

# Fluctuations in effective models



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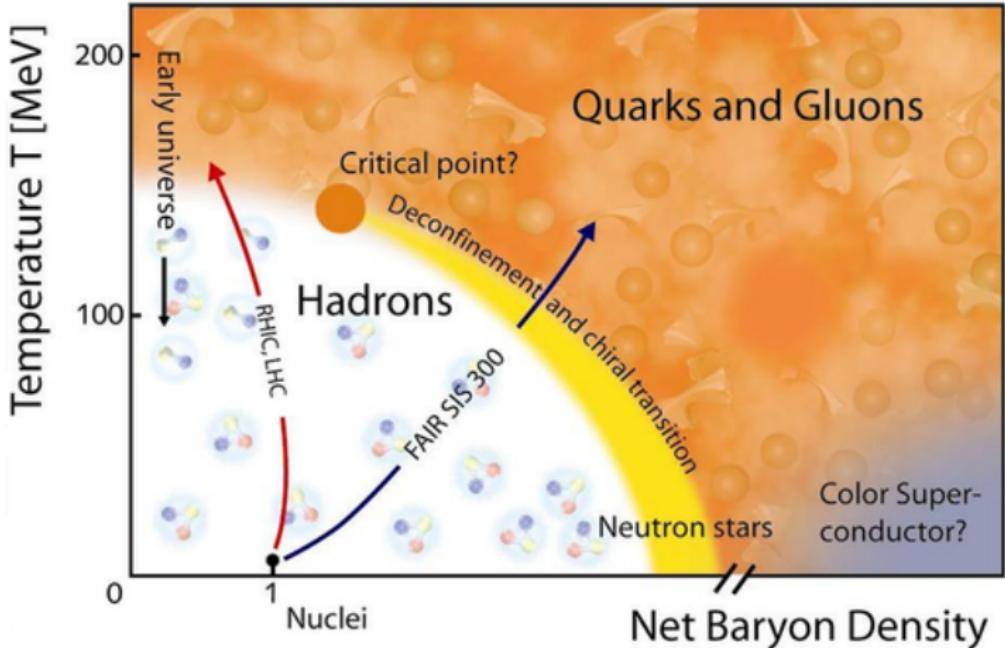
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# QCD phase diagram



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# Table of Contents

Coming up:

- ▶ Calculation of baryon number cumulants (thermal equilibrium)
- ▶ General structure of cumulants
- ▶ Freeze-out line in effective models
- ▶ Consistency of data with model predictions
- ▶ Effect of the repulsive vector interaction

# Polyakov–Quark-Meson model



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$$\mathcal{L} = \bar{q} [iD_\mu \gamma^\mu - g (\sigma + i\gamma_5 \vec{\pi} \cdot \vec{\pi})] q + \frac{1}{2} (\partial_\mu \sigma)^2 + \frac{1}{2} (\partial_\mu \pi)^2 - U(\sigma, \vec{\pi}) - U_P(T, \phi, \bar{\phi})$$

with the mesonic potential

$$U(\sigma, \vec{\pi}) = \frac{\lambda}{4} (\sigma^2 + \vec{\pi}^2 - v^2)^2 - H\sigma$$

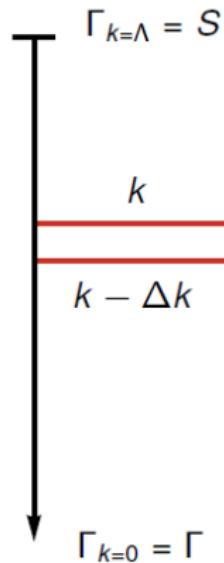
- ▶ Degrees of freedom: light quarks, pions, sigma meson (2 flavors)
- ▶ Low energy effective theory of QCD
- ▶ Describes chiral symmetry breaking
- ▶ Polyakov-loop: suppression of single quark fluctuations at low temperatures
- ▶ Same universality class as QCD

# Functional Renormalization Group

- ▶ Nonperturbative method
- ▶ Calculates the quantum effective action which translates to the pressure
- ▶ Wetterich equation:

$$\partial_k \Gamma_k [\Phi, \bar{\psi}, \psi] = \frac{1}{2} S \text{Tr} \left[ \left( \Gamma^{(2)} + R_k \right)^{-1} \partial_k R_k \right]$$

