

# The high-density Equation of State from heavy-ion reactions

## Outline:

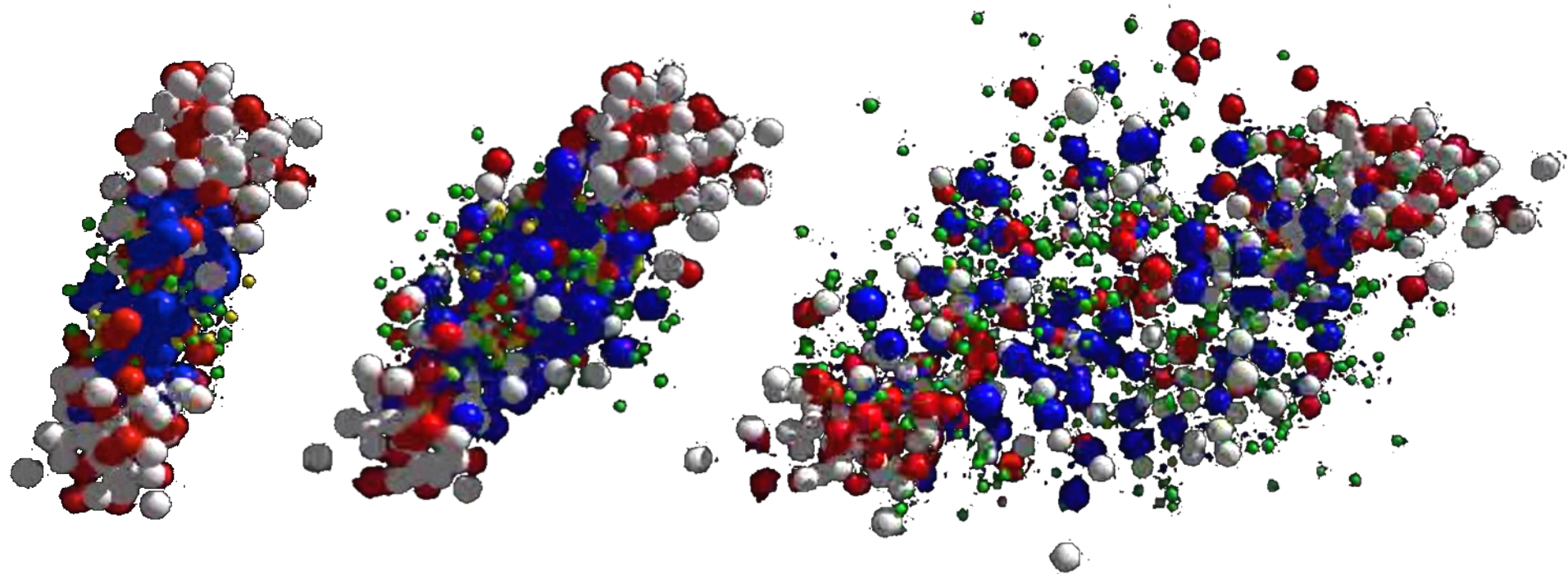
Peter Senger

- Exploring the high-density EoS in the laboratory
- The QCD phase diagram at large  $\mu_B$
- Future experiments: CBM at FAIR and BM@N at NICA



Nuclear equation of state and neutron stars  
International Workshop XLVIII on Gross Properties of Nuclei and Nuclear Excitations  
Hirschegg, Kleinwalsertal, Austria, January 12 - 18, 2020

# Production of dense nuclear matter in high-energy heavy-ion collisions

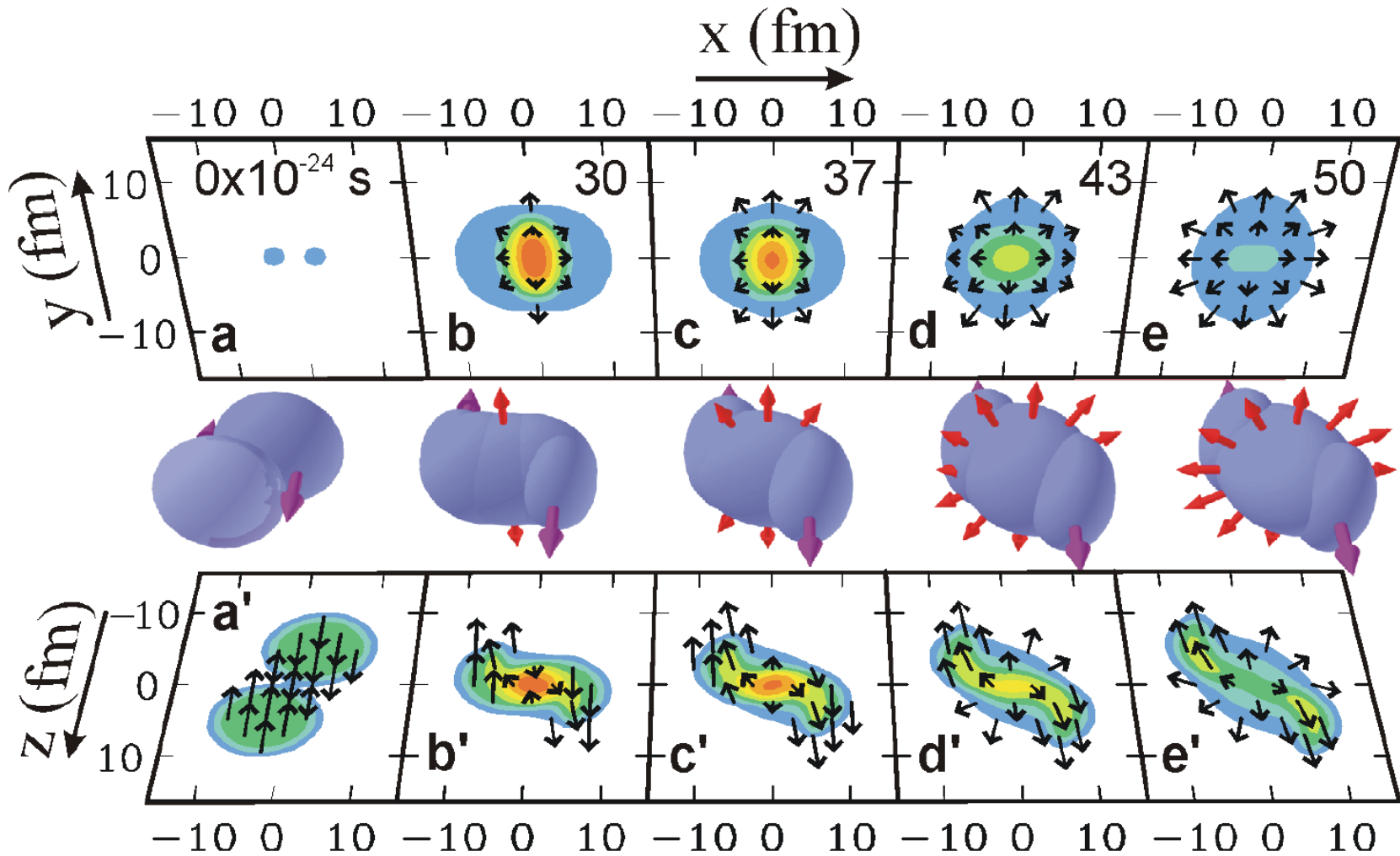


Baryon densities in the laboratory:  $3 - 10 \rho_0$ , but:  
volume about  $1000 \text{ fm}^3$ , lifetime  $10^{-22} \text{ s}$ ,  $T = 70 - 120 \text{ MeV}$ ,  
non-equilibrated system, ...

- extraction of EOS via relativistic transport calculations
- observables: collective flow, subthreshold particle production

# Collective flow of nucleons

semi-central Au+Au collision at 2 AGeV



**Collective flow of nucleons: driven by pressure gradient**

# The nuclear matter equation-of-state

$$P = \delta E / \delta V \Big|_{T=\text{const}}$$

$$V = A / \rho$$

$$\delta V / \delta \rho = - A / \rho^2$$

$$P = \rho^2 \delta(E/A) / \delta \rho \Big|_{T=\text{const}}$$

$$E_A(\rho, \delta) = E_A(\rho, 0) + E_{\text{sym}}(\rho) \cdot \delta^2$$

$$\text{with } \delta = (\rho_n - \rho_p) / \rho$$

Symmetric matter ( $\delta=0$ ):

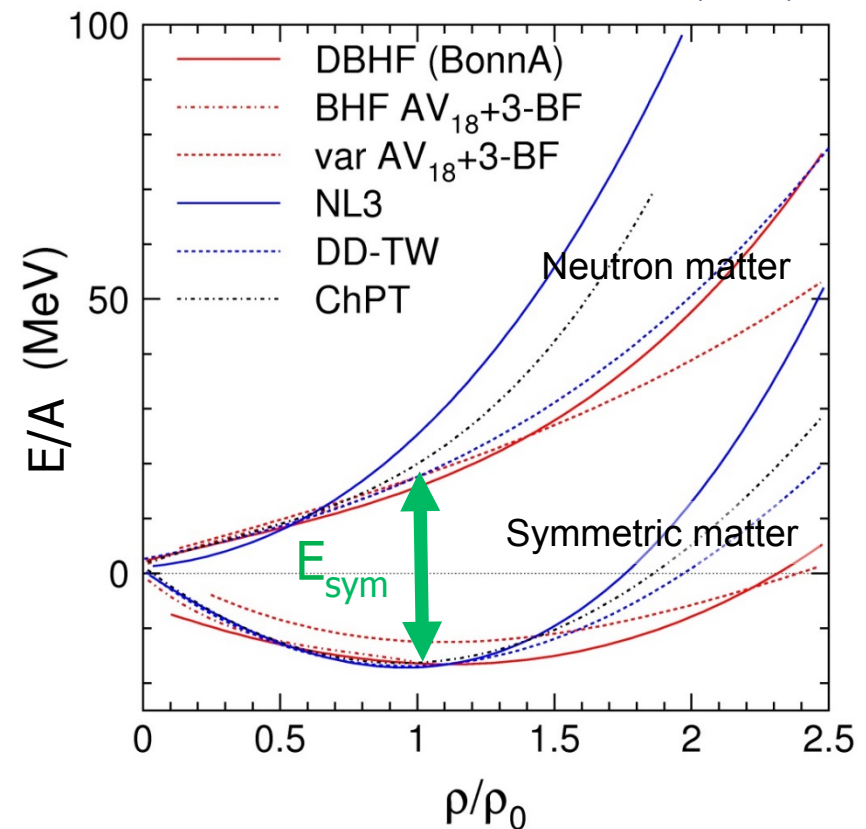
- $E/A(\rho_0) = -16 \text{ MeV}$
- slope  $\delta(E/A)(\rho_0) / \delta \rho = 0$
- curvature  $K_{\text{nm}} = 9\rho^2 \delta^2(E/A) / \delta \rho^2$   
(nuclear incompressibility)

$$T=0: E/A = 1/\rho \int U(\rho) d\rho$$

Effective NN-potential:

$$U(\rho) = \alpha\rho + \beta\rho^\gamma$$

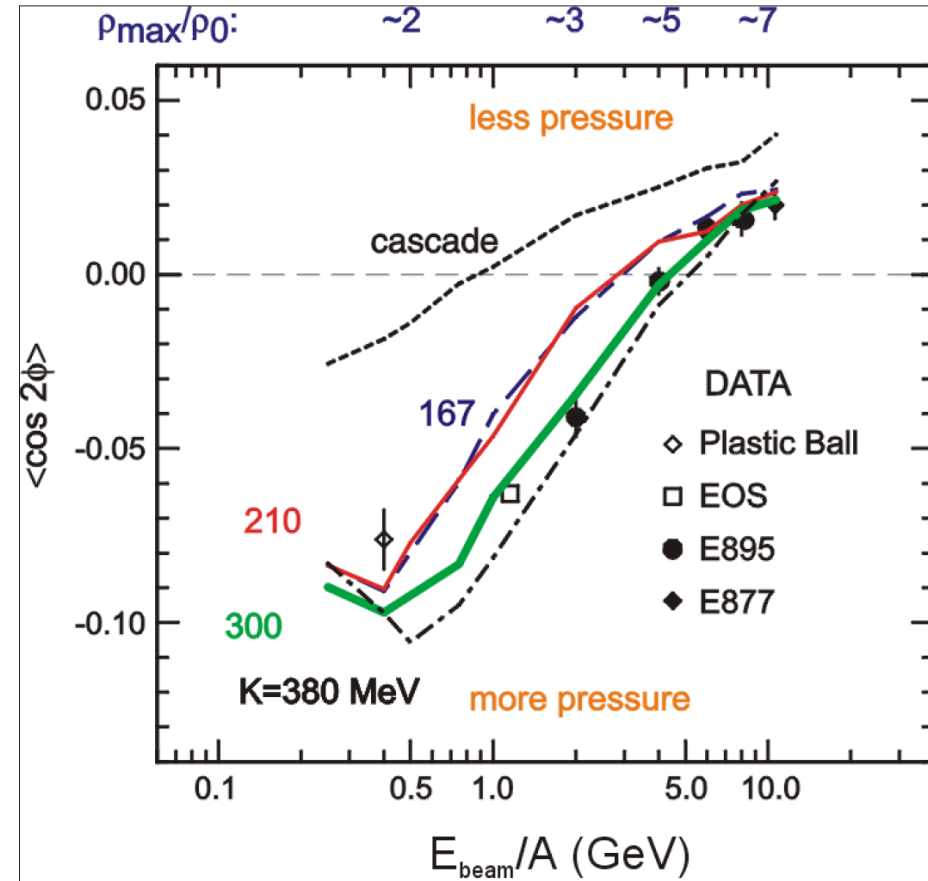
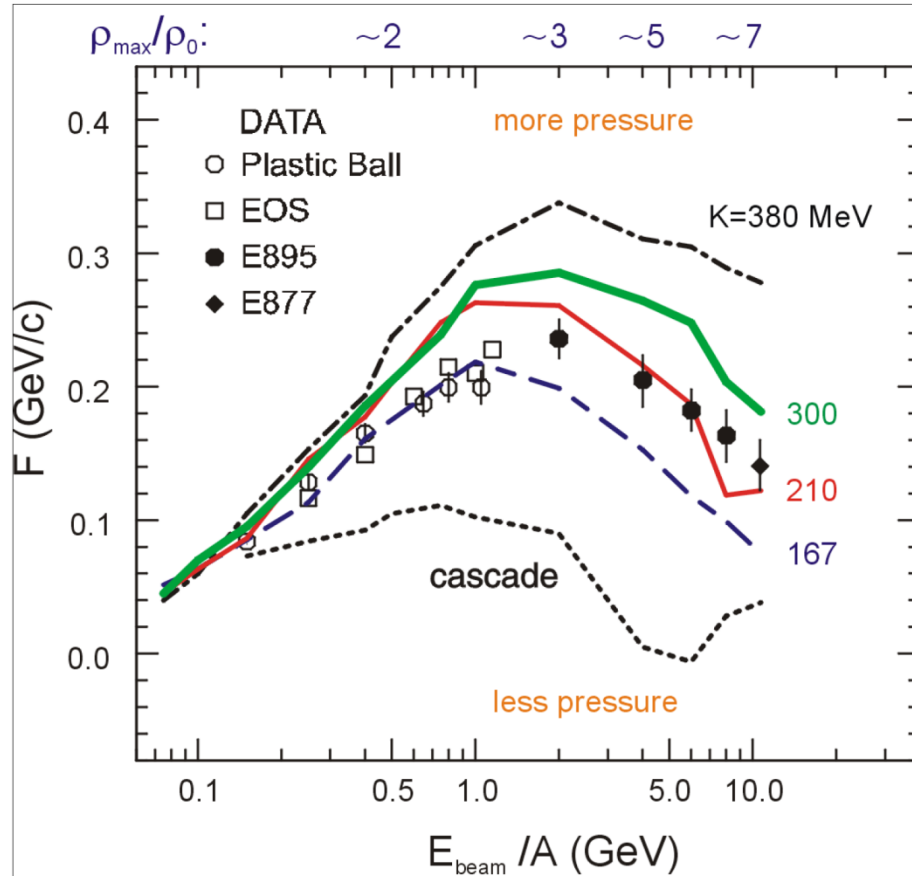
Ch. Fuchs and H.H. Wolter, EPJA 30 (2006) 5





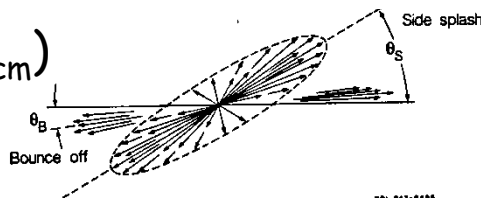
# Nuclear incompressibility from collective proton flow

P. Danielewicz, R. Lacey, W.G. Lynch, Science 298 (2002) 1592

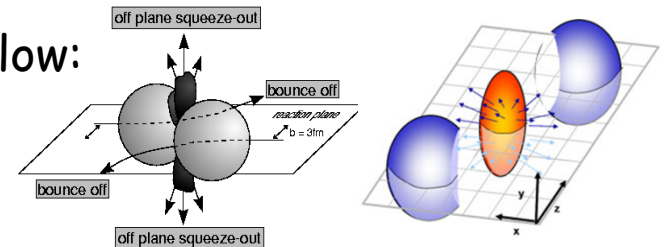


Transverse in-plane flow:

$$F = d(p_x/A)/d(y/y_{cm})$$

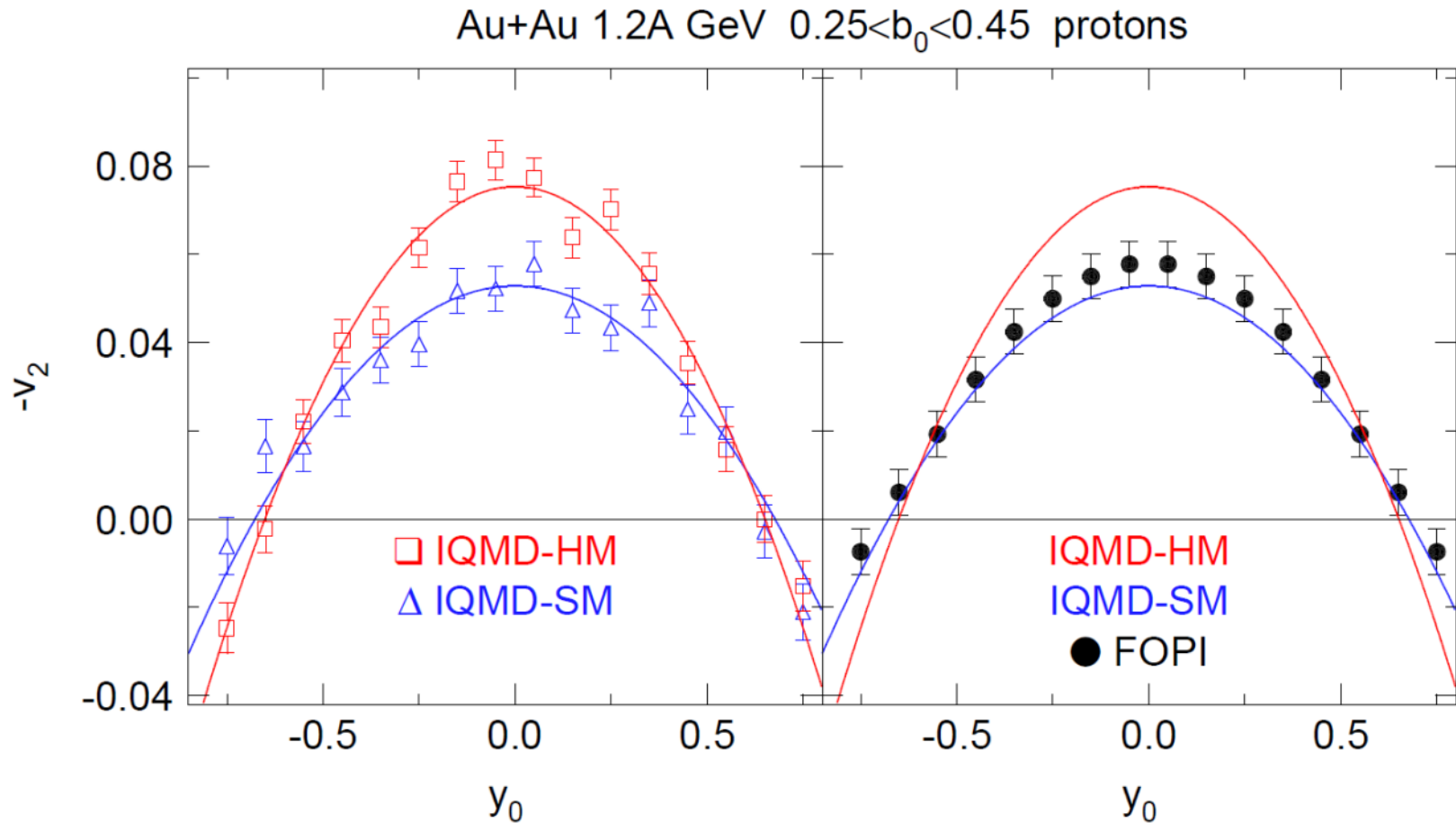


Elliptic flow:



$$dN/d\Phi \propto (1 + 2v_1 \cos\Phi + 2v_2 \cos 2\Phi)$$

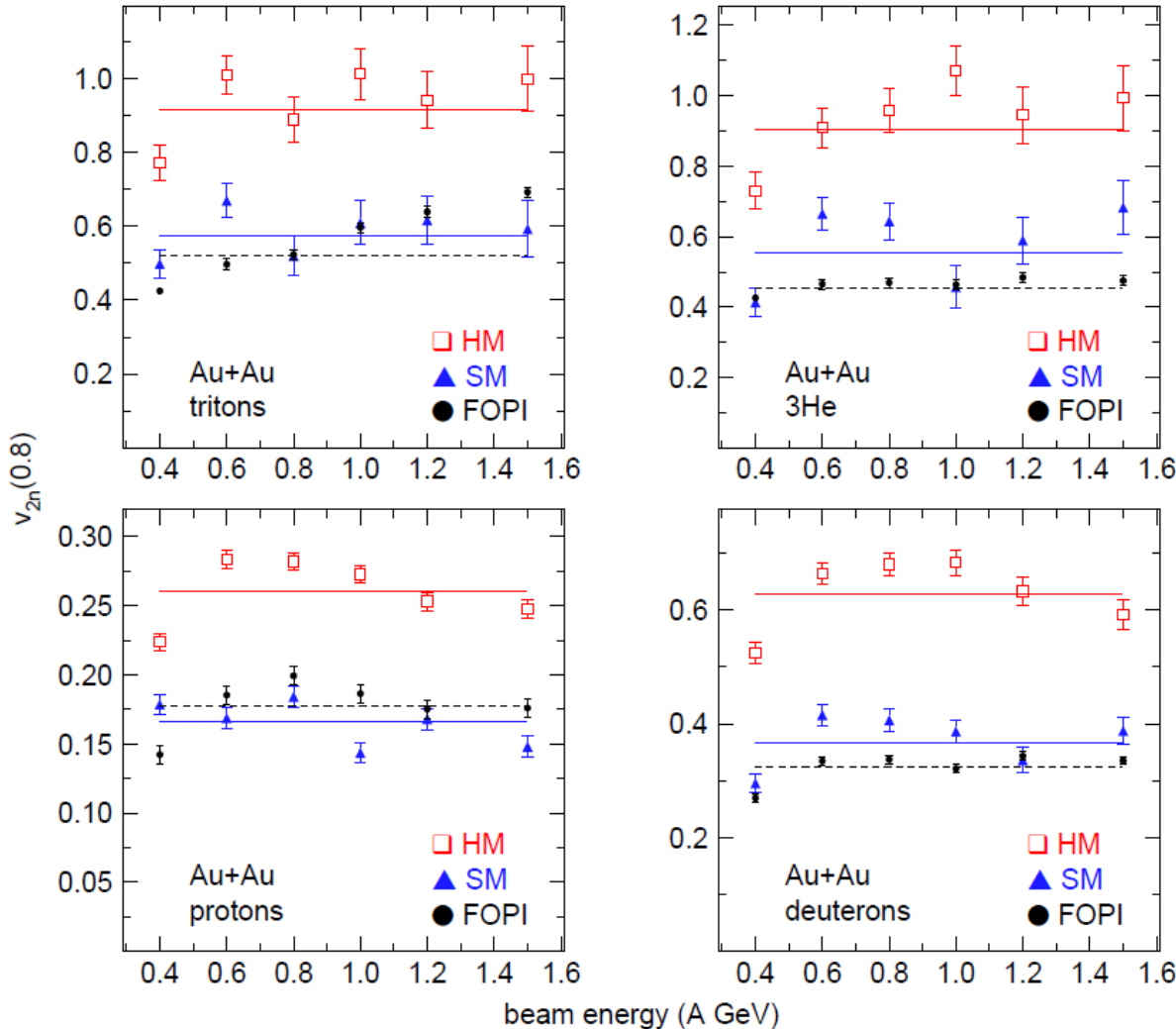
# EOS from proton elliptic flow in Au+Au collisions at 1.2A GeV



