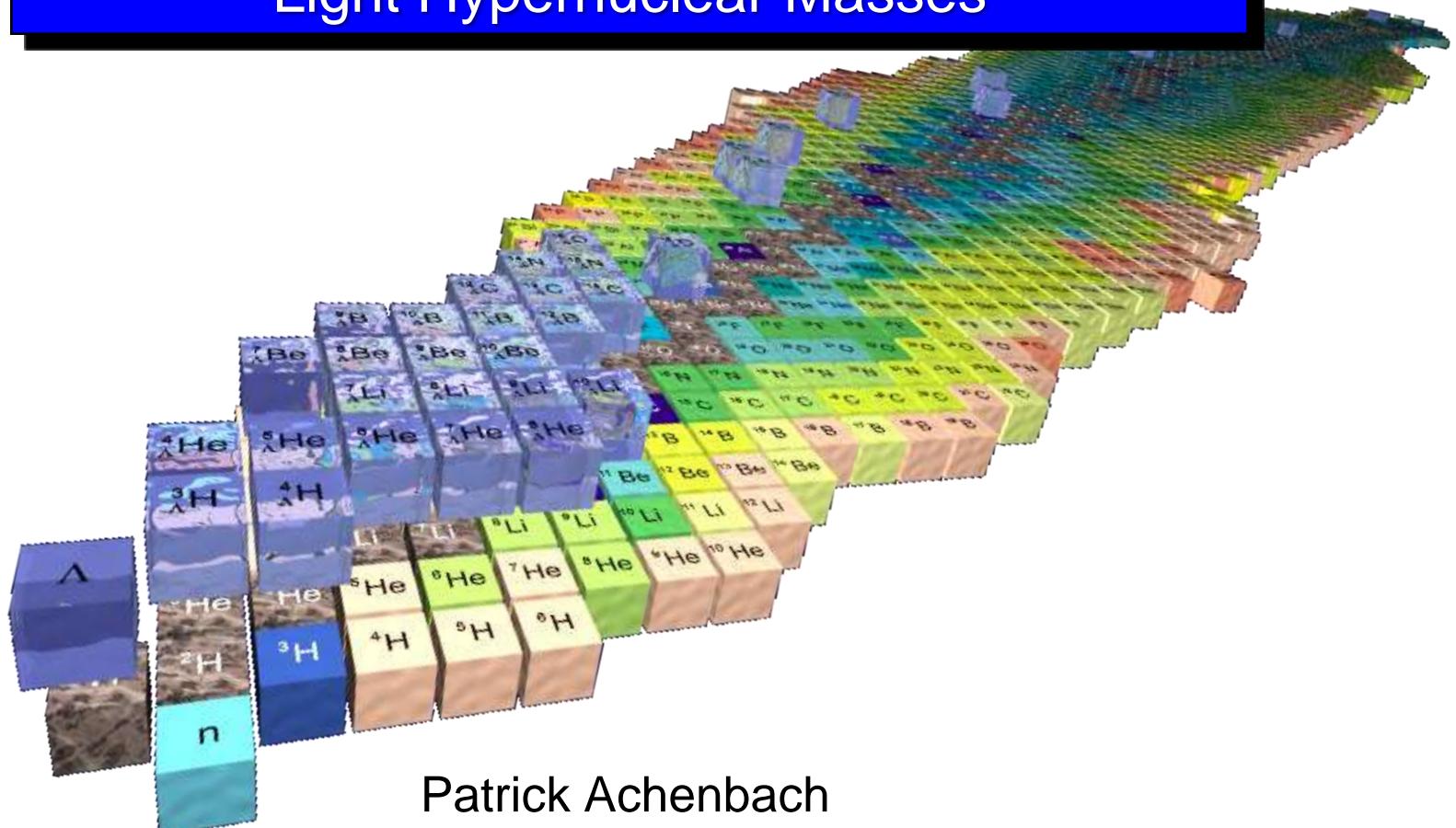


Precision Spectroscopy of Light Hypernuclear Masses



Jan. 2015

First observation of a hypernucleus

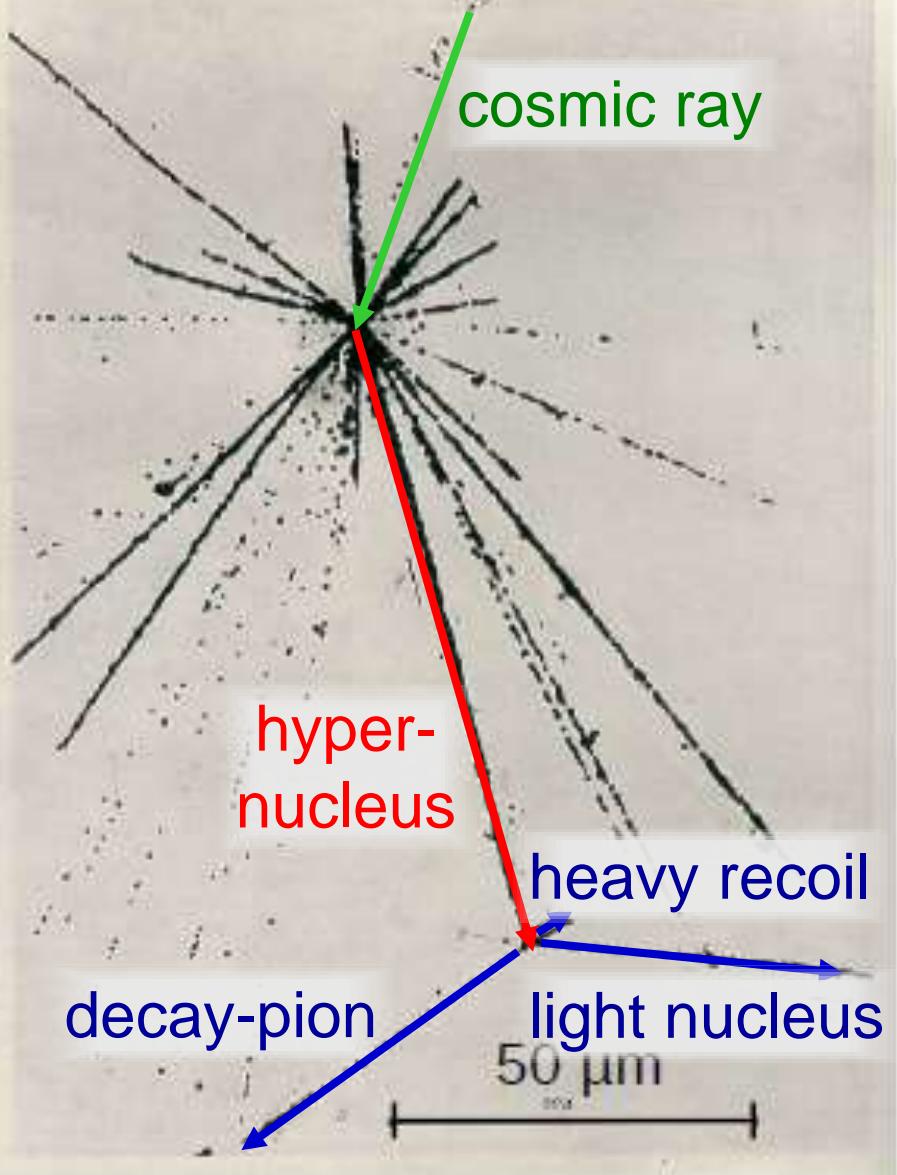
*Delayed Disintegration of a Heavy Nuclear Fragment : I **

By M. DANYSZ and J. PNIEWSKI

Institute of Experimental Physics, University of Warsaw †

“An alternative explanation of the event may be sought in terms of the heavy neutral V-particle [...] It is possible that such particles exist not only as free particles, but also in bound states within nuclei.”

- production in nuclear fragmentation
- identification through pionic decay



[M. Danysz & J. Pniewski, Philos. Mag. 7 (44), 348 (1953)]

List of known hypernuclear masses

	E1	A	J(g.s.)	B_Λ (g.s.)
H	3	1/2+	0.13	5
	4	0+	2.04	4
He	4	0+	2.89	3
	5	1/2+	3.12	2
Li	6		4.18	10
	8		7.16	70
	6			
Be	7	1/2+ ^a	5.58	3
	8	1-	6.80	3
	9		8.50	12
B	7	1/2+	5.16	8
	8		6.84	5
	9	1/2+	6.71	4
C	10		9.11	22
	9		8.29	18
	10		8.89	12
C	11		10.24	5
	12	1-	11.37	6
	12	1-	10.80	18 ^b
	13	1/2+	11.69	12
	14		12.17	33

	E1	A	J(g.s.)	B_Λ (g.s.)
N	14			
	15		3/2+ ^c	
O	16			13.76 16 ^d
	16	0-		12.42 5
Al	18			
	27			
Si	28			16.6 2
	32			
Ca	40			
	51			20.0 2
V	56			
	89			23.1 5
Fe	139			24.5 12
	208			26.3 8
La	209			

$$- B_\Lambda = M_{HYP} - (M_{Core} + m_\Lambda)$$

poor hypernuclei data
compared to ordinary nuclei:

- nuclear structure information for ~ 28 hypernuclides vs. 3175 nuclides
- mass error given by error on Λ binding energy of ~ 20-800 keV for hypernuclei vs. ϵ

Experimental data in MeV from
[Nuclear Wallet Cards, BNL, 2011]

Medium to heavy hypernuclei A > 14

E1	A	J(g.s.)	B _A (g.s.)
N	14		
	15	3/2+ ^c	
O	16		13.76 16 ^d
	16	0-	12.42 5
	18		
Al	27		
	28	e	
Si	28		16.6 2
S	32		
Ca	40		
V	51		20.0 2
Fe	56		
Y	89		23.1 5
La	139		24.5 12
Pb	208		26.3 8
Bi	209		

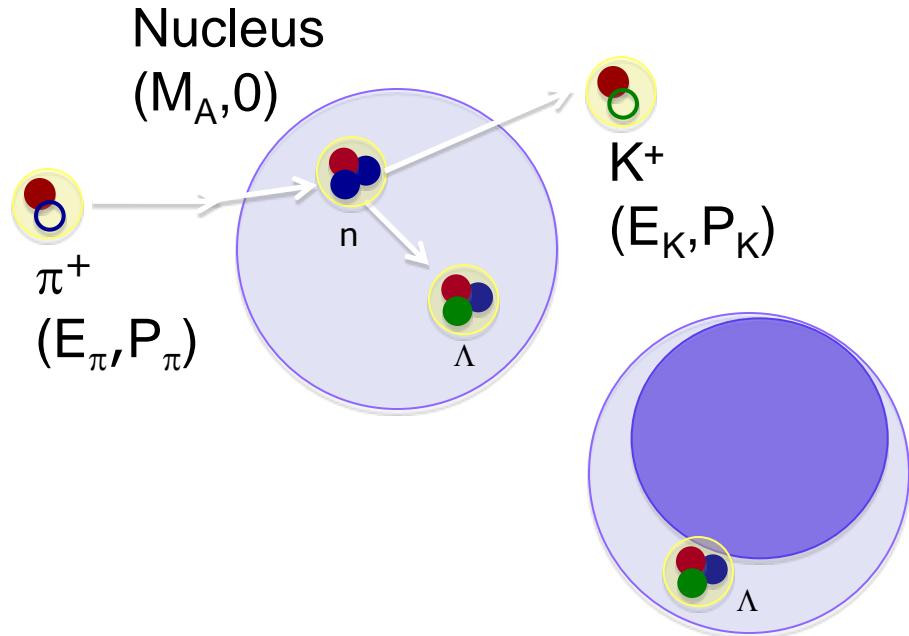
data from counter experiments in (π^+, K^+) or (K^-, π^-) reactions using thick targets
~ 1500-3000 keV mass resolution

Experimental data in MeV from [Nuclear Wallet Cards, BNL, 2011]

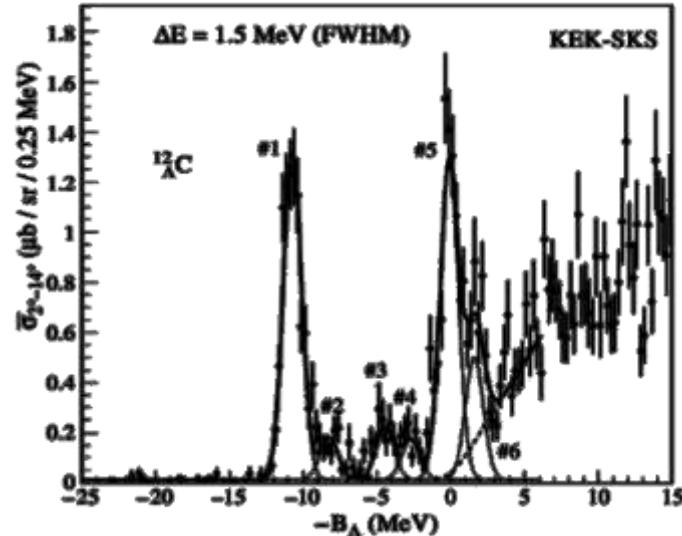
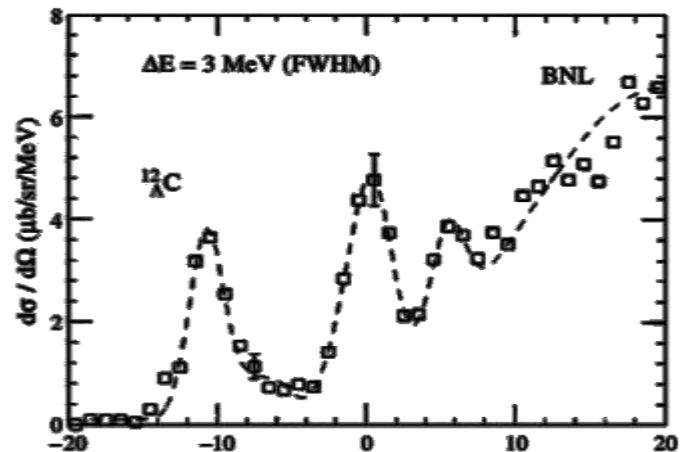
Production spectroscopy

BNL-AGS 3 MeV (FWHM)

[Pile et al., Phys. Rev. Lett. 66 (1991) 2585]



$$M_{HYP} = \sqrt{(E_\pi + M_A - E_K)^2 - (p_\pi - p_K)^2}$$



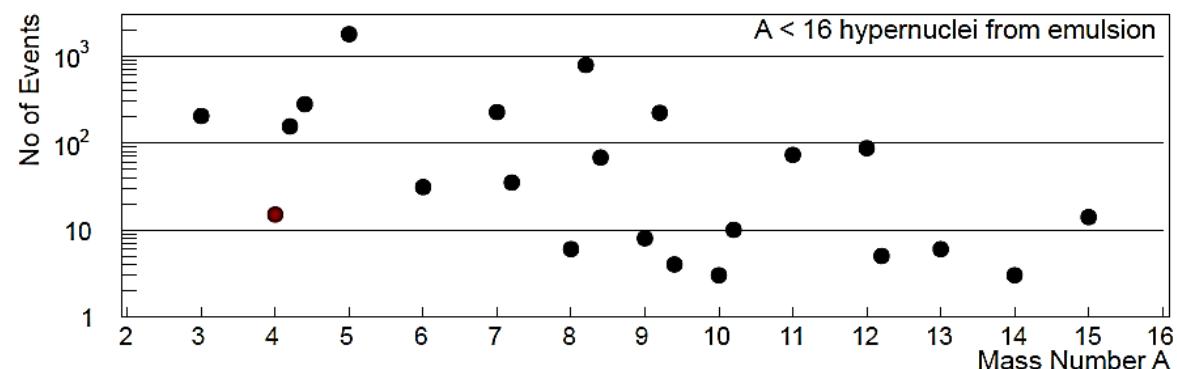
KEK-SKS: 1.5 MeV (FWHM)

[Hotchi et al., Phys. Rev. C 64(2001) 044302]

Light hypernuclear masses $A \leq 14$

E1	A	J(g.s.)	B_A (g.s.)
----	---	---------	--------------

H	3	1/2+	0.13 5
	4	0+	2.04 4
He	4	0+	2.89 3
	5	1/2+	3.12 2
	6		4.18 10
	8		7.16 70
Li	6		
	7	1/2+ ^a	5.58 3
	8	1-	6.80 3
	9		8.50 12
Be	7	1/2+	5.16 8
	8		6.84 5
	9	1/2+	6.71 4
	10		9.11 22
B	9		8.29 18
	10		8.89 12
	11		10.24 5
C	12	1-	11.37 6
	12	1-	10.80 18 ^b
	13	1/2+	11.69 12
	14		12.17 33



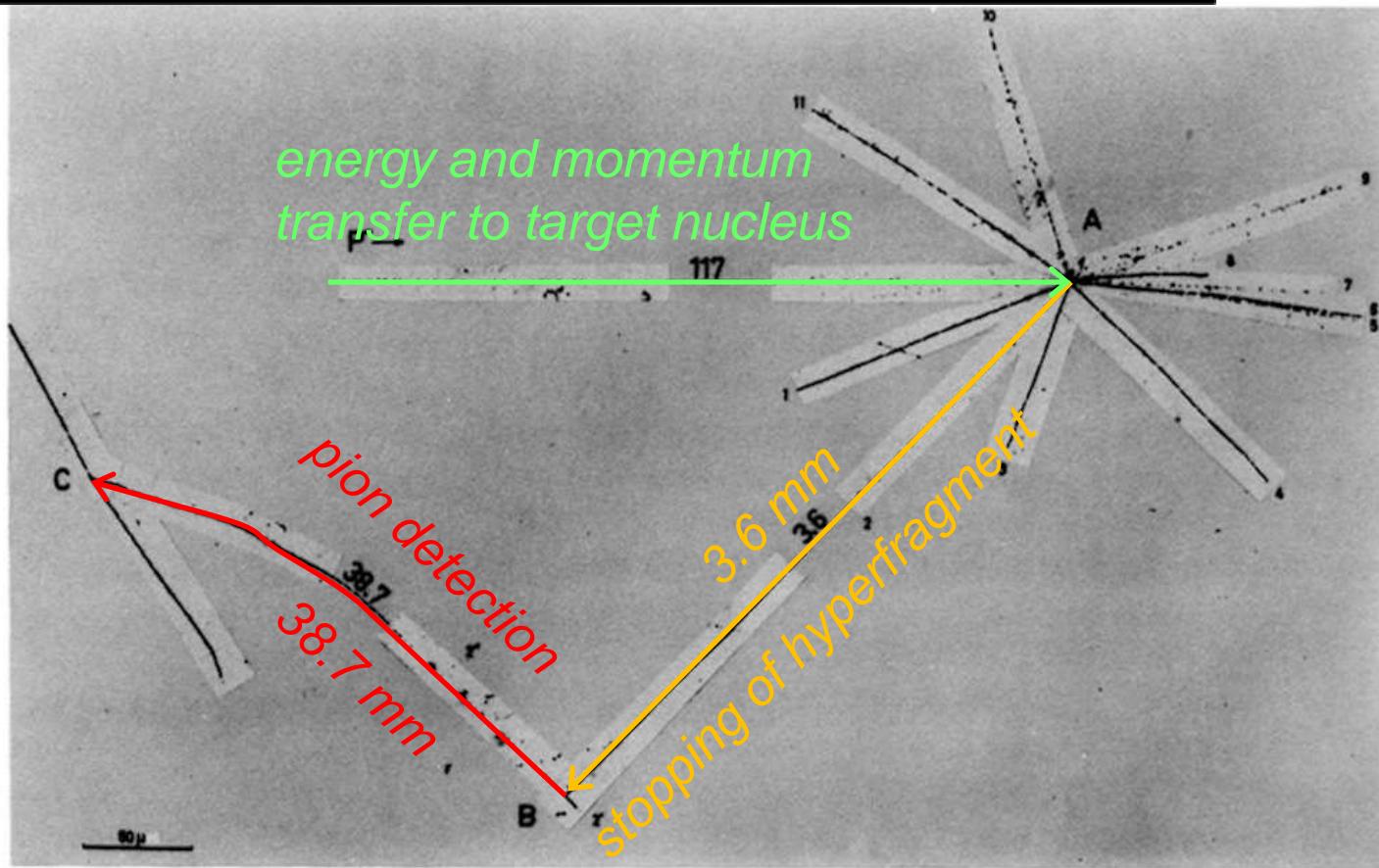
data from emulsion experiments

- often low event counts
- systematic difficulties because of varying emulsion properties
- in addition new data on ${}^7_A\text{He}$ by HKS (± 250 keV) and ${}^6_A\text{Li}$ and ${}^6_A\text{H}$ by FINUDA (± 1100 keV)