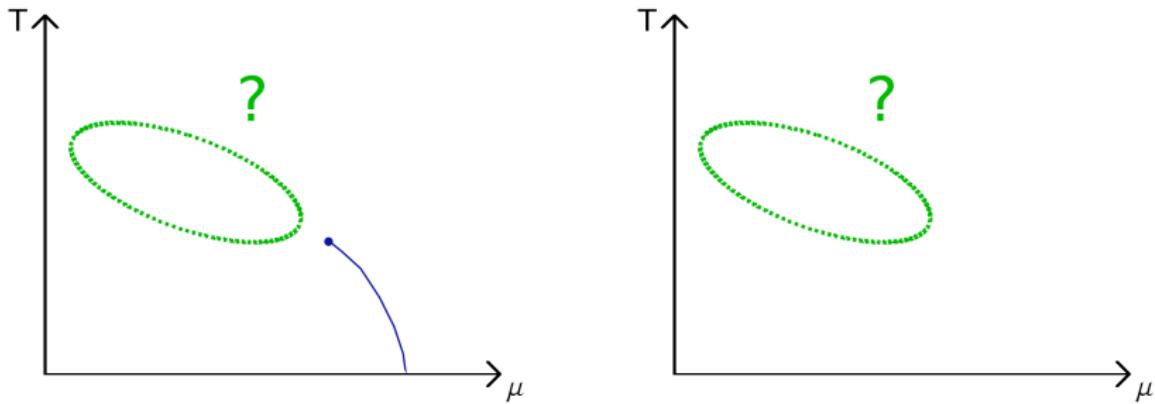
- ▶ Equation is solved on a grid



courtesy A. Tripolt

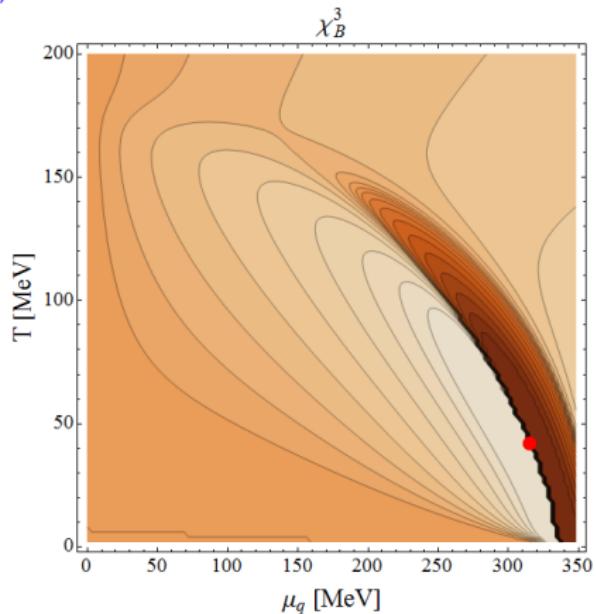
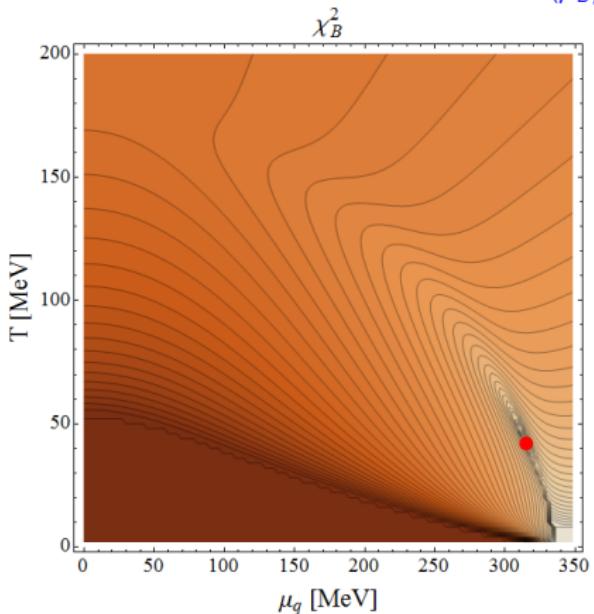
# Application of the model

- ▶ Qualitative fit to vacuum physics
- ▶ Use the remaining freedom to change the CEP location
- ▶ Calculate the baryon number cumulants  $\chi_B^n$
- ▶ Plot cumulant ratios on different lines



# Baryon number cumulants - an overview (MF)

$$\chi_B^n = \frac{1}{T^4} \frac{\partial^n P(T, \mu_B)}{\partial(\mu_B/T)^n}, \quad \mu_B = 3\mu_q$$

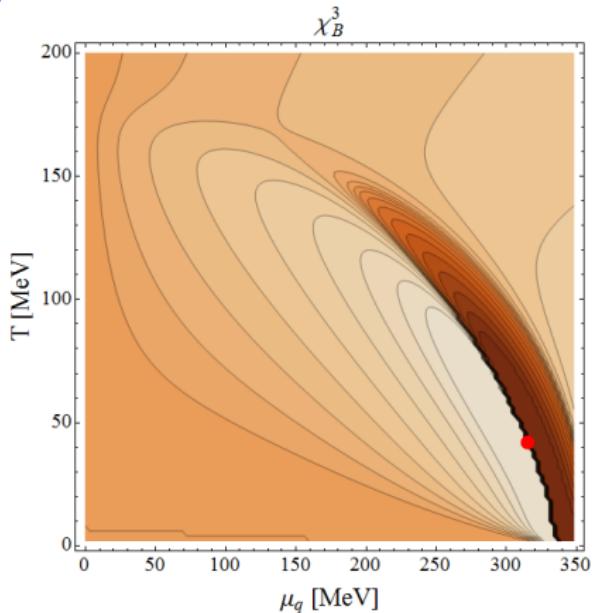
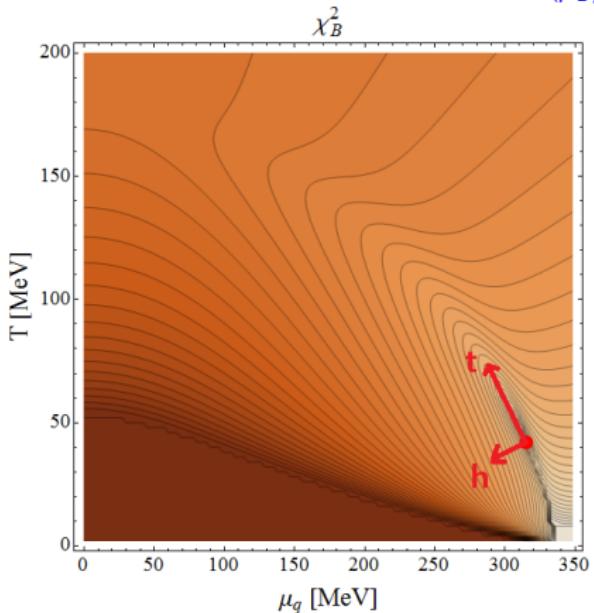


# Baryon number cumulants - an overview (MF)



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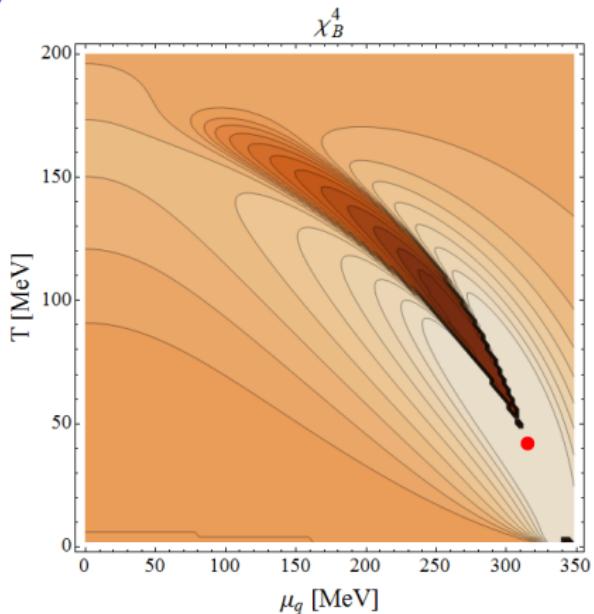
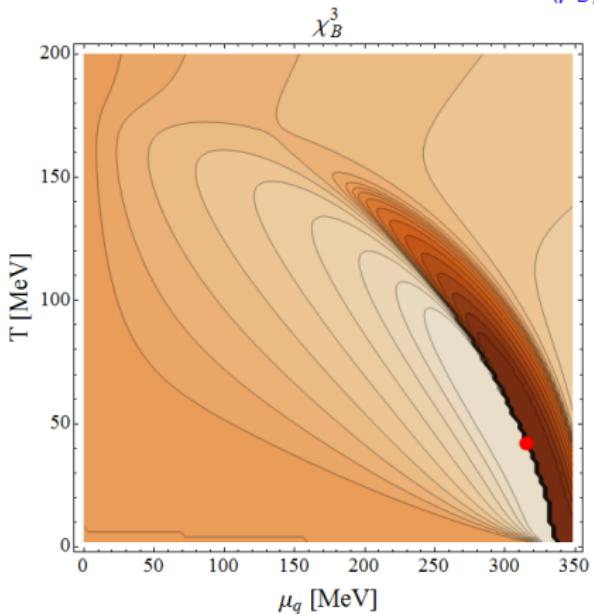