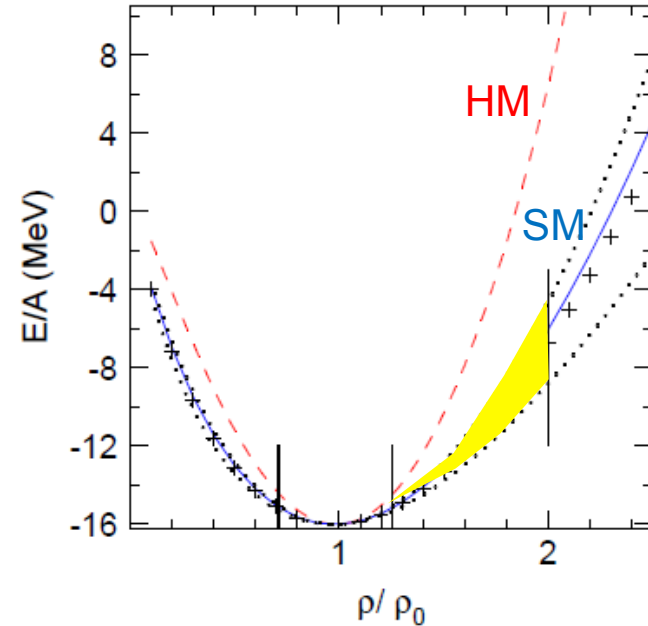
# EOS from the elliptic flow of fragments in Au+Au collisions at SIS18 energies ( $\rho < 3\rho_0$ )

A. Le Fevre , Y Leifels, W. Reisdorf, J. Aichelin, Ch. Hartnack, Nucl. Phys. A945 (2016) 112

$0.25 < b_0 < 0.45$   $u_{t0} > 0.4$



HM/SM/FOPI



HM:  $K = 380$  MeV  
SM:  $K = 200$  MeV

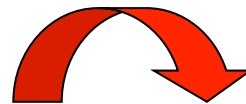
# Collective flow in Au+Au collisions and the EOS of symmetric nuclear matter

Beam energy A GeV	central density	flow observable	incompressibility K
0.4 – 1.5	$\rho = 1 - 3 \rho_0$	$v_2$ of p, d, t, 3He	$\approx 200$ MeV
2 – 10	$\rho = 3 - 7 \rho_0$	$v_1$ of protons	$\approx 200$ MeV
2 – 10	$\rho = 3 - 7 \rho_0$	$v_2$ of protons	$\approx 300$ MeV

Within microscopic transport models the collective flow is sensitive to:

- The nuclear matter equation of state
- In-medium nucleon-nucleon cross sections
- Momentum dependent interactions

Independent observables?

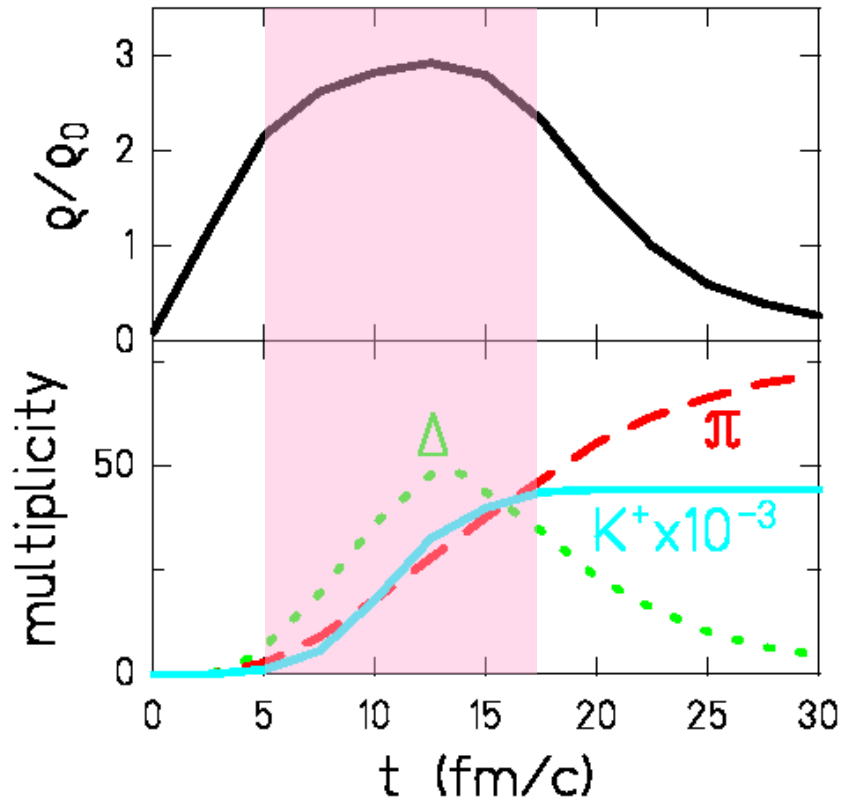


particle production

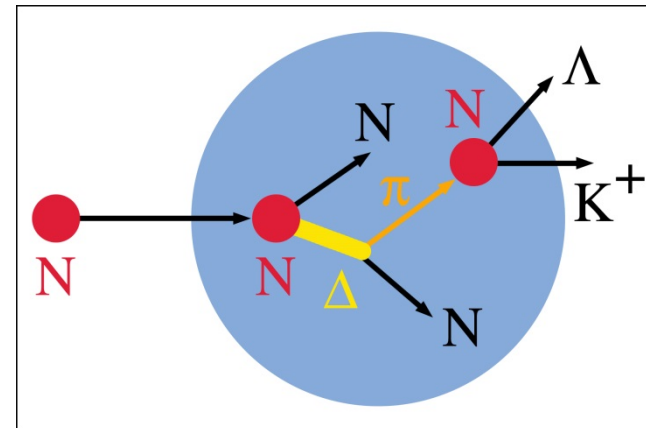


# Probing the nuclear equation-of-state ( $\rho = 1 - 3 \rho_0$ ) by $K^+$ meson subthreshold production in HI collisions

RBUU: Au+Au 1 AGeV,  $b=0$  fm



Threshold reached by piling up energy in sequential collisions which are enhanced with increasing density



# Probing the nuclear equation-of-state ( $\rho = 1 - 3 \rho_0$ ) by $K^+$ meson production in C+C and Au+Au collisions

**Idea:**  $K^+$  yield  $\propto$  baryon density  $\propto$  compressibility

Transport model (RBUU)

**Au+Au at 1 AGeV:**

$\kappa = 200 \text{ MeV} \Rightarrow \rho_{\text{max}} \approx 2.9 \rho_0 \Rightarrow K^+ \nearrow$

$\kappa = 380 \text{ MeV} \Rightarrow \rho_{\text{max}} \approx 2.4 \rho_0 \Rightarrow K^+ \searrow$

**Reference system C+C:**

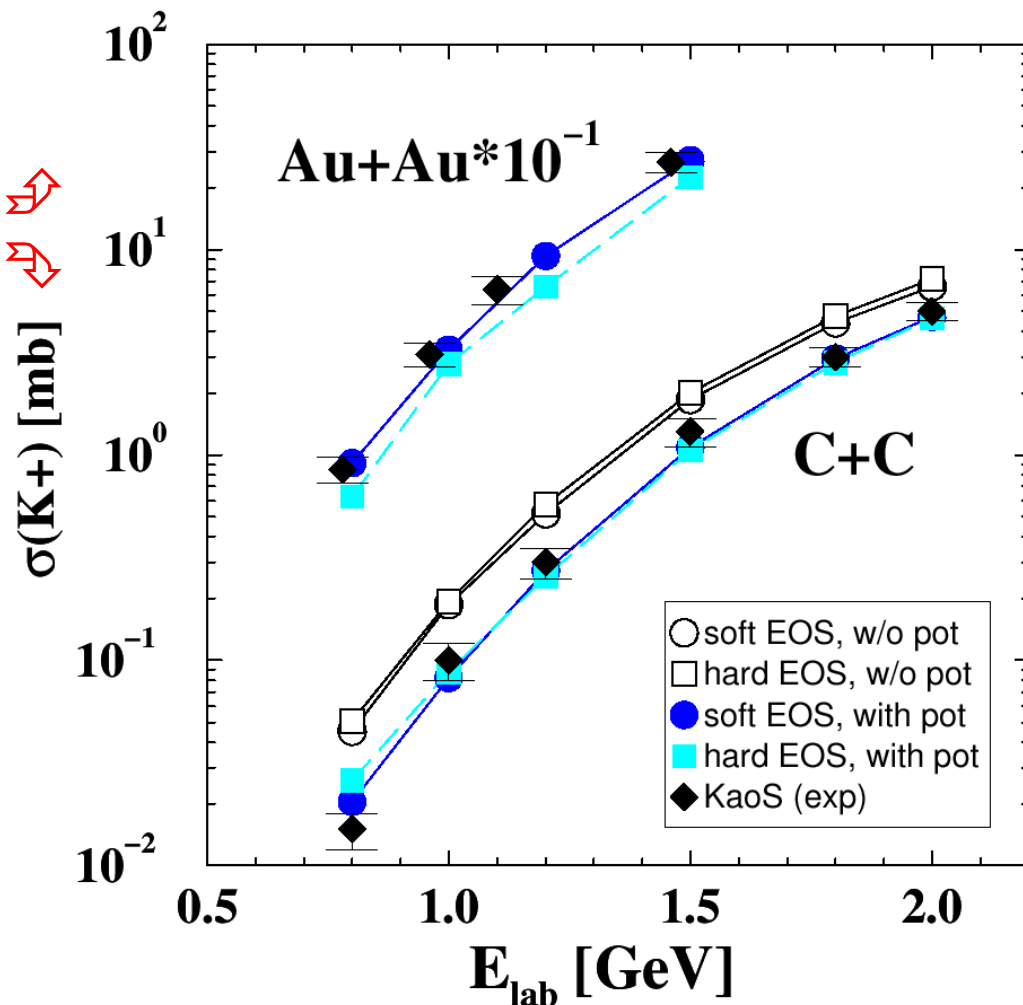
$K^+$  yield not sensitive to EOS

Experiment:

C. Sturm et al., (KaoS Collaboration),  
Phys. Rev. Lett. 86 (2001) 39

Theory:

Ch. Fuchs et al.,  
Phys. Rev. Lett. 86 (2001) 1974

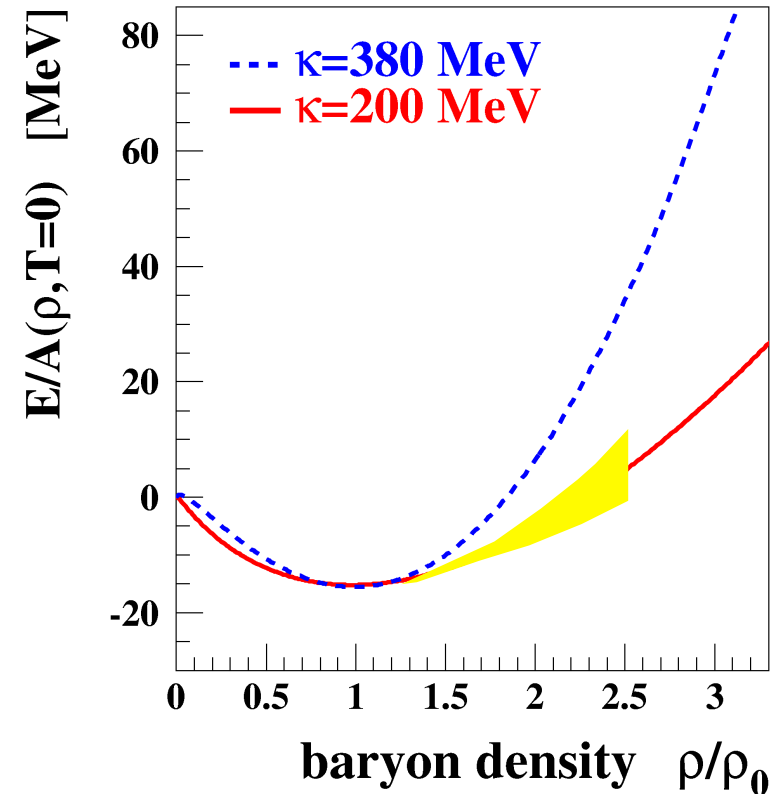
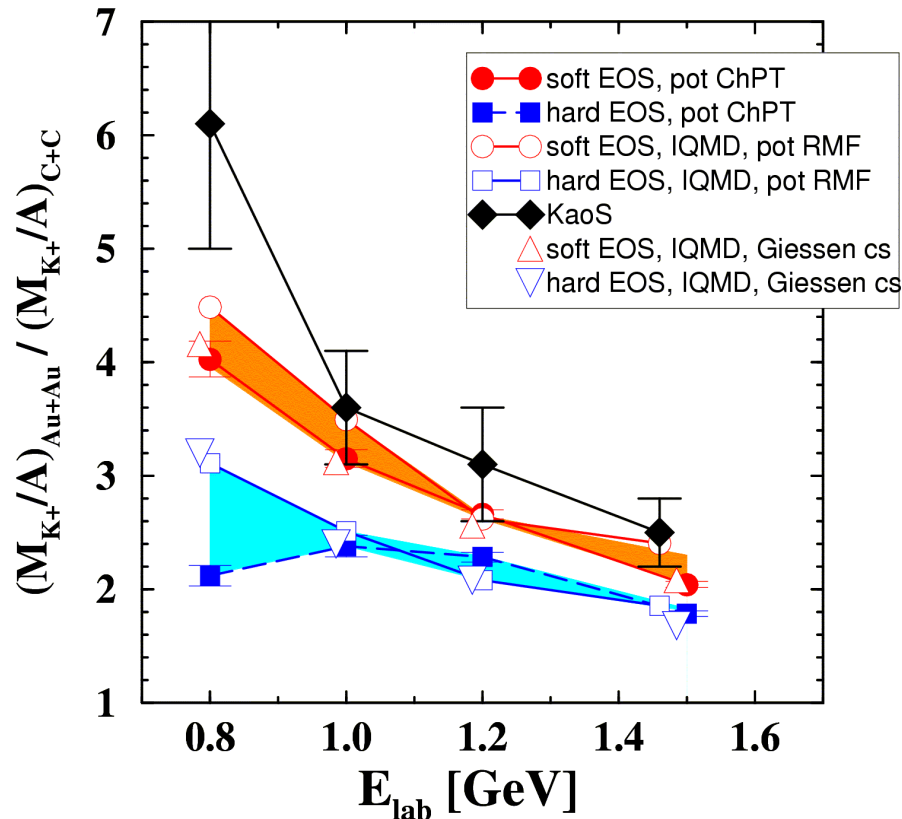


# The compressibility of (symmetric) nuclear matter

Experiment: C. Sturm et al., (KaoS Collaboration) Phys. Rev. Lett. 86 (2001) 39

Theory: QMD Ch. Fuchs et al., Phys. Rev. Lett. 86 (2001) 1974

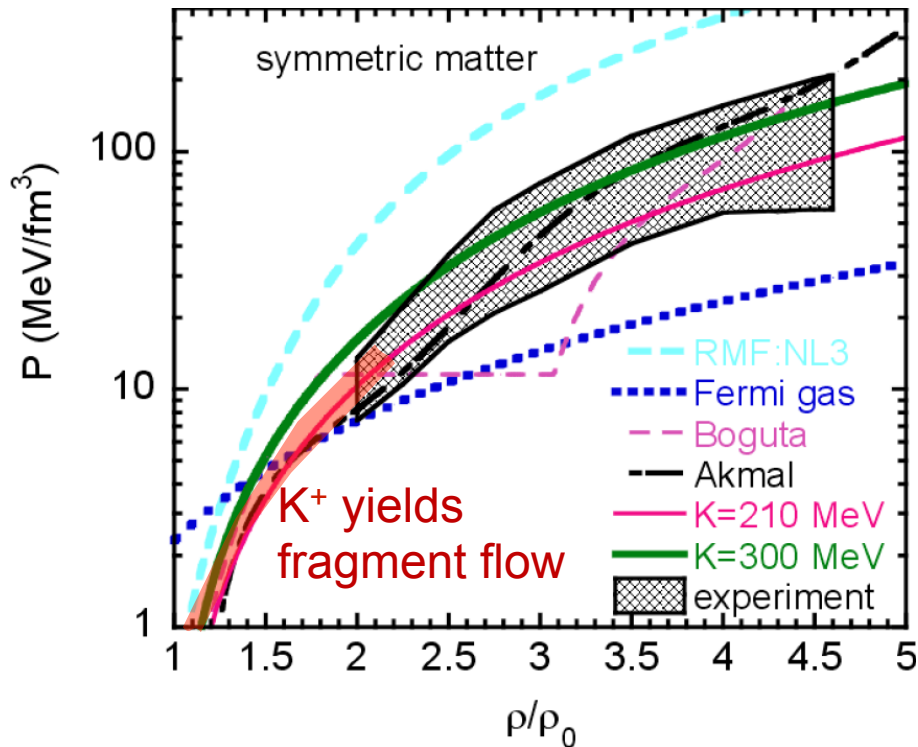
IQMD Ch. Hartnack, J. Aichelin, J. Phys. G 28 (2002) 1649



Au/C ratio: cancellation of systematic errors both in experiment and theory

Soft equation-of-state:  $\kappa \leq 200$  MeV  
Confirmation of flow measurements

# Nuclear incompressibility from heavy-ion collisions



hard EoS  
soft EoS

EoS at  $\rho \geq 3 \rho_0$  ?

