



Heavy quark production in e^+e^- & pp collisions

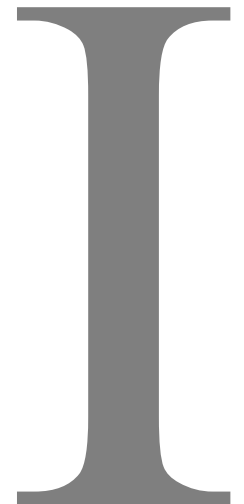
Seminar talk by Bernhard Maaß



- I. Introduction to heavy quark production
- II. Producing quarks in e^+e^- collisions
- III. Hadronic structure and e^-p collisions
- IV. Advanced experiments: pp collisions



Introduction to heavy quark production



Heavy quarks

Drei Generationen
der Materie (Fermionen)

	I	II	III		
Masse →	2,4 MeV	1,27 GeV	171,2 GeV	0	? GeV
Ladung →	$\frac{2}{3}$	$\frac{2}{3}$	$\frac{2}{3}$	0	0
Spin →	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	1	0
Name →	u up	c charm	t top	γ Photon	H Higgs Boson
	4,8 MeV	104 MeV	4,2 GeV	0	
	$-\frac{1}{3}$	$-\frac{1}{3}$	$-\frac{1}{3}$	0	
	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	1	
Quarks	d down	s strange	b bottom	g Gluon	
	<2,2 eV	<0,17 MeV	<15,5 MeV	91,2 GeV	
	0	0	0	0	
	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	1	
	ν_e Elektron- Neutrino	ν_μ Myon- Neutrino	ν_τ Tau- Neutrino	Z⁰ Z Boson	
	0,511 MeV	105,7 MeV	1,777 GeV	80,4 GeV	
	-1	-1	-1	±1	
	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	1	
Leptonen	e Elektron	μ Myon	τ Tau	W[±] W Boson	Eichbosonen

charm: SLAC and Brookhaven
 e^+e^- annihilation (1974)

bottom: Fermilab
p-nucleus (1977)

top: Tevatron
 p^+p^- annihilation (1995)

collider...

SLAC: acceleration of e^+ and e^- up to 50 GeV

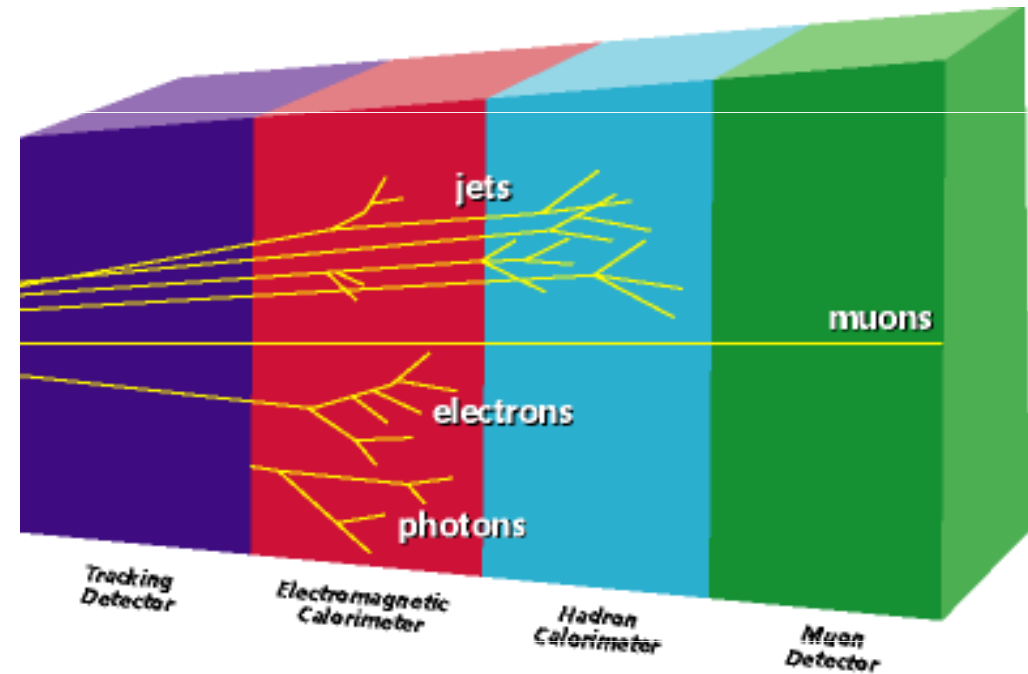
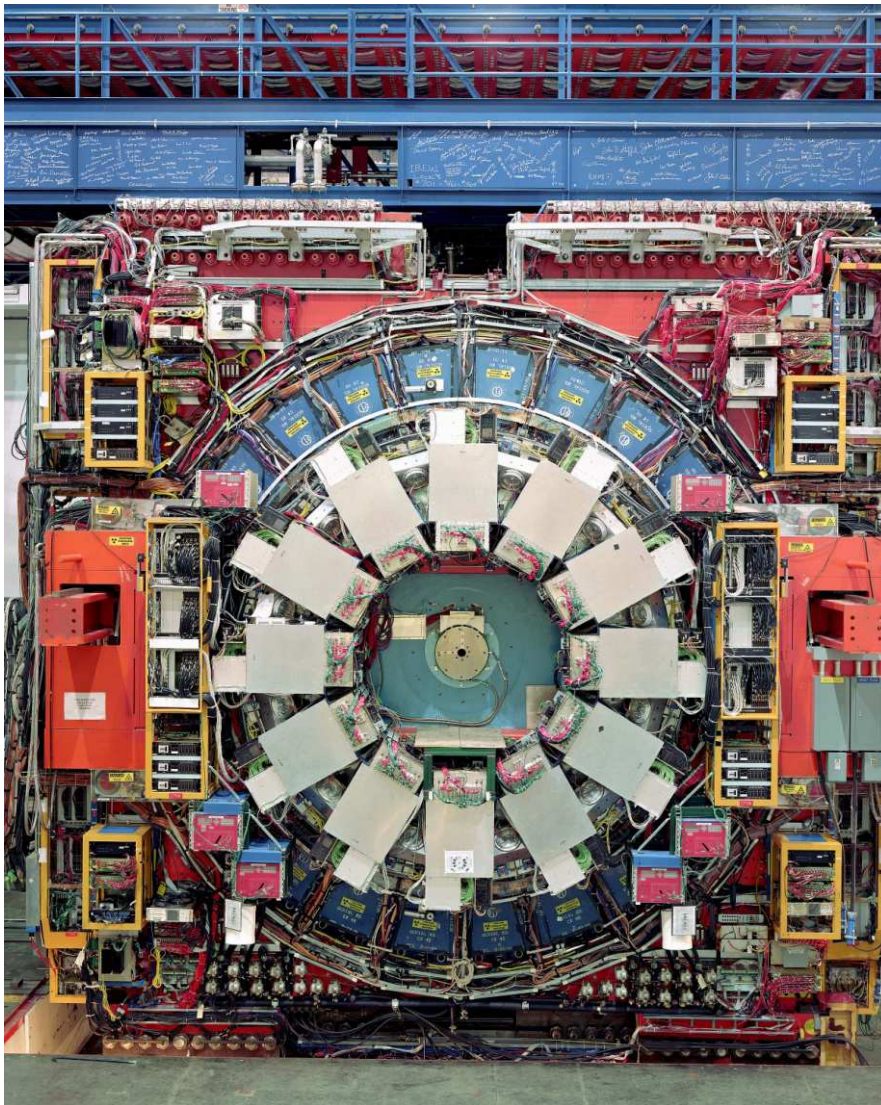


Tevatron:
acceleration of p^+ and p^- up to 900 GeV
(when discovering top-quarks)

Source: wikipedia: SLAC, Tevatron

... and particle detectors

I. Introduction | II. e^+e^- collisions | III. hadronic structure | IV. pp collisions



CDF-Detector from Tevatron

Source: <http://www-cdf.fnal.gov/>, [povh]