# Baryon number cumulants - an overview (MF)



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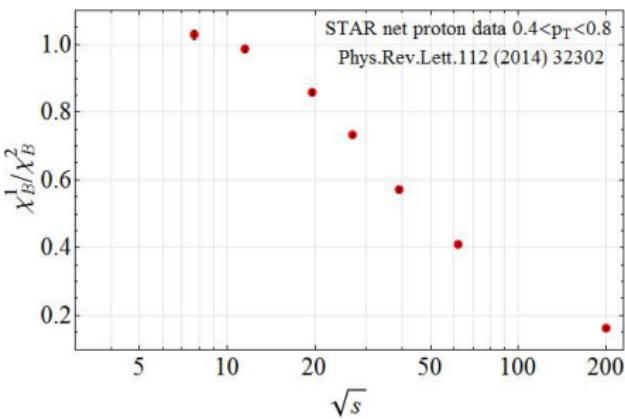
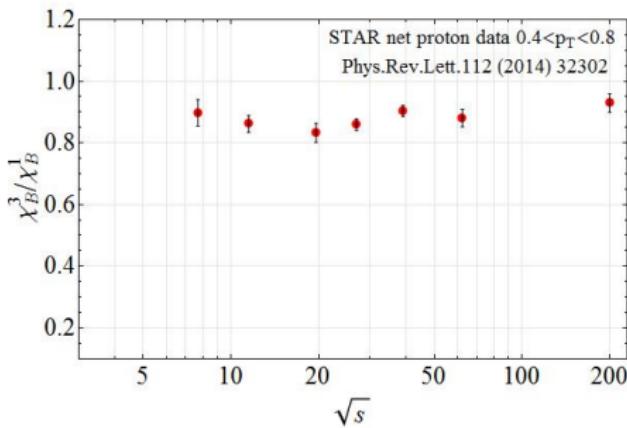
# Freeze-out condition



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Baryon number cumulants:  $\chi_B^n = \frac{1}{T^4} \frac{\partial^n P(T, \mu_B)}{\partial(\mu_B/T)^n}$

$$\chi_B^1/\chi_B^2 \leftrightarrow M/\sigma^2 \quad \chi_B^3/\chi_B^1 \leftrightarrow S\sigma^3/M \quad \chi_B^4/\chi_B^2 \leftrightarrow \kappa\sigma^2$$



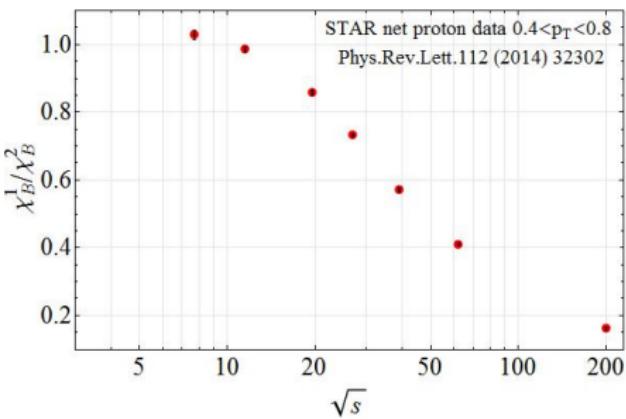
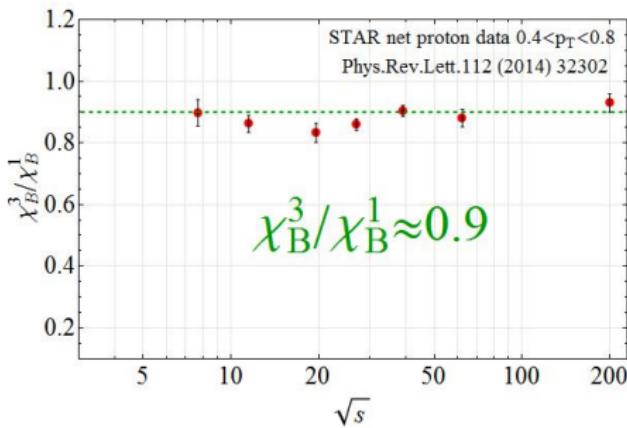
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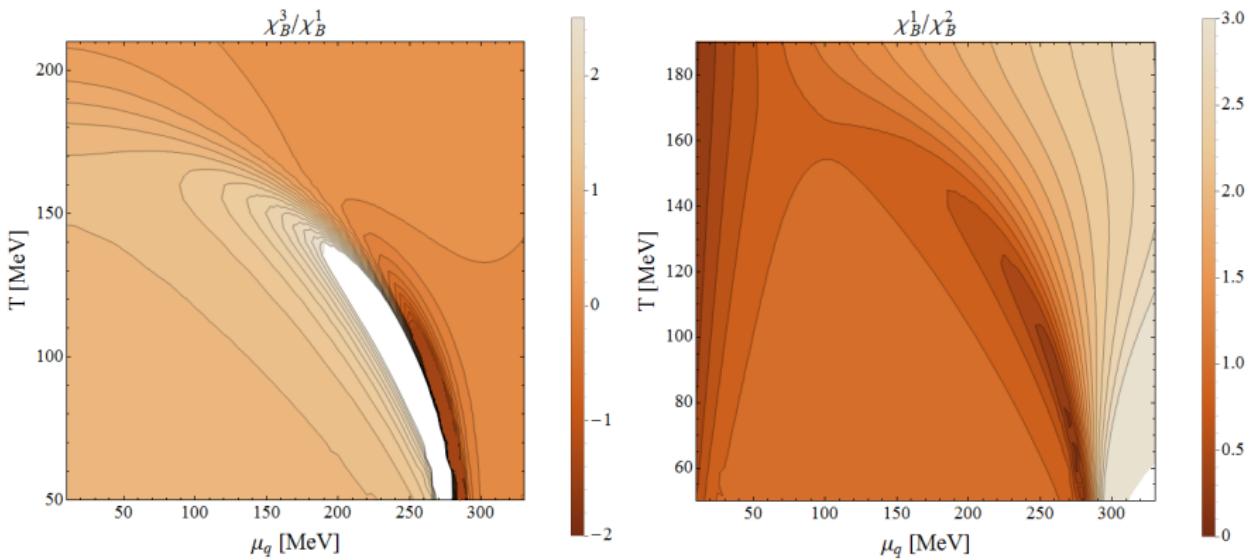
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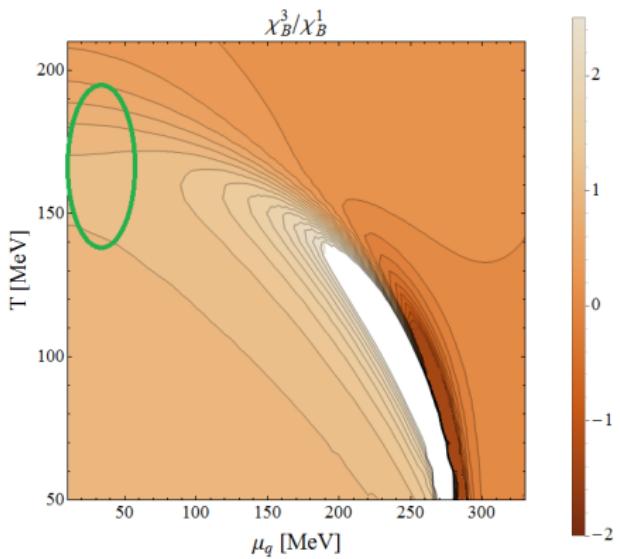
# General behavior of the cumulant ratios