Collective flow of protons:

P. Danielewicz, R. Lacey, W.G. Lynch,  
Science 298 (2002) 1592

Collective flow of protons and light fragments

A.Le Fevre et. al., Nucl. Phys. A945 (2016) 112

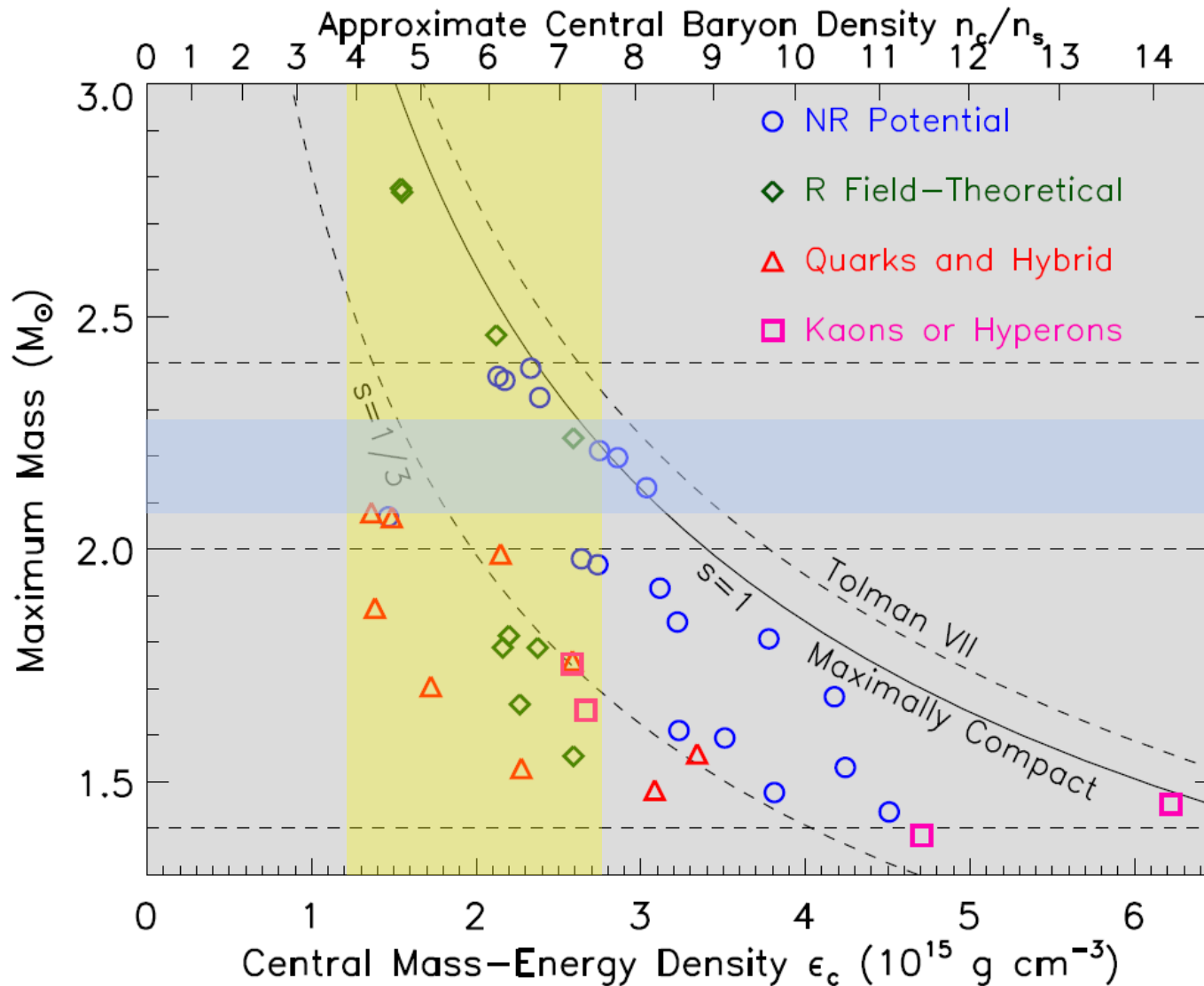
Kaon yields

C. Sturm et al., (KaoS Collab.) PRL 86 (2001) 39

C. Fuchs PRL 86 (2001) 1974



# Mass-density relation of neutron stars for different EOS



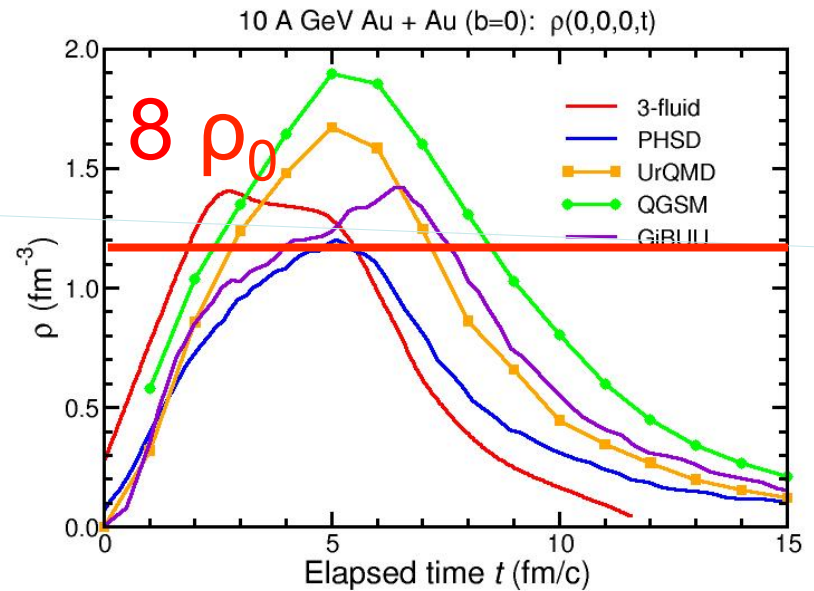
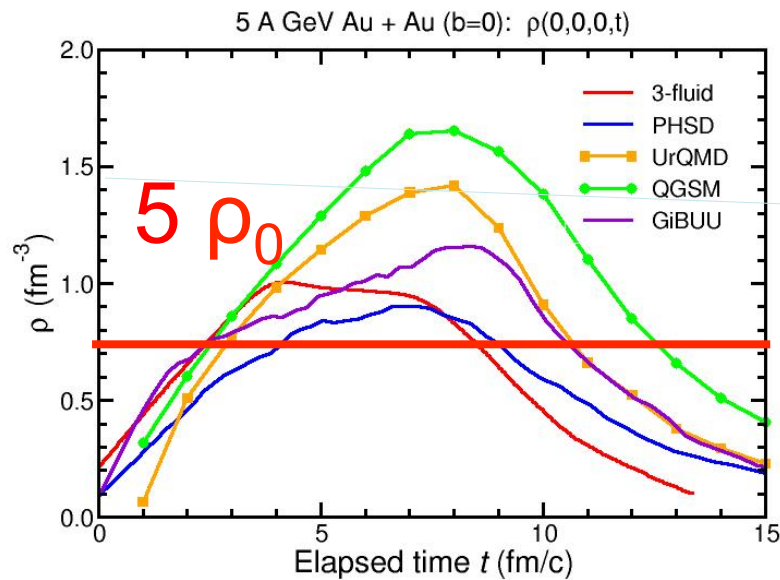
PSR J0740+6620  
 $M = 2.17 \pm 0.11 M_{\text{sun}}$   
 H. Cromartie et al.,  
 arXiv:1904.06759 (2019)

# Baryon densities in central Au+Au collisions

I.C. Arsene et al., Phys. Rev. C 75, 24902 (2007)

## 5 A GeV

## 10 A GeV



# Future attempts to study the high-density EOS

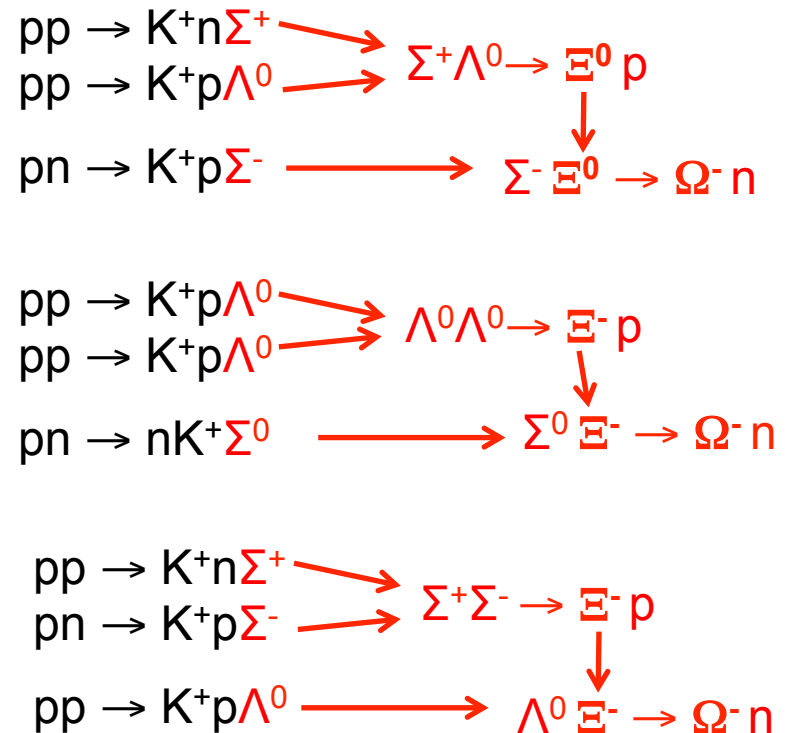
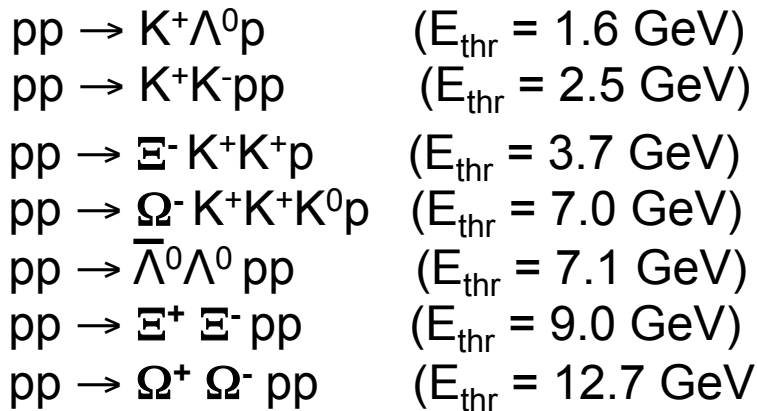
- Systematic studies of collective flow of baryons
- Threshold production of multi-strange hyperons

Idea:

$\Xi$  and  $\Omega$  yield at subthreshold energies  $\sim$  multi-step collisions  $\sim$  density  $\rightarrow$  EOS

## Hyperon production via multiple collisions

### Strangeness production:



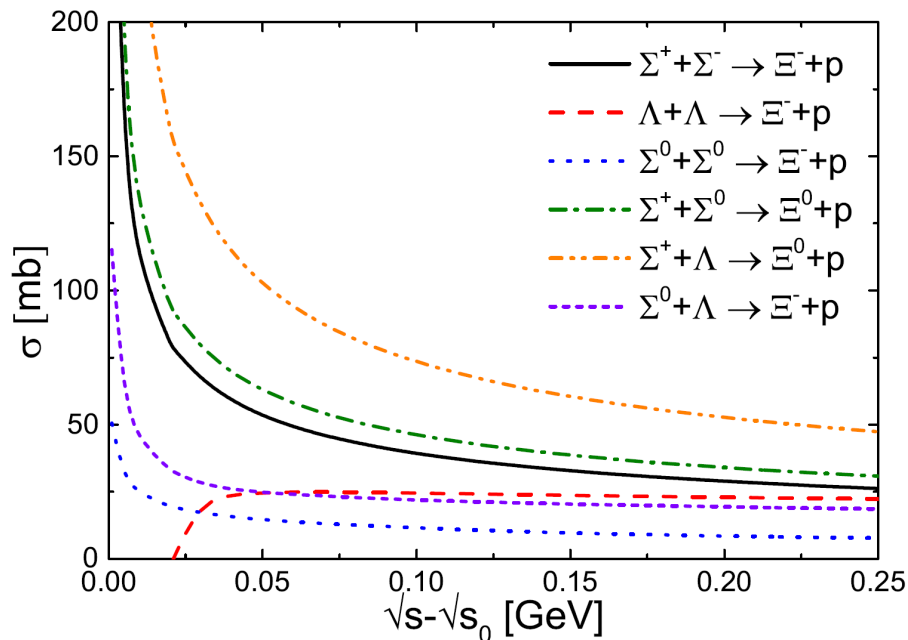
# Future attempts to study the high-density EOS

- Systematic studies of collective flow of baryons
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Idea:

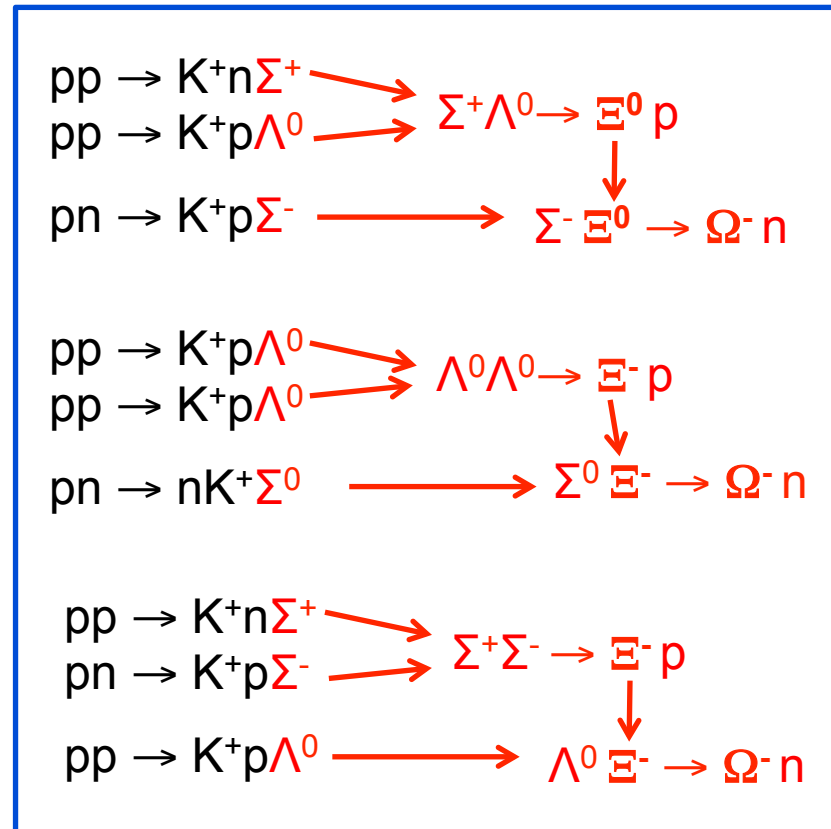
$\Xi$  and  $\Omega$  yield at subthreshold energies  $\sim$  multi-step collisions  $\sim$  density  $\rightarrow$  EOS

Isospin-dependent strangeness-exchange cross sections in UrQMD



G. Graef, J. Steinheimer, F. Li, M. Bleicher,  
Phys. Rev. C 90, 064909 (2014)

Hyperon production via multiple collisions





# Future attempts to study the high-density EOS

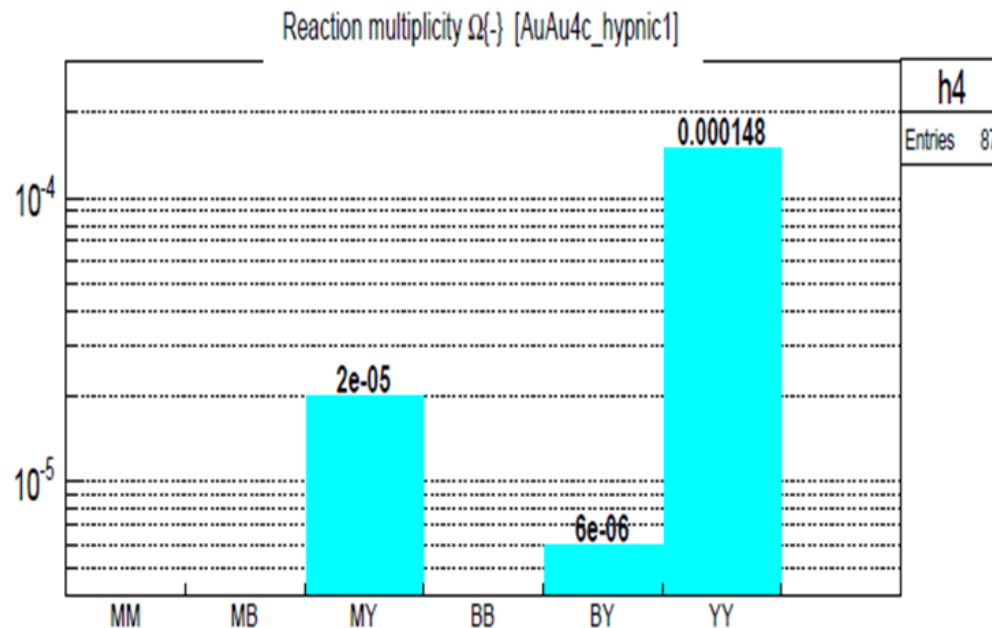
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Idea:

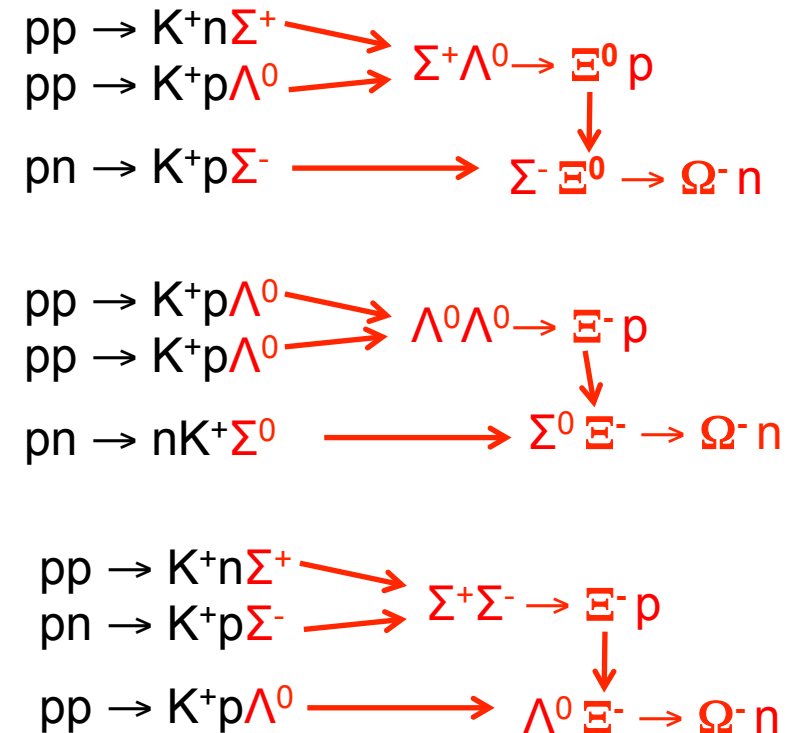
$\Xi$  and  $\Omega$  yield at subthreshold energies  $\sim$  multi-step collisions  $\sim$  density  $\rightarrow$  EOS

Hyperon production via multiple collisions

$\Omega^-$  production in 4 A GeV Au+Au

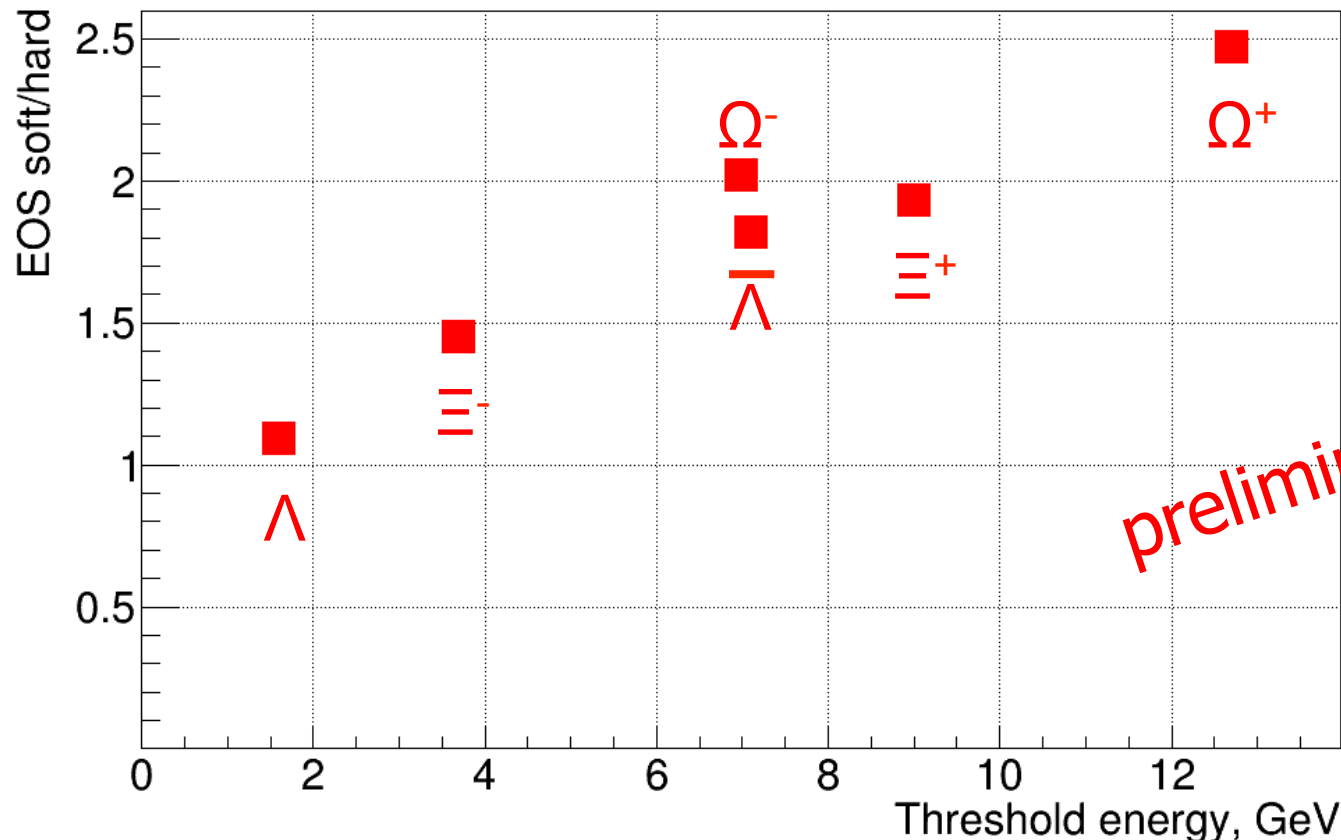


HYPQGSM calculations, K. Gudima et al.



# Multi-strange hyperons: promising observables for the EOS of symmetric matter

6 M central Au+Au collisions at 4A GeV  
soft EOS (K=240 MeV) / hard EOS (K=350) MeV



preliminary !