Experimental data in MeV from
[Nuclear Wallet Cards, BNL, 2011]

Hypernuclear decay-pion spectroscopy in emulsion

Example for Λ^4H



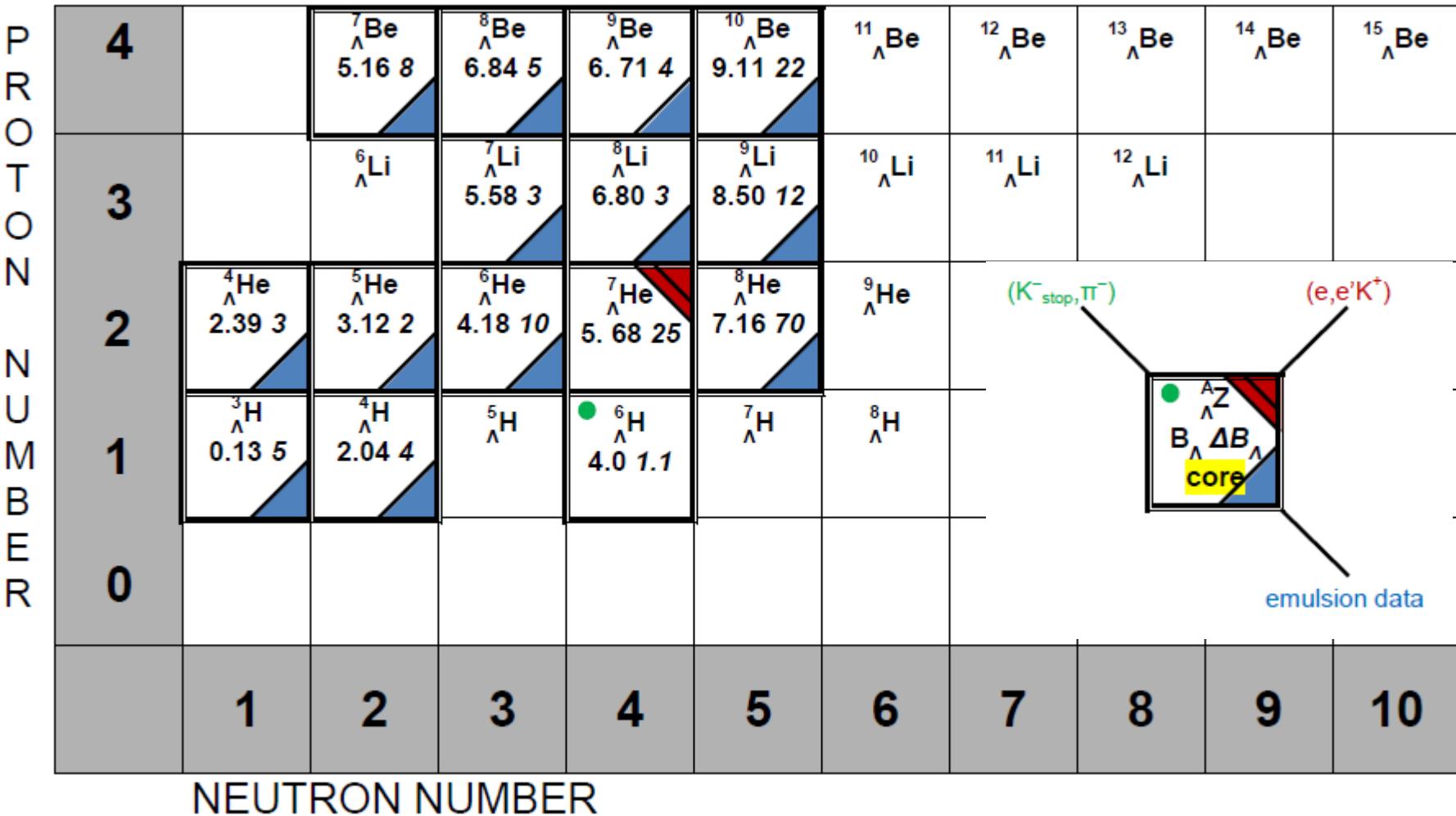
The result is that the event is consistent only with a ΛH^4 fragment undergoing mesonic two-body decay. The binding energy of the Λ in ΛH^4 is then $B_\Lambda = 2.6 \pm 1.0$ Mev, which is consistent also with other measurements of this quantity.⁹



where $Q = 54.6 \pm 1.0$ Mev.

[A.G. Ekspong et al., Phys. Rev. Lett. 3 (1959) 103]

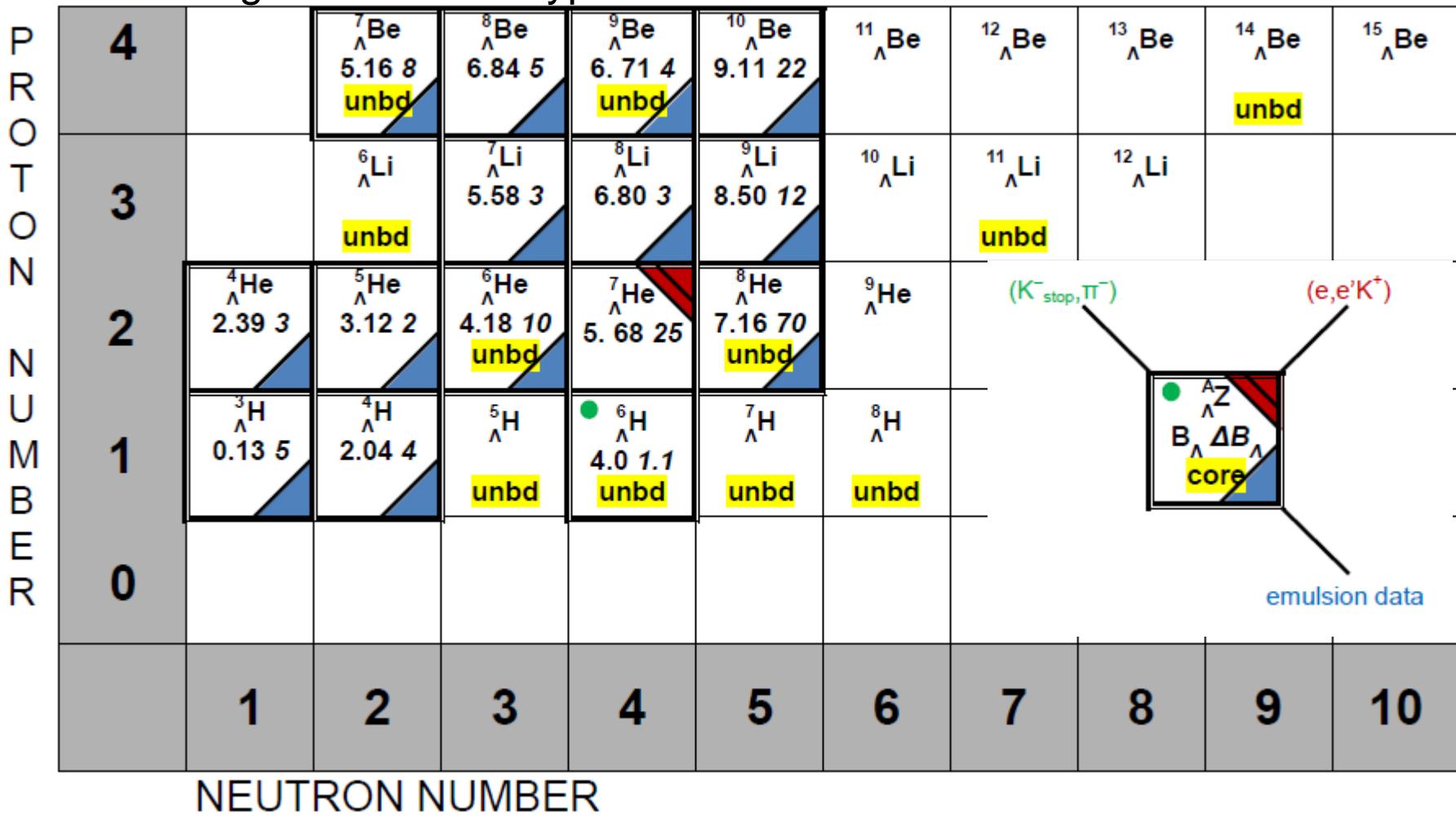
Spectroscopy of light hypernuclei



Spectroscopy of light hypernuclei

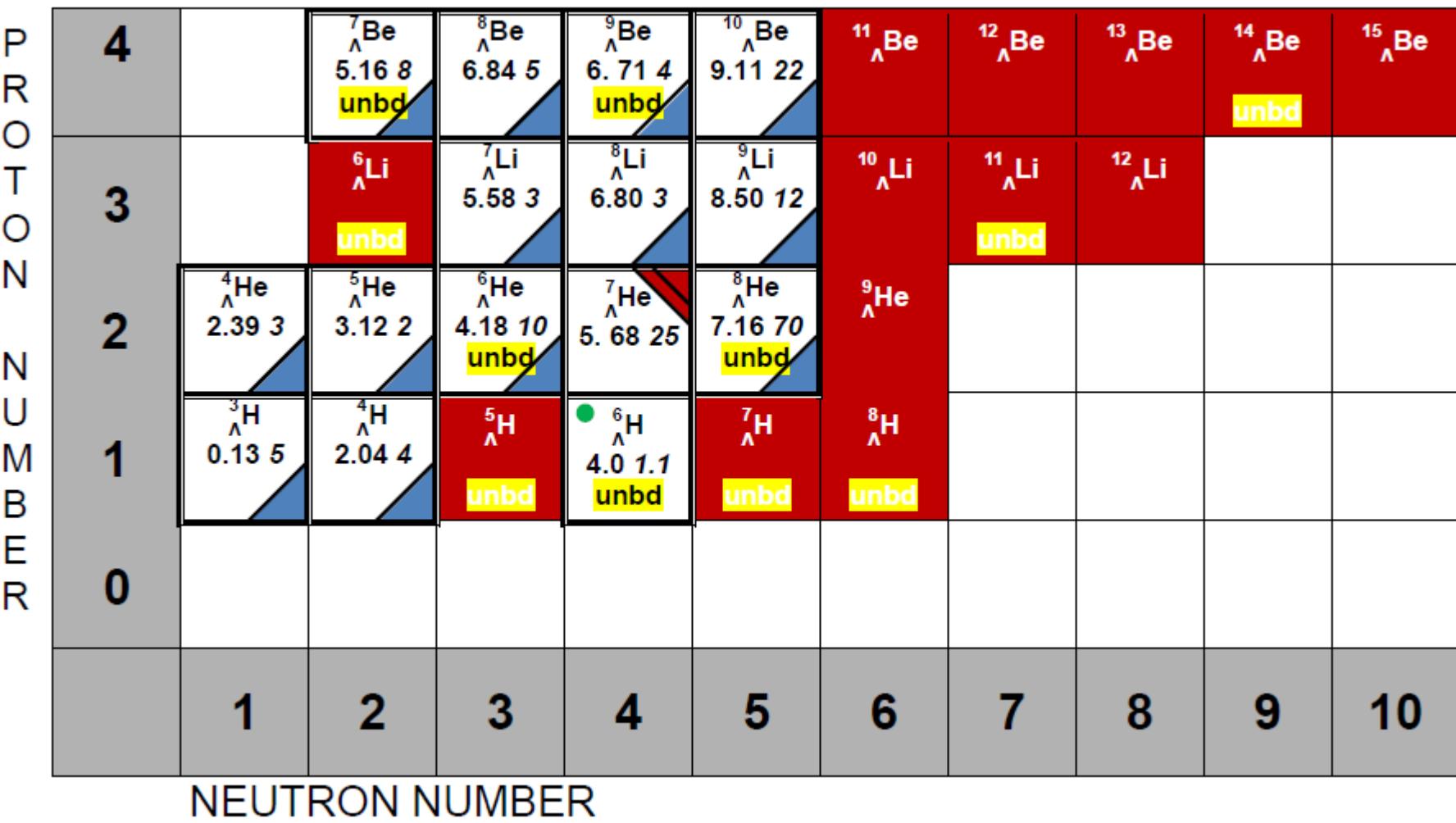
superheavy unstable-core hyperisotopes exist because of
the stabilizing role of the Λ -hyperon [Dalitz & Levi Setti, NC 30 (1963)]