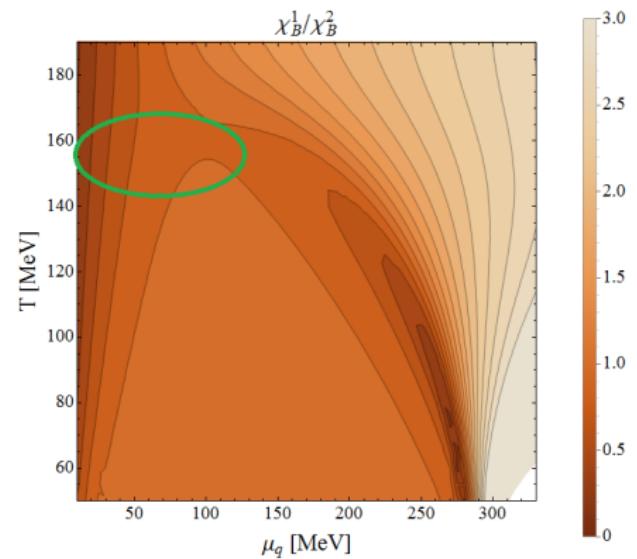
# General behavior of the cumulant ratios



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Mainly determined by  $T$

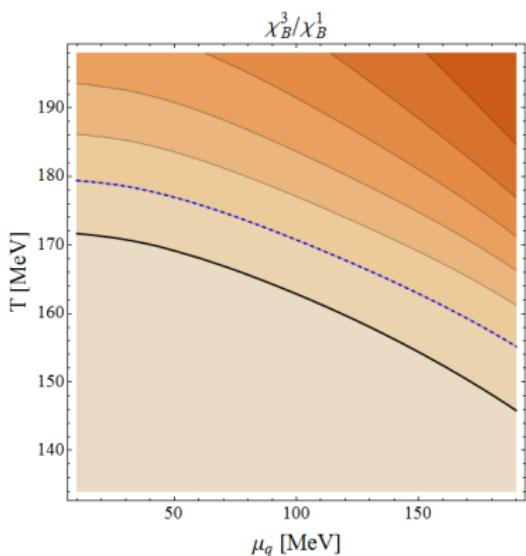


Mainly determined by  $\mu$

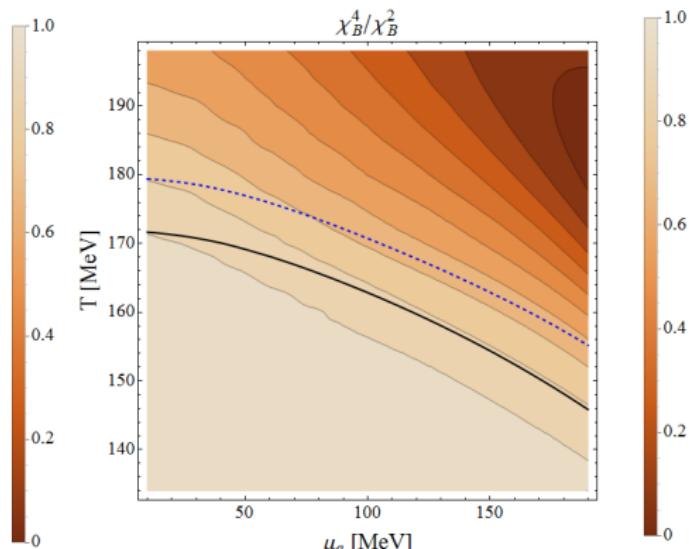
# No CEP scenario



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Black line:  $\chi_B^3/\chi_B^1 = 0.9$

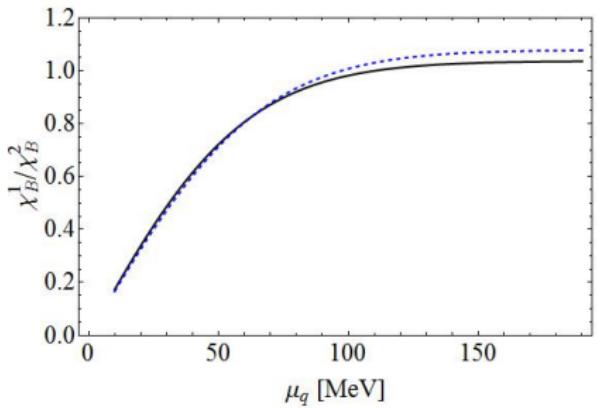


Blue (dashed) line:  $\chi_B^4/\chi_B^2 = 0.8$

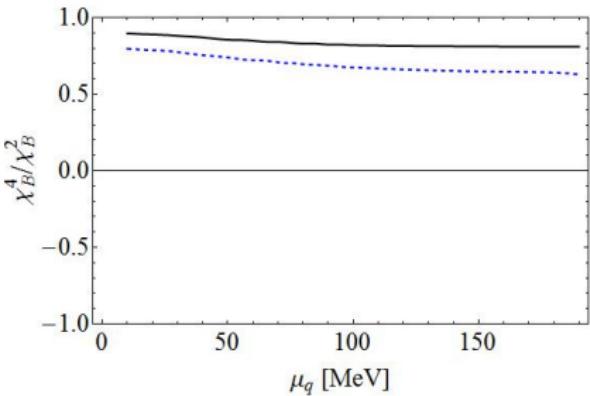
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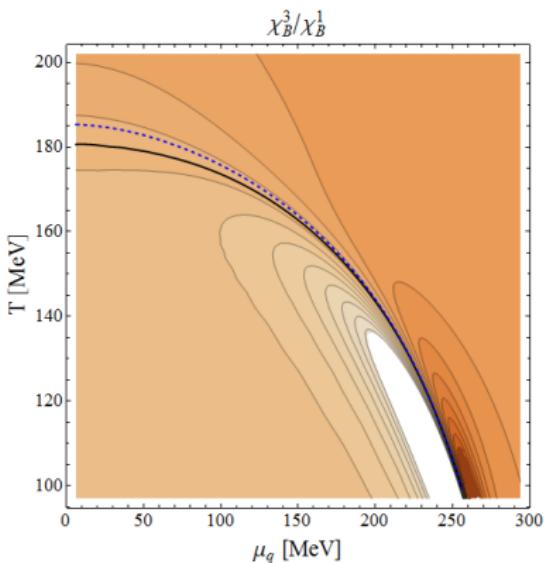