# The nuclear symmetry energy

$$E_A(\rho, \delta) = E_A(\rho, 0) + E_{\text{sym}}(\rho) \cdot \delta^2$$

$$E_{\text{sym}}(\rho) = E_{\text{sym}}(\rho_0) + \frac{L}{3} \left( \frac{\rho - \rho_0}{\rho_0} \right) + \frac{K_{\text{sym}}}{18} \left( \frac{\rho - \rho_0}{\rho_0} \right)^2$$

Empirical value  $E_{\text{sym}}(\rho_0) \approx 30 \text{ MeV}$

slope 
$$L = 3\rho_0 \left. \frac{\partial E_{\text{sym}}(\rho)}{\partial \rho} \right|_{\rho=\rho_0}$$

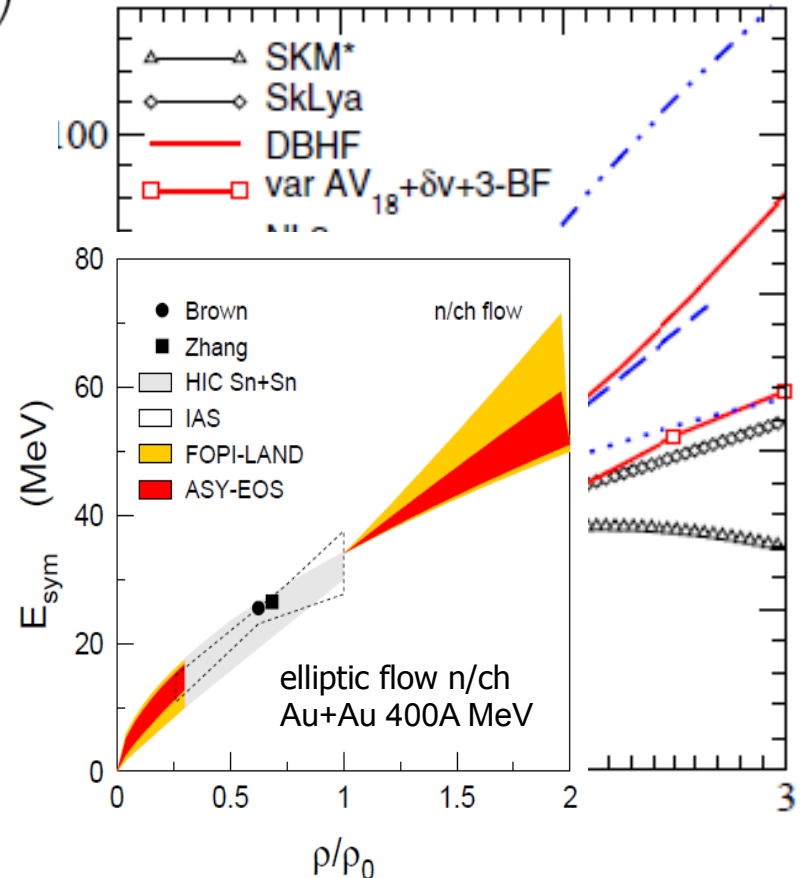
theoretical value  $L(\rho_0) \approx 60 \text{ MeV}$

B.A. Li and X. Han, Phys. Lett. B 727 (2013) 276

curvature 
$$K_{\text{sym}} = 9\rho_0^2 \left. \frac{\partial^2 E_{\text{sym}}(\rho)}{\partial^2 \rho} \right|_{\rho=\rho_0}$$

theoretical value  $K_{\text{sym}} = -700 \text{ to } 470 \text{ MeV}$

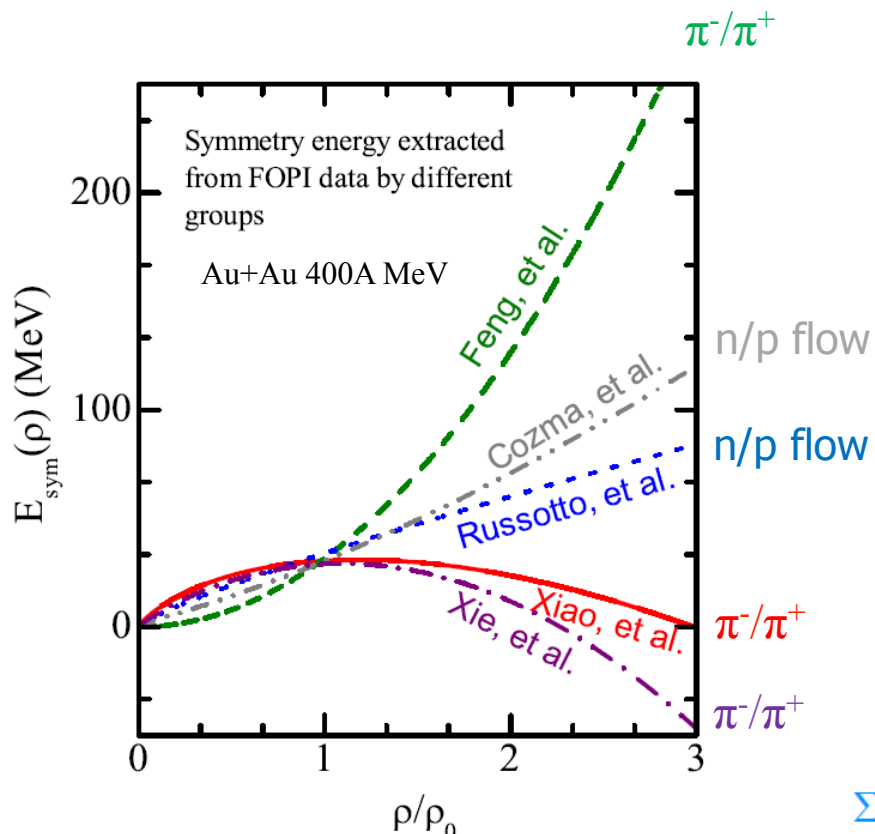
Ch. Fuchs and H.H. Wolter, EPJA30 (2006) 5



P. Russotto et al., Phys. Rev. C 94, 034608 (2016)

# The symmetry energy $E_{\text{sym}}$ at high density

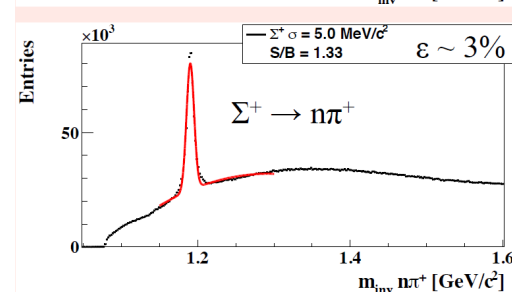
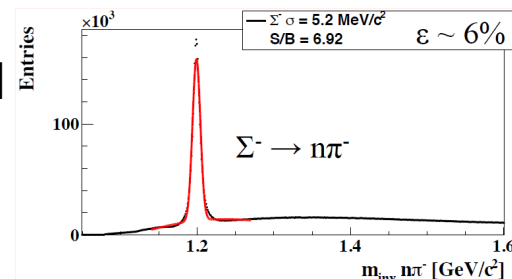
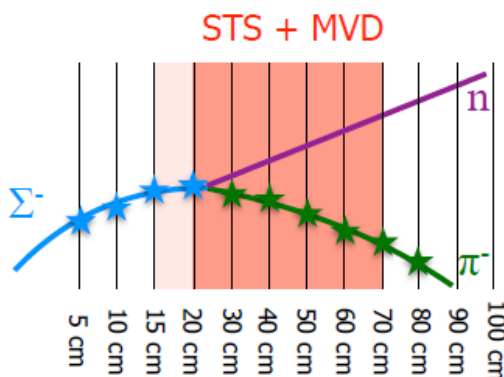
- Elliptic flow neutrons/protons
- Particles with opposite isospin ?
- **Flow of  $\Sigma^+$  and  $\Sigma^-$  ?**



W.-M. Guo et al., Phys. Lett. B738 (2014) 397

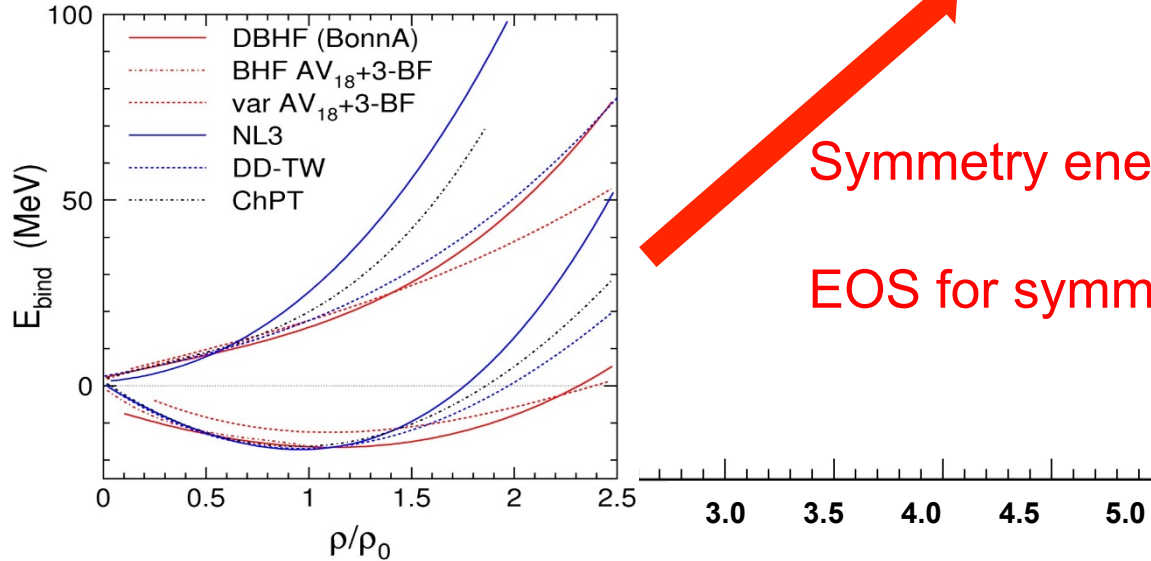
$I_3$	particle	production	$E_{\text{thr}}$ GeV	decay
+1	$\Sigma^+(uus)$	$pp \rightarrow \Sigma^+K^+n$ $pp \rightarrow \Sigma^+K^0p$ $pn \rightarrow \Sigma^+K^0n$	1.8	$\Sigma^+ \rightarrow p\pi^0$ $\Sigma^+ \rightarrow n\pi^+$
-1	$\Sigma^-(dds)$	$pn \rightarrow \Sigma^-K^+p$ $nn \rightarrow \Sigma^-K^+n$	1.8	$\Sigma^- \rightarrow n\pi^-$

## Missing mass method



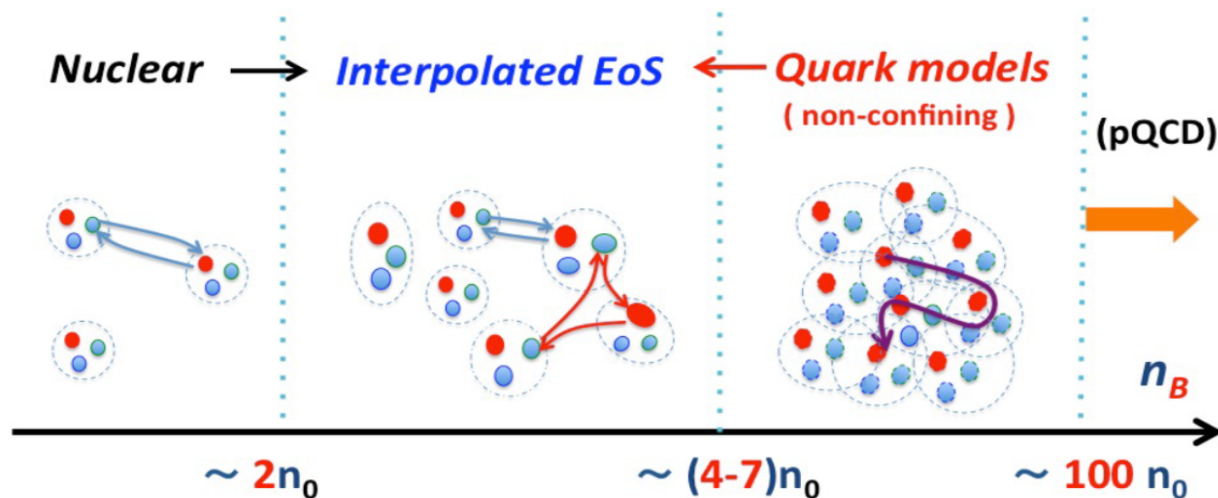


# Properties of nuclear matter at neutron star core densities



Symmetry energy ?

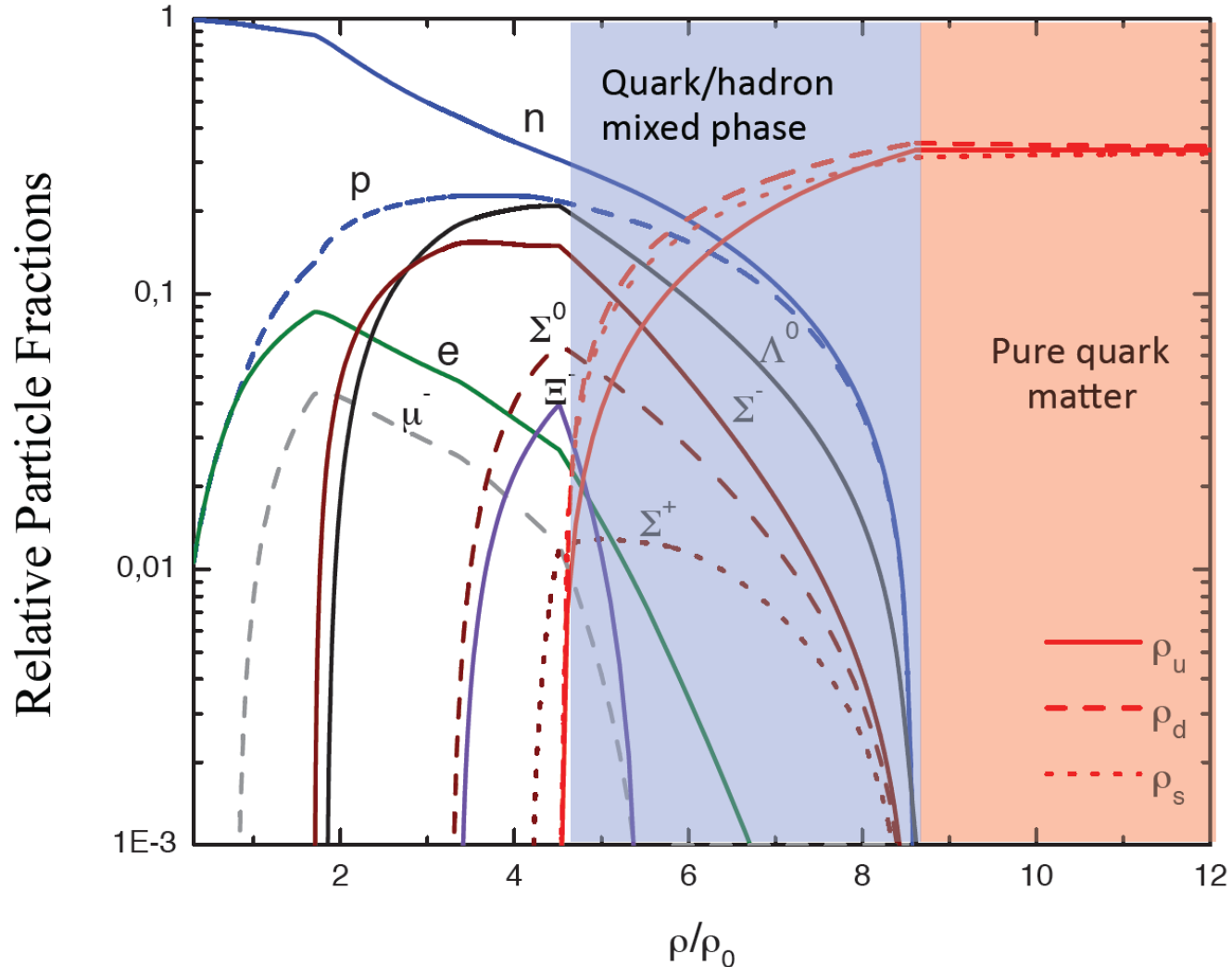
EOS for symmetric matter?



Courtesy of T. Kojo

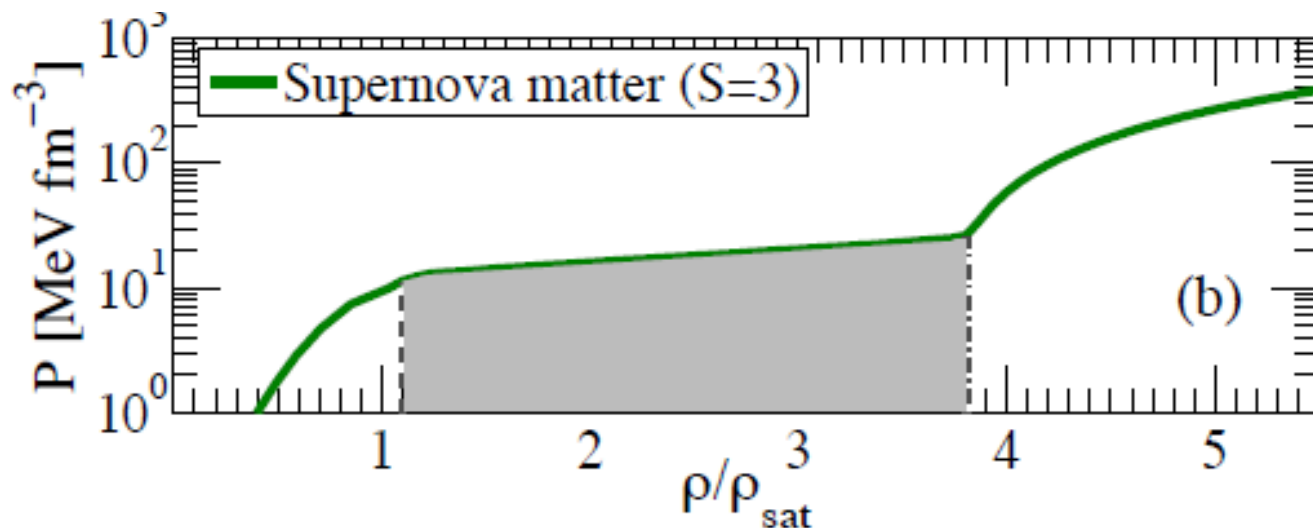
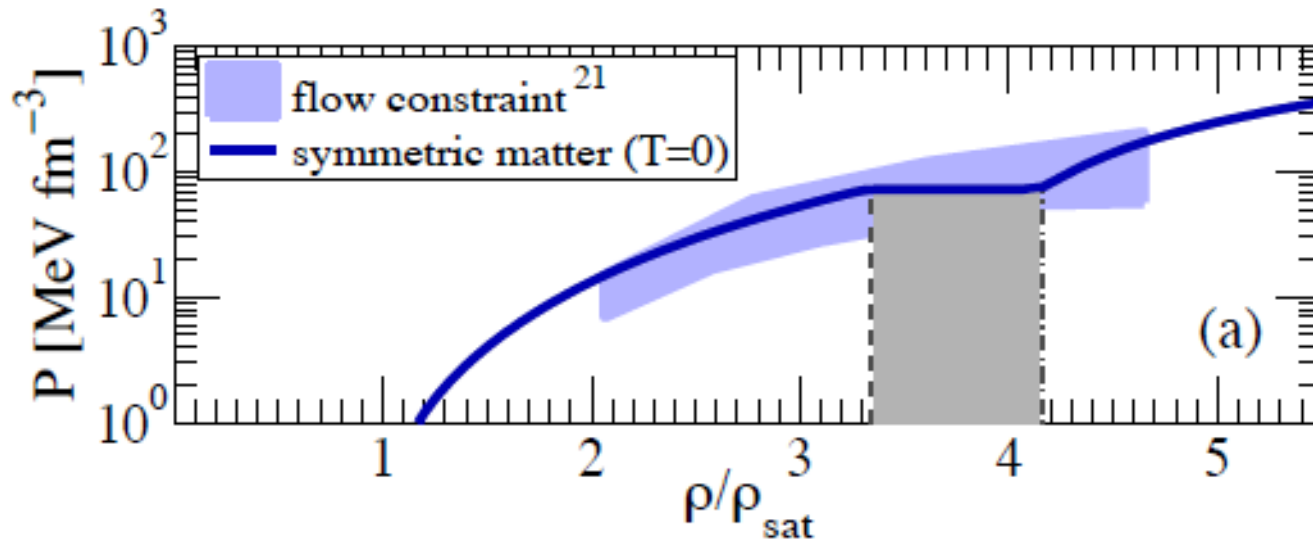
# Degrees-of-freedom at high density?

M. Orsaria, H. Rodrigues, F. Weber, G.A. Contrera, arXiv:1308.1657  
Phys. Rev. C 89, 015806, 2014 (SU(3)-NJL model calculations)