unbd unbound
core nucleus



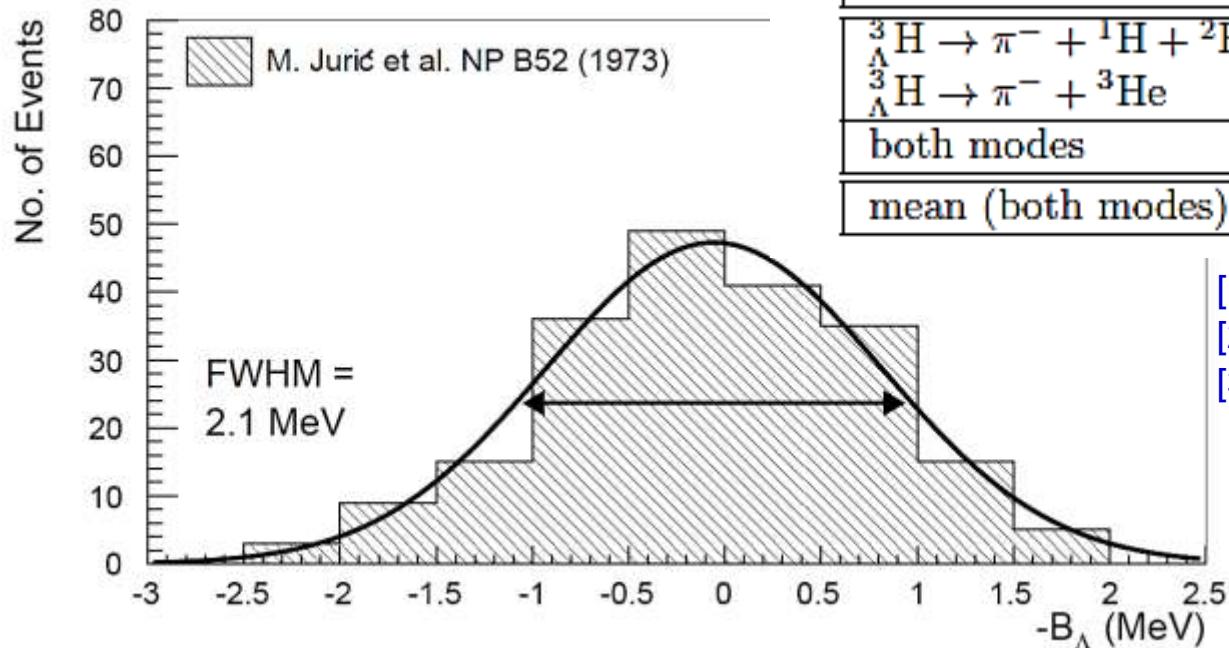
Spectroscopy of light hypernuclei

undiscovered



The mass $A = 3$ System

World data on ${}^3_{\Lambda}\text{H}$

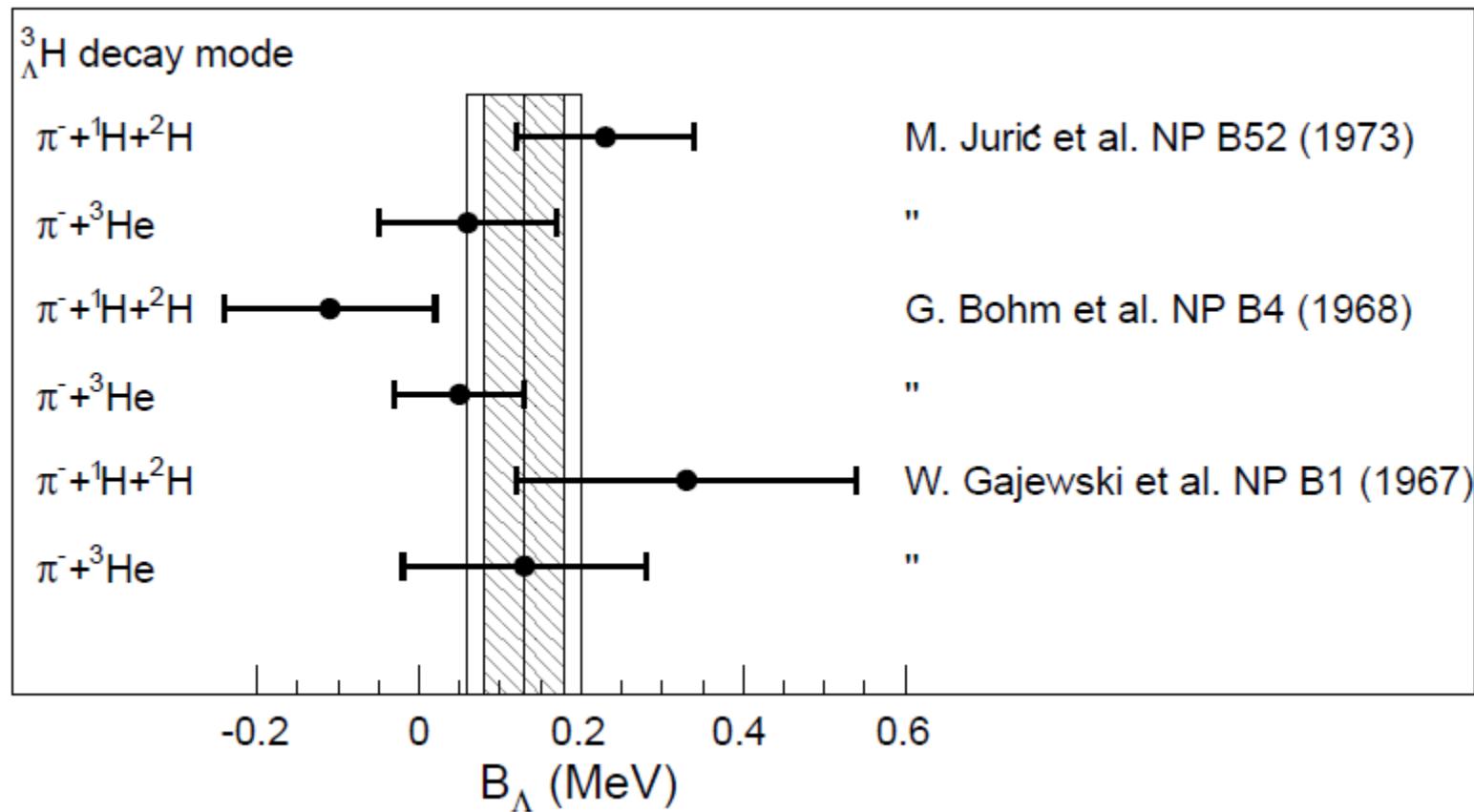


${}^3_{\Lambda}\text{H}$ decay mode	N	B_{Λ} (MeV)	Ref.
${}^3_{\Lambda}\text{H} \rightarrow \pi^- + {}^1\text{H} + {}^2\text{H}$	24	$+0.23 \pm 0.11$	[1]
${}^3_{\Lambda}\text{H} \rightarrow \pi^- + {}^3\text{He}$	58	$+0.06 \pm 0.11$	[1]
both modes	82	$+0.15 \pm 0.08$	[1]
${}^3_{\Lambda}\text{H} \rightarrow \pi^- + {}^1\text{H} + {}^2\text{H}$	16	-0.11 ± 0.13	[2]
${}^3_{\Lambda}\text{H} \rightarrow \pi^- + {}^3\text{He}$	86	$+0.05 \pm 0.08$	[2]
both modes	102	$+0.01 \pm 0.07$	[2]
${}^3_{\Lambda}\text{H} \rightarrow \pi^- + {}^1\text{H} + {}^2\text{H}$	6	$+0.33 \pm 0.21$	[3]
${}^3_{\Lambda}\text{H} \rightarrow \pi^- + {}^3\text{He}$	26	$+0.13 \pm 0.15$	[3]
both modes	32	$+0.20 \pm 0.12$	[3]
mean (both modes)	204	$+0.13 \pm 0.05$	[1]

- [1] M. Juric et al., NP B52 (1973)
- [2] G. Bohm et al. NP B4 (1968)
- [3] W. Gajewski et al. NP B1 (1967)

Hypertriton: the lightest bound hypernuclear system
about 200 analysed events from emulsion experiments

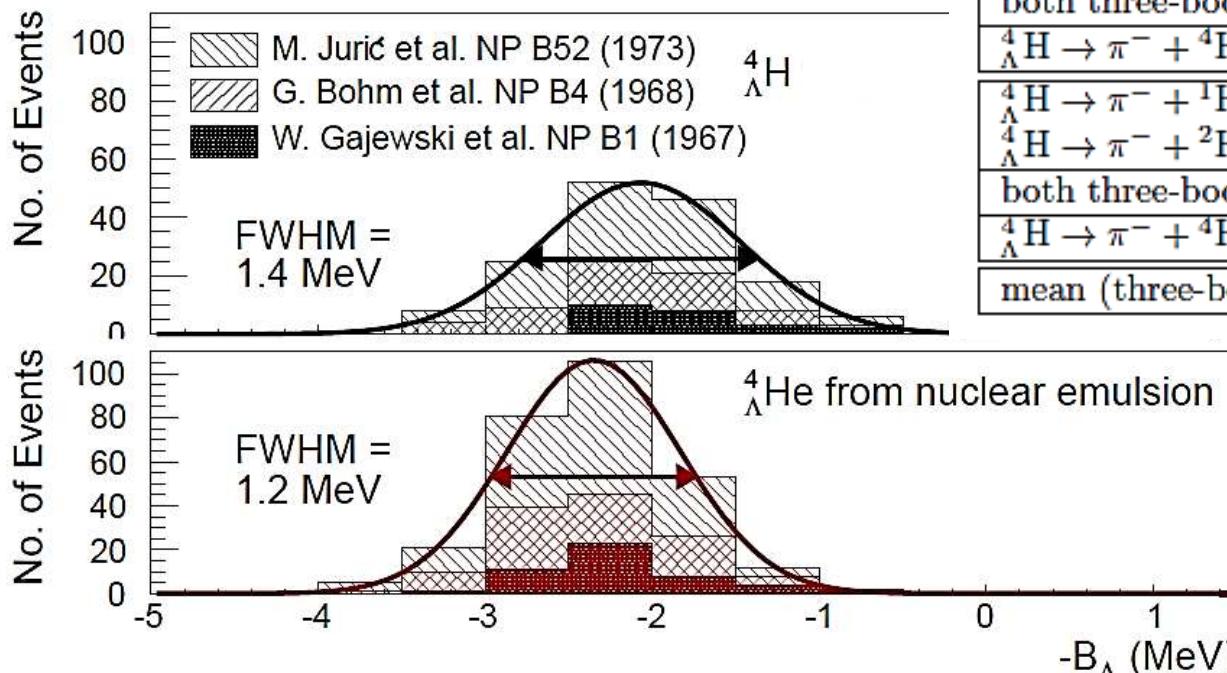
World data on ${}^3_{\Lambda}\text{H}$



Two-body and three-body decays in agreement

The mass $A = 4$ System

World data on $A = 4$ system

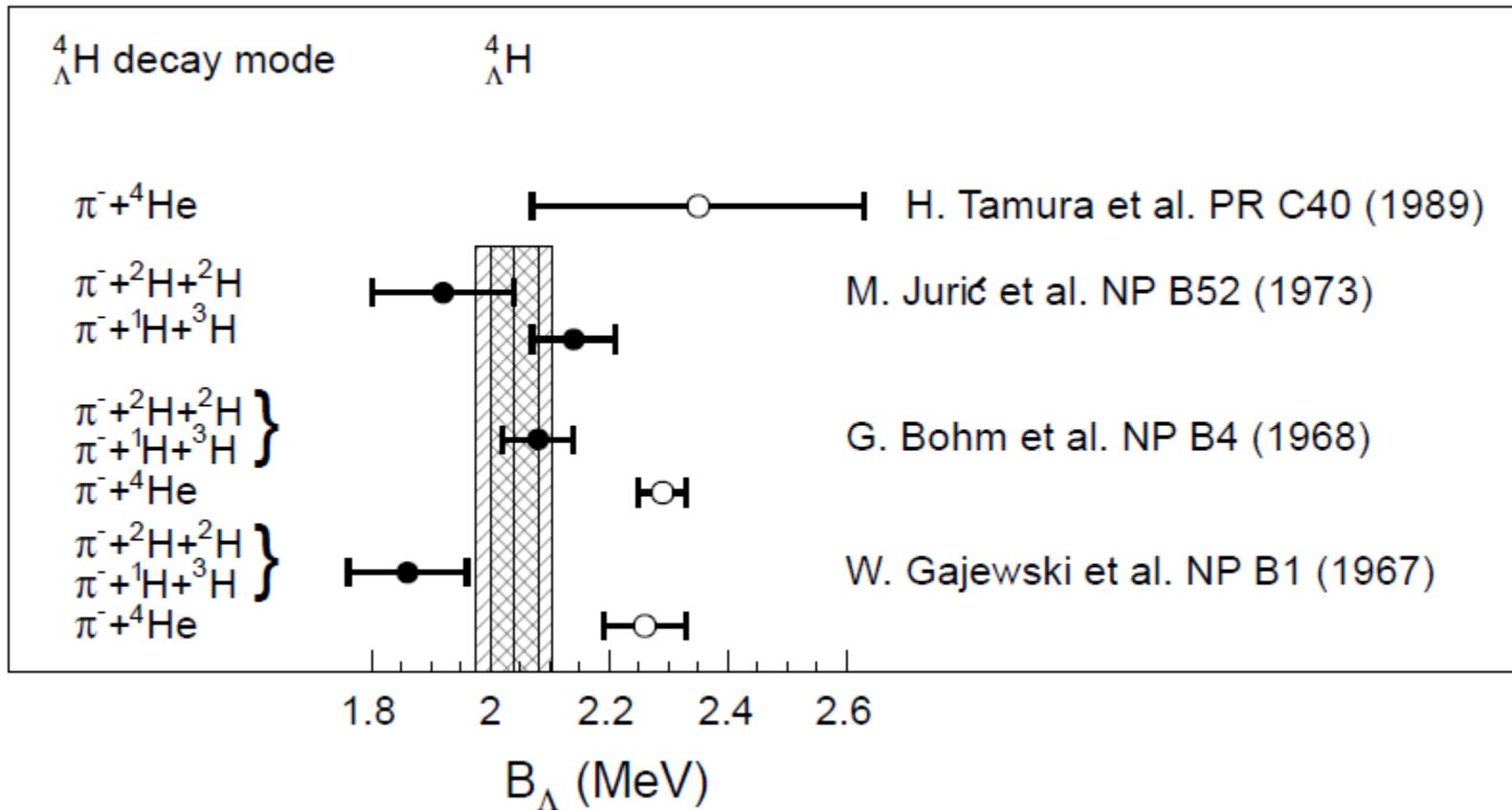


${}^4_{\Lambda}\text{H}$ decay mode	N	B_{Λ} (MeV)	Ref.
${}^4_{\Lambda}\text{H} \rightarrow \pi^- + {}^1\text{H} + {}^3\text{H}$	56	+2.14 ± 0.07	[1]
${}^4_{\Lambda}\text{H} \rightarrow \pi^- + {}^2\text{H} + {}^2\text{H}$	11	+1.92 ± 0.12	[1]
both three-body modes	67	+2.08 ± 0.06	[1]
${}^4_{\Lambda}\text{H} \rightarrow \pi^- + {}^1\text{H} + {}^3\text{H}$	63		[2]
${}^4_{\Lambda}\text{H} \rightarrow \pi^- + {}^2\text{H} + {}^2\text{H}$	7		[2]
both three-body modes	70	+2.08 ± 0.06	[2]
${}^4_{\Lambda}\text{H} \rightarrow \pi^- + {}^4\text{He}$	552	+2.29 ± 0.04	[2]
${}^4_{\Lambda}\text{H} \rightarrow \pi^- + {}^1\text{H} + {}^3\text{H}$	21		[3]
${}^4_{\Lambda}\text{H} \rightarrow \pi^- + {}^2\text{H} + {}^2\text{H}$	2		[3]
both three-body modes	23	+1.86 ± 0.10	[3]
${}^4_{\Lambda}\text{H} \rightarrow \pi^- + {}^4\text{He}$	208	+2.26 ± 0.07	[3]
mean (three-body)	155	+2.04 ± 0.04	[1]

- [1] M. Juric et al., NP B52 (1973)
- [2] G. Bohm et al. NP B4 (1968)
- [3] W. Gajewski et al. NP B1 (1967)

- Only three-body decay modes used for hyperhydrogen
- 155 events for hyperhydrogen, 279 events for hyperhelium

World data on Λ^4H

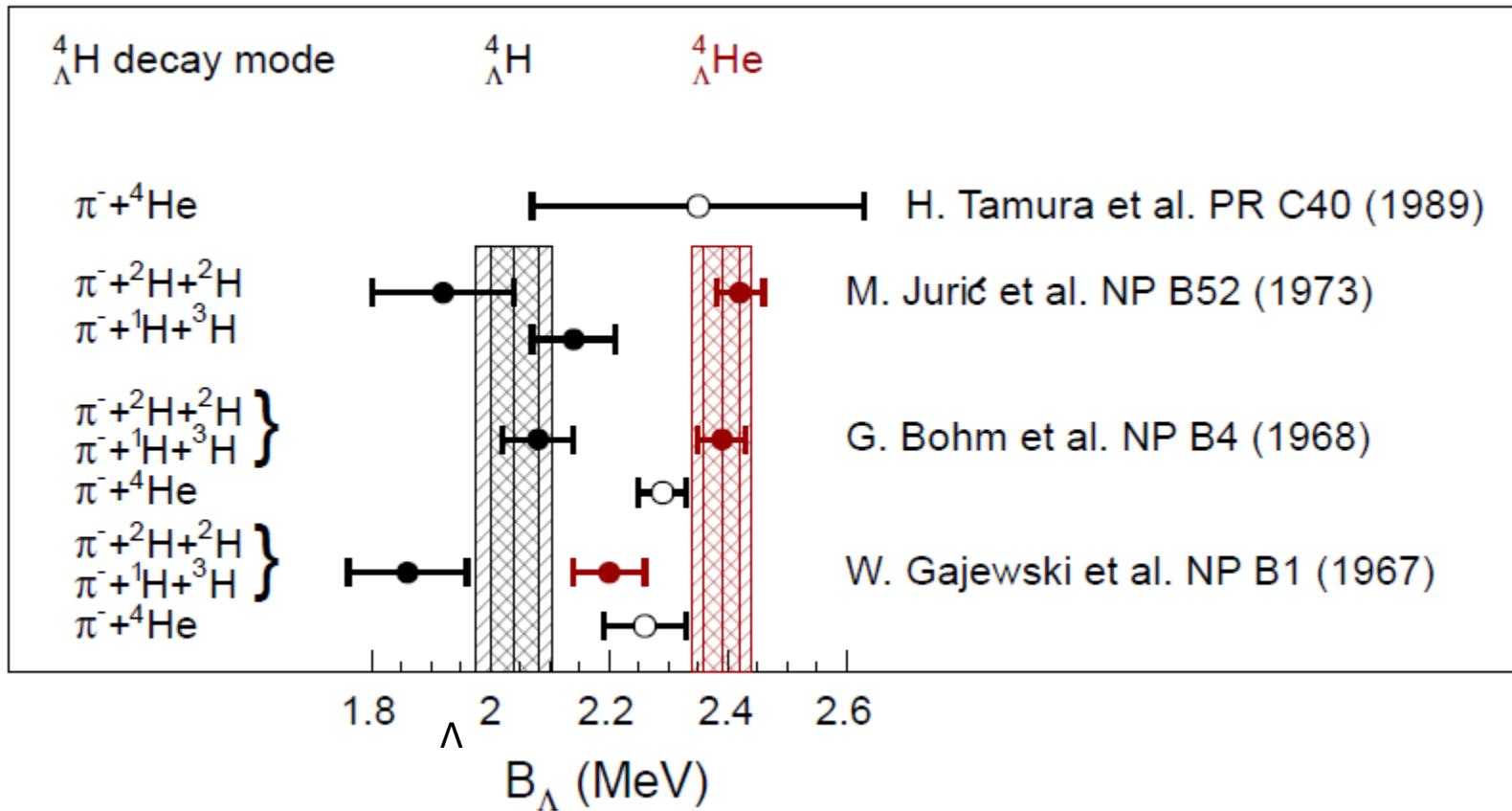


$$\left. \begin{array}{l} {} \\ {} \end{array} \right\} \begin{array}{l} \text{decay} \\ \text{decay} \end{array} \begin{array}{l} \pi^- + {}^1\text{H} + {}^3\text{H}: B = 2.14 \pm 0.07 \text{ MeV} \\ \pi^- + {}^2\text{H} + {}^2\text{H}: B = 1.92 \pm 0.12 \text{ MeV} \end{array} \right\} 0.22 \text{ MeV difference}$$

$$\text{Total: } B = 2.08 \pm 0.06 \text{ MeV}$$

[M. Juric et al. NP B52 (1973)]

World data on $A = 4$ system

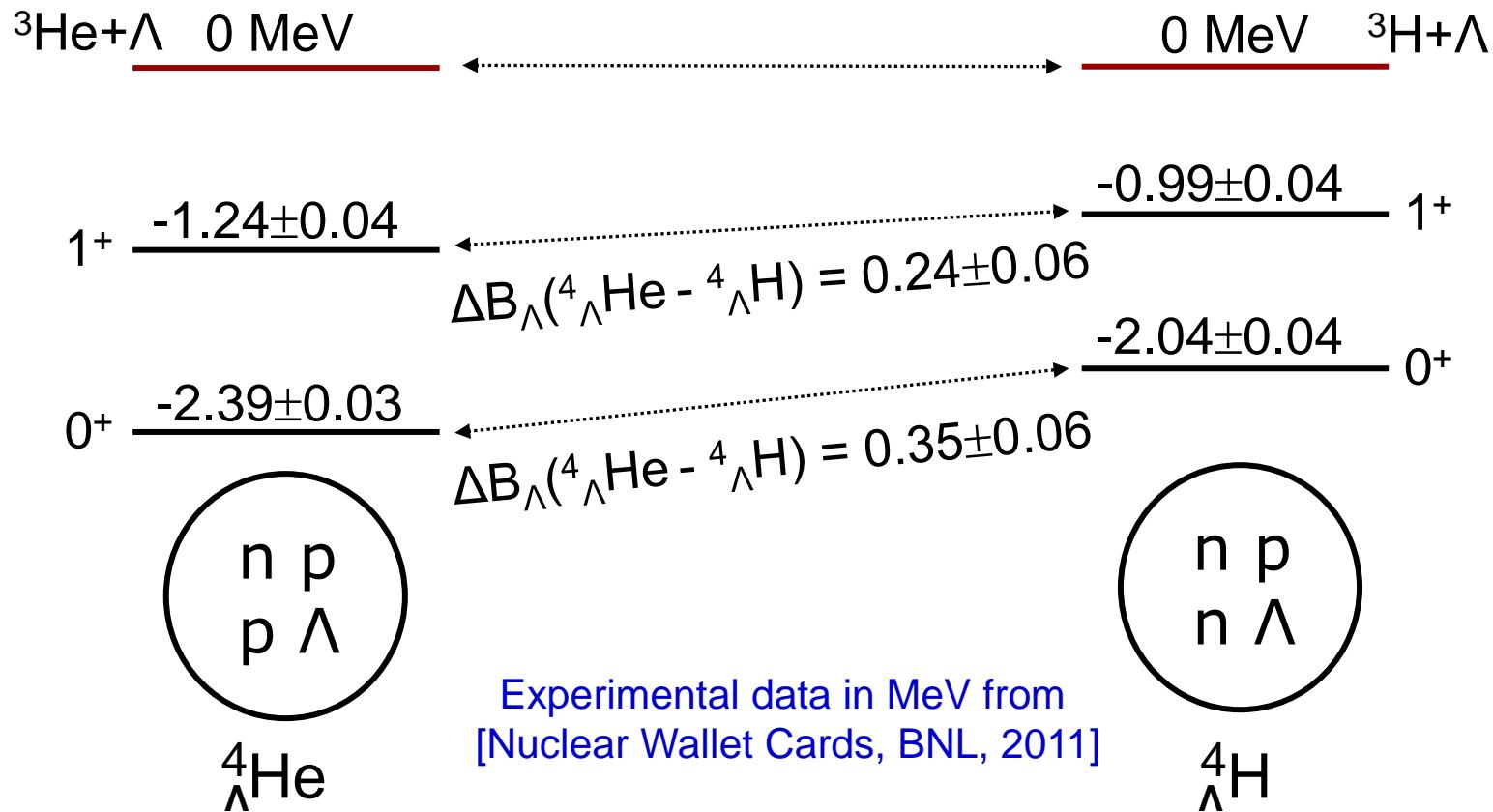


${}^4_{\Lambda}\text{He} \xrightarrow{\text{decay}} \pi^- + {}^1\text{H} + {}^3\text{He}: B = 2.42 \pm 0.05 \text{ MeV}$ }
 ${}^4_{\Lambda}\text{He} \xrightarrow{\text{decay}} \pi^- + {}^2\text{H} + {}^2\text{H}: B = 2.44 \pm 0.09 \text{ MeV}$ } 0.02 \text{ MeV difference}