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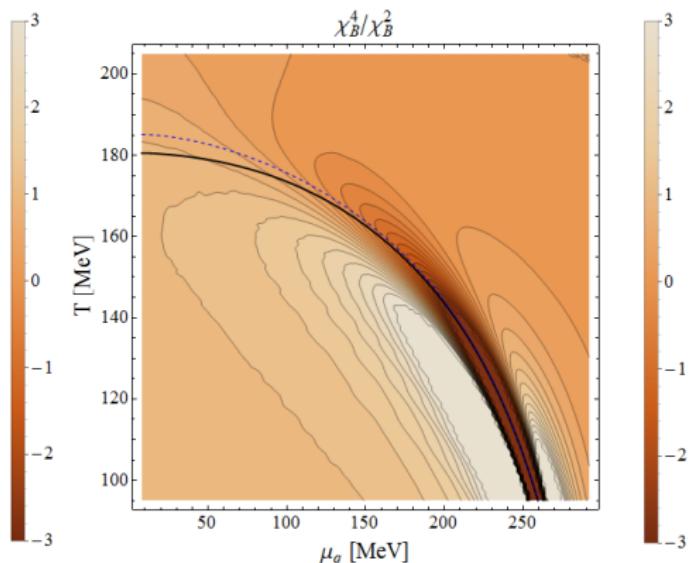
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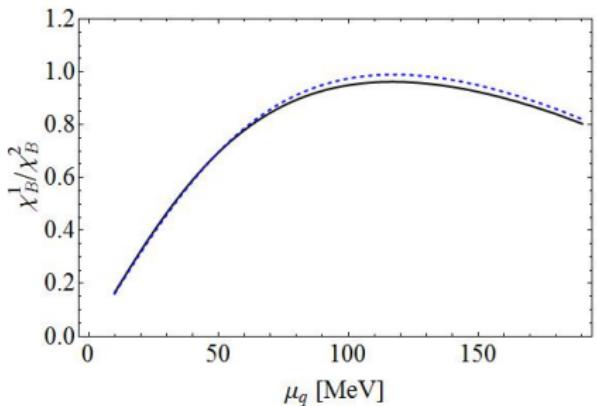


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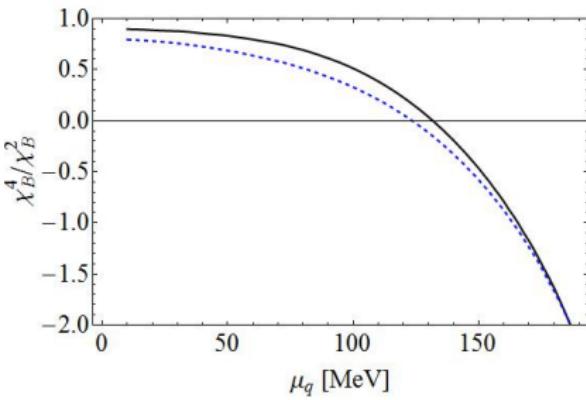


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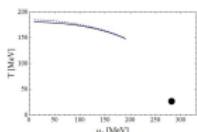


Black line:  $\chi_B^3/\chi_B^1 = 0.9$   
 $\chi_B^1/\chi_B^2$  has a maximum

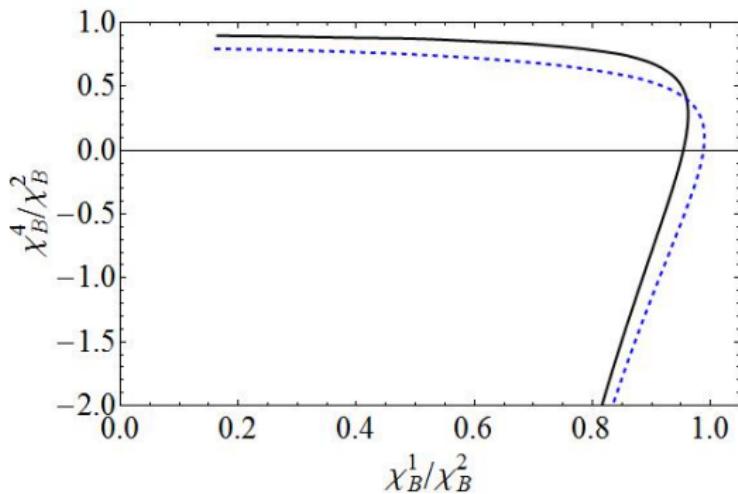
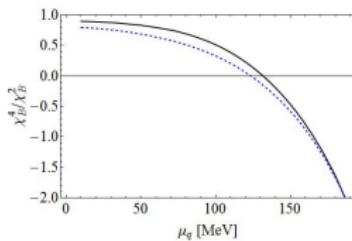
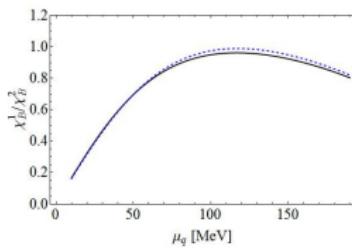


Blue (dashed) line:  $\chi_B^3/\chi_B^1 = 0.8$   
 $\chi_B^4/\chi_B^2$  decreases monotonously