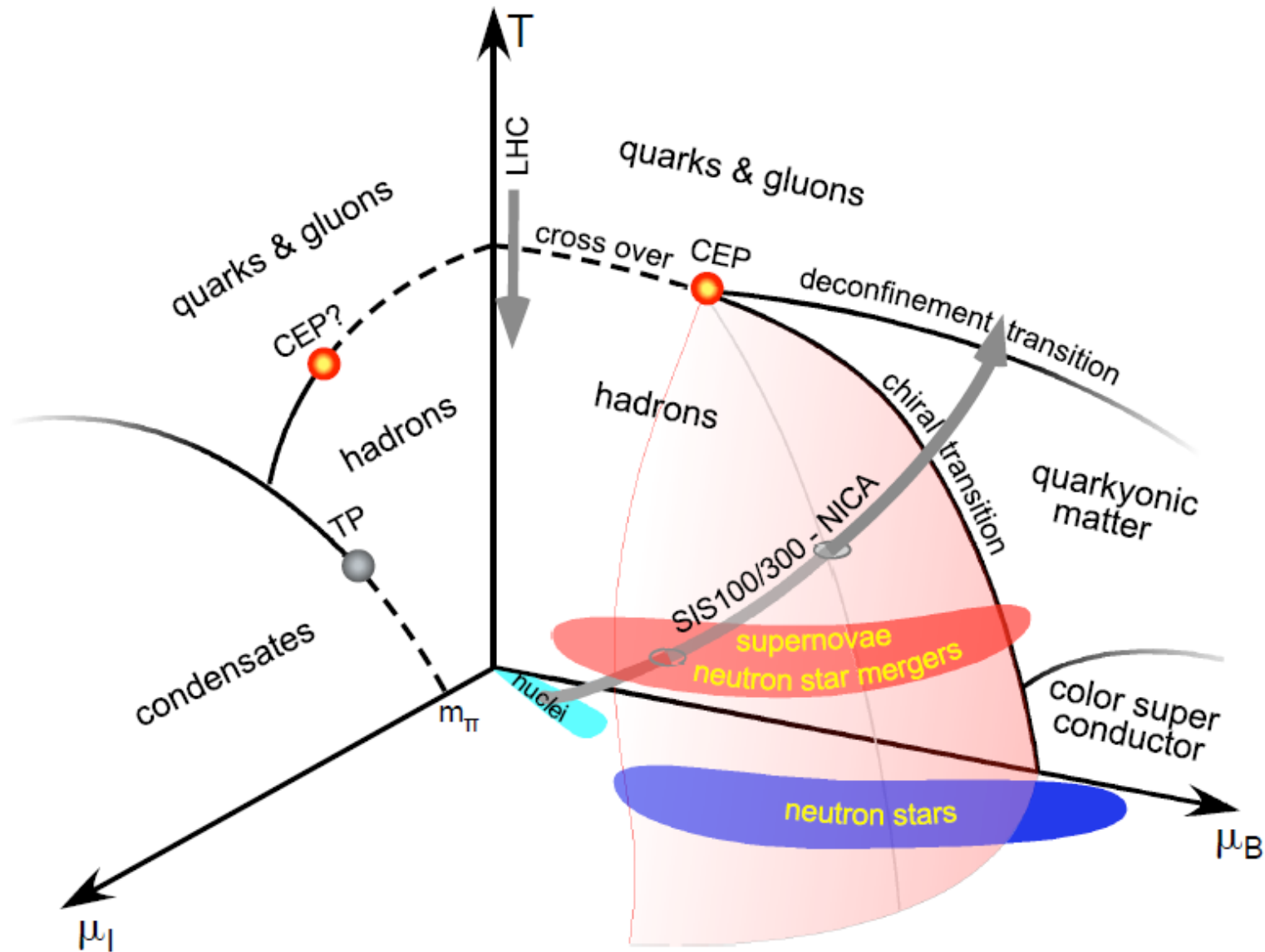


# EOS with phase transition

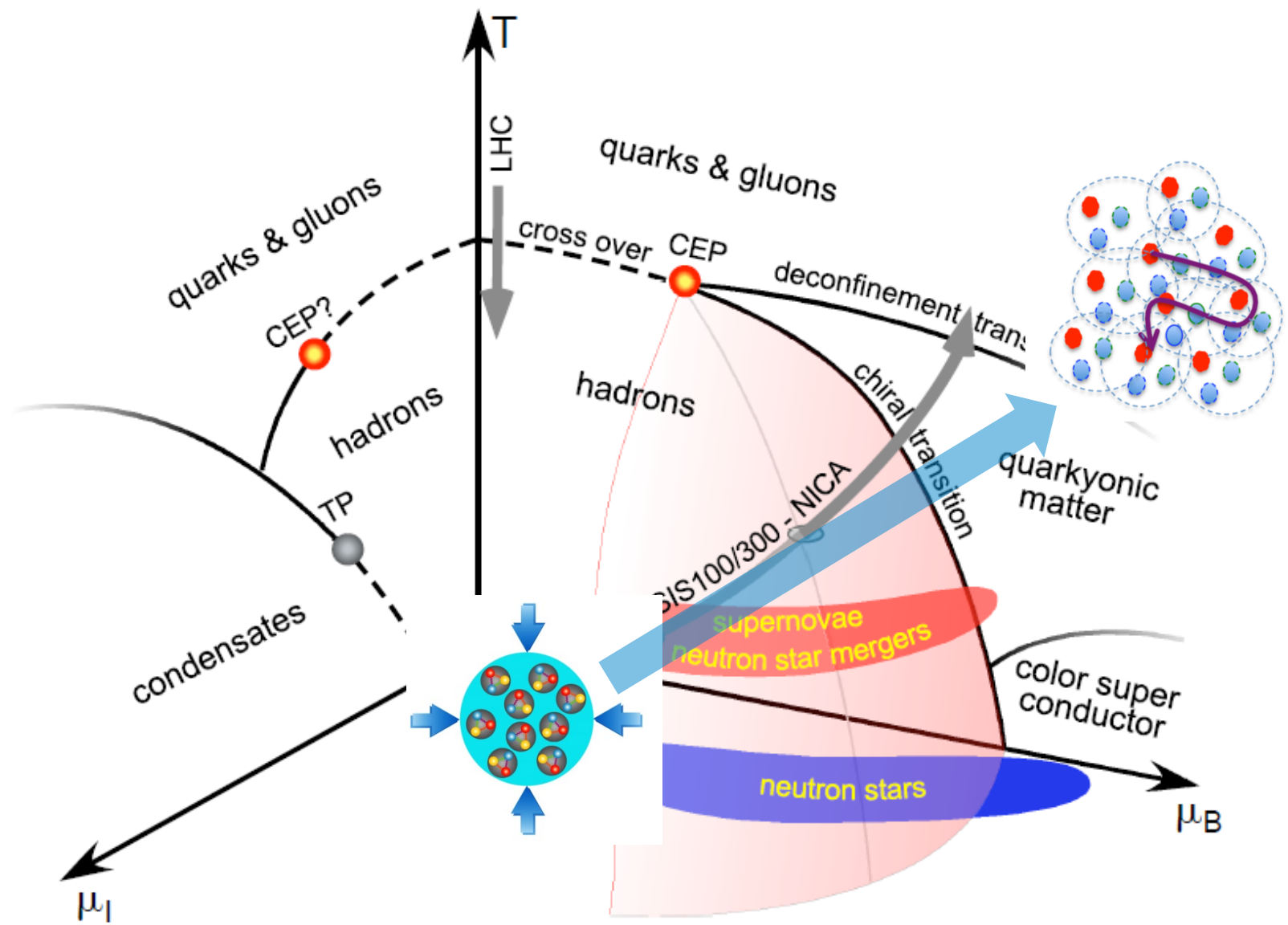
T. Fischer, N. Bastian, M. Wu, S. Typel, T. Klähn, D. Blaschke,  
Nature Astronomy (2018), DOI: 10.1038/s41550-018-0583-0, arXiv:1712.08788v2  
Quark deconfinement as supernova explosion engine for massive blue-supergiant stars



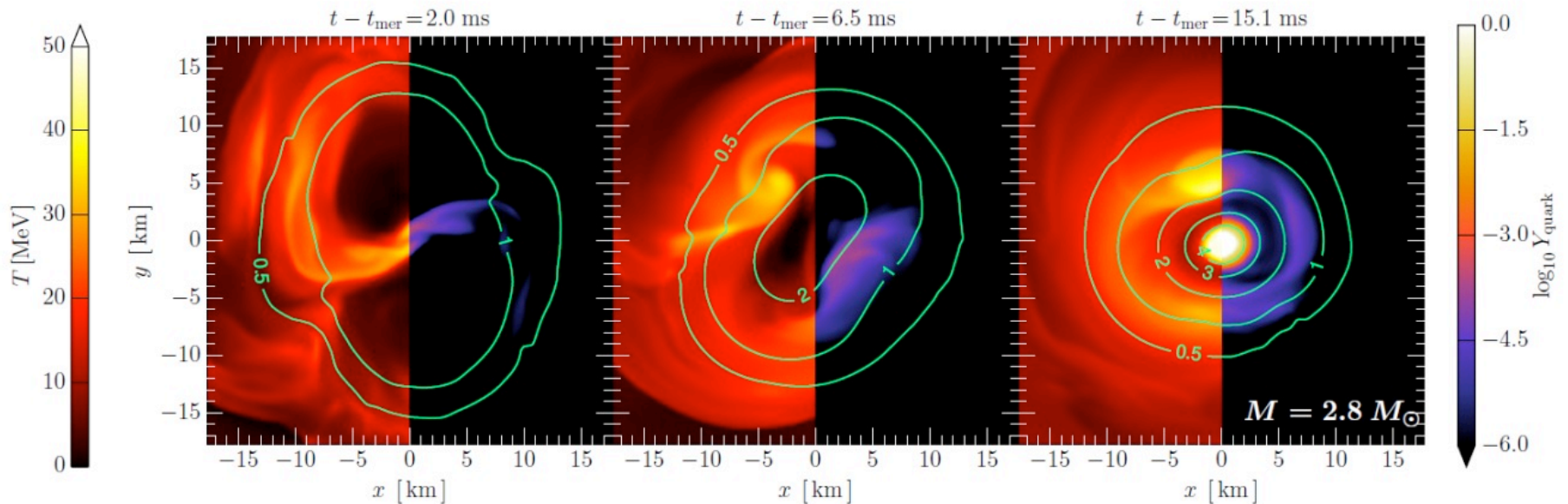
# Exploring the QCD phase diagram



# Exploring the QCD phase diagram



# Quark-hadron phase transitions in general-relativistic neutron-star mergers ?



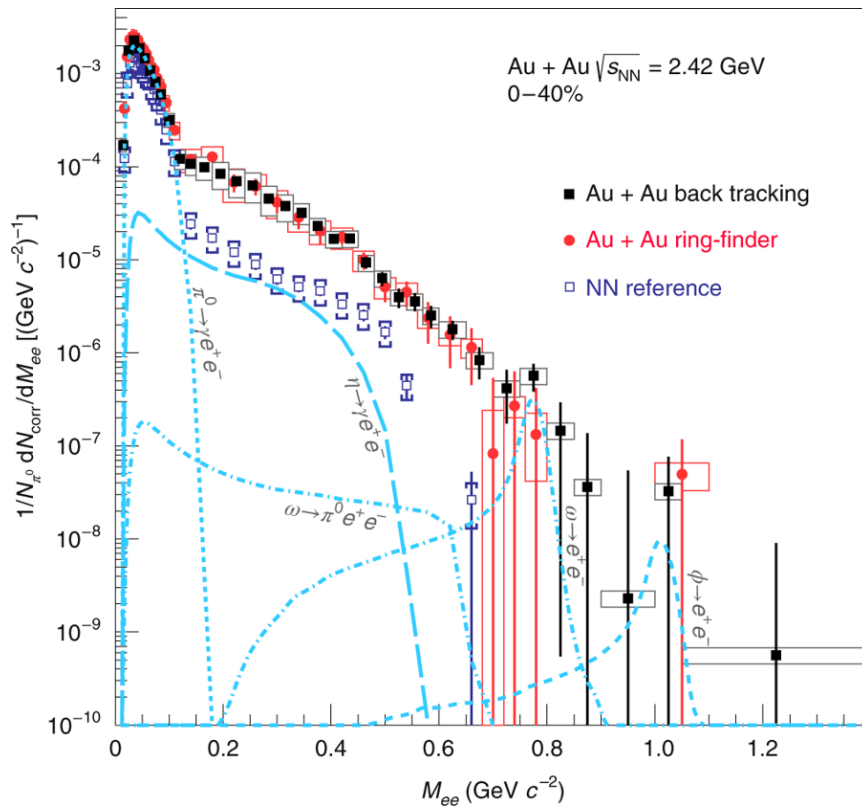
E. Most et al., (... M Hanauske, L. Rezzola), Phys. Rev. Lett. 122, 061101 (2019)

Transition from hadronic matter to quark matter  
at  $\rho > 4 \rho_0$  and  $T > 50$  MeV ?

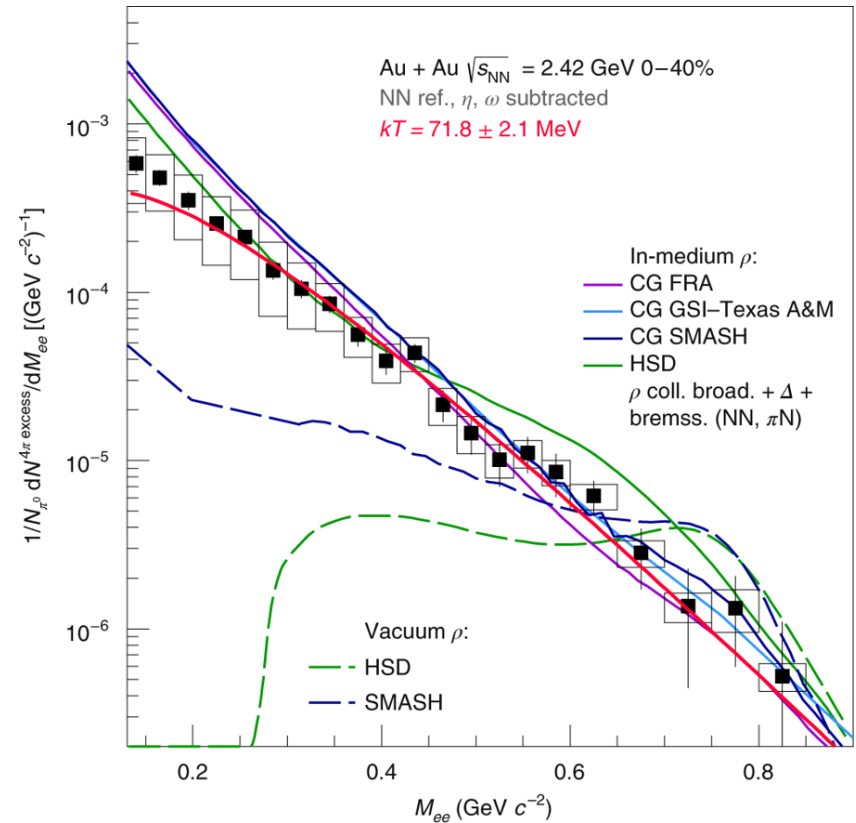
# Thermal radiation from dense QCD matter

Au+Au collisions at 1.25 A GeV:  $\rho \leq 2.5 \rho_0$ ,  $T \approx 72$  MeV

Di-electron yield



Di-electron excess yield after subtraction of vector mesons

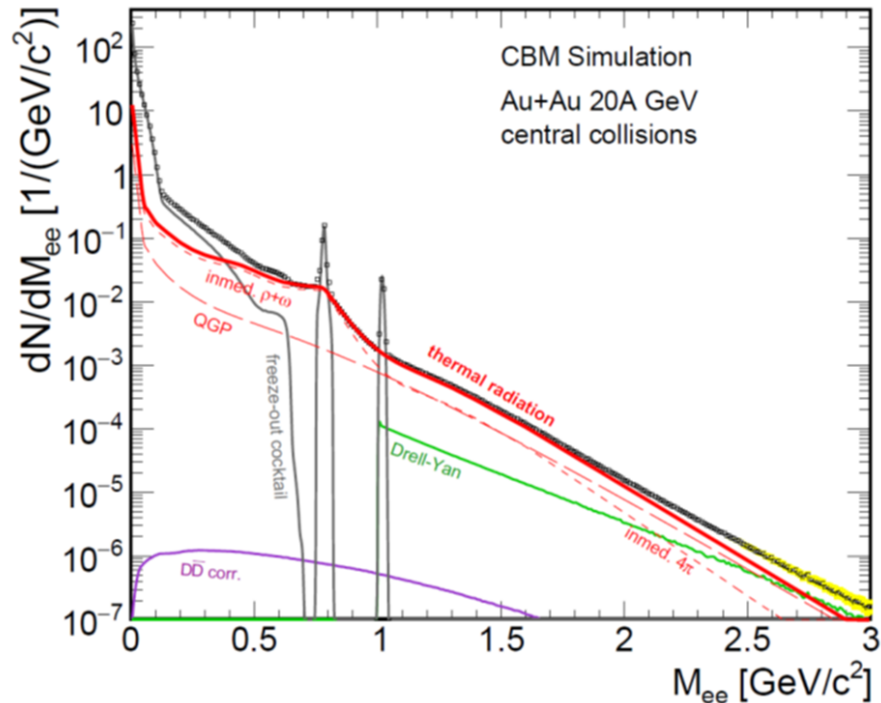




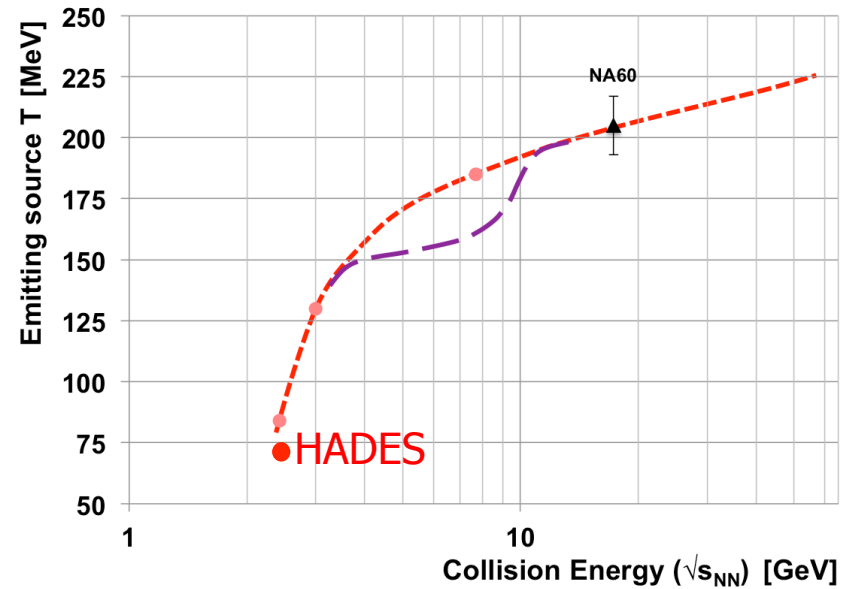
# Experimental indication for a phase transition at large $\mu_B$ ?

Invariant mass ( $M_{inv} > 1 \text{ GeV}/c^2$ ) of lepton pairs as function of beam energy  $\rightarrow$  thermal radiation from fireball  $\rightarrow$  caloric curve  $\rightarrow$  phase coexistence (1<sup>st</sup> order transition)

Invariant mass distribution of lepton pairs



Slope of dilepton invariant mass spectrum  
 $1 \text{ GeV}/c^2 < M_{inv} < 2.5 \text{ GeV}/c^2$



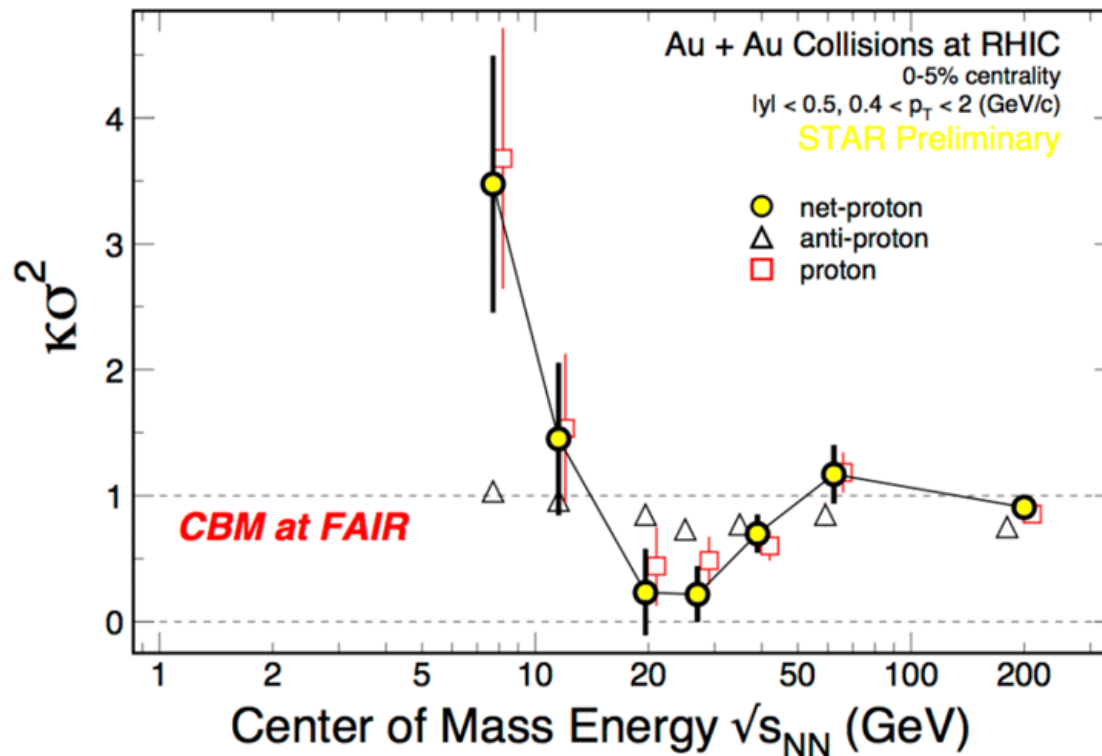
T. Ablasimov et al., (CBM Collaboration)  
Eur. Phys. J. A 53 (2017) 60

# Searching for the critical endpoint of the 1<sup>st</sup> order phase transition at SIS100 energies ?

“Critical opalescence”:

Event-by-event fluctuations of conserved quantities (B,S,Q)

4<sup>th</sup> moment of net-proton multiplicity distribution



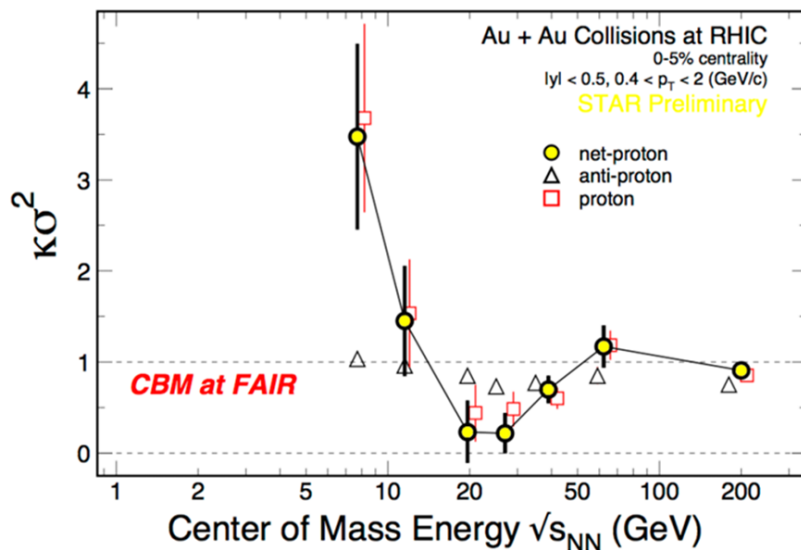
Data:  
STAR at RHIC  
beam energy scan

# Experimental indication for a phase transition at large $\mu_B$ ?

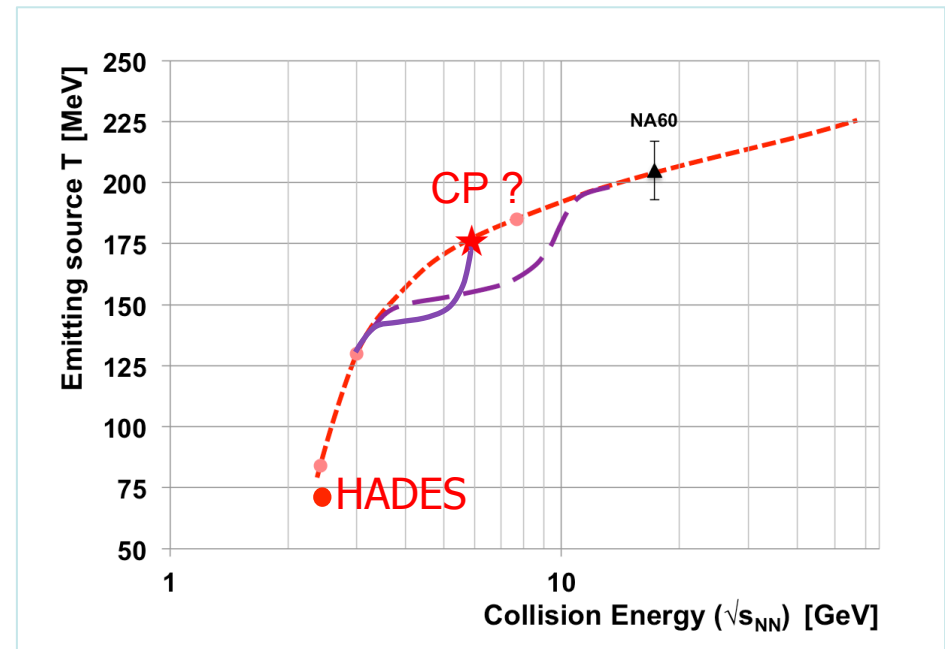
Required: consistent signatures from different observables