Total: $B = 2.42 \pm 0.04 \text{ MeV}$

[M. Juric et al. NP B52 (1973)]

The $A = 4$ isospin doublet



- Nucleon-hyperon interaction can be studied by strange mirror pairs
- Coulomb corrections are < 50 keV for the $^4_{\Lambda}\text{H} - ^4_{\Lambda}\text{He}$ pair

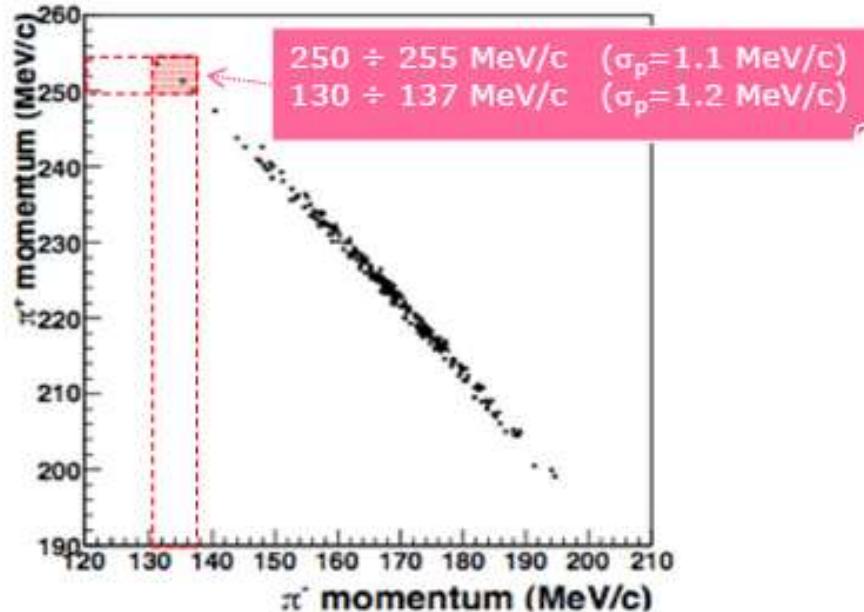
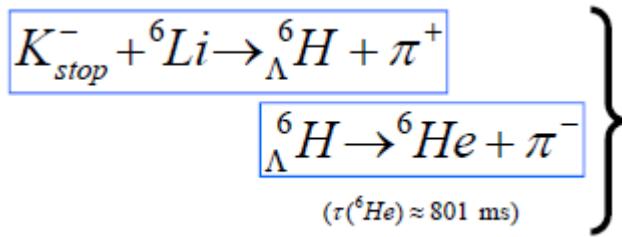
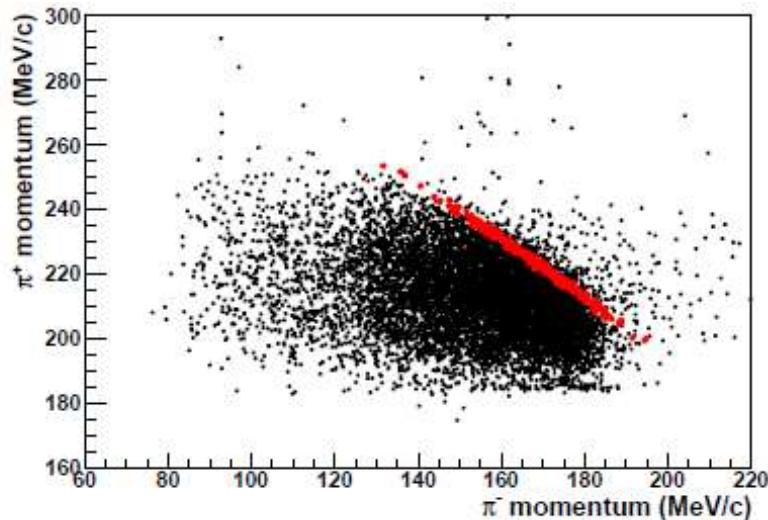
Modern calculations on $A = 4$ system

Calculation	Interaction	$B_\Lambda(^4_\Lambda H_{gs})$	$B_\Lambda(^4_\Lambda He_{gs})$	ΔB_Λ ($^4_\Lambda He - ^4_\Lambda H$)
A. Nogga, H. Kamada and W. Gloeckle, PRL 88, 172501 (2002)	SC97e	1.47	1.54	0.07
	SC89	2.14	1.80	0.34
H. Nemura, Y. Akaishi and Y. Suzuki, PRL 89, 142504 (2002)	SC97d	1.67	1.62	-0.05
	SC97e	2.06	2.02	-0.04
	SC97f	2.16	2.11	-0.05
	SC89	2.55	2.47	-0.08
E. Hiyama, M. Kamimura, T. Motoba, T. Yamada and Y. Yama PRC 65, 011301 (R) (2001)	AV8	2.33	2.28	-0.05

World data average 2.04 ± 0.04 2.39 ± 0.03 0.35 ± 0.06

With precise spectroscopy details of NY-interaction can be inferred

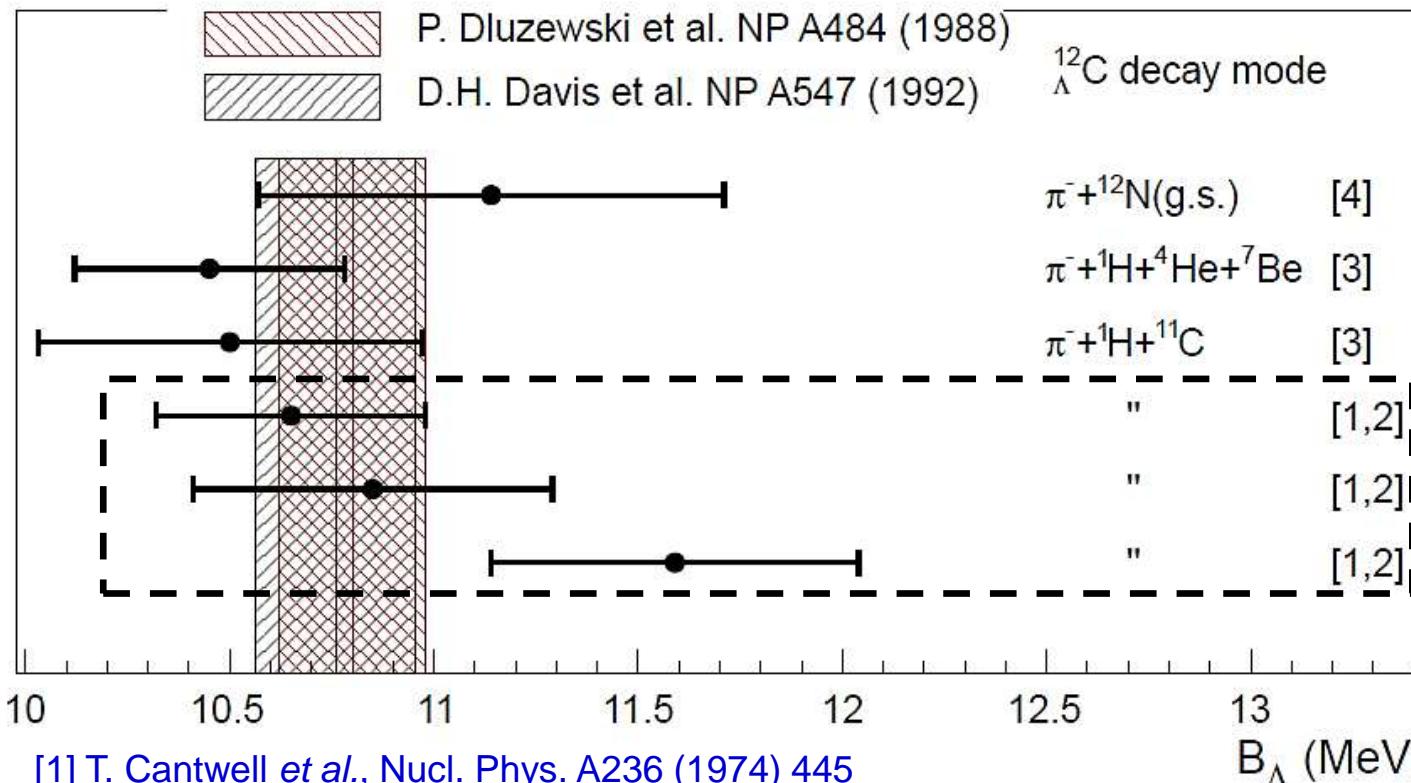
Observation of ${}^6_{\Lambda}\text{H}$ by FINUDA



T_{sum} (MeV)	p_{π^+} (MeV/c)	p_{π^-} (MeV/c)	$M({}^6_{\Lambda}\text{H})_{\text{prod}}$ (MeV)	$M({}^6_{\Lambda}\text{H})_{\text{decay}}$ (MeV)
202.6 ± 1.3	251.3 ± 1.1	135.1 ± 1.2	5802.33 ± 0.96	5801.41 ± 0.84
202.7 ± 1.3	250.1 ± 1.1	136.9 ± 1.2	5803.45 ± 0.96	5802.73 ± 0.84
202.1 ± 1.3	253.8 ± 1.1	131.2 ± 1.2	5799.97 ± 0.96	5798.66 ± 0.84

[FINUDA, PRL 108, 042501 (2012); arXiv:1203.1954v2 (2012)]

World data on ${}^{12}\Lambda$ C



[1] T. Cantwell *et al.*, Nucl. Phys. A236 (1974) 445

[2] M. Juric *et al.*, Nucl. Phys. B52 (1973) 1

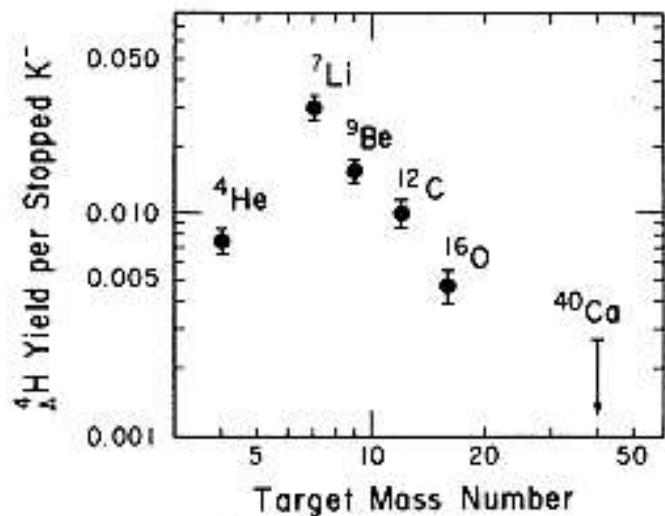
[3] J. Pniewski and D. Ziemska, Proc. of the Seminar on kaon and nucleon interaction and hypernuclei, Zvenigorod (1977) p. 33; Nukleonika 23 (1978) 797;
P. Dluzewski, M.Sc. thesis, University of Warsaw (1977)

[4] S.A. Bunyatov *et al.*, Sov. J. Nucl. Phys. 28 (1978) 222

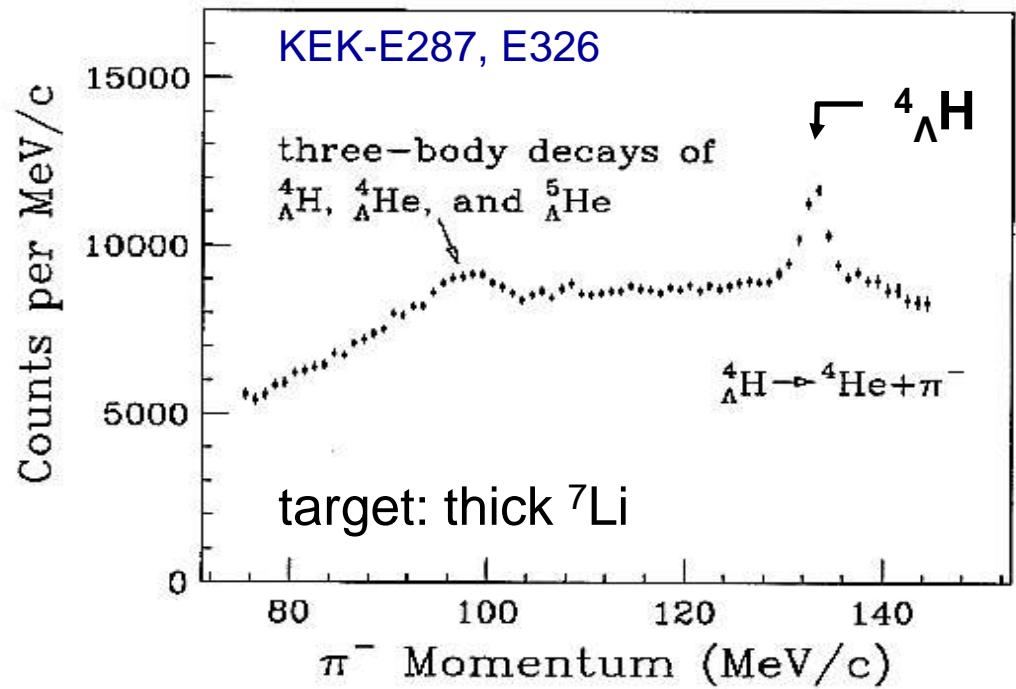
In total only 6 events from 3 different decay modes

Hyperfragment decay-pion spectroscopy

Formation of hyperhydrogen on light nuclei



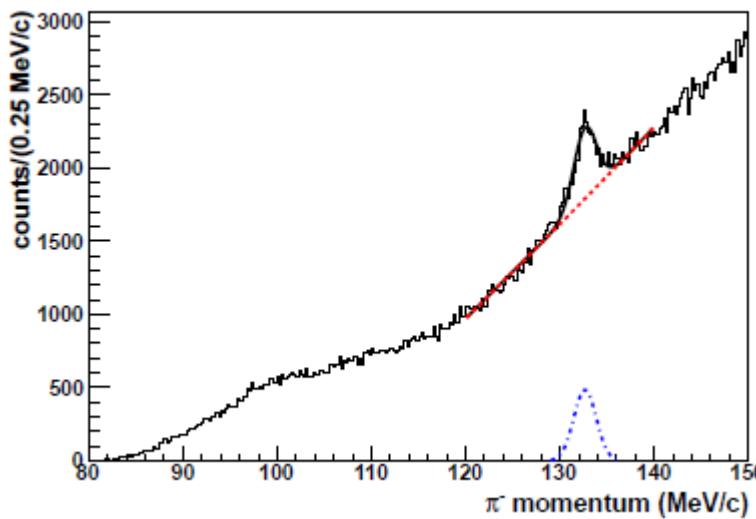
target dependence



- first detection of hyperfragments in a spectrometer
- limited momentum resolution

[H. Tamura et al. Phys. Rev. C 40 (1989)]