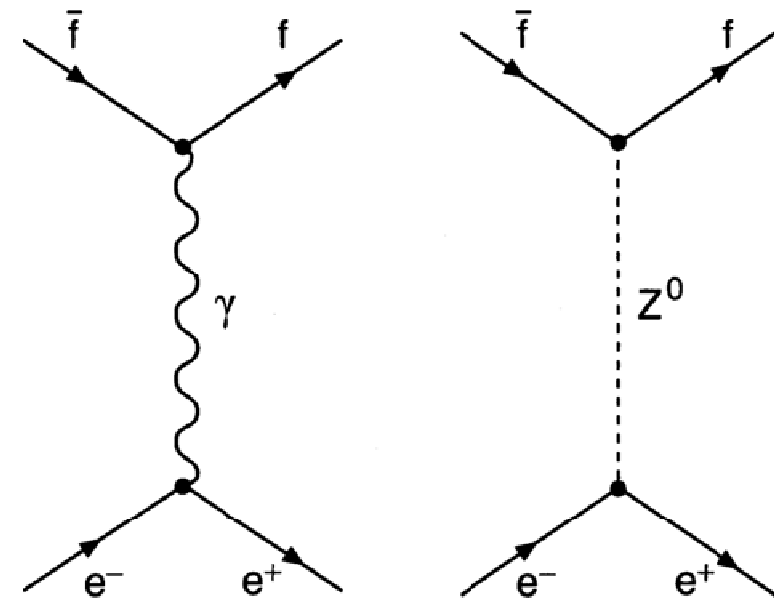
Producing quarks in e^+e^- collisions



e^+e^- annihilation

the basic process

$$e^+ + e^- \rightarrow \bar{q} + q$$



all weak/em-interacting particles
can be produced

Source: [povh]

muon production as reference

Muon production

$$e^+ + e^- \rightarrow \mu^+ + \mu^-$$

EM-process due to high Z⁰ mass – easy to calculate

μ-mass: 105.7 MeV

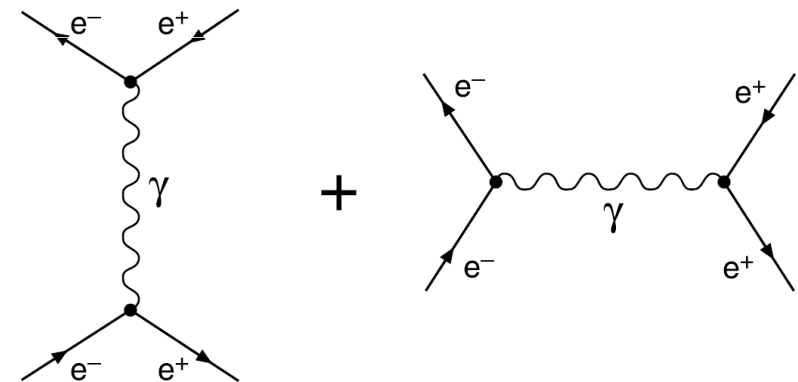
T-mass: 1.777 GeV

Z⁰-mass: 91.2 GeV

reaction cross section:

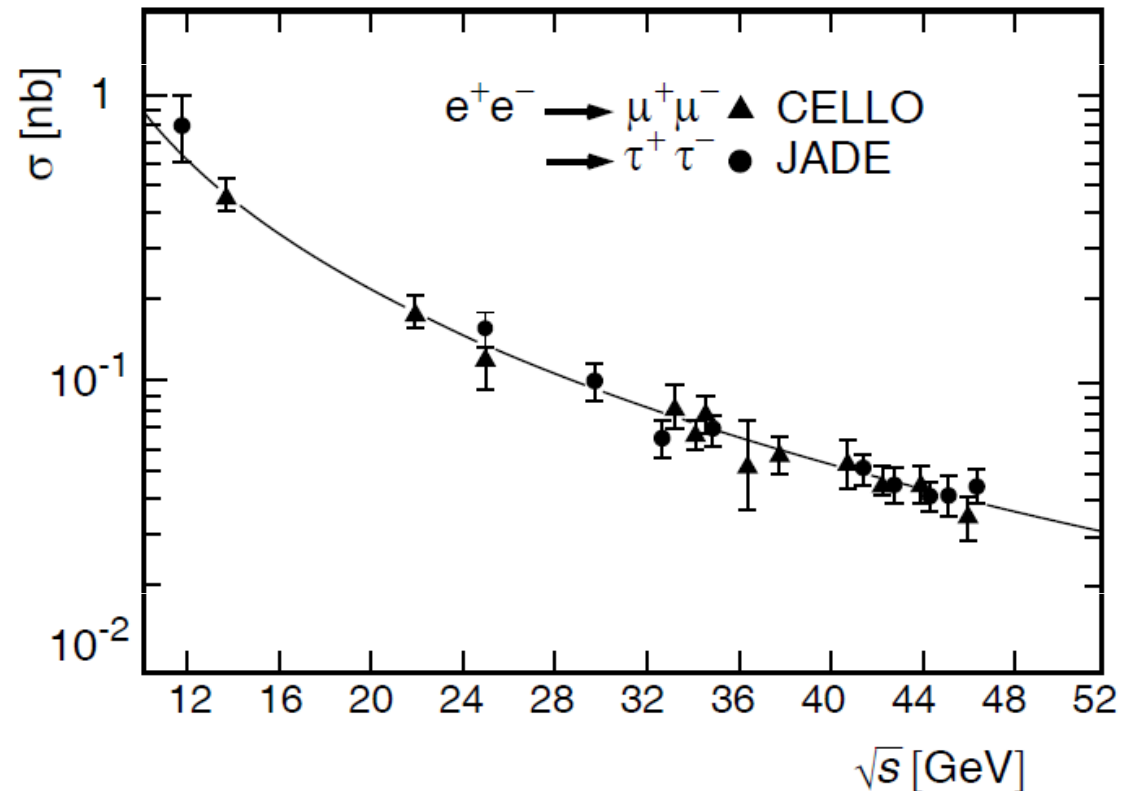
$$\sigma(e^+e^- \rightarrow \mu^+\mu^-) = 21.7 \frac{\text{nbarn}}{(E^2/\text{GeV}^2)}$$

Bhabha-Diffraction



Source: [povh]

lepton universality

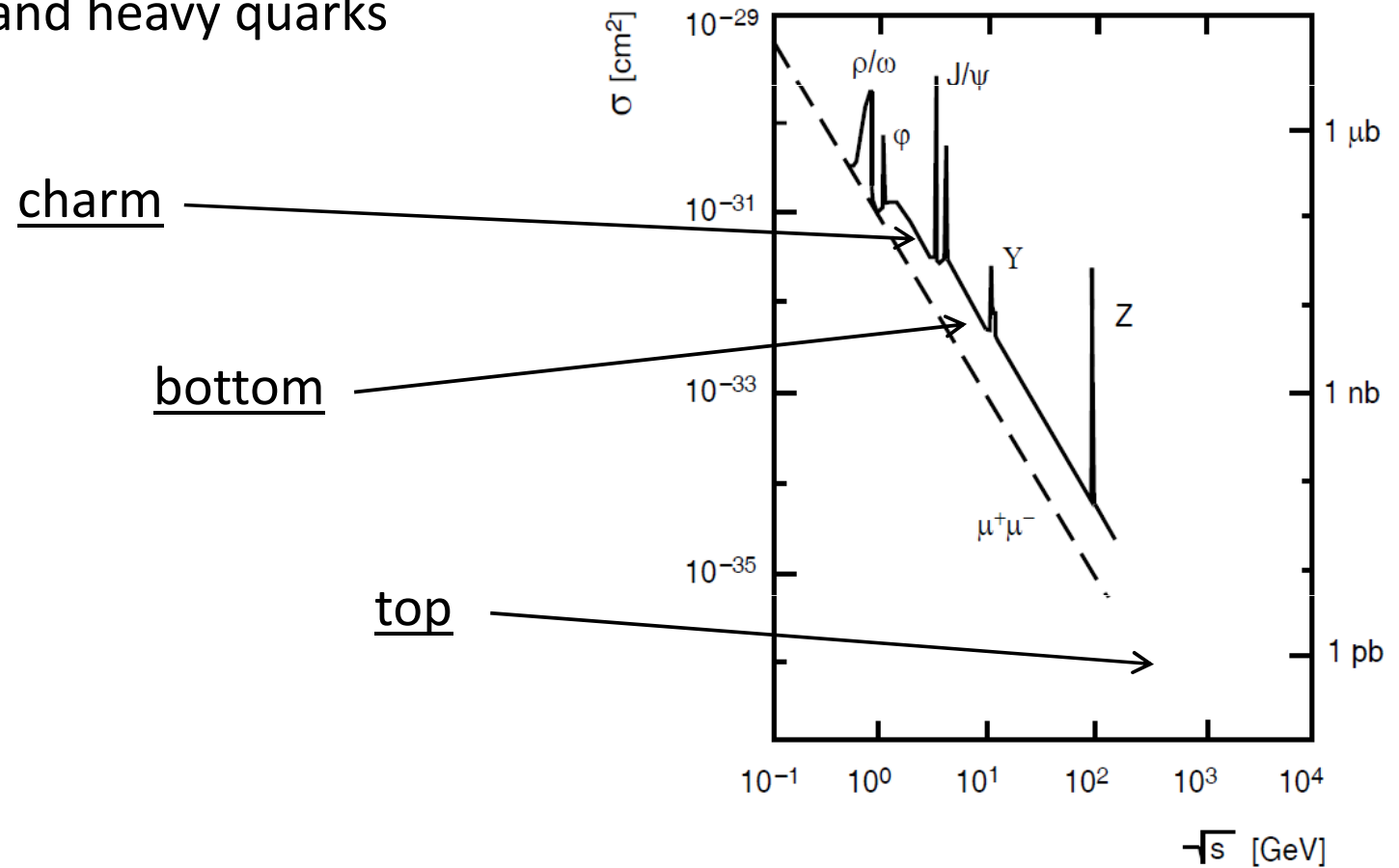


lepton universality / leptons are point-masses ($< 10^{-18}\text{m}$)