# CEP scenario



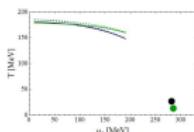
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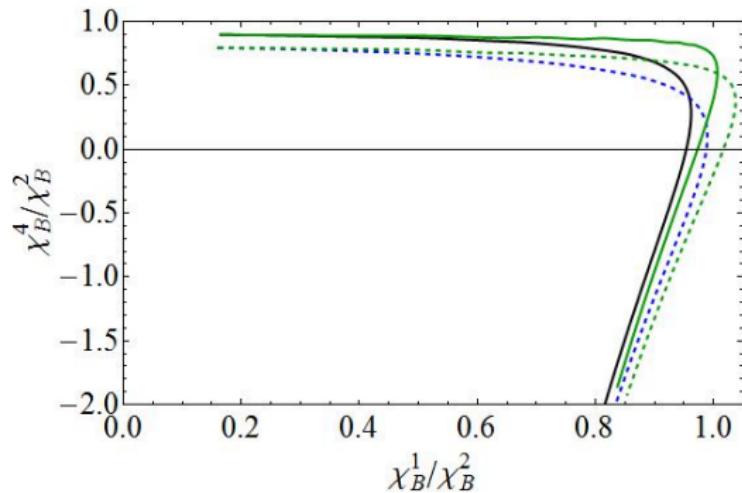
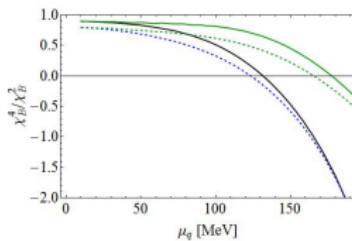
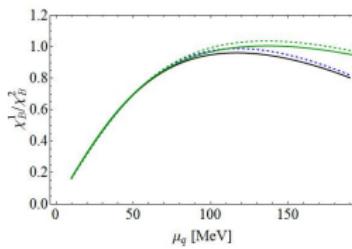
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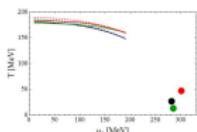
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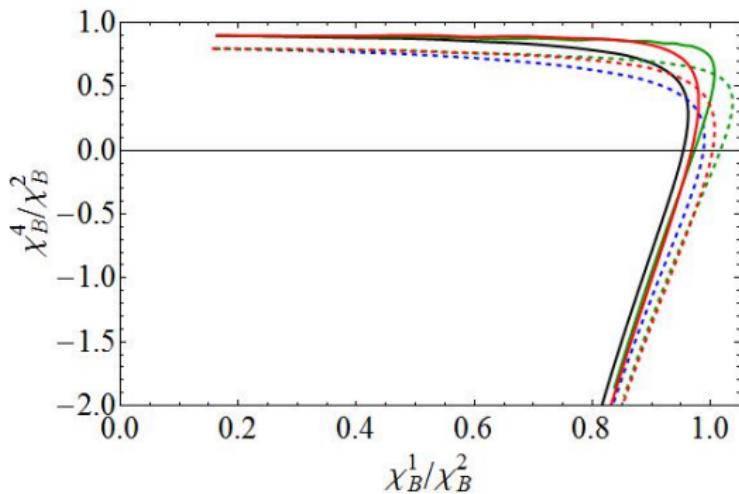
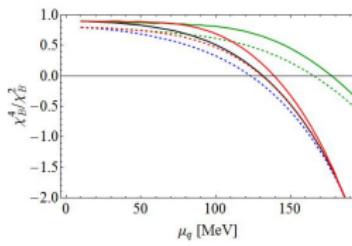
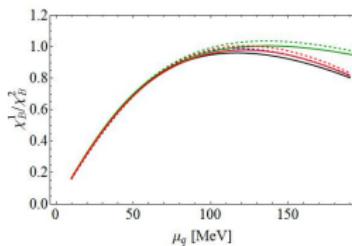
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# CEP scenario



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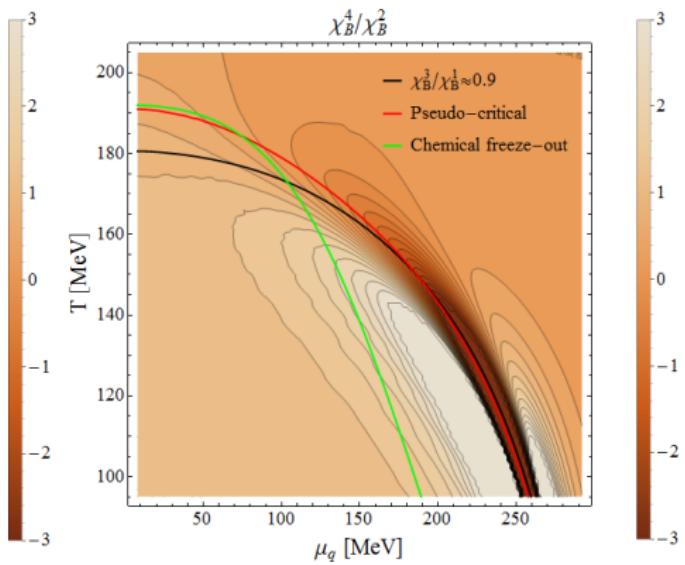
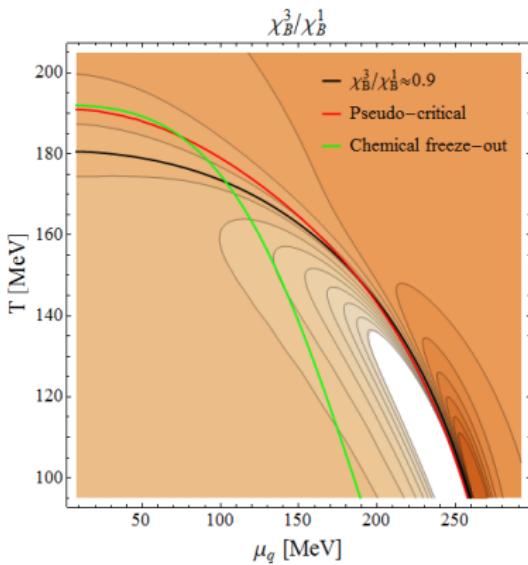
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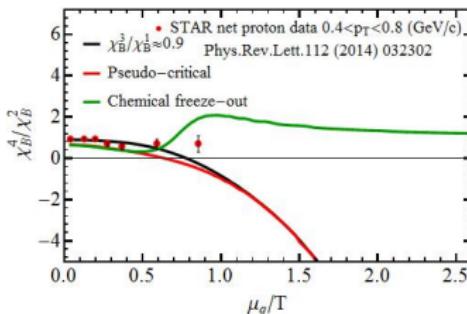
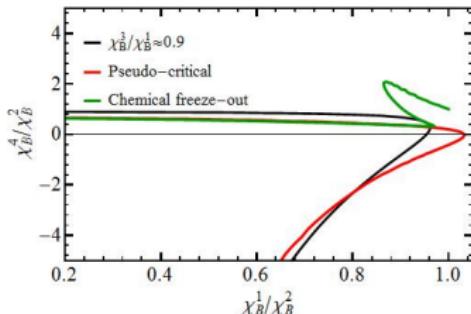
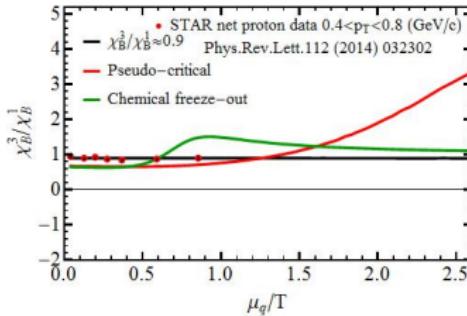
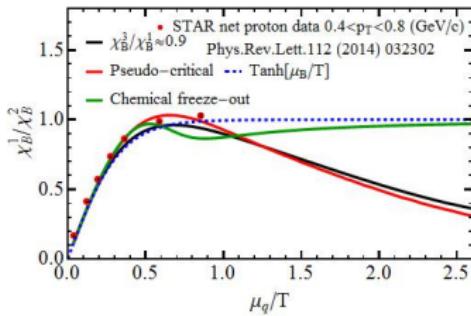
# Comparision of different "freeze-out" lines