Observation of ${}^4_{\Lambda}\text{H}$ by FINUDA



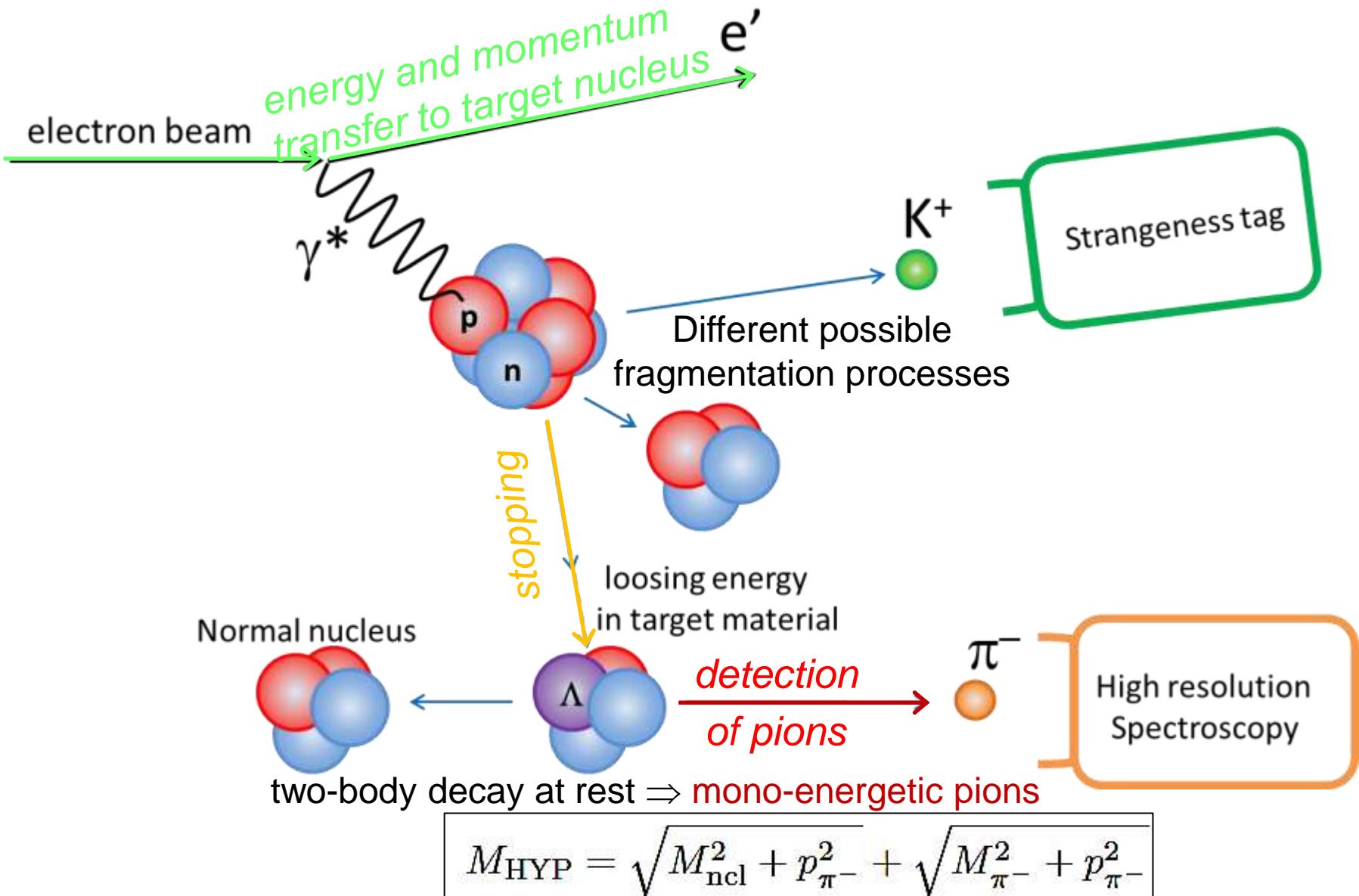
gaussian function representing the ${}^4_{\Lambda}\text{H}$ mesonic decay contribution (dot-dashed (blue in the web version) curve); the fit gives a $\chi^2/\text{ndf} = 79.1/74$, a mean $\mu_p = (132.6 \pm 0.1)$ MeV/c and a standard deviation $\sigma_p = (1.2 \pm 0.1)$ MeV/c for the gaussian function, directly measuring the experimental resolution. For comparison, $p_{\pi^-} = (132.80 \pm 0.08)$ MeV/c from $B_{\Lambda}({}^4_{\Lambda}\text{H}) = 2.04 \pm 0.04$ MeV, as determined from emulsion studies [2]; hence the absolute uncertainty is 0.2 MeV/c. and the corresponding systematic uncertainty in the kinetic energy is then $\sigma_{T_{sys}}(\pi^-) = 0.14$ MeV. [FINUDA, arXiv:1203.1954v2 (2012)]

experimental resolution 2.8 MeV/c (FWHM)

→ factor 2 worse compared to emulsion

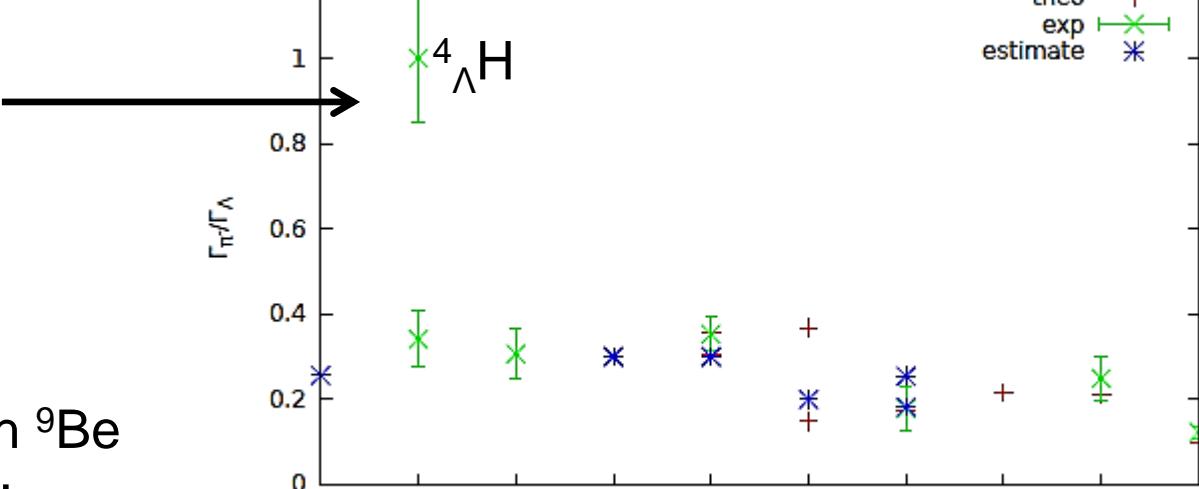
absolute calibration error $(133.03 - 132.6)$ MeV/c ~ 400 keV/c

Hyperfragment decay-pion spectroscopy with electron beams



Accessible hyperisotopes

highest pionic
decay rate

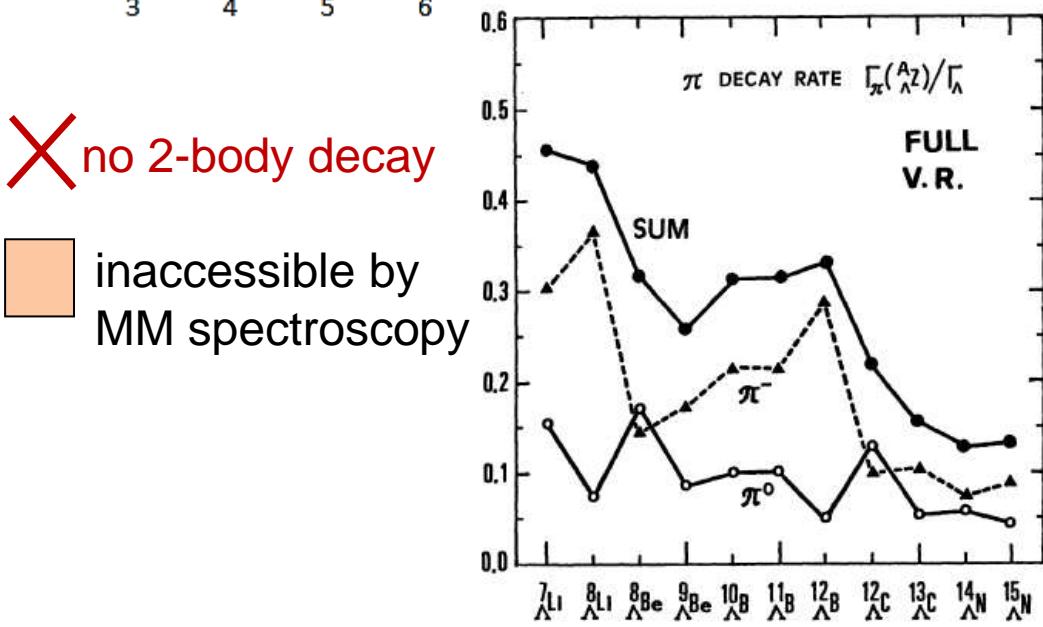


Accessible isotopes with ${}^9\Lambda\text{Be}$
from ${}^3\Lambda\text{H}$, ${}^4\Lambda\text{H}$, ... to ${}^9\Lambda\text{Li}$:

PROTON NUMBER	NEUTRON NUMBER				
	1	2	3	4	5
3		${}^6\Lambda\text{Li}$ 5.58 3	${}^7\Lambda\text{Li}$ 6.80 3	${}^8\Lambda\text{Li}$ 8.50 12	
2	${}^4\Lambda\text{He}$ 2.36 3	${}^5\Lambda\text{He}$ 3.12 2	${}^6\Lambda\text{He}$ 4.18 10	${}^7\Lambda\text{He}$ 5.68 25	${}^8\Lambda\text{He}$ 7.16 70
1	${}^3\Lambda\text{H}$ 0.13 5	${}^4\Lambda\text{H}$ 2.04 4	${}^5\Lambda\text{H}$ 4.0 1.1		

no 2-body decay

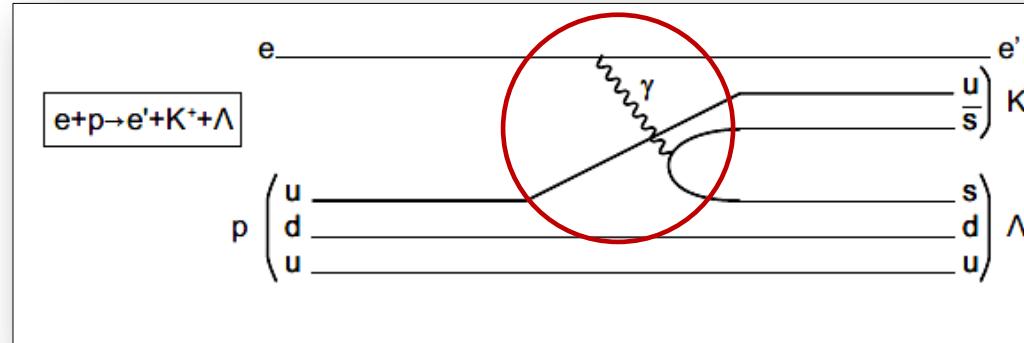
inaccessible by
MM spectroscopy



[T. Motoba & K. Itonaga, PTPS 117 (1994)]

Electroproduction

hadronic system responds to electromagnetic field produced by scattered electron



$$E_{CM} = \sqrt{2E_\gamma M_p + M_p^2} = M_\Lambda + M_{K^+} = 1,6\text{GeV}$$
$$\Rightarrow E_\gamma = 0,9\text{GeV}$$



1. CEBAF accelerator at Jefferson Lab (US)
2. MAMI-C accelerator at Mainz University (Germany)

Experimental challenges

- cross-section for hypernuclei formation
 - very small (~ 100 nb/sr)
 - strongly peaked at **zero degree electron scattering angle**
 - falling with increasing kaon angle**
- magnetic spectrometers with high resolving powers » 1 m:
 - challenge for **short-lived particles** (kaon lifetime 12,5 ns!)
- **forward-scattering region** ($< 10^\circ$) blocked by the exit beam-line
- **kaon count rate small** compared to background rates
- large rates of Bremsstrahlung and Møller scattering

Magnetic spectrometer facility at MAMI

Momentum resolution:

$$\delta p/p < 10^{-4}$$

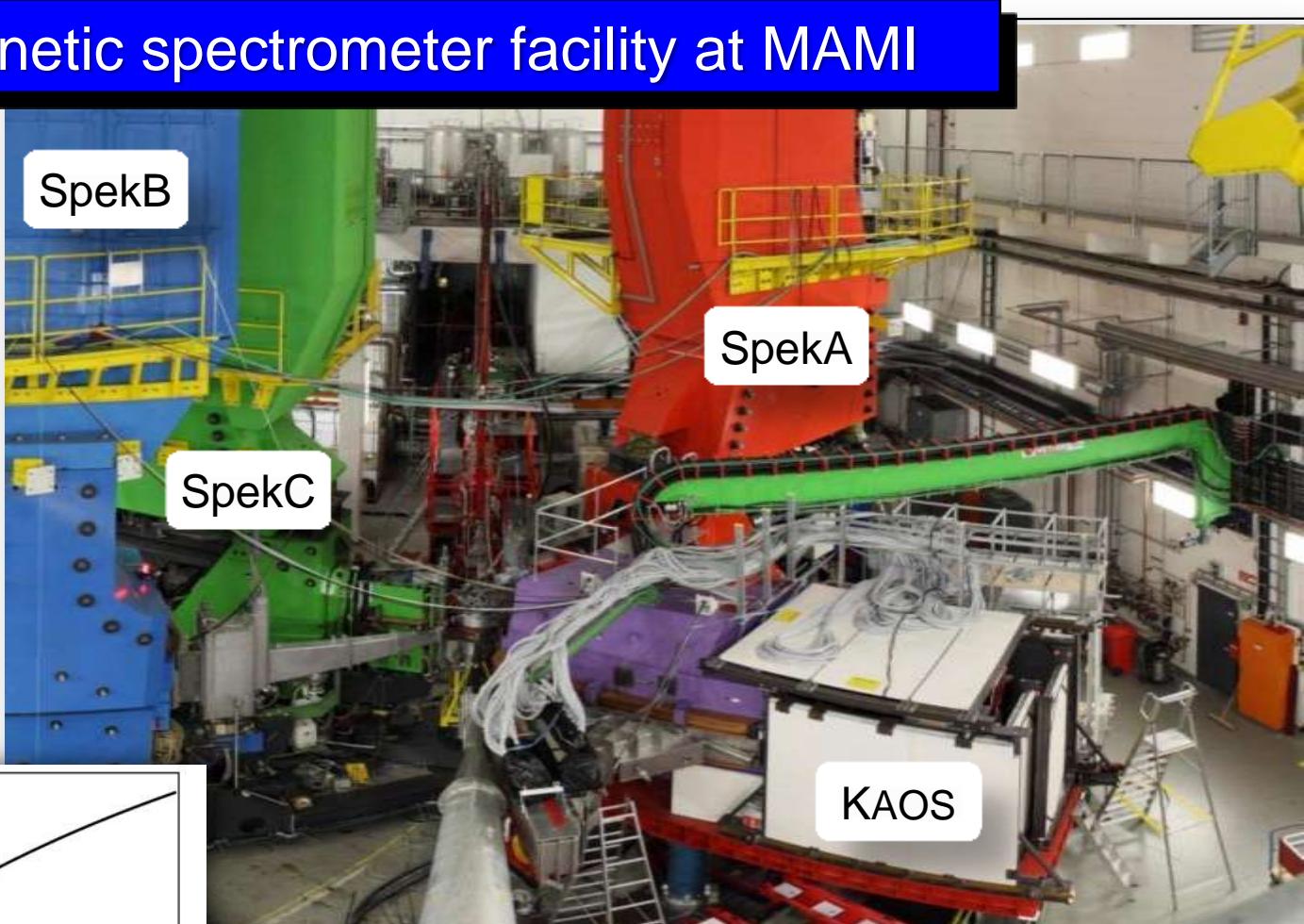
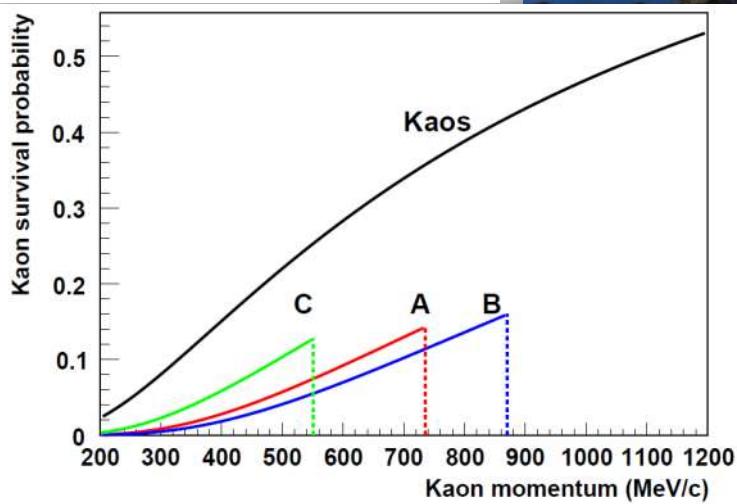
Momentum acceptance:

$$\Delta p/p = 20\%$$

Accepted solid angle:

$$\begin{aligned}\Delta\Omega &= 11.5^\circ \times 8.0^\circ \\ &= 28 \text{ msr}\end{aligned}$$

Kaon survival probability:

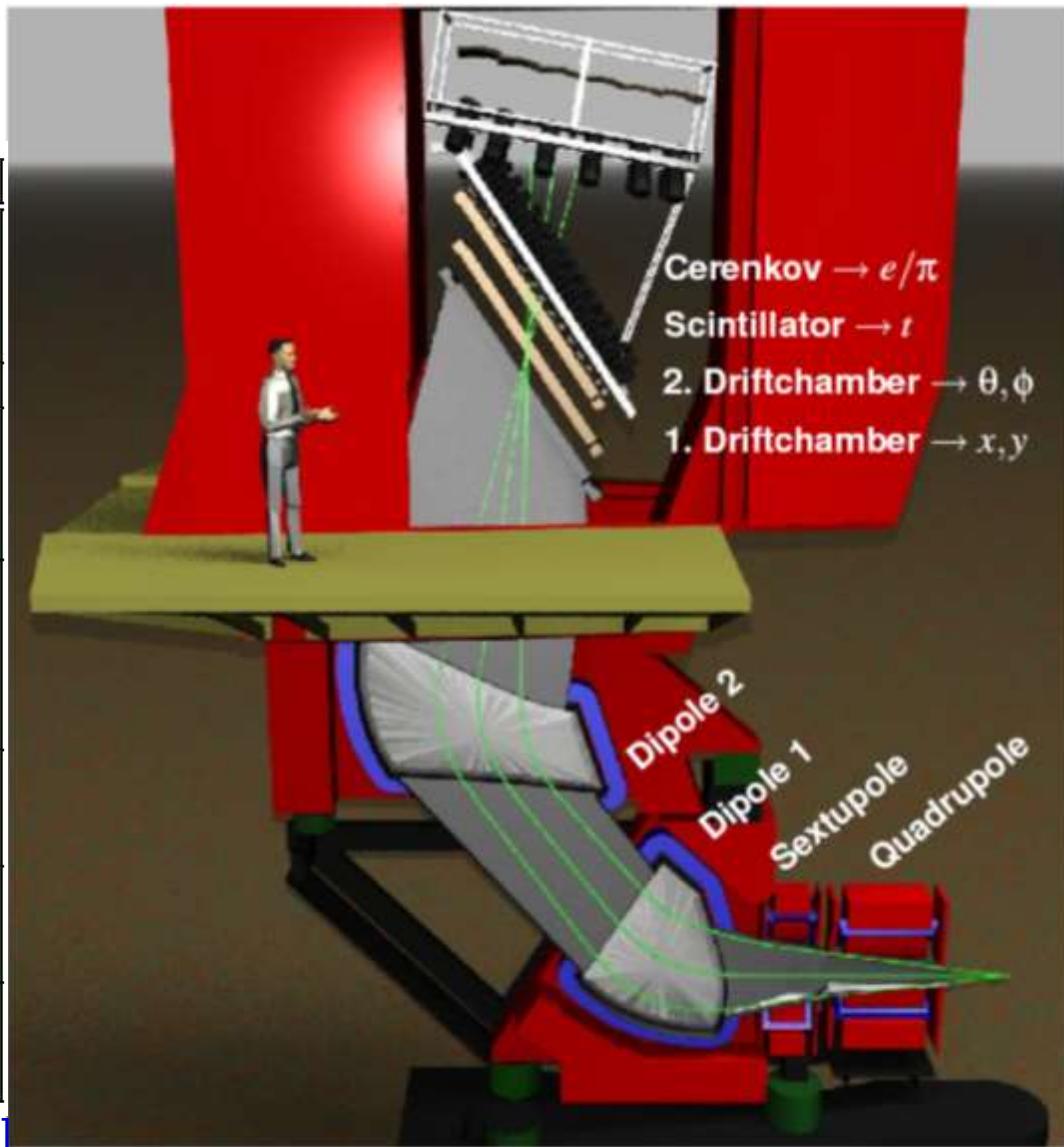


Magnetic focusing spectrometers at MAMI:

- 3 high-resolution $\Delta p/p \sim 10^{-4}$ spectrometers (SpekA,B,C)
- 1 short-orbit spectrometer (KAOS, since 2008)

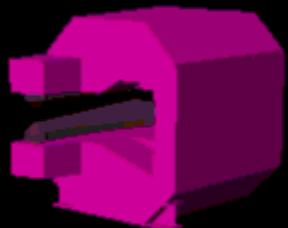
Magnet Optics for the QSDD Design

Spectrometer		A	B	C
Configuration	QSDD	D	QSDD	
Focussing properties				
dispersive plane	$pt \rightarrow pt$	$pt \rightarrow pt$	$pt \rightarrow pt$	
nondispersivel plane	$\parallel \rightarrow pt$	$pt \rightarrow pt$	$\parallel \rightarrow pt$	
Maximum momentum	[MeV/c]	735	870	551
Solid angle	[msr]	28	5.6	28
Angular range				
minimum angle	18°	7°	18°	
maximum angle	160°	62°	160°	
Momentum acceptance	[%]	20	15	25
Angular acceptance				
dispersive plane	[mrad]	± 70	± 70	± 70
nondispersivel plane	[mrad]	± 100	± 20	± 100
long-target acceptance	[mm]	50	50	50
Angle of focal plane		45°	47°	45°
Length of focal plane	[m]	1.80	1.80	1.60
Length of trajectory	[m]	10.75	12.03	8.53
Dispersion (central)	[cm/%]	5.77	8.22	4.52
Magnification (central)		0.53	0.85	0.51
Dispersion / Magnification	[cm/%]	10.83	9.64	8.81
Momentum resolution		10^{-4}	10^{-4}	10^{-4}
angular resolution at target	[mrad]	≤ 3	≤ 3	≤ 3
position resolution at target	[mm]	3 – 5	1	3 – 5



[K.I. Blomqvist et al., Nucl. Inst. Meth. A 403 (1998)]

Setup of Kaos

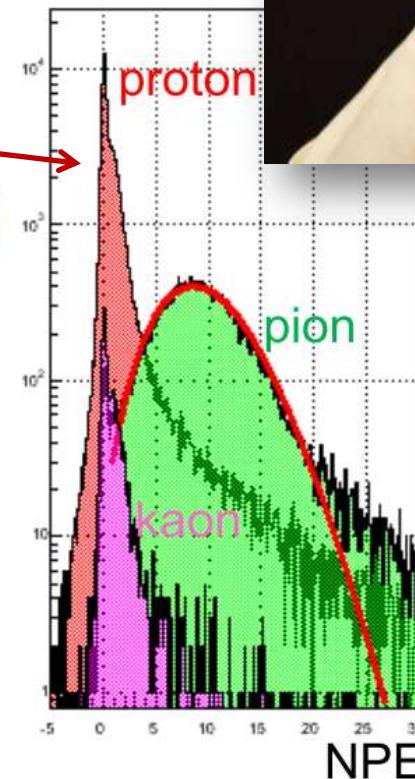
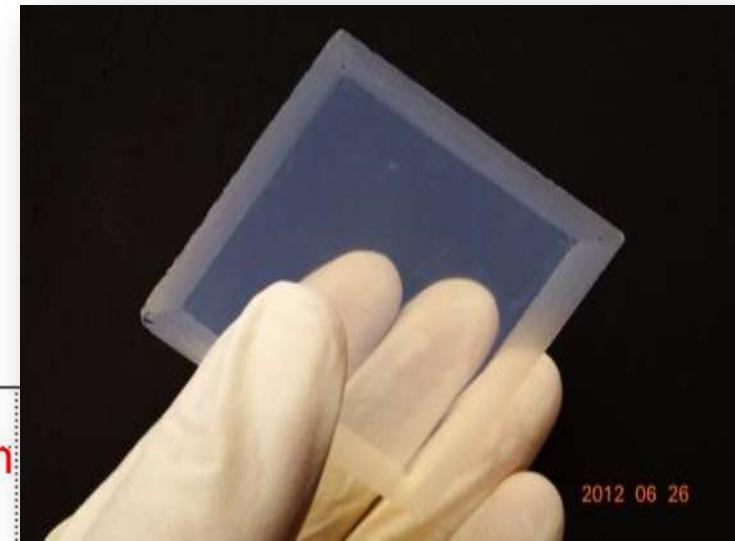
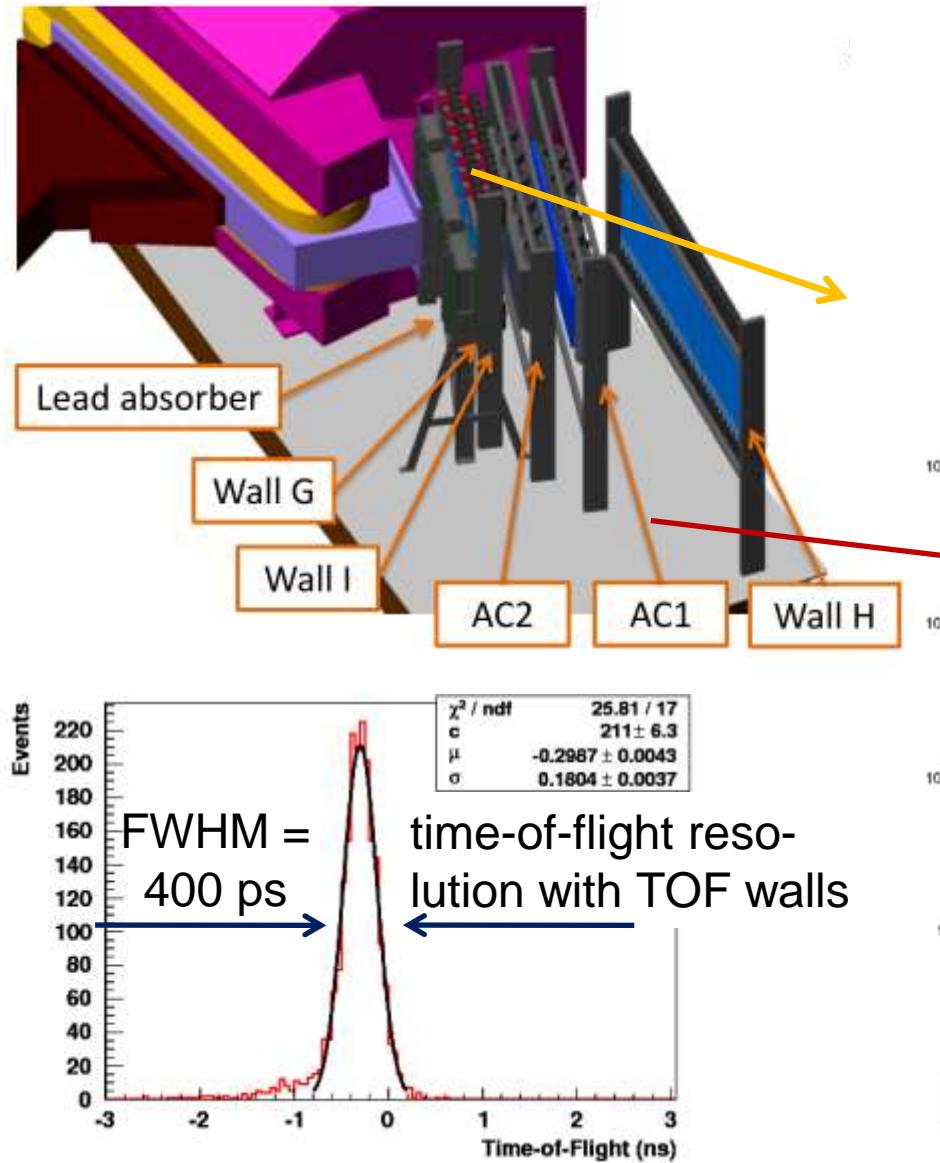


Precision spectroscopy of light hypernuclear masses

Jan. 2015

P Achenbach, U Mainz

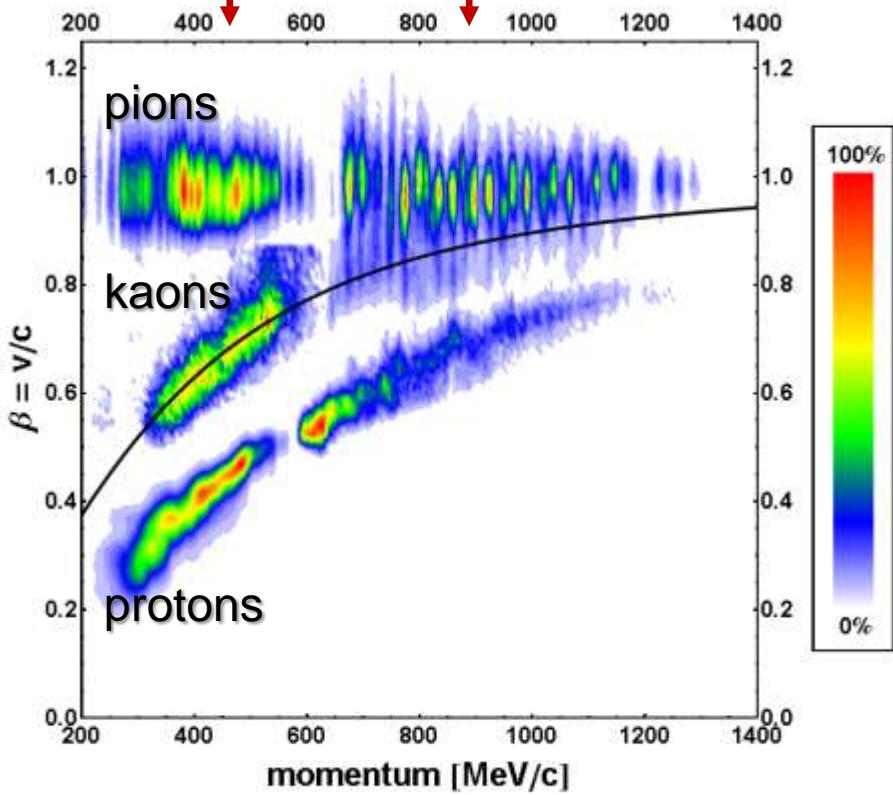
Particle detection system in KAOS



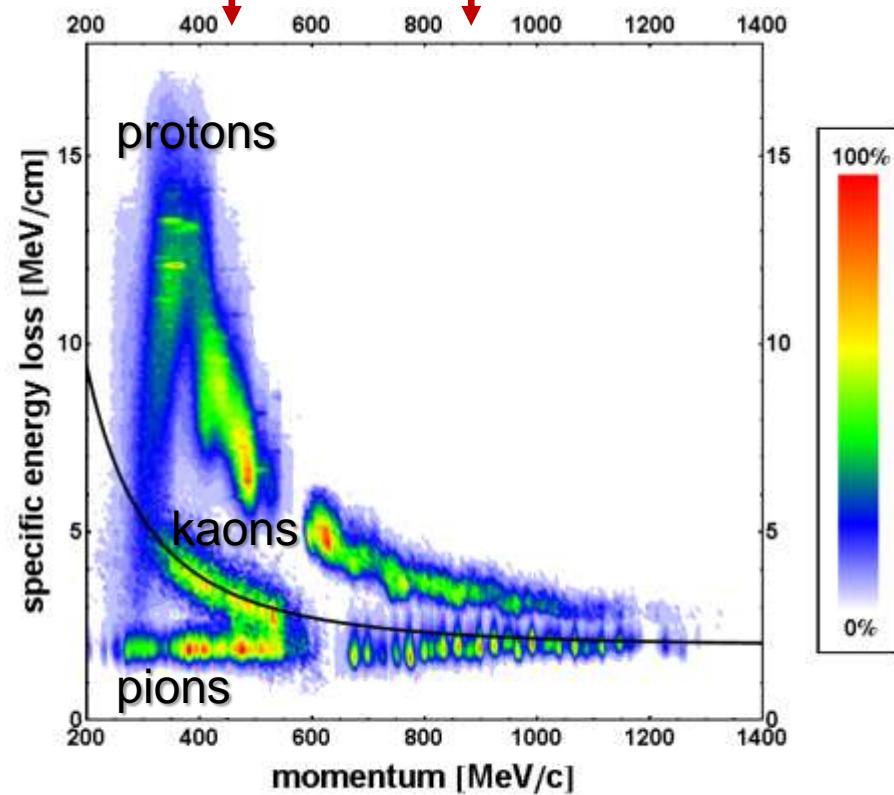
pion detection $\epsilon > 95\%$
by aerogel Cherenkov

Kaon identification using TOF system

low / high momentum setting



low / high momentum setting

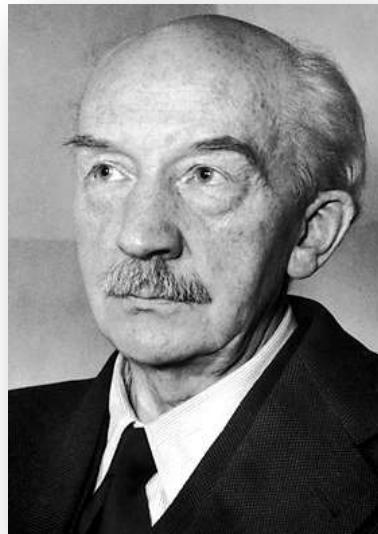


- K_{AOS} can cover 200–1300 MeV/c in only 2 settings
- clean kaon identification at low momenta
- Cherenkov information needed at high momenta

Reminder: Coincidence Method

Walther Bothe:
The Nobel Prize
in Physics 1954:

"for the coincidence
method and his
discoveries made
therewith"



[W. Bothe & H. Geiger: Zeitschr. f. Phys. 32 (1925) 639]

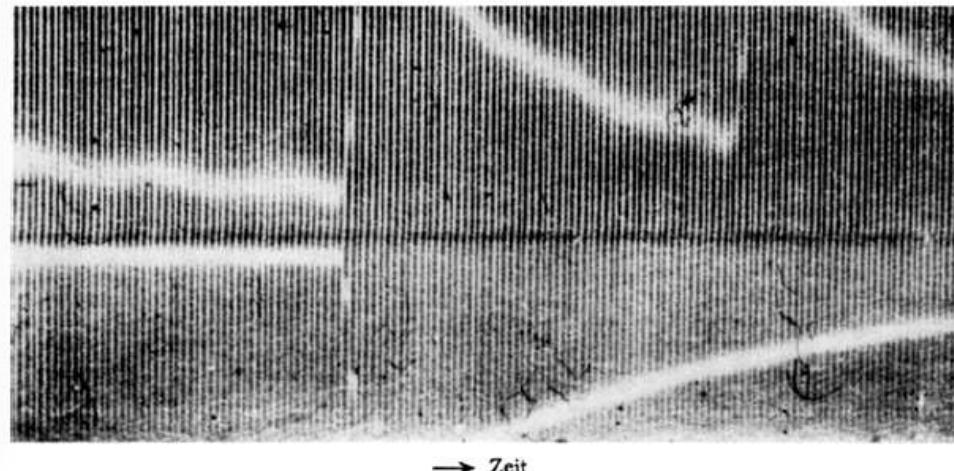


Fig. 7. Beispiel einer Koinzidenz. Streifenabstand $1/1000$ Sekunde.
Oben e^- -Ausschläge, unten $h\nu$ -Ausschlag.

"... we succeeded after a few failures to establish the accuracy of any temporal "coincidence" between the two pointer readings as being 10^{-4} sec."

Bothe's system: resolving time $\delta t = 10^{-4}$ sec = 100 000 ns

DAQ rate $R = 300\text{-}500/\text{min} \sim 8 \text{ Hz}$

modern system: $\delta t \sim 100 \text{ ps}$

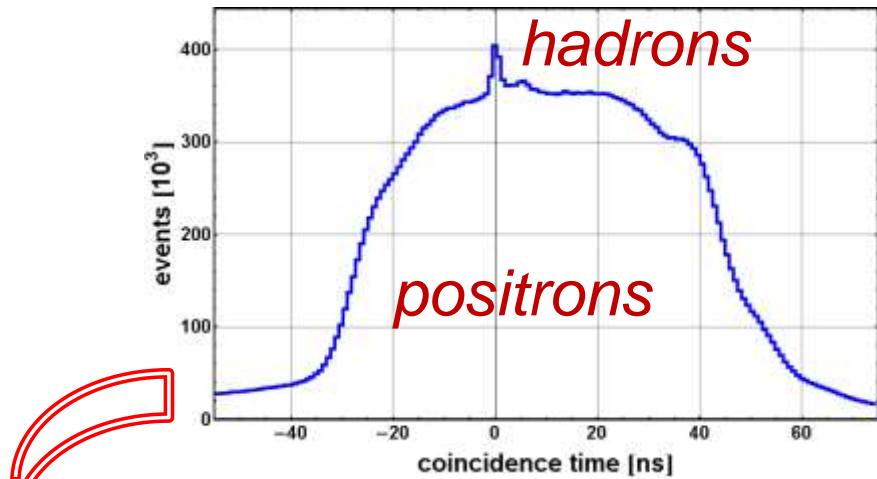
$R \sim \text{kHz-MHz}$

→ 5-6 orders of magnitude improvement

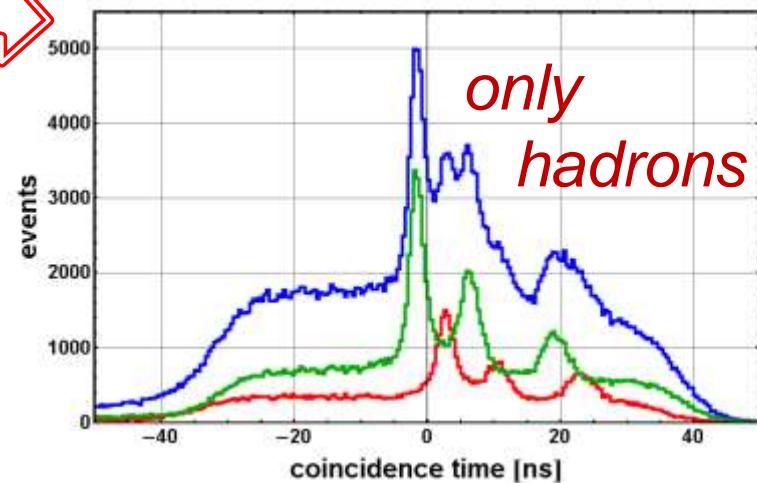
Kaos spectrometer changed into zero-degree tagger