Source: [povh]

Resonances and quarks

Resonances with light and heavy quarks
are observed



maximum e^+e^- collider cm-energy: ~ 172 GeV

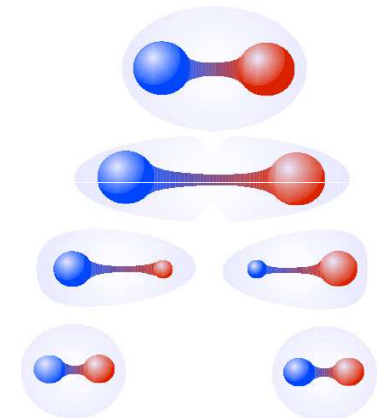
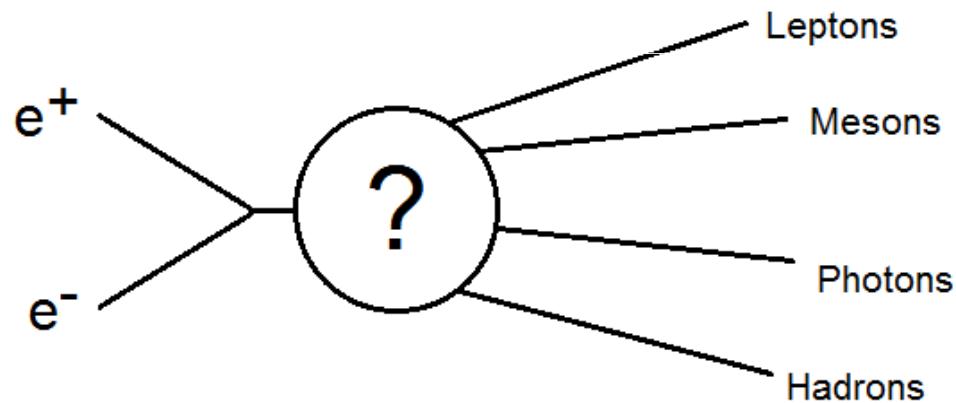
Source: [povh]

between the resonance

„free quarks“ can be produced between the resonances.

$$e^+e^- \rightarrow q\bar{q} \rightarrow \text{Hadrons}$$

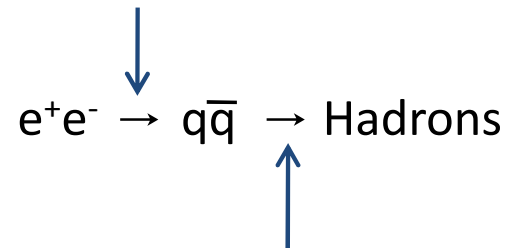
Due to color confinement, the quark/antiquark-pair will immediately hadronize („fragmentation“)



Source: [bethke]

Fragmentation

The (perturbative) process is on a scale of $d \ll 1\text{fm}$



The fragmentation process occurs on much larger scales - $d \gg 1\text{fm}$

Every quark/antiquark will hadronize and therefore:

$$\sigma(e^+e^- \rightarrow q\bar{q}) = \sigma(e^+e^- \rightarrow \text{Hadrons})$$

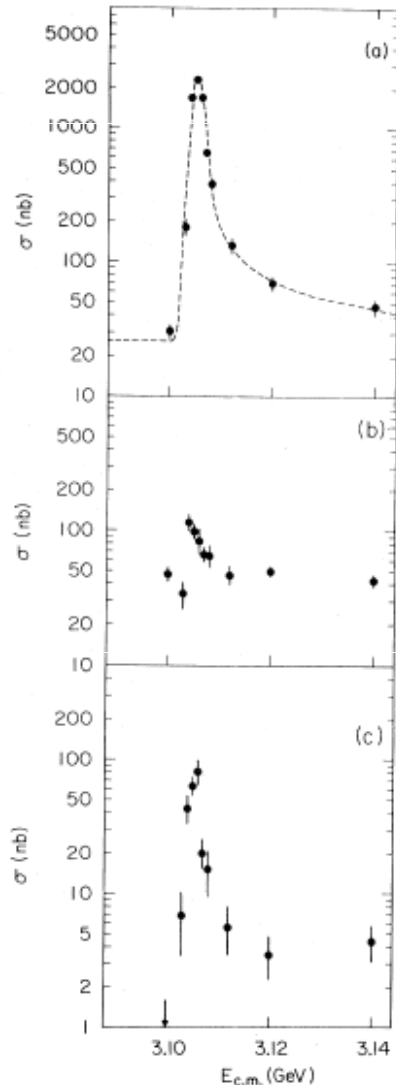
when $\sigma(q\bar{q} \rightarrow \text{Hadrons}) = 1$

Charm discovery



Discovery of the charm-quark:

The charm decays (mainly) into Pions and Kaons. These particles have to be detected and identified.



Decay mode	Mass Region (GeV/c^2)		
	1.50–1.85	1.85–2.40	2.40–4.00
$K^-\pi^+$ and $K^+\pi^-$	0.25	0.18	0.08
$K_s^0\pi^+\pi^-$	0.57	0.40	0.29
$\pi^+\pi^-$	0.13	0.13	0.09
K^+K^-	0.23	0.12	0.10
$K^-\pi^+\pi^+$ and $K^+\pi^-\pi^-$	0.51	0.49	0.19
$K_s^0\pi^+$ and $K_s^0\pi^-$	0.26	0.27	0.09
$K_s^0K^+$ and $K_s^0K^-$	0.54	0.33	0.09
$\pi^+\pi^-\pi^+$ and $\pi^+\pi^-\pi^-$	0.48	0.38	0.18
$K^\mp\pi^\pm$, $\bar{K}^0\pi^+\pi^-$, and $K^0\pi^+\pi^-$	1.16	0.90	0.58
K^+K^- and $\pi^+\pi^-$	0.23	0.16	0.15
$K^\mp\pi^\pm\pi^\pm$, $\bar{K}^0\pi^\pm$, and $K^0\pi^\pm$	0.64	0.51	0.30
\bar{K}^0K^\pm , K^0K^\pm , and $\pi^+\pi^-\pi^\pm$	1.10	0.76	0.29

Source: [charm], [charm2]

Production ratio

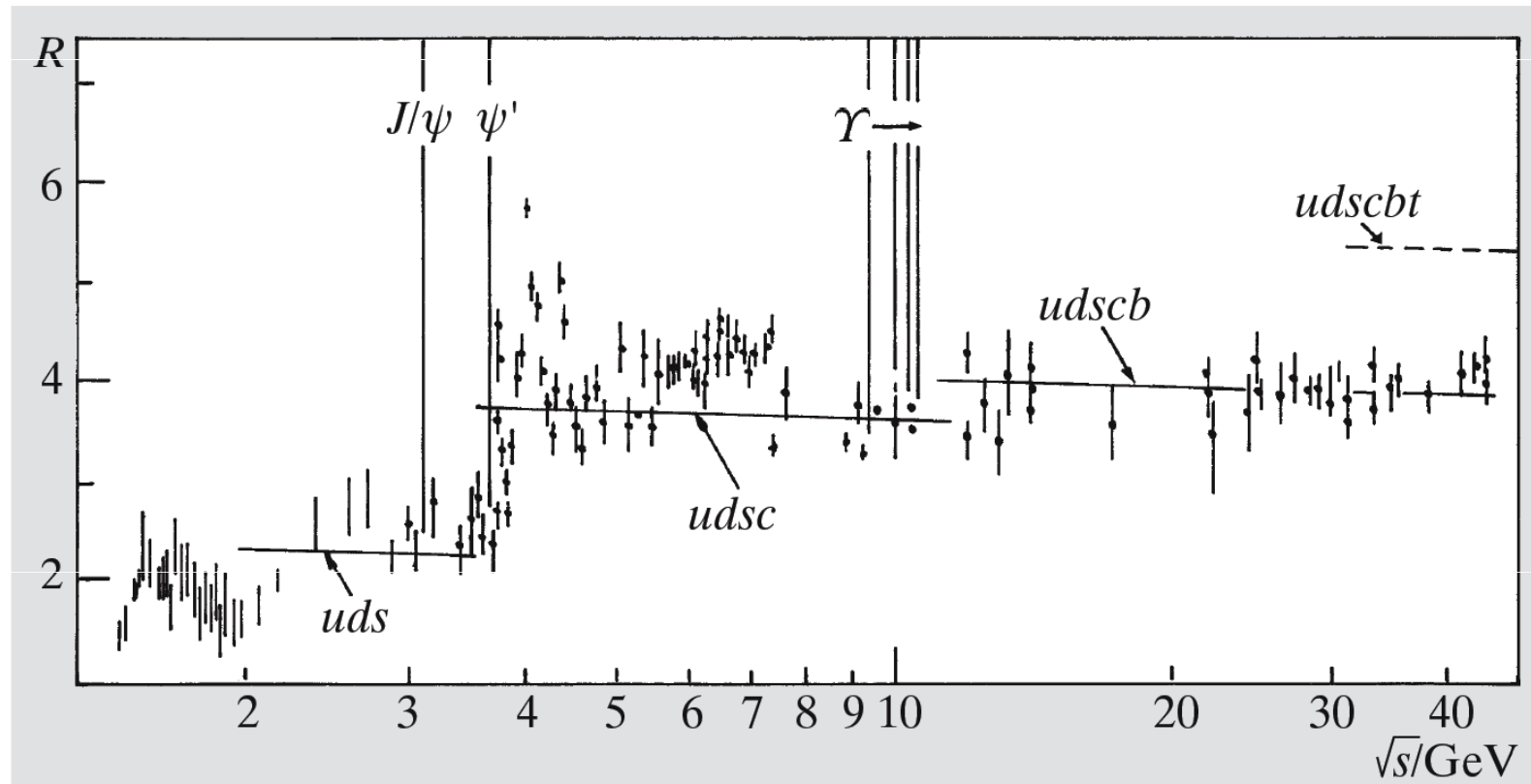
Cross section ratio:

$$R = \frac{\sigma(e^+e^- \rightarrow H)}{\sigma(e^+e^- \rightarrow \mu^+\mu^-)} = \frac{\sum_f \sigma(e^+e^- \rightarrow q_f q_{\bar{f}})}{\sigma(\mu^+\mu^-)}$$

The cross sections of the different quark flavours are summed up:

$$R = 3 \cdot \sum_f z_f^2 = 3 \cdot \left\{ \underbrace{\left(\frac{2}{3} \right)^2 + \left(-\frac{1}{3} \right)^2 + \left(-\frac{1}{3} \right)^2}_{3 \cdot 6/9} + \underbrace{\left(\frac{2}{3} \right)^2 + \left(-\frac{1}{3} \right)^2}_{3 \cdot 10/9} \right\} = 3 \cdot \frac{11}{9}$$

Stepwise quark production

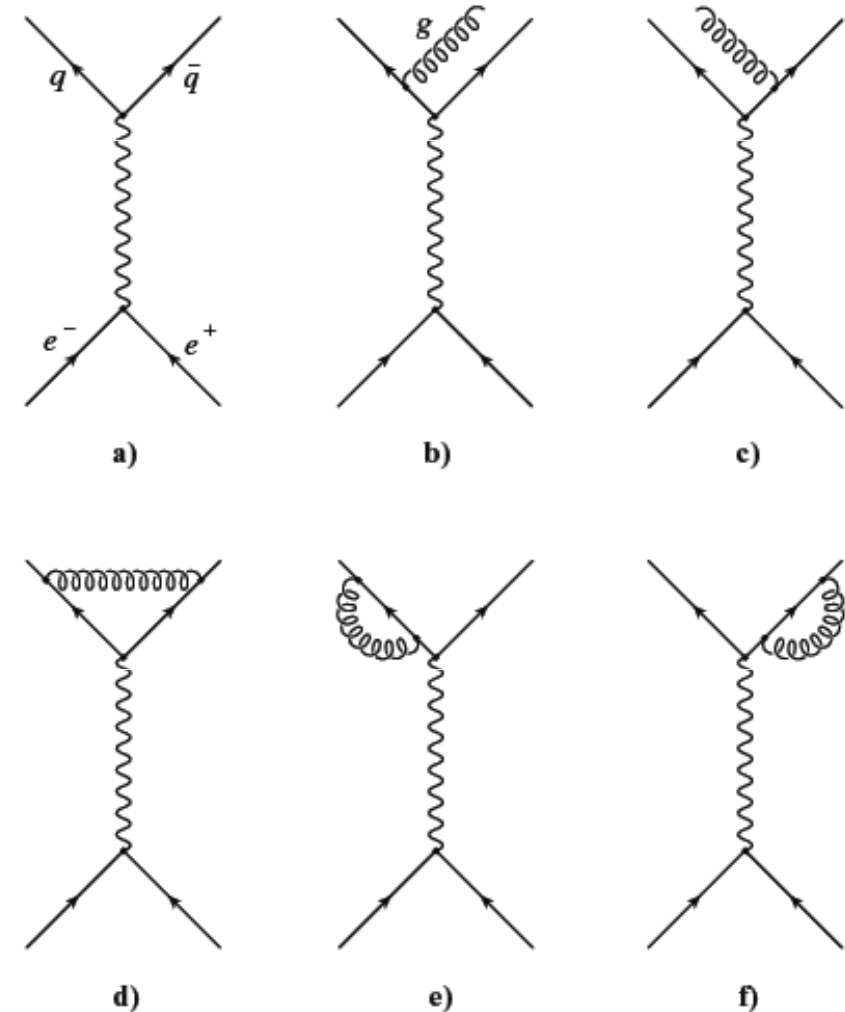


Source: [berger]

Gluons and QCD corrections

Quarks can emit gluons
due to strong interaction:

$$e^+ + e^- \rightarrow q + q + g$$



A perturbative calculations yields:

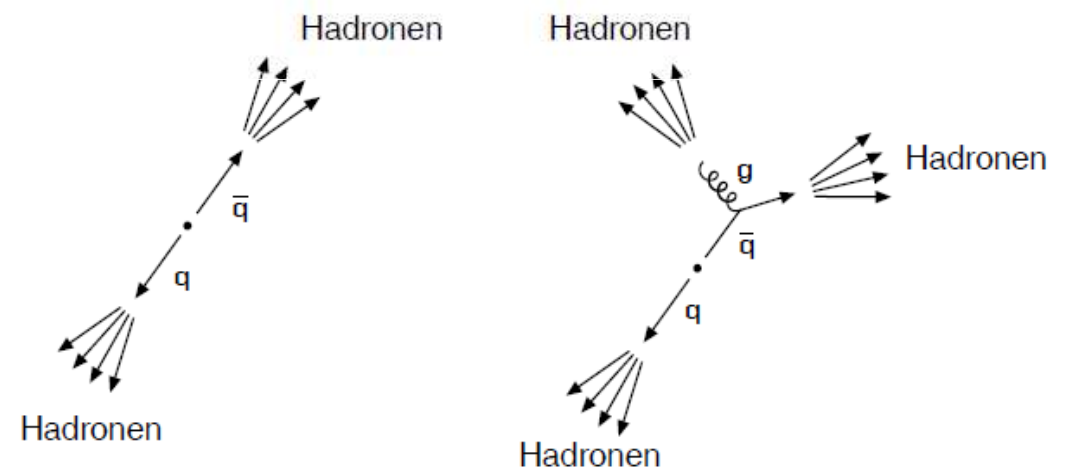
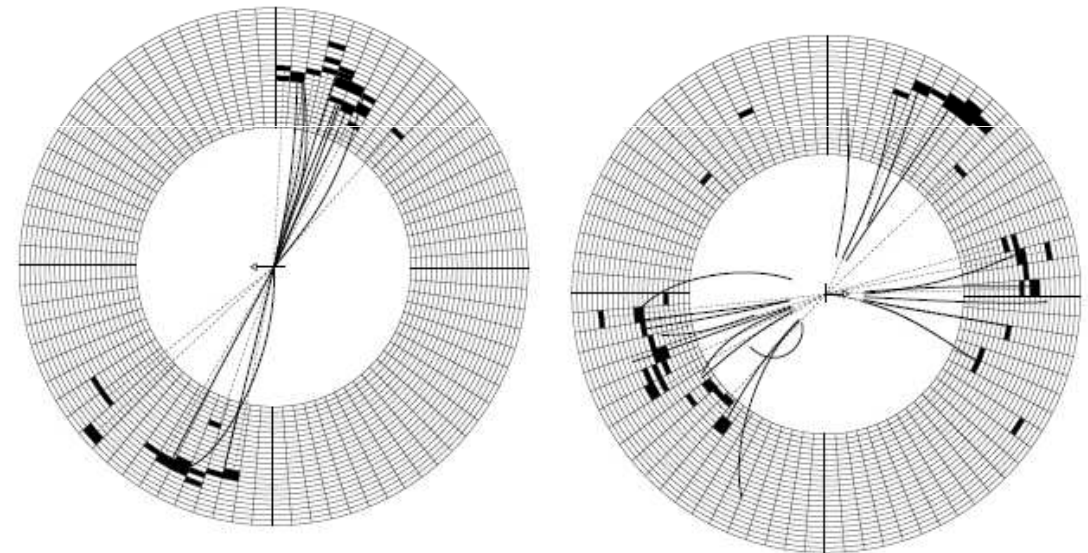
$$\sigma(e^- e^+ \rightarrow \text{Hadronen}) = \sigma_0 \left(1 + \frac{\alpha_S(s)}{\pi} \right)$$

Source: [berger]

Jets

After fragmentation of the quarks, the hadrons can be detected as jets.