For example:

## Critical opalescence

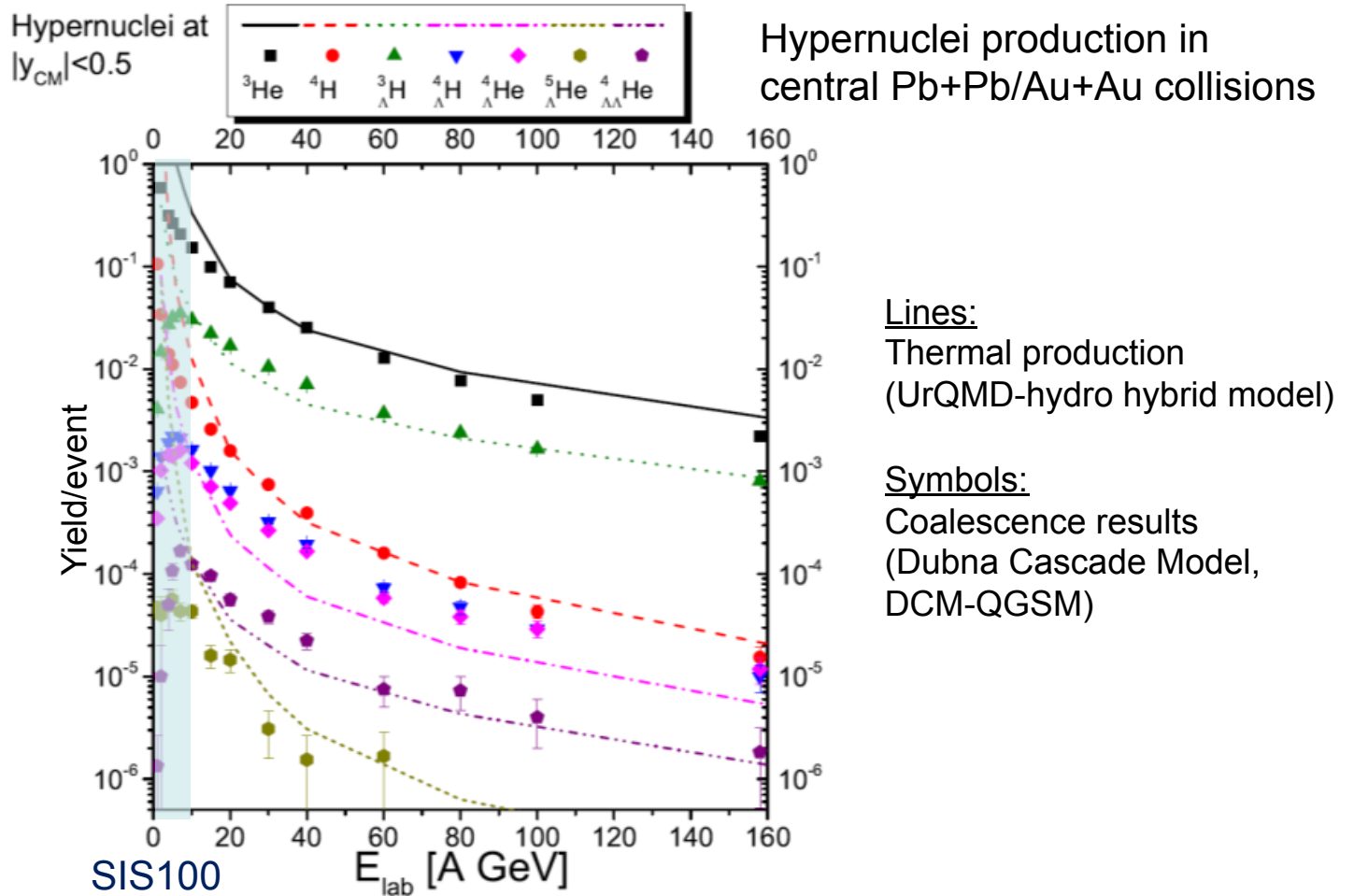


## Caloric curve



# Hyperons in neutron stars

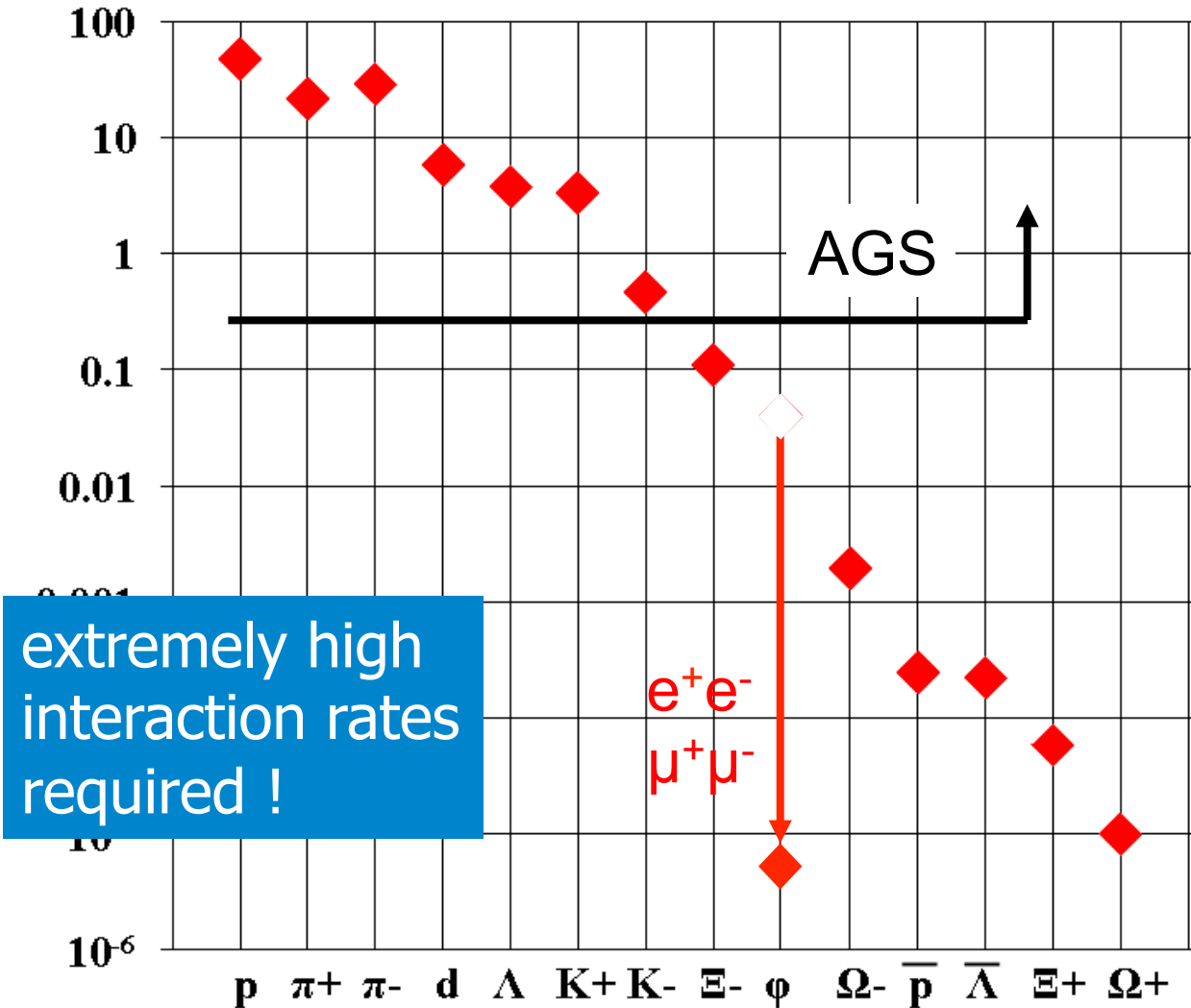
Study of  $\Lambda N$ ,  $\Lambda NN$ , and  $\Lambda\Lambda N$  interactions



# Experimental challenges

## Particle yields in central Au+Au 4 A GeV

Multiplicity Statistical model, A. Andronic, priv. com.



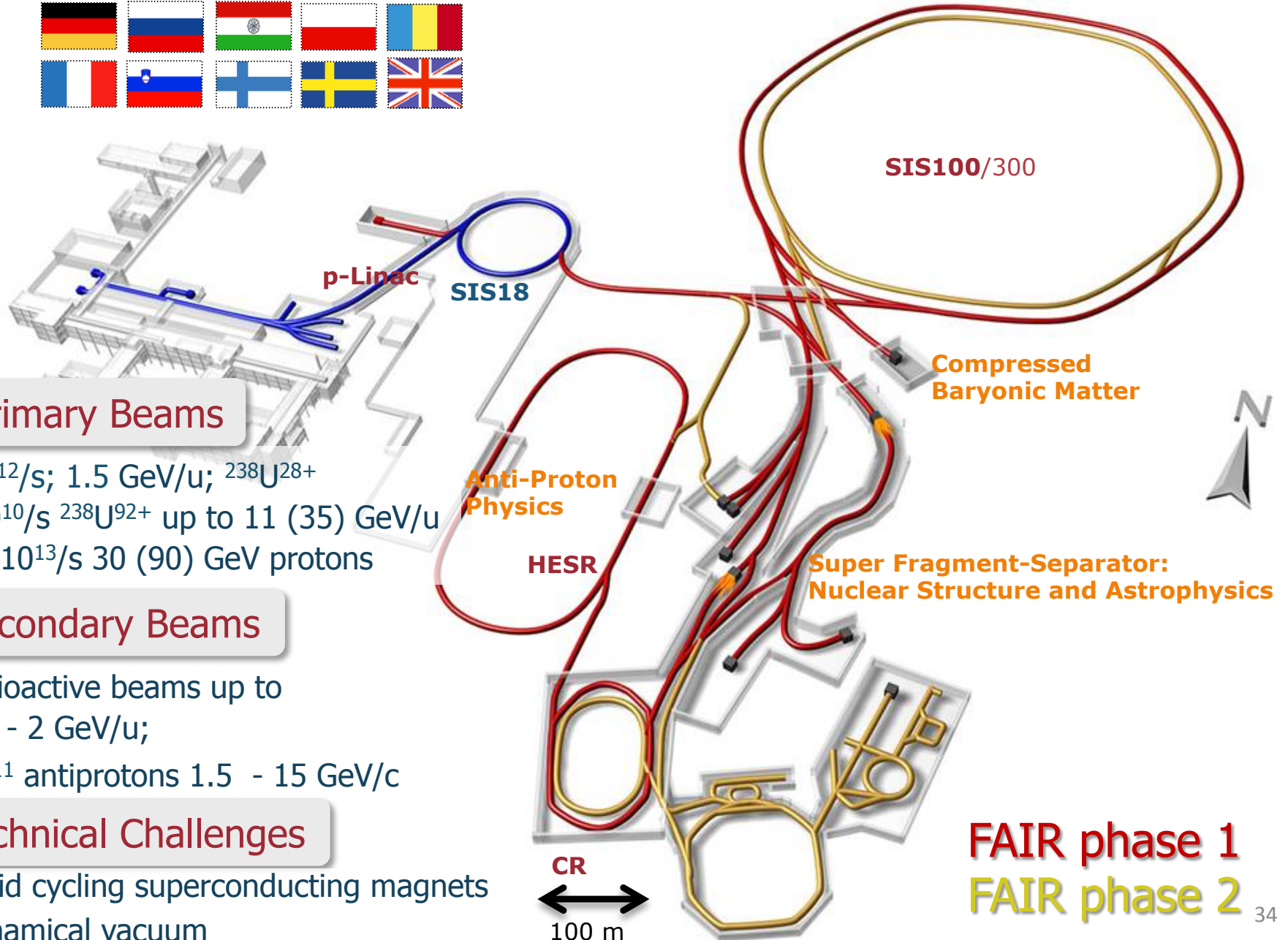


# Experimental requirements

- $10^5 - 10^7$  Au+Au reactions/sec
- identification of leptons and hadrons
- fast and radiation hard detectors and FEE
- free-streaming readout electronics
- high speed data acquisition and high performance computer farm for online event selection
- 4-D event reconstruction



# Facility for Antiproton & Ion Research



## Primary Beams

- $10^{12}/s$ ; 1.5 GeV/u;  $^{238}\text{U}^{28+}$
- $10^{10}/s$   $^{238}\text{U}^{92+}$  up to 11 (35) GeV/u
- $3 \times 10^{13}/s$  30 (90) GeV protons

## Secondary Beams

- radioactive beams up to 1.5 - 2 GeV/u;
- $10^{11}$  antiprotons 1.5 - 15 GeV/c

## Technical Challenges

- rapid cycling superconducting magnets
- dynamical vacuum

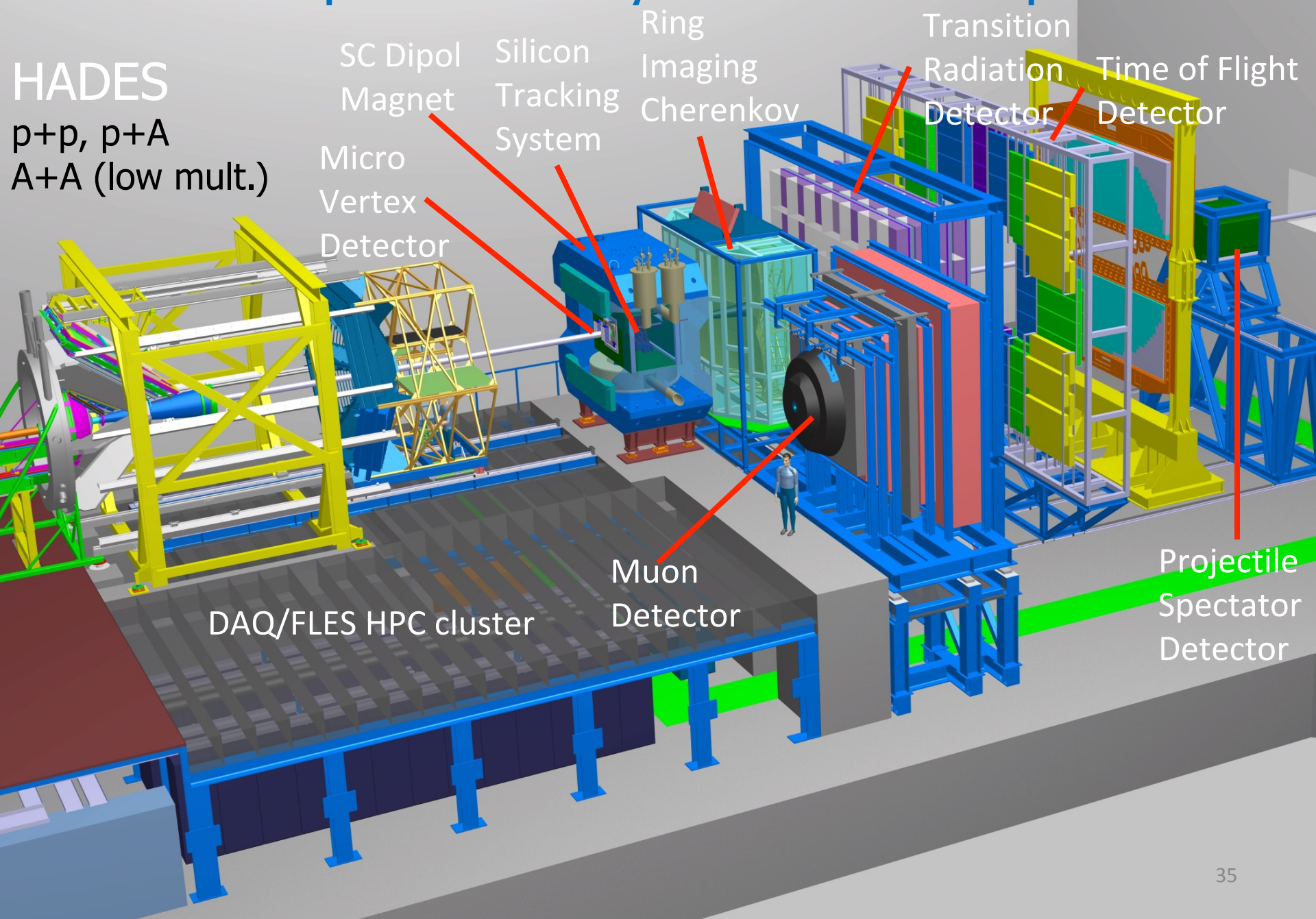
**FAIR phase 1**  
**FAIR phase 2**



# The Compressed Baryonic Matter Experiment

HADES

p+p, p+A  
A+A (low mult.)



SC Dipol  
Magnet

Silicon  
Tracking  
System

Ring  
Imaging  
Cherenkov

Transition  
Radiation  
Detector

Time of Flight  
Detector

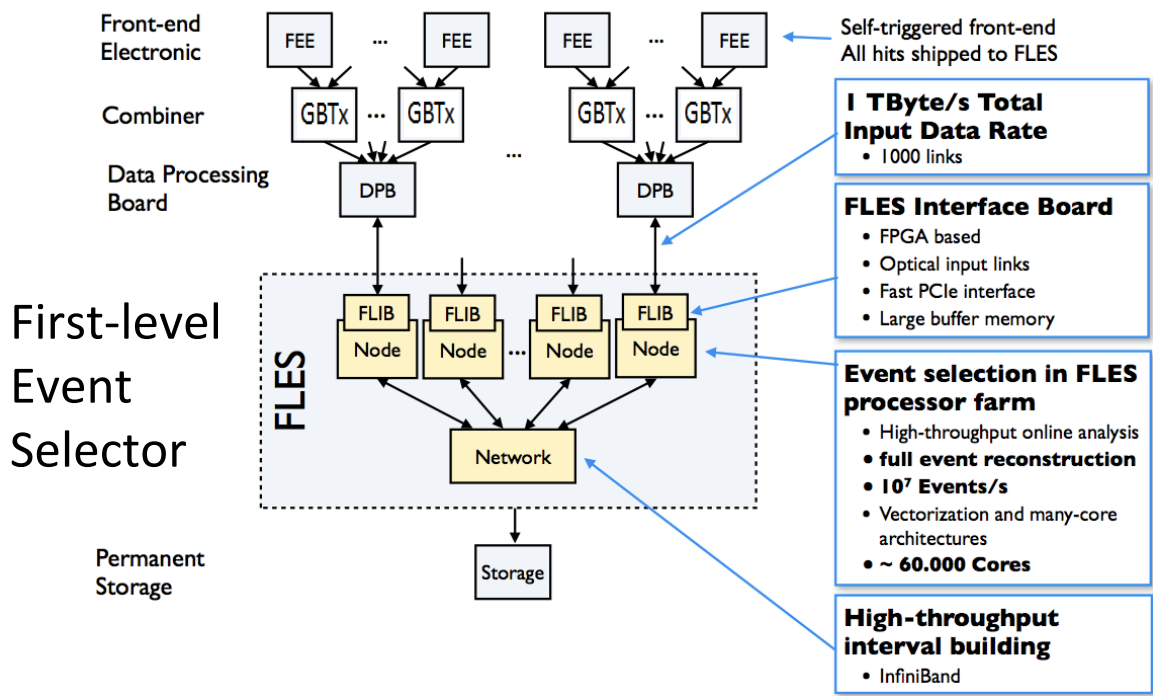
Micro  
Vertex  
Detector

Muon  
Detector

Projectile  
Spectator  
Detector

DAQ/FLES HPC cluster

# CBM DAQ and online event selection



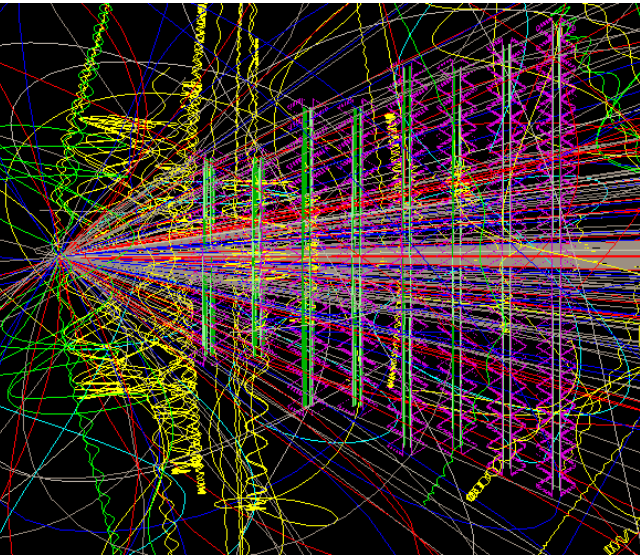
## Novel readout and data acquisition system:

- no hardware trigger on events, free-streaming data read-out
- each detector hit provided with a time stamp
- full online „4-D“ track reconstruction, event definition and data selection by high-speed algorithms running on the GSI GreenIT cube

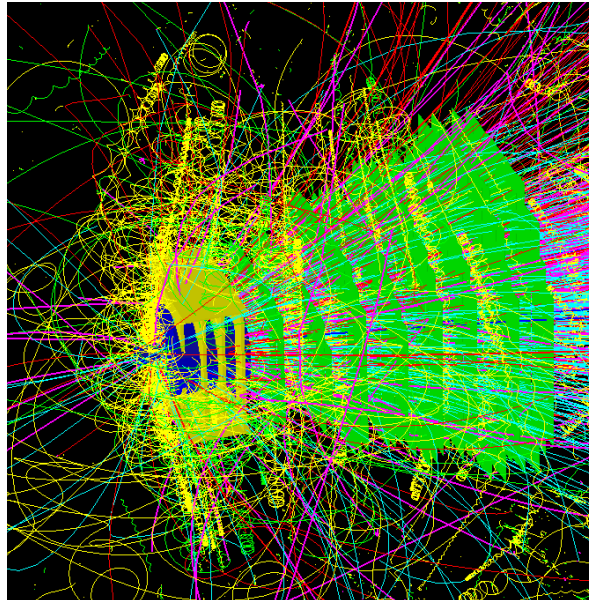


# 4D track and event reconstruction

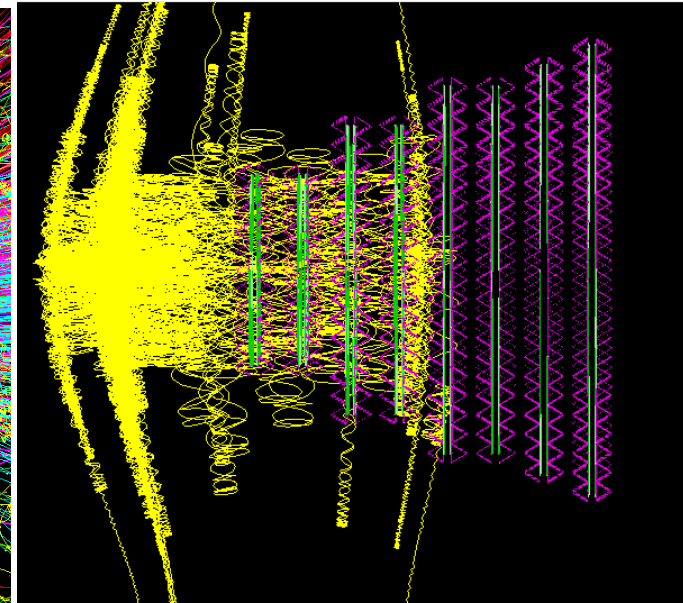
Au+Au 8 A GeV  
peripheral collision  
UrQMD + GEANT3