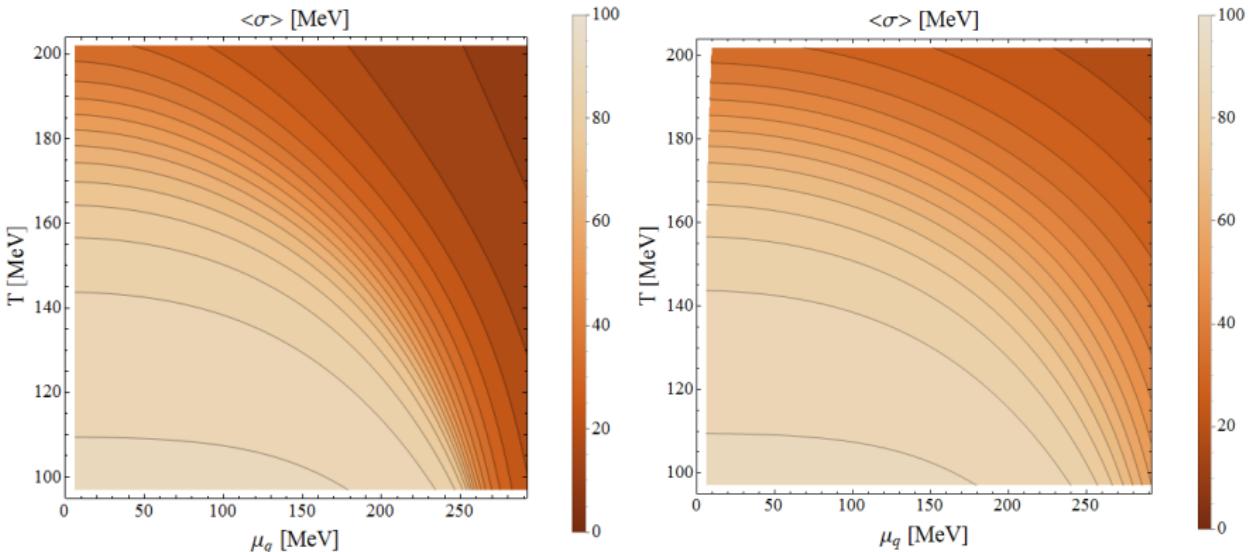
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# Comparision of different "freeze-out" lines



# Effect of vector interaction – condensate

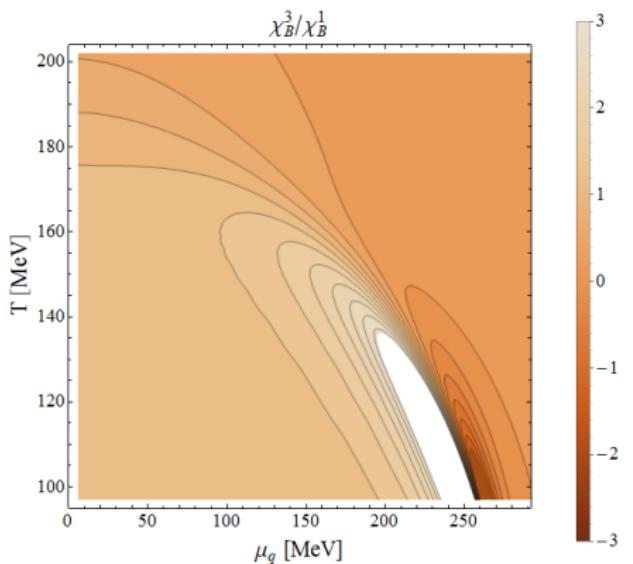


Rescaling of the  $\mu$  axis:  $\mu = \mu_{eff} + G_V \langle n \rangle_{\mu_{eff}}$

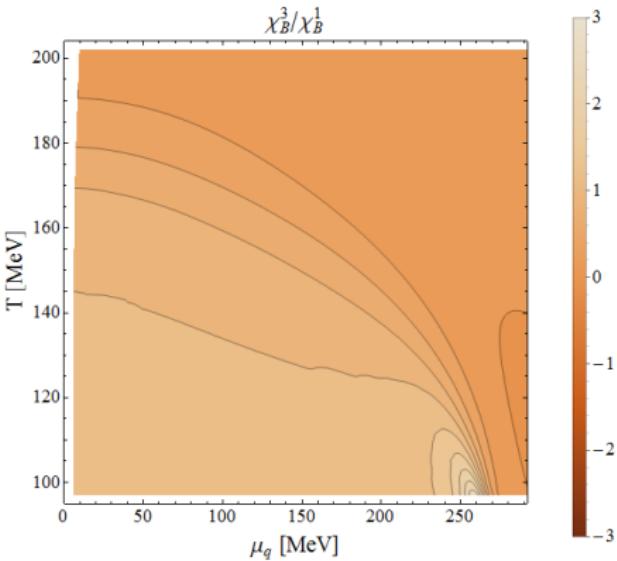
# Effect of vector interaction – $\chi_B^3/\chi_B^1$