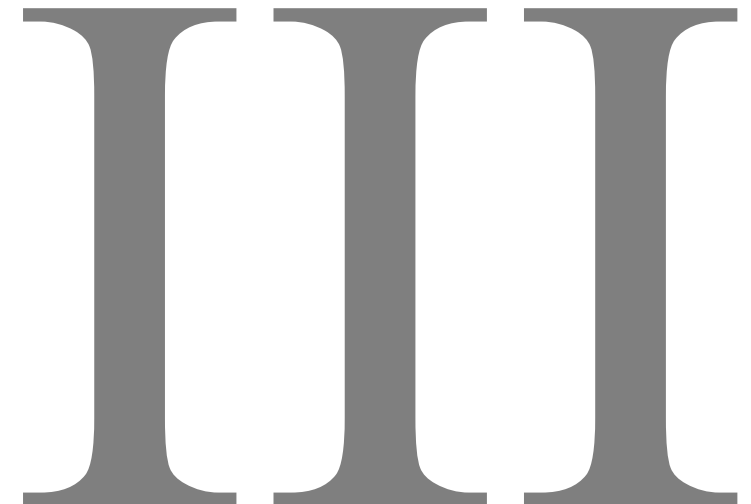
The ratio 2-jet/3-jet events allows the determination of the strong coupling α_s



Source: [povh]



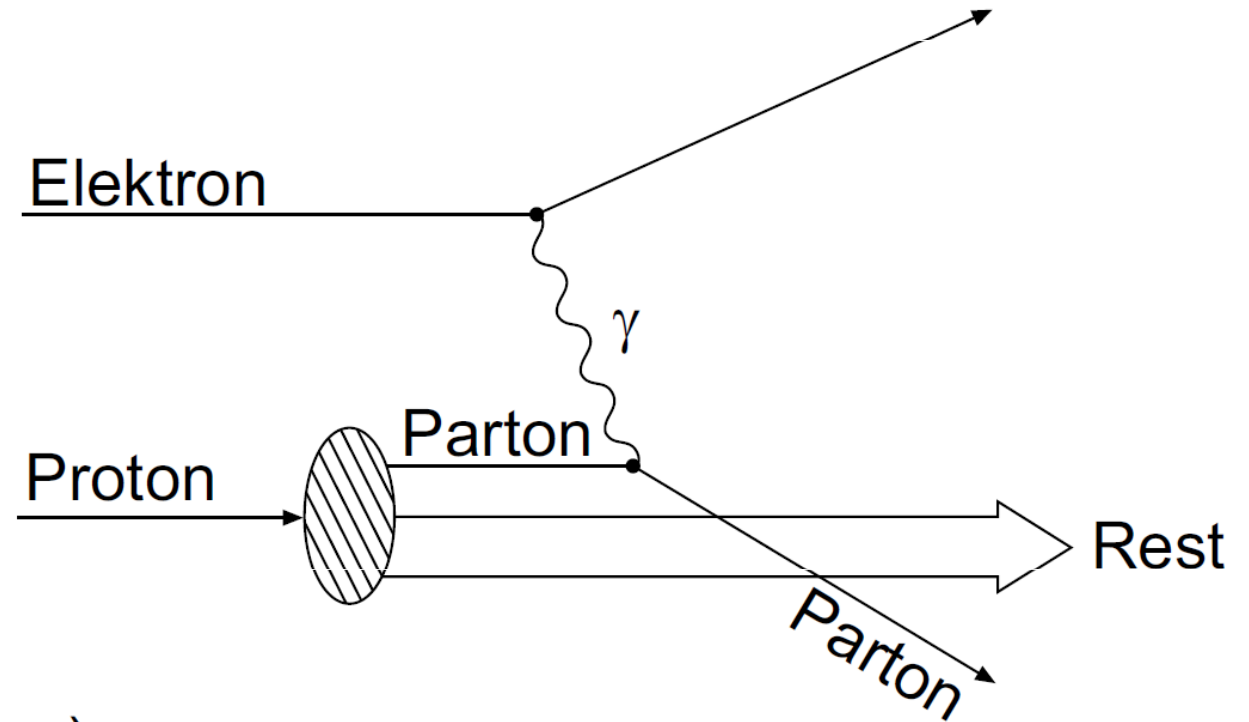
Hadronic structure and e^-p collisions



Parton modell

Parton model:

The proton consists of partons which are involved in the scattering process.



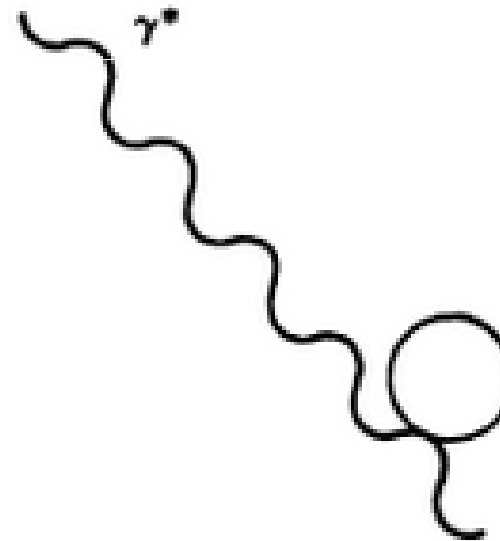
Source: [povh]

Deep inelastic scattering

inelastic scattering:
 $e + p \rightarrow e + X$

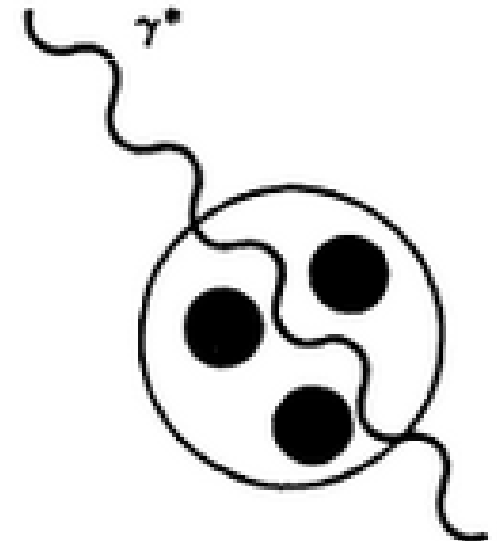
at higher (virtual) photon energies,
the proton sub-structure is revealed:

it contains three quarks.