Au+Au 8 A GeV  
central collision  
UrQMD + GEANT3

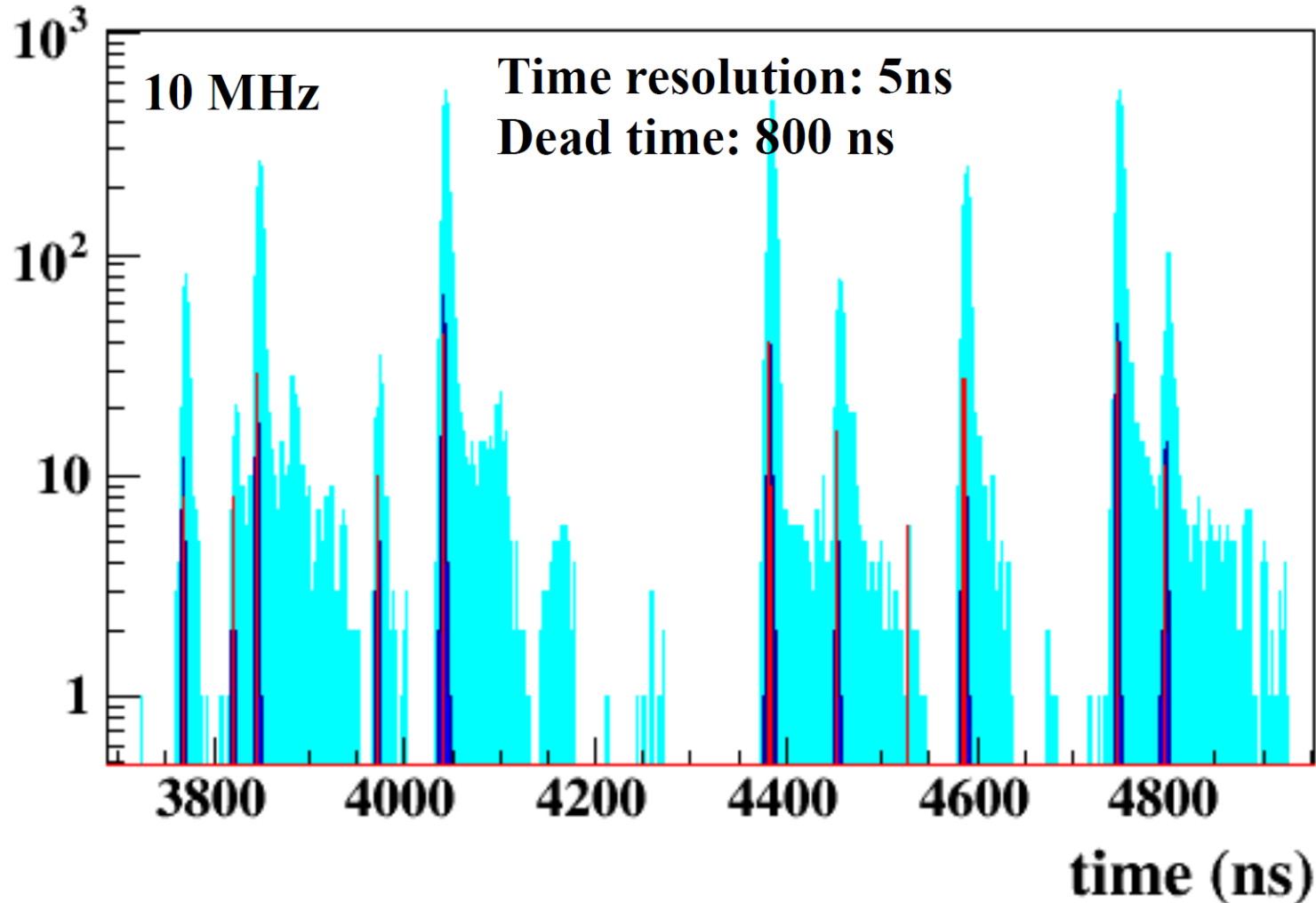


Au beam 8 A GeV  
one single ion  
passing the target  
FairIon + GEANT3



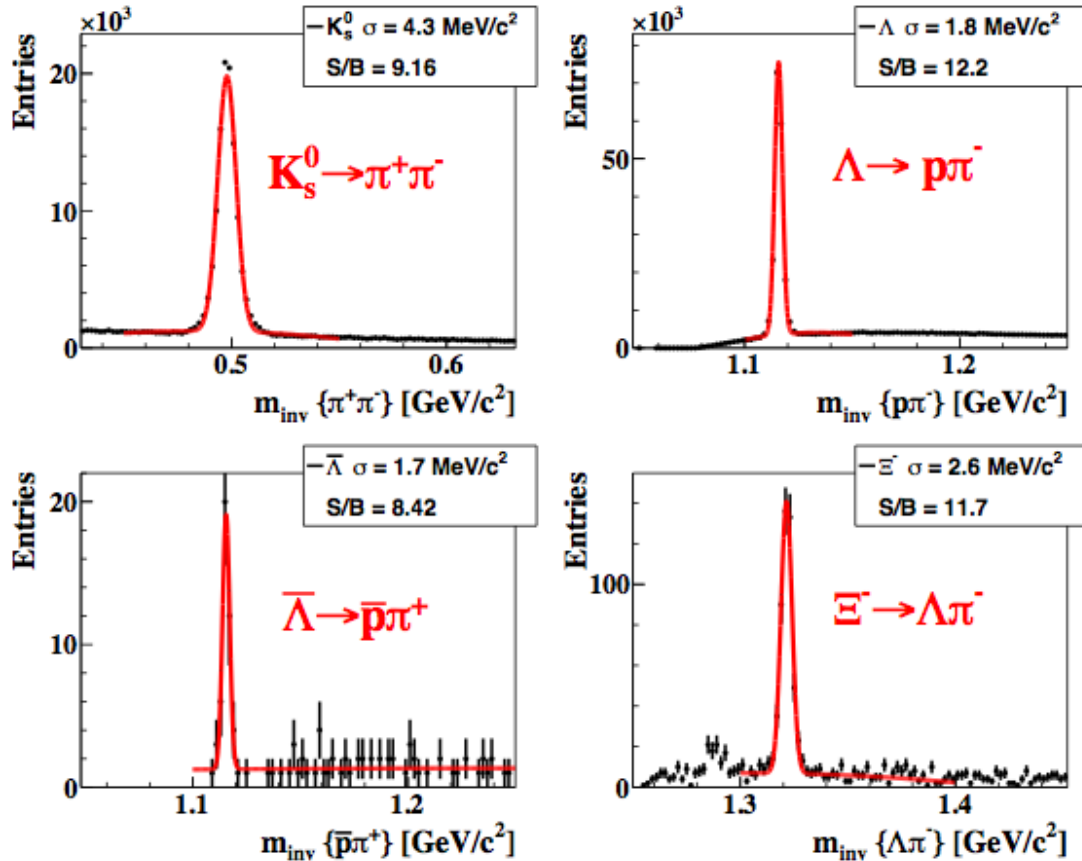
# 4D track and event reconstruction

High rate scenario: STS hits+tracks+ mcEvent vs time



# 4D track and event reconstruction

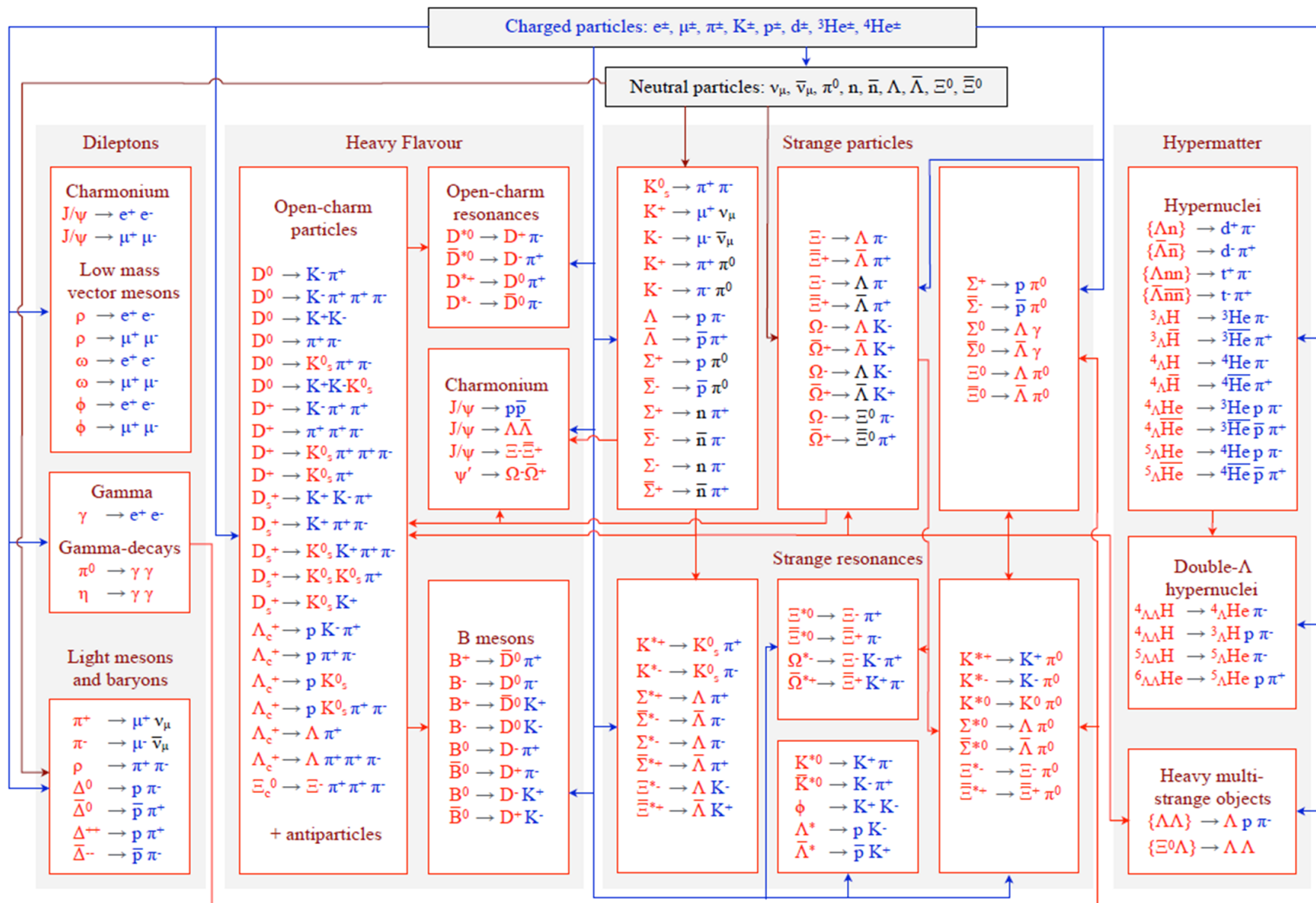
10 MHz Au+Au, 10 AGeV,  
300k mbias UrQMD events, ideal PID



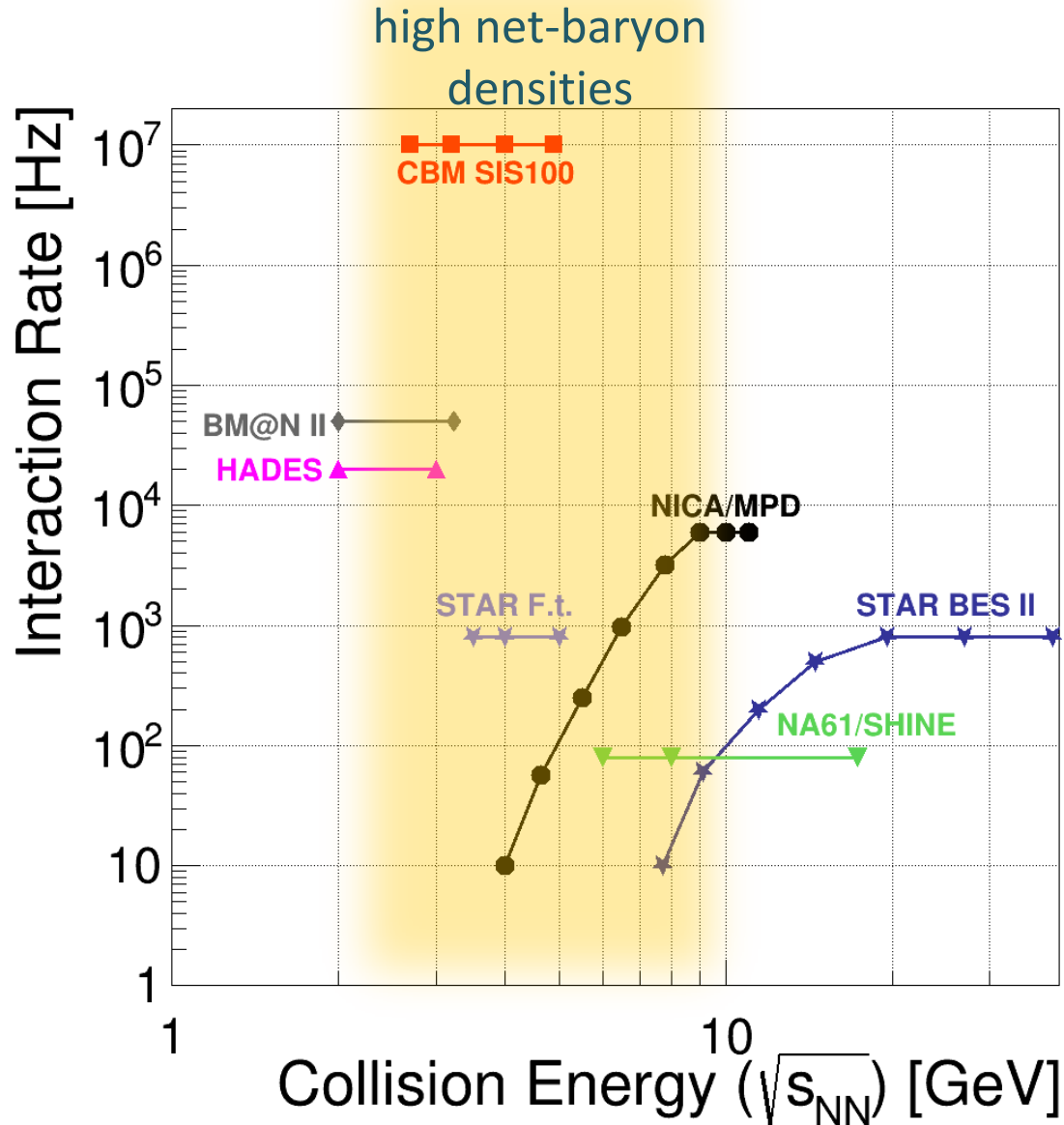
		$K^0_s$	$\Lambda$	$\bar{\Lambda}$	$\Xi^-$
3 D	$\epsilon_{method}, \%$	68.6	61.2	67	46.7
	$\epsilon_{4\pi}, \%$	20.7	19.4	28	10.5
	S/B	10.6	23.7	12.7	21.8
0.1 MHz	$\epsilon_{method}, \%$	68.5	62.0	62	45.2
	$\epsilon_{4\pi}, \%$	21.1	20.6	32	11.7
	S/B	9.8	12.9	10	14.2
1 MHz	$\epsilon_{method}, \%$	67.5	60.9	59	46.0
	$\epsilon_{4\pi}, \%$	19.4	18.7	26	10.6
	S/B	9.3	12.5	10	12.3
10 MHz	$\epsilon_{method}, \%$	66.8	60.0	64	41.8
	$\epsilon_{4\pi}, \%$	17.6	16.7	28	8.2
	S/B	9.2	12.2	8	11.7

all mother particles emitted from one primary vertex

# Online particle identification in CBM: The KF Particle Finder



# Experiments exploring dense QCD matter



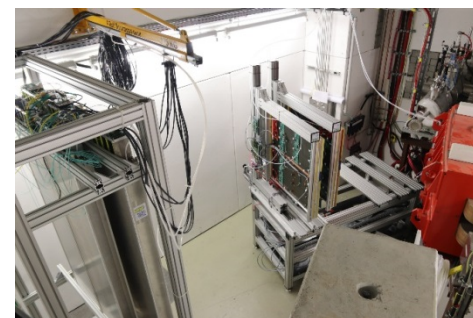
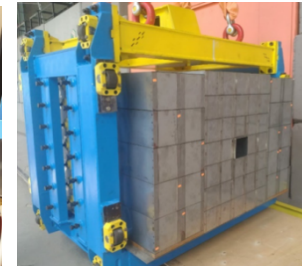
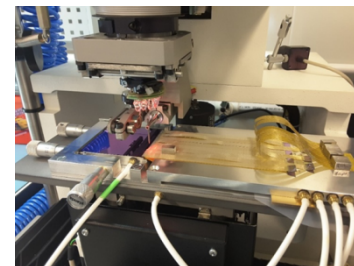
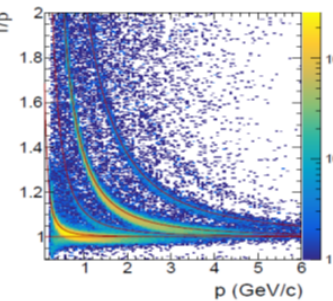
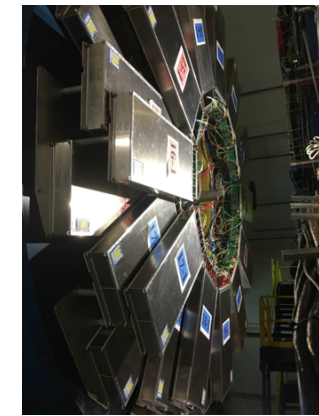
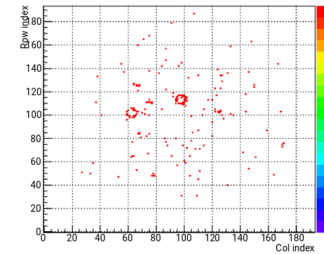
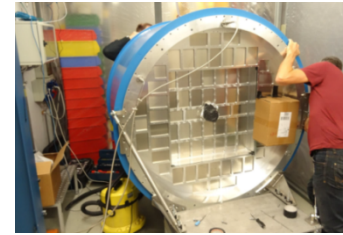
Complementary approaches towards the study of dense baryonic matter, but joint technical developments:

- CBM photon detector used in HADES
- CBM TOF detector and reconstruction software used in STAR
- Forward calorimeters for CBM and NA61/SHINE
- Silicon detector and software developments for NICA



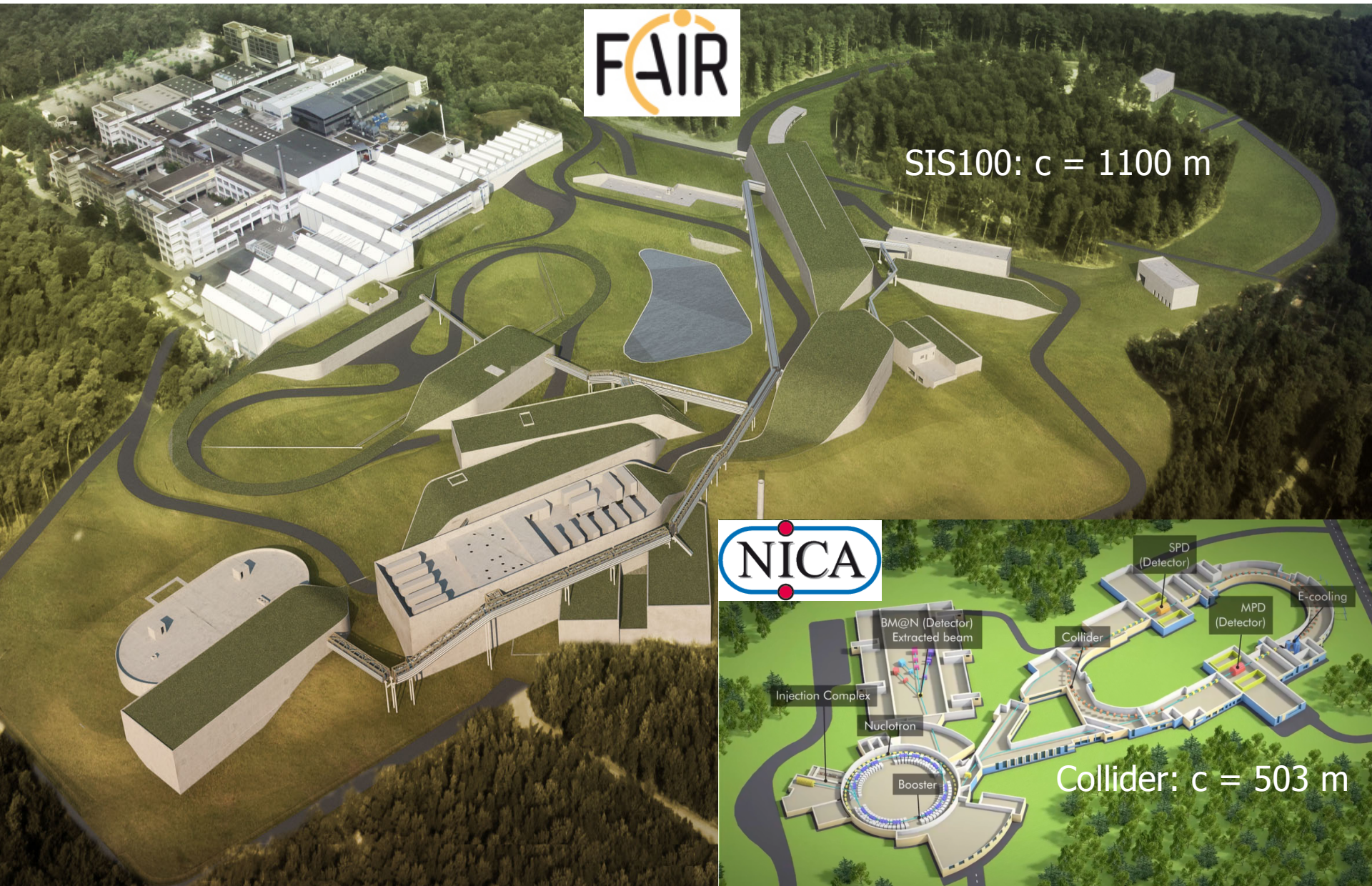
# CBM „phase 0“ experiments on dense QCD matter