without absorber



with absorber

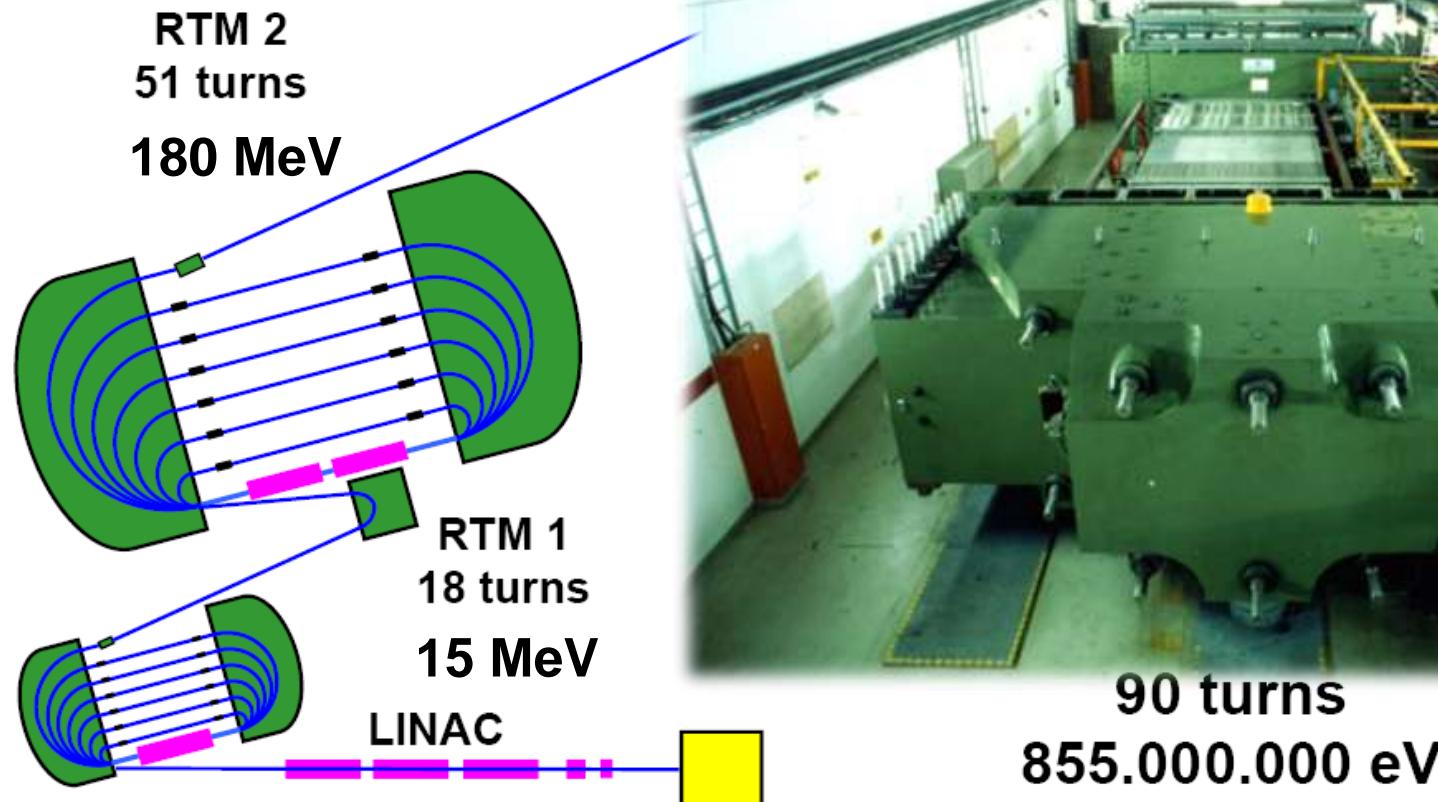


- Suppression of large positron flux with 25 X_0 lead absorber wall
- Much cleaner spectra for all hadrons

Decay-pion spectroscopy results from MAMI

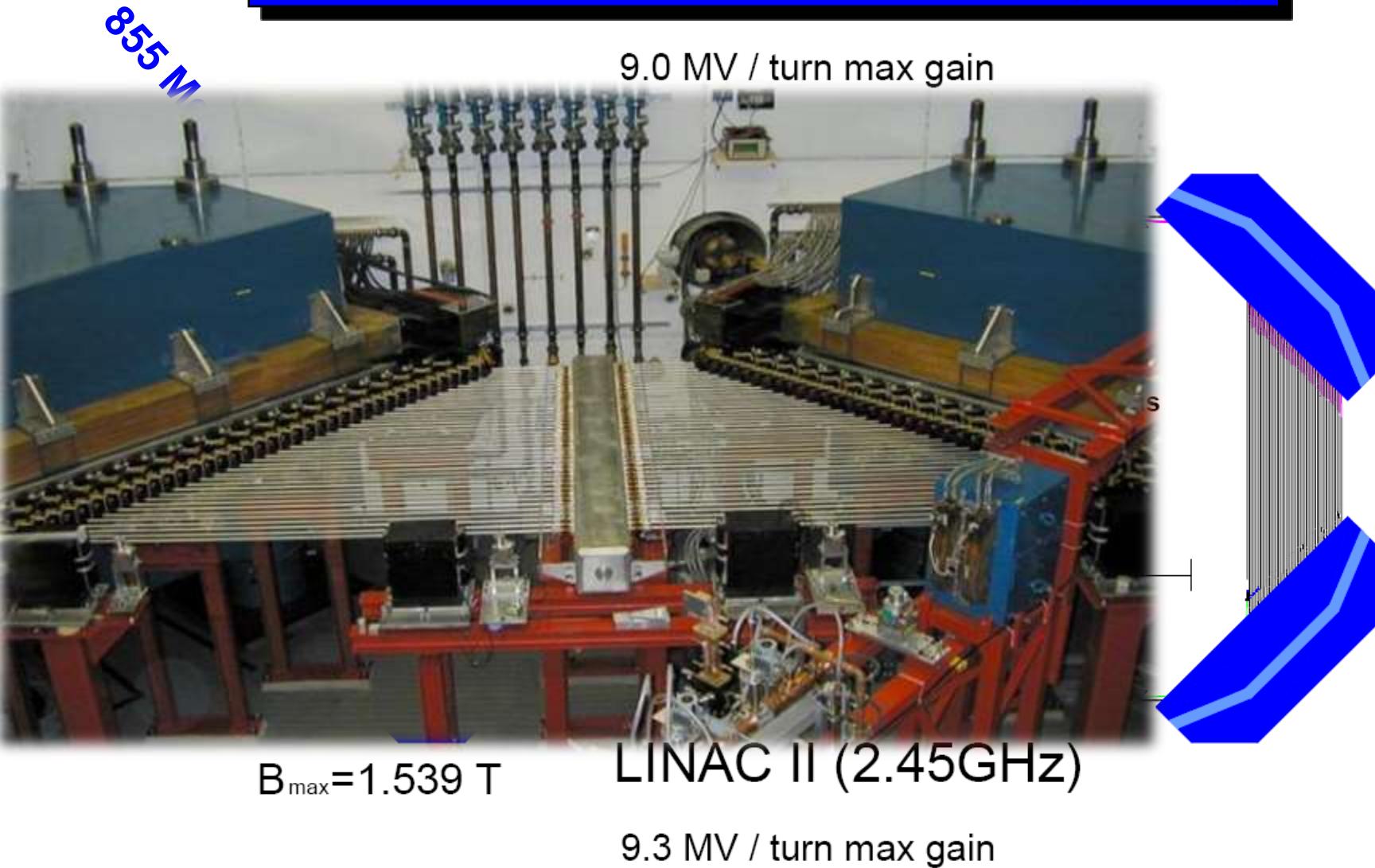
Race-Track Microtron (RTM)

Cascade of 3 RTMs with each 2 magnets + x times the same linac with radio-frequency acceleration (cw bunch structure 0.4 ns)



RTM3: single pass energy gain $7.5 \text{ MeV} \times 90 \text{ turns} = 675 \text{ MeV}$ total energy gain
with only 163 kW RF power for 67.5 kW of beam power @ 100 mA

Harmonic Double Sided Microtron (HDSM)



[K.-H. Kaiser et al., Nucl. Instr. Meth. A 593 (2008) 159]

Experimental realization at MAMI

Primary Beam

Energy	1.5 GeV
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Target

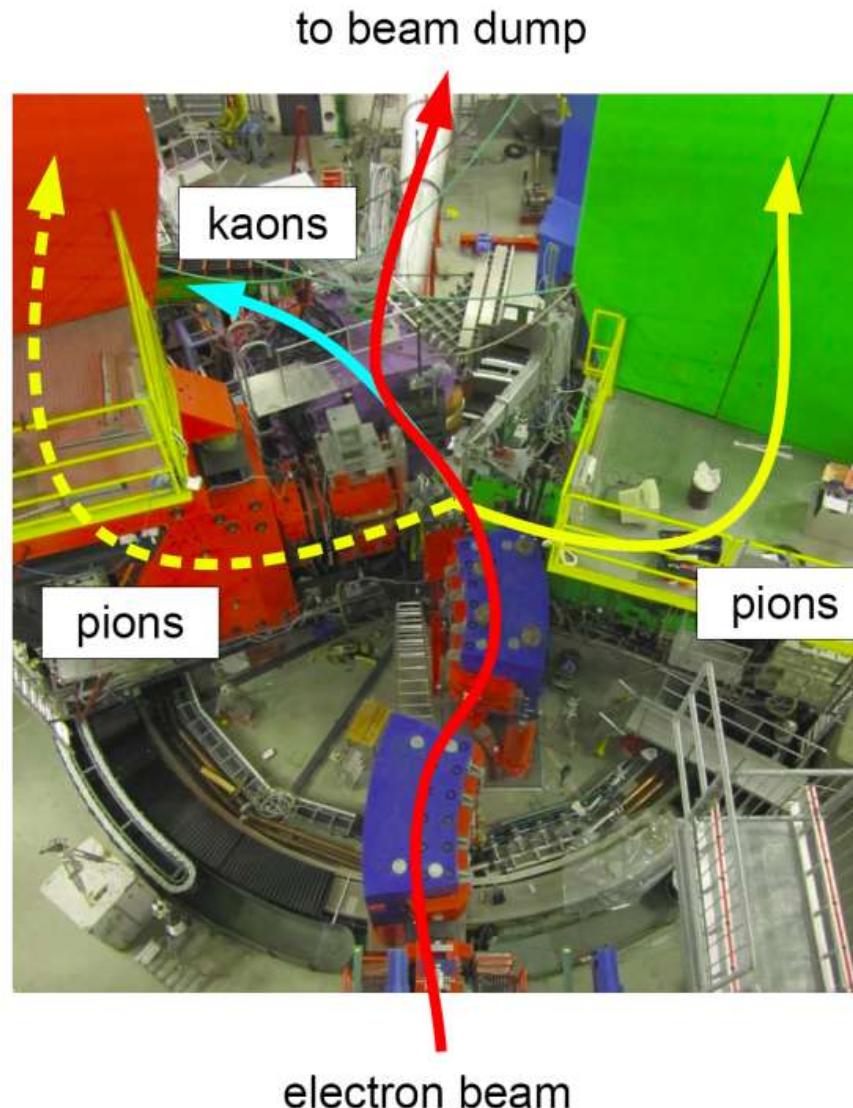
Material	${}^9\text{Be}$
Thickness	125 μm
Tilt angle	54 deg

Kaos

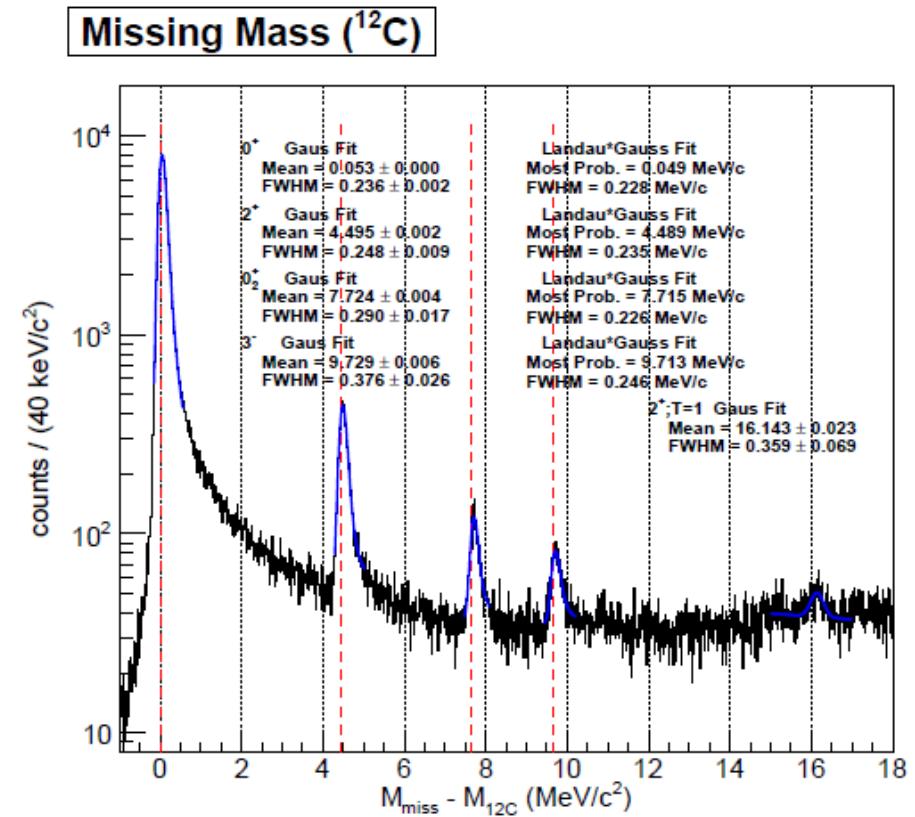
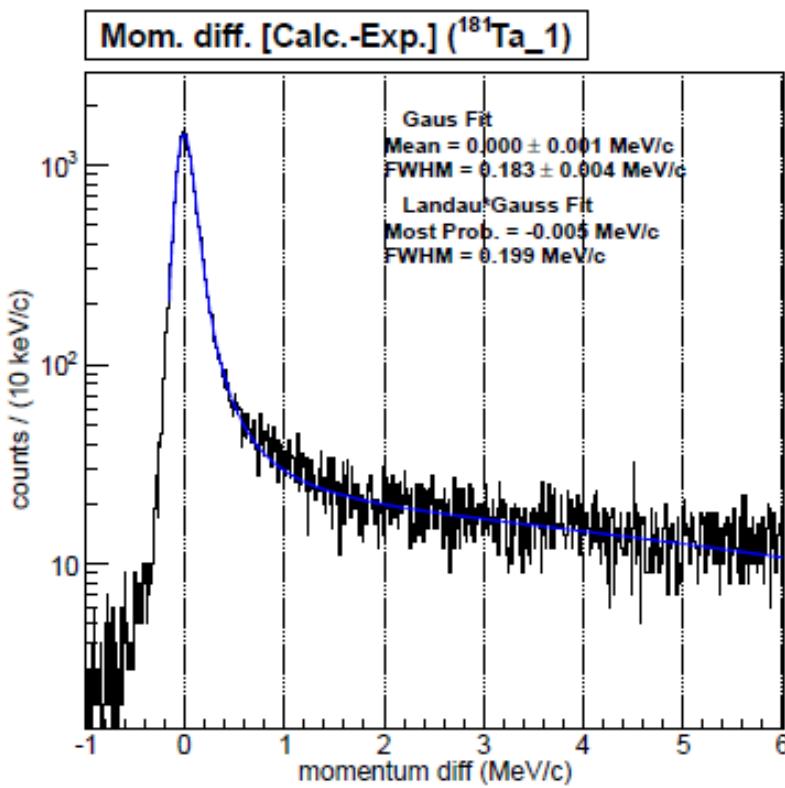
Cent. Mom	+900 MeV/c
Detector	MWPC, TOF, AC

Spek-A, C

Cent. Mom	- 115 / -125 MeV/c
Detector	DC, TOF, GC



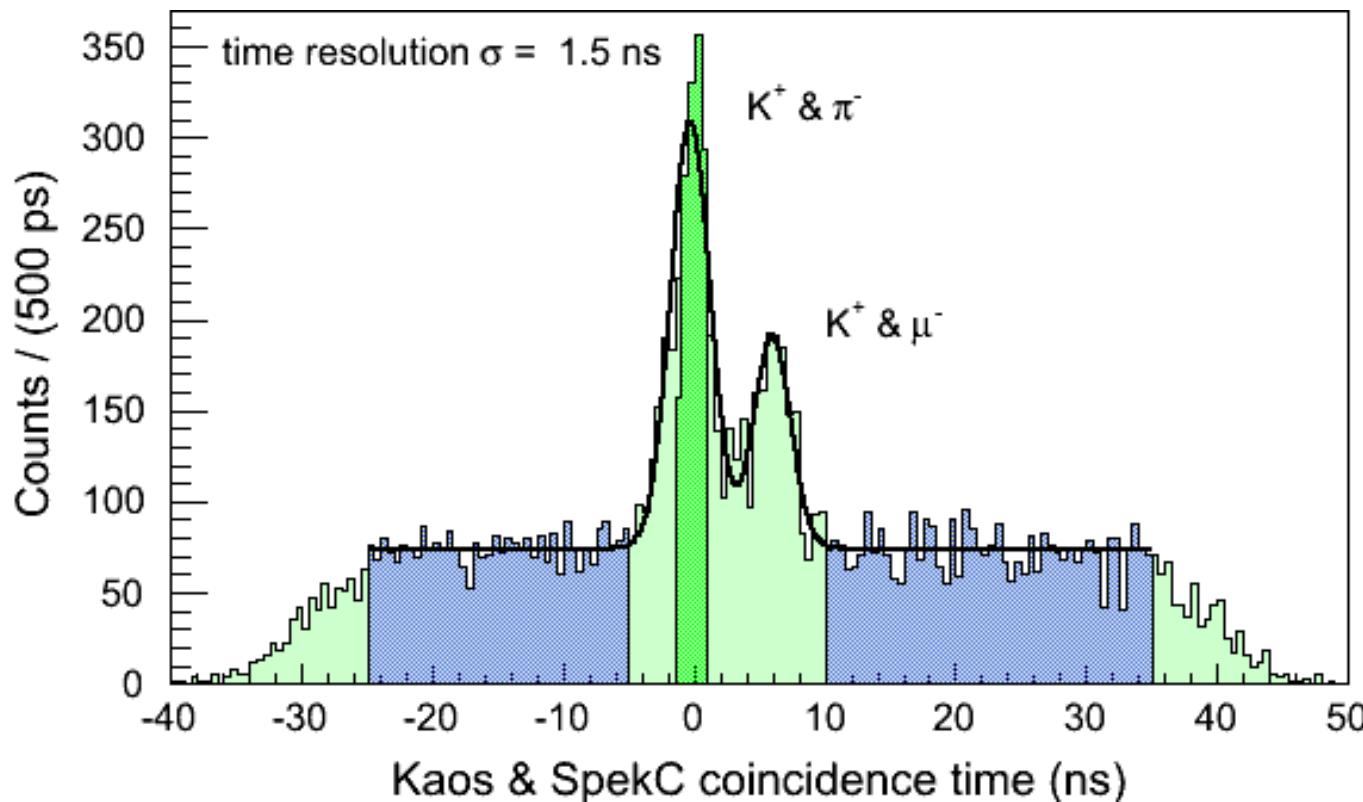
Decay pion momentum accuracy



- elastic & inelastic scattering off Ta and C to calibrate spectrometers
- elastic line FWHM of 200 keV/c at 200 MeV/c momentum
- beam energy measured with absolute accuracy of ± 160 keV