(a) Low Q^2

$< 1 \text{ GeV}$



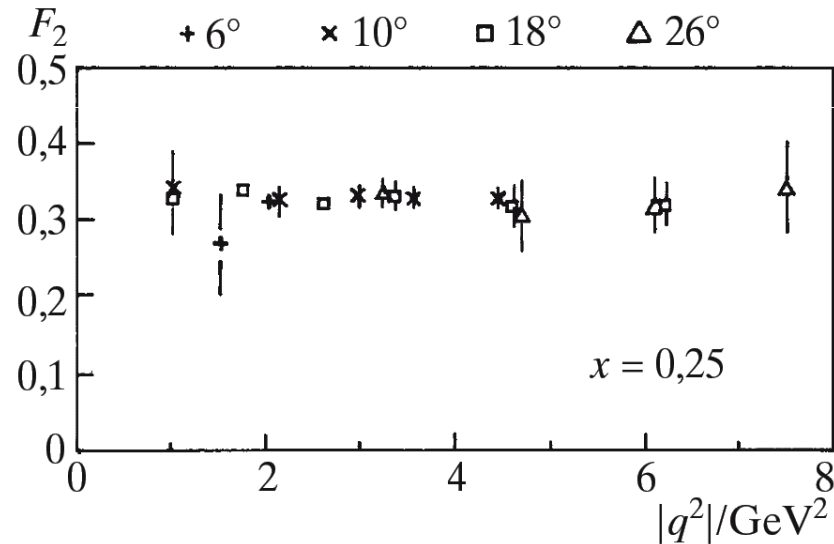
(b) Medium Q^2

$> 1 \text{ GeV}$

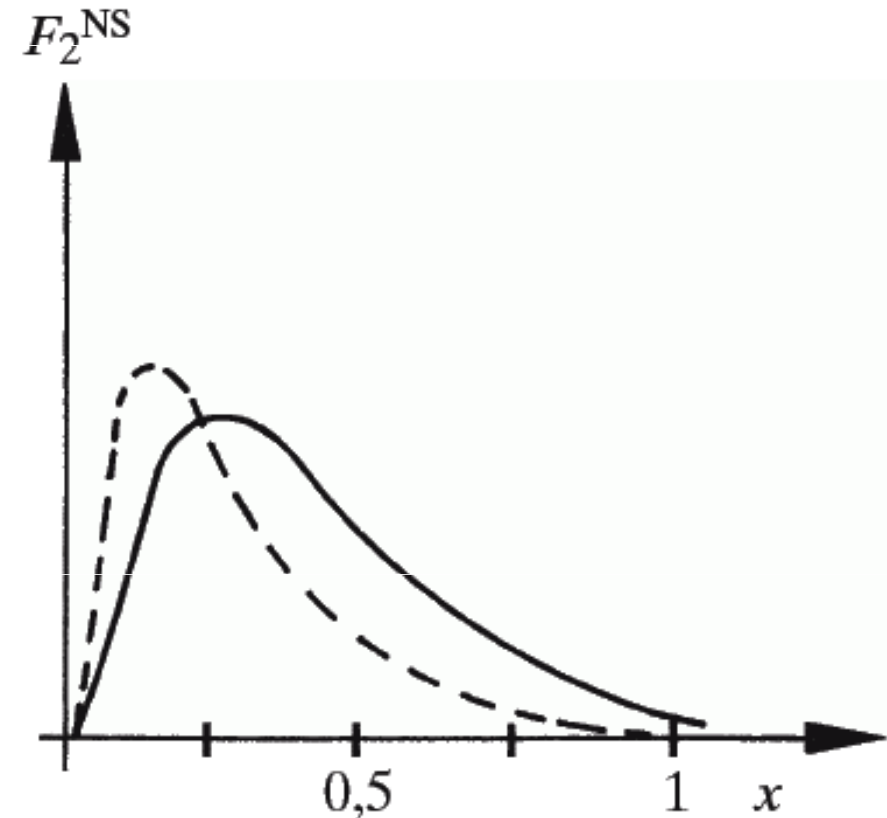
$1 \text{ GeV} \sim 1.24 \text{ fm}$

Source: [bethke]

Scaling and scaling violation



scaling of structure function...

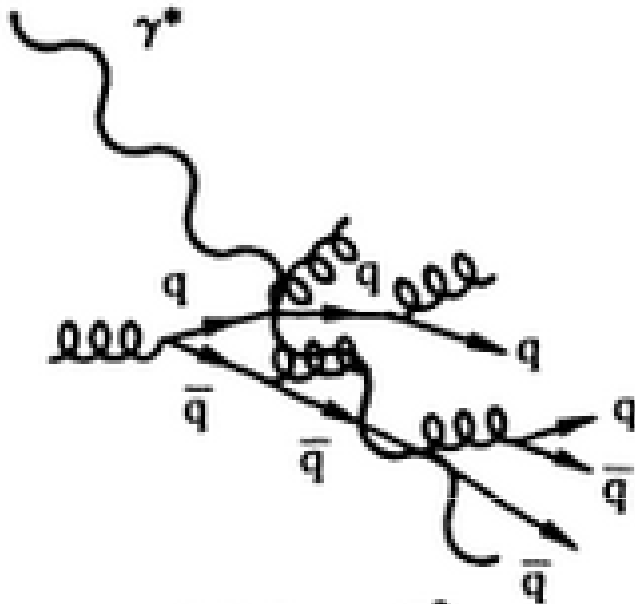


...and scaling violation

Source: [povh],[berger]

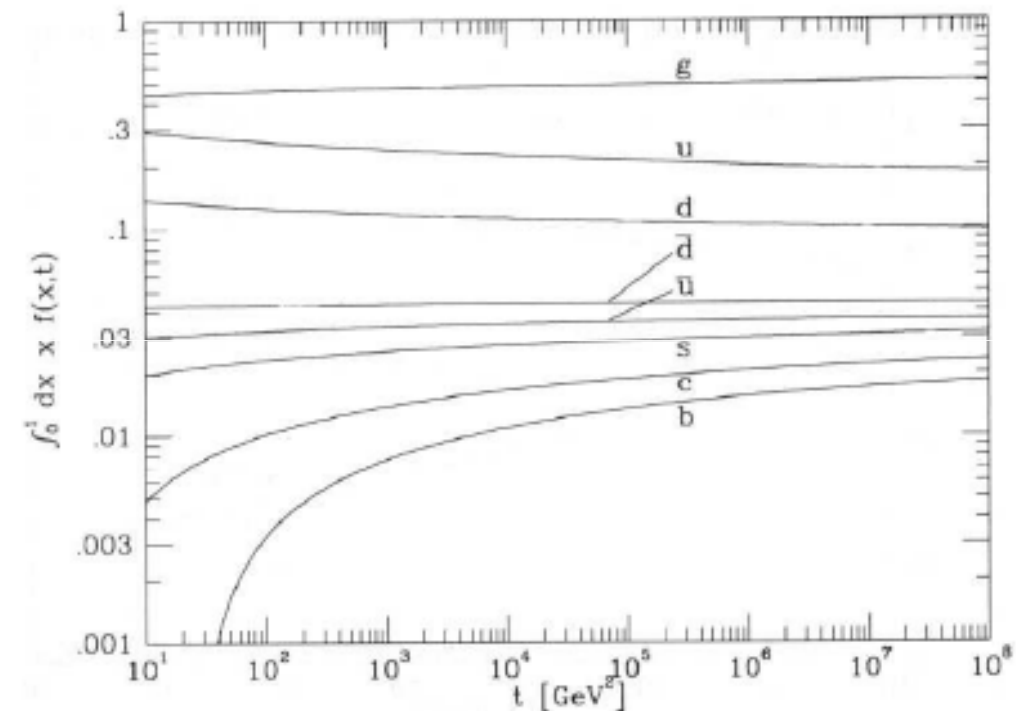
sea quarks and gluons

Sea quarks and gluons contribute to the proton structure function. They are revealed at higher scattering energies.



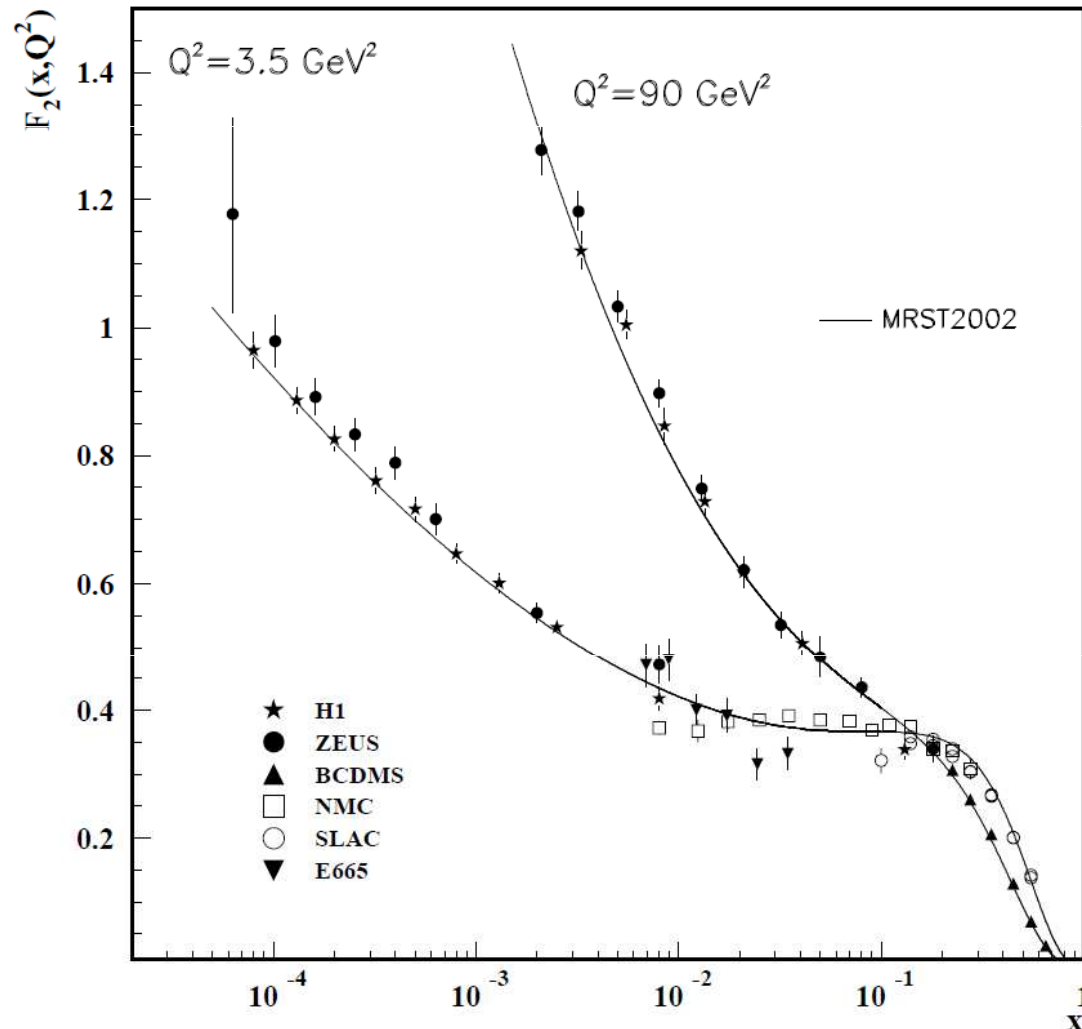
(c) Large Q^2

$\ll 1 \text{ GeV}$



Source: [bethke]

Structure function



The parton distribution function can be calculated via DGLAP-equations.