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No vector interaction

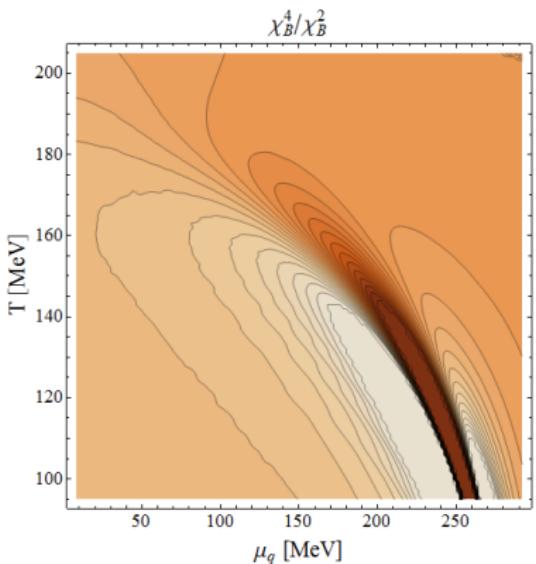


Significant vector interaction

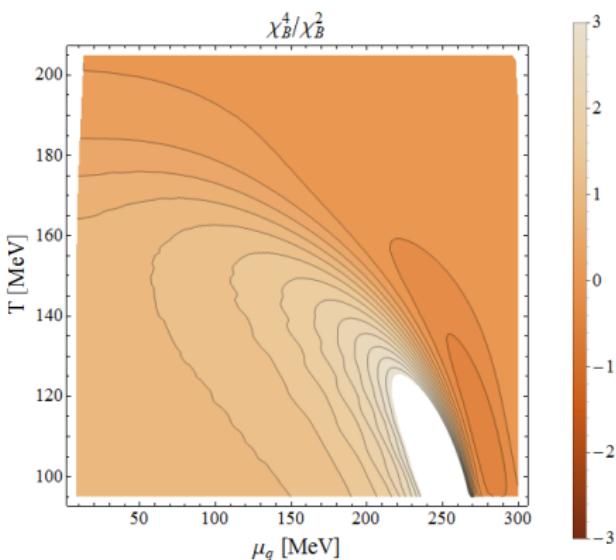
# Effect of vector interaction – $\chi_B^4/\chi_B^2$



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No vector interaction

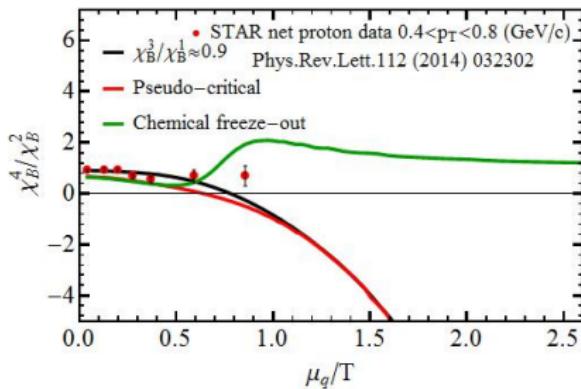
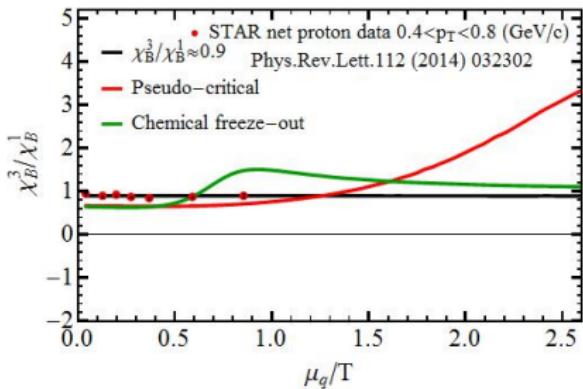


Significant vector interaction

# Effect of vector interaction – Curves



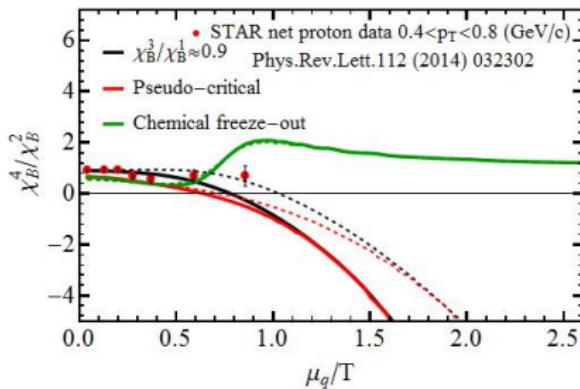
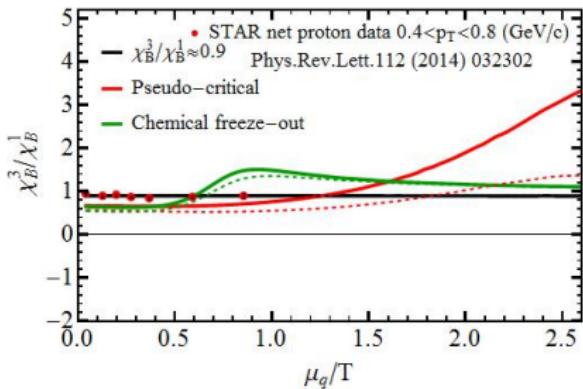
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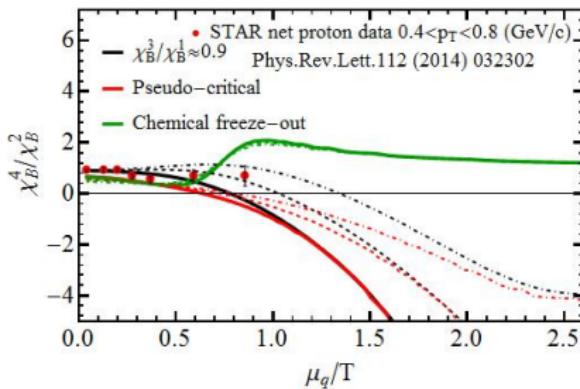
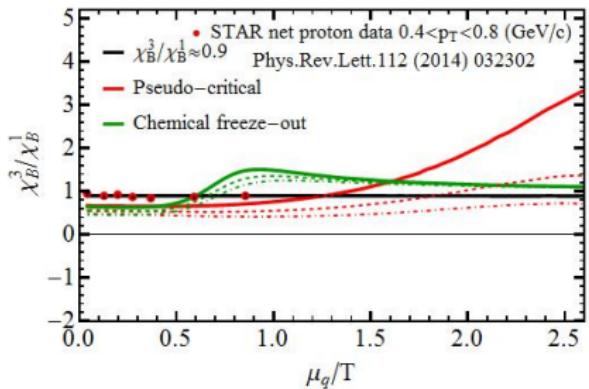
# Effect of vector interaction – Curves



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# Effect of vector interaction – Curves



Vector interaction decreases the signal of the CEP at fixed small chemical potentials

# Summary

- ▶ Baryon number cumulants up to  $\chi_B^4$  obtained in the FRG framework
- ▶ Consistent freeze-out line determination is important
- ▶ The CEP does influence the behavior of the cumulants
- ▶ Correlation between  $\chi_B^4/\chi_B^2$  and  $\chi_B^3/\chi_B^1$
- ▶ Vector interaction decreases the effect of the CEP

# Backup

# Ising model in Landau-theory



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gap equation:  $M^3 + a(T - T_c)M - H = 0$   
susceptibility:  $\chi = \frac{\chi_0}{a(T - T_c) + 3M^2}$

$T = T_c$  limit:  $M \sim H^{1/3}$   
 $\chi \sim H^{-2/3}$

$H = 0$  limit:  $M \sim (T - T_c)^{1/2}$   
 $\chi \sim (T - T_c)^{-1}$