1. CBM RICH photon detector: 430 out of 1100 multi-anode photo-multipliers (MAPMT) installed in HADES experiment and used for physics runs
2. CBM TOF detector: 10% of the CBM TOF modules including read-out chain installed and used at STAR/RHIC (BES II 2019/2020)
3. Four Silicon Tracking Stations and a Projectile Spectator Detector will be installed in the BM@N experiment at the Nuclotron in JINR/Dubna (start 2022 with Au-beams up to 4.5A GeV )
4. miniCBM experiment installed at GSI/SIS18 and commissioned with beam for a full system test with high-rate nucleus-nucleus collisions from 2020 - 2023

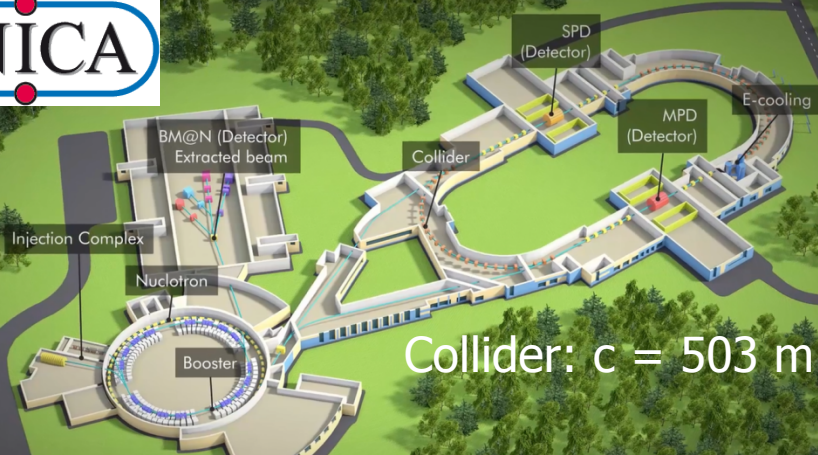




# FAIR and NICA



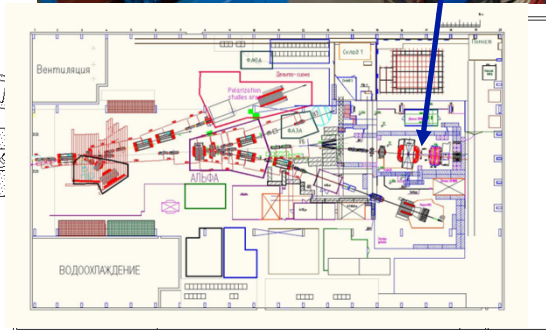
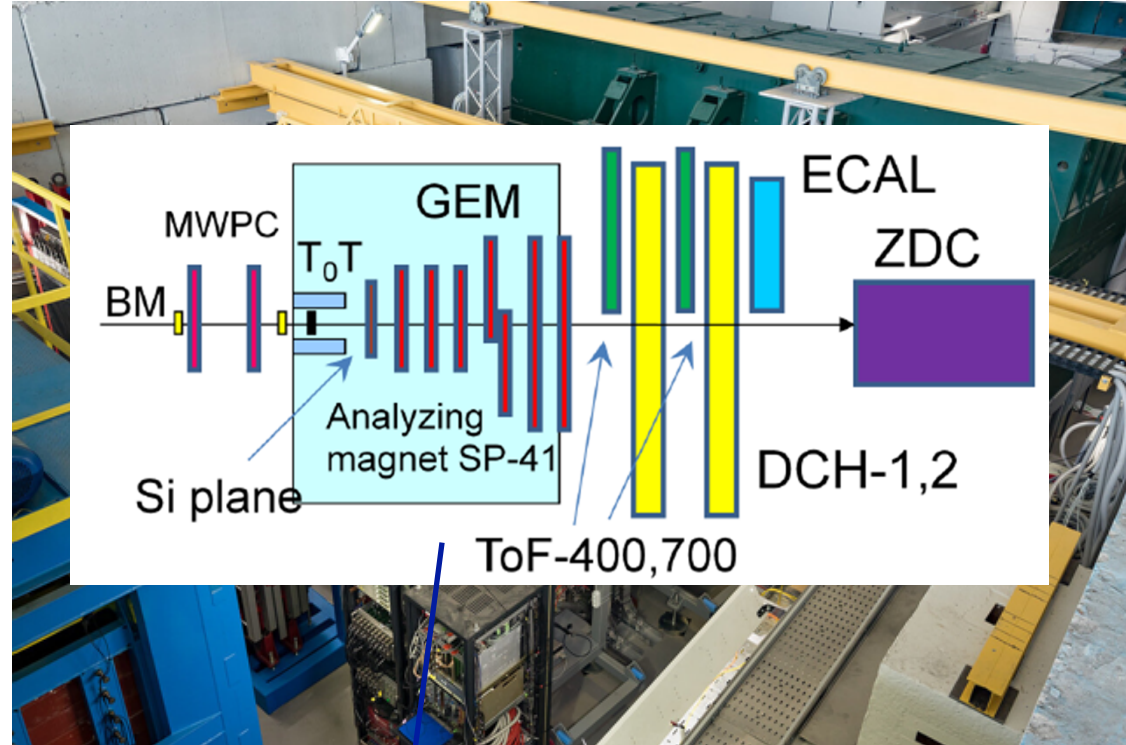
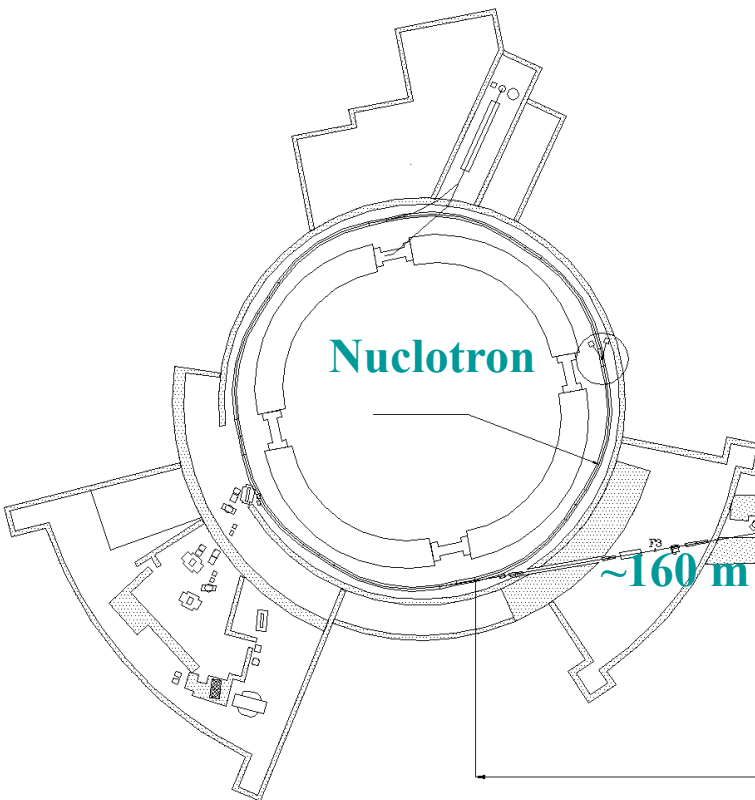
SIS100:  $c = 1100$  m



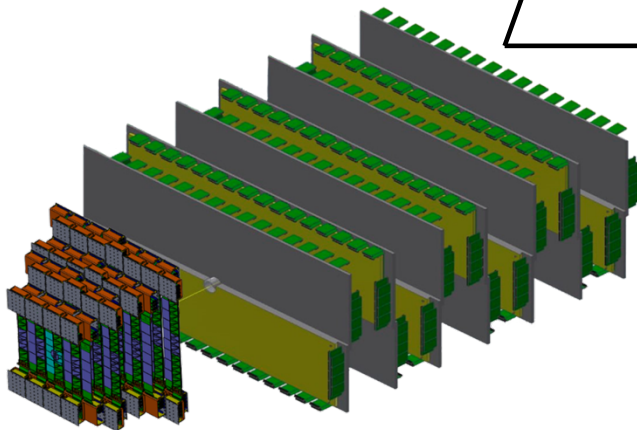
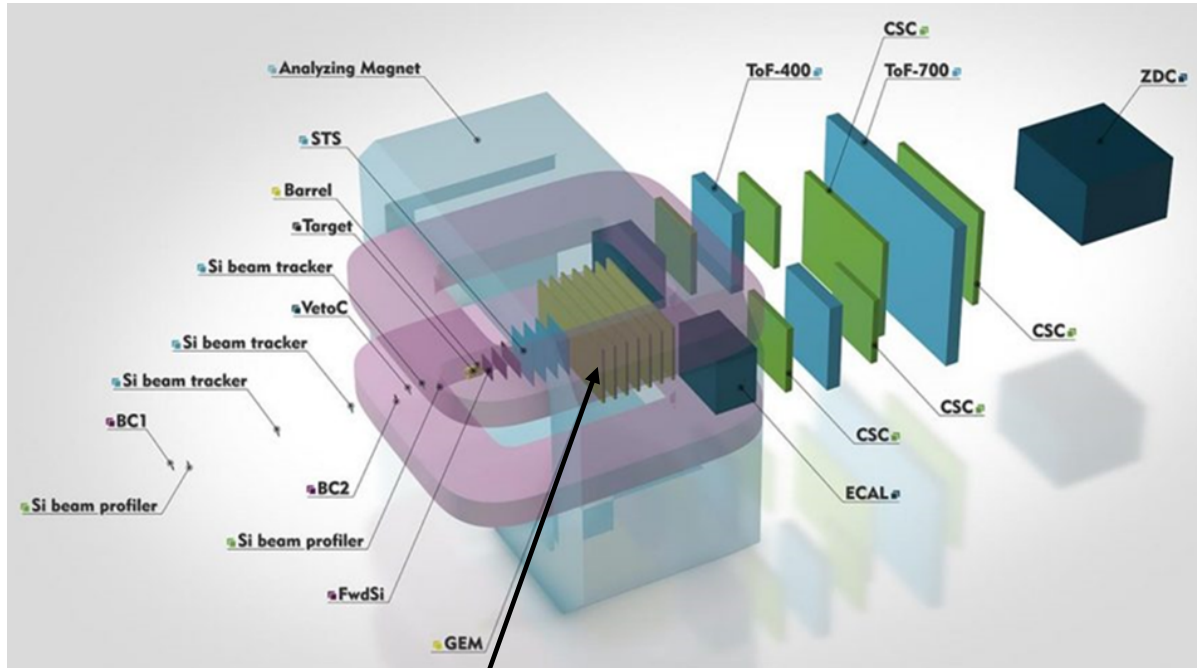
Collider:  $c = 503$  m



# The Baryonic Matter at Nuclotron (BM@N) experiment

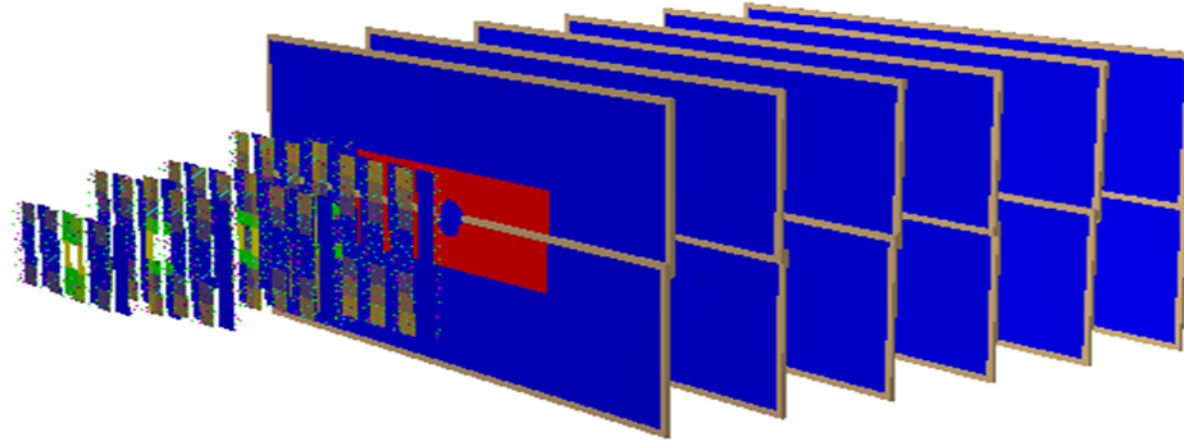


# BM@N upgrade for Au+Au collisions up to 4.5A GeV



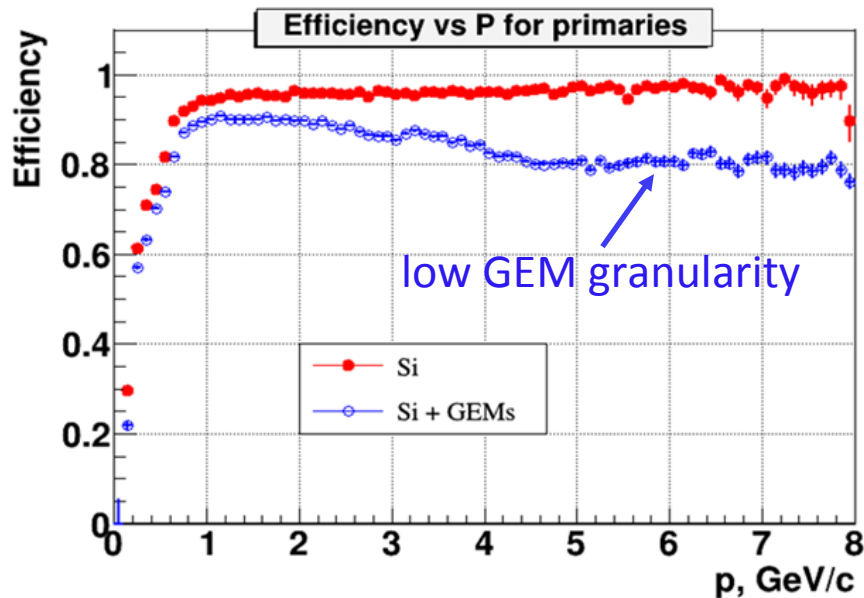
The hybrid tracking system:  
4 stations double-sided micro-strip silicon sensors  
7 stations Gas-Electron-Multiplier (GEM) chambers

# BM@N upgrade for Au+Au collisions

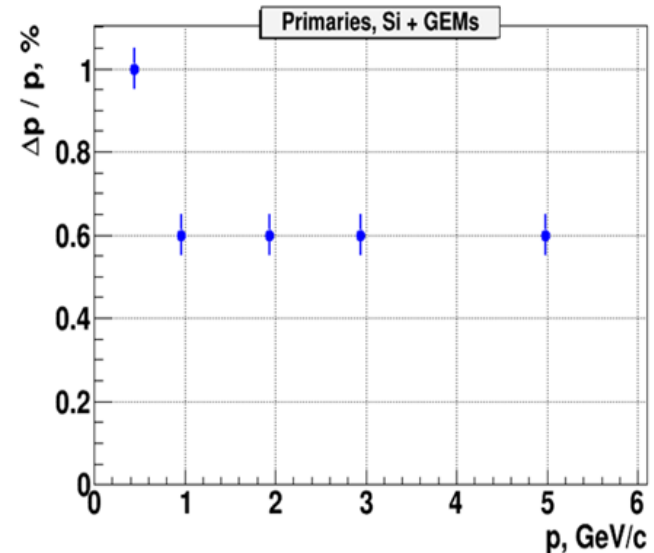


central Au+Au collisions at 4A GeV (QGSM generator)

track reconstruction efficiency



momentum resolution





## Joint development of instrumentation for NICA and FAIR/CBM

Grant 5.6 M€ over 4 years for manpower (starting 2020)

Task	Partners
Integration, installation, and test of Silicon Trackers for NICA and CBM	JINR Dubna, FAIR/GSI, Univ. Tübingen
Developments for the data acquisition chain, for data preprocessing and computing procedures	JINR Dubna, FAIR/GSI, WUT Warsaw
Development of common software packages for simulation and data analysis, participation in physics performance studies	JINR Dubna, FAIR/GSI, MEPHI, Wigner Inst. Budapest
Development and construction of beam monitors, target chamber, beam pipe for NICA and CBM	JINR Dubna, FAIR/GSI
Development and construction of Zero Degree Calorimeters for NICA and CBM	INR Moscow, NRI-CAS Prague
Develop a beyond state of the art CMOS pixel sensors (MAPS) for high-rate Silicon trackers	JINR Dubna, FAIR/GSI, Univ. Frankfurt, KINR Kiev, IPHC Strasbourg,





October 2019



# The CBM Collaboration: 58 institutions, > 460 members

## China:

CCNU Wuhan  
Tsinghua Univ.  
USTC Hefei  
CTGU Yichang  
Chongqing Univ.  
IMP Lanzhou

## Czech Republic:

CAS, Rez  
Techn. Univ. Prague

## France:

IPHC Strasbourg

## Hungary:

KFKI Budapest  
Eötvös Univ.

## Germany:

Darmstadt TU  
FAIR  
Frankfurt Univ. IKF  
Frankfurt Univ. FIAS  
Frankfurt Univ. ICS  
GSI Darmstadt  
Giessen Univ.  
Heidelberg Univ. P.I.  
Heidelberg Univ. ZITI  
HZ Dresden-Rossendorf  
KIT Karlsruhe  
Münster Univ.  
München TU  
Tübingen Univ.  
Wuppertal Univ.  
ZIB Berlin

## India:

Aligarh Muslim Univ.  
Bose Inst. Kolkata  
Panjab Univ.  
Rajasthan Univ.  
Univ. of Jammu  
Univ. of Kashmir  
Univ. of Calcutta  
B.H. Univ. Varanasi  
VECC Kolkata  
IOP Bhubaneswar  
IIT Kharagpur  
IIT Indore  
Gauhati Univ.

## Japan:

KEK Tsukuba

## Korea:

Pusan Nat. Univ.

## Poland:

AGH Krakow  
Jag. Univ. Krakow  
Warsaw Univ.  
Warsaw Univ. Tech.

## Romania:

NIPNE Bucharest  
Univ. Bucharest

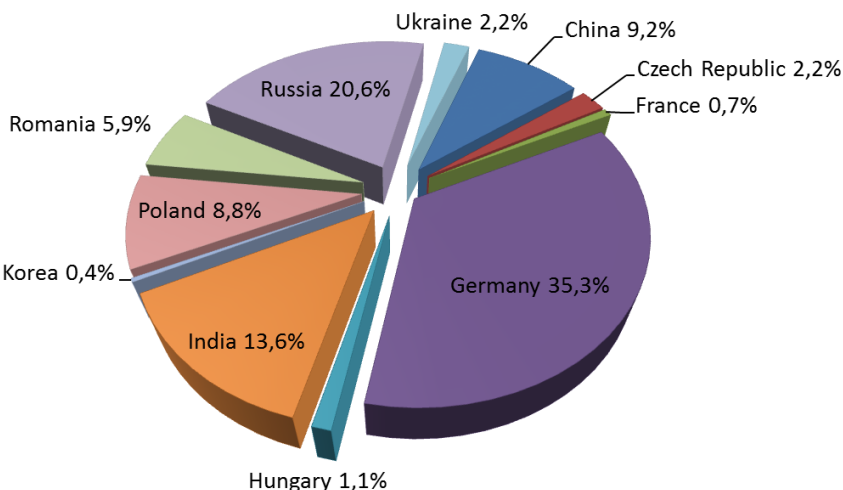
## Russia:

IHEP Protvino  
INR Troitzk  
ITEP Moscow  
Kurchatov Inst., Moscow  
VBLHEP, JINR Dubna  
LIT, JINR Dubna  
MEPHI Moscow  
PNPI Gatchina  
SINP MSU, Moscow

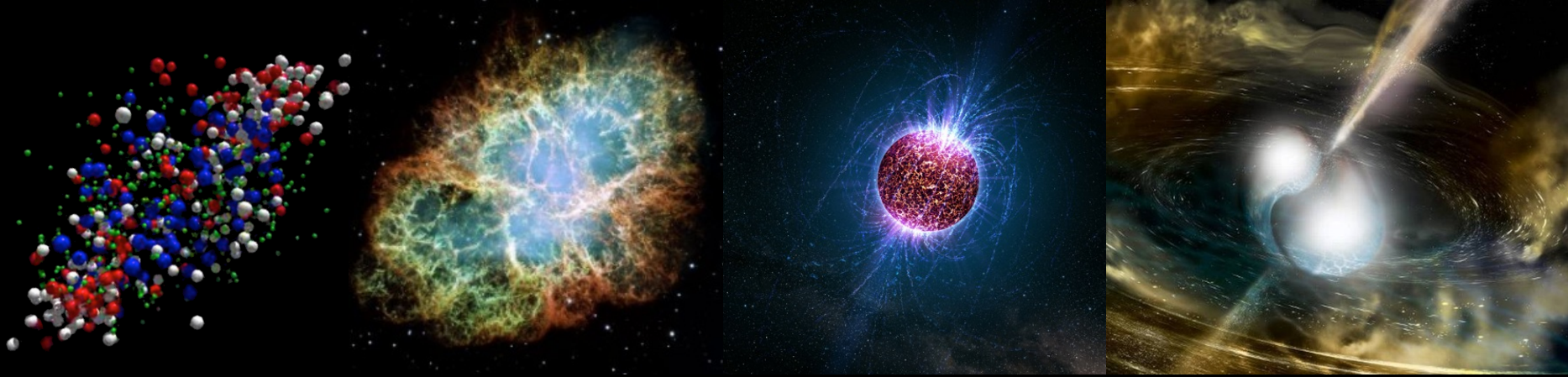
## Ukraine:

T. Shevchenko Univ. Kiev  
Kiev Inst. Nucl. Research

CBM Scientists







## Summary

- The goal of the CBM experiment at FAIR is to explore fundamental properties of dense QCD matter by measuring multi-differential observables (hadrons and leptons) with unprecedented precision. First beams of Au ions up to  $11A$  GeV are expected in 2025.
- The BMN experiment at NICA offers the opportunity to prototype the CBM silicon tracking system, and to start the investigation of dense nuclear matter produced in Au+Au collisions at beam energies of up to  $4.5A$  GeV in 2023.