Source: [strucfunrpp]

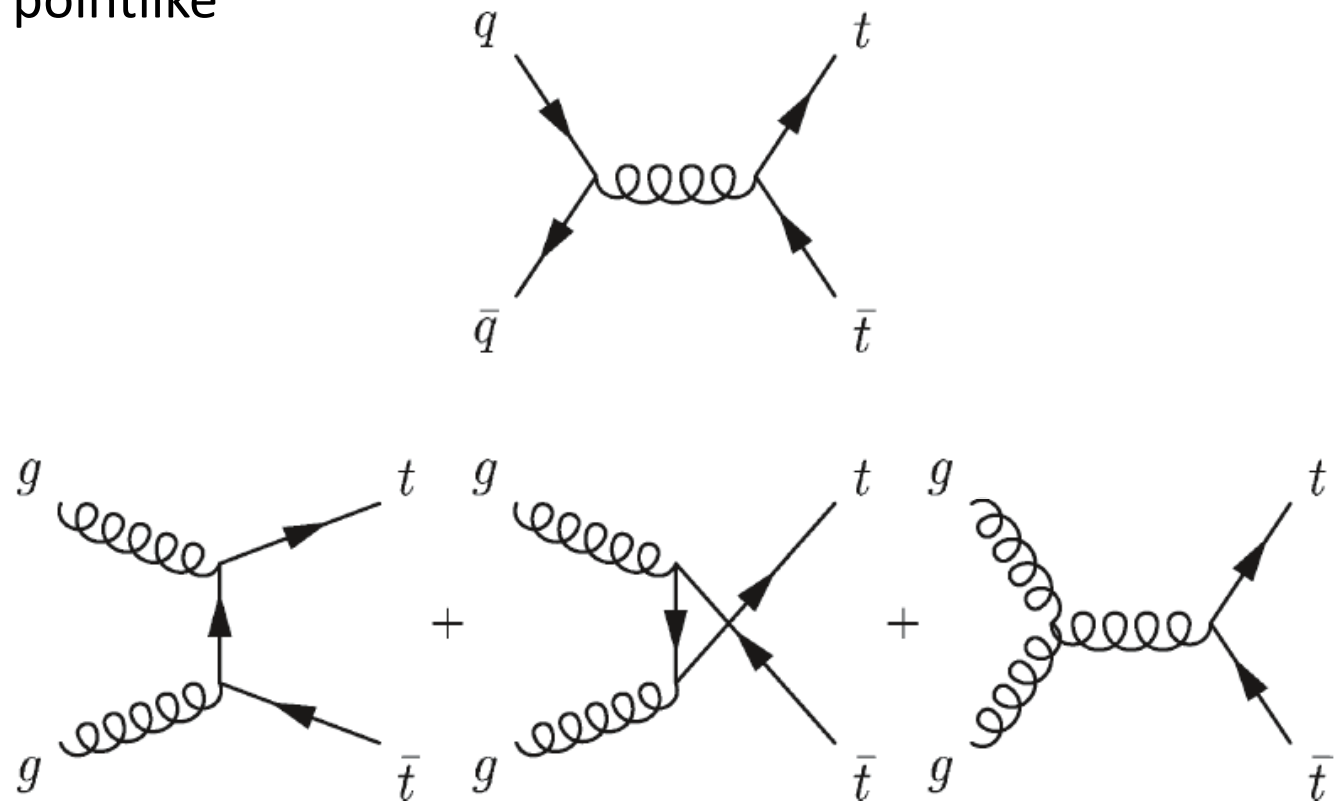


Advanced experiments: pp collisions

IV

proton-proton collisions

hard process: scattering of pointlike proton constituents.

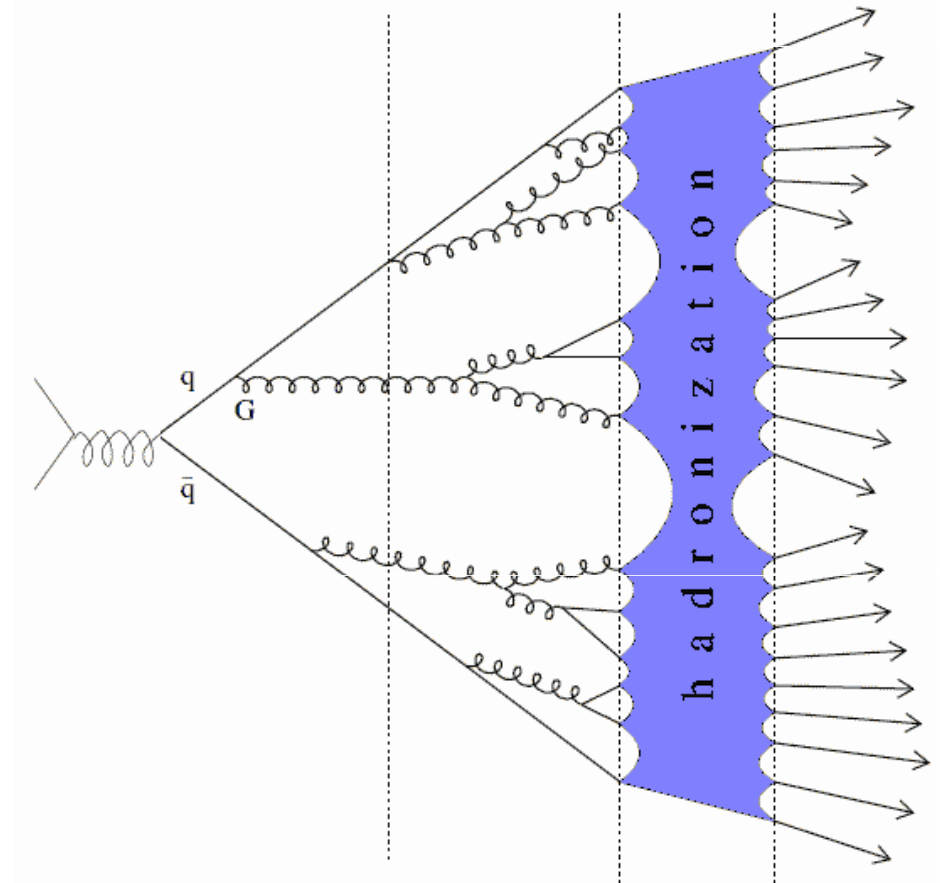


Source: [beck]

Hard and soft processes

hard process: the proton structure does not change in the time of the scattering process. It can be calculated perturbative.

soft process: in the soft reaction, the quarks fragmentize and form hadrons. This takes place in an infinite time frame.



Source: [bethke]

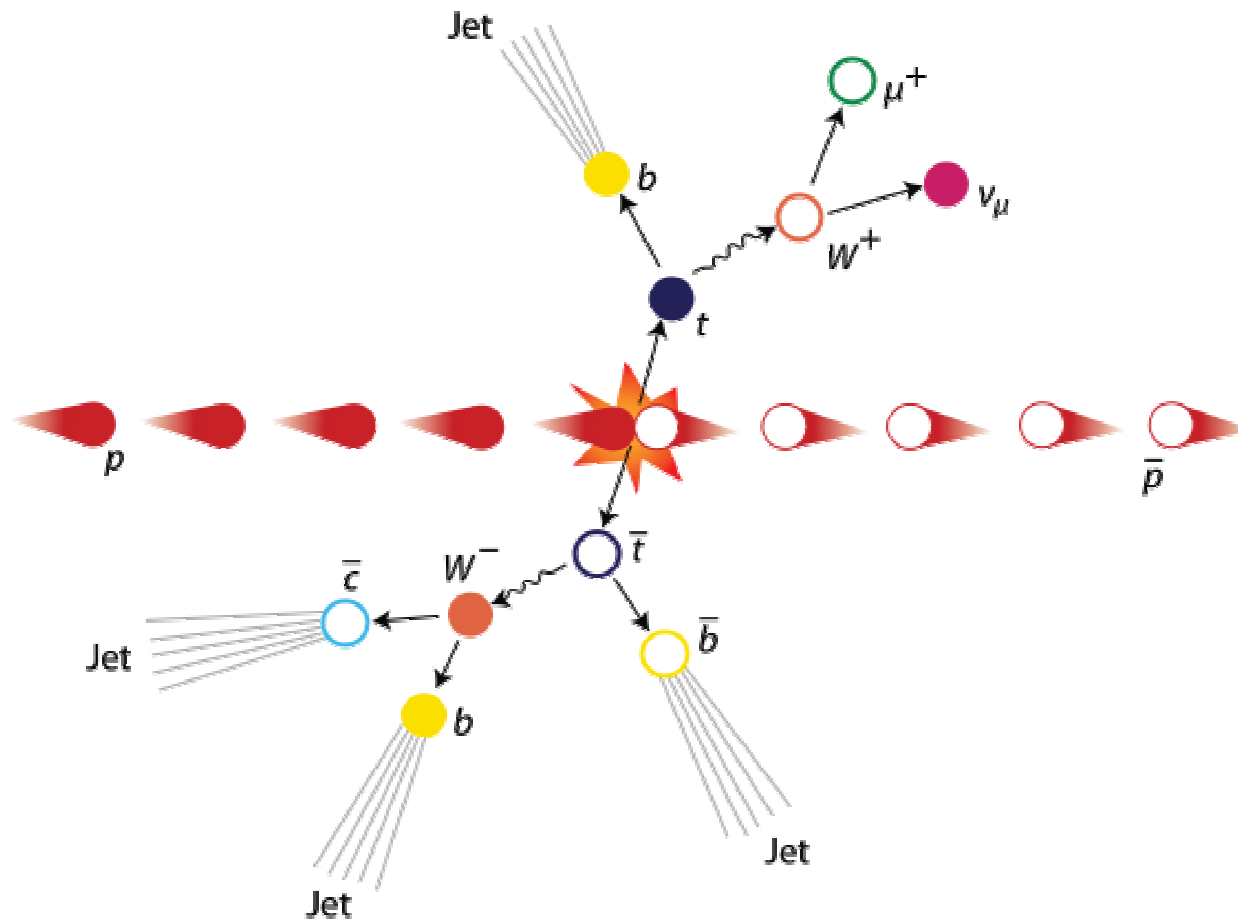
Factorization describes the total scattering cross section, which links the parton densities and the cross section of the hard process.