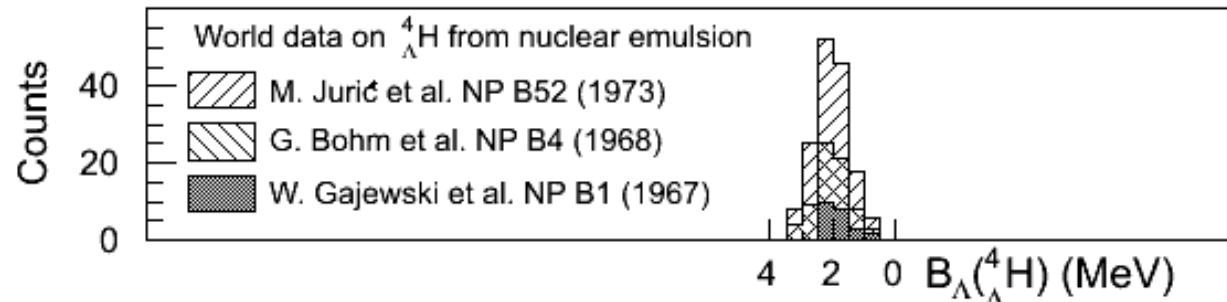
Reaction identification

with cut on gas Cherenkov
signal for electron rejection

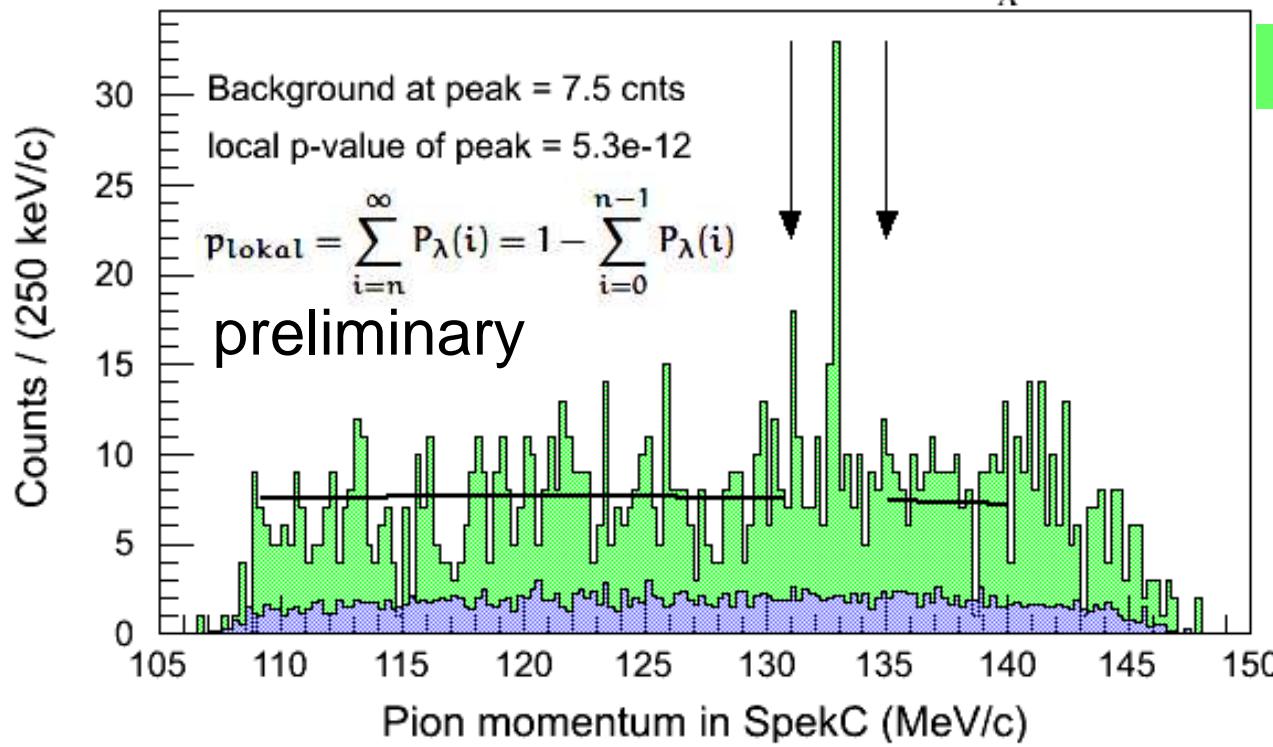


- established clean tag on strangeness production at zero-degree
- decay-pion detection with Spectrometer A & C ($d\mu/p < 10^{-4}$)
- more than 1000 pion-kaon-coincidences from weak decays of hyperons

Hyperhydrogen peak search



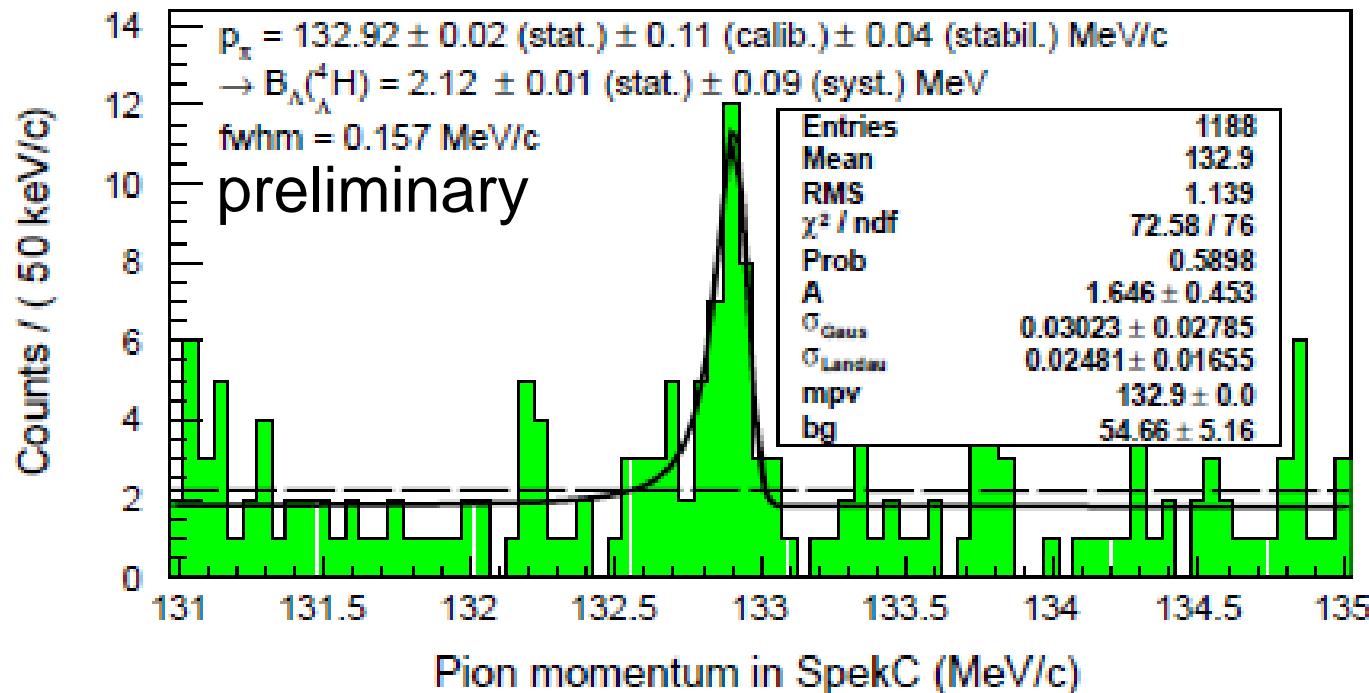
Emulsion data



MAMI data

local excess observed inside the hyperhydrogen search region

Binding energy extraction



$$M(^4\Lambda H) = \sqrt{M^2(^4\text{He}) + p_\pi^2} + \sqrt{M_\pi^2 + p_\pi^2} \quad \text{and}$$

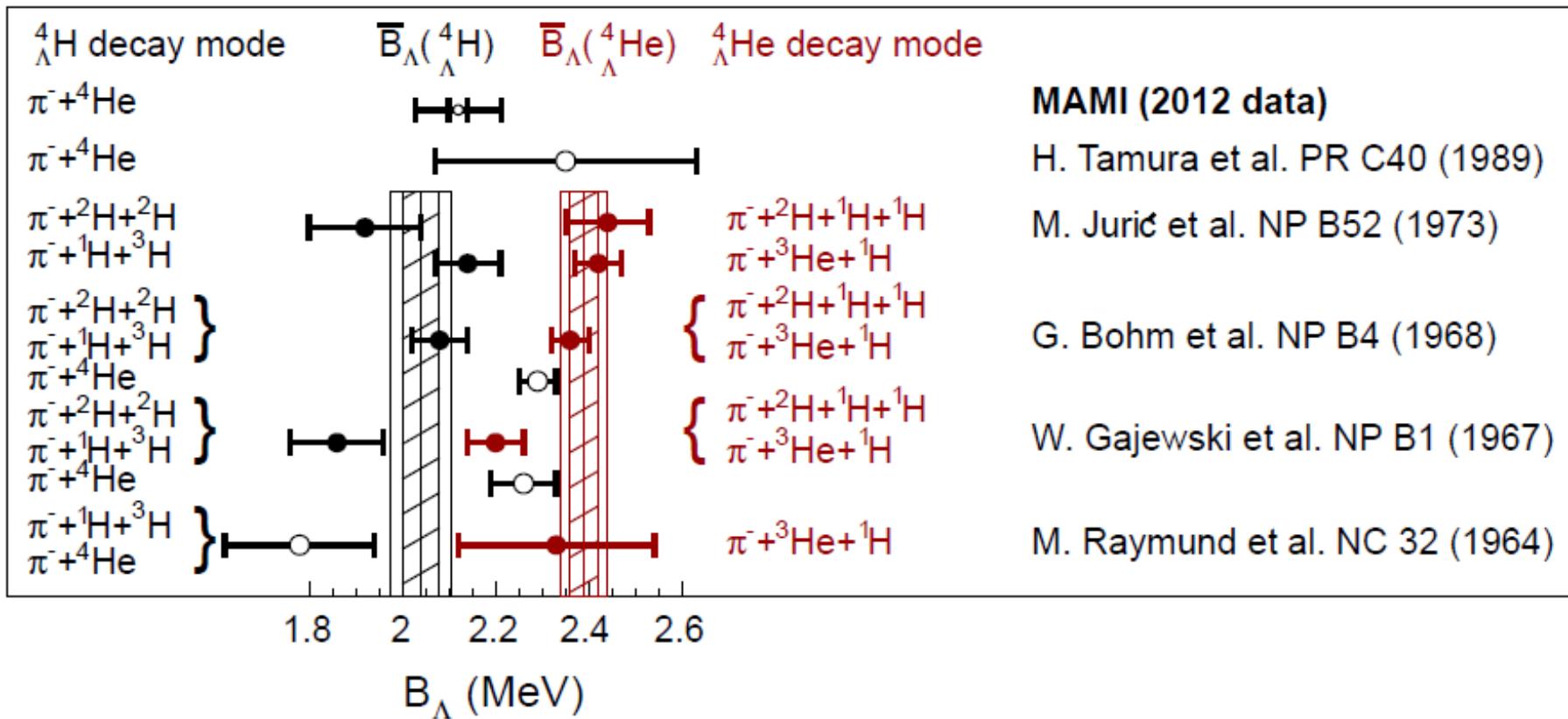
$$B_\Lambda = M(^3\text{H}) + M_\Lambda - M(^4\Lambda H) \quad \text{with } c = 1$$

$$S = \sqrt{-2 \ln \frac{L(BG)}{L(S+BG)}} = 4.7 \text{ with binned analysis}$$

S

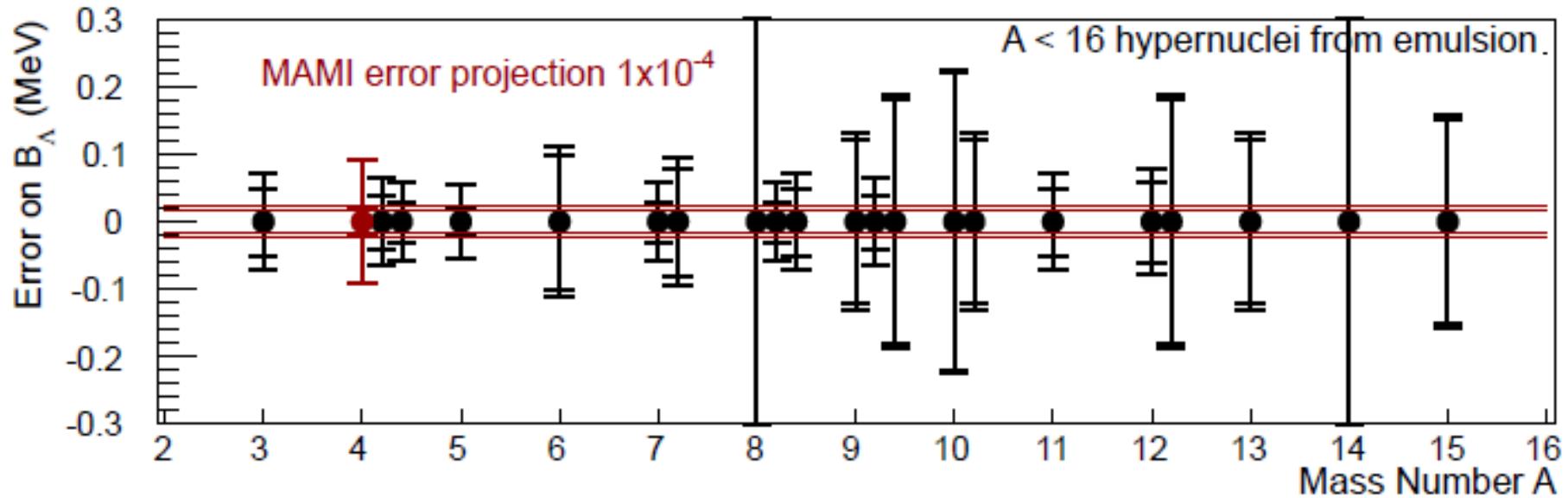
~ 4-5 with unbinned analysis

World data on $A = 4$ system



MAMI experiment confirmed Λ separation energy of ${}^4_{\Lambda}\text{H}$:
 $B_{\Lambda} \sim 2.12 \pm 0.1$ MeV (MAMI 2014 prelim.)

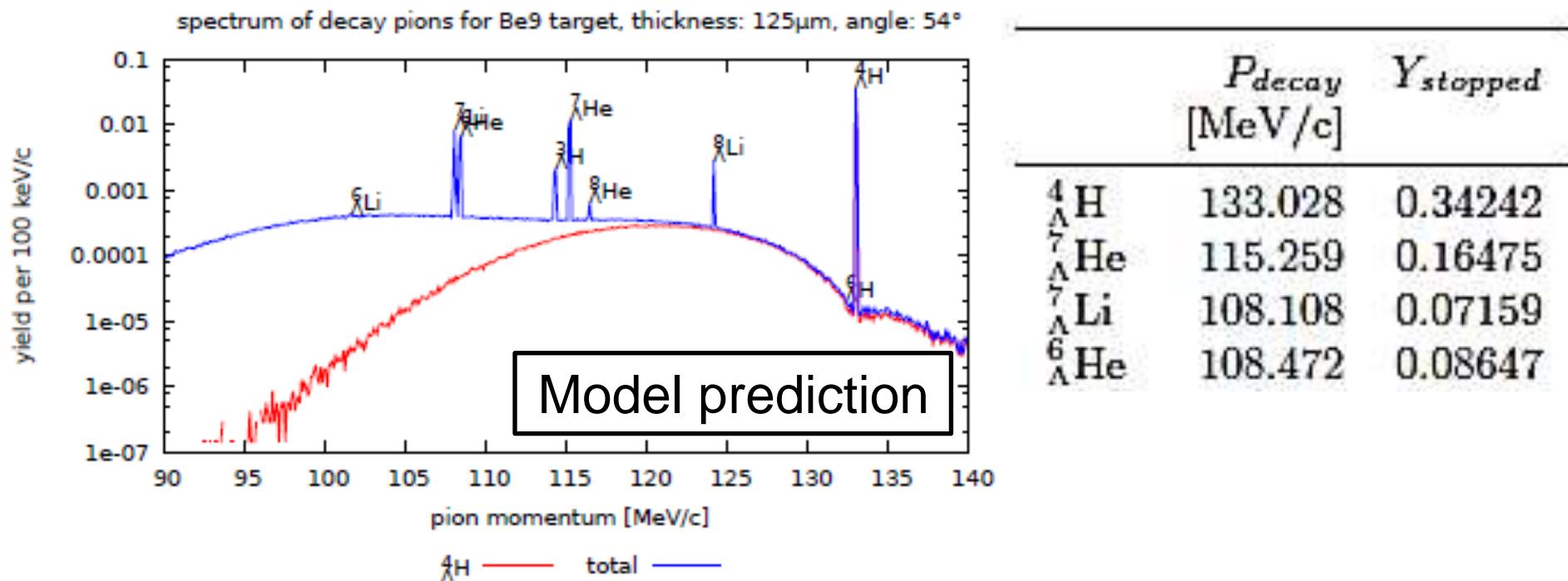
Comparison of errors



Emulsion: dominated by statistical error

MAMI: dominated (sofar) by systematic error of beam energy

Continuation of Experiment



- In 2014 next generation experiment performed with 5 x higher statistics
- Different target materials are under investigation
- Dominating systematic error can be reduced by improved calibrations

Conclusions and prospects

- Decay-pion spectroscopy it is now becoming a precision science
- Decay-pion spectroscopy gives access to ground state masses of light hypernuclei
- Precise measurements of the $A = 4$ system linked to understanding of charge symmetry breaking in ΛN interaction
- The accuracy of masses of many light hyperisotopes could be improved by this technique