$$\sigma(H_1 + H_2 \rightarrow Q\bar{Q} + X) = \sum_{ij} \int dx_1 f_i^{H_1}(x_1, \mu) \int dx_2 f_j^{H_2}(x_2, \mu) \hat{\sigma}(ij \rightarrow Q\bar{Q} + X)$$

The independence of these elements are a great simplification of the model.

Event detection

Detectable are the particle jets which emerge from the hard scattering process.



Source: wikipedia: top antitop quark event, www-cdf.fnal.gov

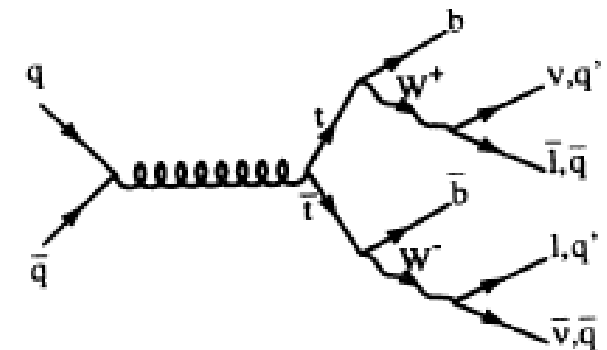
top-quark detection

TABLE I. Decay modes for a $t\bar{t}$ pair and their approximate branching ratios (to lowest order) assuming charged-current decays. The symbol q stands for a light quark: u, d, c, s .

Decay mode	Branching ratio
$t\bar{t} \rightarrow (q\bar{q}'b)(q\bar{q}'\bar{b})$	36/81
$t\bar{t} \rightarrow (q\bar{q}'b)(e\nu\bar{b})$	12/81
$t\bar{t} \rightarrow (q\bar{q}'b)(\mu\nu\bar{b})$	12/81
$t\bar{t} \rightarrow (q\bar{q}'b)(\tau\nu\bar{b})$	12/81
$t\bar{t} \rightarrow (e\nu b)(\mu\nu\bar{b})$	2/81
$t\bar{t} \rightarrow (e\nu b)(\tau\nu\bar{b})$	2/81
$t\bar{t} \rightarrow (\mu\nu b)(\tau\nu\bar{b})$	2/81
$t\bar{t} \rightarrow (e\nu b)(e\nu\bar{b})$	1/81
$t\bar{t} \rightarrow (\mu\nu b)(\mu\nu\bar{b})$	1/81
$t\bar{t} \rightarrow (\tau\nu b)(\tau\nu\bar{b})$	1/81

The top quark decays in bottom quarks before hadronization because of their big mass. A significant signal is a six-jet-event.

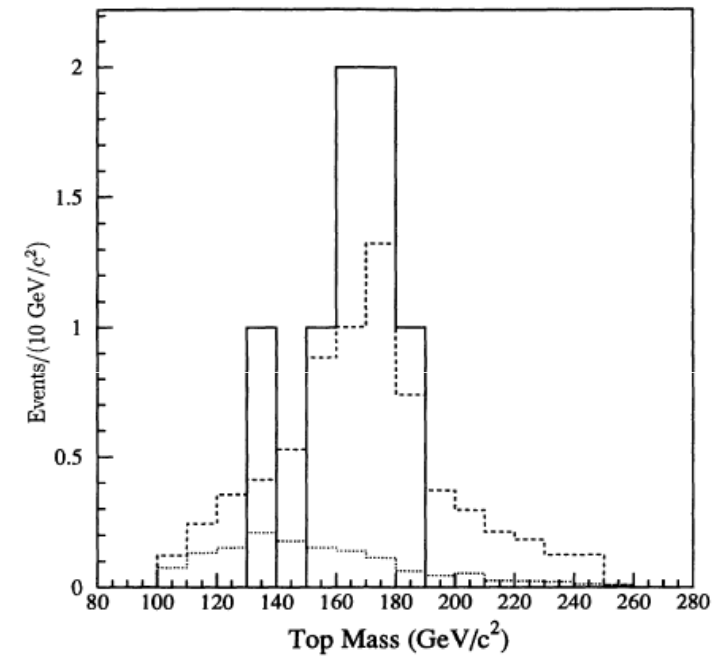
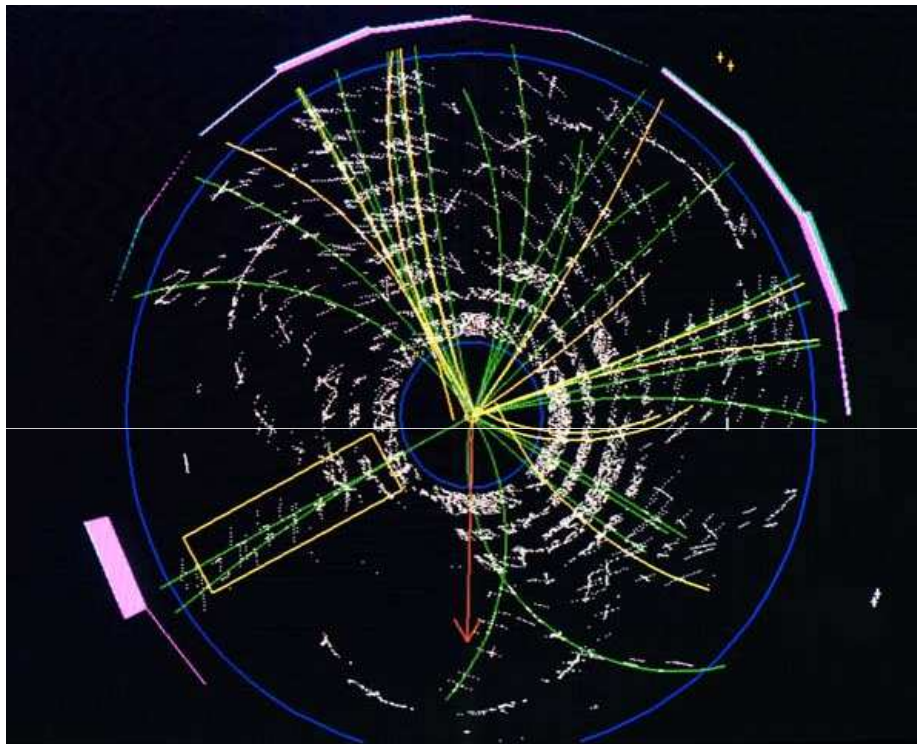
The decay channels can be reconstructed and their cross sections and branching ratios be determined.



Source: [abe],[beck]

top-quark detection

The invariant mass of different decay modes can be combined to the top-quark resonance



Source: www-cdf.fnal.gov, [abe]

Summary

Depending on the c.m. energy, all quarks can be produced in e^+e^- collisions. This is easy in theory because of the point-like leptons, but it is difficult to reach sufficient energies.

pp-collisions have higher energies, but the proton sub-structure causes difficulties when extracting reaction cross sections.

This can be avoided because the hard process in which the quarks are produced occurs to be on a much smaller length and time scale than the soft hadronization (fragmentation) process – the soft and the hard process factorize. The other partons do not participate in the process as well.

Acknowledgment



TECHNISCHE
UNIVERSITÄT
DARMSTADT

I. Introduction | II. e^+e^- collisions | III. hadronic structure | **IV. pp collisions**

Thank you for your attention.

Also, thanks a lot to Professor Friman for the mentoring and support!

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Teilchen und Kerne

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